

# RNA secondary structure prediction beyond thermodynamics

A four-ingredient unifying perspective

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## Single-sequence secondary structure prediction:

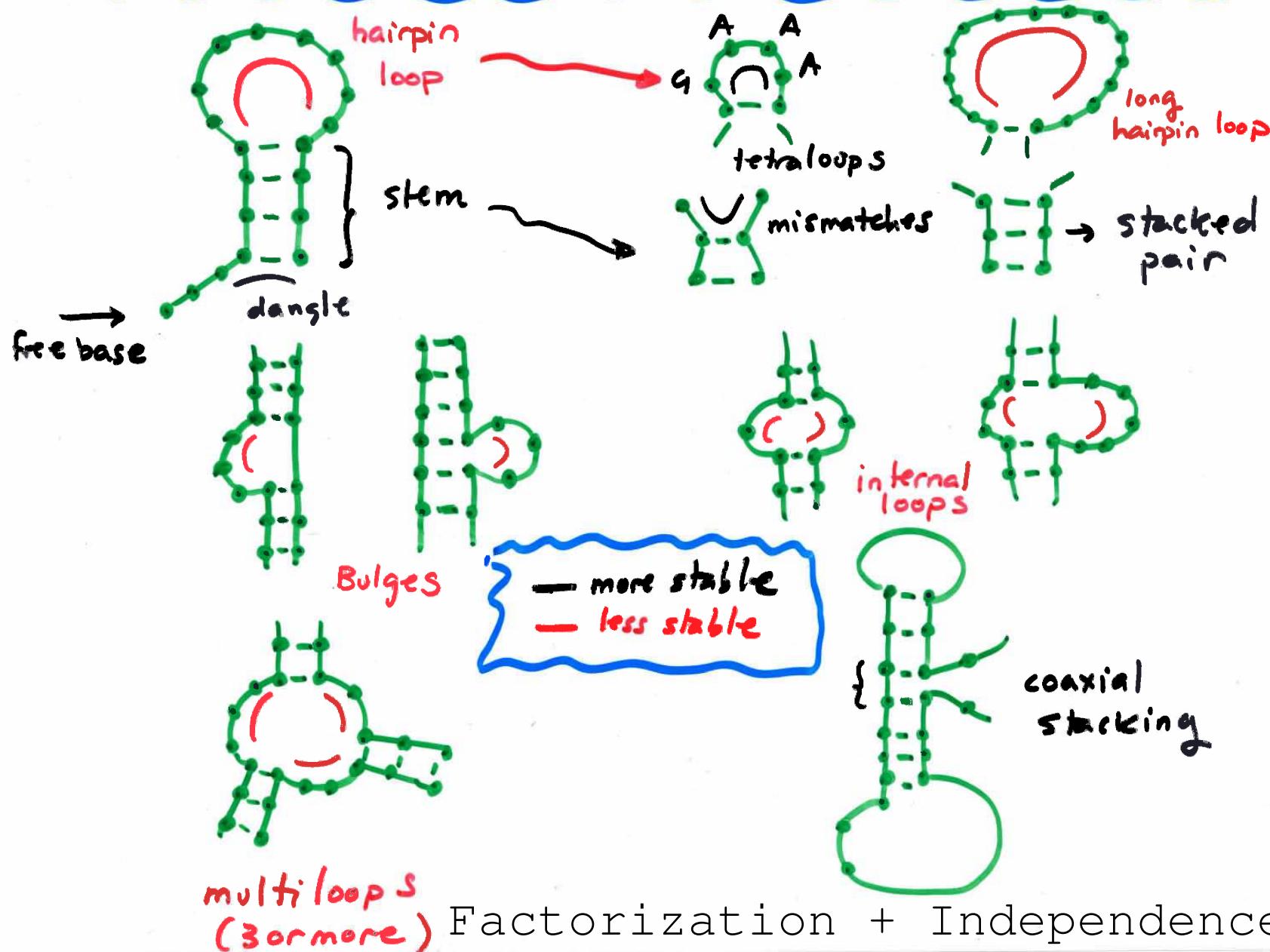
thermodynamic Models Mfold/UNAFold Zuker, Stiegler & Sankoff (1981-)  
ViennaRNA Hofacker & Stadler (1994-)  
RNAsstructure Mathews (1999-)

Humans do it by comparative analysis (C. Woese, R. Gutell)  
accurate - requires a lot of sequences

Evolutionary variation is a statistical signal, not thermodynamic  
use of probabilistic models for RNA secondary structure prediction

# Features of RNA secondary structure

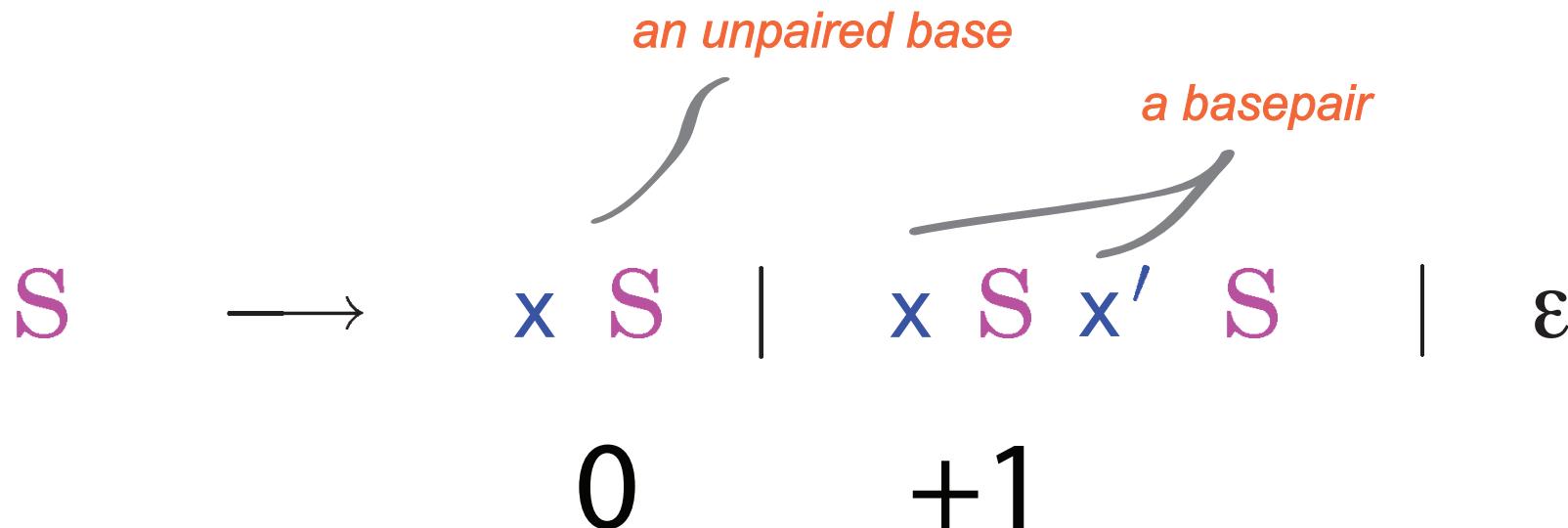
## The nearest-neighbour model of RNA folding



# Context-free grammars

for RNA secondary structure

SIMPLEST



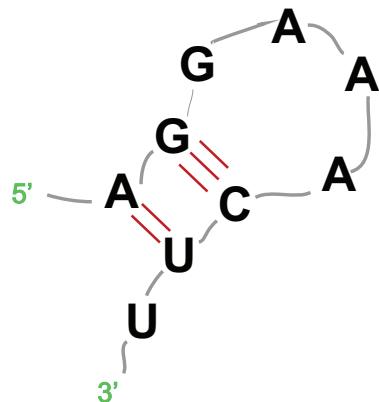
$S$  = nonterminal

$x, x'$  = terminals (A,C,U, or G)

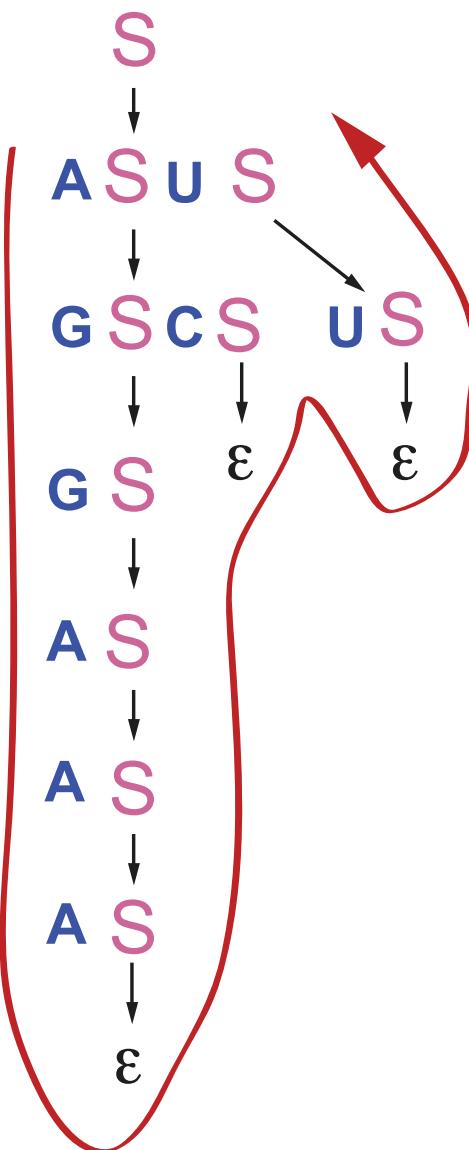
$\epsilon$  = empty string

Nussinov, 1979

# Nussinov structure generation



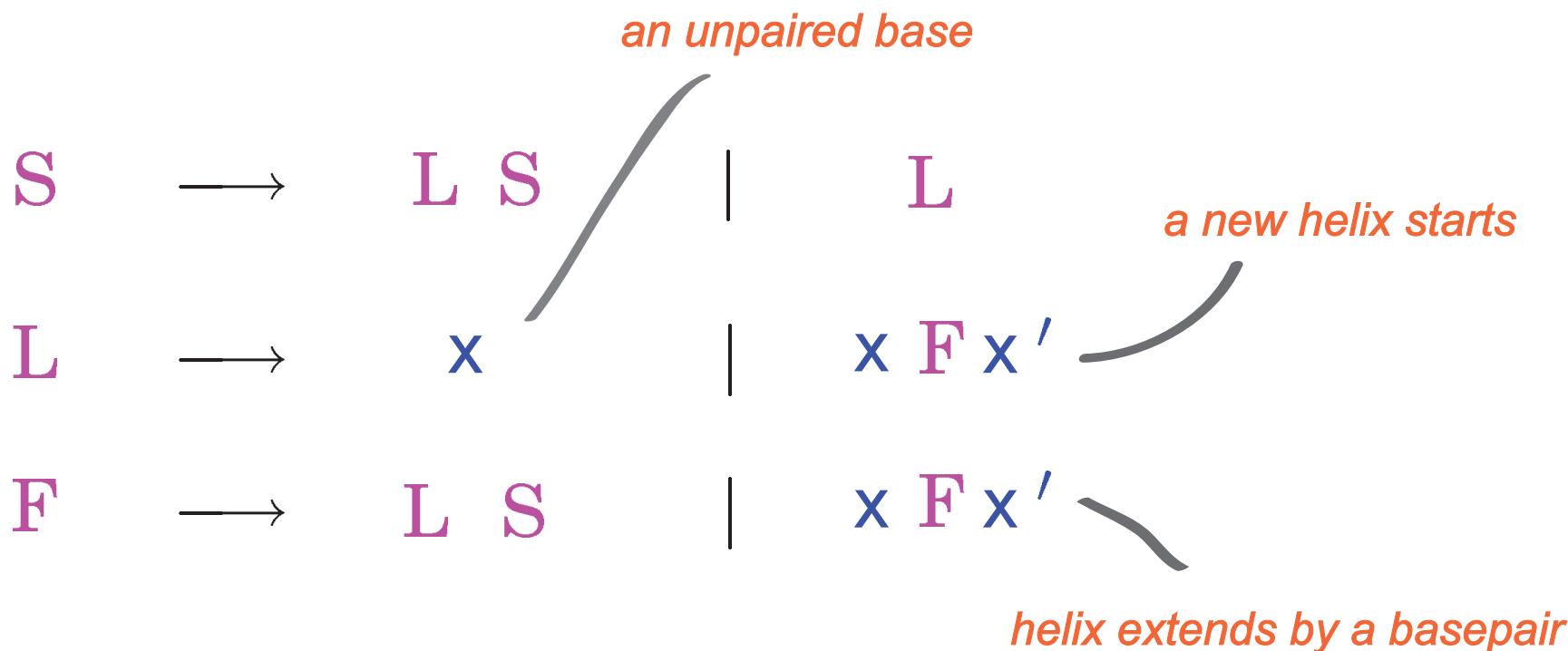
5' - AGGAAACUUU - 3'



# Context-free grammars

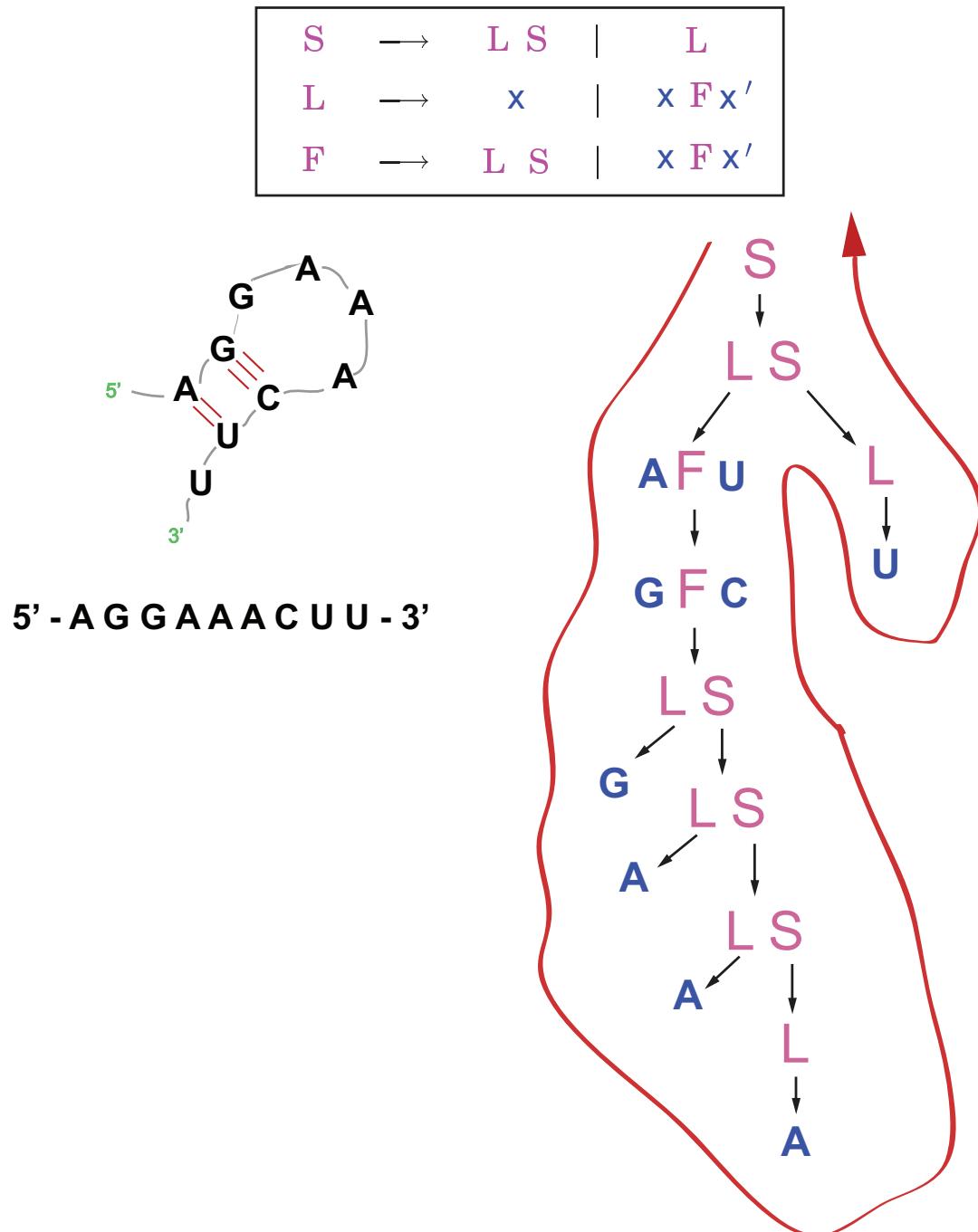
for RNA secondary structure

G6 [Pfold]



Hein & Knudsen, 1999  
Dowell & Eddy, 2004

# G6 structure generation



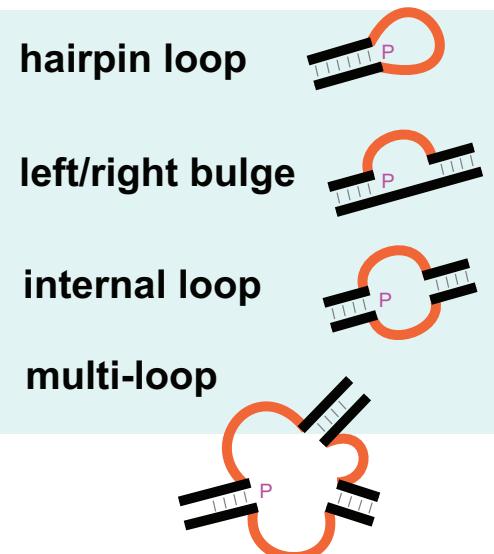
# A “basic” complex grammar

$$S \rightarrow a \quad S \quad | \quad F0 \quad S \quad | \quad \epsilon$$

$$\begin{array}{l} F0 \rightarrow a \quad F5 \quad a' \quad \text{---} \quad \text{a new helix starts} \\ F5 \rightarrow a \quad F5 \quad a' \quad \text{---} \quad \text{helix extends by a basepair} \end{array}$$

$$F5 \rightarrow a \quad P \quad a' \quad \text{---} \quad \text{a helix ends} \quad \text{---} \quad \text{inside a helix....}$$

$$\begin{array}{l} P \rightarrow a_1 \dots a_n \\ P \rightarrow a_1 \dots a_n \quad F0 \\ P \rightarrow F0 \quad a_1 \dots a_n \\ P \rightarrow a_1 \dots a_n \quad F0 \quad a_{n+1} \dots a_m \\ P \rightarrow M1 \quad M \end{array}$$



$$\begin{array}{l} M \rightarrow M1 \quad M \quad | \quad R \\ M1 \rightarrow a \quad M1 \quad | \quad F0 \\ R \rightarrow R \quad a \quad | \quad M1 \end{array}$$

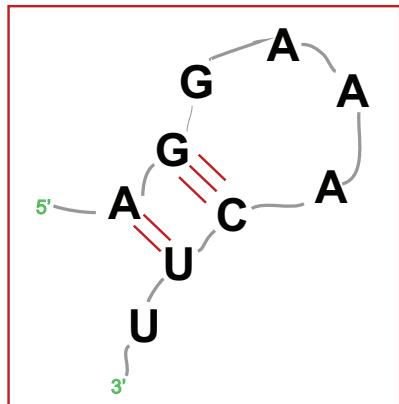
# Scoring Schemes

## Thermodynamic versus Statistical

Thermodynamic

$\Delta G$  (Kcal/mol)

er, SantaLucia, Freier, Zuker, 1987)



dangles off A=U = - 0.16

C stacked on A=U = - 3.41

hairpin loop of 4 nts = + 9.09

AA stability bonus = - 3.97

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Final  $\Delta$ Free Energy = + 1.55 Kcal/mol

# Scoring Schemes

## Thermodynamic versus Statistical

# Thermodynamic

$\Delta G$  (Kcal/mol)

(Turner, SantaLucia, Freier, Zuker, 1987)

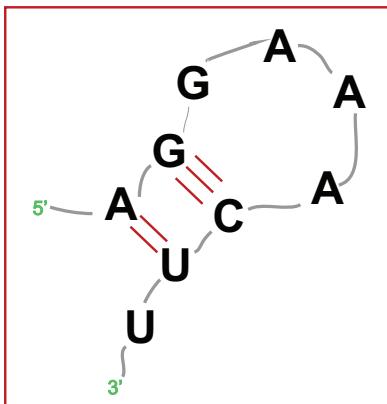
**U      dangles off A = U = - 0.16**

**G≡C stacked on A≡U = -3.41**

hairpin loop of 4 nts      = + 9.09

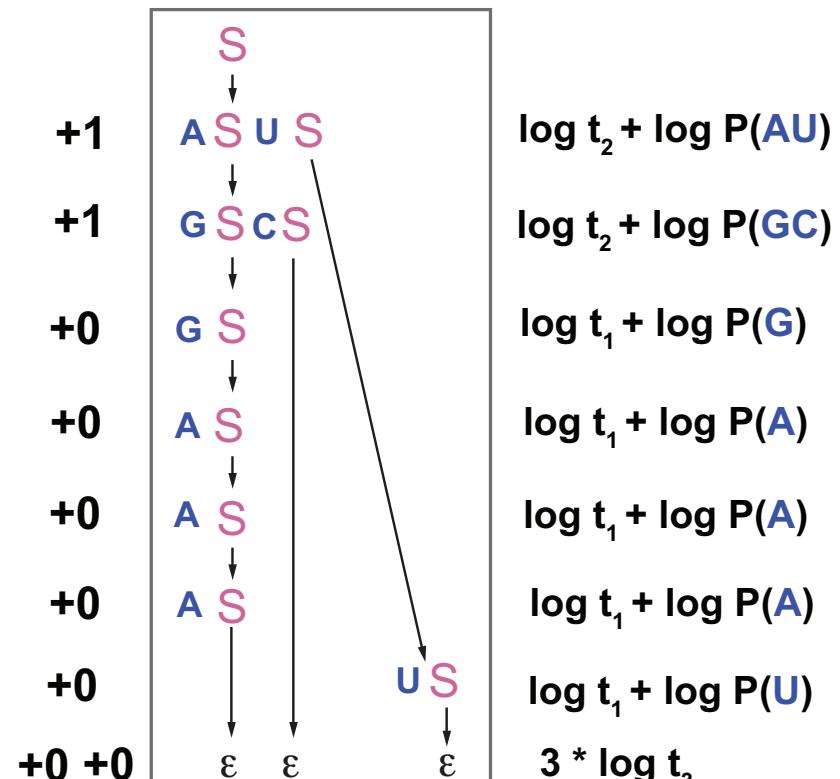
GAAA stability bonus = -3.97

Total ΔFree Energy = + 1.55 Kcal/mol



## Statistical

<b>S</b>	$\longrightarrow$	<b>x S</b>		<b>x S x' S</b>		<b><math>\varepsilon</math></b>	
transition probabilities	$t_1$	(0.5)		$t_2$	(0.24)	$t_3$	(0.26)
emission probabilities	$P(a)$ =0.25			$P(AU \text{ or } GC \text{ or } GU)=1/6$			



$$+2 \quad \log P(\text{total}) = \sum(\text{all the terms}) \\ = -23.5 \quad (6 \times 10^{-11})$$

# Free Energies ≈ log Probabilities

# Going beyond thermodynamic models

One **complicated** thermodynamic model to several **simple probabilistic** models

Thermodynamic models outperform Probabilistic models

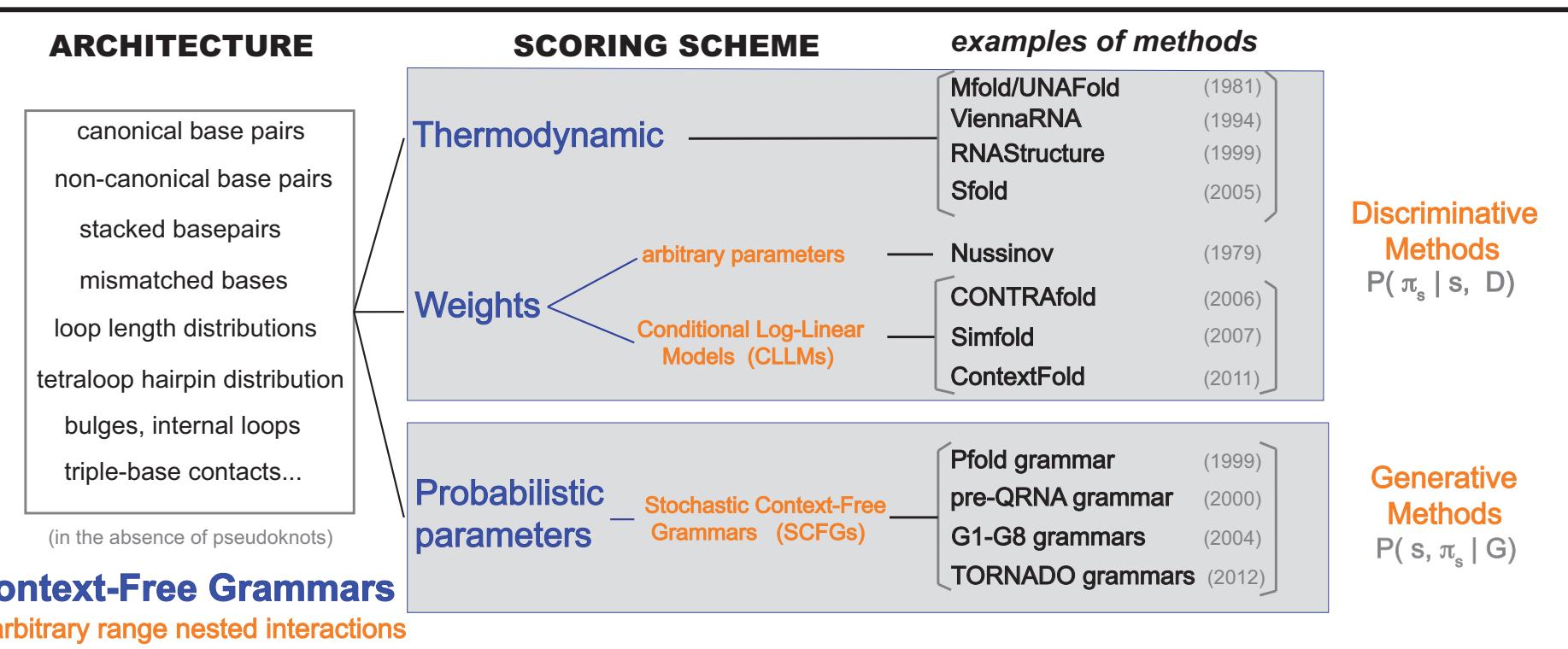
Grammar	Parameters	Folding Accuracy	Scoring Scheme
G6	21	48 %	probabilistic
ViennaRNA	~14,000	54 %	Thermodynamic

Still performance is poor

Previous literature claimed: probabilistic models are **too constrained and cannot** implement all the complexities of the thermodynamic models. Need to move to other type of statistical methods.

# Disentangle

## architecture from scoring scheme



# Why Statistical Models?

specifically with probabilistic parameters

Statistical models **learn** parameters from known RNA structures which is an **ever-growing** source of information versus the **slowly-produced** thermodynamic parameters.

Advantage of statistical **probabilistic** models:

Easily Trainable

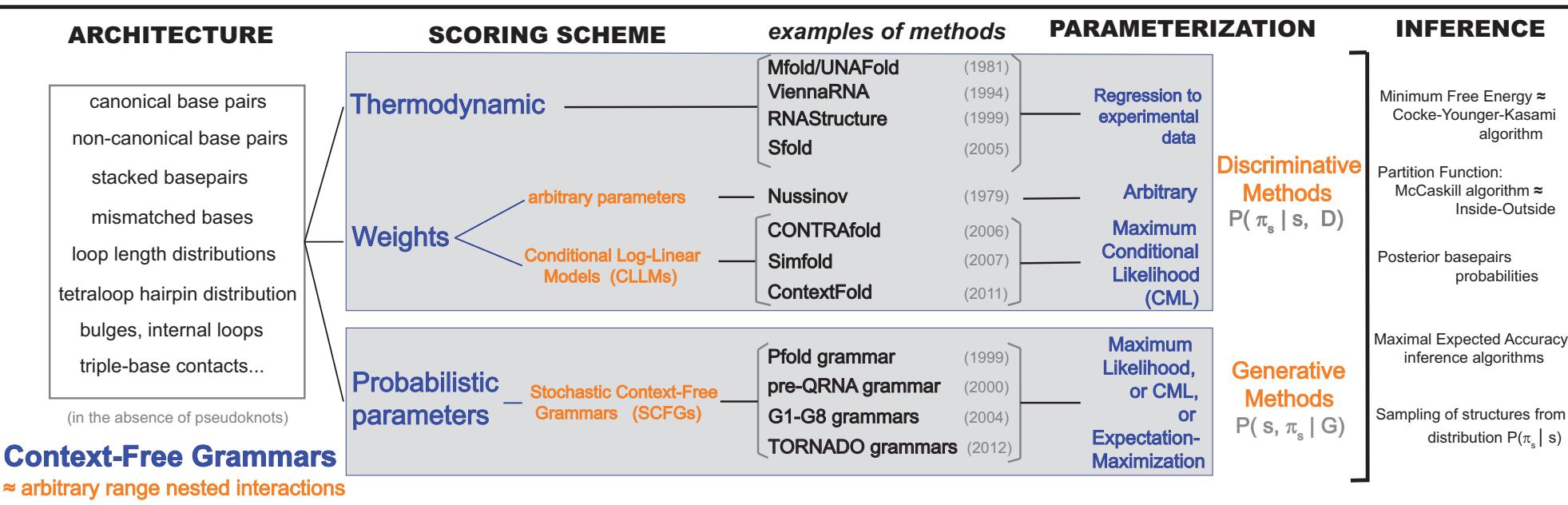
Generative

Optimal comparison of alternative hypotheses

(Neyman & Pearson '33)

Easy integration of complementary sources of information

# THE 4 INGREDIENTS



PARAMETERIZATION  
specific for the different scoring schemes

INFERENCE  
formally identical algorithms for all scoring schemes

# INFERENCE ALGORITHMS

**PROBABILISTIC**

**CYK algorithm**

**Inside algorithm**

**THERMODYNAMIC**

**Minimum Free Energy**

**McCaskill algorithm**

Outside algorithm

Posterior decoding algorithms

Maximum Expected Accuracy inference algorithm

Sampling of structures from the distribution  $P(\pi|seq)$

Same algorithms for all scoring systems

$L^3$  in time

$L^2$  in memory

# TORNADO

tool to swap ingredients

Architecture

Scoring scheme

Parameterization

Folding algorithm

Relative performance of probabilistic  
versus thermodynamic scores?

Hold architecture fixed, vary scoring schemes

Contribution of the different elements of  
RNA 2D structure?

Hold architecture, hold everything else fixed

# Existing complex grammars

have created TORNADO “emulations” of the state of the art RNA models that exist to date.

ViennaRNA  
thermodynamic

14,000 parameters

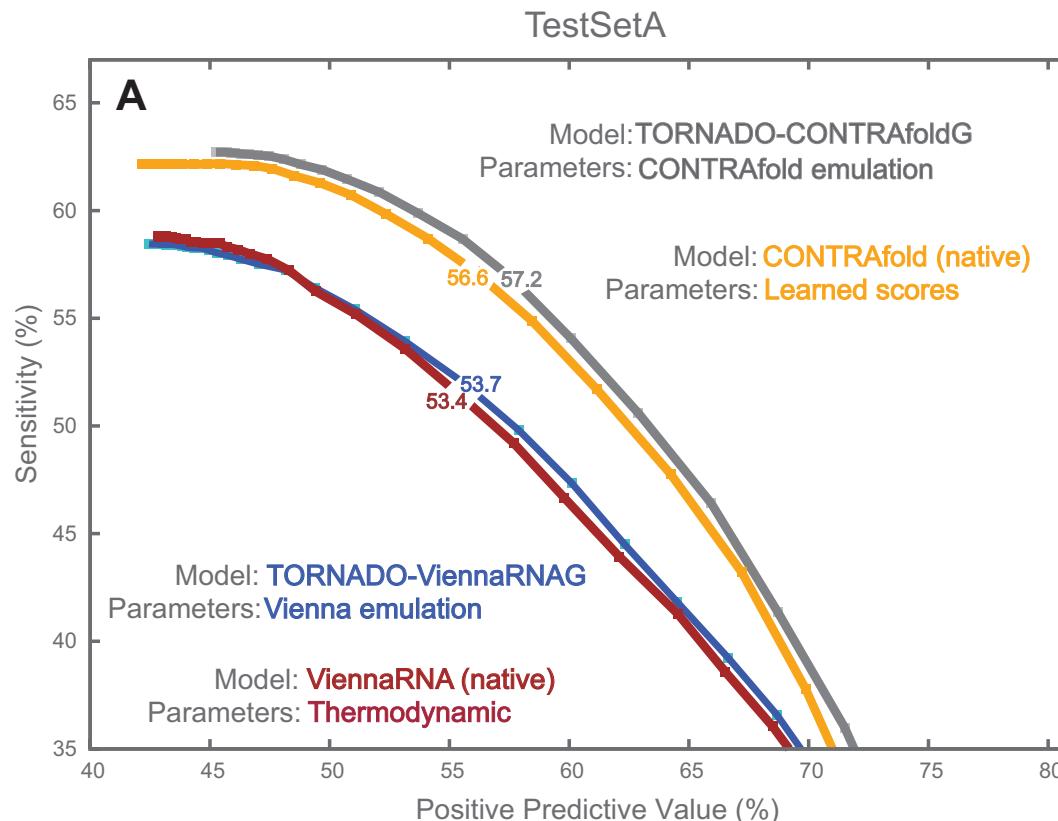
ViennaRNA-G  
TORNADO grammar

CONTRAFold  
learned parameters

1,500 parameters

CONTRAFold-G  
TORNADO grammar

# Context-free grammars reproduce the complexity of the thermodynamic nearest-neighbor model



Sensitivity

= fractions of true basepairs predicted correctly

Positive Predictive Value = fraction of predicted basepairs that are correct

# Probabilistic Complex Grammars

What happens if now one turns the parameters of these models into **probabilities** trained using known RNA structures?

# Parameterization

## Training and test sets

### Literature-Based

Dowell&Eddy, 2004; Do et al, 2006; Andronescu et al, 2007;  
Lu et al, 2009; Andronescu et al, 2010.

3166 Sequences  
48 % basepaired  
< 0.1 % non-canonical

- SSU/LSU domains (1004)
- tRNA (157)
- SRP RNA (215)
- RNaseP RNA (150)
- tmRNA (266)
- 5S RNA (112)
- group I introns (50)
- group II introns (4)
- telomerase RNA (12)
- <50 nts hairpins (962)
- other structures (234)

TrainSetA

697 Sequences  
52 % basepaired  
2.3 % non-canonical



TestSetA

SSU/LSU domains (135)  
tRNA (140)  
SRP RNA (31)  
RNaseP RNA (29)  
tmRNA (63)  
5S RNA (50)  
group I introns (28)  
group II introns (4)  
telomerase RNA (30)  
<50 nts hairpins (179)  
other structures (8)

structurally  
dissimilar



### Rfam-based

22 RNA families with 3D structure

1094 Sequences  
46 % basepaired  
4.8 % non-canonical



- 5.8S rRNA (41)
- U1 (40)
- U2 (32)
- 7 Riboswitches (365)
- 9 Cis regulatory RNAs (575)
- 2 Ribozymes (41)

TrainSetB

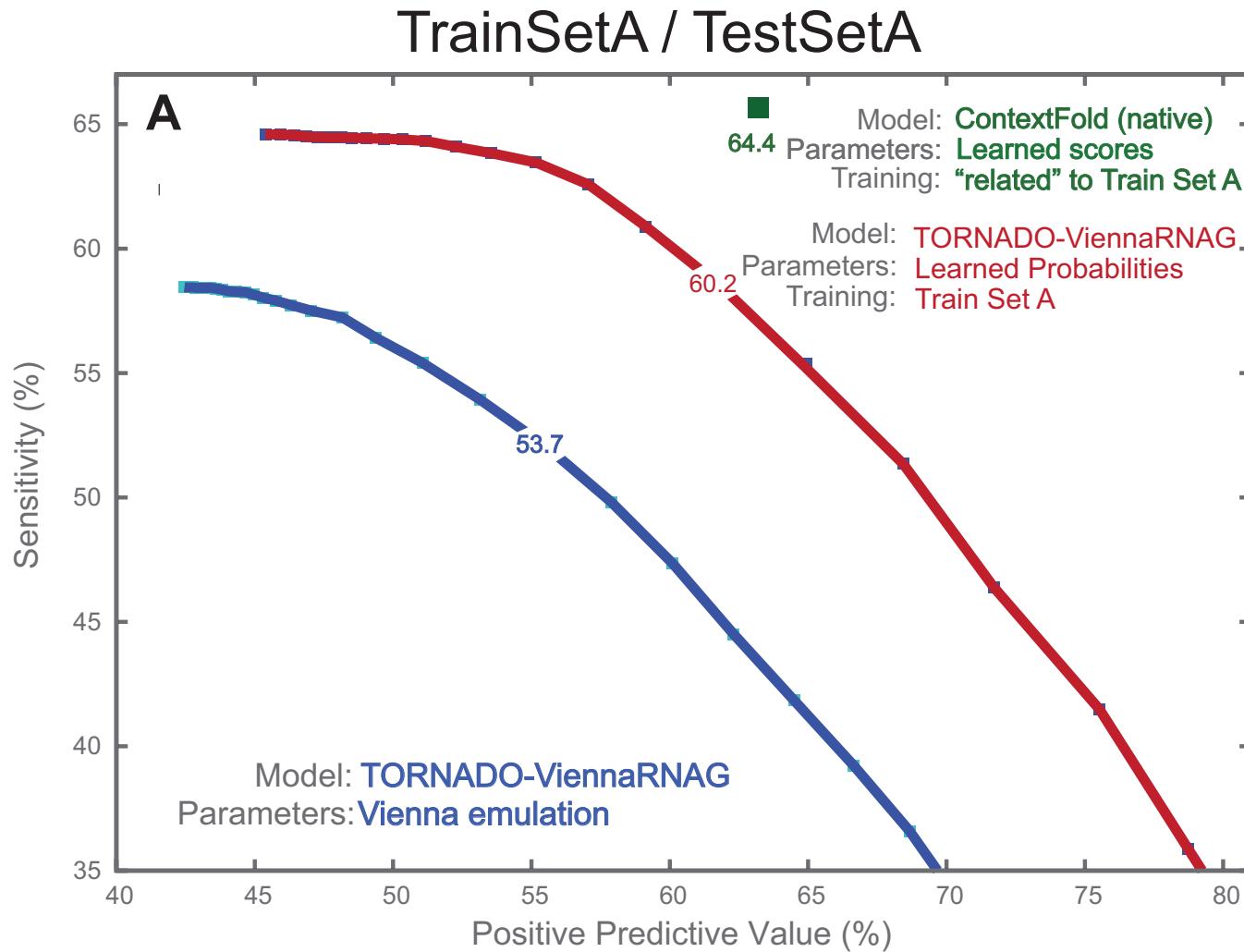
430 Sequences  
44 % basepaired  
8.3 % non-canonical



TestSetB

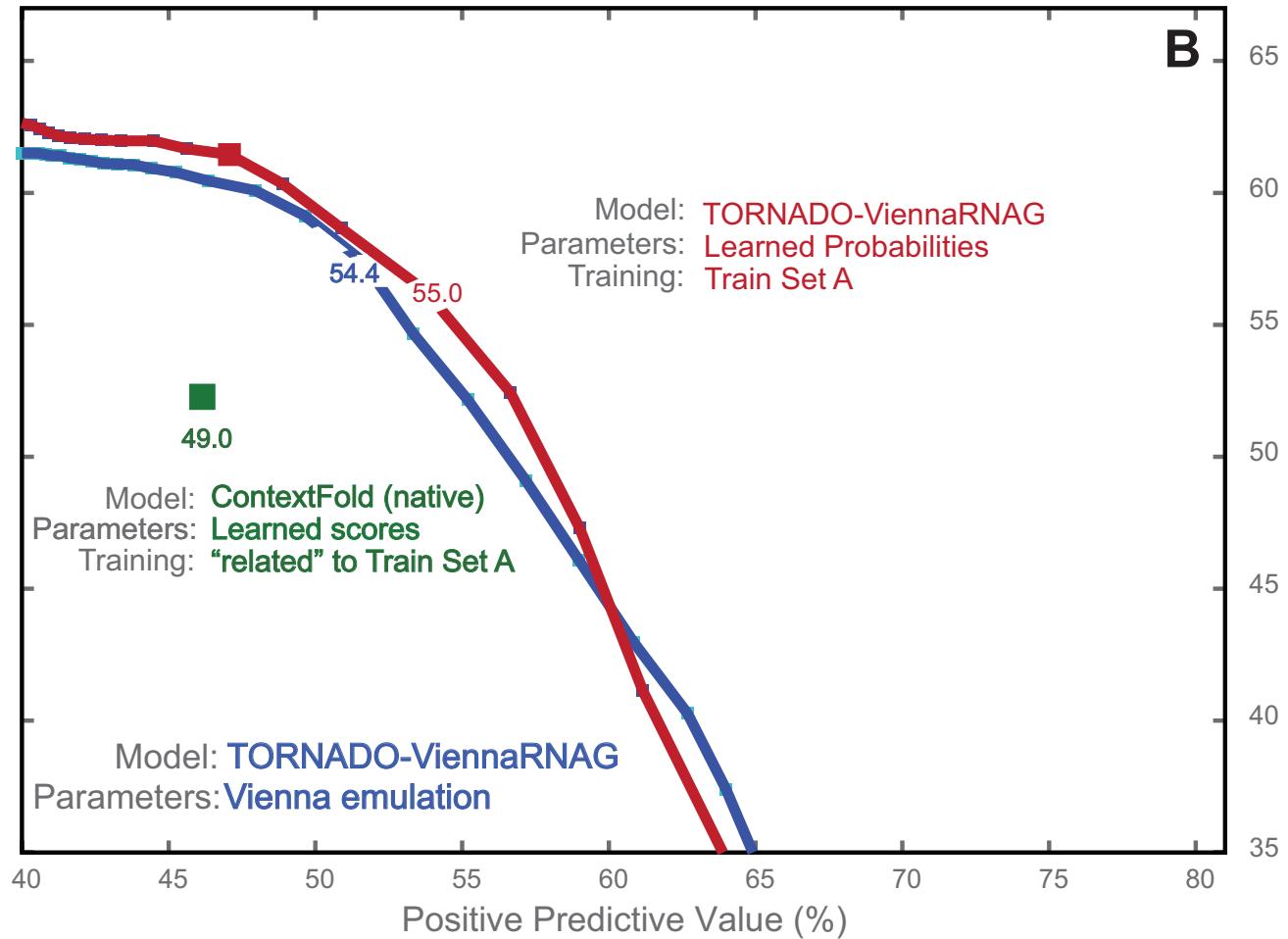
- 5.8S rRNA (14)
- U1 (18)
- U2 (45)
- 7 Riboswitches (233)
- 9 Cis regulatory RNAs (116)
- 2 Ribozymes (3)
- bacteriophage pRNA (1)

# Benchmark on same structures



# Benchmark on different structures

TrainSetA / TestSetB



Need to train in one type of structures and test on a completely different set

# Folding Accuracy

## METHOD

METHOD	ARCHITECTURE		SCORING SCHEME	PARAMETERIZATION	FOLDING METHOD	BENCHMARK	
	# free tied parameters (6 bps)	(16 bps)				set best F (%)	TestSetA
Basic grammar	11	21	probabilistic	maximum likelihood	c-MEA	49.1	47.5
CONTRAfold v2.02	532	572	probabilistic	maximum likelihood	c-MEA	56.9	56.5
CONTRAfoldG	~300	—	weights	maximum cond. likelihood	c-MEA	57.2	57.9
NAFold-3.8	1,278	5448	probabilistic	maximum likelihood	c-MEA	58.3	58.6
mfold BL	~3,500	—	thermodynamic	fit to exp. data	CYK	51.0	51.3
NAstructure v5.2	~3,500	—	weights	maximum cond. likelihood	CYK	56.5	55.3
EnnRNA v1.8.4	12,700	—	thermodynamic	fit to exp. data	GCE	53.5	53.8
EnnRNAAG	12,700	—	thermodynamic	fit to exp. data	GCE	53.7	54.3
EnnRNAAG_plus	14,307	90,497	probabilistic	maximum likelihood	c-MEA	60.2	59.4
contextFold v1.00	14,557	91,997	probabilistic	maximum likelihood	c-MEA	60.5	59.5
CONTRAfold v2.02	205,000	—	weights	maximum cond. likelihood	CYK	64.4	49.0

Probabilistic methods implemented in TORNADO

Contrafold  
58%

Thermodynamic  
54%

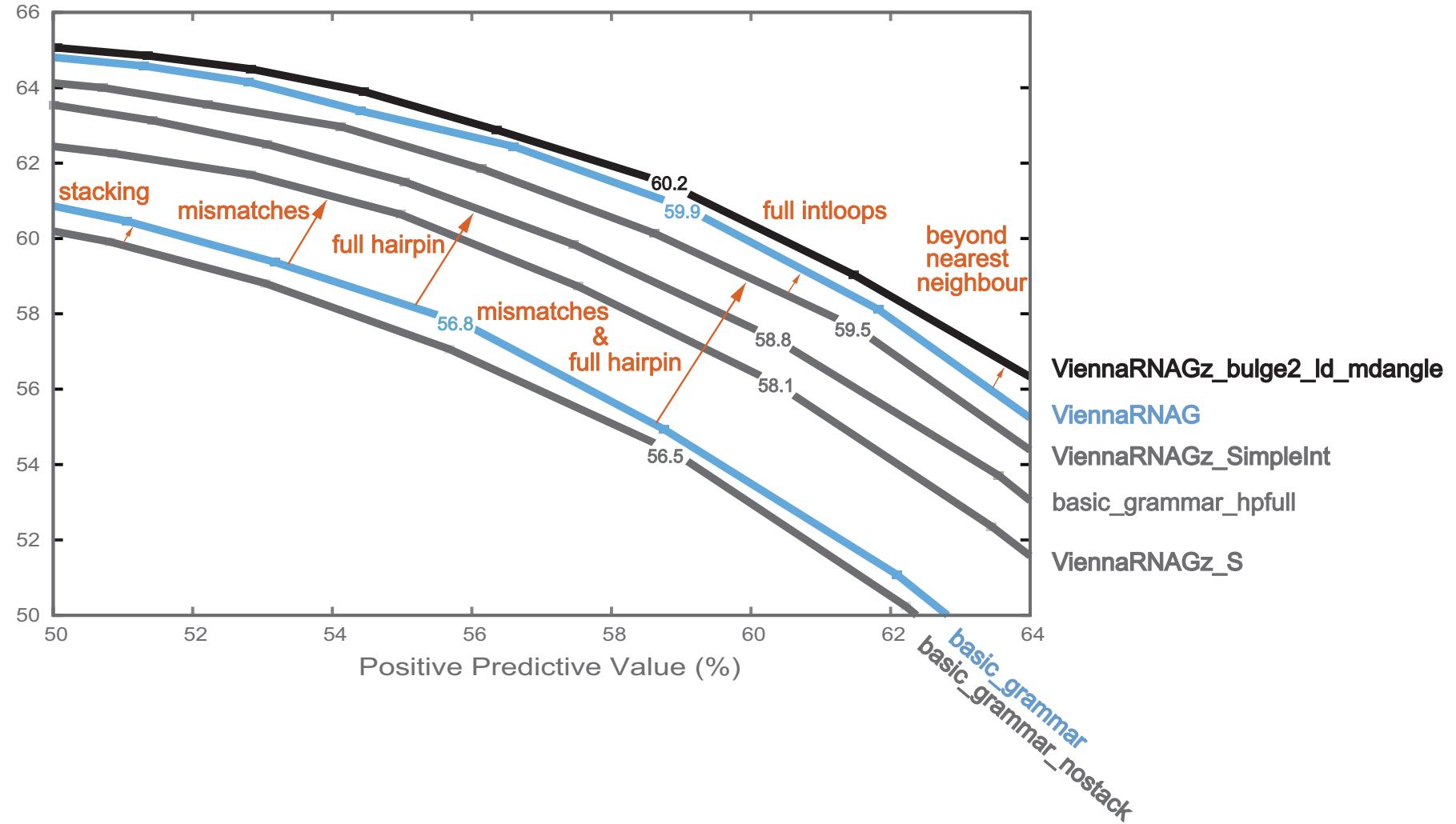
SCFGs  
60%

# A gradation of SCFGs

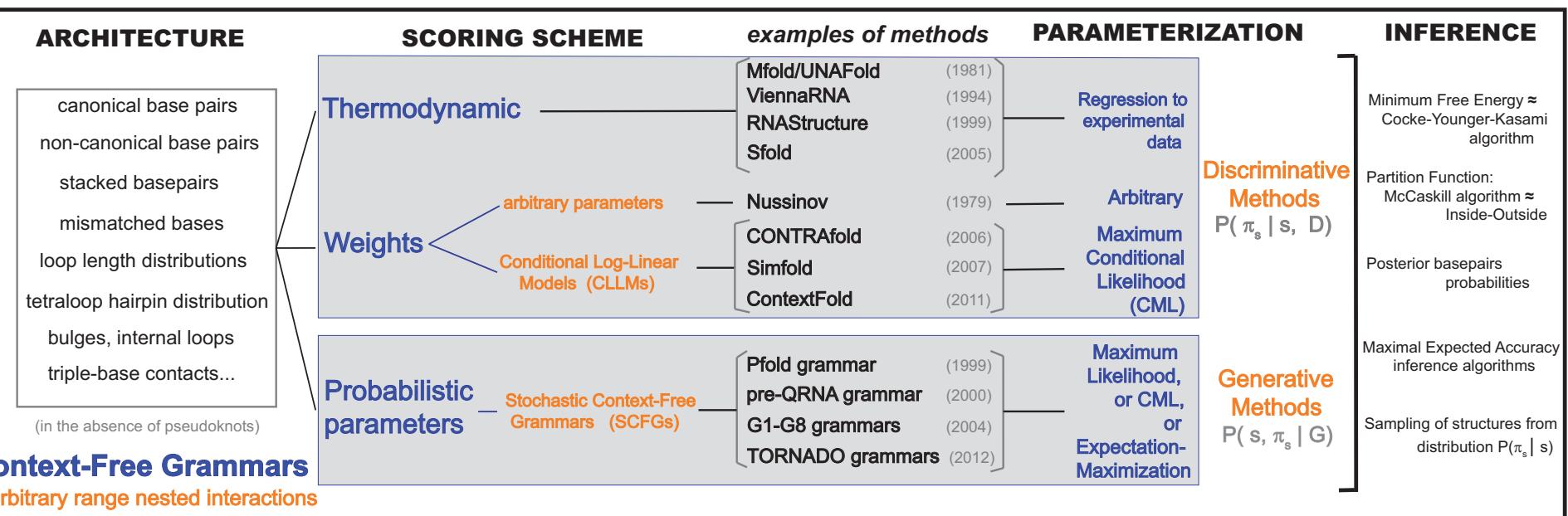
## exploring different structural features

Grammar	Total Free Tied Parameters		Remarks
	4x4 bps	6 bps	
<b>g6</b>	21	11	Pfold grammar
g6s	261	41	Pfold + stacking
g6_stem	294	74	Pfold + stacking + helix length dist.
basic_grammar_nostack	572	532	loop length dist.
<b>basic_grammar</b>	1,022	582	loop length dist + stacking.
basic_grammar_dangle	1,143	643	basic_grammar + dangles
ViennaRNAGz_S	1,862	892	ViennaRNAGz_SimpleInt without tetraloops
CONTRAfoldGS	2,101	811	CONTRAfoldG with simpler 1nt bulges
basic_grammar_hpfull	5,342	2,202	basic_grammar + hairpin tetraloops + hairpin closing mismatches
<b>CONTRAfoldG</b>	5,448	1,278	CONTRAfold emulation
ViennaRNAGz_SimpleInt	6,105	2,495	ViennaRNAG minus 2x2,2x1 Internal loops
ViennaRNAGz_nostack	90,497	14,257	ViennaRNAG minus stacking
<b>ViennaRNAG</b>	90,947	14,307	ViennaRNA emulation
ViennaRNAGz_stem	90,980	14,340	ViennaRNAG + stem length dist.
ViennaRNAGz_bulge2	91,670	14,400	ViennaRNAG + explicit 1,2 bulges
ViennaRNAGz_ld	91,012	14,374	ViennaRNAG + all emissions by length dist
ViennaRNAGz_mangle	91,187	14,397	ViennaRNAG + multiloop mismatches
ViennaRNAGz_bulge2_ld_mdangle	91,977	14,557	ViennaRNAG + explicit 1,2 bulges + + all length dist + multiloop mismatches

# tacking less important than expected



# The four ingredients of single-sequence RNA secondary structure prediction



**TORNADO allows us to select all four ingredients independently**

- (1) Probabilistic models can describe **the complex features** of the nearest-neighbor model of RNA folding and more
- (2) Probabilistic models are **easily trainable** on known data, while they use identical algorithms for inference
- (3) Probabilistic models (trained properly) **perform as well or better. Performance ceiling.**

# Complex model easily overfit

Complex RNA models **learn** many features of the structures  
Adequate benchmarking requires to use **training sets** with  
**different folds** than those in **testing sets**

# Last Thought

All methods, thermodynamic or statistic (both probabilistic and weighted), can be formally expressed as context-free grammars, thus the architecture is independent of the scoring scheme.

RNA Folding Servers to also include probabilistic scorings?