

$$\mathrm{rank}_{\mathrm{psd}}(S_d) \sim \log d$$