

# Graphene supports the propagation of subwavelength optical solitons

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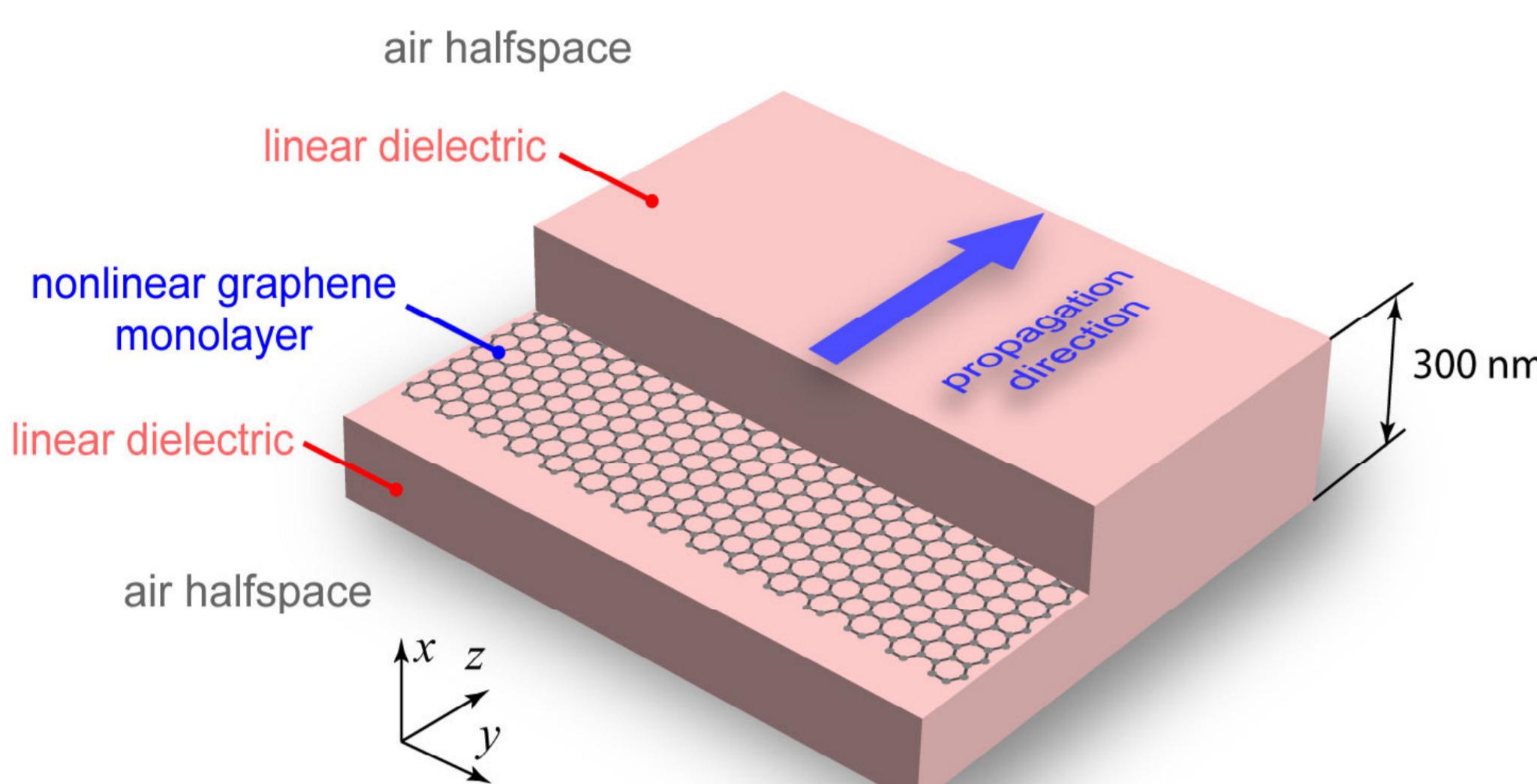
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We study theoretically nonlinear propagation of light in a graphene monolayer. We show that the large intrinsic nonlinearity of graphene at optical frequencies enables the formation of quasione-dimensional self-guided beams (spatial solitons) featuring subwavelength widths at moderate electric-field peak intensities. We also demonstrate a novel class of nonlinear self-confined modes resulting from the hybridization of surface plasmon polaritons with graphene optical solitons.

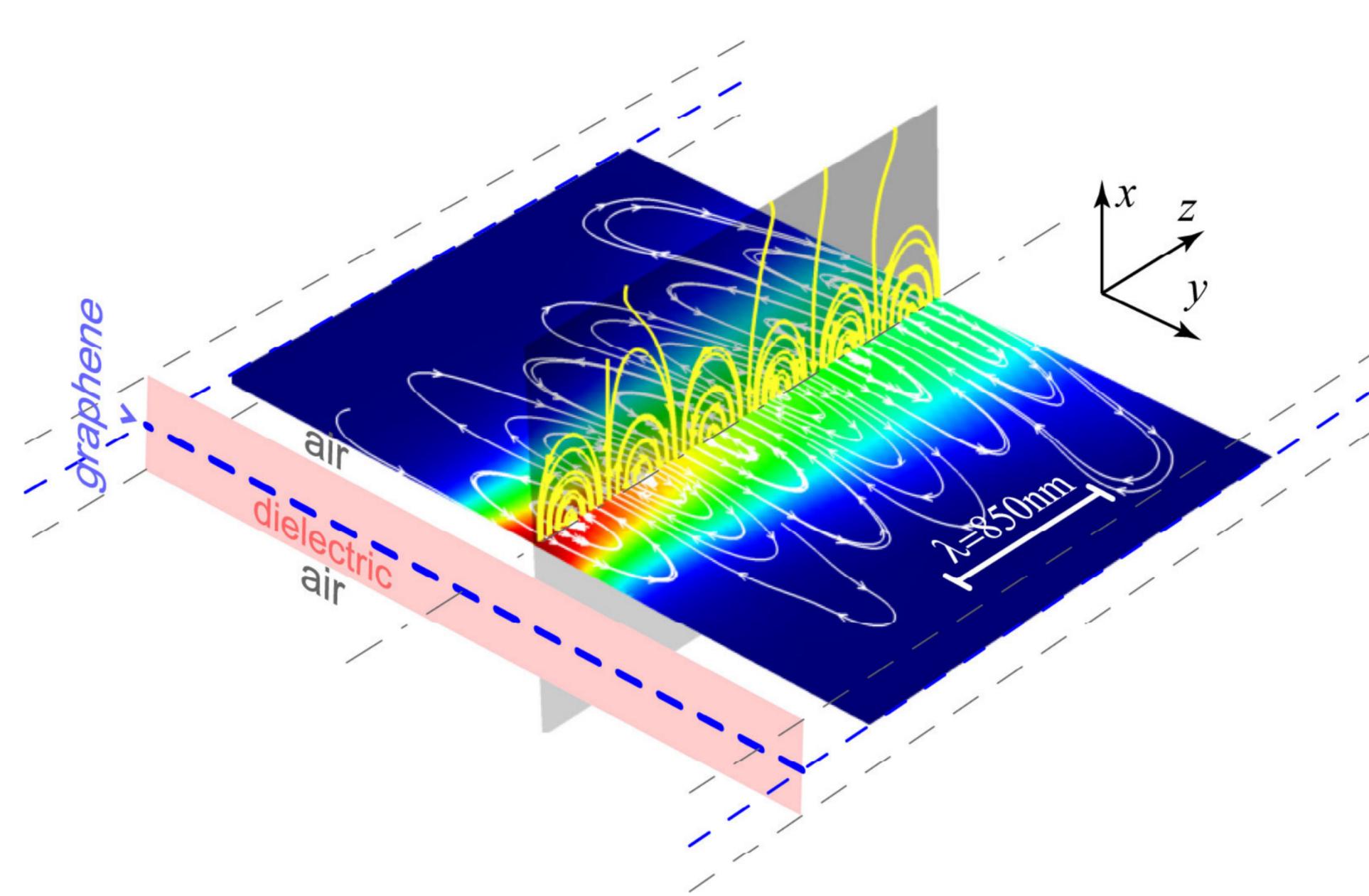
## Geometry

Sketch of the studied system.



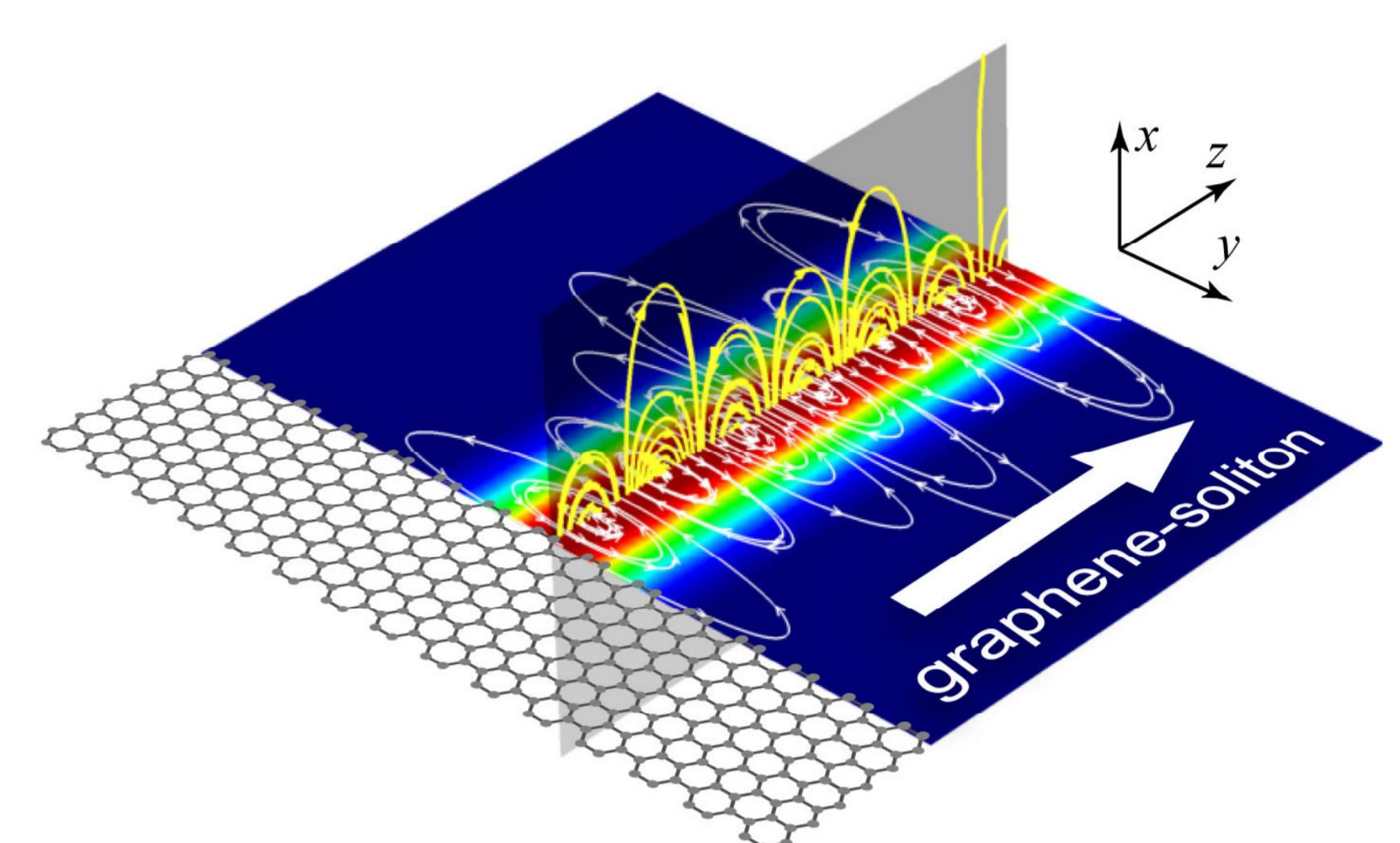
## Diffraction

Linear propagation: decay of the input beam.



## Spatial soliton

Propagation without change of the profile.



## Quasi-analytical model:

$$E = \frac{1}{2}[A(x)f(y, z)\exp(i\beta_0 z) + c.c.]$$

We assume that solutions has this form

$$\mathbf{j} = \partial\mathbf{P}/\partial t = \delta(x)\sigma_{gr}(E)\mathbf{E}$$

$$\text{Nonlinear 2D conductivity}$$

$$\sigma_{gr}(E) = \sigma_{LIN} + \frac{3}{4}\sigma_{gr}^{(3)}|E|^2$$

$$\text{Inhomogeneous Helmholtz equation}$$

$$c^2\nabla^2\mathbf{E} - \frac{\partial^2\mathbf{E}}{\partial t^2} = \frac{1}{\epsilon_0}\frac{\partial^2\mathbf{P}}{\partial x^2}$$

$$\text{Nonlinear Schrodinger equation}$$

$$2i\beta_0\frac{\partial f}{\partial z} + \frac{\partial^2 f}{\partial y^2} + g|f|^2f = 0$$

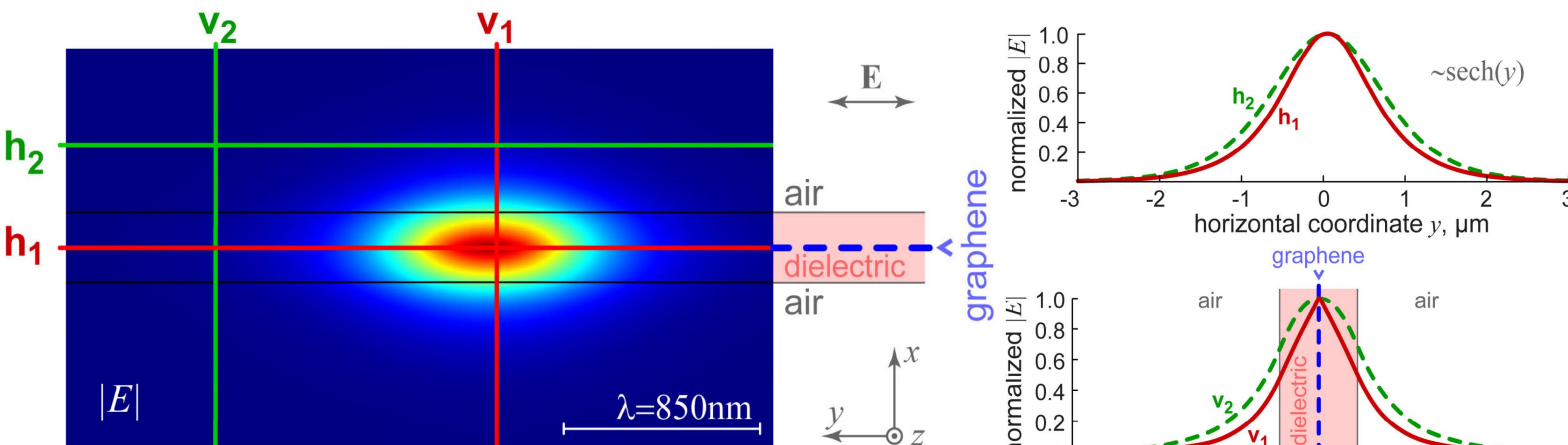
The parameters are

$$g = \frac{3}{4}i\sigma_{gr}^{(3)}\omega/\epsilon_0 c^2 I, \quad I = \int_{-\infty}^{\infty}|A(x)|^2 dx$$

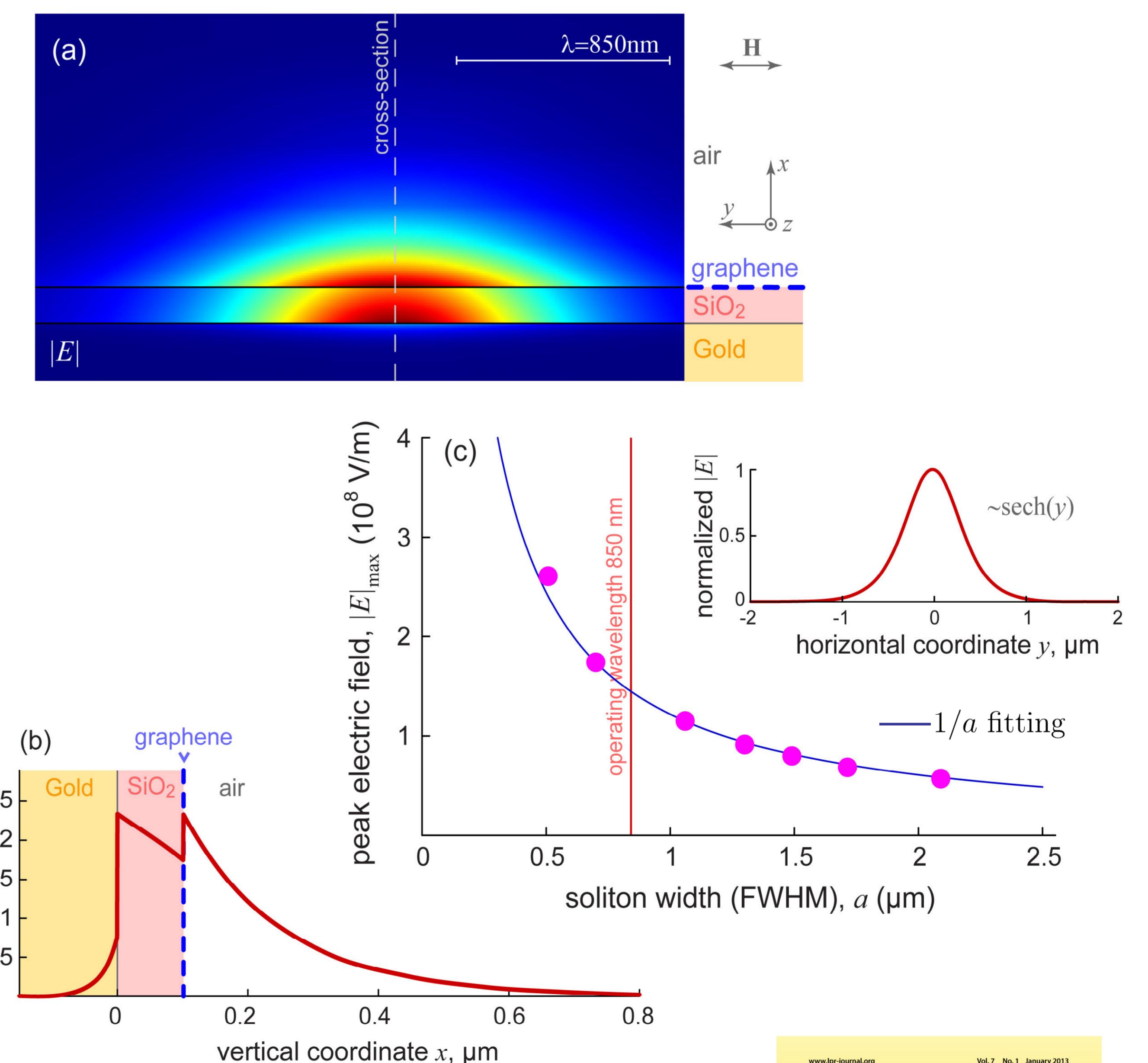
Canonical first-order soliton solution

$$f(y, z) = \frac{1}{w}\sqrt{\frac{2}{g}}\operatorname{sech}(y/w)\exp(iz/2\beta_0 w^2)$$

## Graphene-solitons



## Hybrid graphene-SPP-solitons



## Summary:

- Graphene monolayers can support both TE and TM spatial optical solitons due to the extremely large magnitude of its nonlinear third-order susceptibility.
- Graphene-solitons can have a subwavelength lateral width.
- Quasi-analytical model predicts the field intensities needed for soliton formation.

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