

Licia Verde

Unsolved problems in ...  
Large-scale structure

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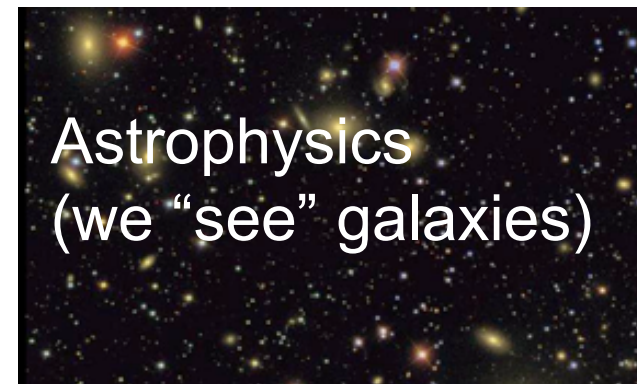
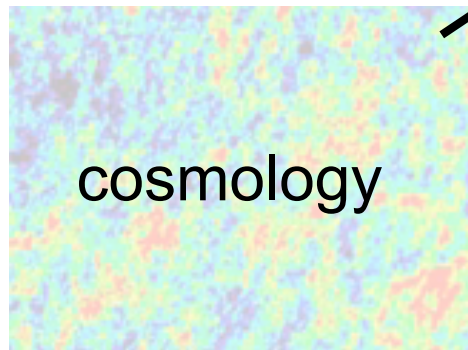
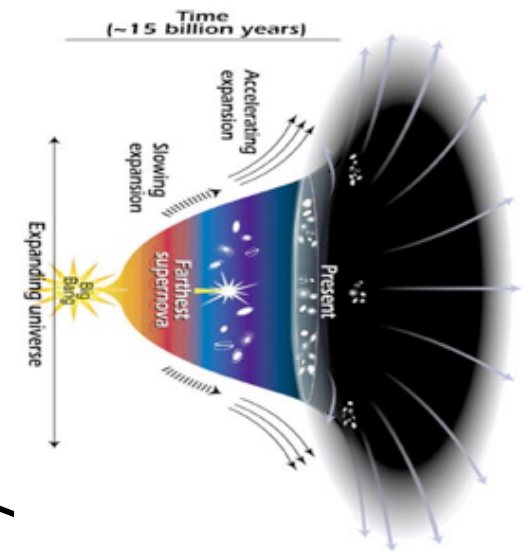
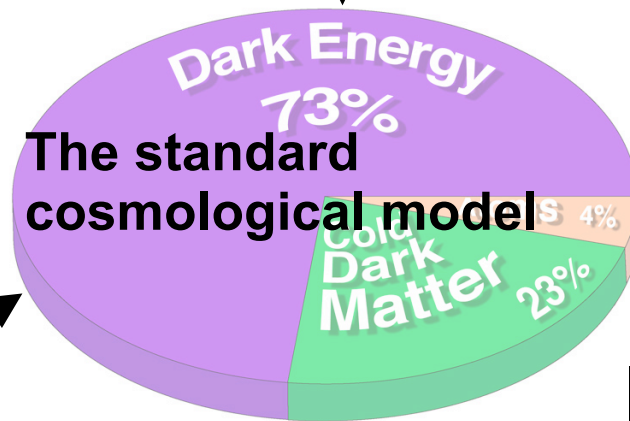


Institut de Ciències  
del Cosmos



# An extremely successful model for a preposterous Universe

Fundamental physics  
(particle physics, gravity)





# The status of cosmology

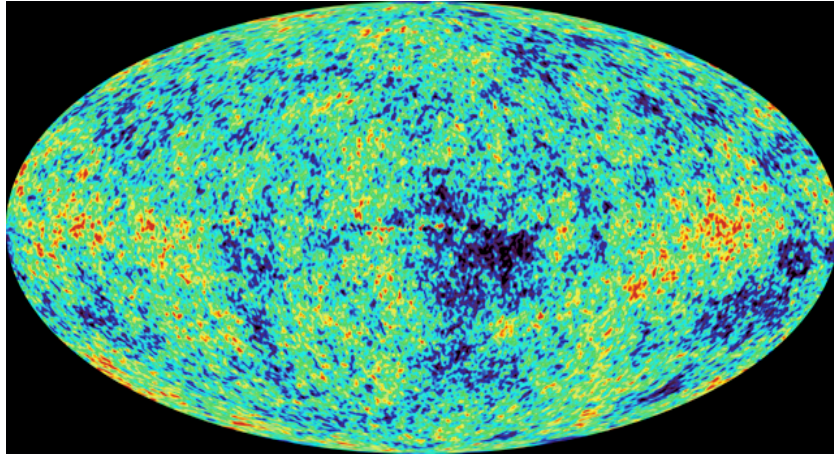


The status of LSS



Last Judgment, Vasari, Florence Duomo

# Why large scale structure



CMB: Spectacular results

A snapshot of the Universe at recombination

Simple, clean physics

Perturbations are still linear, close to the initial conditions

Window into the early universe

**BUT**

13Gyr of Universe's history are just a "shadow" via secondary anisotropies

Physics happening

e.g., accelerated expansion, neutrinos properties, dark matter properties, etc.

The CMB gives mostly 2D info (snapshot), LSS add the third dimension and breaks degeneracies

The non-linearity of perturbations may have extra useful information



The catch is that things get much more  
**MESSY**

**Different probes:**

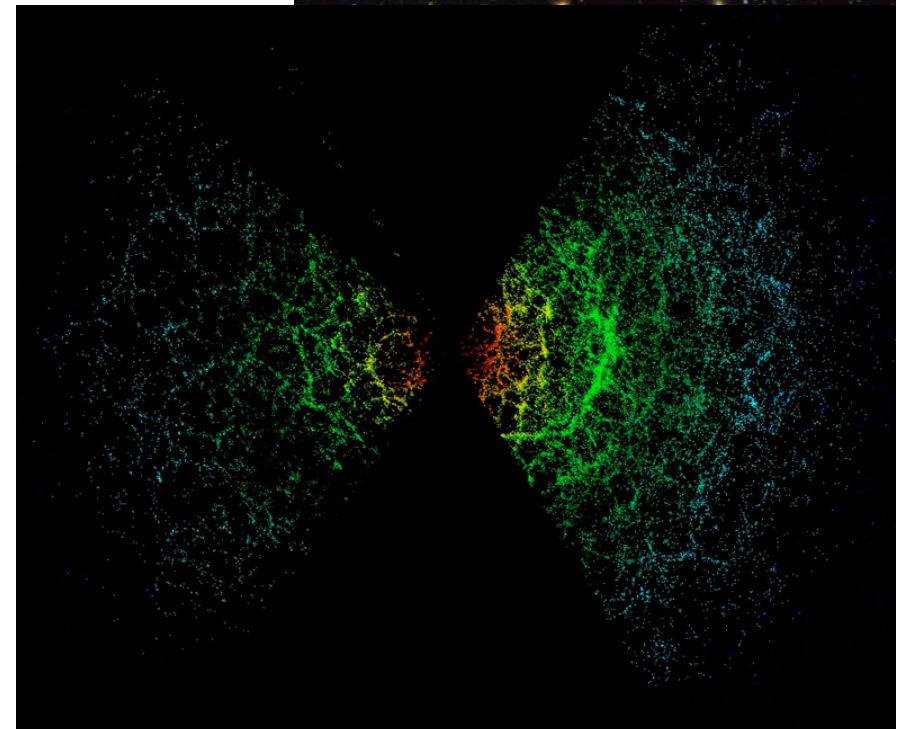
Weak gravitational lensing (A. Heavens)

Galaxy clustering

Galaxy clusters

Lyman-alpha forest

21 cm (A. Loeb, J. Hewitt)



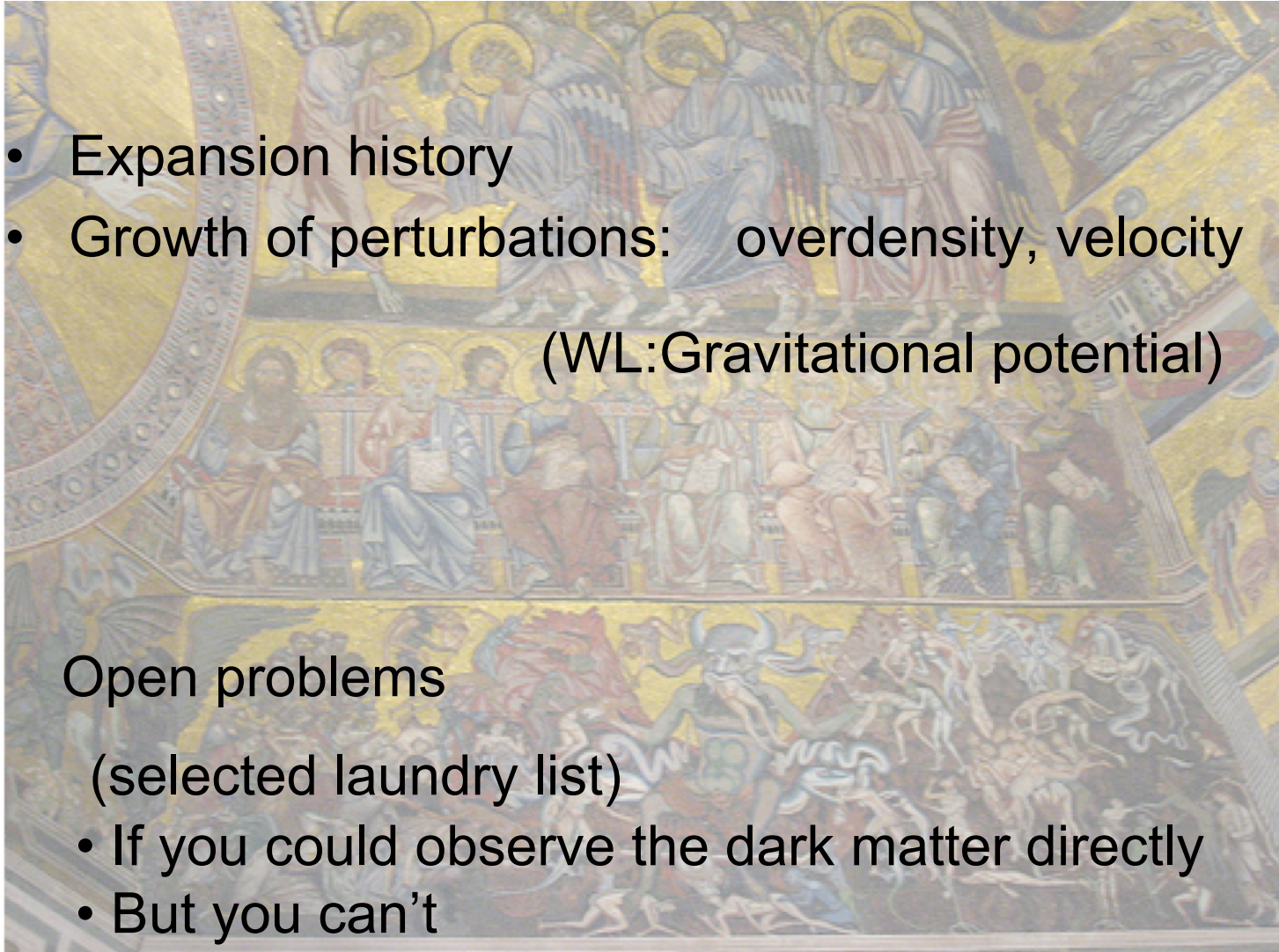
# What can LSS probe

- Expansion history
- Growth of perturbations: overdensity, velocity  
(WL: Gravitational potential)

## Open problems

(selected laundry list)

- If you could observe the dark matter directly
- But you can't





# Preliminaries: statistics

## Real space

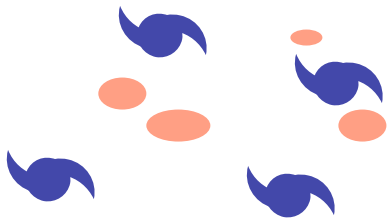
Correlation function

Localized in real space

Highly correlated errors

Not sensitive  
to sky cuts/selection fn

Mix of linear-non linear scales



## Fourier space

Power spectrum

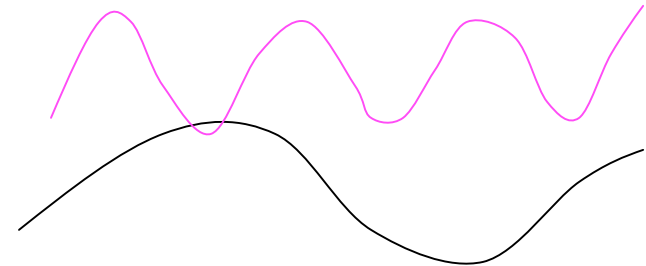
not

Uncorrelated errors  
in linear theory

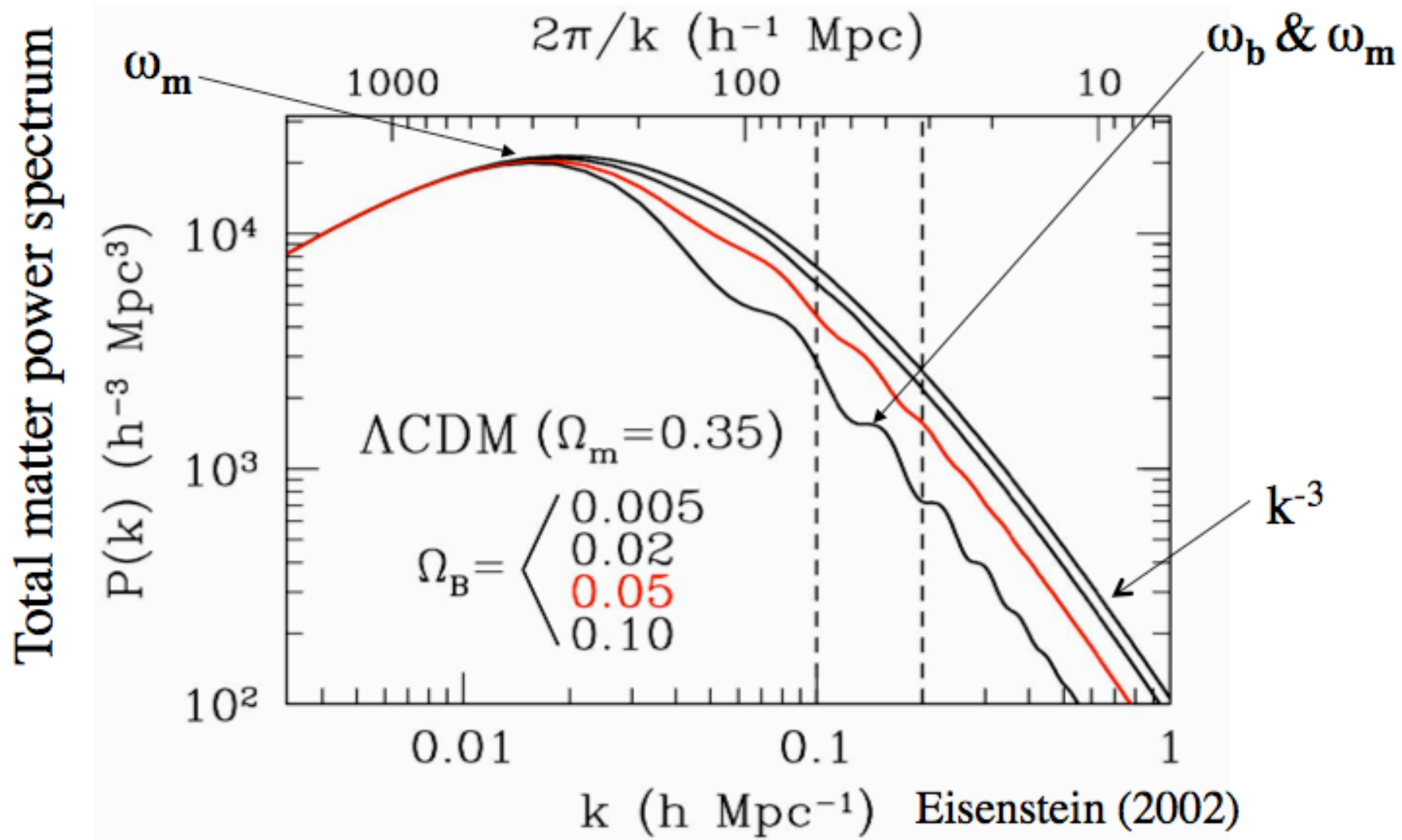
Very sensitive

Clear separation  
linear-non linear scales

FT pairs!

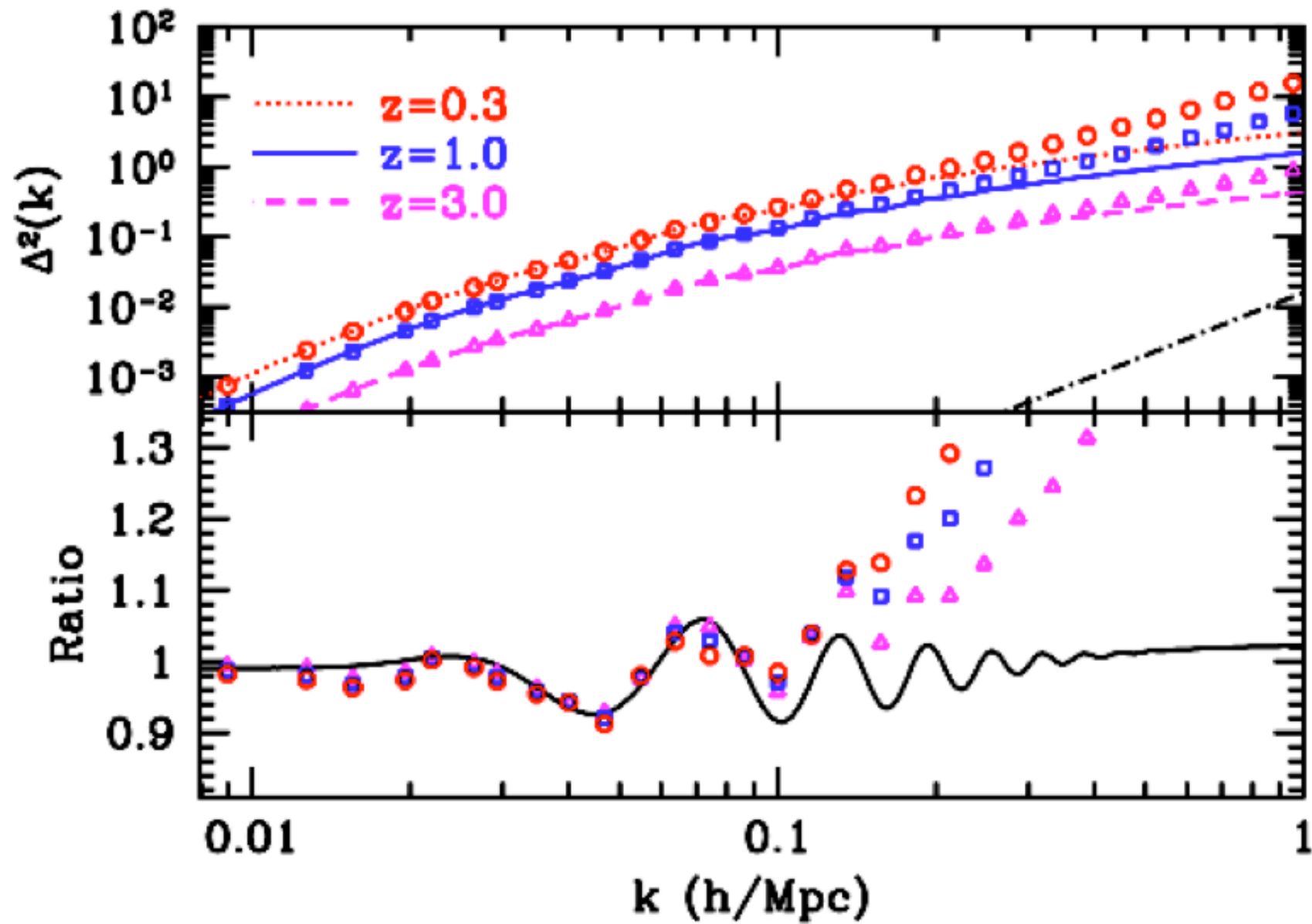


# Matter power spectrum: $P_L(k)$





# Non-linearity



# Non-linearity

Equations of motions ( $\Omega_m=1$ )

Note: no GR

$$\begin{aligned}\frac{\partial \delta}{\partial \tau} + \vec{\nabla} \cdot [(1 + \delta)\vec{v}] &= 0 \\ \frac{\partial \vec{v}}{\partial \tau} + \mathcal{H}\vec{v} + \left(\vec{v} \cdot \vec{\nabla}\right)\vec{v} &= -\vec{\nabla}\Phi \\ \nabla^2\Phi &= \frac{3}{2}\mathcal{H}^2\delta\end{aligned}$$

- Very familiar looking fluid equations
  - means we can borrow methods/ideas from other fields.
- Note the quadratic nature of the non-linearity.
- Since equations are now non-linear, can't use superposition of (exact) solutions even if they could be found!
- Proceed by perturbative expansion.



# Aside (what gauge?)

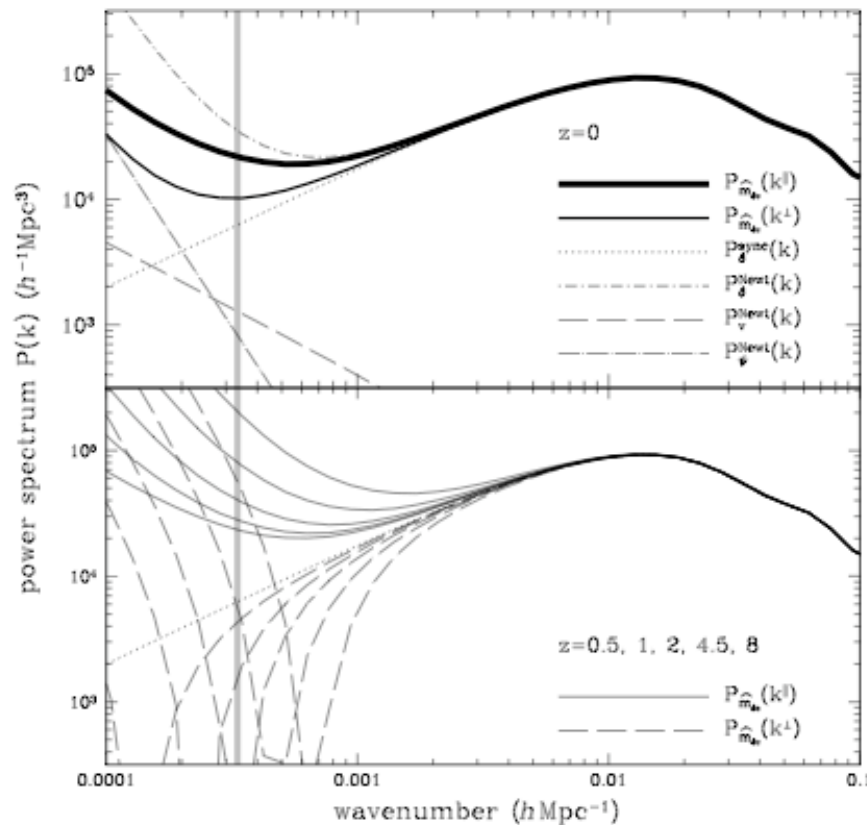


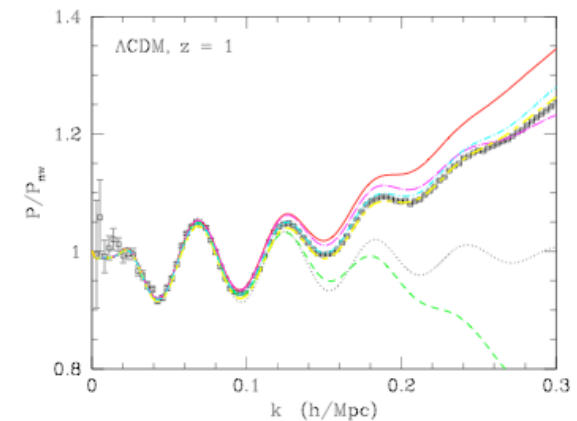
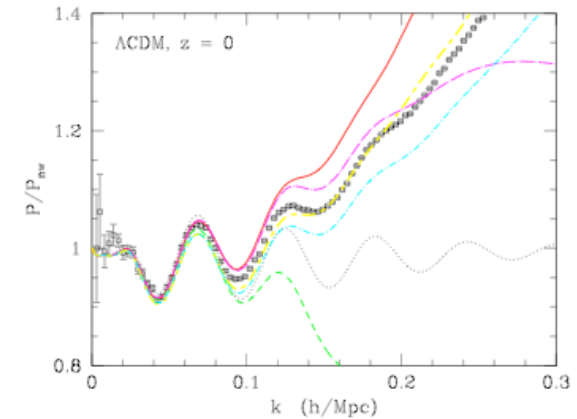
FIG. 1: Matter power spectrum  $P_{\hat{m}_{\delta z}}(k, \mu_k)$  at various redshifts. Upper panel: Solid lines represent the matter power spectrum at  $z = 0$ , computed by using Eq. (7) along the line-of-sight direction ( $\mu_k = 1$ ; thick) and along the transverse direction ( $\mu_k = 0$ ; thin). For reference, various lines indicated in the legend show power spectra of perturbation variables in the conformal Newtonian gauge and the synchronous gauge. Bottom panel: matter power spectrum  $P_{\hat{m}_{\delta z}}(k, \mu_k)$  at  $z > 0$ , but with its amplitude normalized to match  $P_{\hat{m}_{\delta z}}(k, \mu_k)$  at  $z = 0$ . Solid and dashed lines represent  $P_{\hat{m}_{\delta z}}(k, \mu_k)$  with  $\mu_k = 1$  and  $\mu_k = 0$ , respectively. The horizon scale at  $z = 0$  is shown as a vertical line.

- What are we actually measuring ?

On very large scales,  
not clear (Yoo 10)

# Analytical tools to model non-linearities

- Perturbation theory
- Renormalized PT
- Lagrangian PT
- Renormalization group
- Time renormalization group



Open issues: which is best? In what regime? for what models?

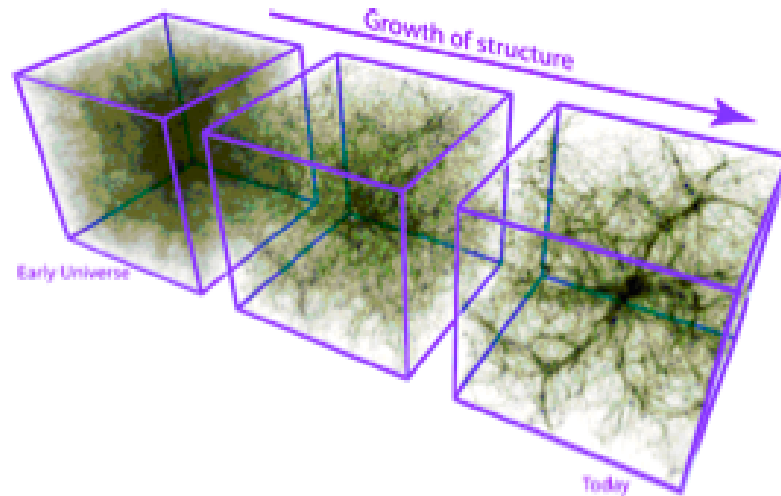
Carlson et al 09 (and refs therein), Pietroni 08, S. Matarrese



# Simulate the heck out of it

(G. Hinshaw)

If it is “just” gravity,  
N-body, DM-only  
simulations should do  
the trick (V. Springel)



Issues: resolution, starting redshift, initial conditions...(Wagner)

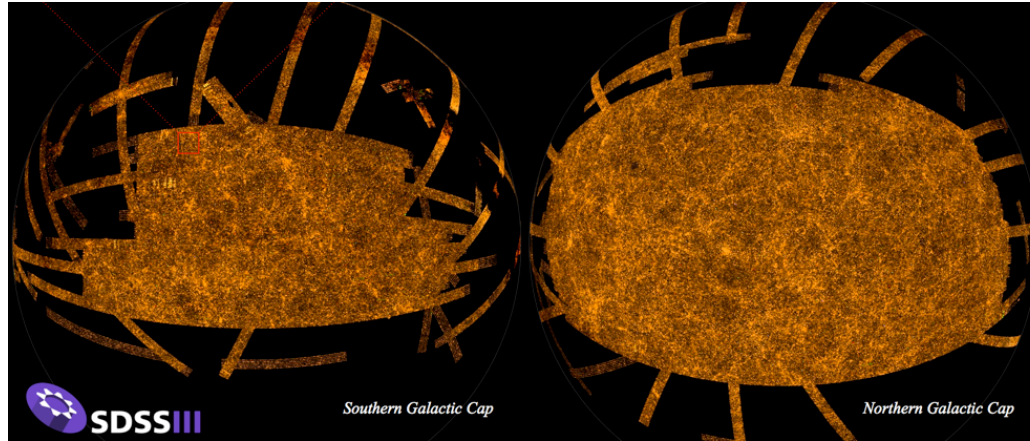
In particular: computationally expensive

How to explore different cosmologies? “cosmic calibration” (LANL)

for future surveys: the entire survey volume cannot be simulated  
What volume is needed? Would many small volumes do? (later)

# ERRORS (covariances)

In the correlation function correlations are always large  
--> Monte-Carlo simulate errors on mock Universes (surveys)



In the power spectrum:

Linear theory, infinite volume no correlations!!!

Effect of the mask (sky-cut) and selection function--> mode coupling

Non-linearities --> mode coupling

Relatively new effect: beat coupling

**CAN'T simulate the full survey volume**

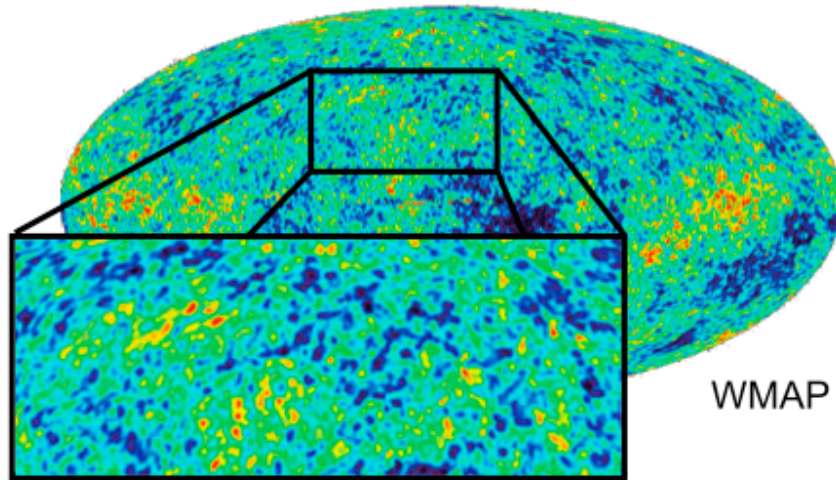
Open issue!

Roland De Putter, Olga Mena for SDSS

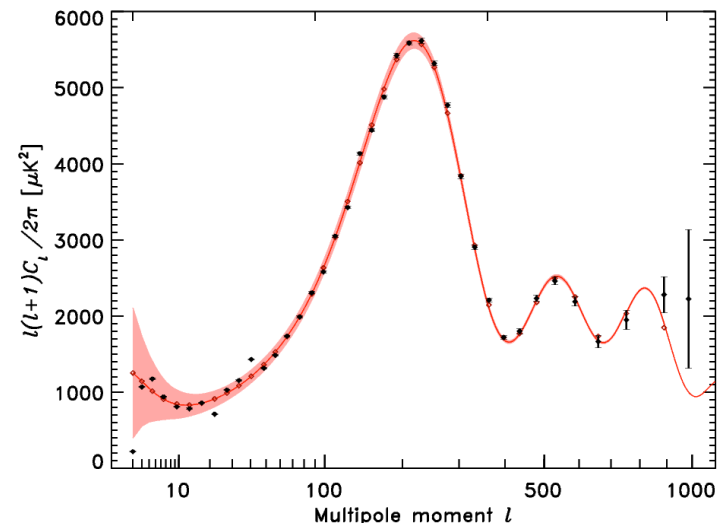
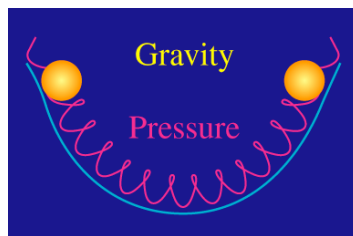
# Expansion history

## BAO Baryon acoustic oscillations

Sound horizon at decoupling

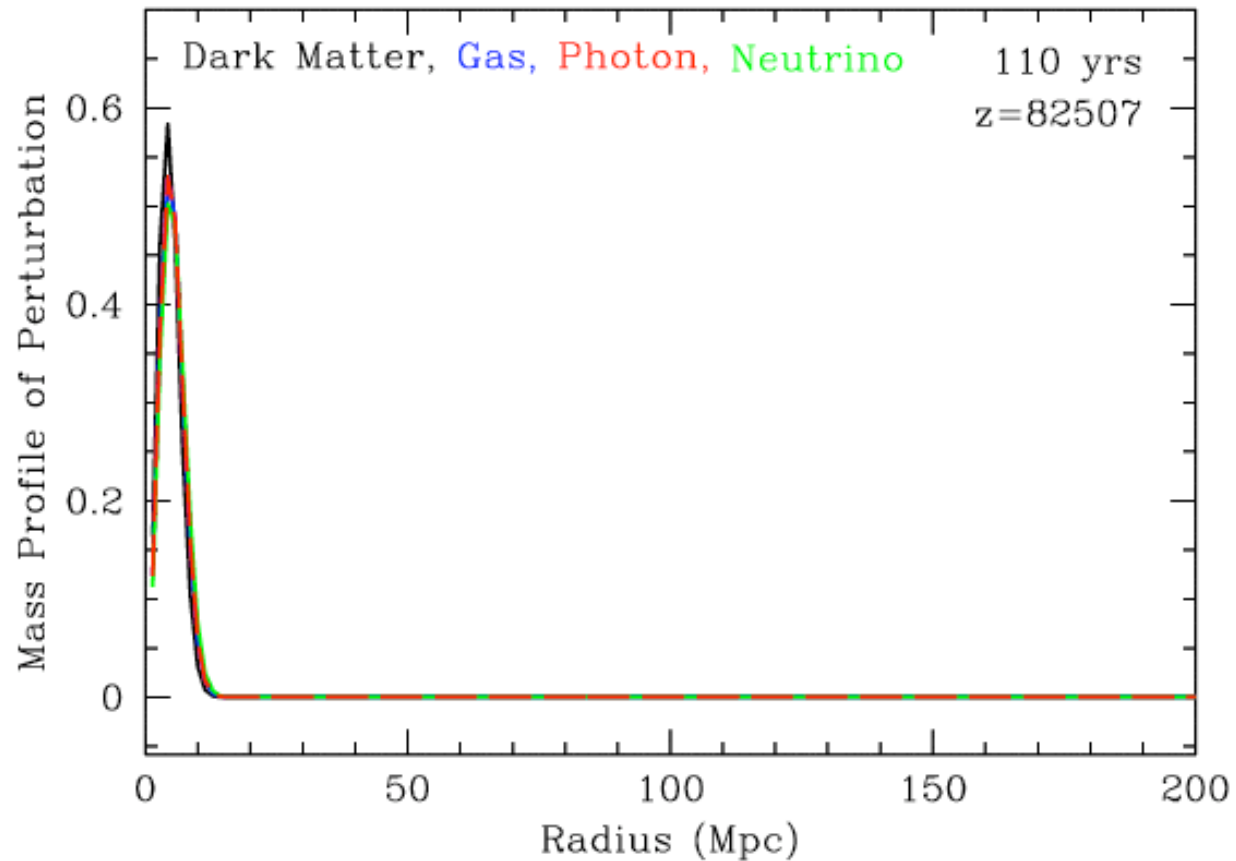


$$k_{\text{bao}} = 2\pi/s$$
$$s = \frac{1}{H_0 \Omega_m^{1/2}} \int_0^{a_*} da \frac{c_s}{(a + a_{\text{eq}})^{1/2}}$$





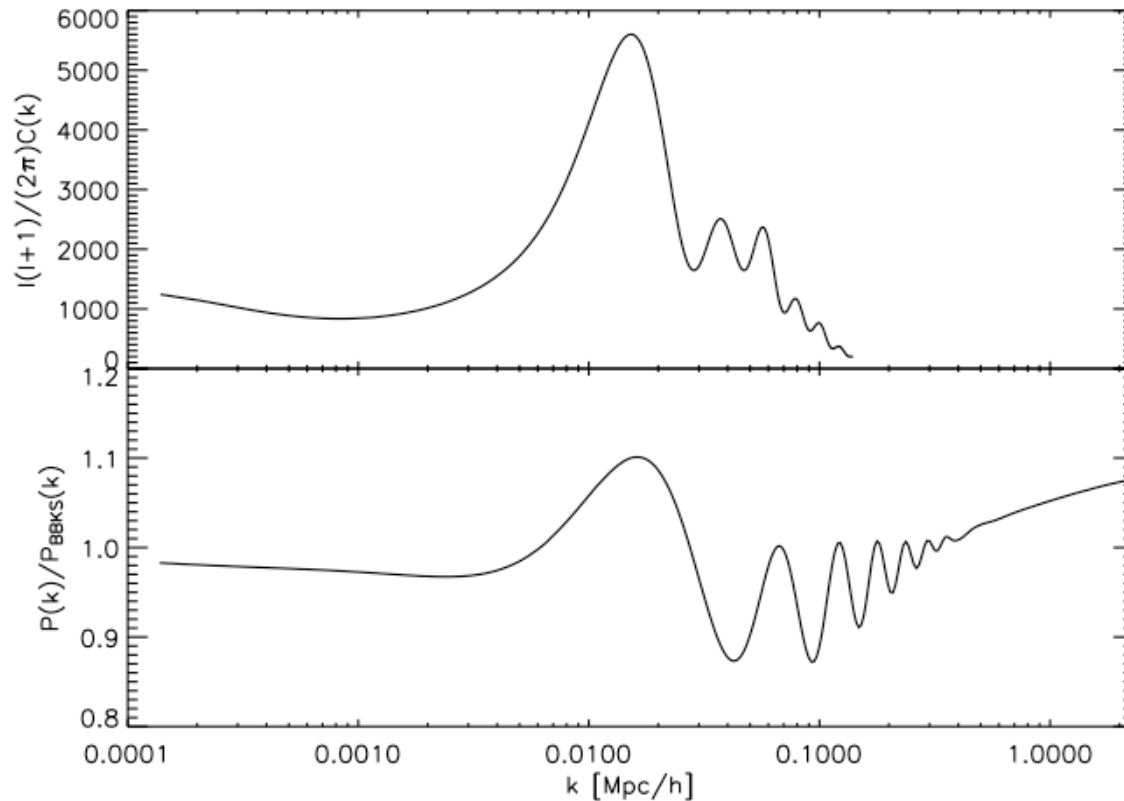
# BAO



For those of you who think in Real space

Courtesy of D. Eisenstein

# BAO



Observe photons

Photons coupled to baryons

“See” dark matter

If baryons are  $\sim 1/6$  of the dark matter these baryonic oscillations should leave some imprint in the dark matter distribution (gravity is the coupling)

For those of you who think in Fourier space

# BAO

Standard rulers at different redshifts

BAO measurements linked to physical BAO scale through:

Radial direction

$$\frac{c}{H(z)} \Delta z$$

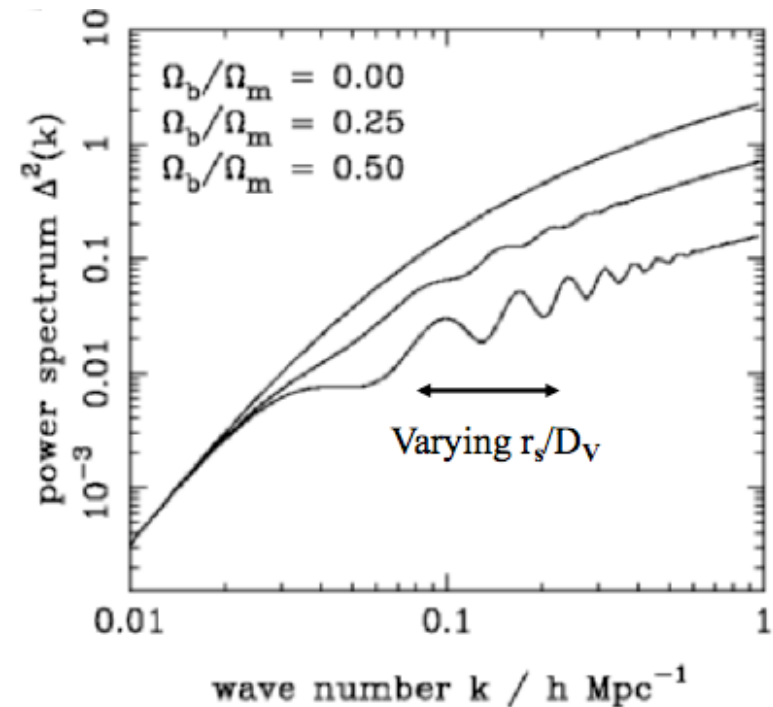
Angular direction

$$(1+z) D_A \Delta \theta$$

On

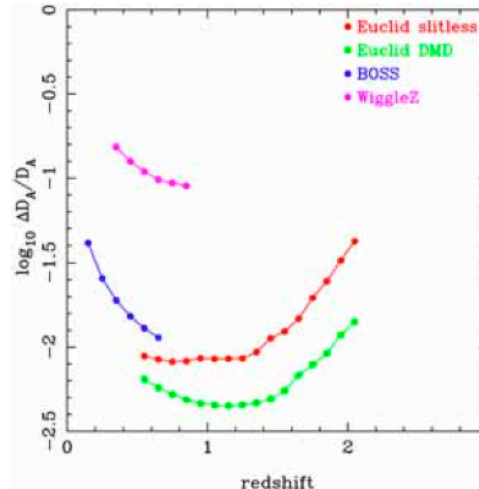
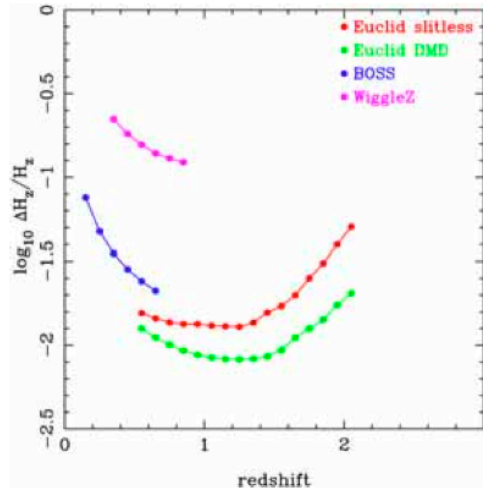
Average:

$$D_V(z) = \left[ (1+z)^2 D_A^2(z) \frac{cz}{H(z)} \right]^{1/3}$$





# Forecasts are great!



EUCLID yellow book  
0912.0914



Open issues: how well is the standard ruler known?  
Shall one also use the AP test?  
Or just relative measurements?

BAO are on linear-mildly non-linear scale:

- non-linearities erase BAO feature: can they be un-done in part?
- can any residual bias be corrected? (see discussion on sims)

# Reconstruction?

Velocity flows and non-linear collapse move matter in the Universe around by of order 10 Mpc relative to its initial comoving position. This tends to move pairs out of the 150 Mpc peak e.g. broaden the BAO.

On the large scales the bulk flows are generated by the density perturbations being surveyed, could one move particles (galaxies) back in time?

Issues: only applied on simulations so far.... (experts?)

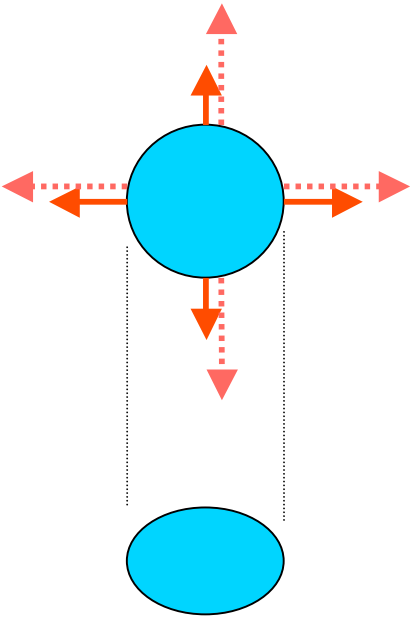
# WHAT ABOUT VELOCITIES?

Redshift-space distortions (Kaiser 1987)

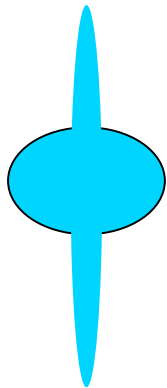
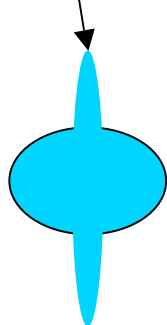
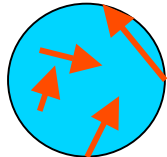
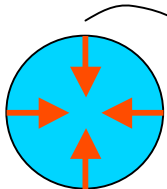
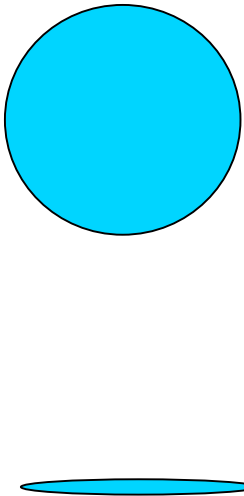
$$z_{\text{obs}} = z_{\text{true}} + \delta v / c$$

$\delta v$  prop. to  $d \ln \delta / d \ln a$   $\delta \rho / \rho$

shells



$\beta$

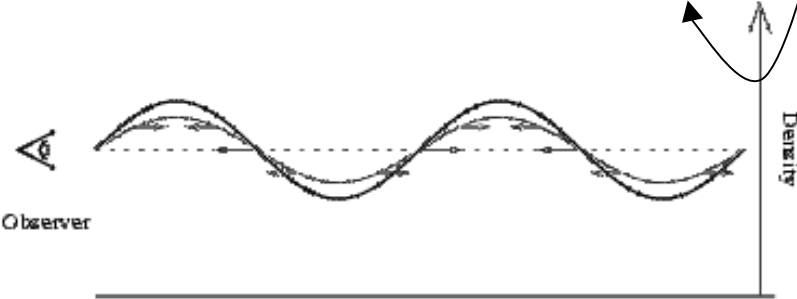


$\sigma_p$

linear

Non-linear

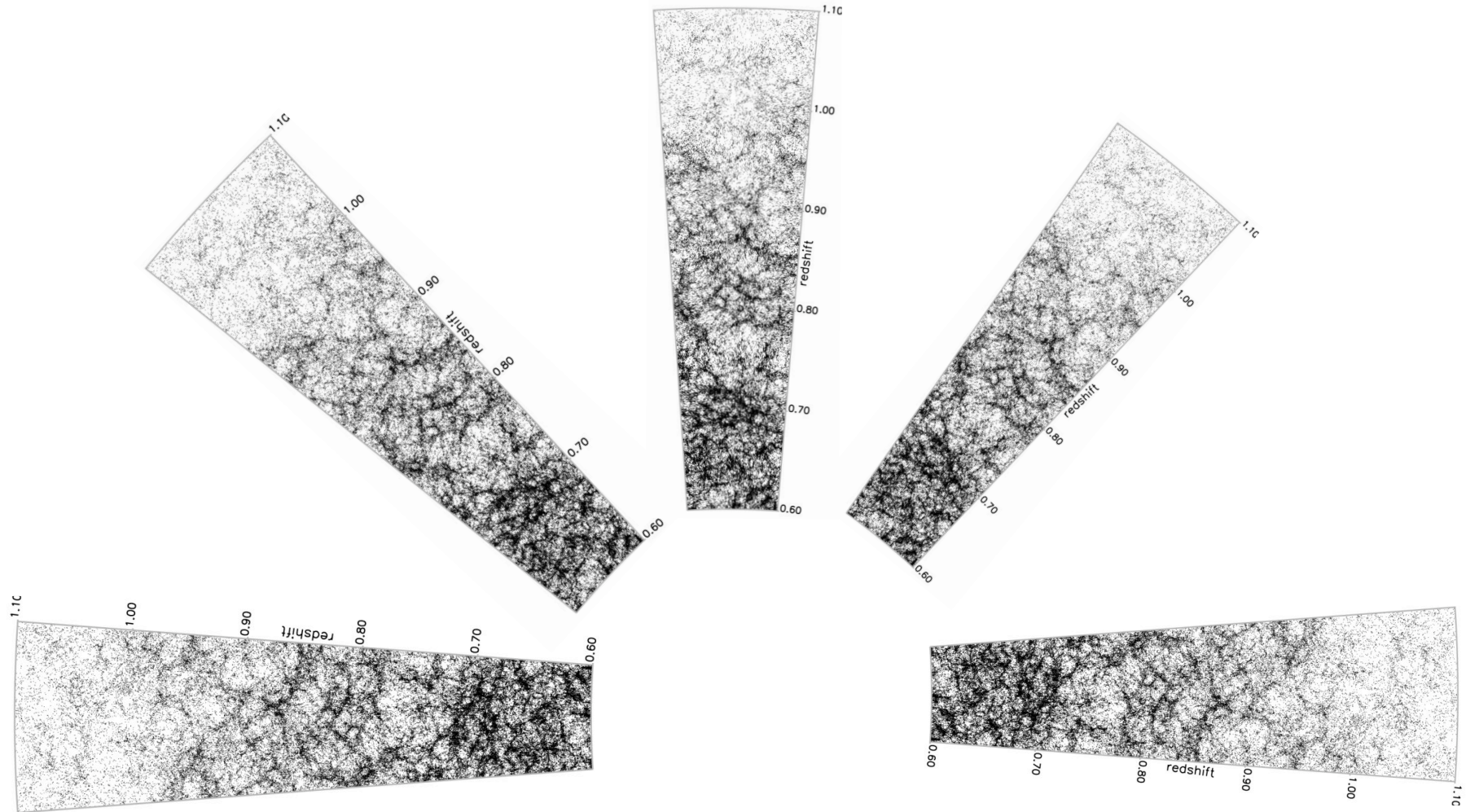
Fourier space



# Unfortunately the sky is not flat

Affects Fourier-based analyses with a dependence on the LOS angle

BAO, redshift-space distortions





# Unfortunately the sky is not flat

Affects Fourier-based analyses with a dependence on the LOS angle

BAO, redshift-space distortions

Open issue: options

Use correlation function (problems with error calculation)

Use small patches where LOS angle does not change (throw info)

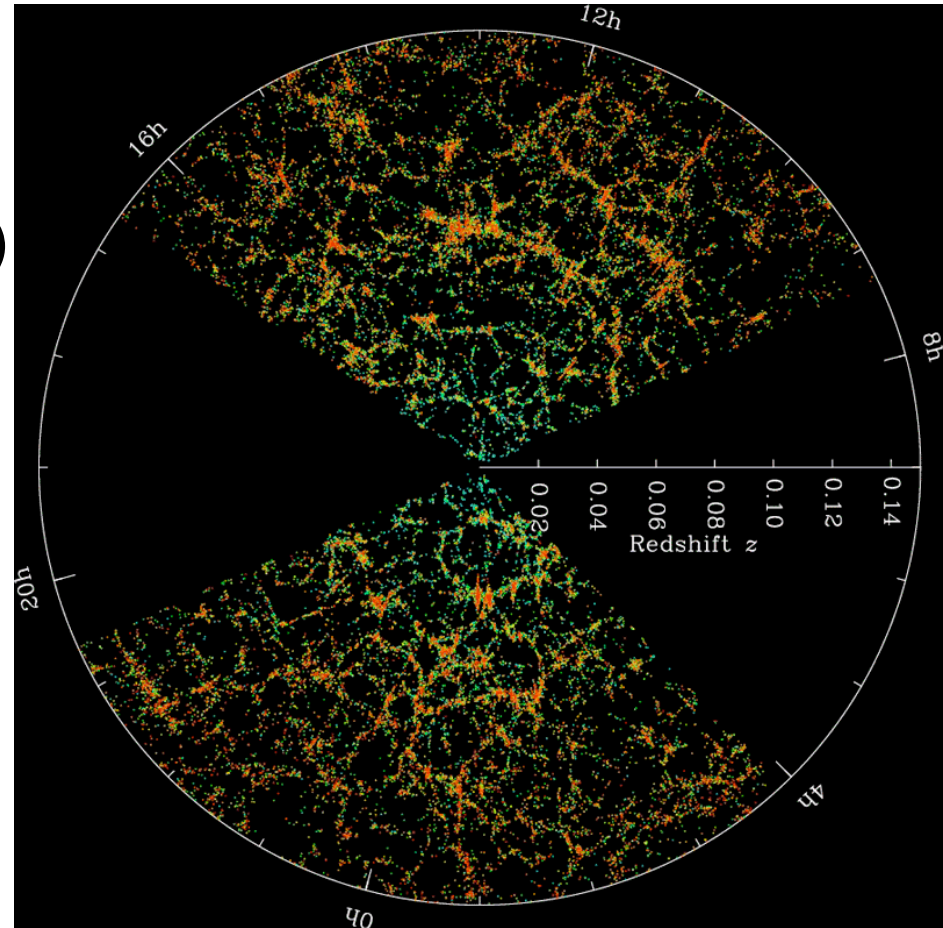
Use radial and angular expansion Sph. Harm+Bessel  
(Heavens, Percival) NOT easy!

Use radial and angular eigenfunctions (not widely used)

Still open...

# If you could see the DM, but you can't

Galaxies:  
galaxy formation(B. Robertson)  
Bias  
Selection of galaxies

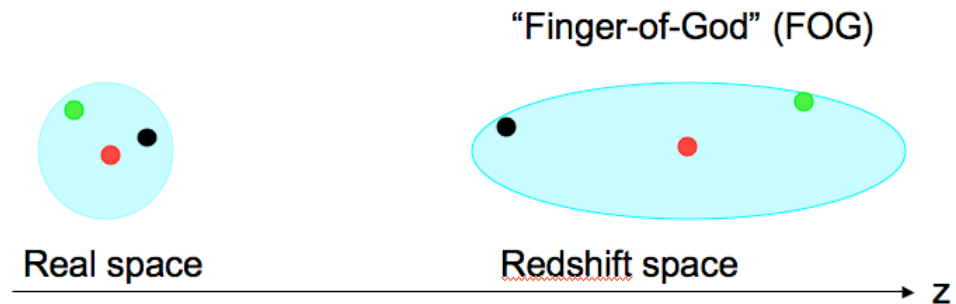
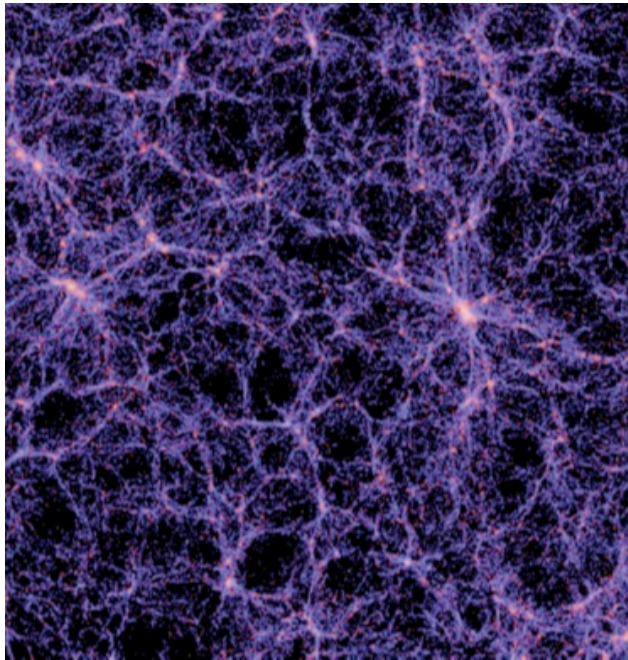


Baryons in the IGM (expected to be closer to the dark matter)

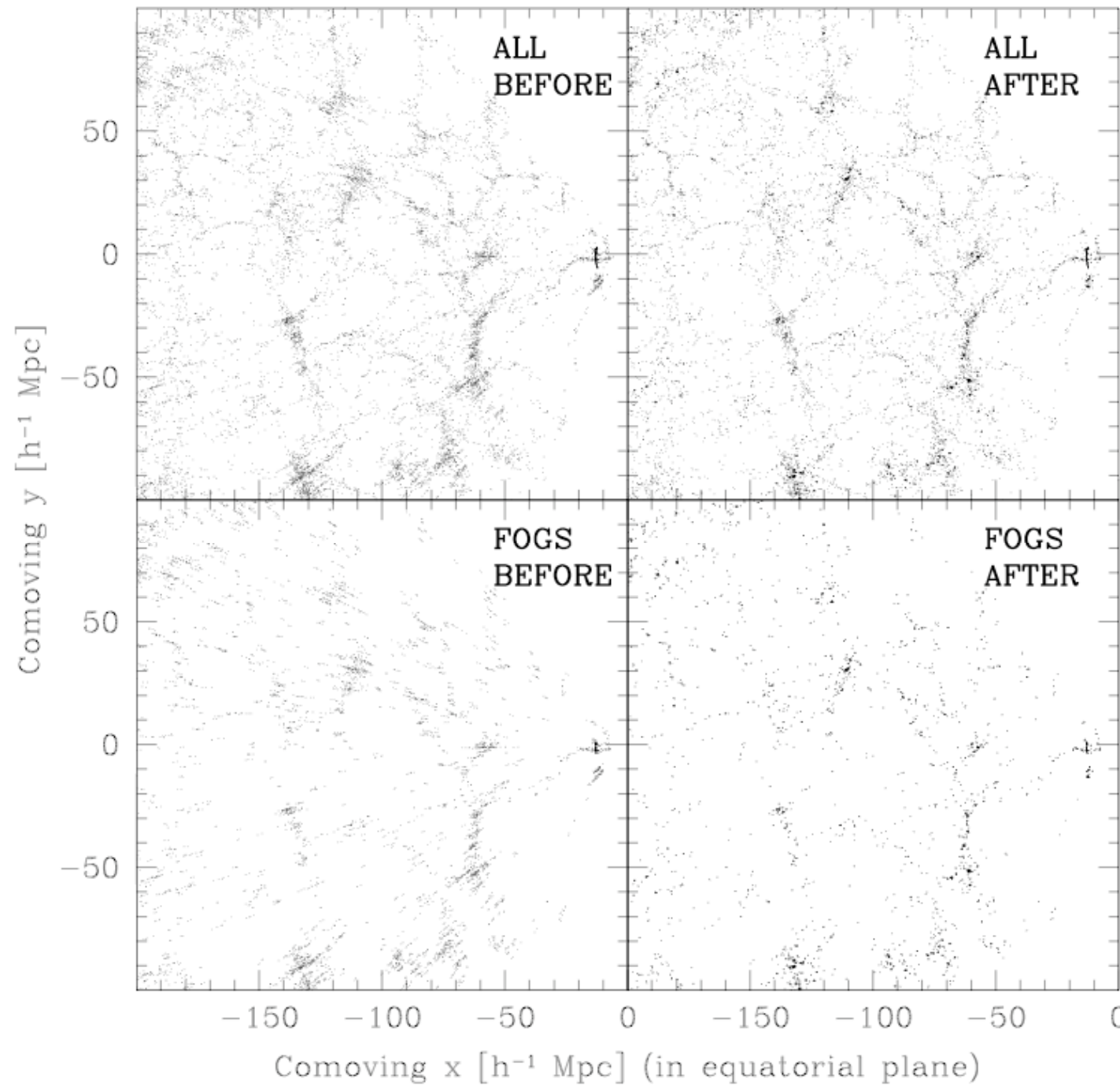
# Challenges, examples

$$\delta = \frac{\delta\rho}{\rho}$$

- density field  $\delta$  goes nonlinear
- uncertainty in the mapping between the galaxy and matter density fields
- Galaxy positions observed in redshift space  
LRG are “special”







From:  
Tegmark et al 04

# More about velocities

galaxy velocities only depend on the distribution of matter

Galaxies as test particles?

Probe temporal metric fluctuations

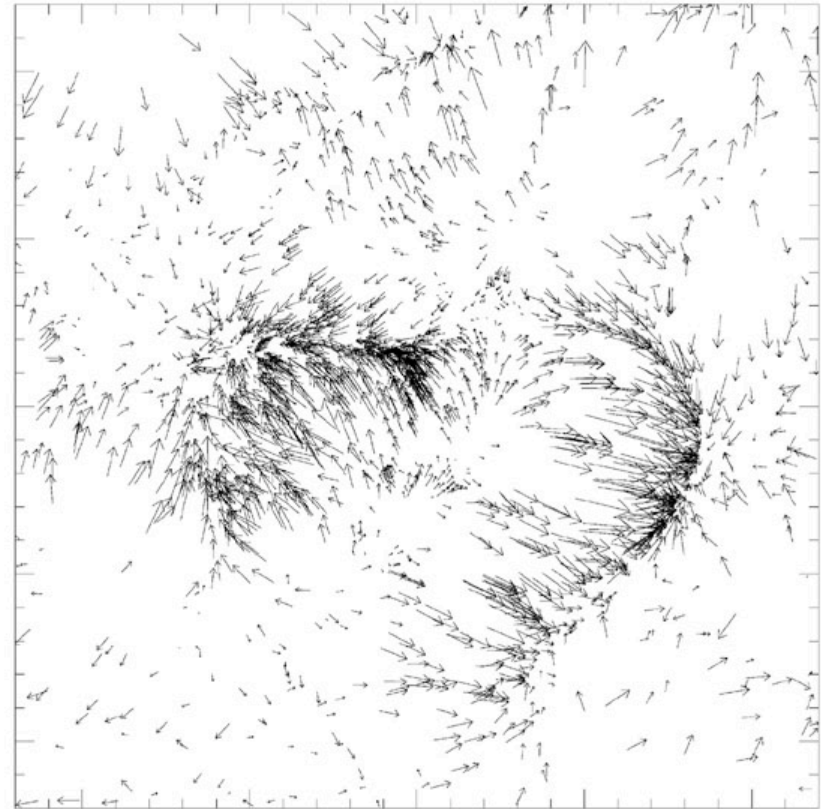
(WL temporal and spatial)

Only LoS measurement

Linear order in perturbations

$$\theta \equiv \nabla \cdot \mathbf{u}, \quad \delta_g^s(k) = \delta_g(k) - \mu^2 \theta(k)$$

$$\begin{aligned} P_g^s(k, \mu, \text{lin}) &\equiv \langle |\delta_g^s(k, \mu)|^2 \rangle, \\ &= P_{gg}(k) - 2\mu^2 P_{g\theta}(k) + \mu^4 P_{\theta\theta}(k) \end{aligned}$$



Yet to uncover full potential

# Large-scale structure $P(k)$ in equations

Information from geometry

- Galaxy clustering as a standard ruler
- BAO or full power spectrum
- Alcock-Paczynski effect

Information from power spectrum shape

- Matter density
- Baryon Acoustic Oscillations
- Neutrino mass
- Inflation fluctuation spectrum
- $f_{\text{NL}}$

$$P_{\text{gal}}(k, \mu, a) = k^n T^2(k) D^2(a) [b(a) + f(a)\mu^2]^2$$

$k$  = comoving wavenumber  
 $\mu$  =  $\cos(\text{angle to line-of-sight})$   
 $a$  = cosmological scale factor  
 $b$  = galaxy bias factor  
 $D$  = linear growth rate  
 $f$  =  $d\ln D/d\ln a$

Information from structure growth

- amplitude of power spectrum
- redshift-space distortions

Slide: courtesy of W. Percival

# Large-scale structure $P(k)$ in equations

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- amplitude of power spectrum
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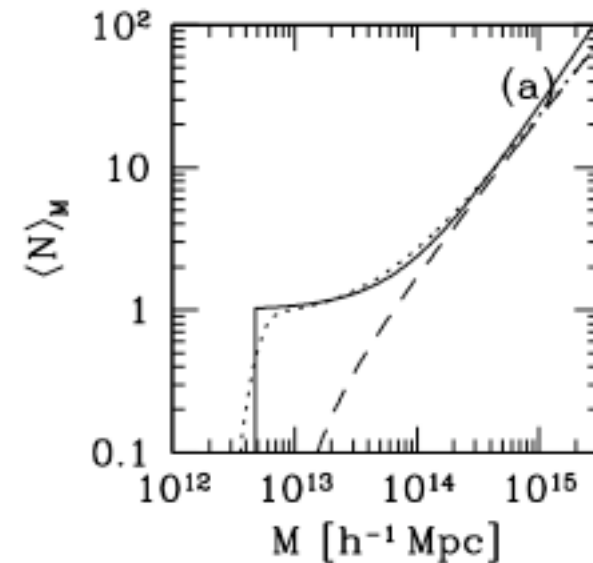
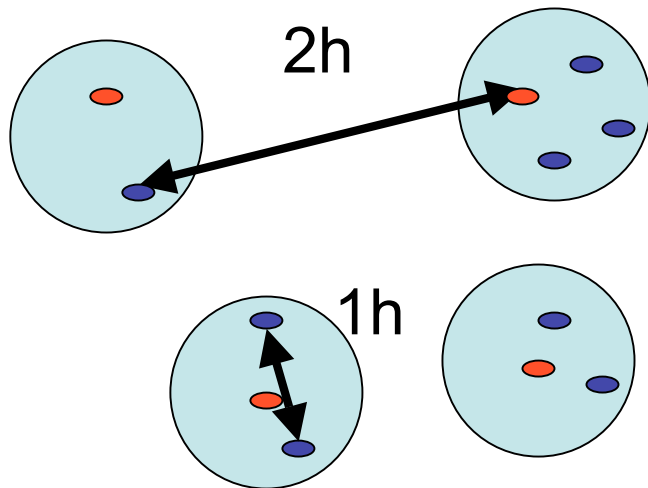


# “bias” can be complicated

Not bias of halos which can be computed from first principles!

- HOD approach ( e.g., Tinker, Zheng, Wechsler...)

Halo model framework



Can HOD be tuned to fit observations?

# Higher-order correlations

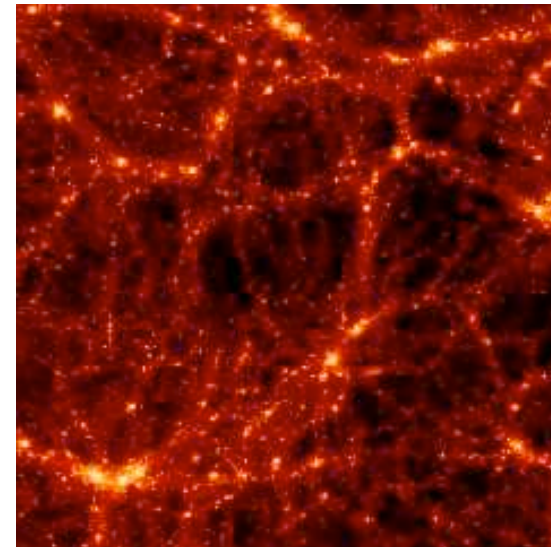
- E.g., Bispectrum or three point function

bias

Initial conditions

Test of gravity

Modeling, error calculations,  
computationally expensive just to compute the signal



# Shot noise and stochasticity

What is shot noise?

Depends on number density

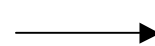
Is it Poisson?

stochasticity

$$\begin{pmatrix} \langle \delta(\mathbf{x})\delta(\mathbf{x}) \rangle & \langle \delta(\mathbf{x})\delta_g(\mathbf{x}) \rangle \\ \langle \delta_g(\mathbf{x})\delta(\mathbf{x}) \rangle & \langle \delta_g(\mathbf{x})\delta_g(\mathbf{x}) \rangle \end{pmatrix} = \langle |\delta_{\text{mass}}(\mathbf{x})|^2 \rangle \begin{pmatrix} 1 & br \\ br & b^2 \end{pmatrix}$$

Could be more complicated

Local mass and momentum conservation



Optimal weighting

So far only for halos and in simulations

# Imperfect observations

- Missing galaxies
- Redshift errors
- Only photometry



Beyond the interest of most of the audience



# NEUTRINOS: Physical effects

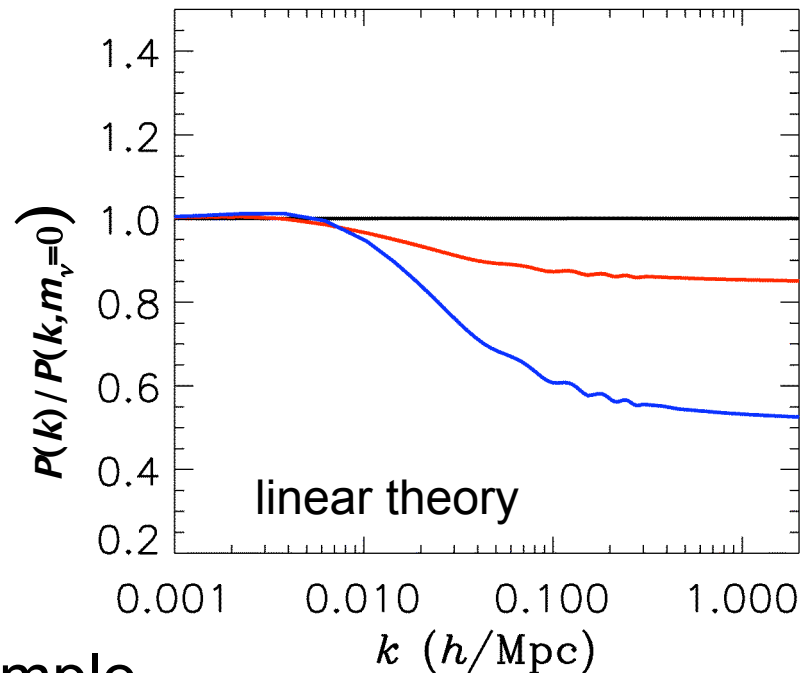
Total mass  $> \sim 1$  eV become non relativistic before recombination CMB

Total mass  $< \sim 1$  eV become non relativistic after recombination:  
alters matter-radiation equality but effect can be “cancelled”  
by other parameters

Degeneracy

After recombination

FINITE NEUTRINO MASSES  
SUPPRESS THE MATTER POWER  
SPECTRUM ON SCALES SMALLER  
THAN THE FREE-STREAMING  
LENGTH



$\Sigma m = 0$  eV

$\Sigma m = 0.3$  eV

$\Sigma m = 1$  eV

Discussion: worked example

C. Peña-G.

# Clusters of galaxies

- Easier to identify clusters of galaxies with DM halos
- Left with 2h term
- If mass can be measured then bias is known (work from >20yrs ago)
- Extra bonus: number density

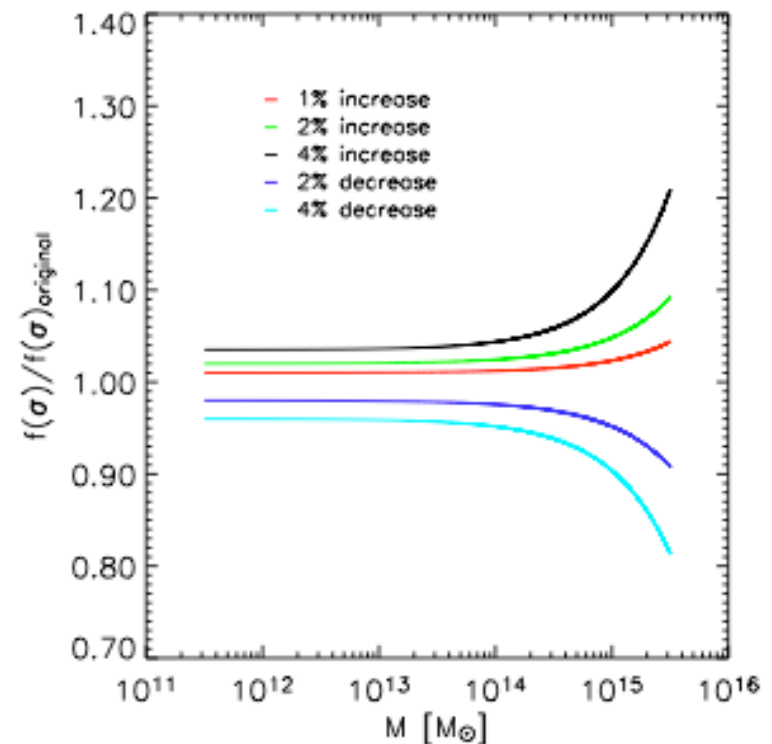
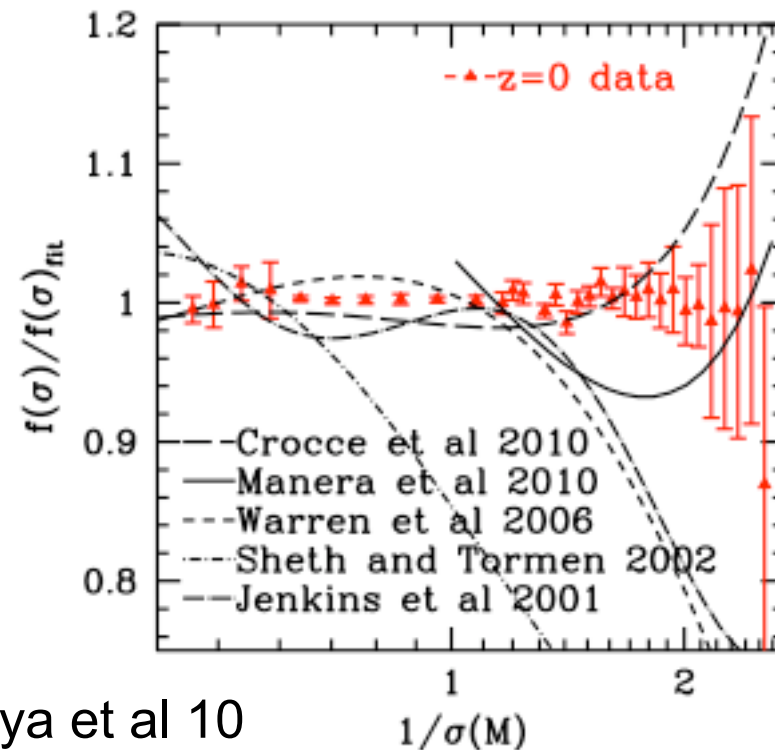


FIG. 1.— Sensitivity of the mass to systematic shifts in individual halo masses. Changes in the mass function are shown with respect to the baseline

# Clusters of galaxies open issues

- Ideally need a mass-limited sample: how?
- SZ surveys promised this but...
- What mass function?



Bhattacharya et al 10

# Halo bias

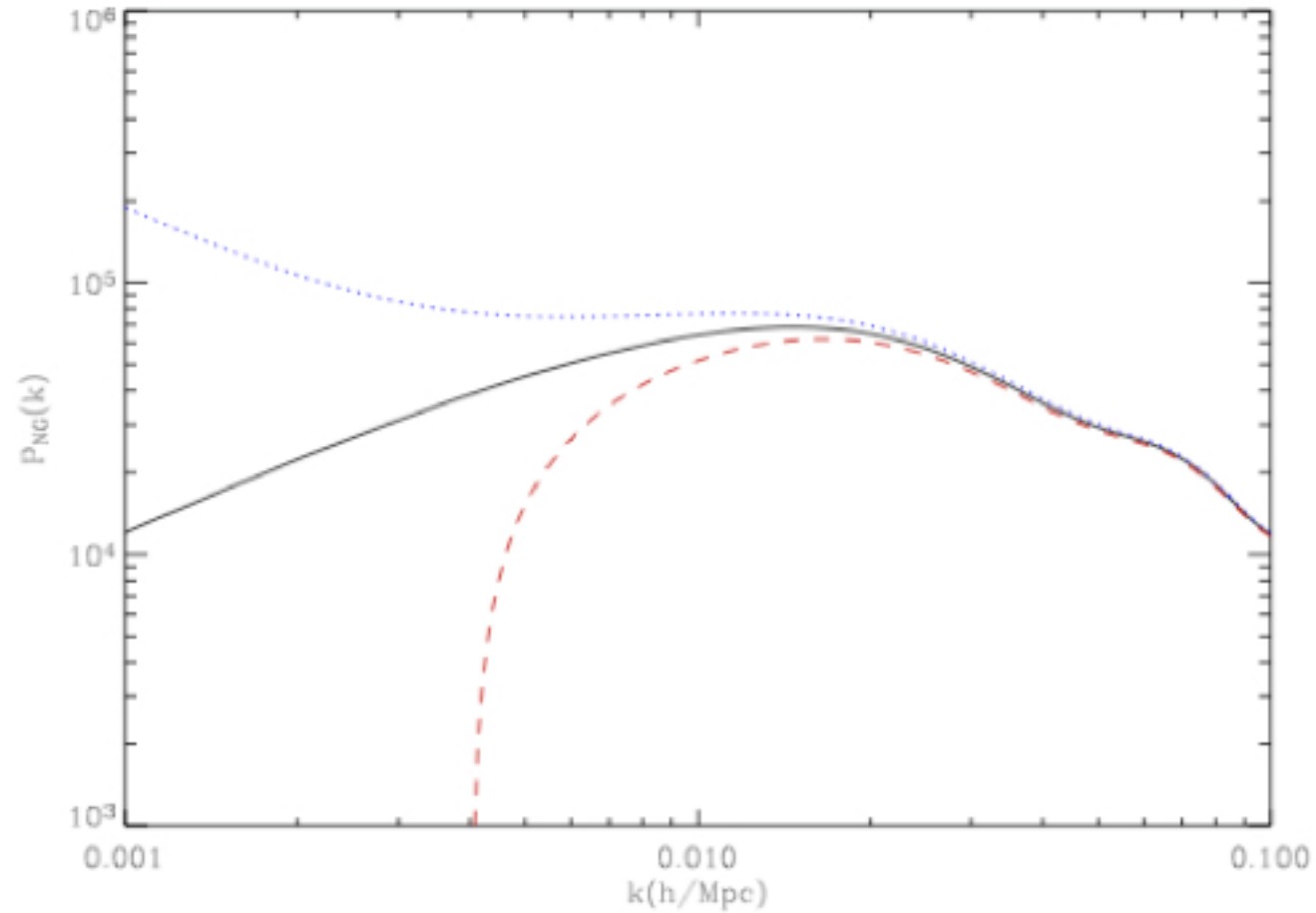
- A Gaussian field and a non-Gaussian field can have the same  $P(k)$
- In a Gaussian field the  $P(k)$  of peaks is completely specified by the  $P(k)$
- In a non-Gaussian field, however, the  $P(k)$  of the **peaks**, depends on all higher order correlations (i.e.  $f_{NL}$ )



# Non-Gaussian halo bias

- Gaussian IC and a non-Gaussian IC can have the same  $P(k)$  for the dark matter
- For Gaussian IC the  $P(k)$  of massive halos is completely specified by the dark matter  $P(k)$
- For Non Gaussian IC, however, the  $P(k)$  of the halos, depends on all higher order correlations (i.e.  $f_{NL}$ )

# The effect



$|f_{NL}|=50, z=0, M > 1.3 \times 10^{13} M_{\text{Sun}}$

# Extremely promising

survey	z range	sq deg	mean galaxy density $(h/Mpc)^3$	$\Delta f_{NL}/q'$ LSS
SDSS LRG's	$0.16 < z < 0.47$	$7.6 \times 10^3$	$1.36 \times 10^{-4}$	40
BOSS	$0 < z < 0.7$	$10^4$	$2.66 \times 10^{-4}$	18
WF MOS low z	$0.5 < z < 1.3$	$2 \times 10^3$	$4.88 \times 10^{-4}$	15
WF MOS high z	$2.3 < z < 3.3$	$3 \times 10^2$	$4.55 \times 10^{-4}$	17
ADEPT	$1 < z < 2$	$2.8 \times 10^4$	$9.37 \times 10^{-4}$	1.5
EUCLID	$0 < z < 2$	$2 \times 10^4$	$1.56 \times 10^{-3}$	1.7
DES	$0.2 < z < 1.3$	$5 \times 10^3$	$1.85 \times 10^{-3}$	8
PanSTARRS	$0 < z < 1.2$	$3 \times 10^4$	$1.72 \times 10^{-3}$	3.5
LSST	$0.3 < z < 3.6$	$3 \times 10^4$	$2.77 \times 10^{-3}$	0.7

Carbone, et al 08 & 09

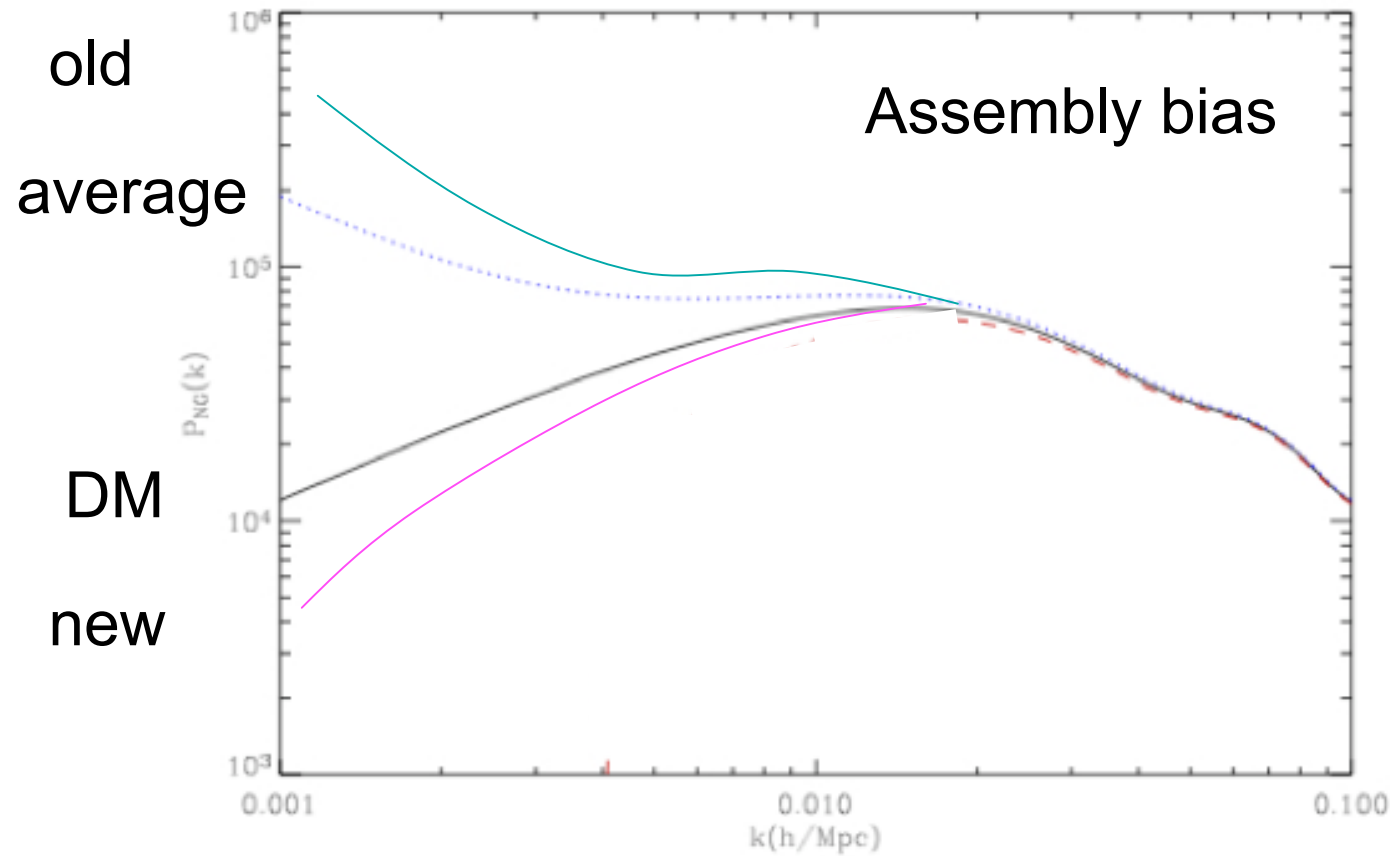
## Open issues:

This is for the LOCAL shape, what about other shapes?

Simulations are key to calibrate the analytics,  
can we simulate this?

Can shapes be distinguished?

# Open issues



Effect of survey window.  
Hints from current data (Matarrese)

# What about the mass function (halos or voids)

Issues: what mass function? (LoVerde, Norena)

What non-gaussianity? (LoVerde)

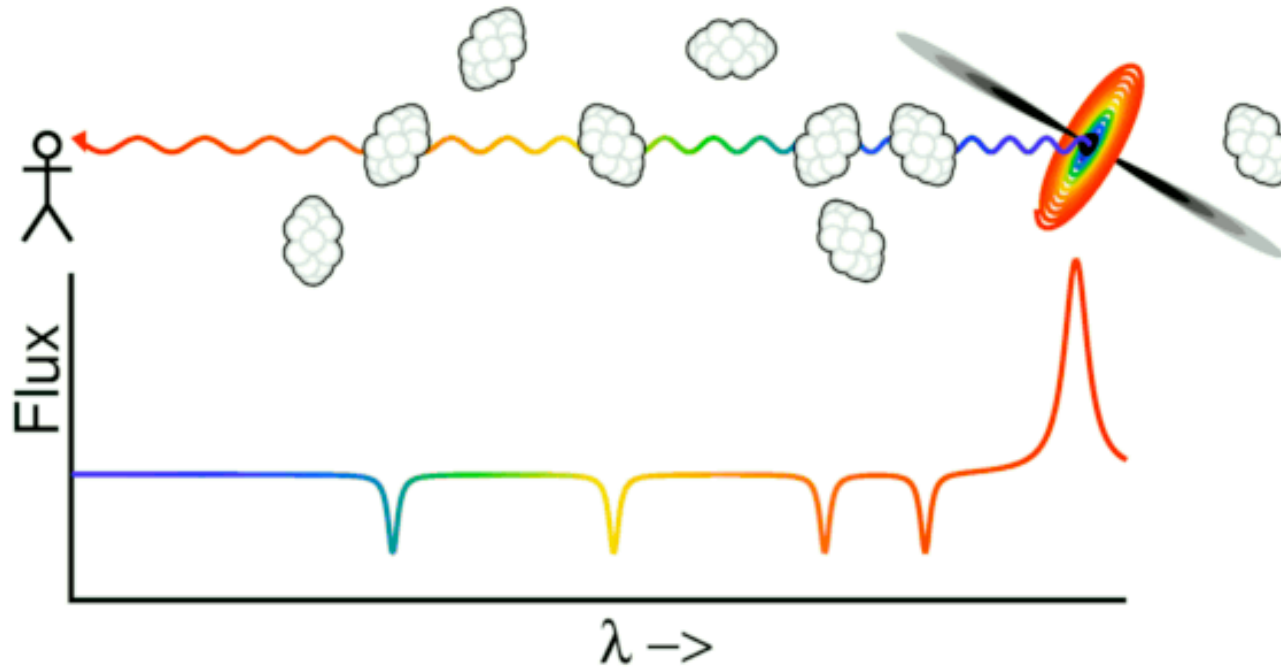
What halo masses? (Hoyle)

Hints from current data... (Hoyle)



# Lyman alpha forest

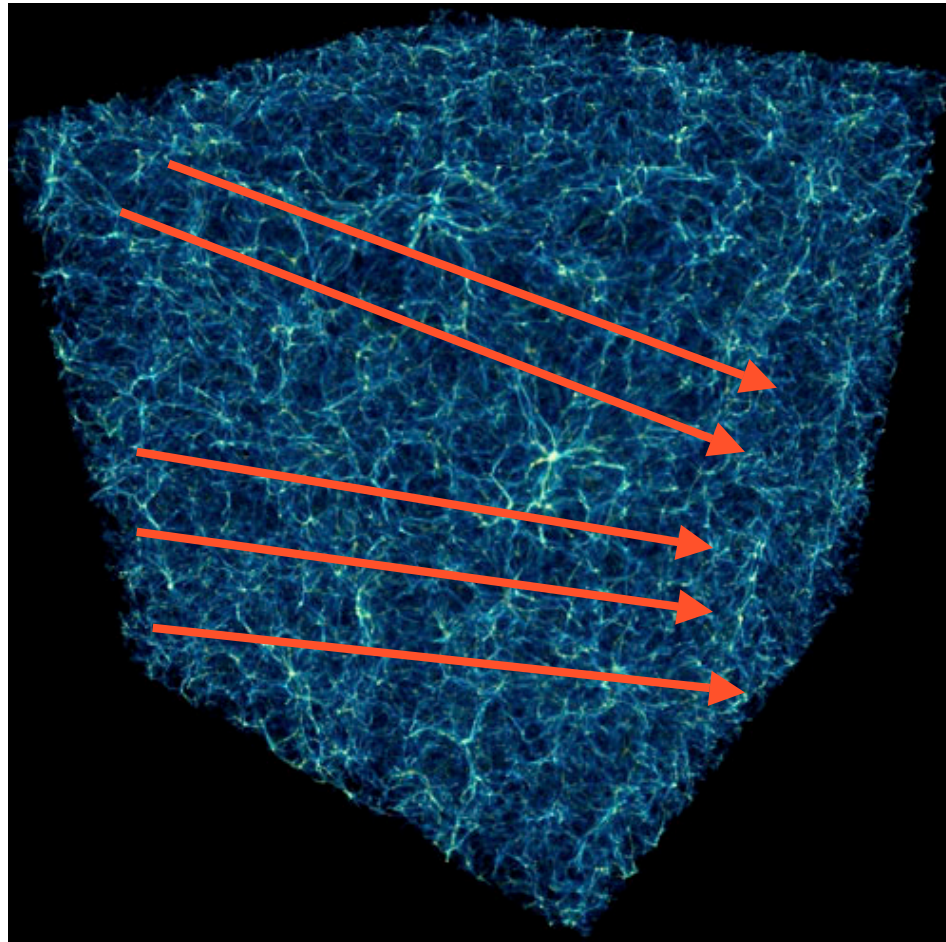
Lyman alpha line of hydrogen at a wavelength of 122 [nm](#).



One sightline: 1D info

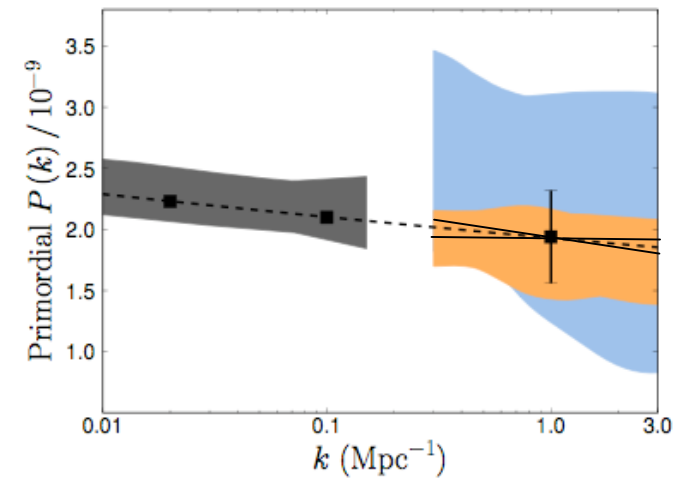
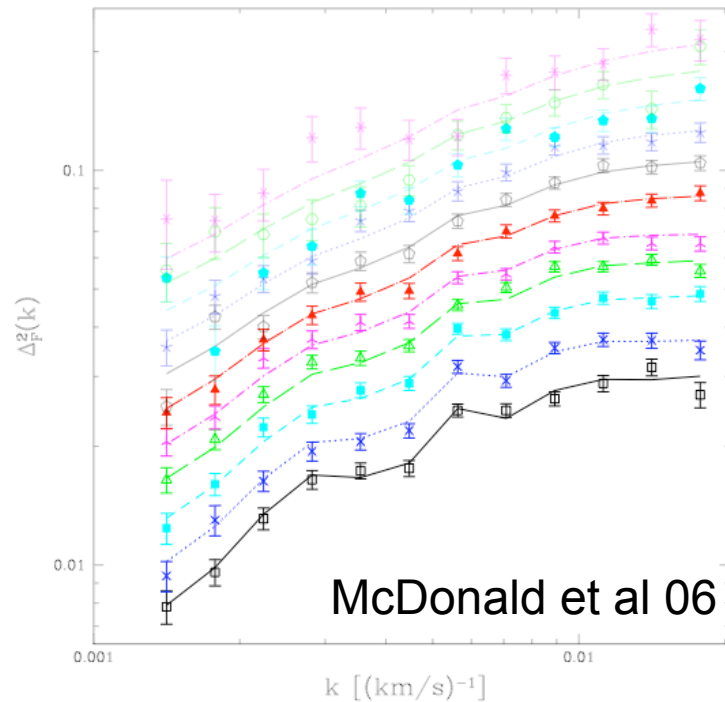
# Lyman alpha forest

Getting 3D info



# Lyman alpha: So far

- 1D info
- Small scales !!!
- High z still (almost) linear



Bird et al 2010

# Complications

(work in progress)

From gas density to flux and effect of peculiar velocity

Reminds you of bias



Rely heavily on simulations this time not DM only:  
hydrodynamical. Still assumptions must be made about  
ionization, IGM thermal history etc.

Back to the problem of how to interpolate between simulations

Open issues: it has not been done before!

Huge effort in SDSS3 Lyman alpha working group (J. Miralda)

# Where LSS competitive?

- Dark energy
- DE vs tests of Gravity
- Neutrino properties
- Shape of the primordial power spectrum
- Primordial NG



# On-going planned surveys

- SDSS3 (BOSS)
- DES
- EUCLID
- BigBoss
- Hetdex
- WFIRST
- Etc...



# Open issues recap

- What are we really measuring? (and modeling?)
- Non-linearities, (analytical and numerical tools)
- Fourier space, real space, Sph Harm,...?
- Error-estimation
- Bias (galaxy formation)
- Velocity, reconstruction?
- Stochasticity
- What to simulate, how to interpolate
- Worked example: neutrinos
- Non-Gaussian halo bias, shapes? Assembly bias? Sims?  
(Worked example: hints from current data)
- Clusters: mass selected sample? Masses? What mass function?  
(Worked example: hints from high-z clusters)
- Lyman-alpha forest: open issues?