

Raman characterization of graphene-based materials

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FAPEMIG



Raman characterization of graphene-based materials:

- Defect density
- Number of layers and stacking order
- Doping
- Strain
- Twist angle in superlattices

Raman spectrum of graphene:

One-phonon Raman bands:

$$\vec{k}_S = \vec{k}_0 - \vec{q}$$

$$q \sim 0$$

Two-phonon Raman bands:

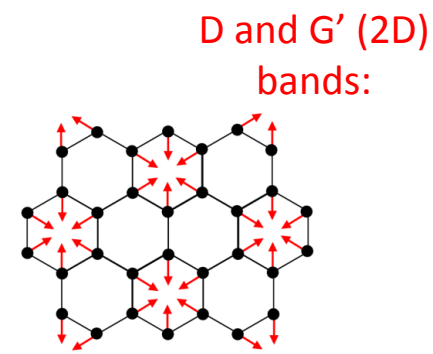
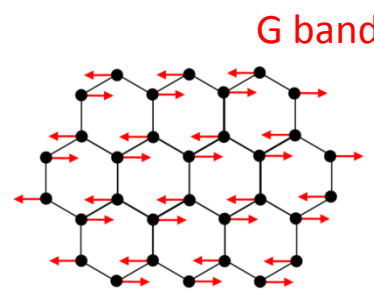
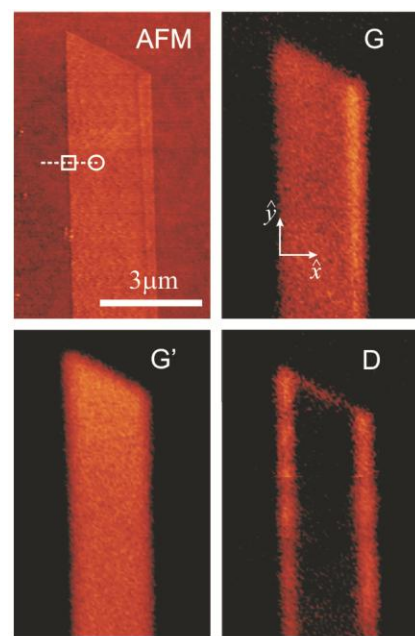
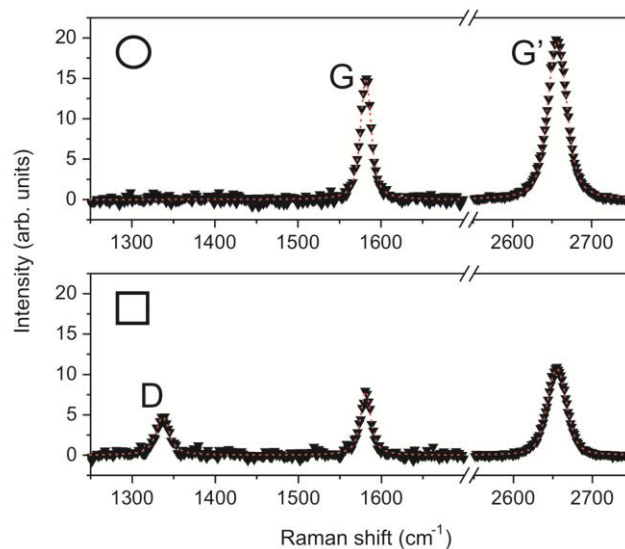
$$\vec{k}_S = \vec{k}_0 - \vec{q}_a - \vec{q}_b$$

$$\vec{q}_a \sim -\vec{q}_b$$

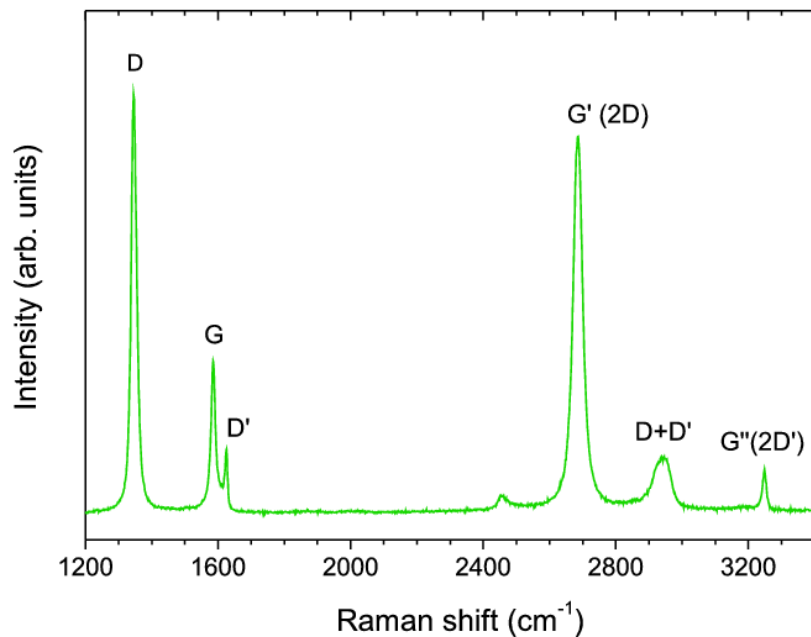
Disorder-induced one-phonon Raman bands:

$$\vec{k}_S = \vec{k}_0 - \vec{q} - \vec{d}$$

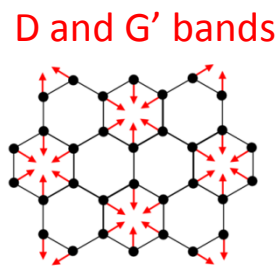
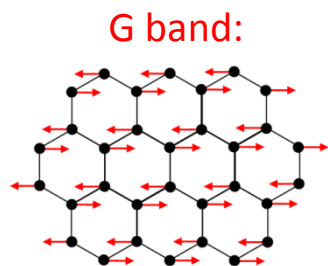
$$\vec{q} \sim -\vec{d}$$



Raman spectrum of graphene:



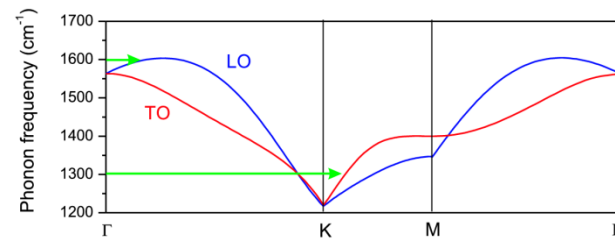
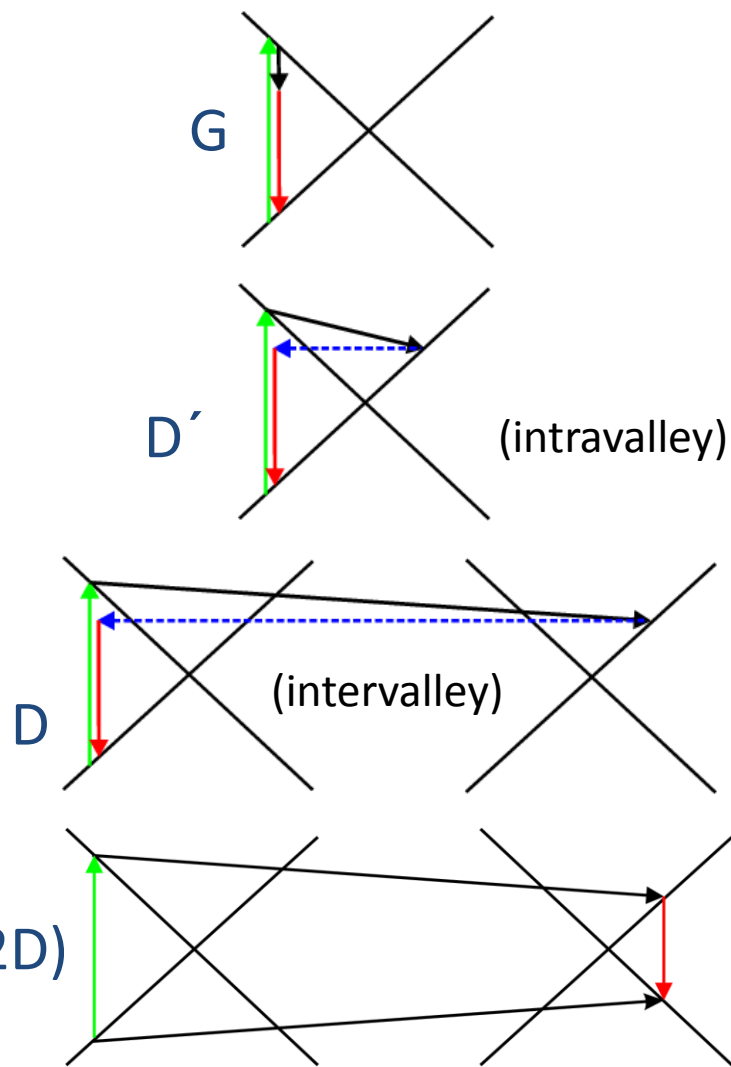
Tuinstra and Koenig. *J. Phys. Chem.* **53**, 1126 (1970).



Thomsen and Reich, *PRL* **85**, 5214 (2000).

Saito et al., *PRL* **88**, 027401 (2002).

Venezuela, Lazzeri, and Mauri, *PRB* **84**, 035433 (2011).



Ion bombarded graphene

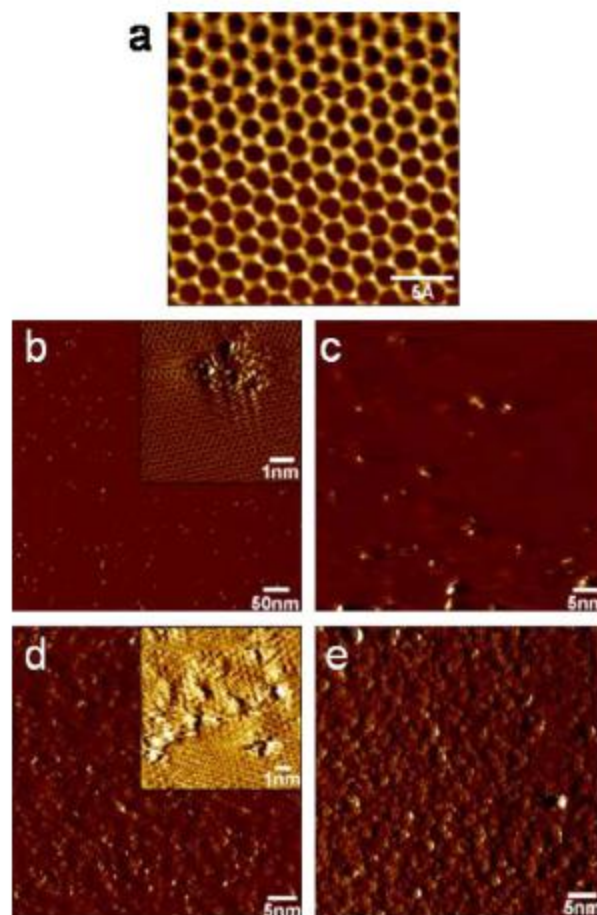
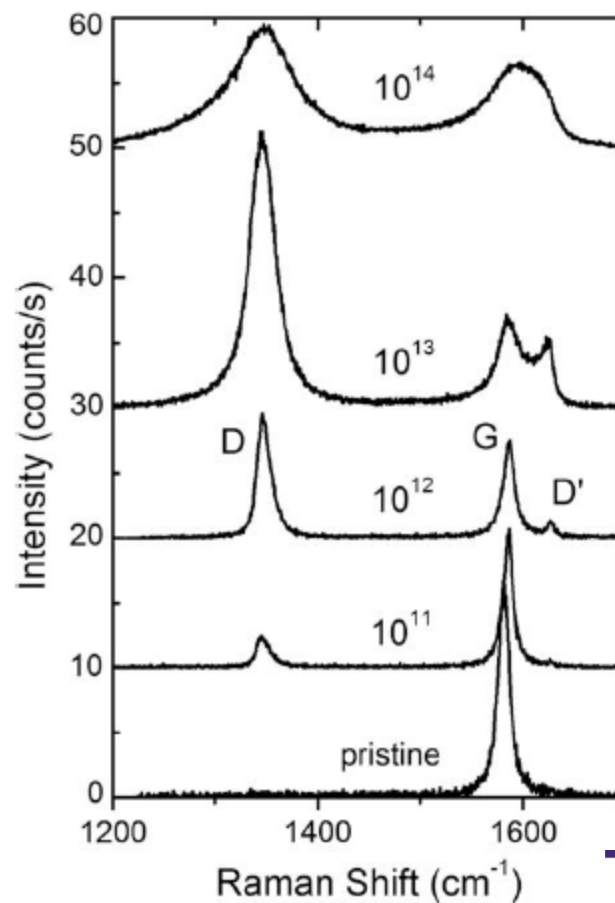
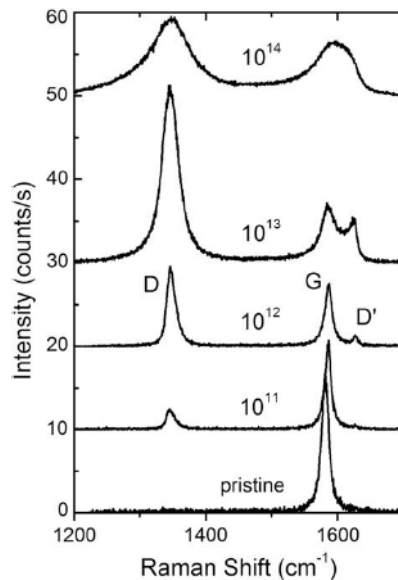
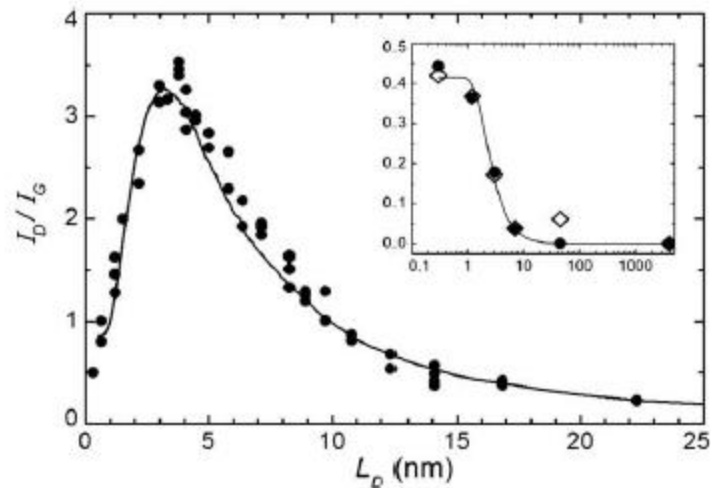
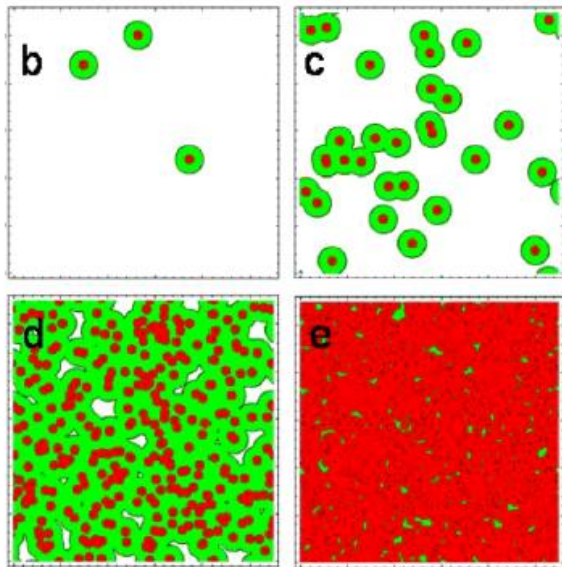
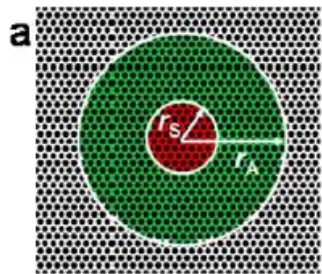


Fig. 1 - STM images of the surface of a bulk HOPG sample subjected to 90 eV Ar⁺ ion bombardment. From (a-e) the panels display results at zero, 10¹¹, 10¹², 10¹³ and 10¹⁴ Ar⁺/cm² ion doses. Insets to (b) and (d) show the detailed atomic structure of the defective areas at their respective ion doses.





$$C_A = 4.56$$

$$C_S = 0.86$$

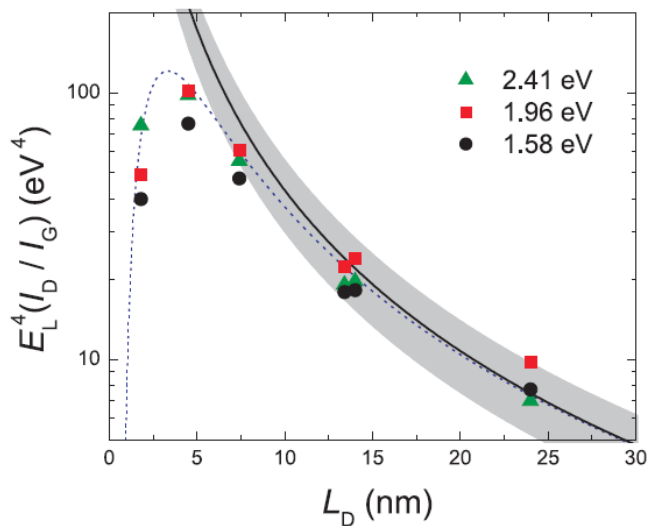
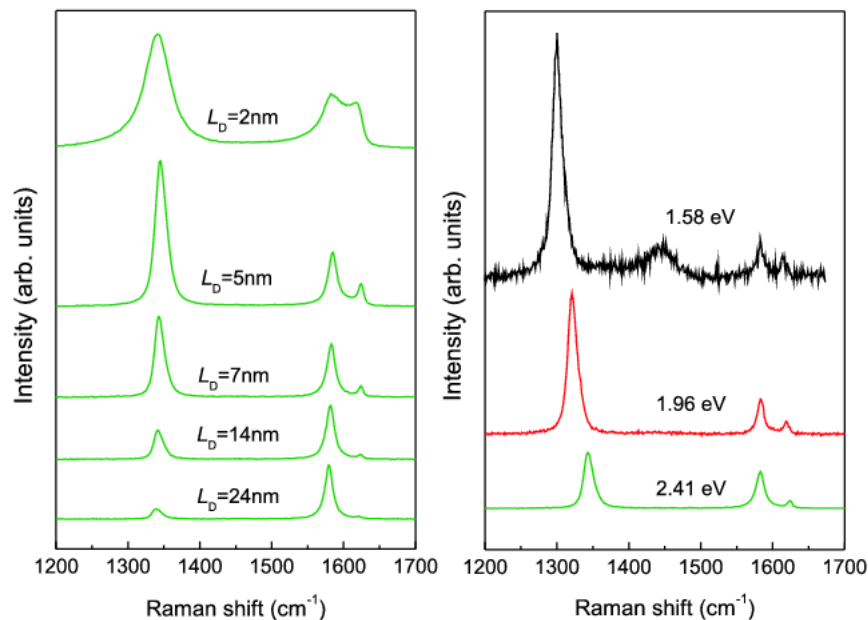
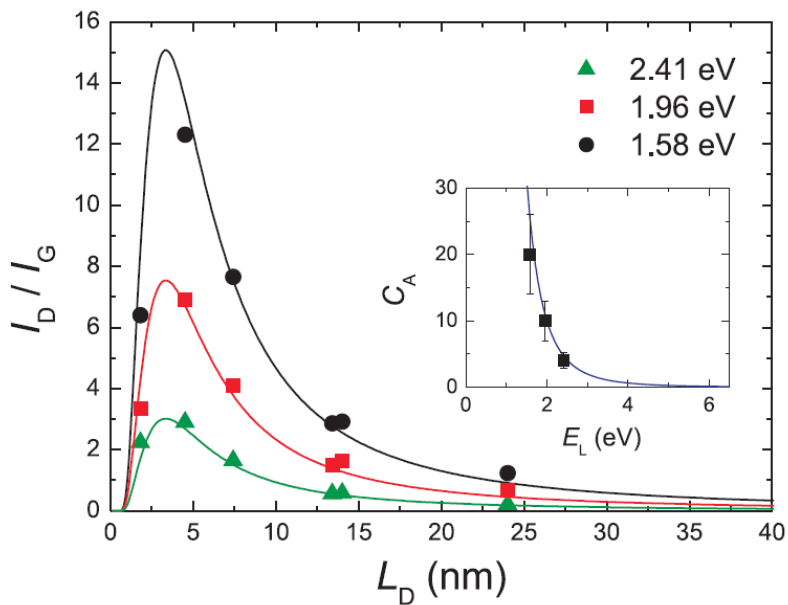
$$r_A = 3 \text{ nm}$$

$$r_S = 1 \text{ nm}$$

$$I_D/I_G = C_A \frac{r_A^2 - r_S^2}{r_A^2 - 2r_S^2} [\exp(-\pi r_S^2/L_D^2) - \exp(-\pi(r_A^2 - r_S^2)/L_D^2)] + C_S [1 - \exp(-\pi r_S^2/L_D^2)]$$

Lucchese et al., Carbon, 48(5), 1592 (2010).

Quantifying defects in graphene by Raman spectroscopy using different excitation laser energies



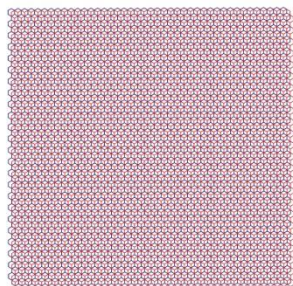
$$L_D^2 (\text{nm}^2) = \frac{(4.3 \pm 1.3) \times 10^3}{E_L^4} \left(\frac{I_D}{I_G} \right)^{-1}$$

$$n_D (\text{cm}^{-2}) = (7.3 \pm 2.2) \times 10^9 E_L^4 \left(\frac{I_D}{I_G} \right)$$

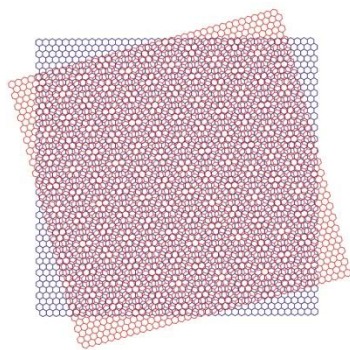
Cançado et al., Nano Lett. 11(8), 3190 (2011).

Graphene superlattices: Moiré patterns

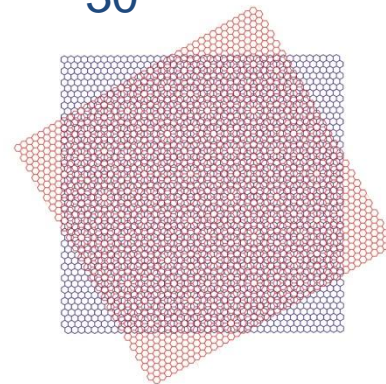
0°, 60°



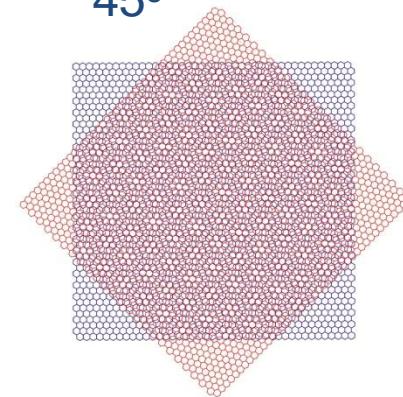
15°



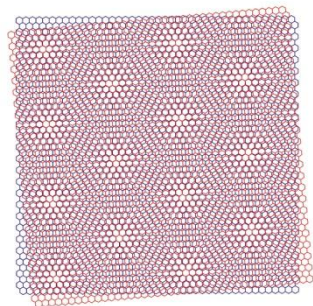
30°



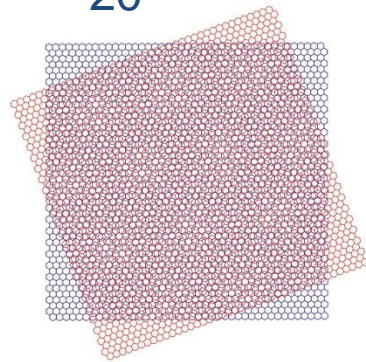
45°



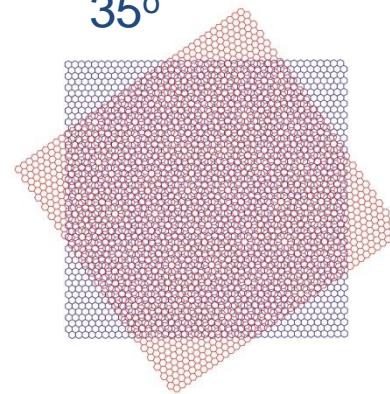
5°



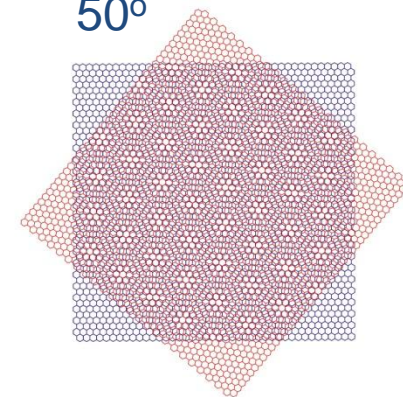
20°



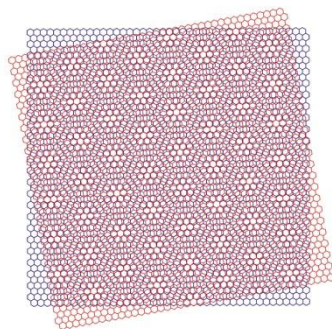
35°



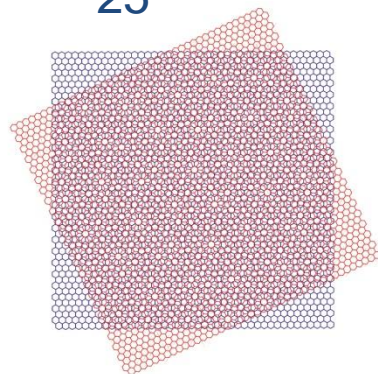
50°



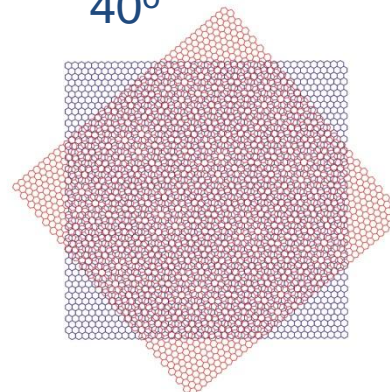
10°



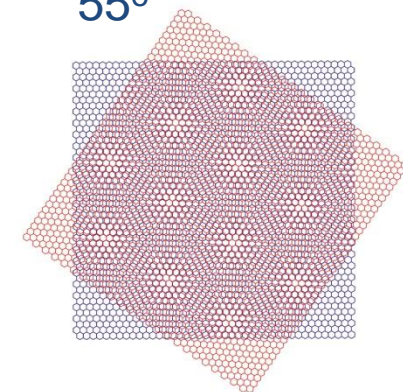
25°



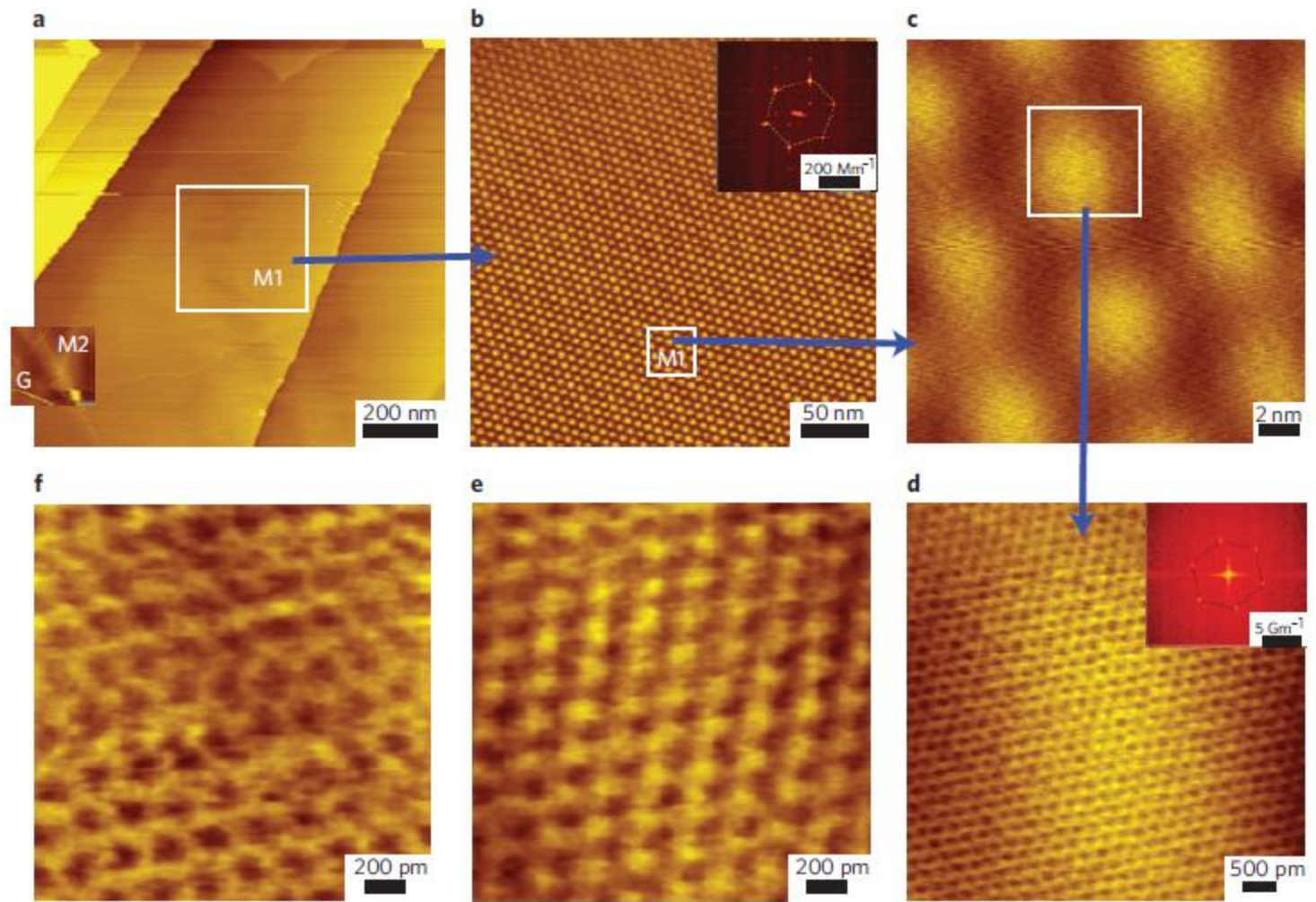
40°

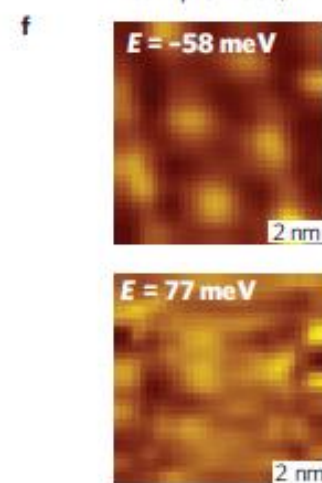
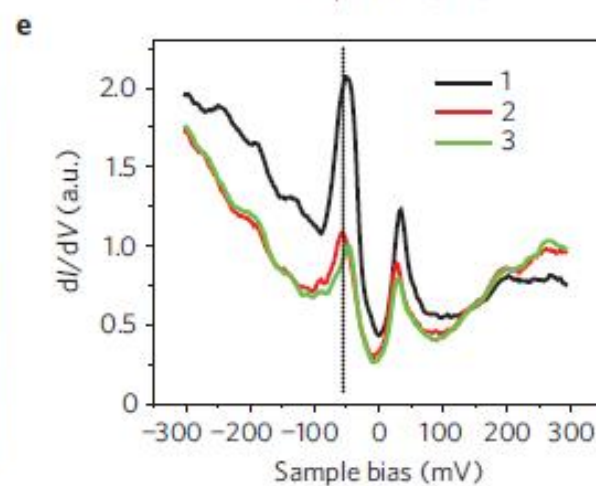
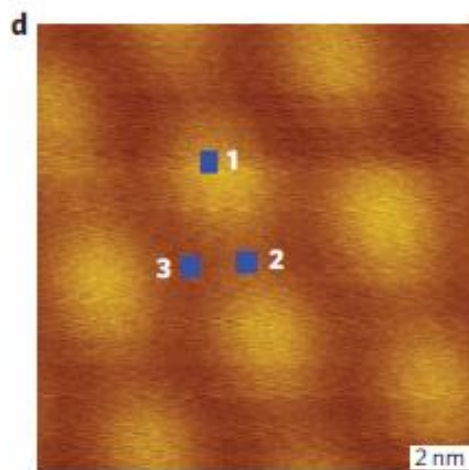
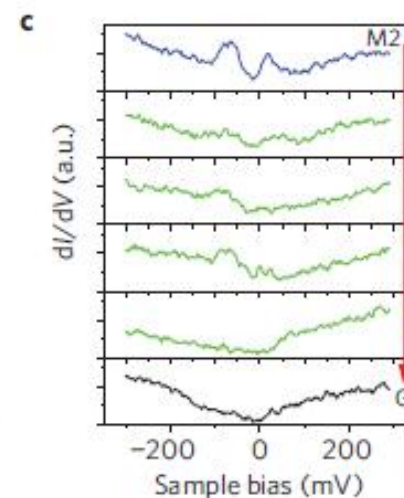
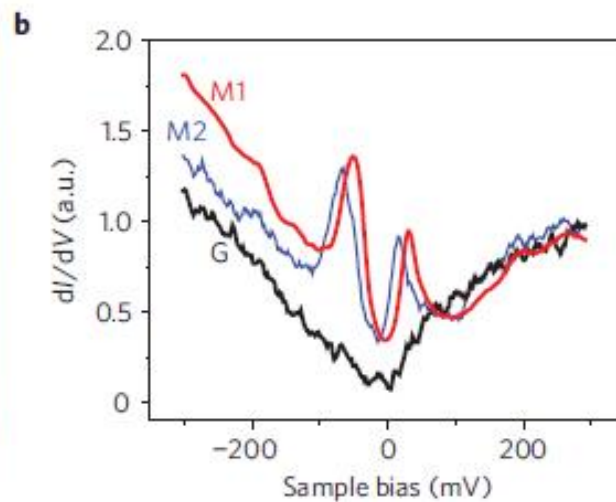
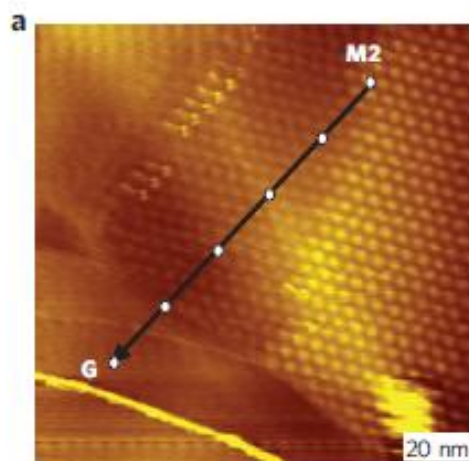


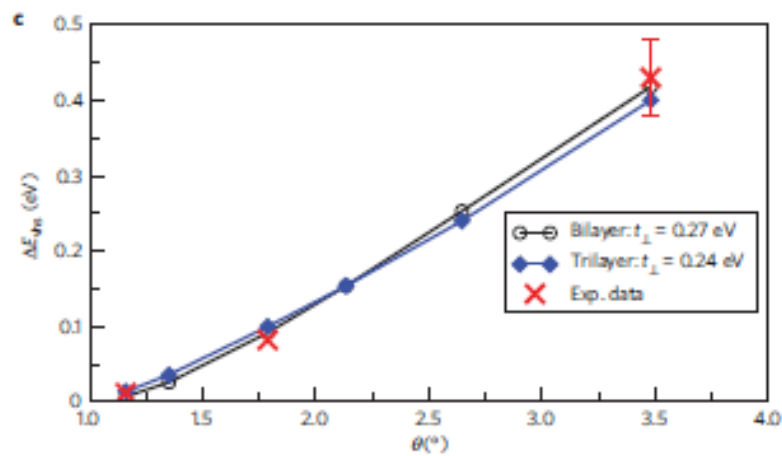
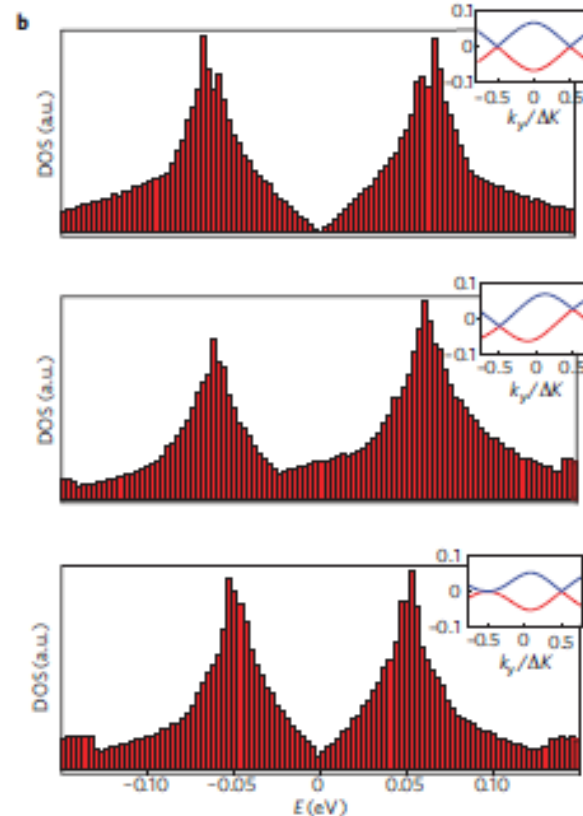
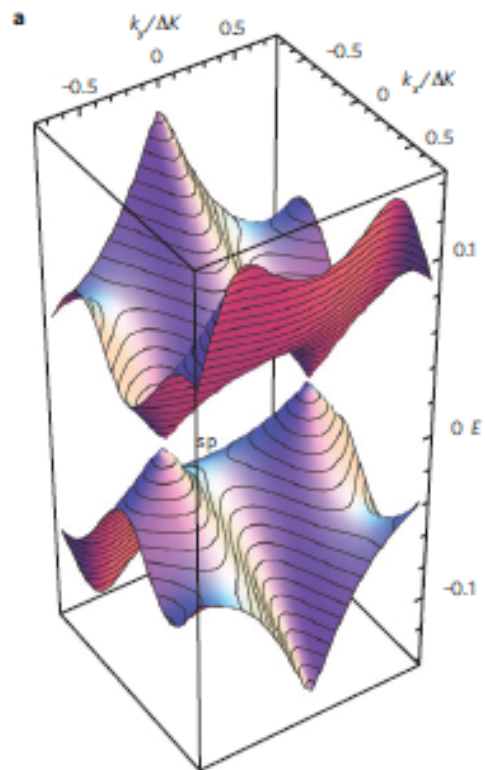
55°



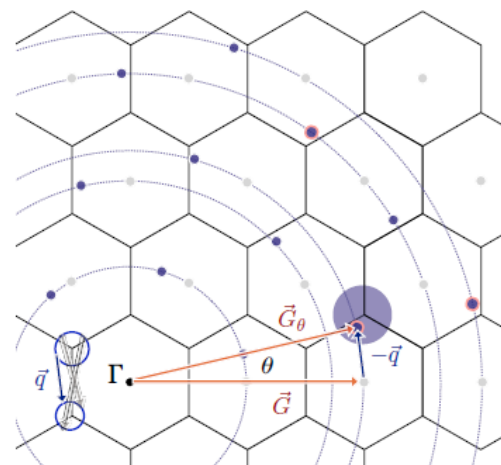
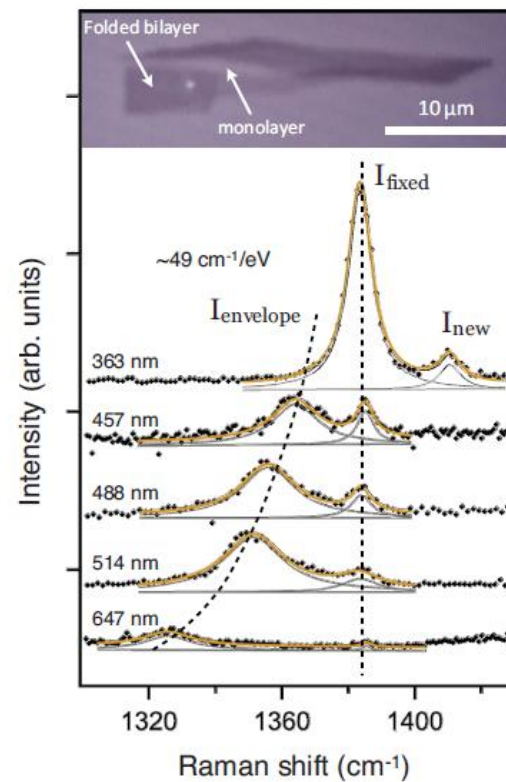
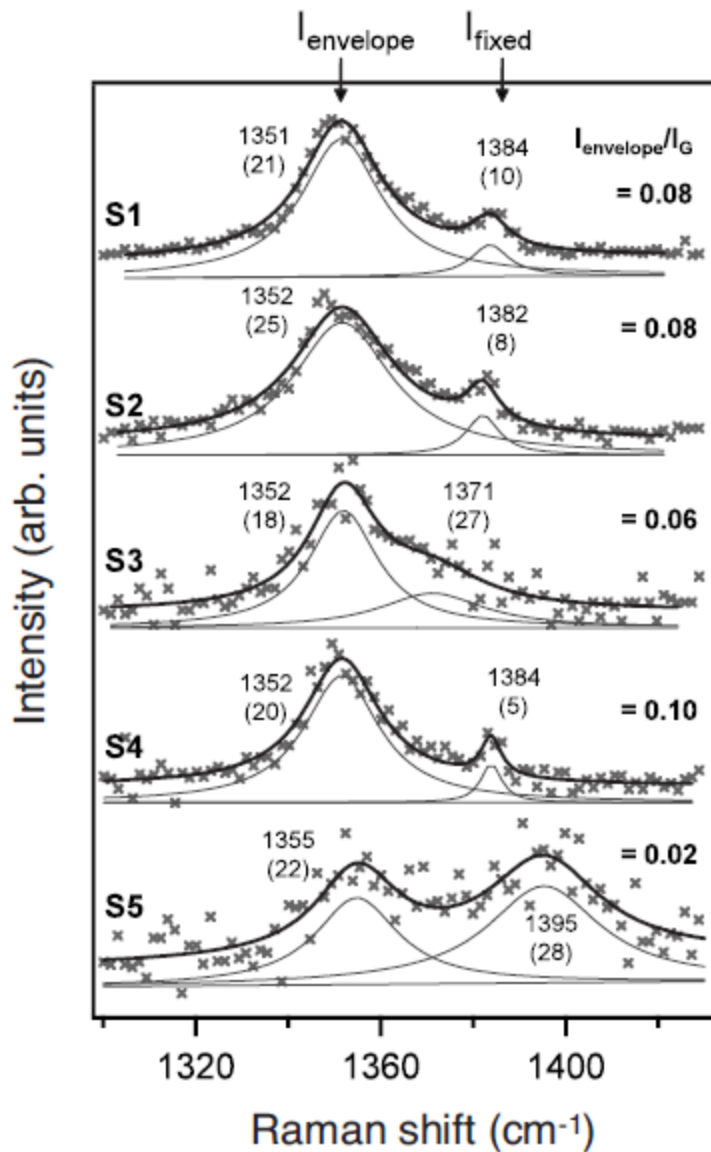
STM measurements



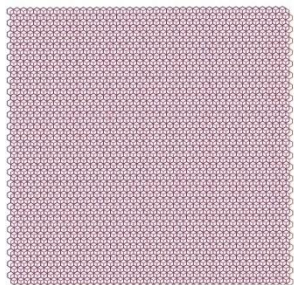




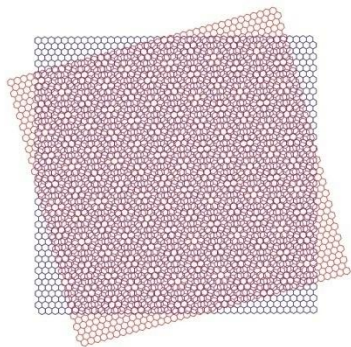
Raman spectrum of folded graphene:



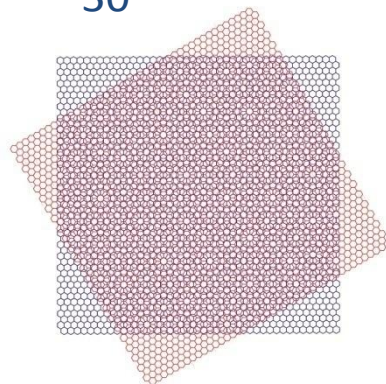
0°, 60°



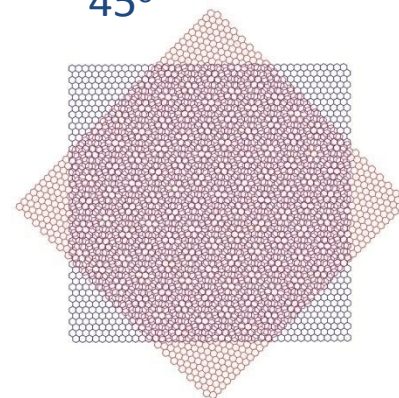
15°



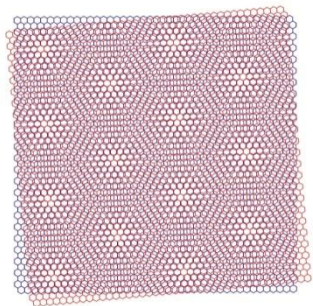
30°



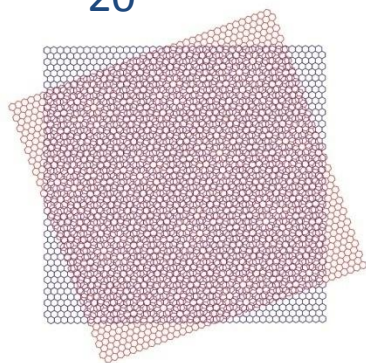
45°



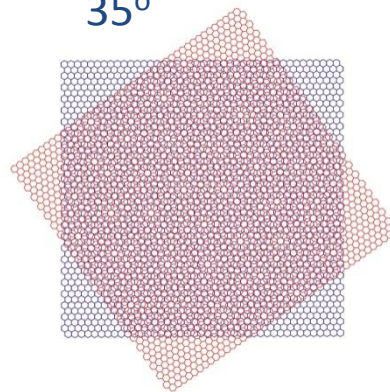
5°



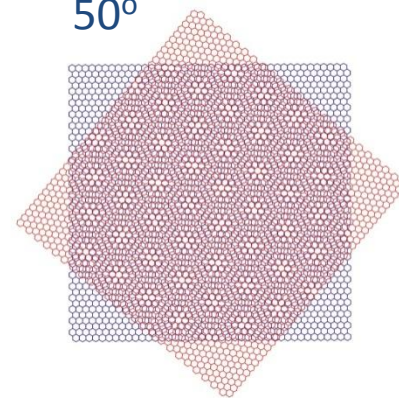
20°



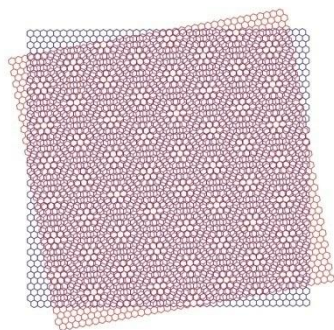
35°



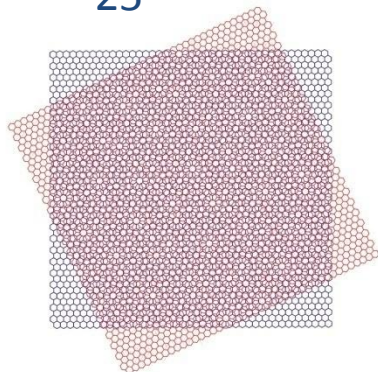
50°



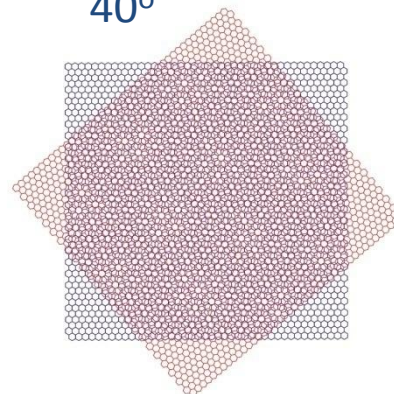
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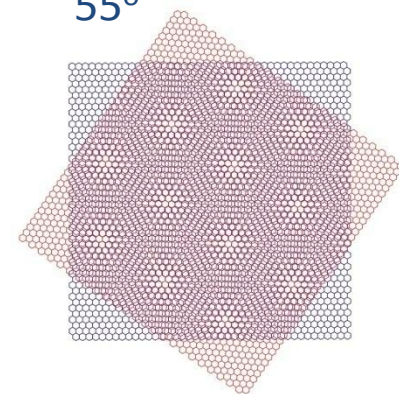
25°

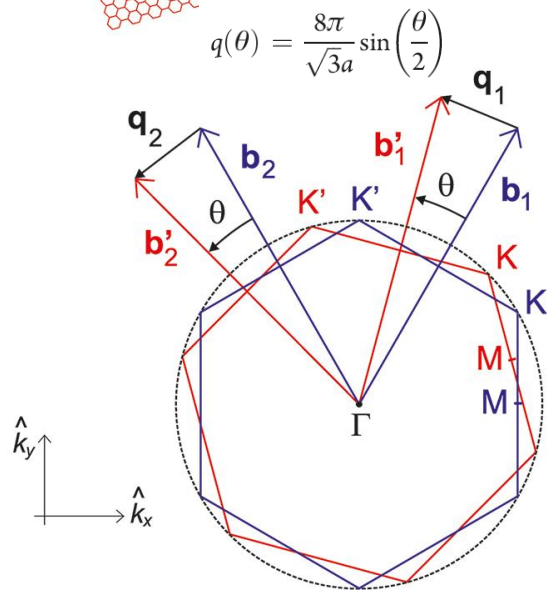
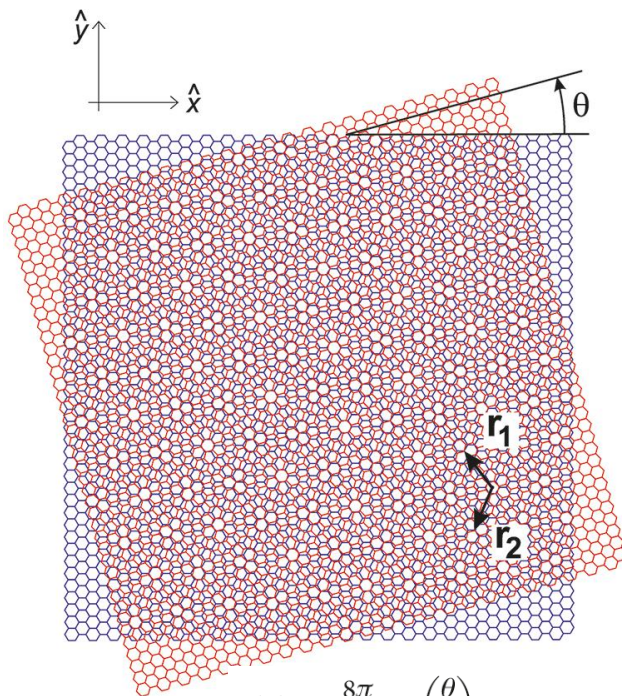


40°



55°





$$q(\theta) = \frac{8\pi}{\sqrt{3}a} \sin\left(\frac{\theta}{2}\right)$$

$$\mathbf{b}_1 = (2\pi/a) [(\sqrt{3}/3)\hat{\mathbf{k}}_x + \hat{\mathbf{k}}_y]$$

$$\mathbf{b}_2 = (2\pi/a) [-(\sqrt{3}/3)\hat{\mathbf{k}}_x + \hat{\mathbf{k}}_y]$$

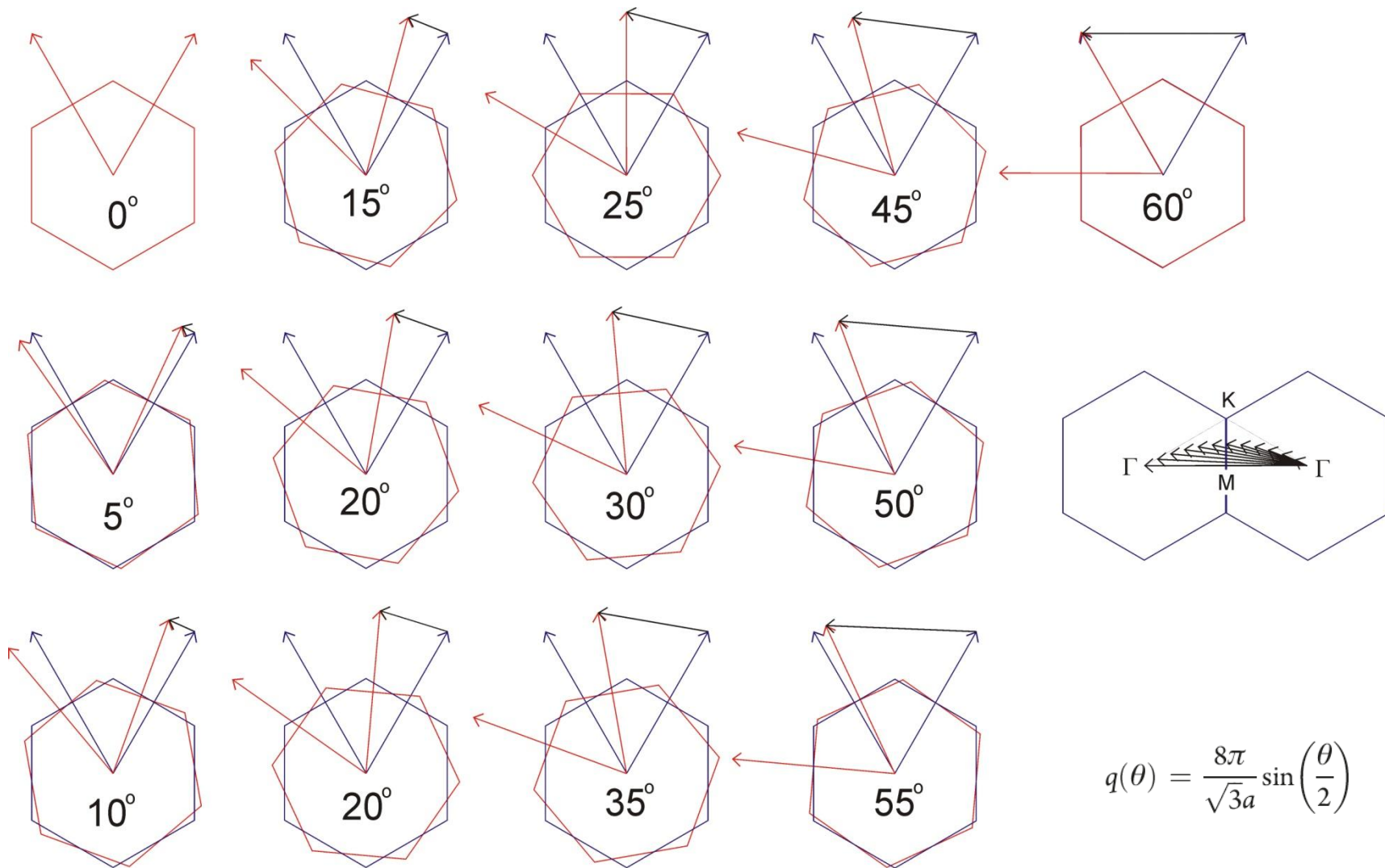
$$\mathbf{b}'_1(\theta) = \frac{2\pi}{\sqrt{3}a} [(\cos\theta - \sqrt{3}\sin\theta)\hat{\mathbf{k}}_x + (\sqrt{3}\cos\theta + \sin\theta)\hat{\mathbf{k}}_y],$$

$$\mathbf{b}'_2(\theta) = \frac{2\pi}{\sqrt{3}a} [(-\cos\theta - \sqrt{3}\sin\theta)\hat{\mathbf{k}}_x + (\sqrt{3}\cos\theta - \sin\theta)\hat{\mathbf{k}}_y].$$

$$\mathbf{q}_1 = \mathbf{b}'_1 - \mathbf{b}_1 \quad \mathbf{q}_2 = \mathbf{b}'_2 - \mathbf{b}_2$$

$$\mathbf{q}_1(\theta) = \frac{2\pi}{\sqrt{3}a} \left\{ [-(1 - \cos\theta) - \sqrt{3}\sin\theta]\hat{\mathbf{k}}_x + [-\sqrt{3}(1 - \cos\theta) + \sin\theta]\hat{\mathbf{k}}_y \right\},$$

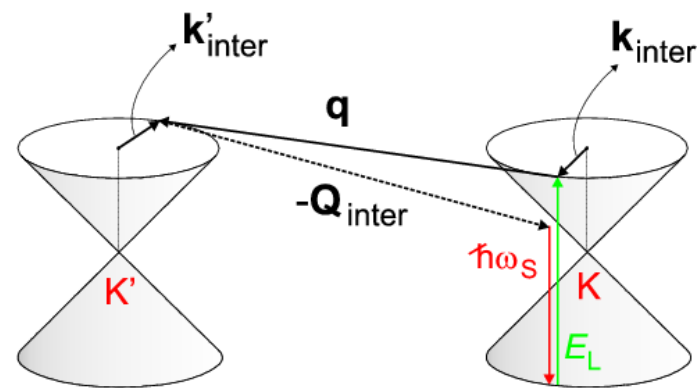
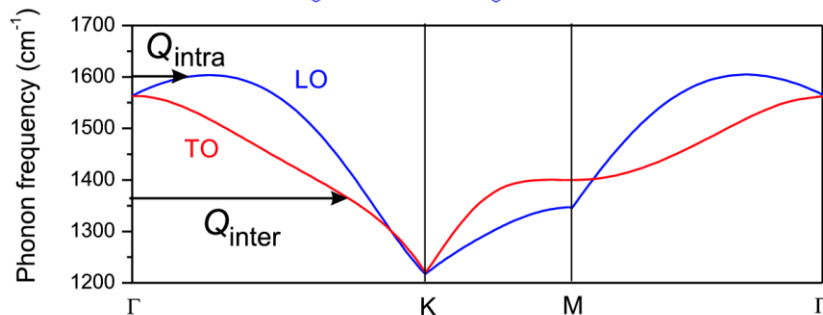
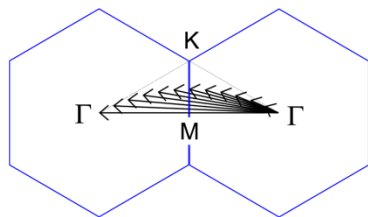
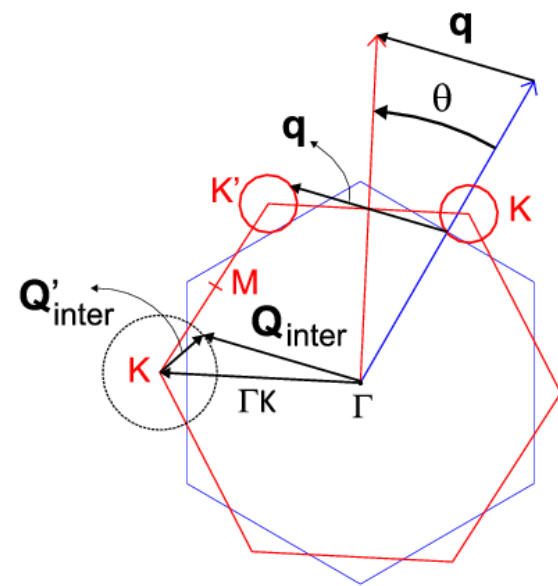
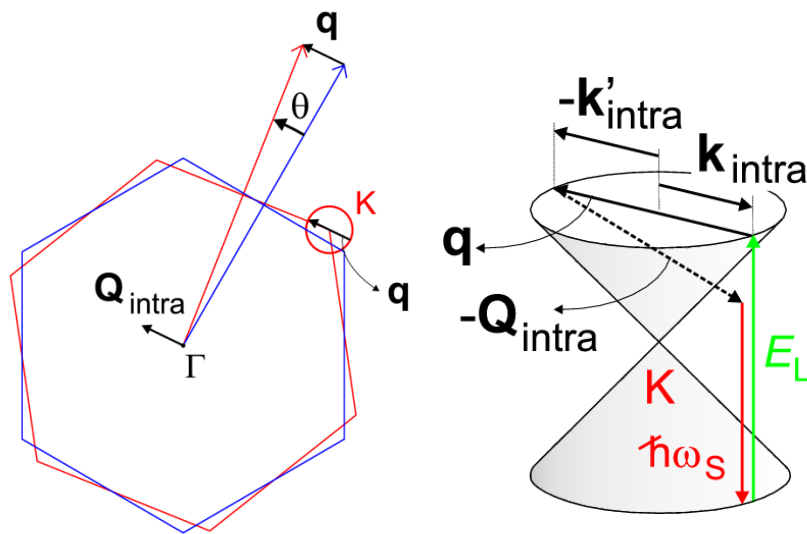
$$\mathbf{q}_2(\theta) = \frac{2\pi}{\sqrt{3}a} \left\{ [(1 - \cos\theta) - \sqrt{3}\sin\theta]\hat{\mathbf{k}}_x + [-\sqrt{3}(1 - \cos\theta) - \sin\theta]\hat{\mathbf{k}}_y \right\}.$$



$$\mathbf{q}_1(\theta) = \frac{2\pi}{\sqrt{3}a} \left\{ \left[-(1 - \cos\theta) - \sqrt{3}\sin\theta \right] \hat{\mathbf{k}}_x + \left[-\sqrt{3}(1 - \cos\theta) + \sin\theta \right] \hat{\mathbf{k}}_y \right\}$$

$$q(\theta) = \frac{8\pi}{\sqrt{3}a} \sin\left(\frac{\theta}{2}\right)$$

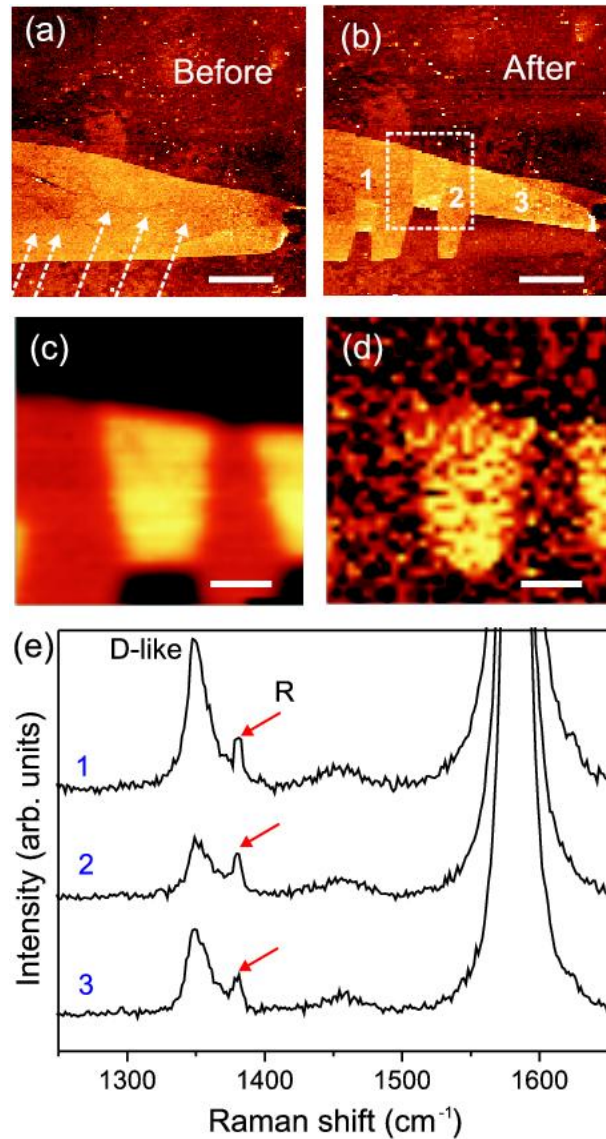
Rotation-induced intravalley and intervalley resonance scattering:



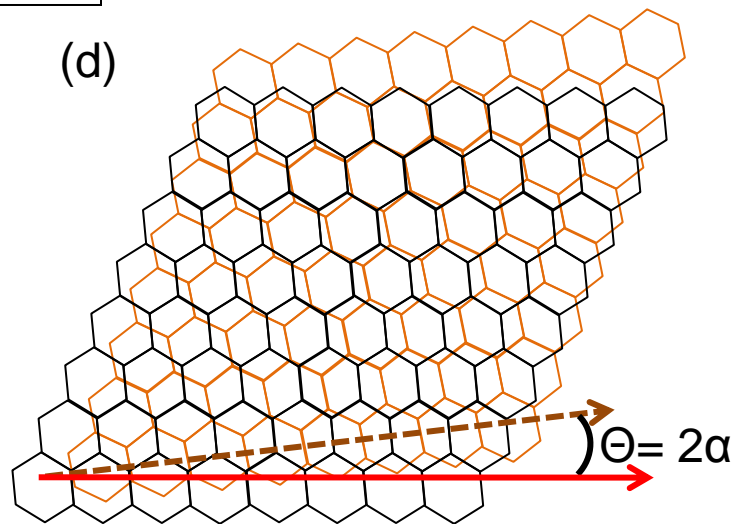
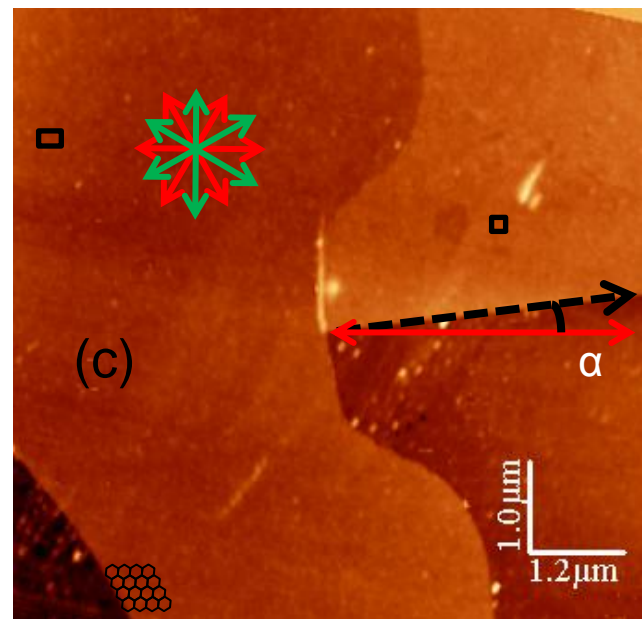
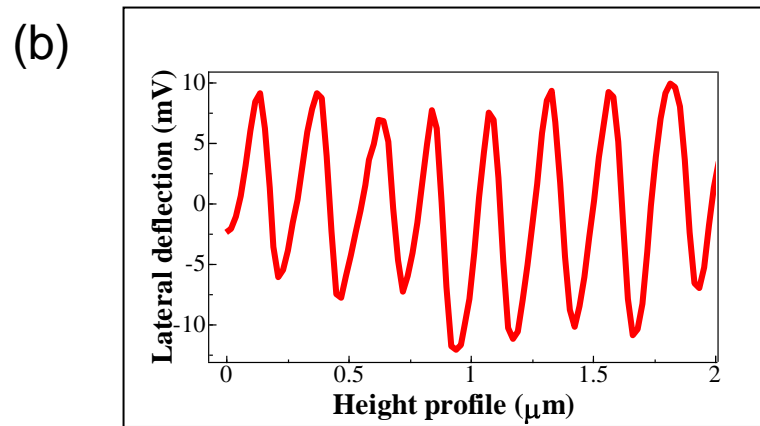
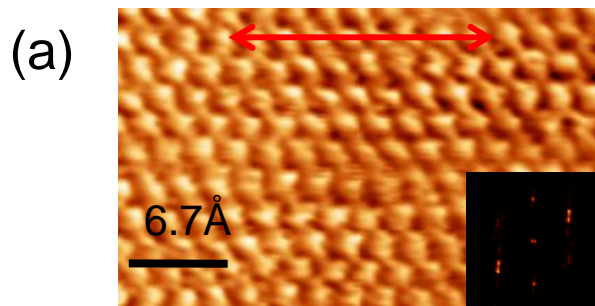
Venezuela, Lazzeri, and Mauri, PRB **84**, 035433 (2011).

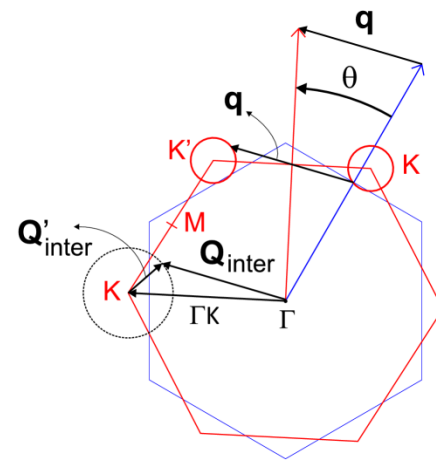
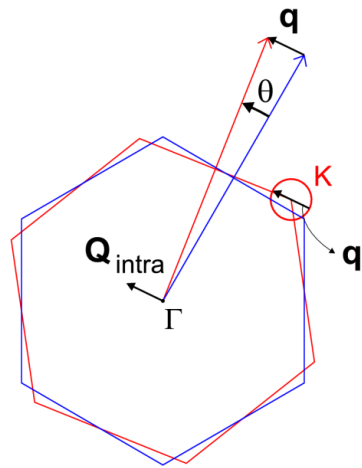
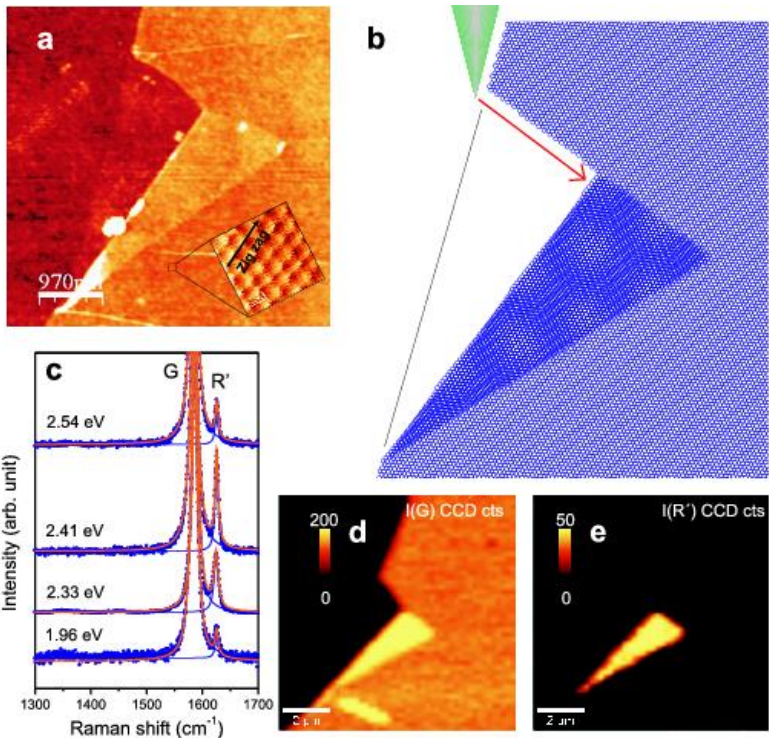
Carozo et al., Nano Lett. **11**, 4527 (2011).

Production of folded graphene:

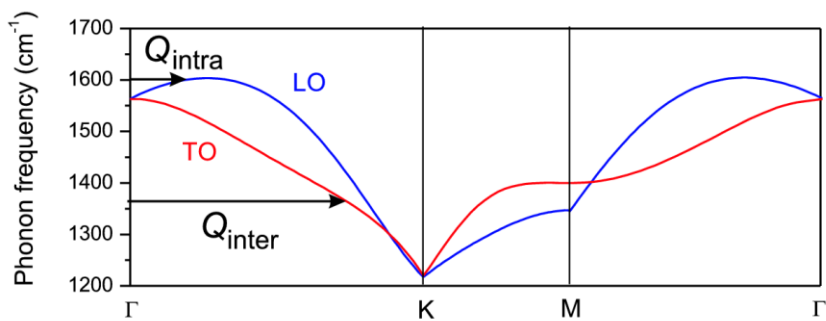


Carozo et al., submitted.



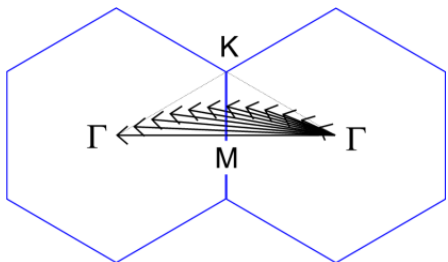


Carozo et al., Nano Lett. **11**, 4527 (2011).

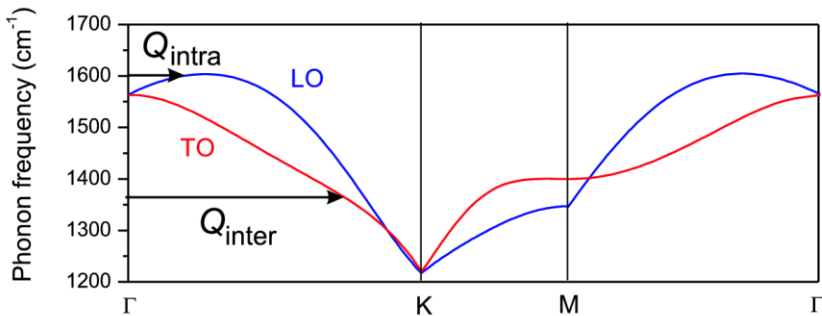
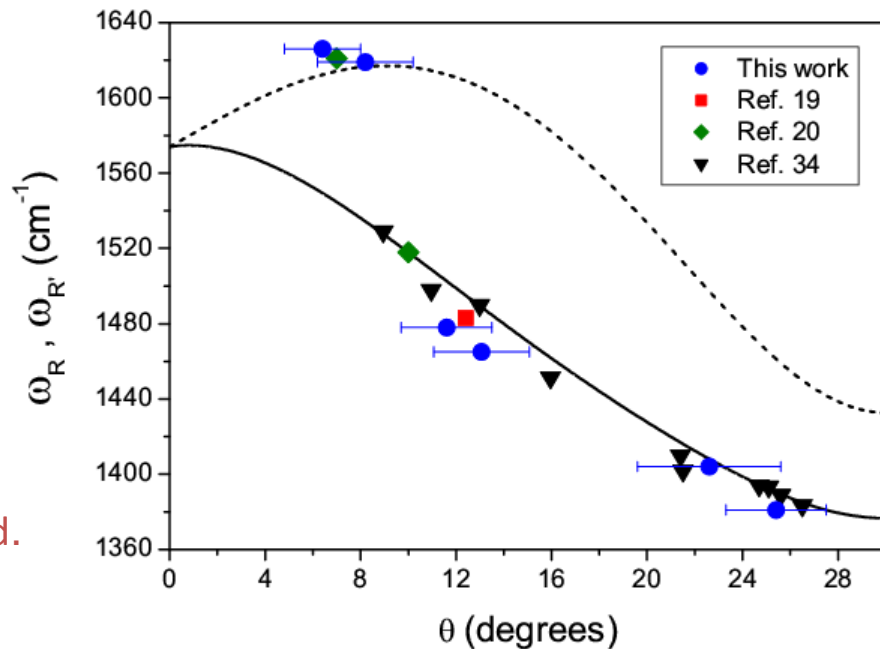


Venezuela, Lazzeri, and Mauri, PRB **84**, 035433 (2011).

$$q = \frac{2\pi}{\sqrt{3}a} \{ [-(1 - \cos\theta) - \sqrt{3}\sin\theta] \hat{k}_x + [-\sqrt{3}(1 - \cos\theta) + \sin\theta] \hat{k}_y \}, \quad \text{Carozo et al., Nano Lett. 11, 4527 (2011).}$$



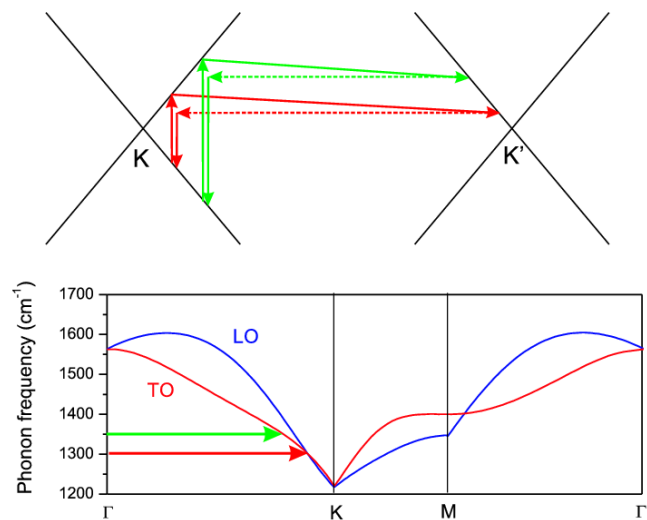
Carozo et al., submitted.



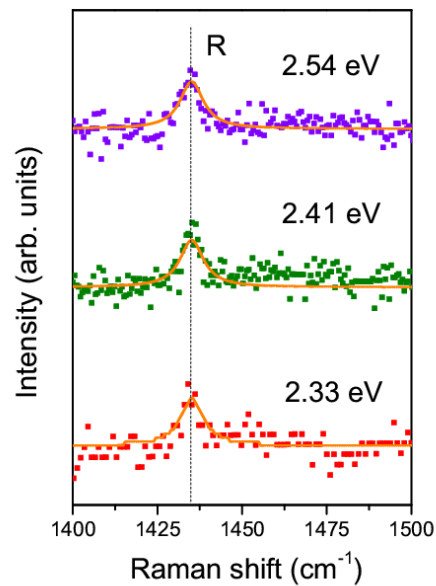
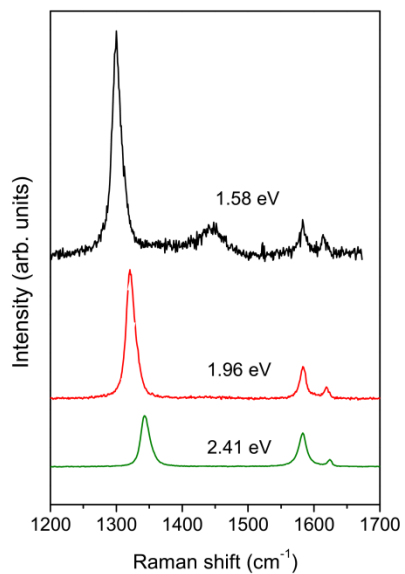
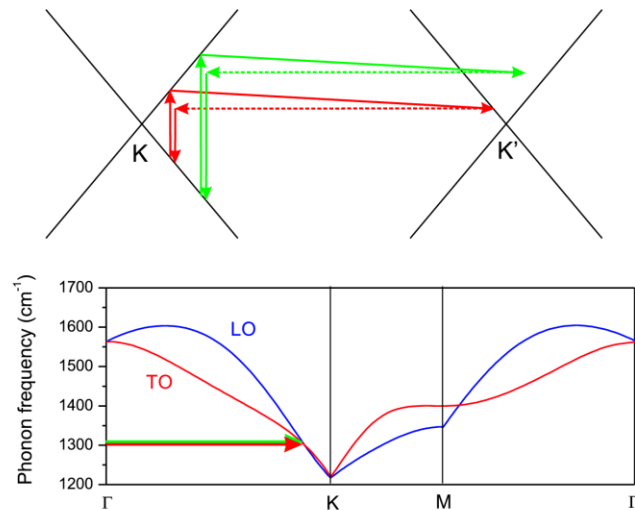
Venezuela, Lazzeri, and Mauri, PRB **84**, 035433 (2011).

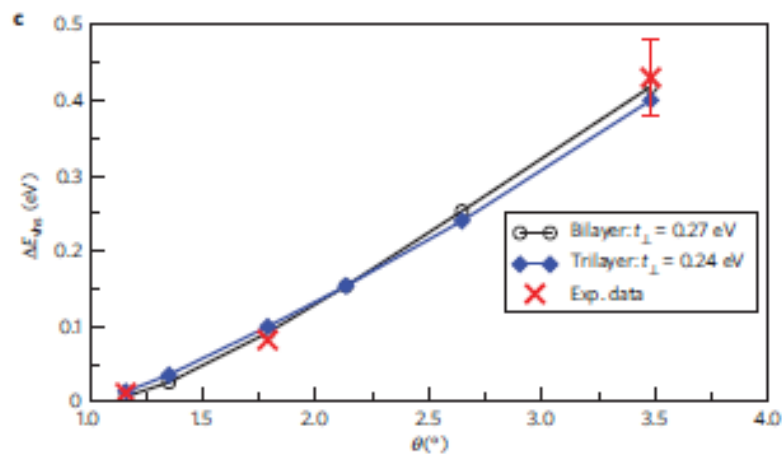
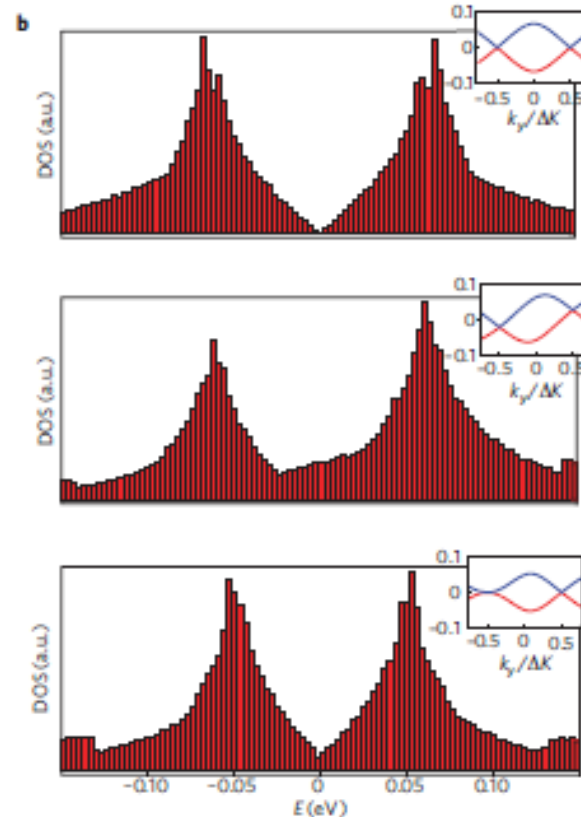
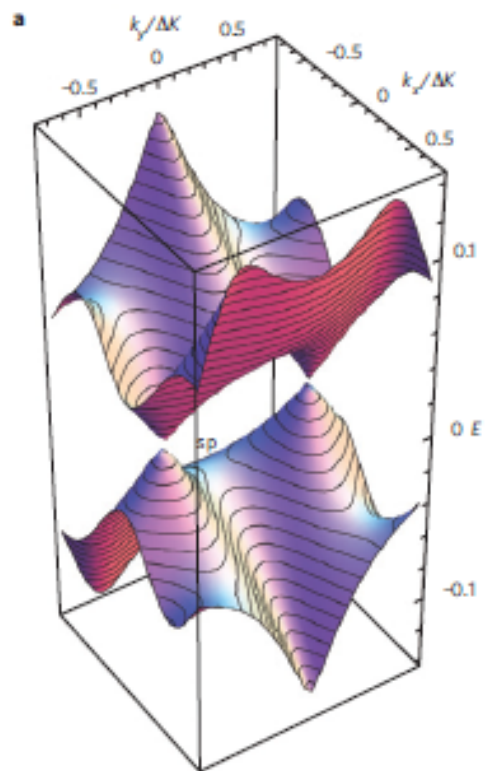
- ◇ Kim et al., PRL **108**, 246103 (2012).
- Havener et al., Nano Lett. **12**, 3162 (2012).
- ▽ Wang et al., arXiv:1301.4488v1 (2013).

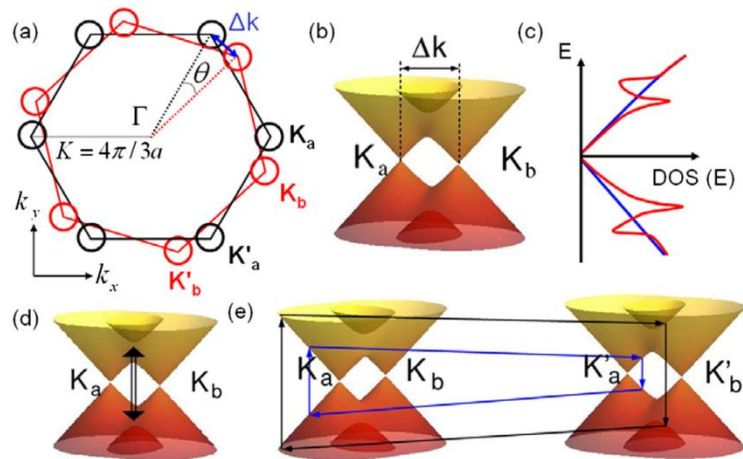
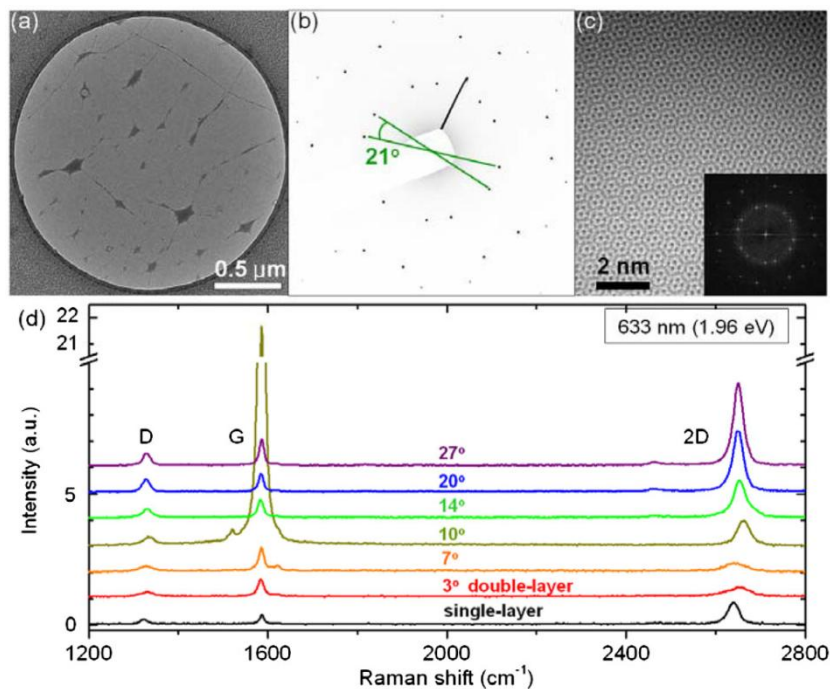
D band dispersion



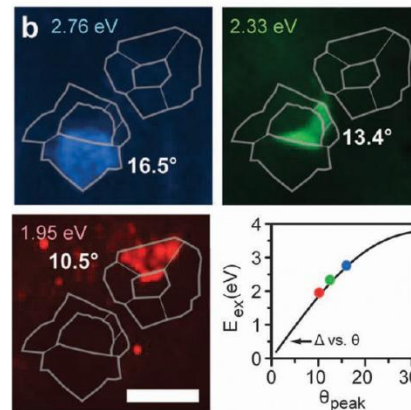
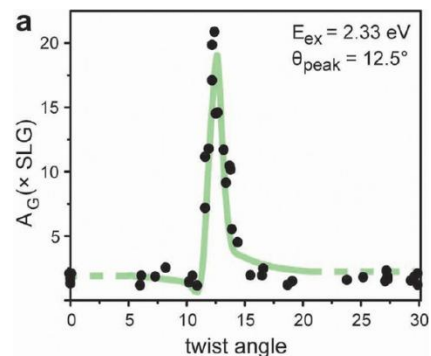
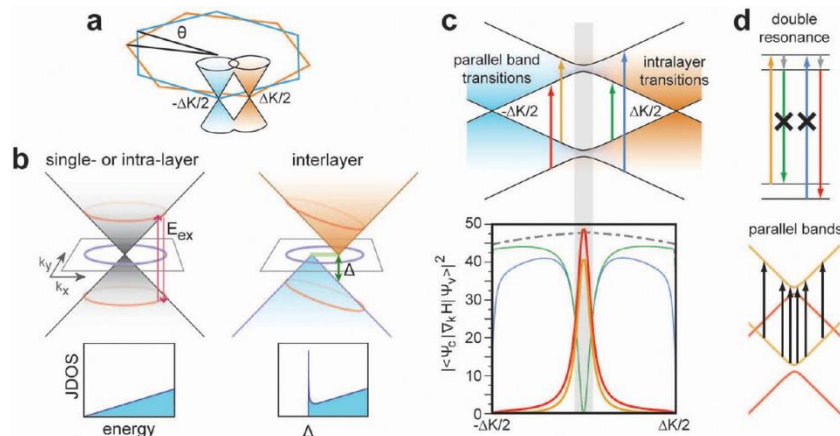
R and R' bands are not dispersive



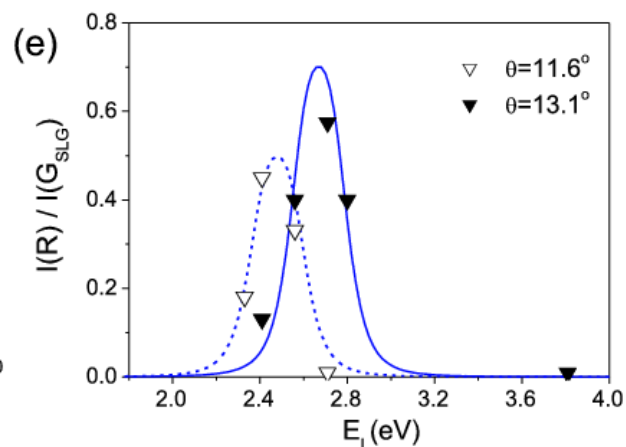
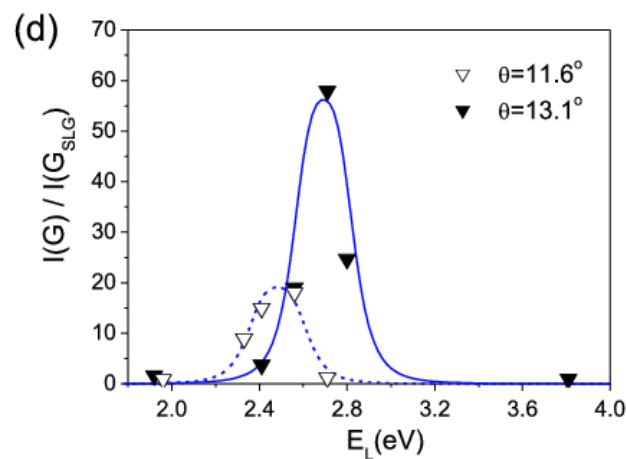
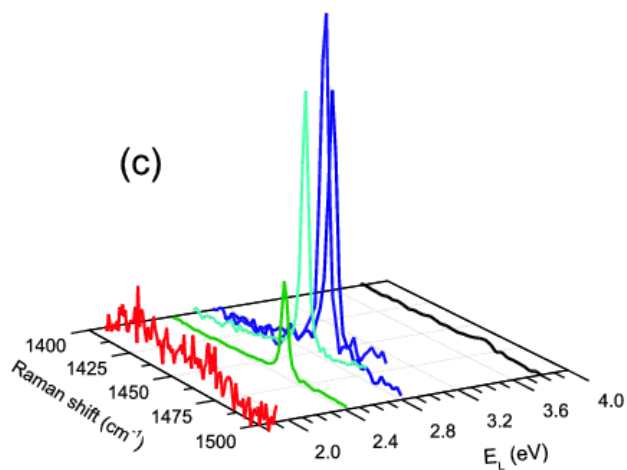
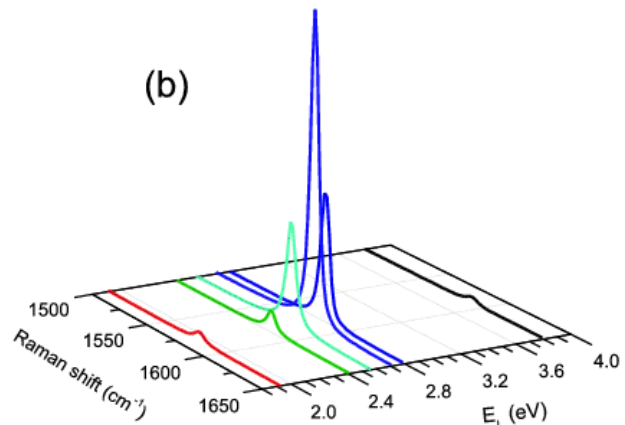
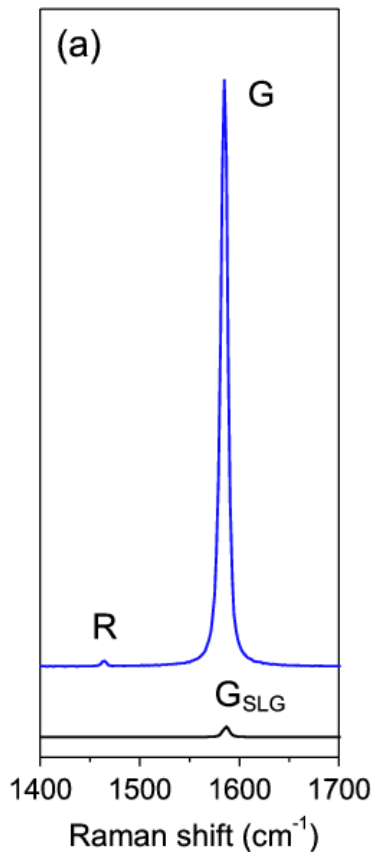




Kim et al., PRL **108**, 246103 (2012).



Havener et al., Nano Lett. **12**, 3162 (2012).

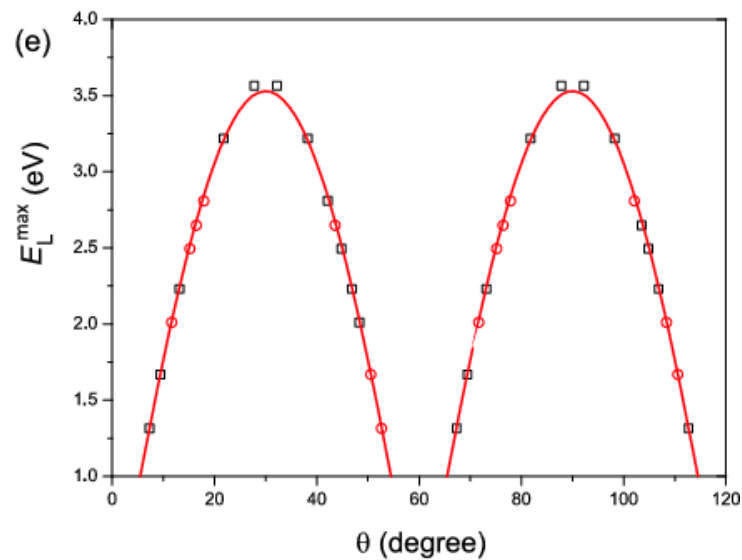
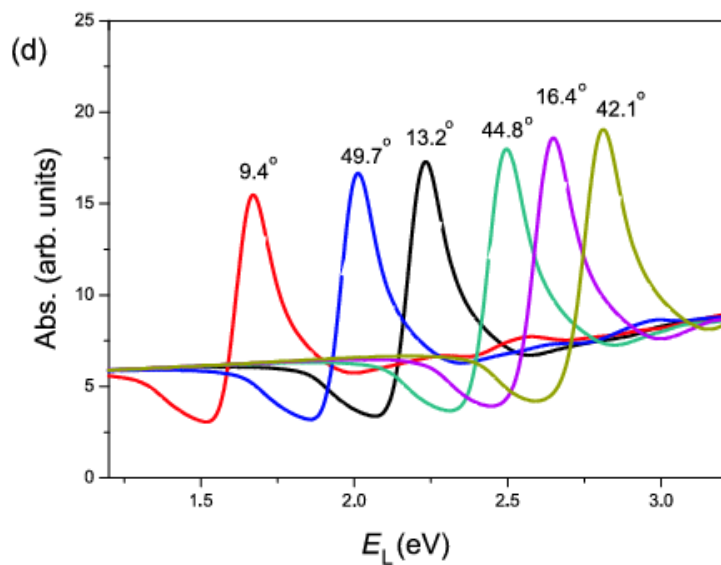
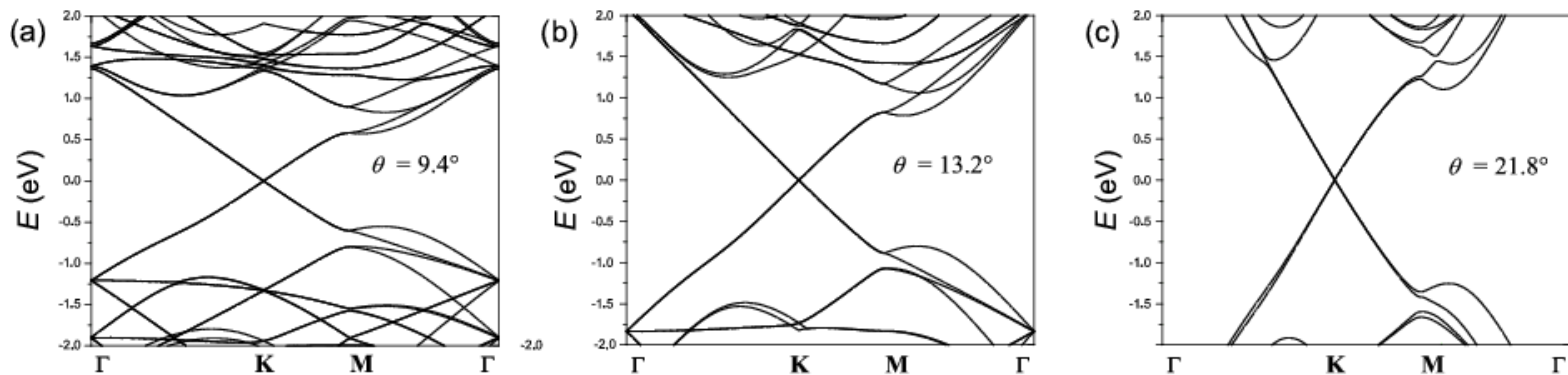


$$\frac{I(G)}{I(G_{SLG})} = \left| \frac{M}{(E_L - E_{vHs} - i\gamma)(E_L - E_{vHs} - \hbar\omega_G - i\gamma)} \right|^2$$

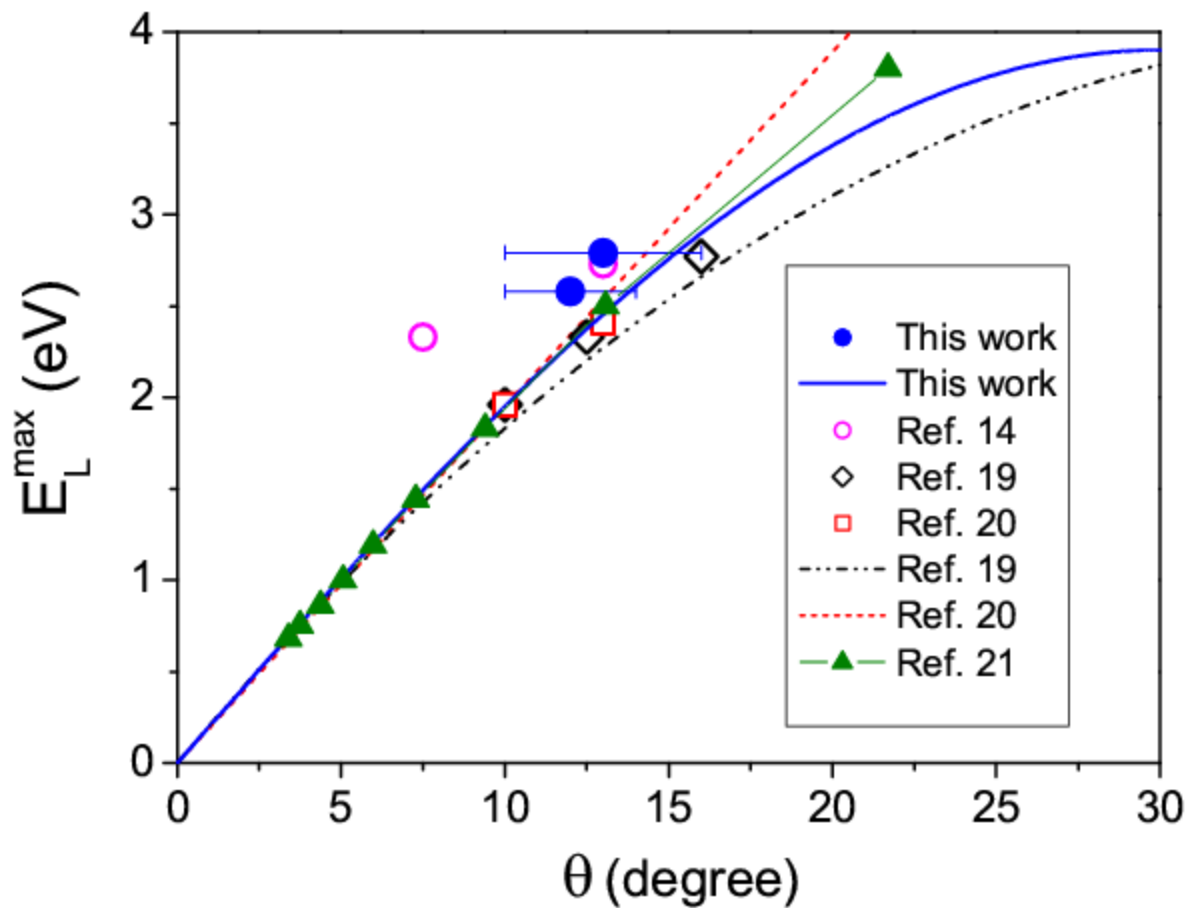
$$\gamma = 0.12 \text{ eV}$$

$$\frac{I(R)}{I(G_{SLG})} = \left| \frac{M'}{(E_L - E_{vHs} - i\gamma)[E_L - E_{eh}(k+q) - i\gamma](E_L - E_{vHs} - \hbar\omega_R - i\gamma)} \right|^2$$

Ab-initio calculations



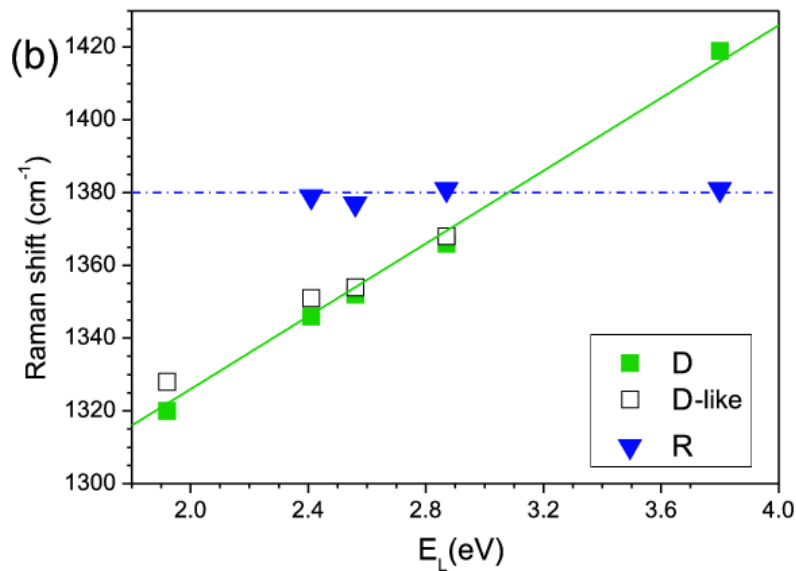
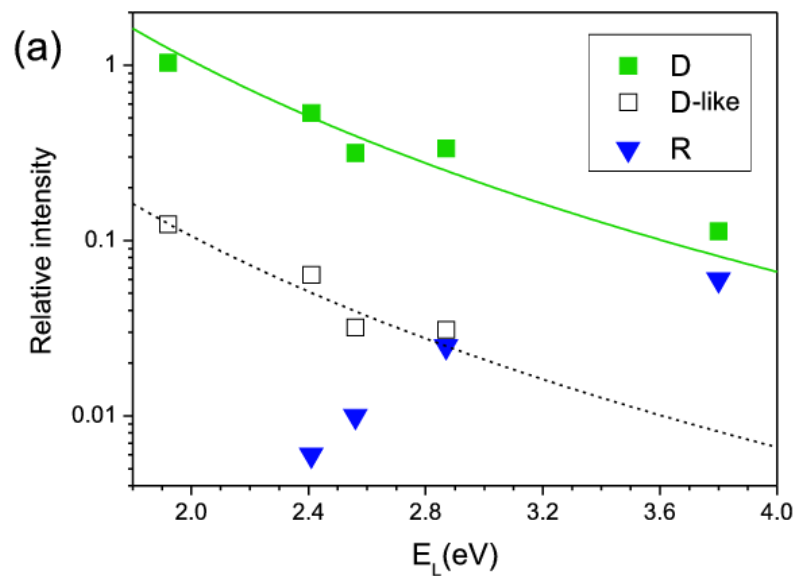
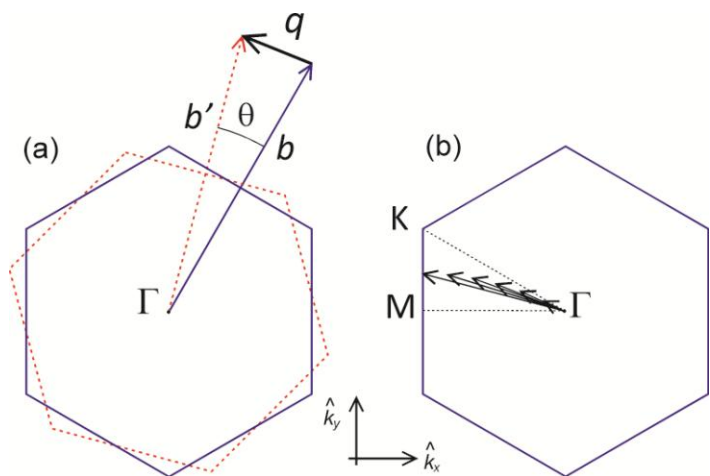
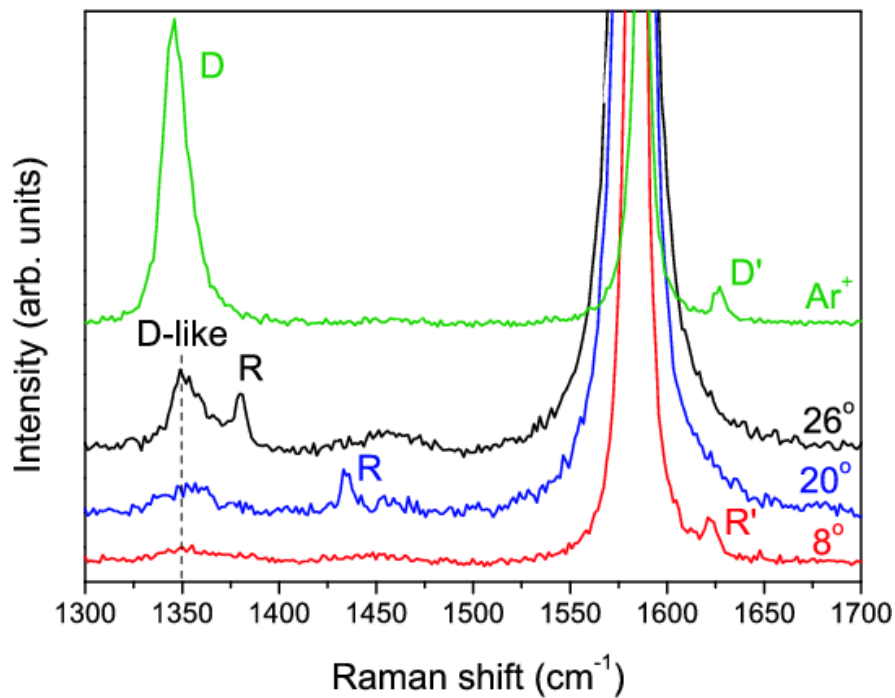
$$E_L^{\max} = E_0 |\sin(3\theta)|$$

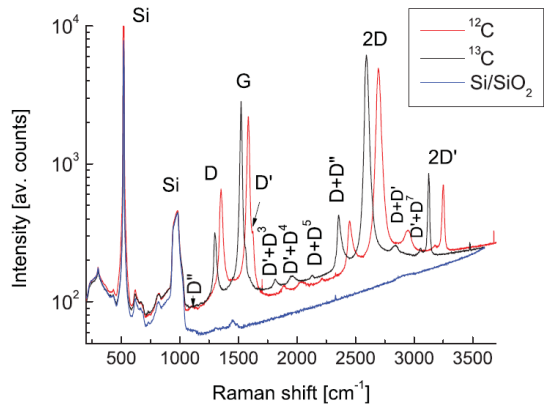


Carozo et al., submitted.

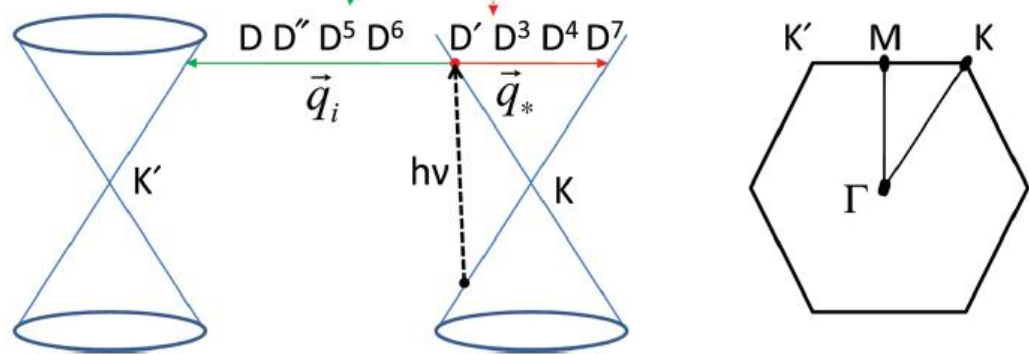
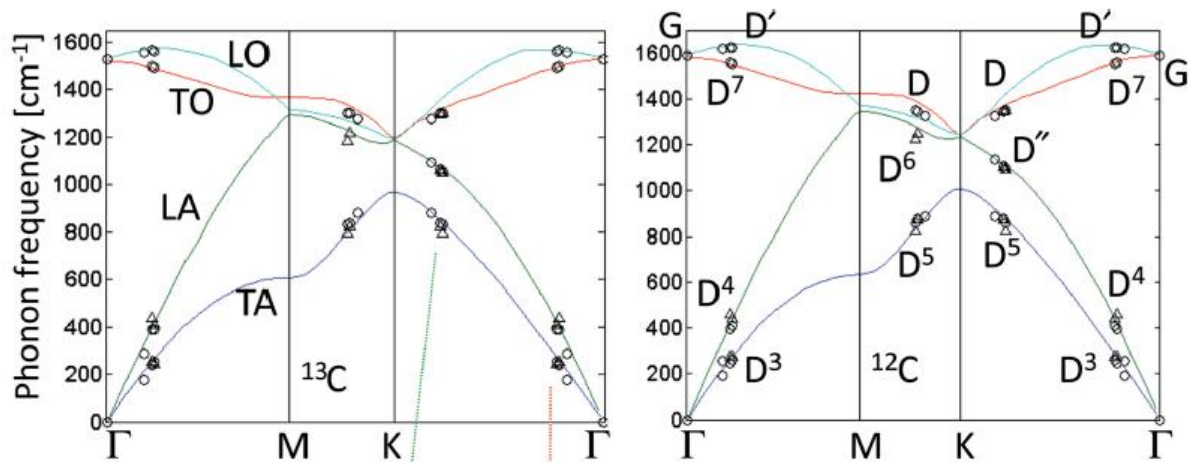
- ◇ Havener et al., *Nano Lett.* **12**, 3162 (2012).
- Kim et al., *PRL* **108**, 246103 (2012).
- ▲ Sato et al., *Phys. Rev. B* **86**, 125414 (2012).
- Ni et al. *Phys. Rev. B* **80**, 125404 (2009).

“D-like” band:

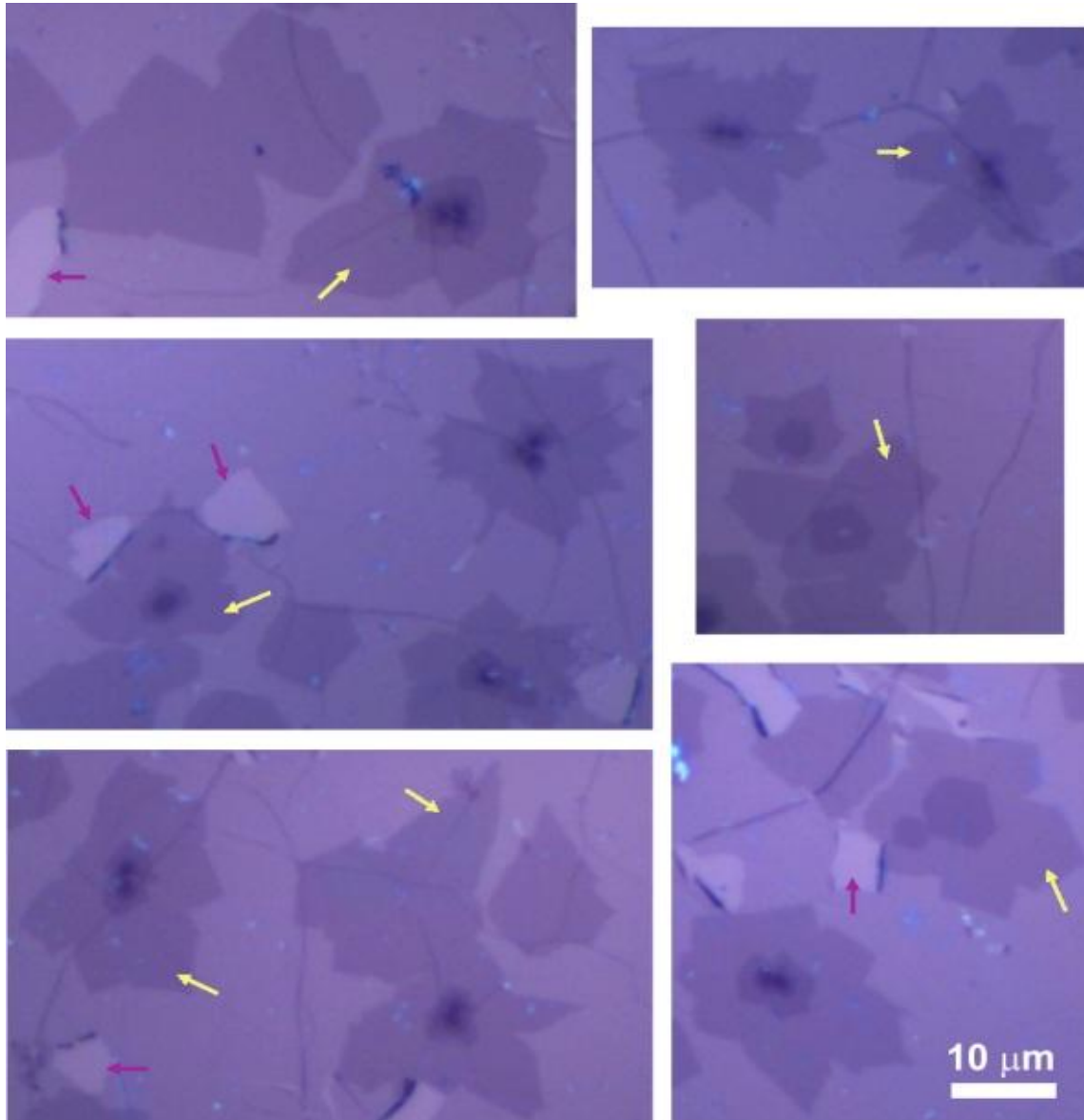




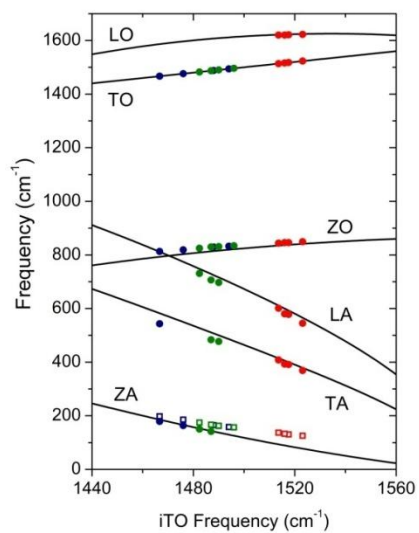
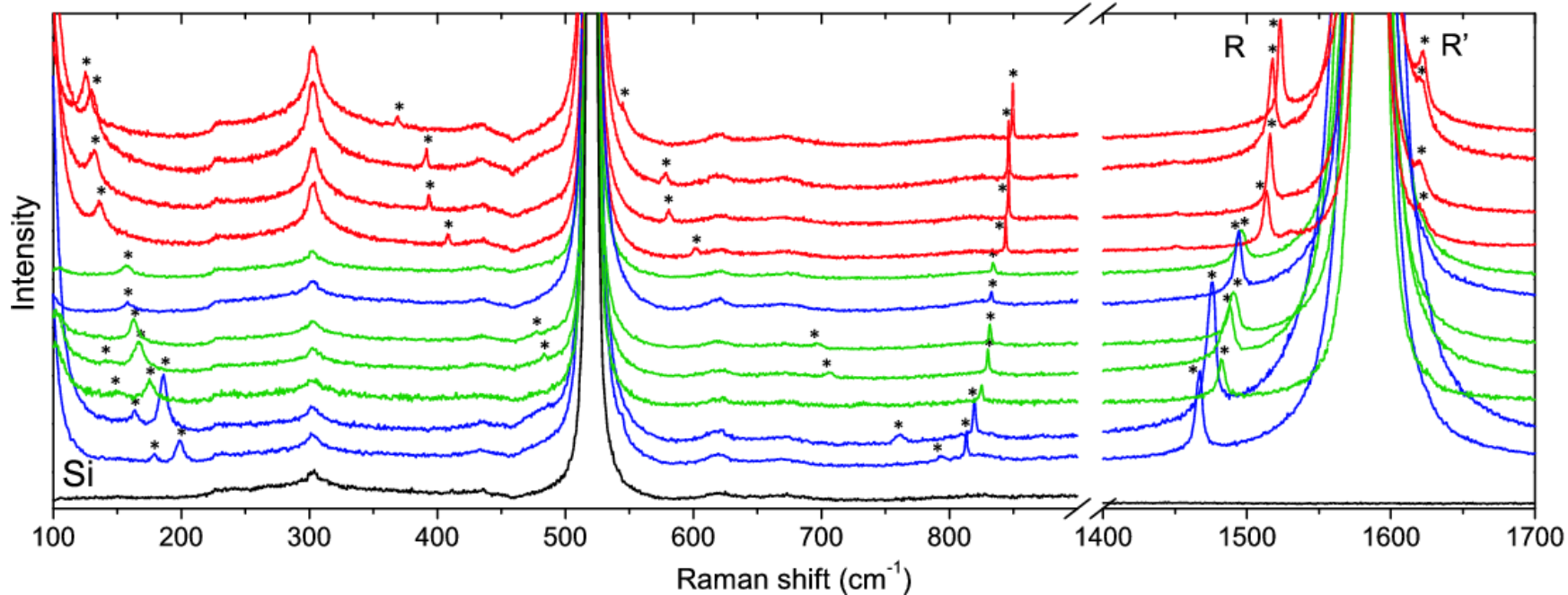
Phonon dispersion of graphene



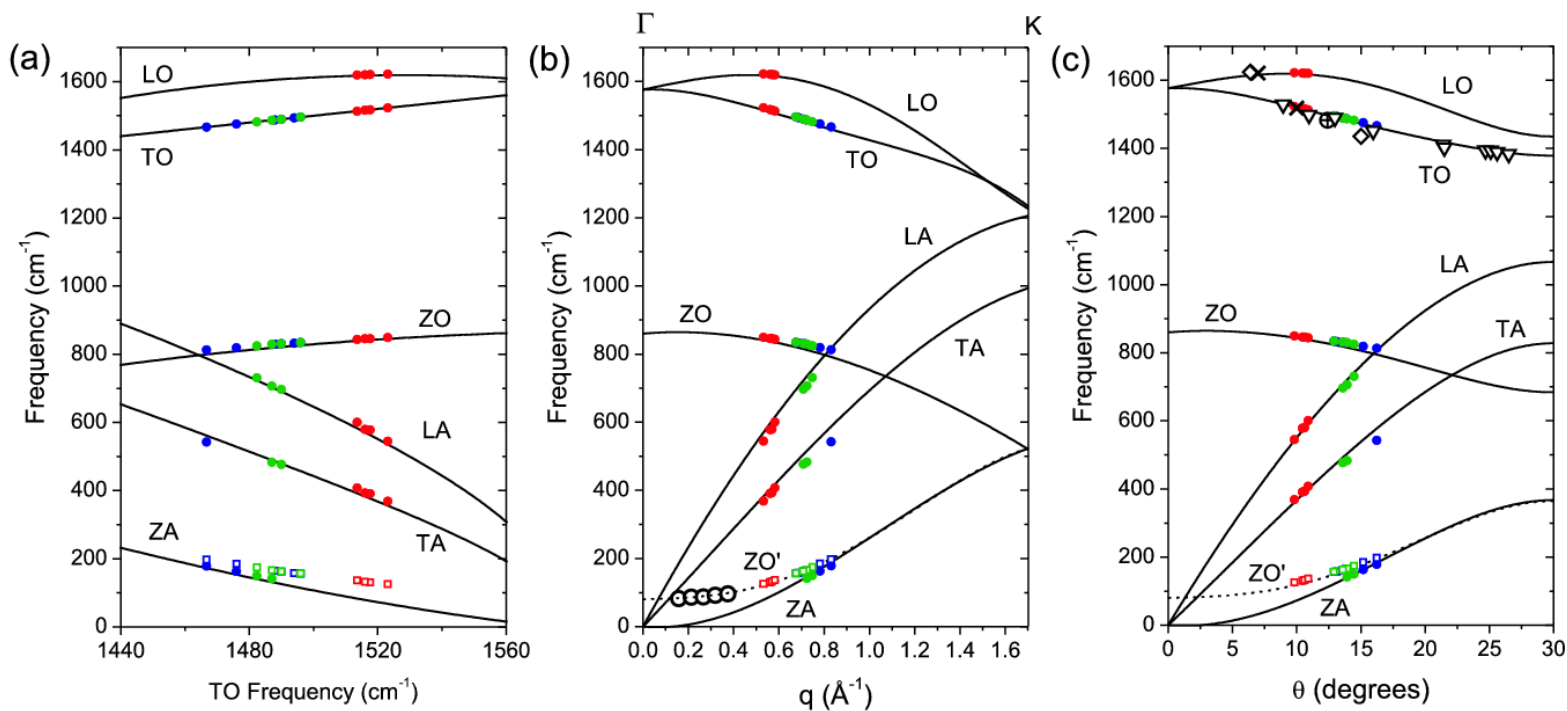
CVD-grown graphene



Phonon dispersion of tBLG

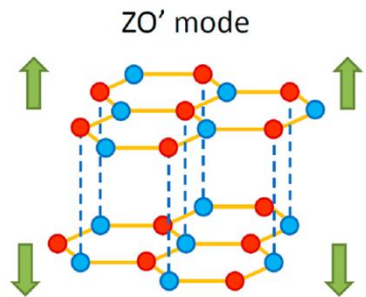
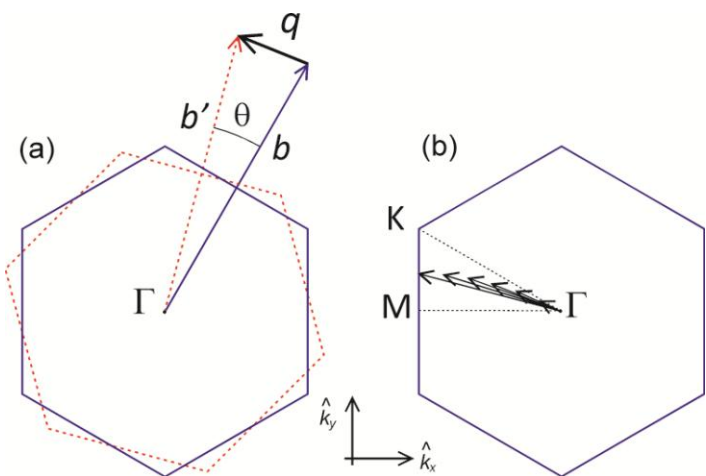


Phonon dispersion of tBLG



J. Campos-Delgado et al., submitted.

- ✕ Kim et al., PRL **108**, 246103 (2012).
- ⊕ Havener et al., Nano Lett. **12**, 3162 (2012).
- ◇ Carozo et al., Nano Lett. **11**, 4527 (2011).
- ▽ Wang et al., arXiv:1301.4488v1 (2013).



Lui et al., Nano Lett. **12**, 5539–5544 (2012).

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