

# Tension in the Void

arXiv:1201.2790

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Modern Cosmology Workshop 2012, Benasque

# Outline

- 1 A-Void Dark Energy
  - The Standard Cosmological Model
  - Inhomogeneous Universes
  
- 2 Observational constraints
  - The BAO scale in LTB universes
  - MCMC analysis
  
- 3) Conclusions

# The Standard Model of Cosmology

Commercial name:  $\Lambda$ CDM<sup>©</sup>

## Ingredients

**GR + FRW + Inflation + SM + CDM +  $\Lambda$**

- Theory of Gravitation: General Relativity
- Ansatz for the metric: Homogeneous + Isotropic
- Initial conditions: Inflationary perturbations
- Standard particle content:  $\gamma$ ,  $\nu$ 's,  $p^+$ ,  $n$ ,  $e^-$
- Cold Dark Matter: some new particle species
- Cosmological constant:  $\Lambda$

# Beyond Homogeneity

Homogeneity + Isotropy  $\rightarrow$  Spherical Symmetry

The Lemaitre-Tolman-Bondi metric

$$ds^2 = -dt^2 + \frac{A'^2(r, t)}{1 - k(r)} dr^2 + A^2(r, t) d\Omega^2$$

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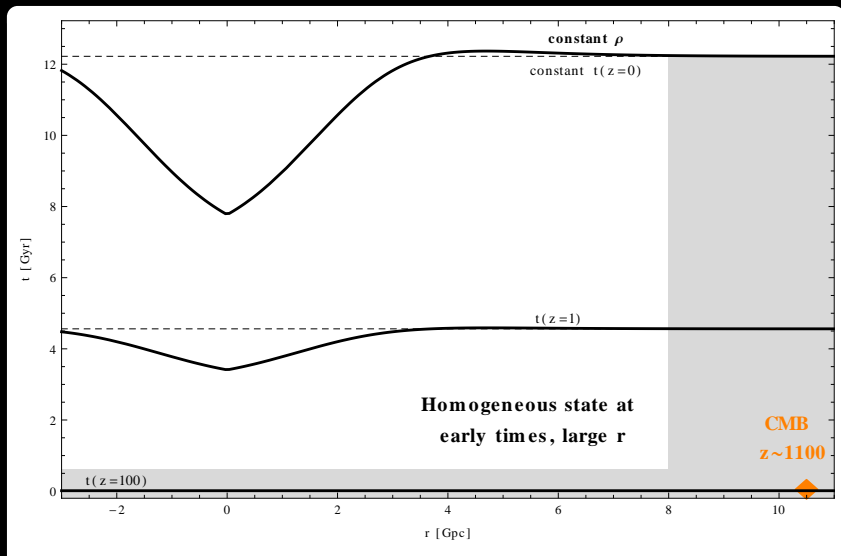
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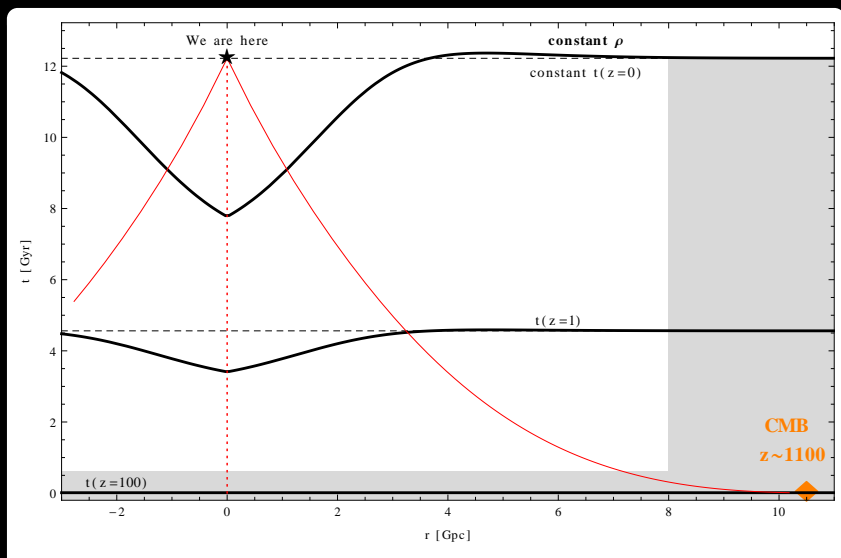
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+  $\rho_b \propto \rho_m \rightarrow$  growth of an spherical adiabatic perturbation

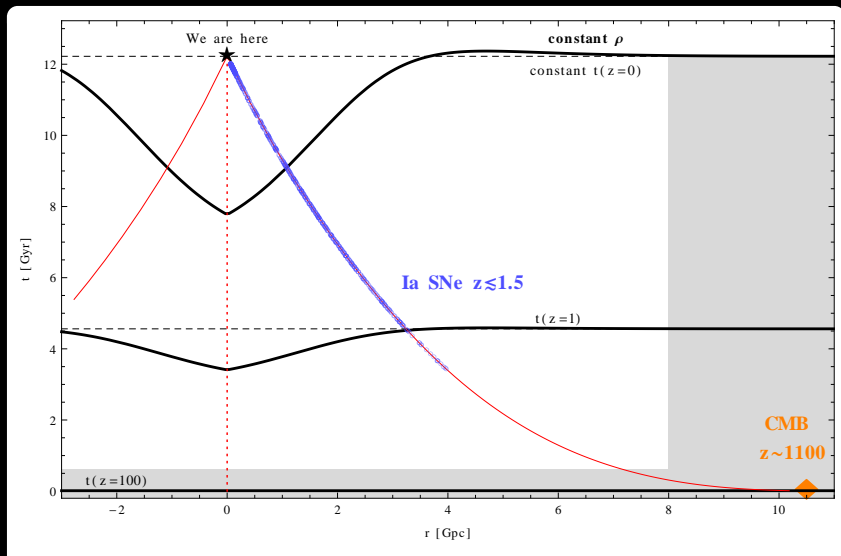
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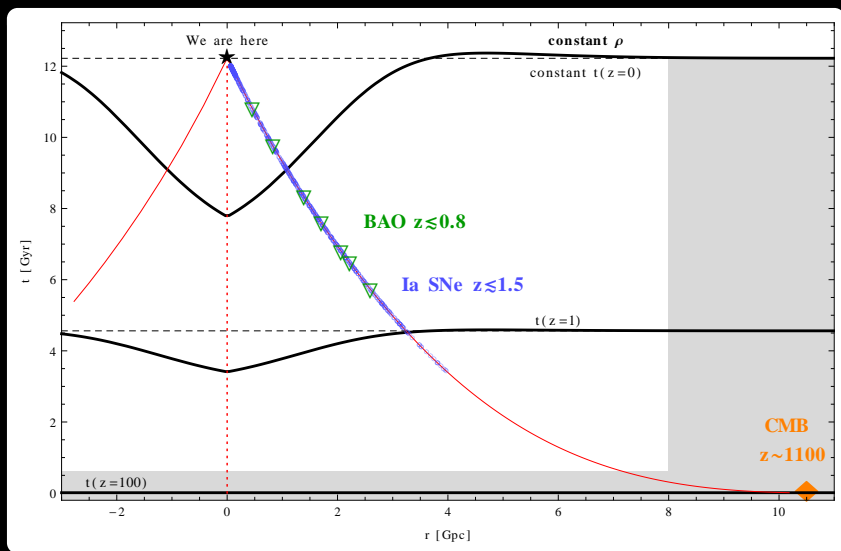
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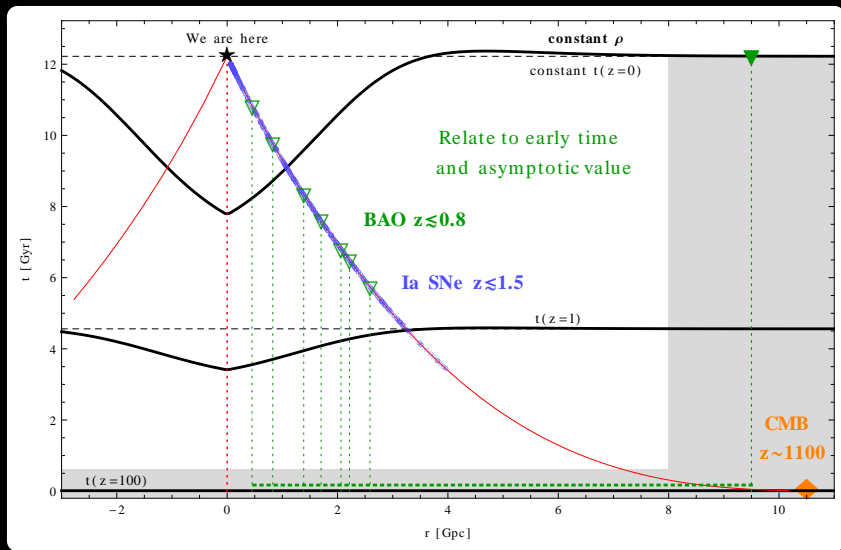
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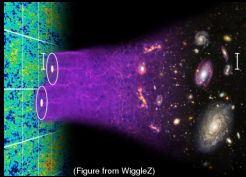
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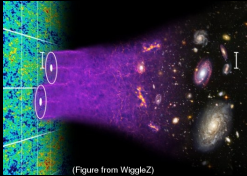


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- Sound waves in the baryon-photon plasma travel a finite distance
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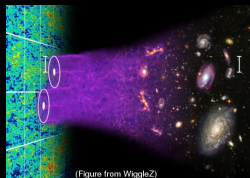


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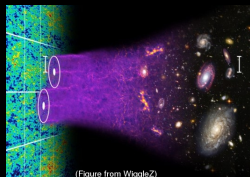
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- Alonso *et al.* 1204.3532: N-body  $\Rightarrow$  locally  $\sim$  FRW w  $\Omega_M(r)$
- February *et al.* 1206.1602: Linear PT  $\Rightarrow \sim 1\%$  shift

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- LTB: evolving ( $t$ ), inhomogeneous ( $r$ ) and anisotropic  $l_T \neq l_R$   
FRW  $\rightarrow$  only time evolution!

# The observed BAO scale

Observations  $\rightarrow$  galaxy correlation in angular and redshift space

Geometric mean  $d \equiv (\delta\theta^2 \delta z)^{1/3}$

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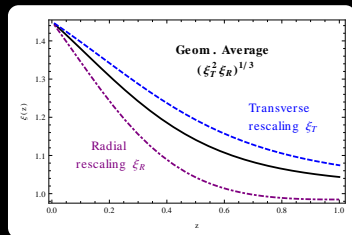
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Different result than FRW

$$d_{\text{LTB}}(z) = \xi(z) d_{\text{FRW}}(z)$$

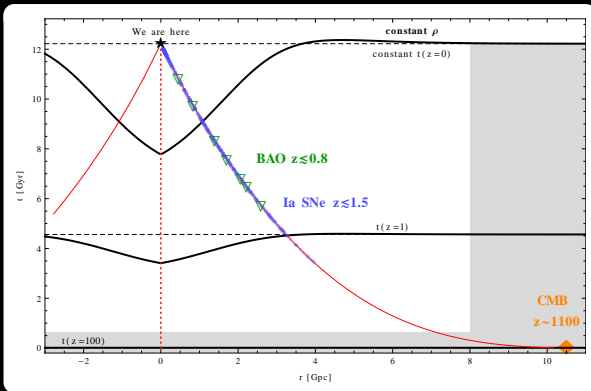
$$\xi(z) = \text{rescaling} = (\xi_T^2 \xi_R)^{1/3}$$

Inhomogeneous, anisotropic



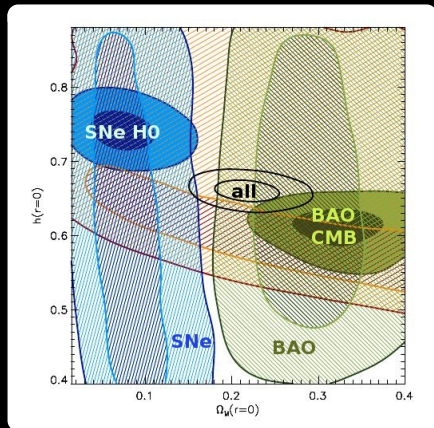


# MCMC data and models



- **GBH profile:**  $\Omega_{in}, \Omega_{out}, R, \Delta R, H_0, f_b$
- **WiggleZ + Carnero *et al.***
- **Union 2 Compilation**
- $H_0 = 73.8 \pm 2.4$   
→ SNe luminosity prior
- **CMB peaks information (simplified analysis)**

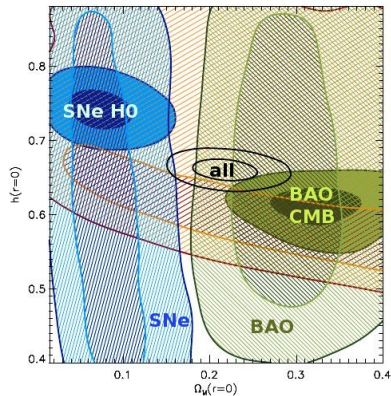
Adiabatic LTB models:  $\Omega_{out} = 1$  and open  $\Omega_{out} \leq 1$

Adiabatic GBH, asympt. flat  $\Omega_{\text{out}} = 1$ Filled: **SNe+H0**, **BAO+CMB**, Dashed: **BAO**, **CMB peaks**, **Supernovae**

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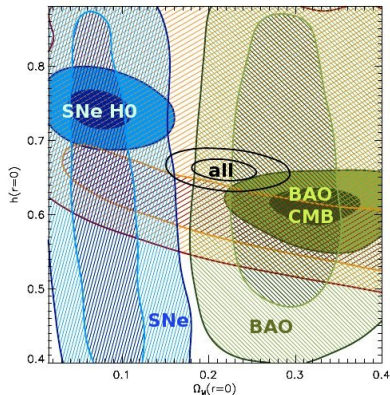
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known, worse if full CMB used



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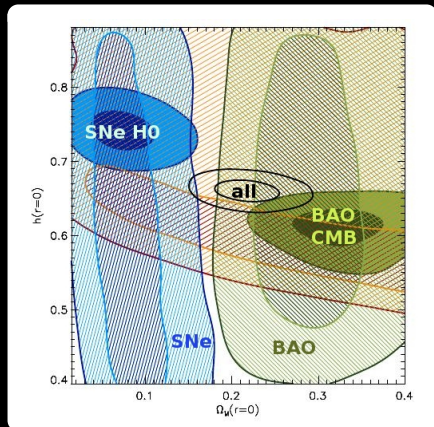
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Do asymptotically open models work better?

Adiabatic GBH, asympt. open  $\Omega_{\text{out}} = 1$   $\Omega_{\text{out}} \leq 1$

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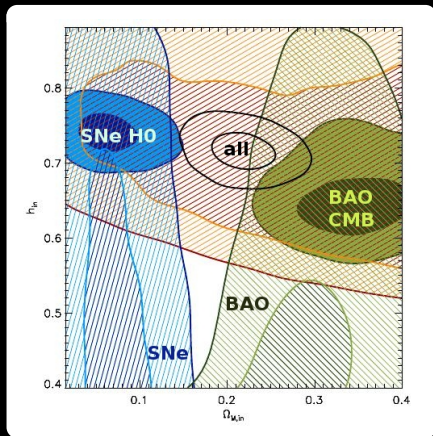
Still  $3\sigma$  Away!!!

Local Expansion Rate:

$$\Omega_{\text{out}} \approx 0.85 \leftrightarrow \text{higher } H_{\text{in}}$$

$$t_0 \propto 1/H_{\text{in}} \rightarrow t_0 \lesssim 12\text{Gyr}$$

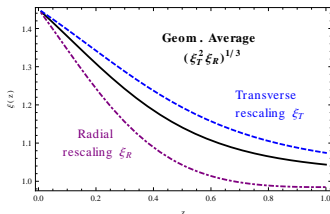
Only better  $H_0$ , but Universe too young



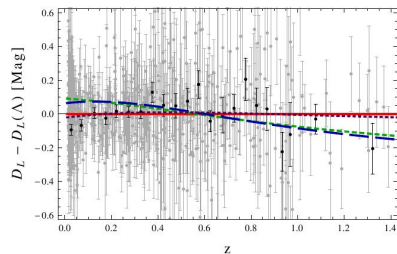
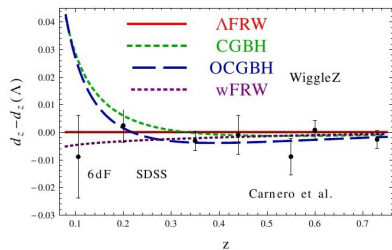
# Best fit models

## Tension in the Void

- Bad fit to SNe and BAO
- SNe measure distance  
BAO: distance+rescaling  
complementary probes
- Strongly ruled out



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Tension in the Void

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- Purely geometrical result, whatever Luminosity & BAO scale  $\Rightarrow$  Standard Rulers vs Standard Candles
- BAO are a powerful complement to SNe in more *general* inhomogeneous models

# Backup Slides

# Supernova Ia - Standard Candles

- **Standardizable Candles:**  $\approx$  Same (corrected) Luminosity

$$D_L(z) = \sqrt{\frac{\text{Luminosity}}{4\pi \text{ Flux}}} = H_0^{-1} f(z, \Omega_\Lambda, \Omega_M) \text{ (FRW)}$$

difficult to model SNe  $\Rightarrow$  Intrinsic Luminosity unknown!!

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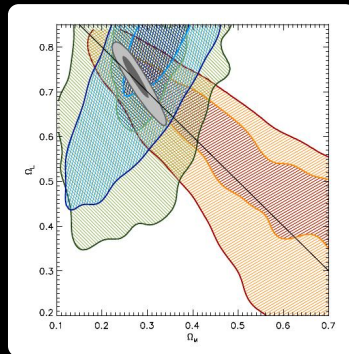
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- In LTB not quite true  $\Rightarrow$  convert constraint

$$H_0 = 73.8 \pm 2.4 \text{ Mpc/Km/s} \leftrightarrow L = -0.120 \pm 0.071 \text{ Mag}$$

# MCMC: FRW- $\Lambda$ CDM reference model

Using **BAO scale**, **CMB peaks**, **Supernovae** and  $H_0 + \text{BAO} + \text{CMB} + \text{SNe}$

- BAO  $\sim$  SNe: Arbitrary length/luminosity (before adding CMB/ $H_0$ )
- CMB constraints much weaker than usual  
 $1 - \Omega_k \lesssim 1\%$



$\Rightarrow$  don't take our CMB constraints too seriously