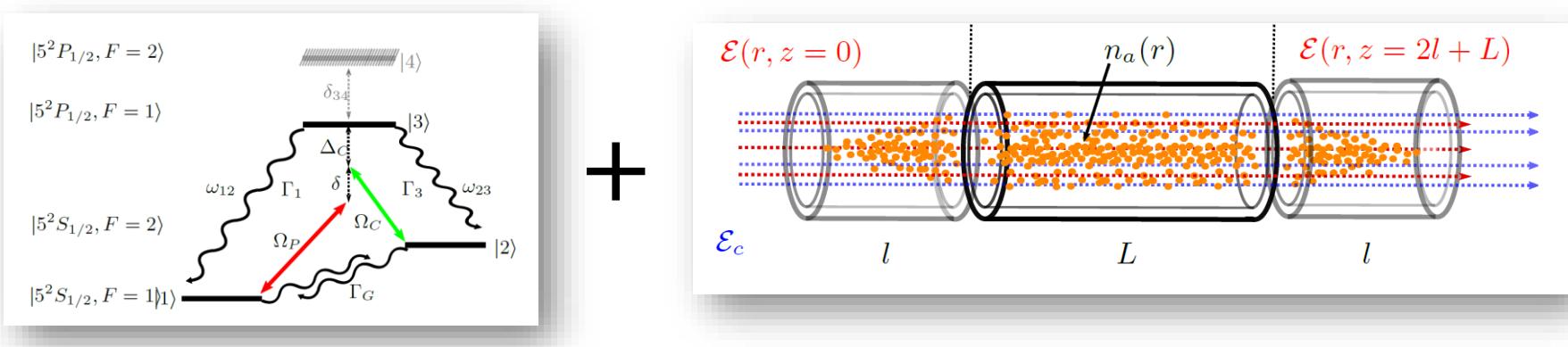


Optimal pulse propagation in an inhomogeneously gas-filled hollow-core fiber



Tight 2D transverse confinement of atoms & light



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Content



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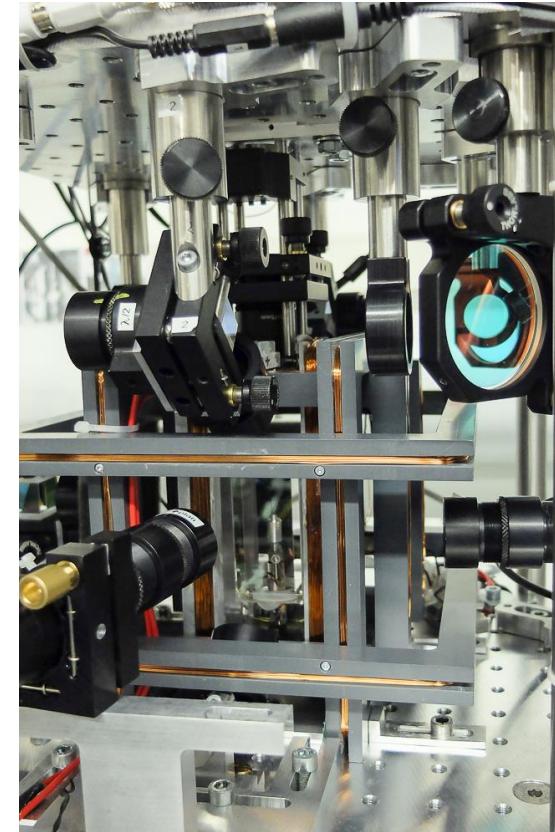
1. Experimental setup
2. Electromagnetically induced transparency
3. Light propagation in a HCF
4. Pulse characterisation in frequency and time
5. Mitigation of lensing effects

Experiment: Tight 2D transverse confinement of atoms & light

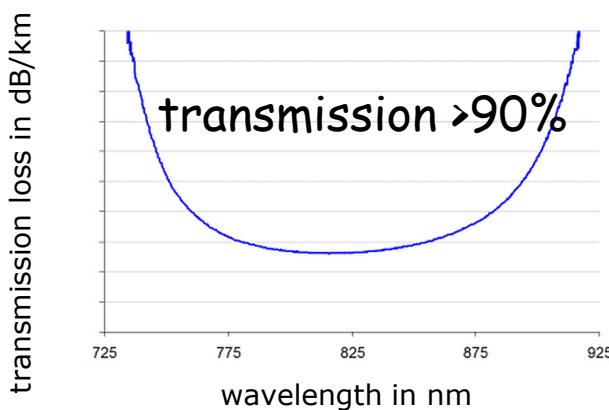
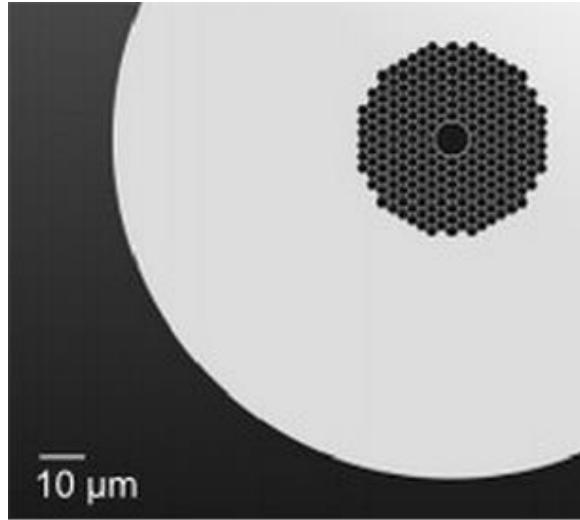
Thorsten Peters



thorsten.peters@physik.tu-darmstadt.de
<http://www.iap.tu-darmstadt.de/nlq/team/>



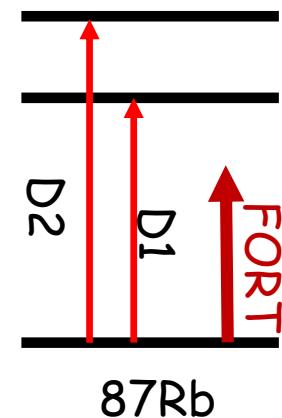
Hollow-core photonic bandgap fiber



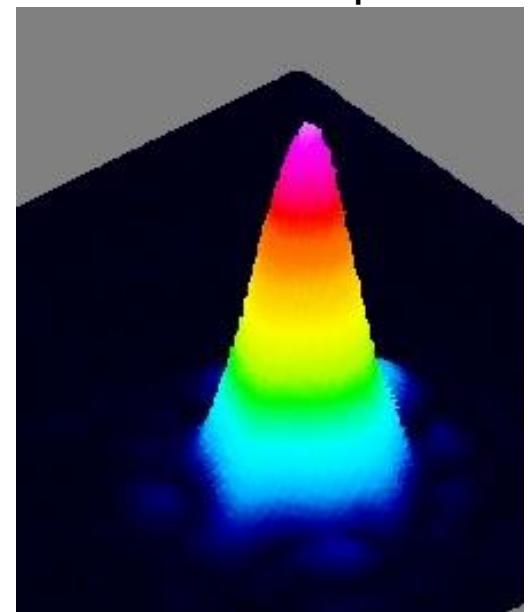
Physical properties

Core diameter ⁽¹⁾	$7.5 \mu\text{m} \pm 1 \mu\text{m}$
Pitch	$2.3 \mu\text{m}$

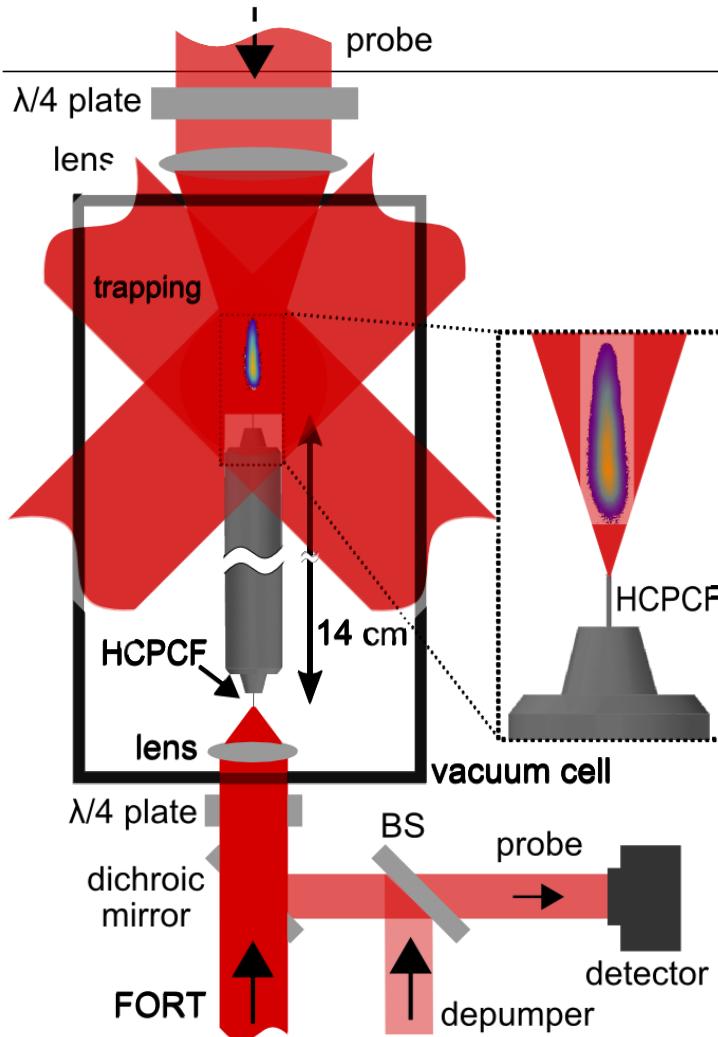
NA = 0.1



near Gaussian profile



Putting atoms into a tube



2 ECDLs @ 780 nm
each 100 mW
 $I \sim I_{\text{sat}}$

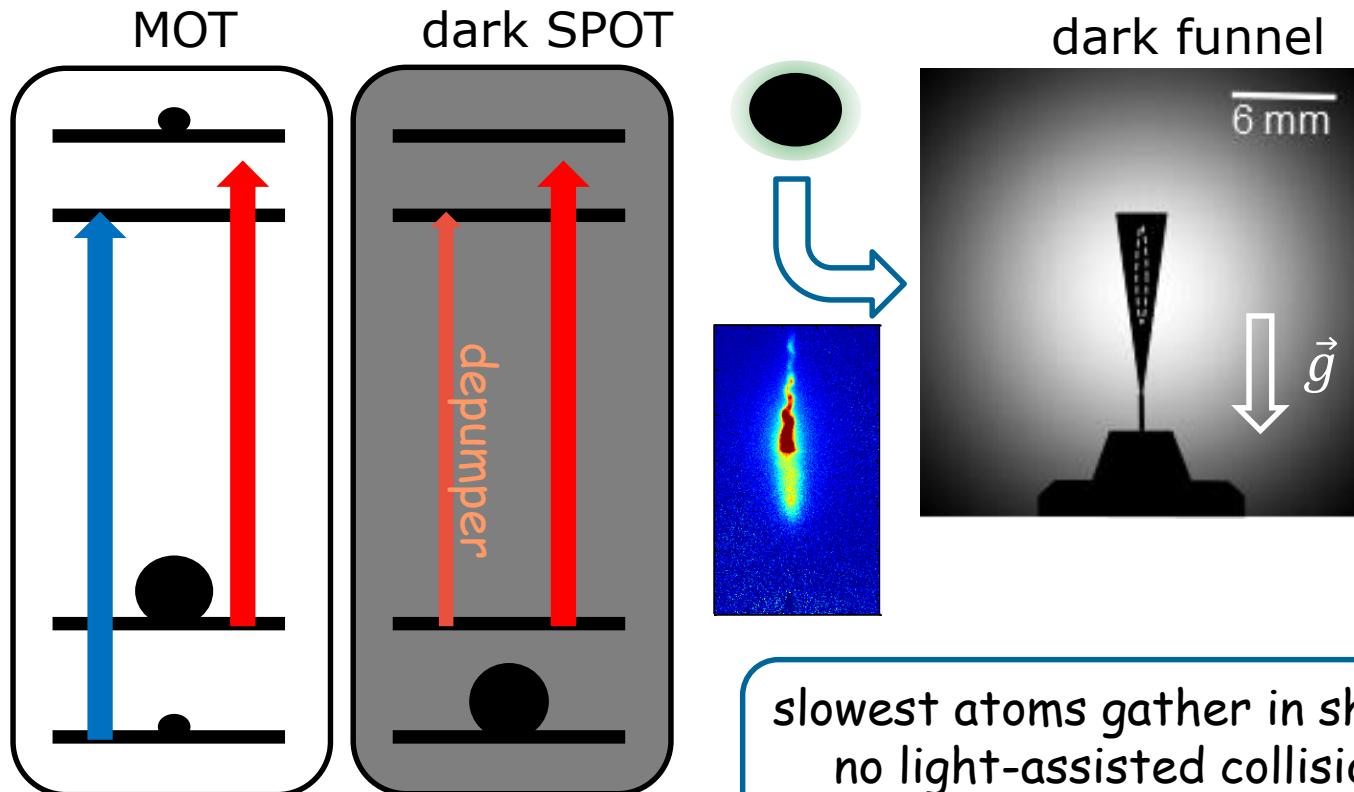
$N \sim 1E7$
 $T \sim 120 \mu\text{K}$
 $V \sim 5 \times 0.8^2 \text{ mm}^3$

FORT:
1 W TA system @
855 nm,
270 mW in fiber

Guiding atoms to the fiber

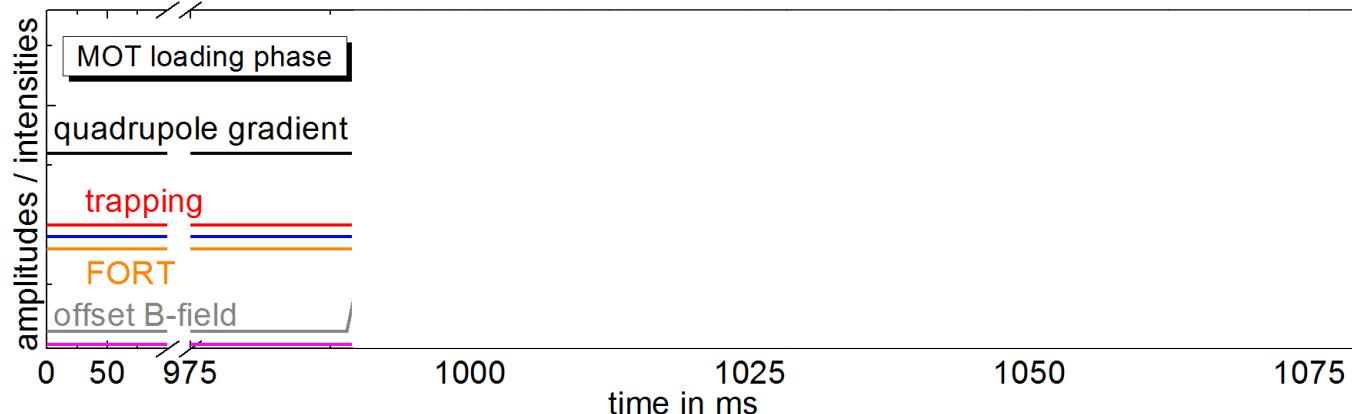
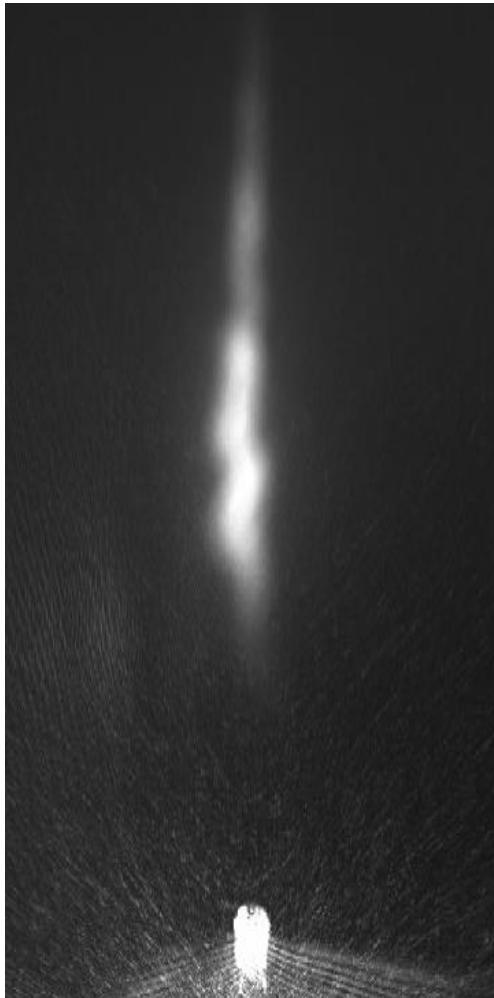


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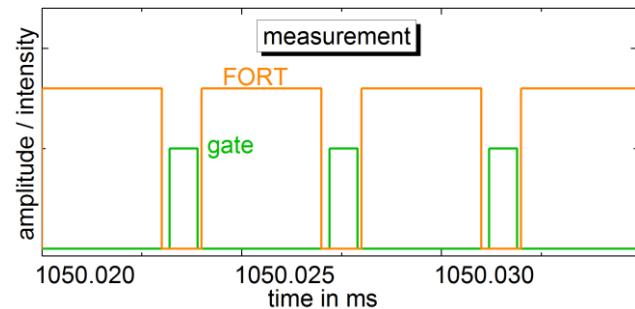
slowest atoms gather in shadow
no light-assisted collisions
► density increases

HCF loading sequence



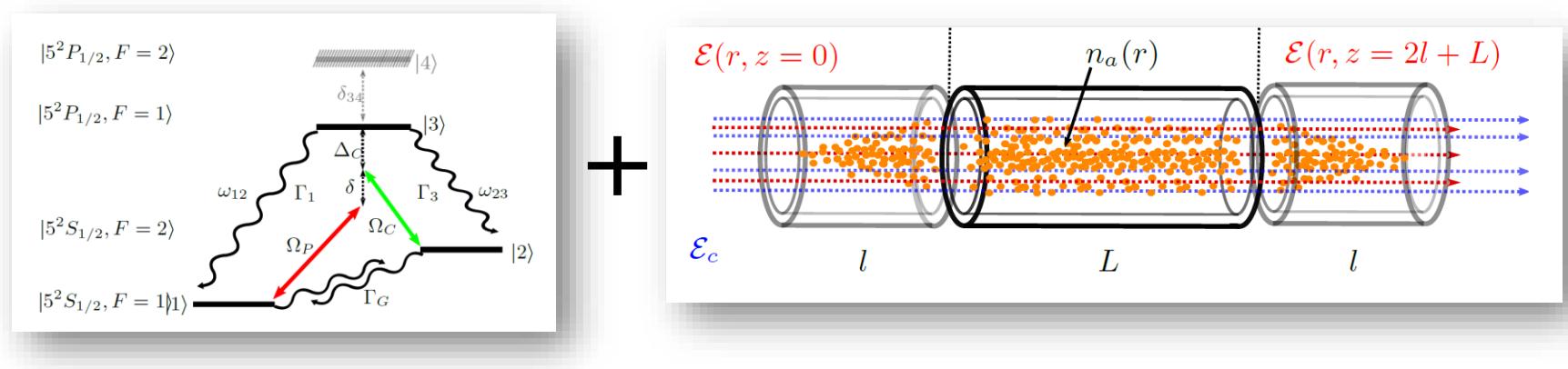
„purge“ repumper:
pump atoms
above fiber to $F=2$
detect atoms
in $F=1$

measurement sequence



F. Blatt, Th. Halfmann, and Th. Peters, "One-dimensional ultracold medium of extreme optical depth," Opt. Lett. **39**, 446-449 (2014)

Theory: Tight 2D transverse confinement of atoms & light



Crystallization of strongly interacting photons in a nonlinear optical fibre

D. Chang, V. Gritsev, G. Morigi, V. Vuletić, M. Lukin, E. Demler, Nature Physics 4, 884 (2008)

Quantum transport of strongly interacting photons in a one-dimensional nonlinear waveguide

M. Hafezi, D. Chang, V. Gritsev, E. Demler, M. Lukin Phys. Rev. A 85, 013822 (2012)

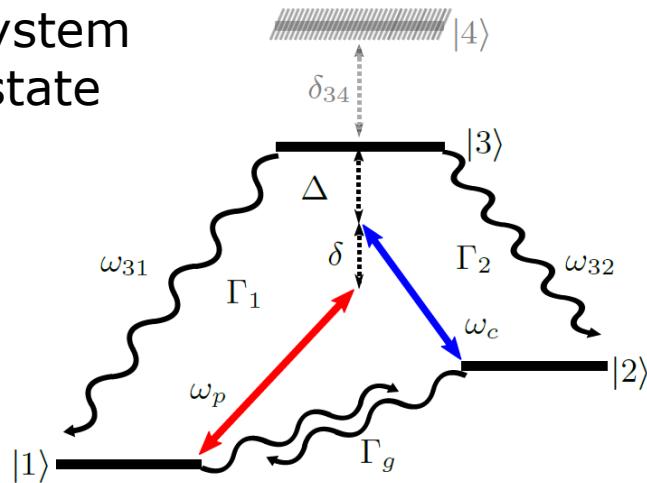
Quantum nonlinear optics — photon by photon

D. Chang, V. Vuletić, M. Lukin, Nature Photonic 8, 685 (2014)

Atomic Raman transitions



Three level system
with ground state
dephasing



Rotating wave Hamilton matrix:

$$H' = \hbar \begin{pmatrix} \Delta + \delta & 0 & \frac{\Omega_p^*}{2} \\ 0 & \Delta & \frac{\Omega_c^*}{2} \\ \frac{\Omega_p}{2} & \frac{\Omega_c}{2} & 0 \end{pmatrix}$$

Two-photon detuning: $\delta = \omega_p - \omega_c - \omega_{21}$

One-photon detuning: $\Delta = \omega_c - \omega_{32}$

Dark state: decouples from interaction

$|D\rangle = \cos \theta |1\rangle - \sin \theta |2\rangle$ at mixing angle: $\tan \theta = \Omega_p / \Omega_c$.

Dynamics with dissipation

Master equation

$$\dot{\hat{\rho}} = -\frac{i}{\hbar}[H', \hat{\rho}] + \sum_{i=1}^2 \Gamma_i (\hat{\sigma}_{i3} \hat{\rho} \hat{\sigma}_{i3}^\dagger - \frac{1}{2} \hat{\sigma}_{i3}^\dagger \hat{\sigma}_{i3} \hat{\rho} - \frac{1}{2} \hat{\rho} \hat{\sigma}_{i3}^\dagger \hat{\sigma}_{i3}) \\ + \Gamma_g (\hat{\sigma}_{ii} \hat{\rho} \hat{\sigma}_{ii} - \frac{1}{2} \hat{\sigma}_{ii} \hat{\rho} - \frac{1}{2} \hat{\rho} \hat{\sigma}_{ii})$$

Rearranging the 9 matrixelements

$$\boldsymbol{\varrho} = (\rho_{11}, \rho_{12}, \rho_{13}, \rho_{21}, \rho_{22}, \rho_{23}, \rho_{31}, \rho_{32}, \rho_{33})$$

$$\partial_t \boldsymbol{\varrho} = iL\boldsymbol{\varrho}, \quad \text{Stationary state} \quad L = \begin{pmatrix} 0 & 0 & \frac{\Omega_p}{2} & 0 & 0 & 0 & -\frac{\Omega_p^*}{2} & 0 & -i\Gamma_1 \\ 0 & i\Gamma_g - \delta & \frac{\Omega_c}{2} & 0 & 0 & 0 & 0 & -\frac{\Omega_p^*}{2} & 0 \\ \frac{\Omega_p^*}{2} & \frac{\Omega_c^*}{2} & i\frac{\Gamma_t}{2} - \delta - \Delta & 0 & 0 & 0 & 0 & 0 & -\frac{\Omega_p^*}{2} \\ 0 & 0 & 0 & \delta + 2i\Gamma_g & 0 & \frac{\Omega_p}{2} & -\frac{\Omega_c^*}{2} & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & \frac{\Omega_c}{2} & 0 & -\frac{\Omega_p^*}{2} & -i\Gamma_2 \\ 0 & 0 & 0 & \frac{\Omega_p^*}{2} & \frac{\Omega_c^*}{2} & i\frac{\Gamma}{2} - \Delta & 0 & 0 & -\frac{\Omega_c^*}{2} \\ -\frac{\Omega_p}{2} & 0 & 0 & -\frac{\Omega_c}{2} & 0 & 0 & \delta + \Delta + i\frac{\Gamma}{2} & 0 & \frac{\Omega_p}{2} \\ 0 & -\frac{\Omega_p}{2} & 0 & 0 & -\frac{\Omega_c}{2} & 0 & 0 & \Delta + i\frac{\Gamma}{2} & \frac{\Omega_c}{2} \\ 0 & 0 & -\frac{\Omega_p}{2} & 0 & 0 & -\frac{\Omega_c}{2} & \frac{\Omega_p^*}{2} & \frac{\Omega_c^*}{2} & i(\Gamma_1 + \Gamma_2) \end{pmatrix}$$

Electromag. induced transparency



Atomic polarization:

$$\mathbf{P}_p(\omega) = n_a \mathbf{d}_{13} \rho_{31}^s = \epsilon_0 \chi^{(1)}(\omega) \mathbf{E}_p(\omega) + \dots$$

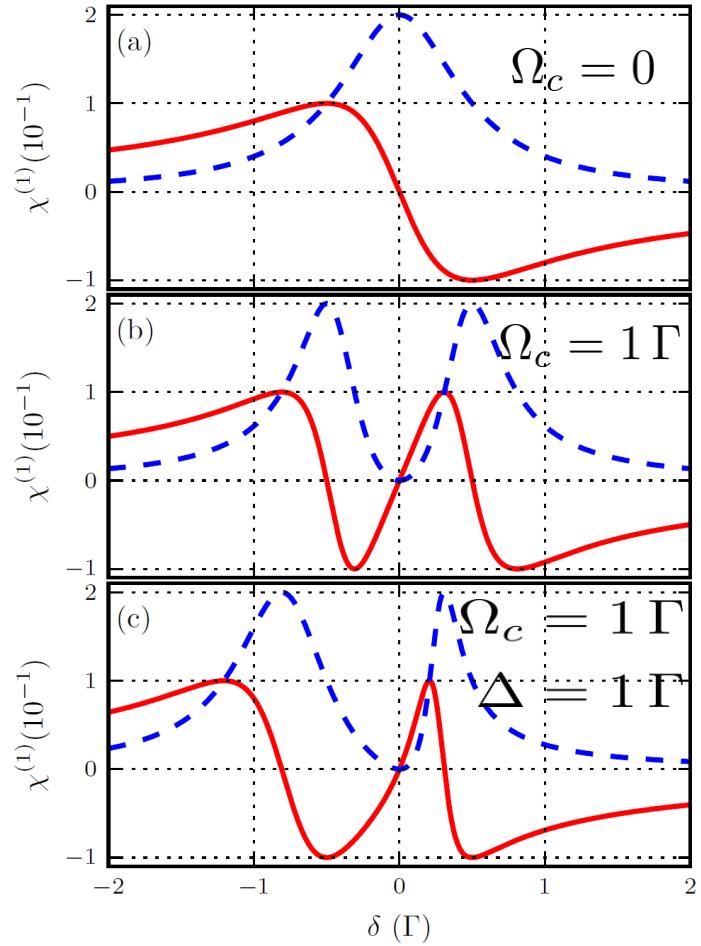
Probe pulse susceptibility:

$$\chi^{(1)} = \chi_0^{(1)} f, \quad \chi_0^{(1)} = n_a \alpha_0, \quad \alpha_0 = \frac{|d_{13}|^2 S_{FF'}}{2\epsilon_0 \hbar \Gamma}$$

$$f = \delta \Gamma \frac{\frac{|\Omega_c|^2}{4} - \delta(\delta + \Delta) + i\delta \frac{\Gamma}{2}}{\left[\frac{|\Omega_c|^2}{4} - \delta(\delta + \Delta)\right]^2 + \delta^2 (\frac{\Gamma}{2})^2}$$

$$= \underline{\delta} \left(1 + \frac{\Delta}{\Gamma} \underline{\delta} \right) + i \frac{\underline{\delta}^2}{2} \left(1 + \frac{2\Delta}{\Gamma} \underline{\delta} \right) + \dots$$

$$\underline{\delta} = \delta / \delta_{\text{EIT}}, \quad \delta_{\text{EIT}} = \frac{|\Omega_c|^2}{4\Gamma}$$



Light propagation in a HCF

inhomogeneous Helmholtz equation: $\varepsilon_r = 1 + \chi$

$$(\nabla^2 + k^2 \varepsilon_r(\mathbf{x}, \omega)) \mathbf{E}_p(\mathbf{x}, \omega) = -\nabla(\mathbf{E}_p \cdot \nabla \log \varepsilon_r),$$

Fiber parameter: $3.5 \mu\text{m} < a_0 < 25 \mu\text{m}$

$$v = \frac{a_0}{\lambda_p} \approx 25 > 1$$

Slowly varying envelope:

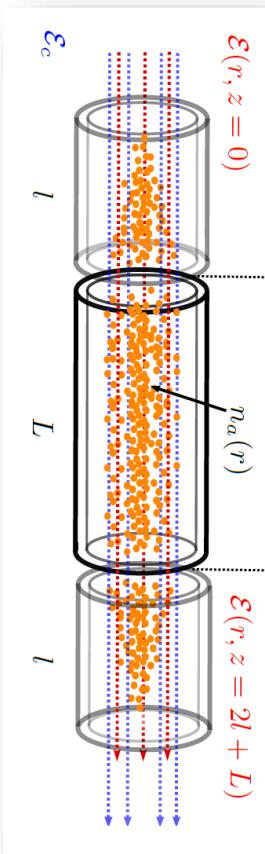
$$\mathbf{E}_p(\mathbf{x}, \omega) = \mathbf{e}_p e^{ik_p z} \mathcal{E}_p(\mathbf{x}, \omega),$$

optical Schrödinger equation $\bar{\lambda} \leftrightarrow \hbar$, $z \leftrightarrow t$:

$$i\bar{\lambda}_p \partial_z \mathcal{E}_p(\mathbf{x}, \omega) = \left[-\frac{\bar{\lambda}^2}{2a_0^2} \Delta_{\perp} - \frac{1}{2} \chi^{(1)}(\mathbf{x}, \omega) \right] \mathcal{E}_p$$

M. Born and E. Wolf, Principles of Optics (Cambridge Univ. Press)

M. Lax, Phys. Rev. A 11, 1365 (1975).



2D modes & complex spectrum



Adiabatic eigenmode

$$\mathcal{E}_p(r, \varphi, z; \delta) = e^{-i\phi(z)} u(r, \varphi, z; \delta) \mathcal{E}_p(\delta),$$

$$\phi(z) = \int_0^z d\zeta q_p \varepsilon(\zeta; \delta)$$

with $q_p = k_p/2v^2$

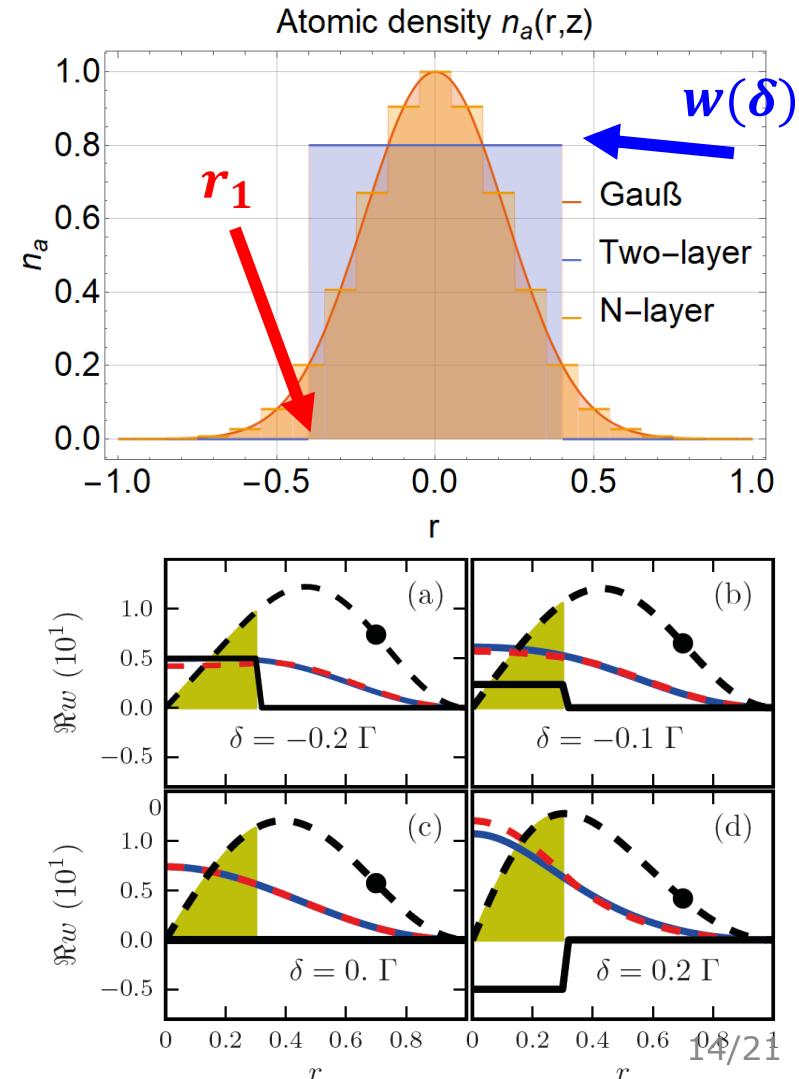
2D Eigen-modes and **complex dispersion**

$$\varepsilon(z; \delta) u(r, z, \varphi; \delta) = [-\Delta_{\perp} + w(r, z; \delta)] u,$$

Optical potential

$$w(r, z; \delta) = -v^2 n_a(r, z) \alpha_0 f(\delta, \Delta, |\Omega_c(r)|),$$

Atomic density: $n_a(r, z) = n_0(z) e^{-\frac{r^2}{\sigma_a^2}}$



Complex dispersion $\varepsilon(\delta)$



Complex transfer function:

$$\mathcal{E}_p^{(\text{out})}(\delta) = \mathcal{T}(\delta)\mathcal{E}_p^{(\text{in})}(\delta),$$

$$\mathcal{T}(\delta) = e^{i\eta + ik(\delta)L}, \quad k(\delta) = k_p - q_p\varepsilon(\delta)$$

Finding the complex dispersion

- Numerically: Gauß density
- Analytically: two-layer density

Homogeneous potential:

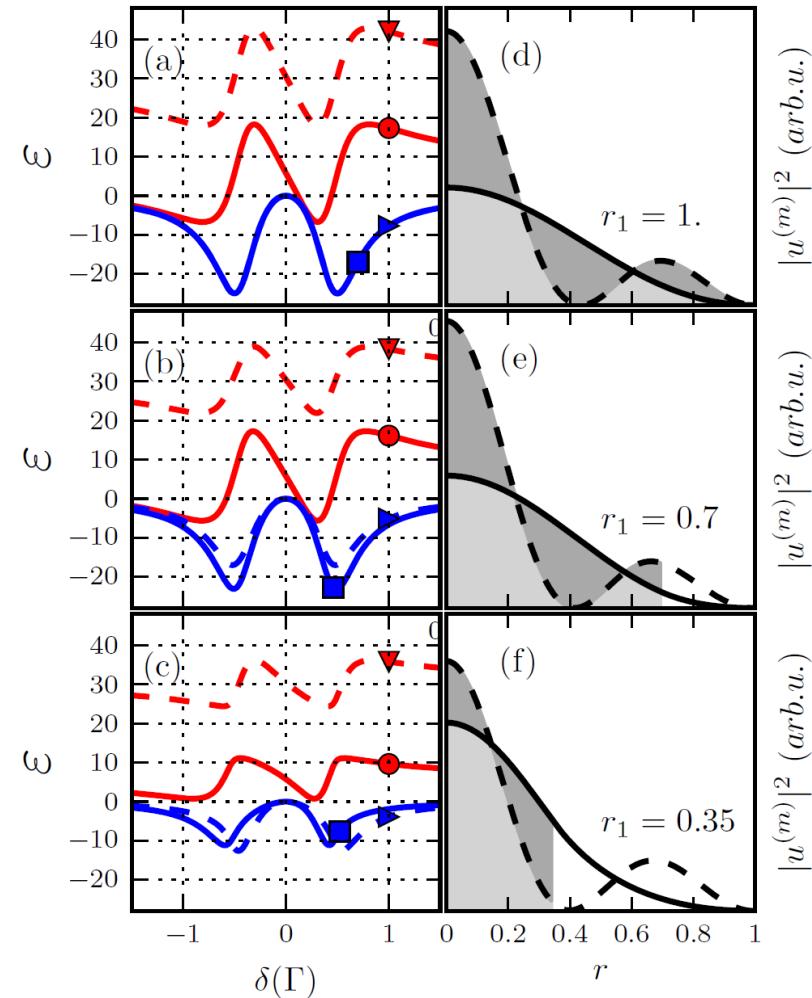
$$u(r) = aJ_0(\kappa r) + bY_0(\kappa r)$$

$$\kappa^2 = \varepsilon - w \in \mathbb{C}$$

Homogeneously filled HCF & BC

$$u^{(m)}(r; \delta) = J_0(j_m r),$$

$$\varepsilon^{(m)}(\delta) = j_m^2 + w(\delta)$$



Implicit function theorem

Implicit function

$$H(w(\delta), \varepsilon(\delta)) = 0$$

Implicit function theorem

$$\partial_{\delta}^n H(w(\delta), \varepsilon(\delta)) = 0$$

Explicit expressions for

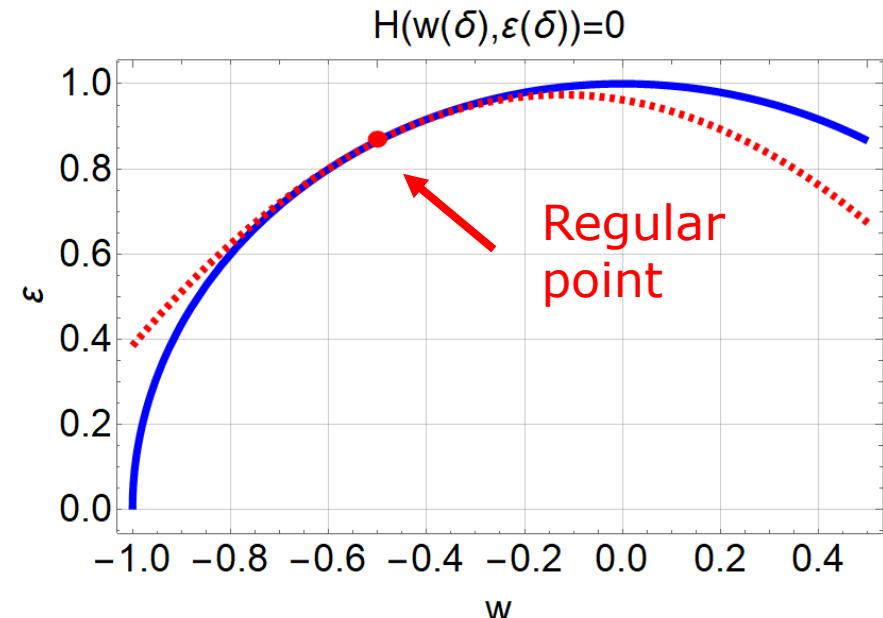
$$\partial_{\delta}^n \varepsilon(\delta = 0)$$

Taylor series for complex dispersion

$$\varepsilon(\delta) = \epsilon + \epsilon' \delta + \frac{\epsilon''}{2} \delta^2 + \mathcal{O}(\delta^3),$$

Two-layer model: quantization condition from boundary condition

$$H = \frac{J_0(\kappa_1 r_1) J_1(\kappa_2 r_1) \kappa_2}{J_0(\kappa_2 r_1) J_1(\kappa_1 r_1) \kappa_1} - \frac{G_0(\kappa_2 r_1) - G_0(\kappa_2)}{G_1(\kappa_2 r_1) - G_0(\kappa_2)}, \quad (w(0) = 0, \varepsilon(0) = j_m^2)$$



Spectral response for pulses

Intensity transmission: $I(\delta) = |\mathcal{E}(\delta)|^2$:

$$I_p^{(\text{out})}(\delta) = |\mathcal{T}(\delta)|^2 I_p^{(\text{in})}(\delta), \quad T(\delta) = e^{-d_{\text{opt}}(\delta)},$$

Optical density (Beer' law) $\theta = q_p L$

$$d_{\text{opt}}(\delta) = -2\theta \Im \epsilon(\delta) > 0, \quad d_{\text{opt}}(0) = 0?$$

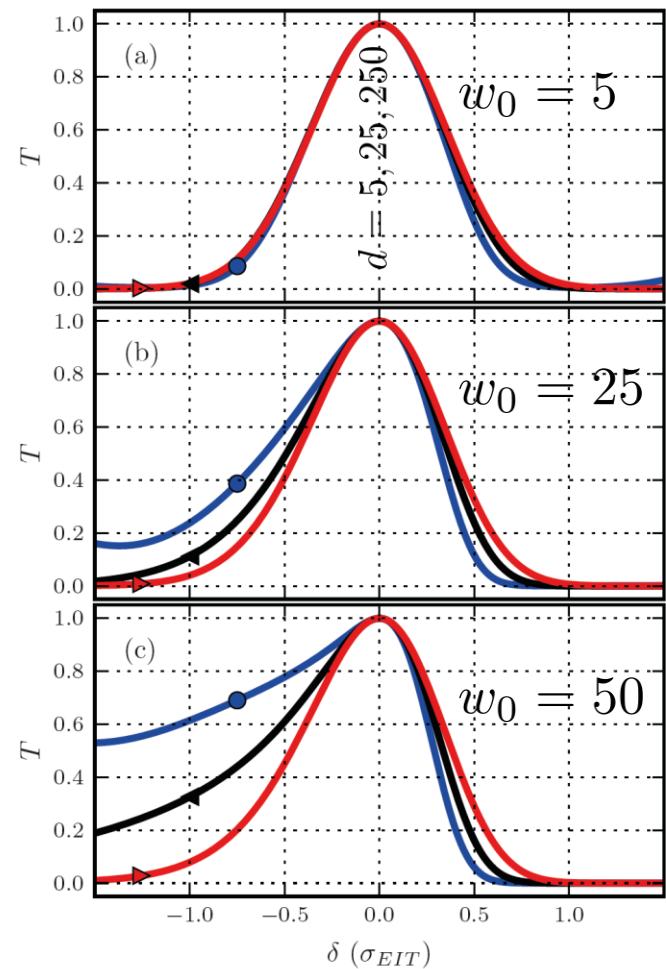
EIT optical density and 1/e full width

$$d_{\text{opt}}(\delta) = \left(\frac{2\delta}{\sigma_{\text{EIT}}} \right)^2 + \dots \quad \sigma_{\text{EIT}} = \frac{2}{\sqrt{-\theta \Im \epsilon''}}$$

Universal result as homogeneous system

$$d_{\text{EIT}} = \frac{|\Omega_c|^2 L}{\Gamma v_g} \gg 1, \quad \sigma_{\text{EIT}} = \frac{|\Omega_c|^2}{\Gamma \sqrt{d_{\text{EIT}}}}$$

Group velocity: $v_g = \frac{1}{\partial_\delta \Re k(0)} = -\frac{1}{q_p \Re \epsilon'(0)}$



Real time pulses: delay, distortion



Output power:

$$P_p^{(\text{out})}(t) = 2c\epsilon_0 |\mathcal{E}_p^{(\text{out})}(t)|^2.$$

OUT field for Gaussian IN field

$$\mathcal{E}_p^{(\text{out})}(t) = e^{-i[\omega_p t - k_p L - \eta]} \Phi(t) \mathcal{E}_p,$$

$$\Phi(t) = \int_{-\infty}^{\infty} d\delta \frac{e^{-i\theta\varepsilon(\delta) - it\delta - \frac{\delta^2}{\Delta\omega^2}}}{2\sqrt{\pi}\Delta\omega}.$$

Parameter

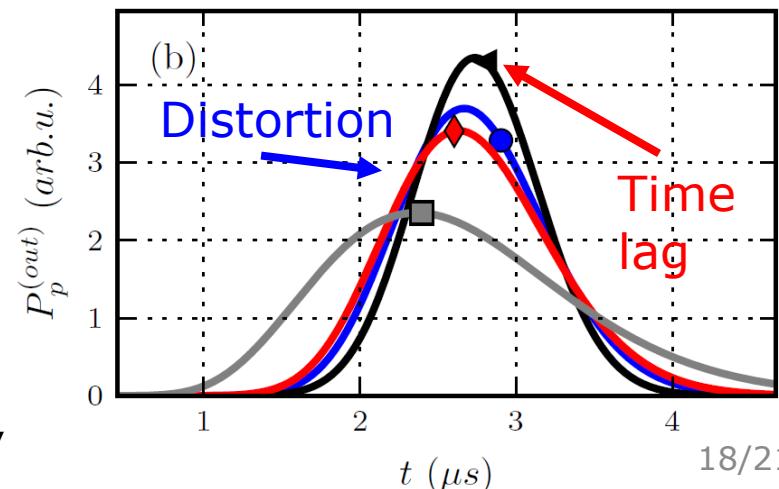
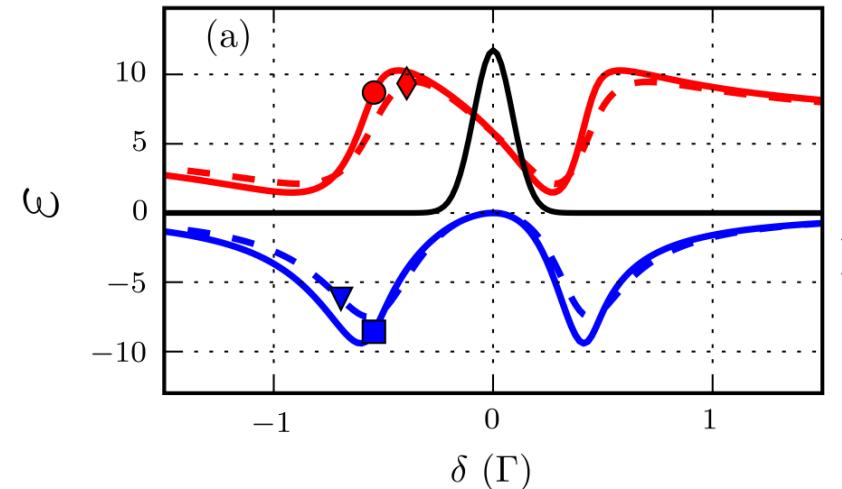
$$(a) r_1 = 0.301, w_0 = 12.5, \Omega_c = \Gamma, \Delta = 0$$

$$(b) \tau_p = 150 \text{ ns}, w_0 = 25.0, d_{opt} = 100$$

one-photon detuning:

$$\Delta/\Gamma = -1 (\bullet), -0.5 (\blacktriangleleft), 0 (\diamondsuit), 0.5 (\blacksquare)$$

M. Noaman, M. Langbecker, P. Windpassinger,
Opt. Lett. 43, 3925 (2018);
A. Hilton, C. Perrella, F. Benabid, B. Sparkes, A. Luiten,
P. Light, Phys. Rev. Applied 10, 044034 (2018)



Gaussian approximation



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Real time response

$$\Phi(t) = \frac{e^{-i\theta\epsilon - \frac{(t-\tau_{\text{lag}})^2}{\tau_p^2(1+i\xi)}}}{2\sqrt{1+i\xi}}, \xi = \frac{2\theta}{\tau_p^2}\epsilon'' \in \mathbb{C}$$

Time lag

$$\tau_{\text{lag}} = -\theta\epsilon' = \frac{L}{v_g} > 0,$$

Pulse width can be minimized

$$(\tau_p^{\text{out}})^2 \equiv \frac{(1 - \Im\xi)^2 + (\Re\xi)^2}{1 - \Im\xi} \tau_p^2 \geq \tau_p^2,$$

Group velocity two-layer model

$$v_g(r_1) = \frac{1}{\mu(r_1)} \frac{|\Omega_c|^2 \chi}{2\Gamma n_a \alpha_0}$$

Light speed reduction to 17 metres per second, L. Hau, S. E. Harris, Z. Dutton, C. Behroozi, Nature 397, 594 (1999)

Mitigation of lensing effects

Minimal pulse width

$$\Re \varepsilon''(\delta = 0, \Delta, r_1, n_a, \dots) = 0$$

E. g., optimal one-photon detuning

$$\Delta_{\text{opt}}^{(m)}(r_1) = \Gamma \alpha_0 v^2 n_a \mathcal{C}^{(m)}(r_1),$$

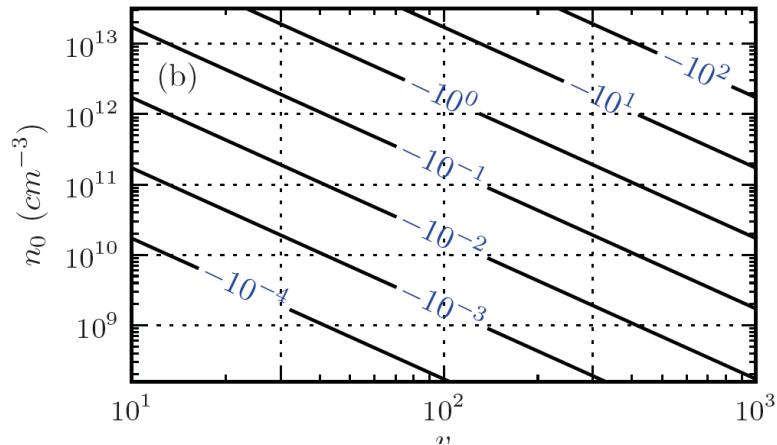
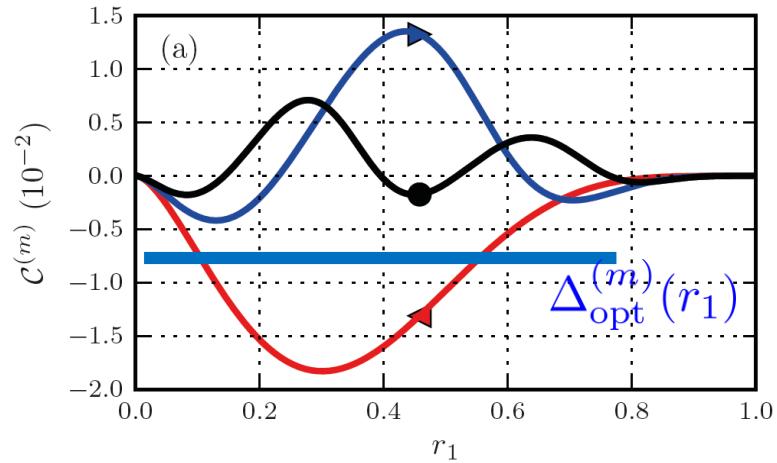
$$\mathcal{C}^{(m)}(r_1) = \frac{H_{\varepsilon\varepsilon} H_w}{2H_\varepsilon^2} - \frac{H_{w\varepsilon}}{H_\varepsilon} + \frac{H_{ww}}{2H_w}$$

Or, minimize deviation

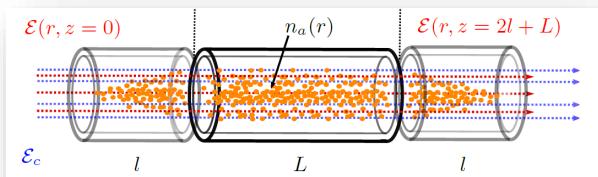
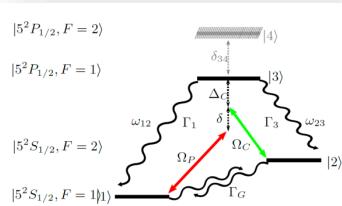
$$|\Delta_{\text{opt}}^{(m)}(r_1) - \Gamma \alpha_0 v^2 n_a \mathcal{C}^{(m)}(r_1)|$$

by modifying density

$$\Delta_{\text{opt}}^{(1)}(r_1) \Big|_{N_a=\text{const}} = \Gamma \alpha_0 v^2 \frac{N_a}{\pi L} \frac{\mathcal{C}^{(1)}(r_1)}{r_1^2}$$



Conclusion



1. Experimental setup
2. Electromagnetically induced transparency
3. Light propagation in a HCF
4. Pulse characterisation in frequency and time
5. Mitigation of lensing effects
6. <https://arxiv.org/abs/1905.02807>



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