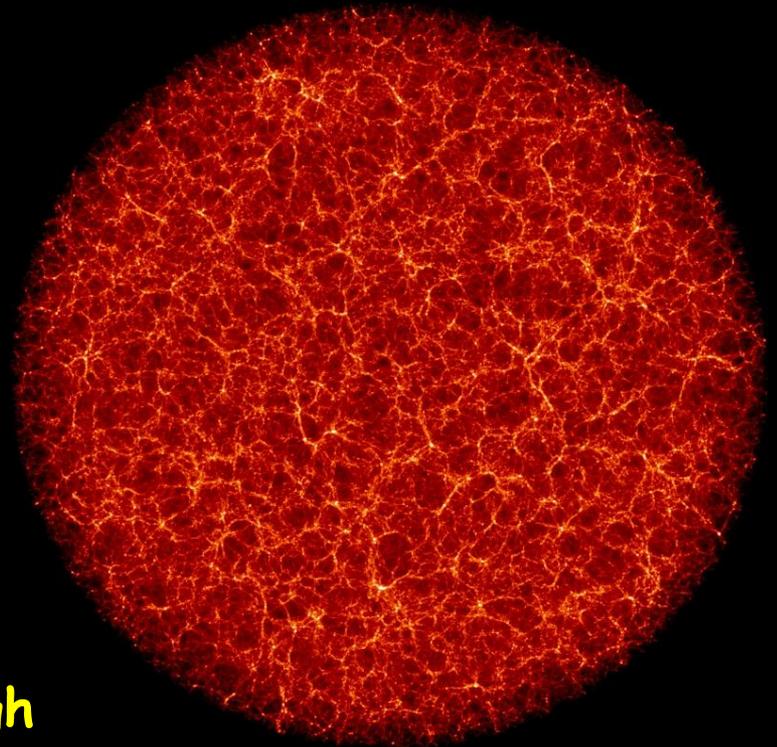
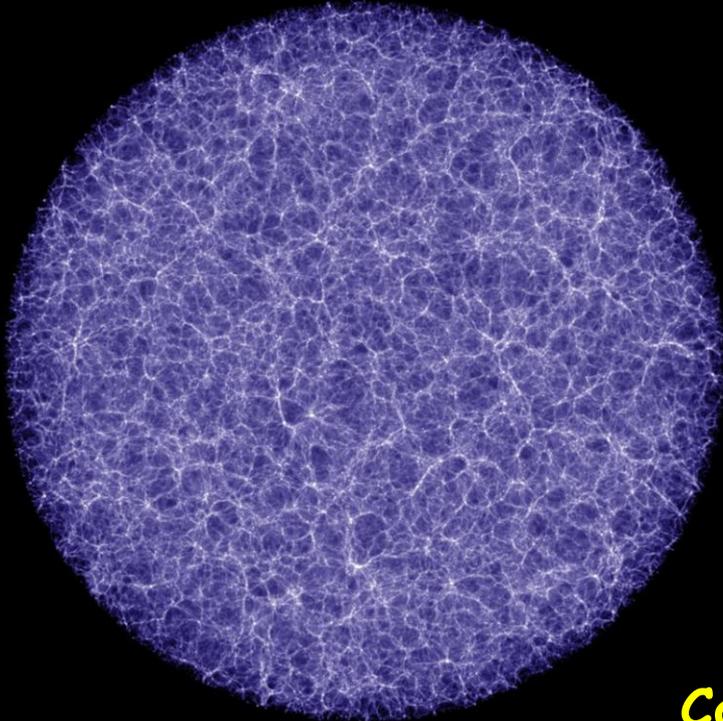


# Simulating quintessence cosmologies: growth of structure and redshift space distortions



**Carlton Baugh**  
**Institute for Computational Cosmology**  
**Durham University**

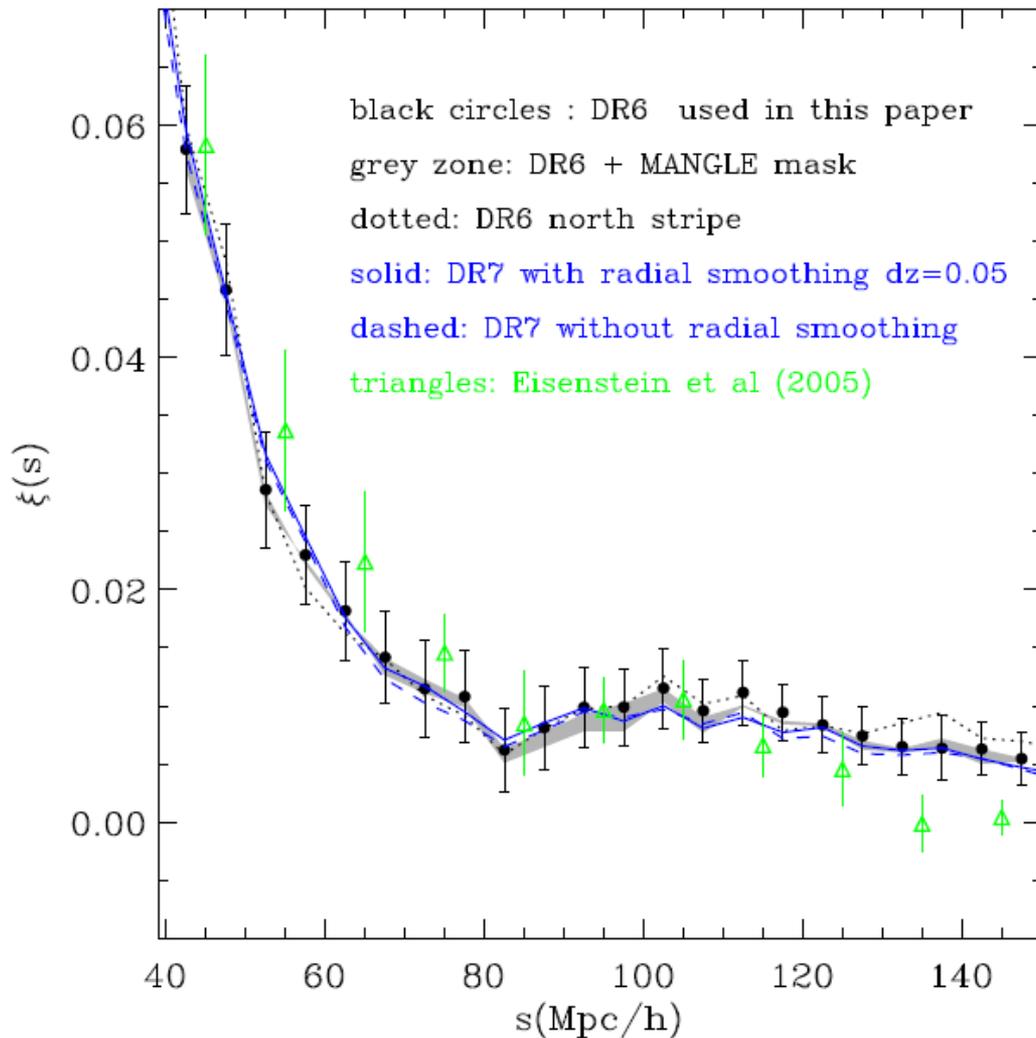
# Outline: two main topics

- Quintessence N-body simulations  
[Jennings et al. 2010 MNRAS, 401, 2181](#)
- Redshift-space distortions  
[Jennings et al. 2010, arXiv:1003.4282 in press](#)

Collaborators:

Elise Jennings, Silvia Pascoli, Raul Angulo (MPA)

# The BAO signal in galaxy clustering



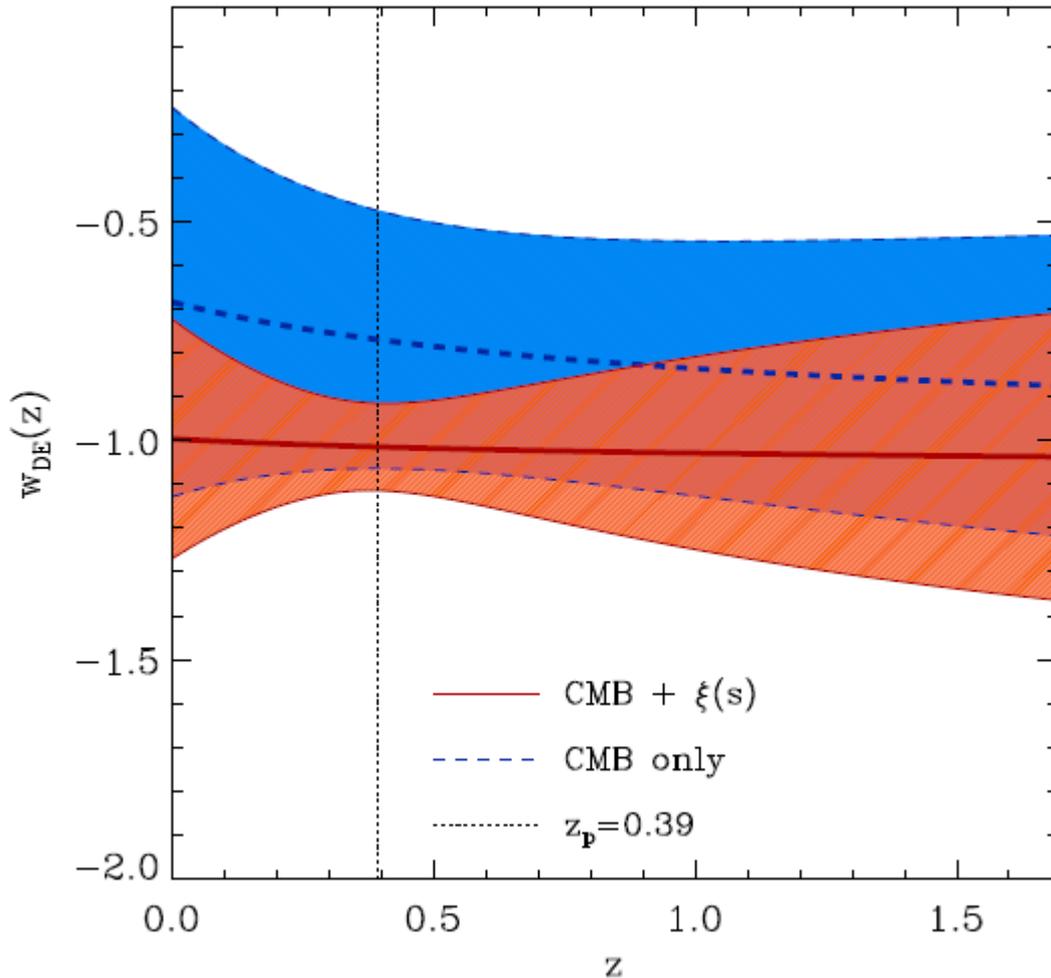
SDSS Luminous Red  
Galaxy

Cabre & Gaztanaga 2009  
Gaztanaga et al 2009

Sanchez et al. 2009

# Evolution in the DE eqn of state?

EFFECTIVE EQUATION OF STATE



Equation of state parameter:

$$w = \frac{P}{\rho}$$

Cosmological constant:

$$w = -1$$

REDSHIFT

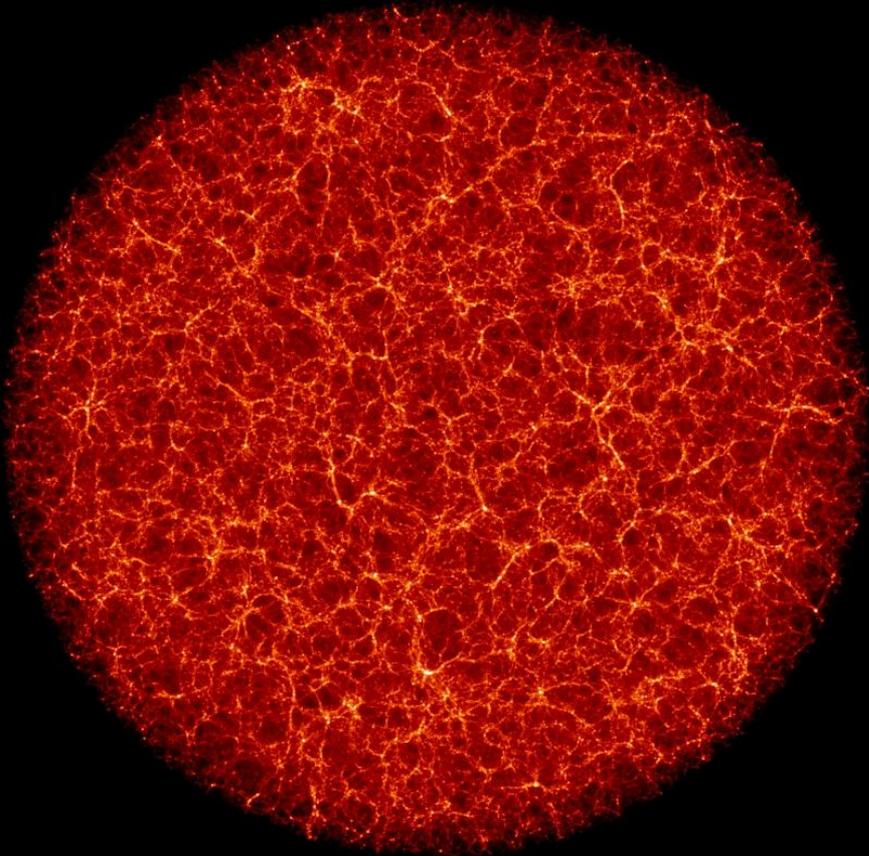
Sanchez et al. 2009

# Modelling the Gigaparsec Universe

- Why do we need simulations?
- Modelling quintessence dark energy
- Redshift space distortions

# Why do we need simulations?

- Dark energy/modified gravity tests use LSS
- Isn't linear perturbation theory good enough?
- Need high precision measurements as models give similar predictions
- Need high precision theory too!



# Baryonic Acoustic Simulations at the ICC BASICC

$L = 1340/h \text{ Mpc}$   $V = 2.4/h^3 \text{ Gpc}^3$

(20 x Millennium volume)

$N = 1448^3$  (>3 billion particles)

Can resolve galactic haloes

130,000 hours CPU on Cosmology Machine

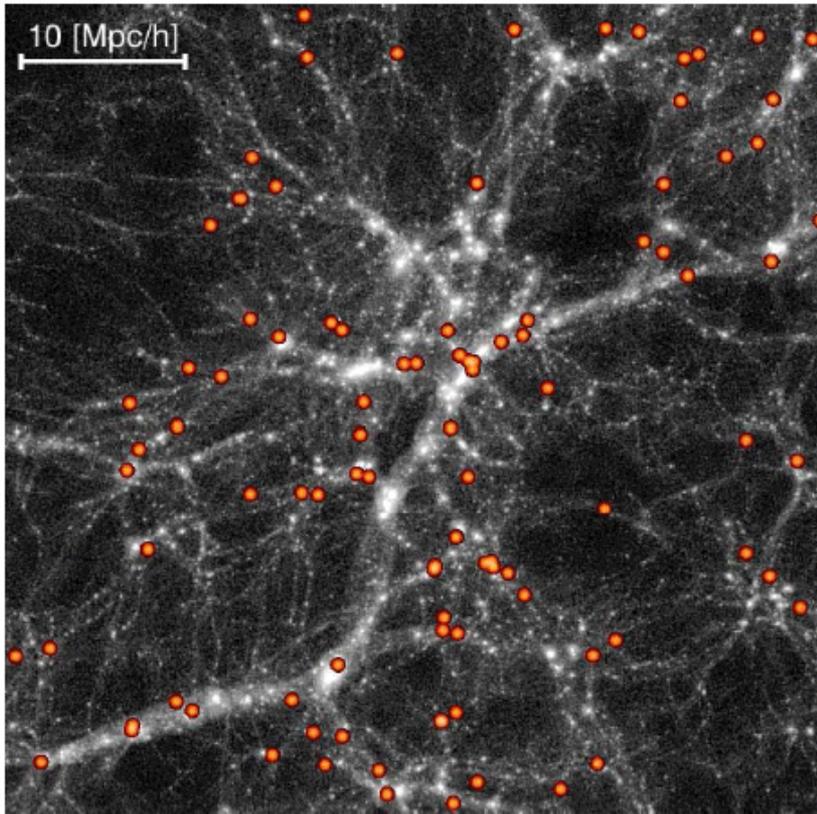
Combine with semi-analytical galaxy formation model GALFORM

50 low-res BASICC runs for errors  
(= 1000 Millenniums!)

Angulo et al. 2008

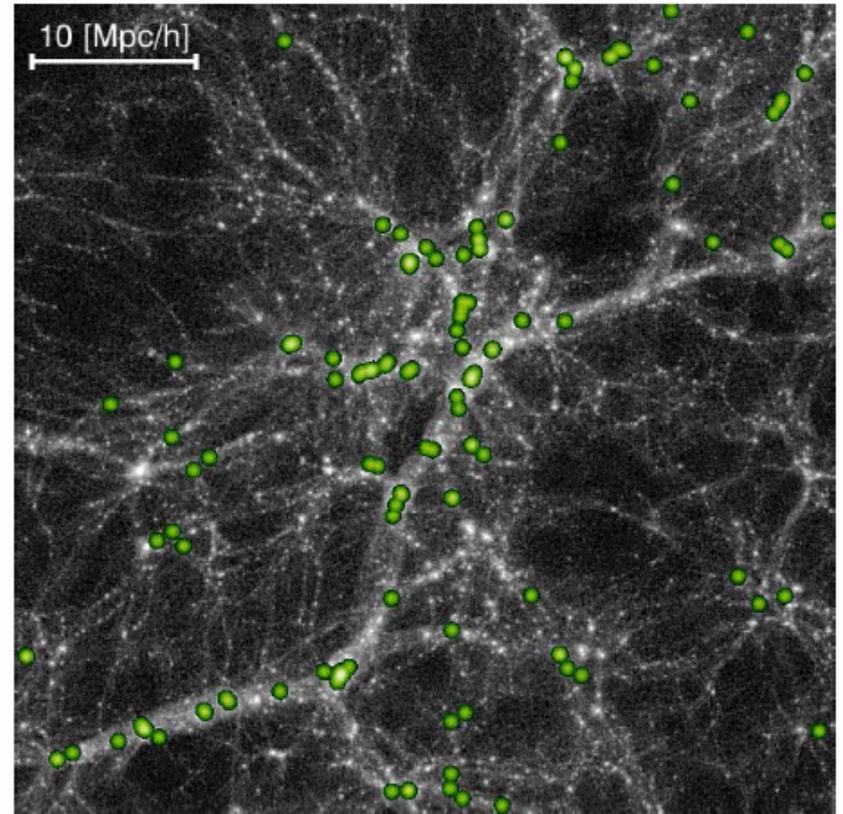


# Combine with galaxy formation model



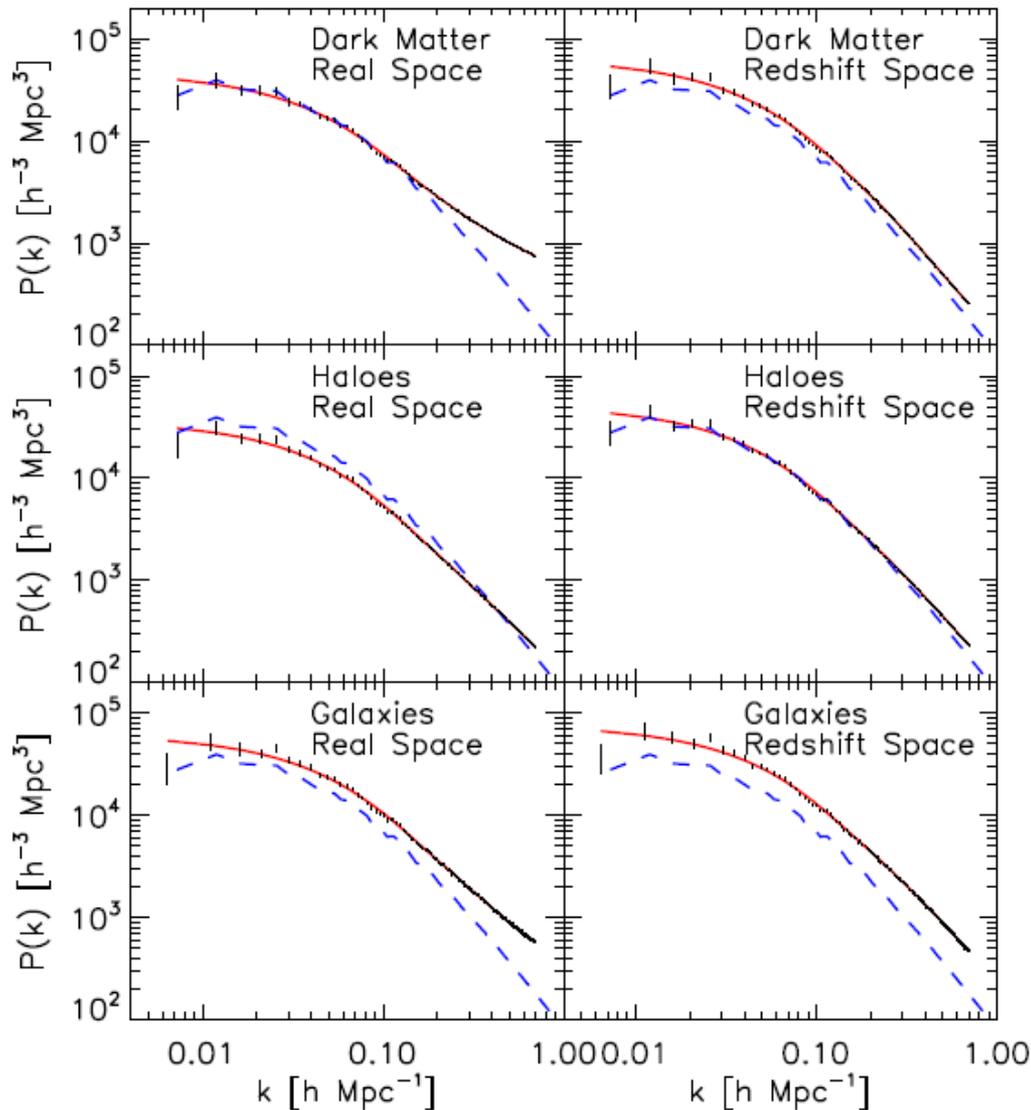
H-alpha emitters

$z=1$



H-band selection

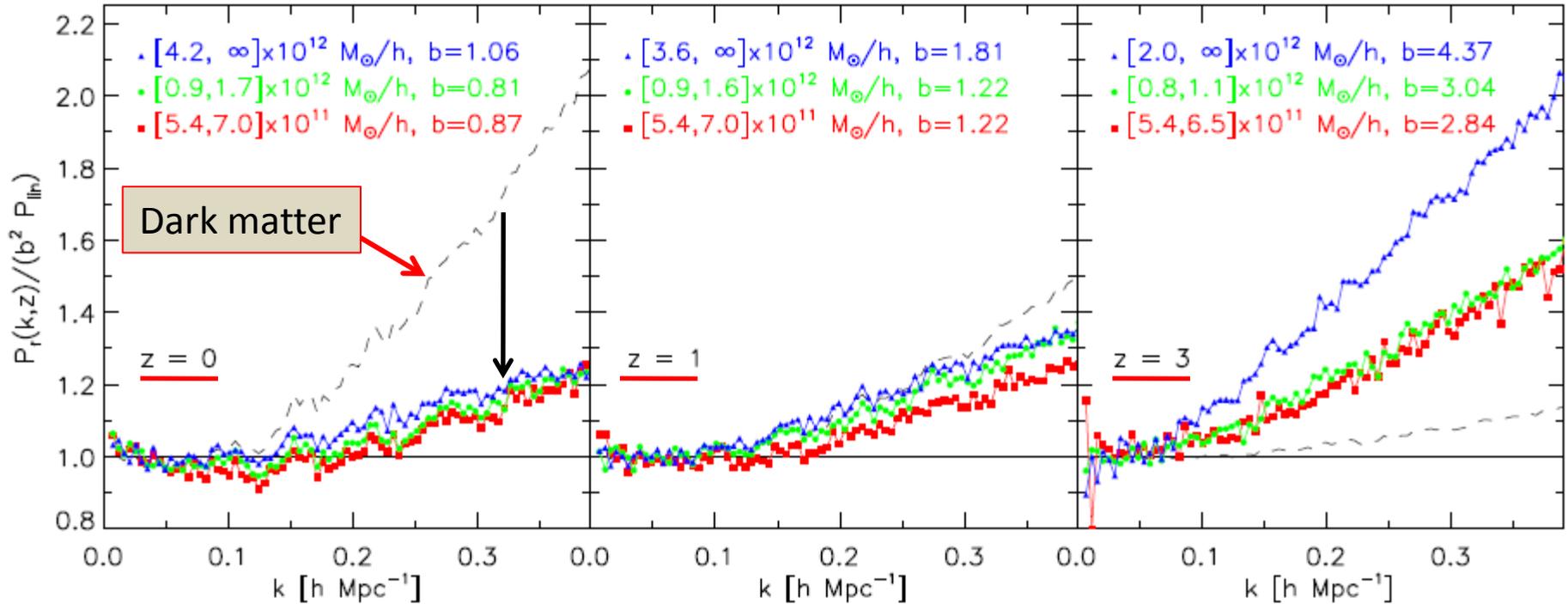
# So, is linear theory good enough?



No! Because of .....

- Nonlinear growth of fluctuations
- Redshift space distortions
- Scale dependent halo and galaxy bias

# Scale dependent bias



Remove asymptotic bias: Scale dependent halo bias

# Quintessence Dark Energy

- Alternative to cosmological constant
- Solves fine tuning and coincidence problems
- Dynamical scalar field

Scalar Fields in Cosmology

$$H^2 = \frac{8\pi G}{3} \left[ \rho_m + \rho_r + \frac{\dot{\phi}^2}{2} + V(\phi) \right]$$

Dark Energy equation of state:

$$w(\phi) = \frac{P_\phi}{\rho_\phi} = \frac{\dot{\phi}^2 / 2 - V(\phi)}{\dot{\phi}^2 / 2 + V(\phi)}$$

Lots of choice for potential  $V$  !

- **Inverse (INV)** (Zlatev et al. 1999)

$$V(\phi) \sim M^{(4+\alpha)} \phi^{-\alpha}$$

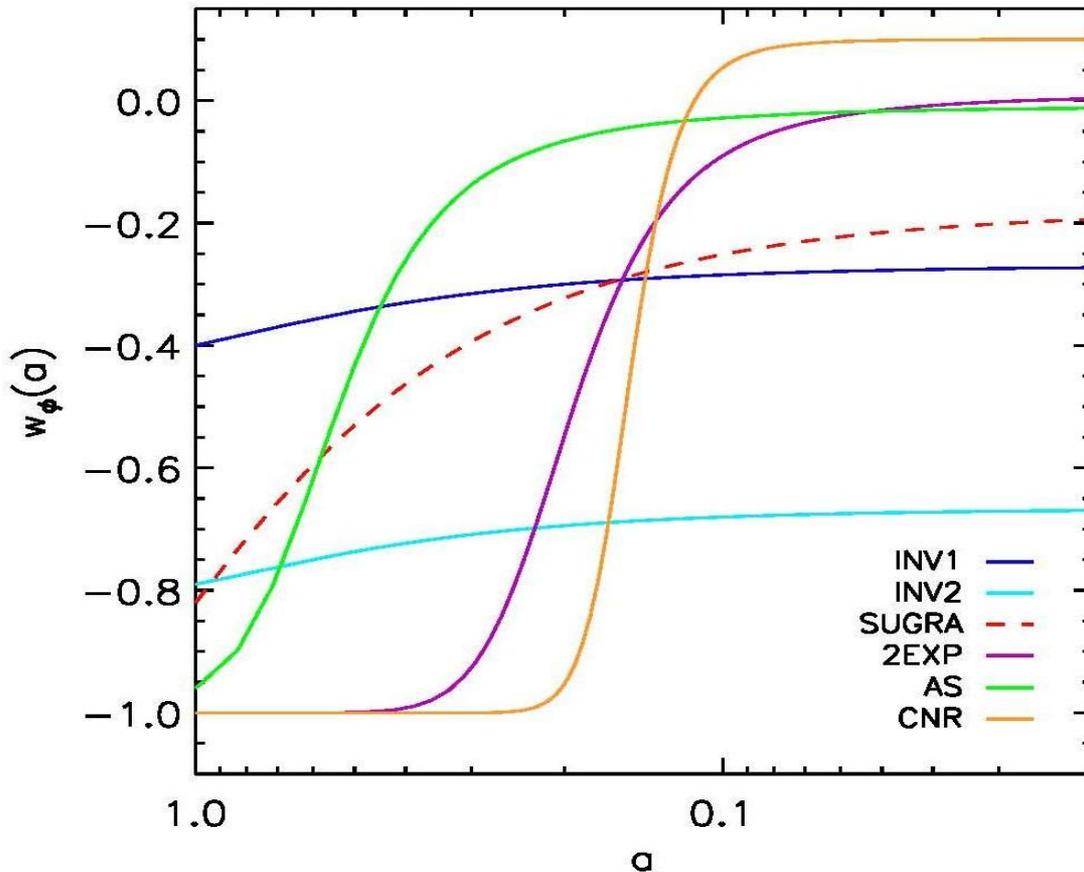
- **Albrecht-Skordis (AS)**

$$V(\phi) \sim V_p(\phi) e^{-\lambda\phi} \quad V_p(\phi) = (\phi - B)^\alpha + A$$

- **SUGRA** (Brax & Martin 1999)

$$V(\phi) \sim 1/\phi^\alpha e^{\phi^2/2}$$

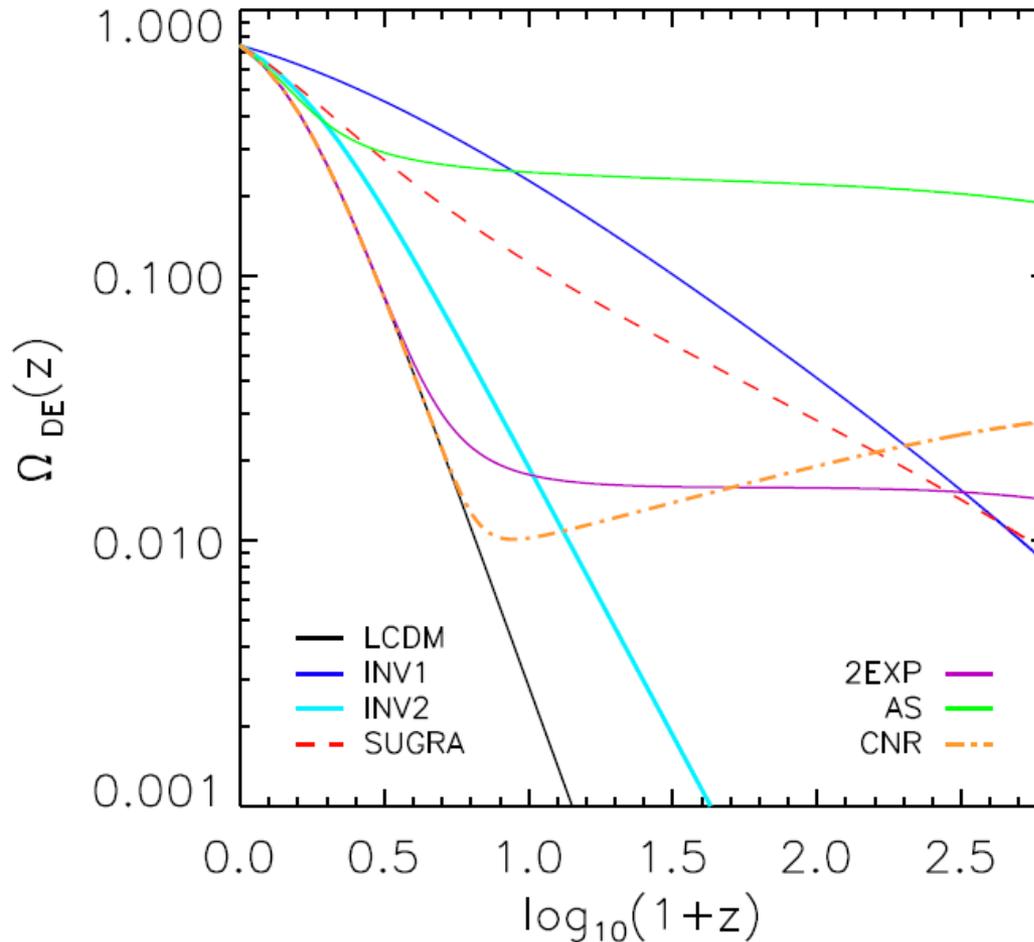
# How can we describe this range of models?



- Rich variety of  $w(z)$
- Need to describe this accurately to  $z > 100$  in an N-body simulation
- Two parameter models out by 10% already at  $z=1$
- Use 4 parameter model Corasaniti & Copeland
- Accurate to  $< 5\%$  to  $z=1000$

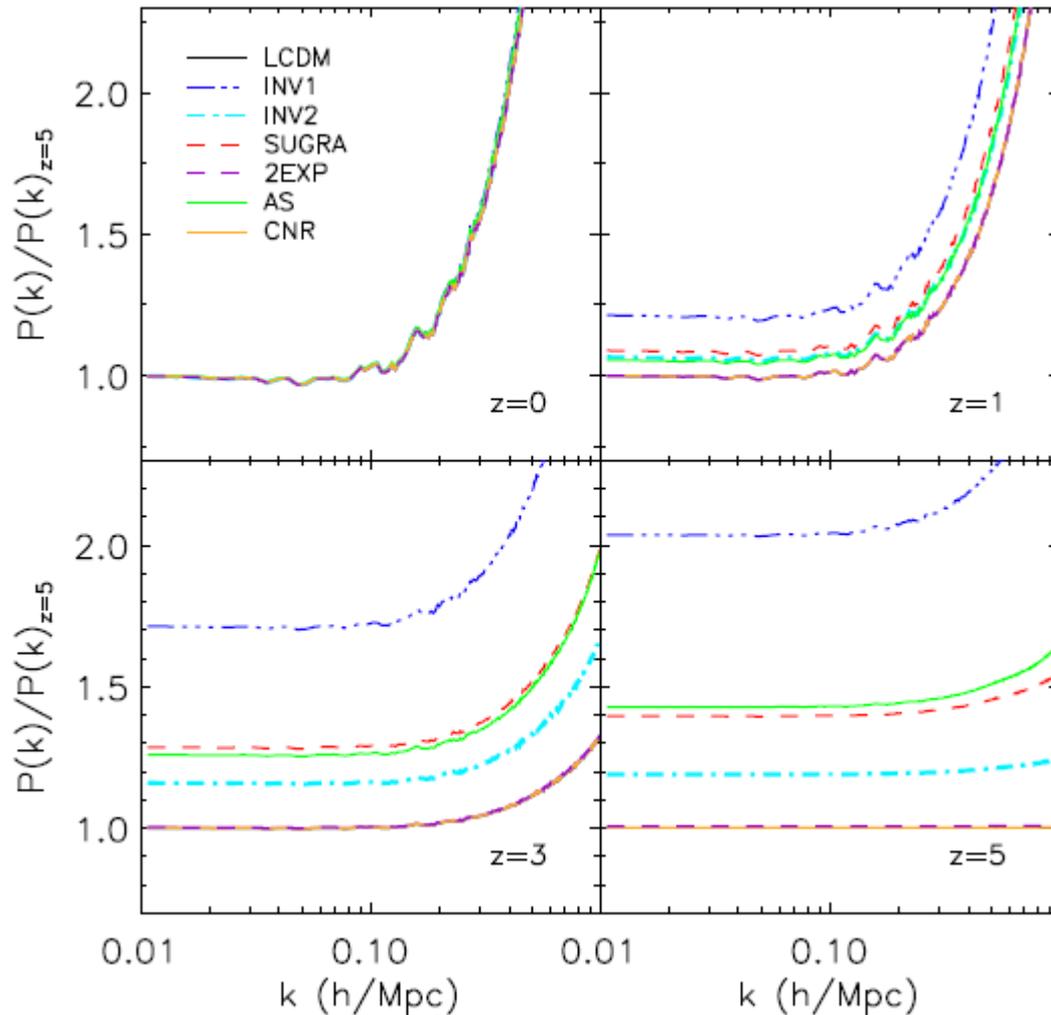
# Simulating quintessence DE

Dark energy density parameter



- Models have different expansion histories to LCDM
- Structure grows at different rates

# Stage I: The growth of structure



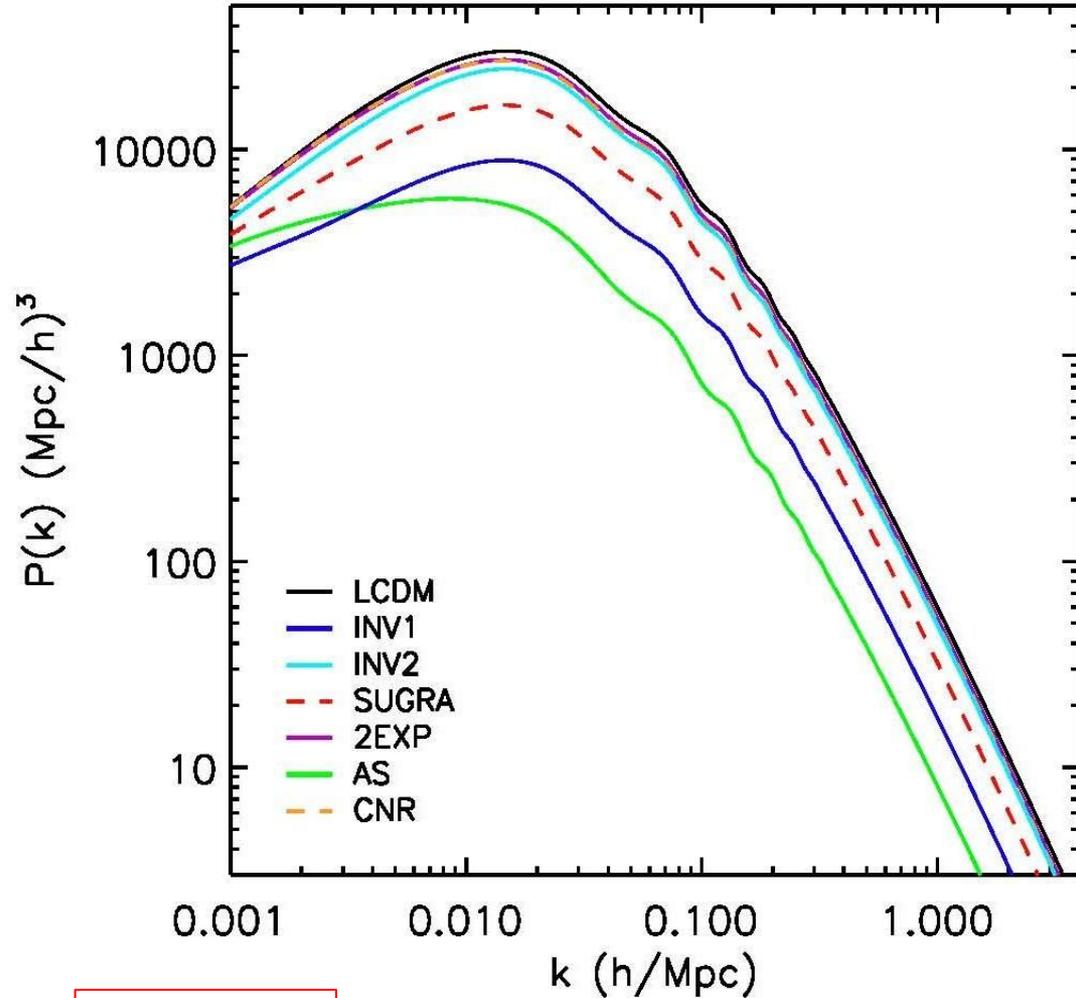
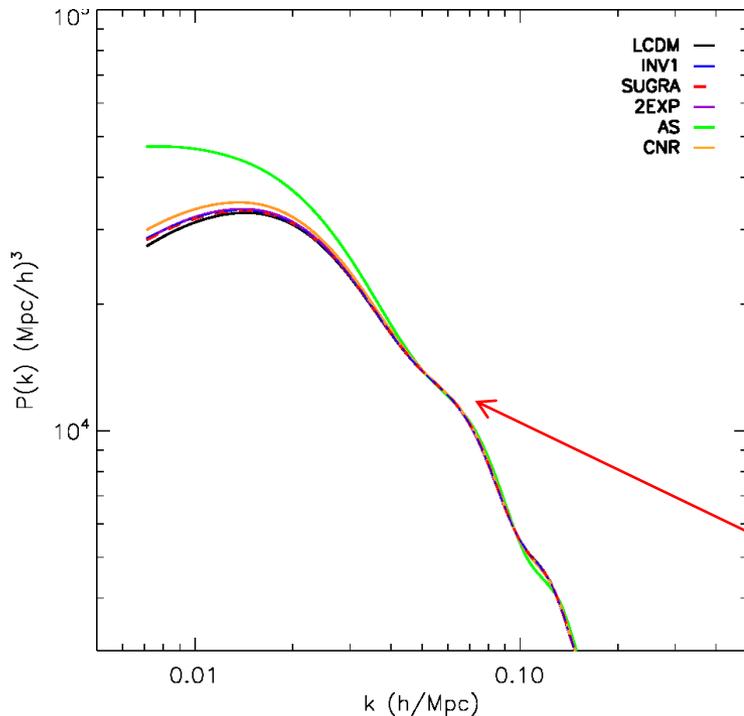
- LCDM input  $P(K)$
- Change expansion history using  $w(z)$

# Stage II : Quintessence and linear theory power

Growth of  $\delta_m$  during matter dominated era

- Negligible dark energy  $\delta_m \propto a$
- With appreciable dark energy:

$$\delta_m \propto a^{[\sqrt{25-24\Omega_{DE}}-1]/4}$$



Normalise to  $\sigma_8=0.8$

Jennings et al 2010

# Stage III : Consistency with observational data

## Cosmological distance priors

'Acoustic Scale'

$$l_A(z_*) = (1 + z_*) \pi \frac{D_A(z_*)}{r_s(z_*)}$$

'Shift parameter'

(Bond et al. 1997)

$$R_{conc}(z_*) = \frac{\sqrt{\Omega_m H_0^2}}{c} (1 + z_*) D_A(z_*)$$

Redshift at decoupling

(Hu & Sugiyama 1996)

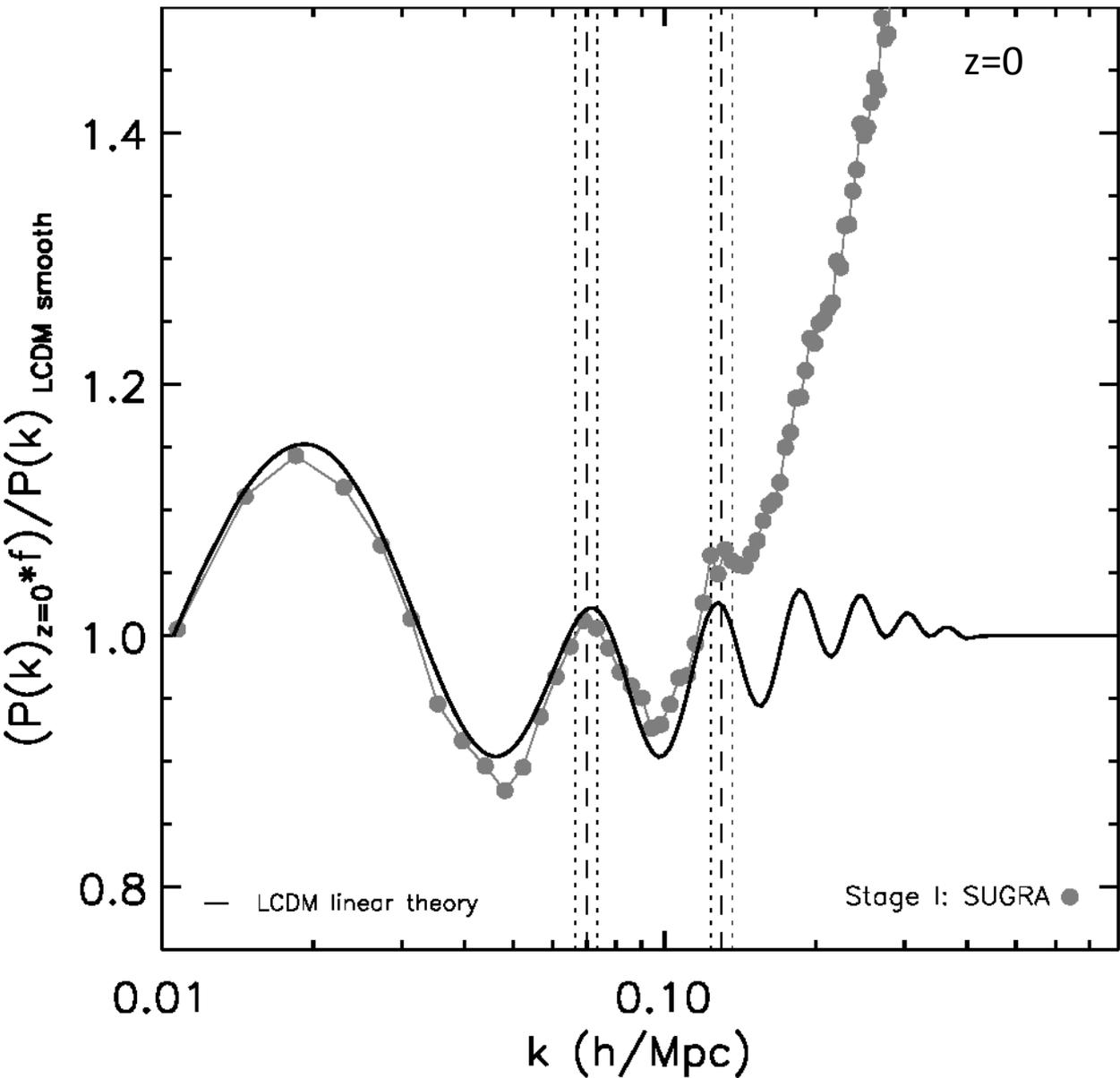
$$z_* = z_*(\Omega_m h^2, \Omega_B h^2)$$

	$z_*$	$l_A(z_*)$	$R(z_*)$
WMAP 5-yr ML	$1090.51 \pm 0.95$	$302.10 \pm 0.86$	$1.710 \pm 0.019$

Fit to the distance priors for each quintessence model using  $\Lambda$ CDM parameters

	$\chi_{total}^2/\nu$
INV1	15.34
INV2	1.81
SUGRA	3.88
2EXP	1.09
AS	2.04
CNR	1.37

# Baryon acoustic oscillations

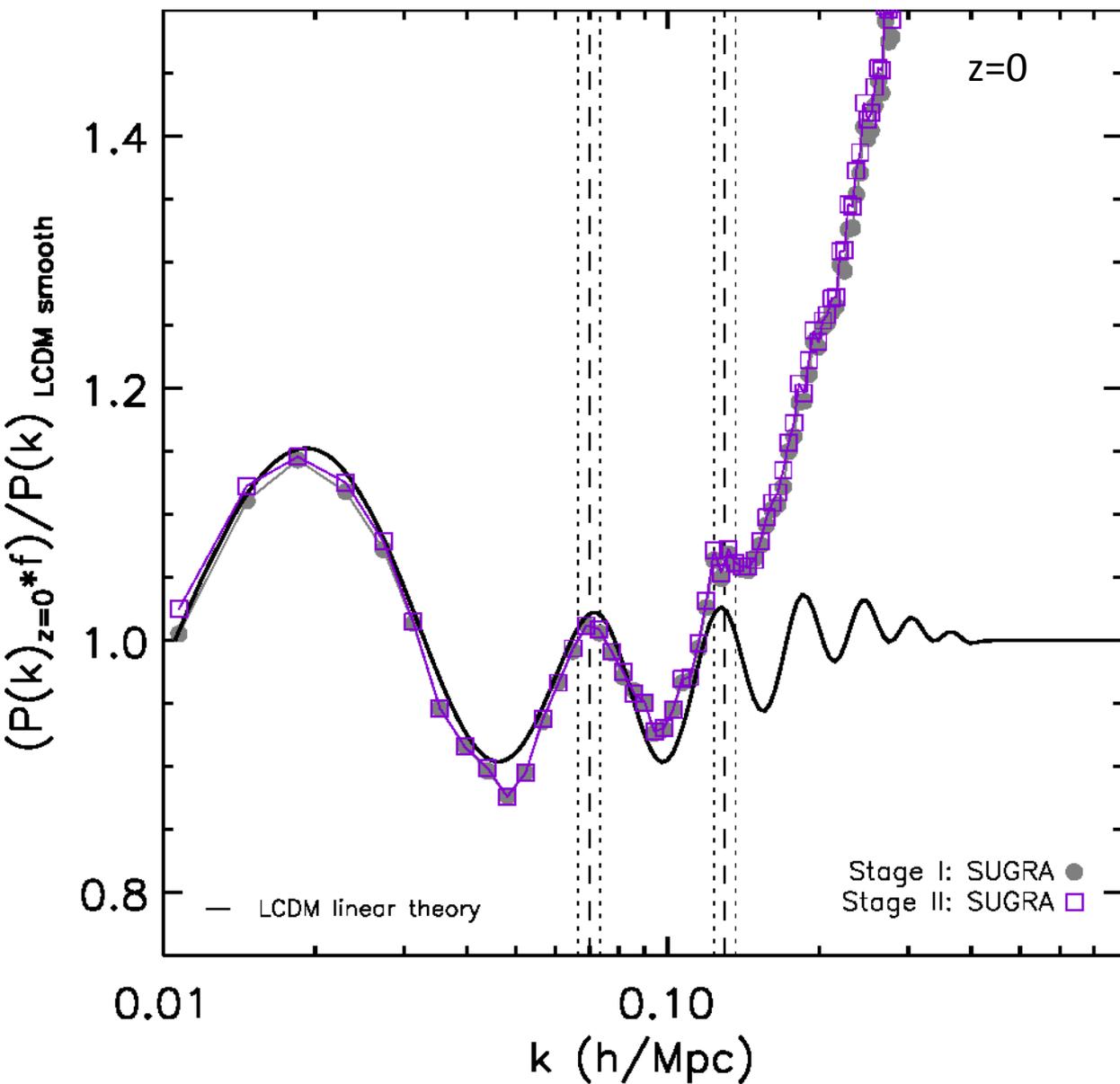


SUGRA

Stage I : SUGRA linear growth factor

Multiplicative factor  $f$  corrects the scatter of the measured power from the expected linear theory

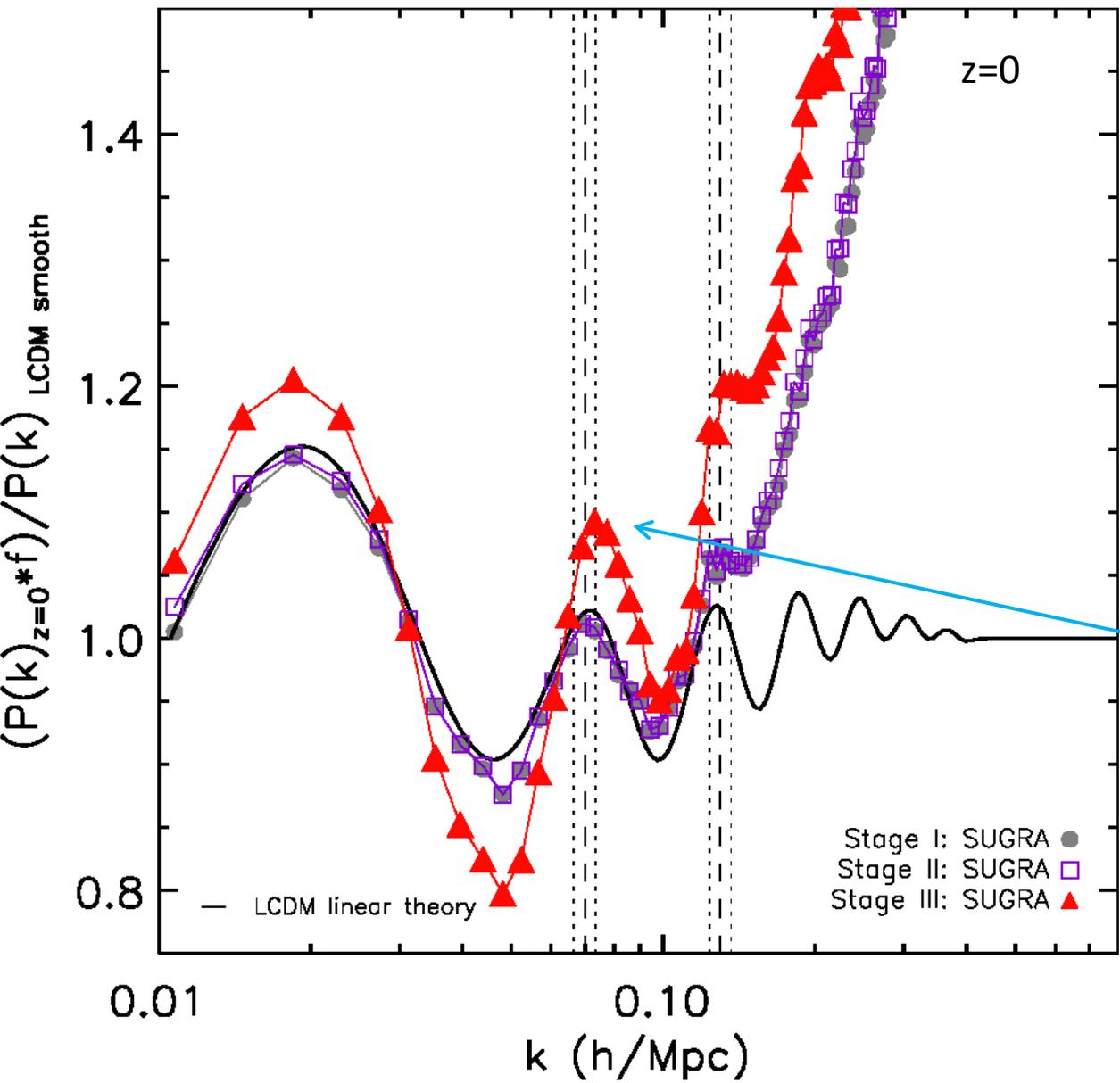
# Baryon acoustic oscillations



SUGRA

Stage I : SUGRA linear growth factor  
Stage II : SUGRA linear theory

# Baryon acoustic oscillations

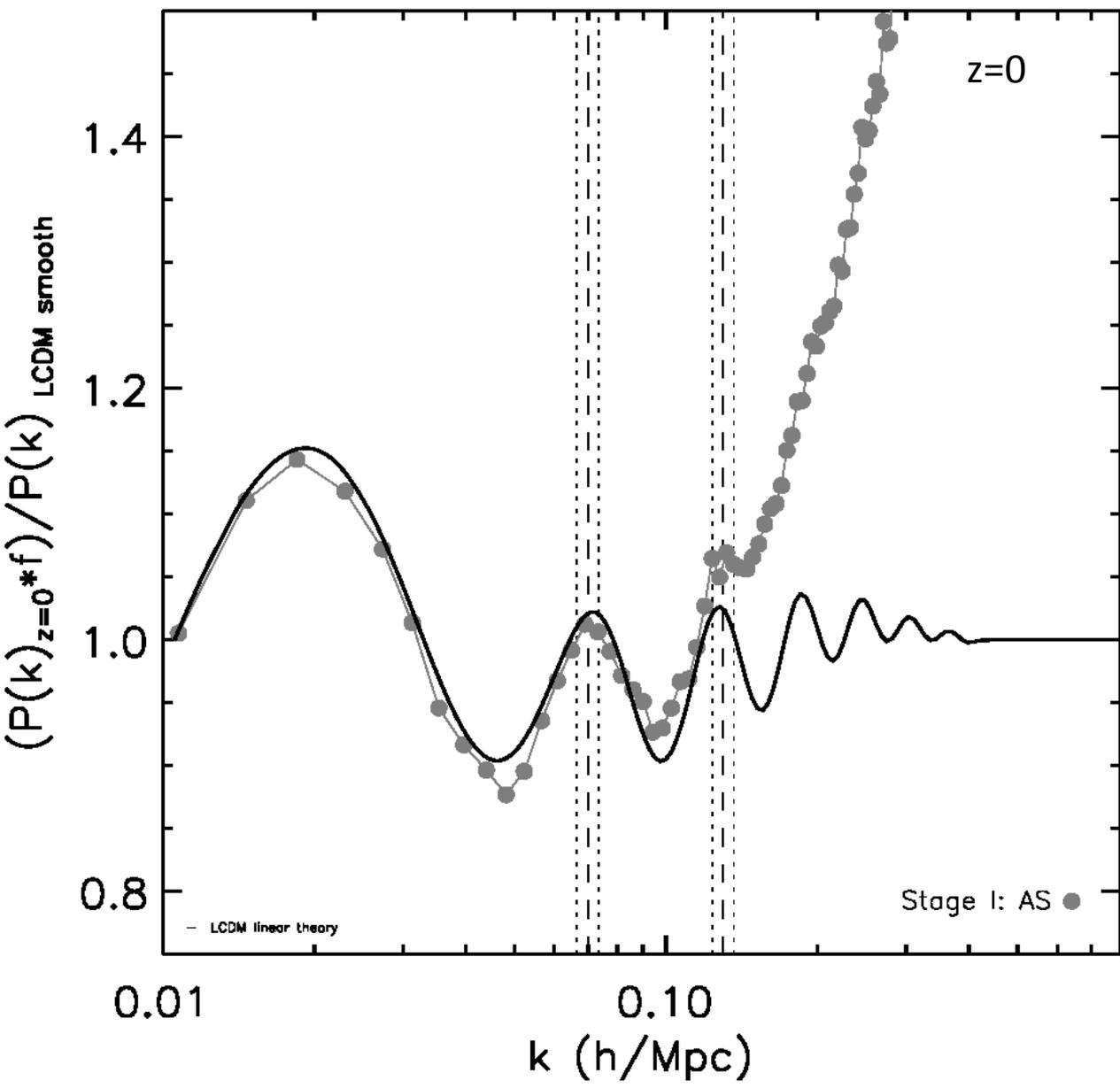


SUGRA

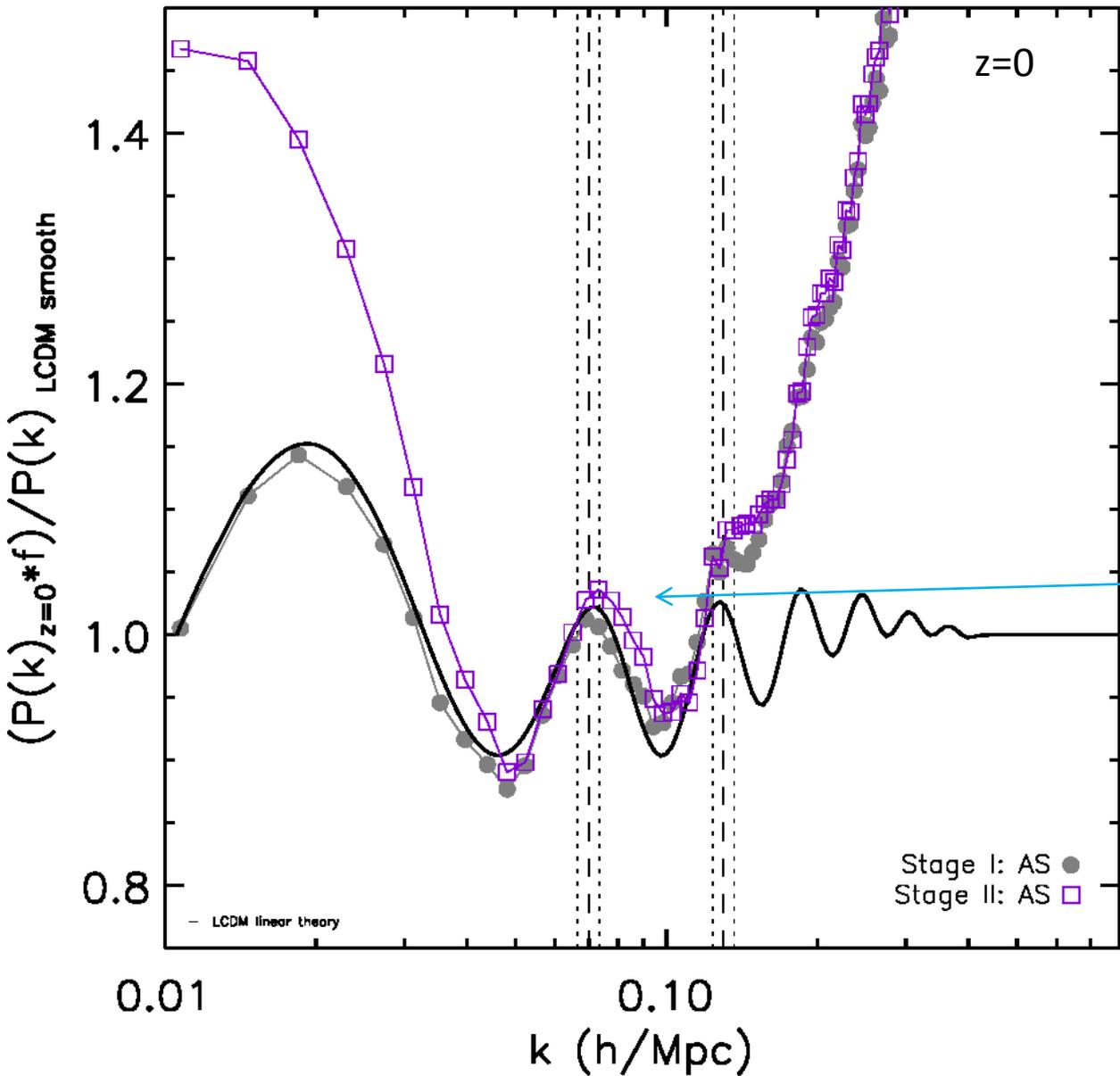
- Stage I : SUGRA linear growth factor
- Stage II : SUGRA linear theory
- Stage III: SUGRA best fit parameters

5% shift in second peak

# Baryon acoustic oscillations



# Baryon acoustic oscillations



AS

Stage I : AS linear growth factor  
Stage II : AS linear theory

Shift in second peak using LCDM parameters

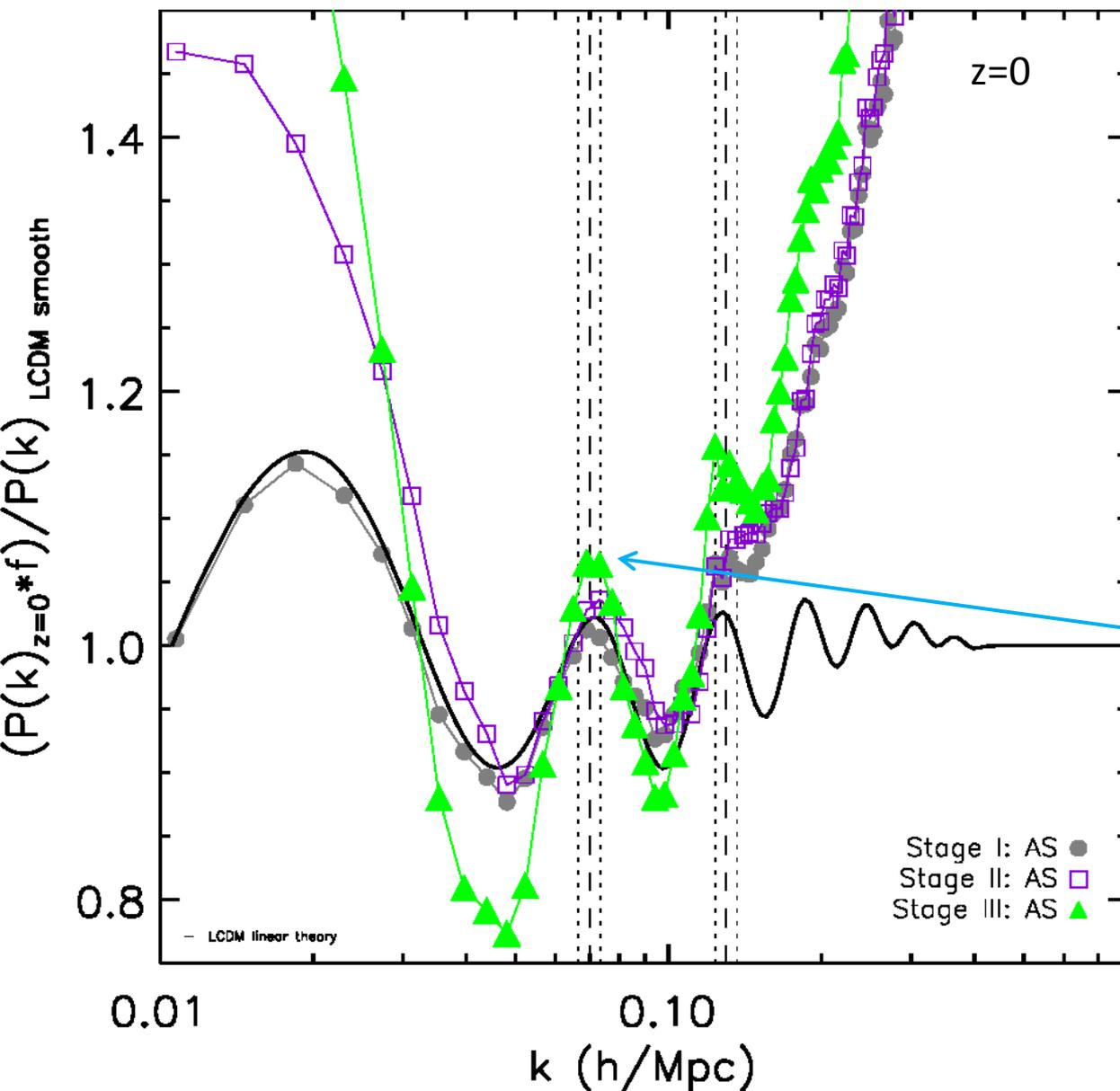
Sound horizon at  $l_{ss}$

$\Lambda$ CDM  $r_s = 146.28 \text{Mpc}$

Stage I: AS  $r_s = 137.8 \text{Mpc}$

**Jennings et al. 2010**

# Baryon acoustic oscillations



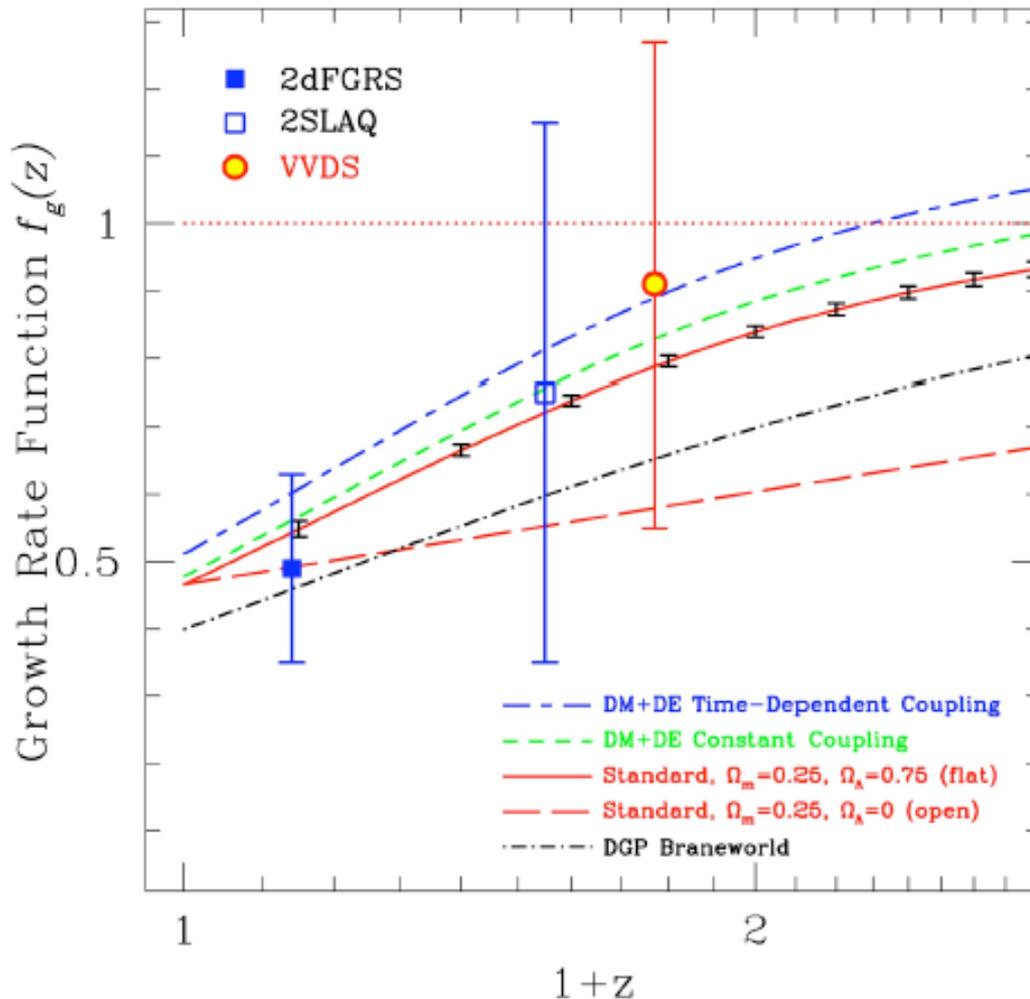
Sound horizon at lss

$\Lambda\text{CDM } r_s = 146.8\text{Mpc}$

Stage III: AS  $r_s = 149.8\text{Mpc}$

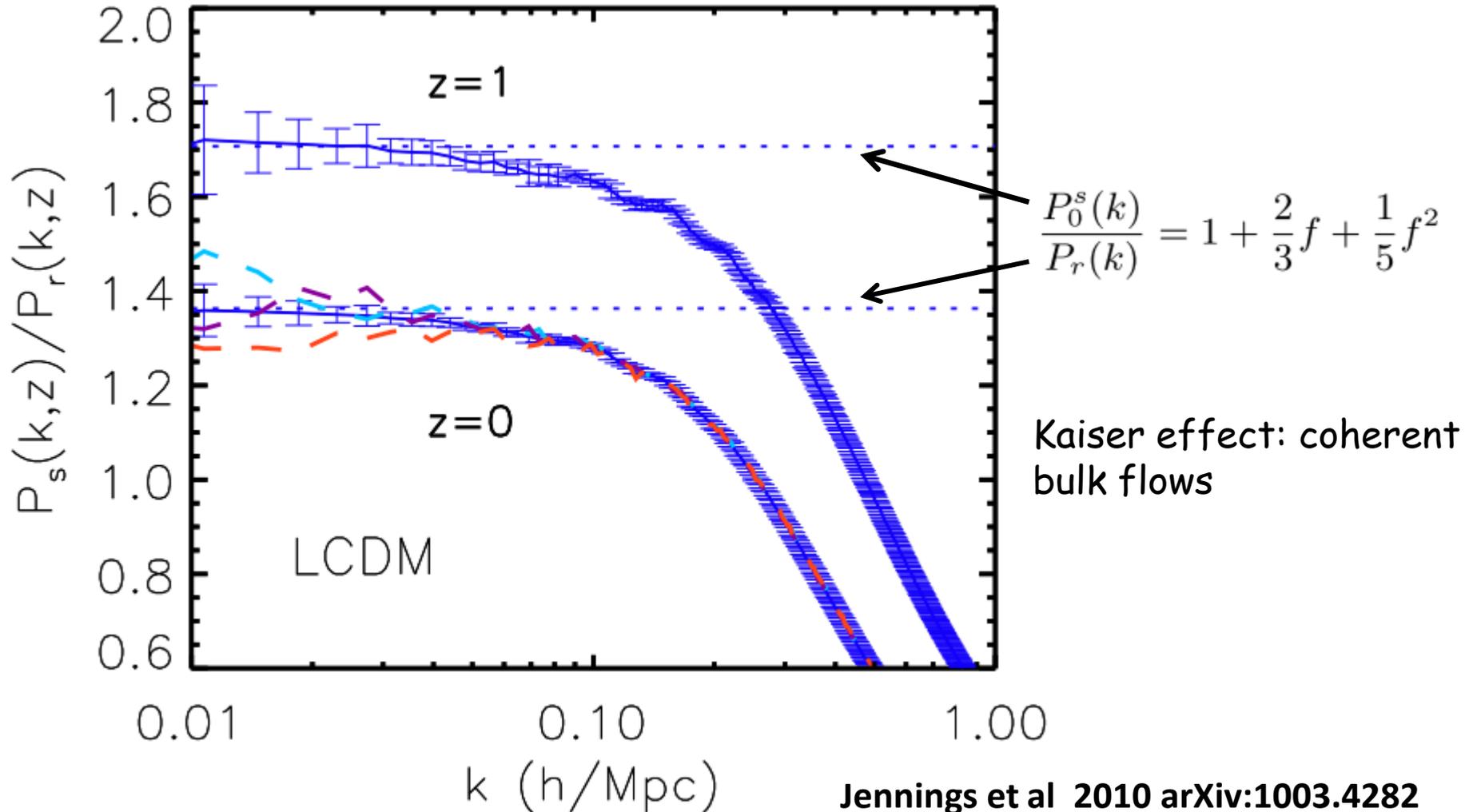
**Jennings et al. 2010**

# Growth rate of structure



- Expansion history  $a(t)$  influences growth of structure
- Compare  $a(t)$  from  $z$ -space distortions with independent estimate derived from  $H(z)$
- Distinguish dark energy and modified gravity

# Measuring the growth factor: redshift space distortions of $P(k)$

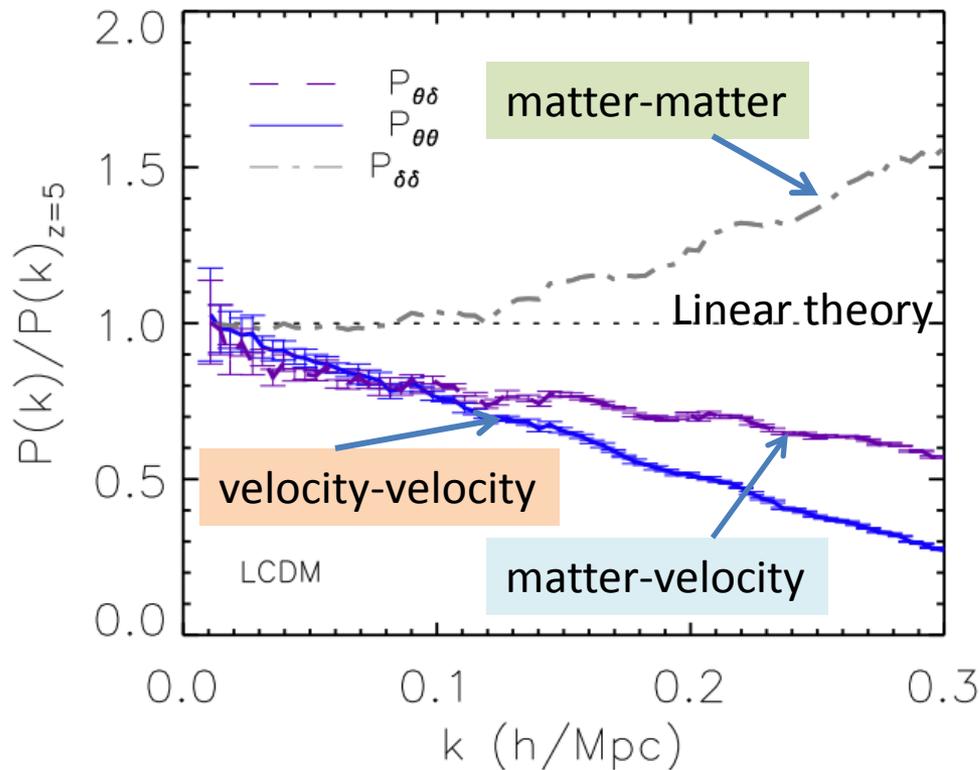


# Redshift space distortions: The Kaiser (1987) model

$$\frac{P_0^s(k)}{P^r(k)} = 1 + \frac{2}{3}f + \frac{1}{5}f^2 \quad f = d \ln D / d \ln a.$$

1. The small scale velocity dispersion can be neglected.
2. The velocity gradient  $|d\vec{u}/dr| \ll 1$ .
3. The velocity and density perturbations satisfy the linear continuity equation.
4. The real space density perturbation is assumed to be small,  $|\delta(r)| \ll 1$ , so that higher order terms can be neglected.

# Accurate redshift space distortions



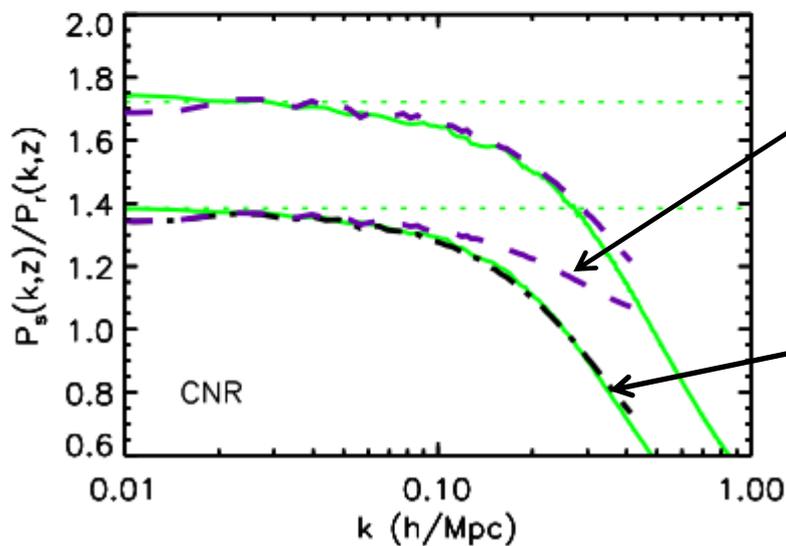
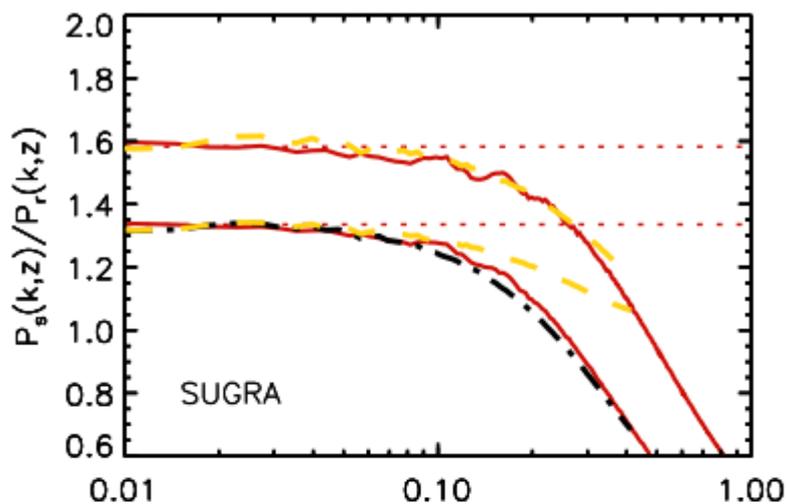
Kaiser formula: linear theory

$$\frac{P_0^s(k)}{P_r(k)} = 1 + \frac{2}{3}f + \frac{1}{5}f^2$$

Nonlinear terms: Scoccimarro 2004

$$P_0^s(k) = P_{\delta\delta}(k) + \frac{2}{3}fP_{\delta\theta}(k) + \frac{1}{5}f^2P_{\theta\theta}(k)$$

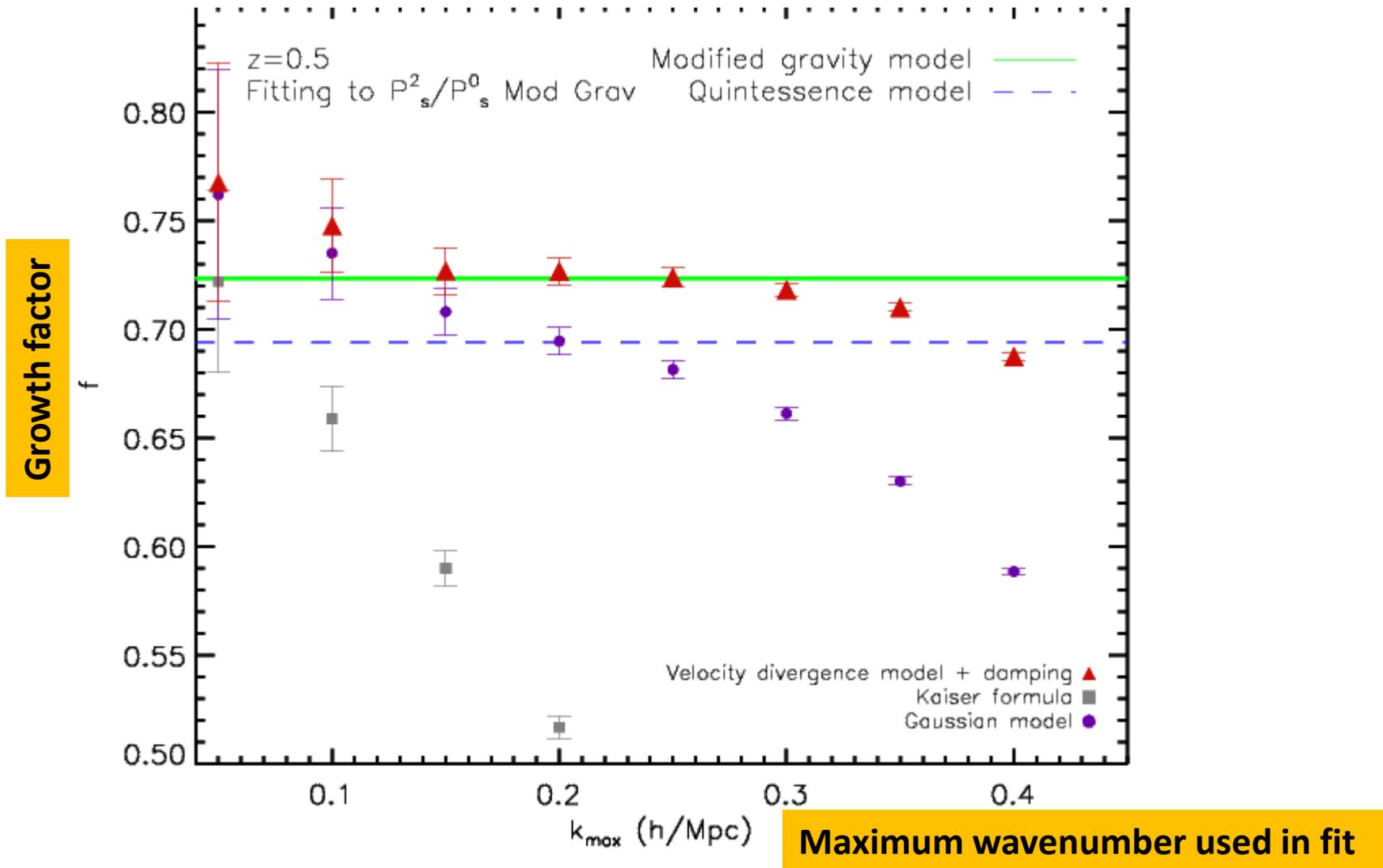
# Accurate redshift space distortions



$$P_0^s(k) = P_{\delta\delta}(k) + \frac{2}{3}fP_{\delta\theta}(k) + \frac{1}{5}f^2P_{\theta\theta}(k)$$

Including velocity dispersion

# Impact on recovered growth factor



# Summary

- Linear perturbation theory is not accurate enough even on surprisingly large scales
- Simulations DM + galaxies reveal: scale dependent bias and scale dependent redshift space distortions
- Quintessence simulations:
  - alter expansion rate
  - early dark energy: change linear  $P(k)$  shape
  - alter best fit parameters for consistency with obs.
- BAO (and mass function) cannot distinguish all quintessence models from cosmological constant
- Redshift space distortions more complicated than generally thought - but better models do exist

# “QUICC” Quintessence at the ICC

**L-Gadget2** (Springel 2005)

$$N_p = 2.69 \times 10^8 \text{ particles}$$

$$L_{\text{box}} = 1500 h^{-1} \text{ Mpc}$$

Softening:  $\epsilon = 50 h^{-1} \text{ kpc}$

Starting redshift:  $z_i = 200$

Mass resolution:

$$M_p = 9.067 \times 10^{11} h^{-1} M_{\odot}$$

$$r_{\text{mean}} \sim 2.3 h^{-1} \text{ Mpc}$$

$\Lambda$ CDM Cosmological parameters (A.

Sánchez et al. 2009)

$$\Omega_m = 0.261 \quad \Omega_B = 0.044$$

$$h = 0.715 \quad n_s = 0.96$$

$$\sigma_8 = 0.8$$

