

$$|\Psi_{\kappa}\rangle = \sum_{j=0}^{\kappa-1} |\rho^j\rangle \otimes |a_j\rangle$$