

Ultralight dark matter

Kfir Blum (CERN, Weizmann)

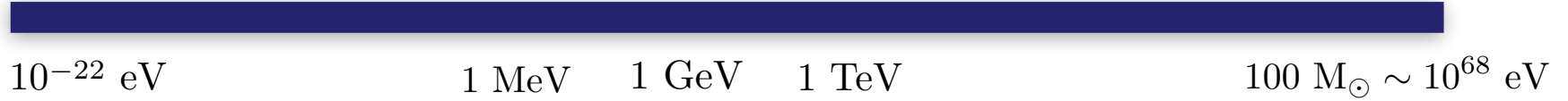
Bar, Blas, KB, Sibiryakov, 1805.00122

Bar, KB, Sato, Eby, 1903.03402

Bar, KB, Lacroix, Panci, 1905.11745

Benasque 2019

dark matter mass



Ultralight (“fuzzy”) DM

WIMPs

Primordial black holes

dark matter mass

10^{-22} eV

1 MeV

1 GeV

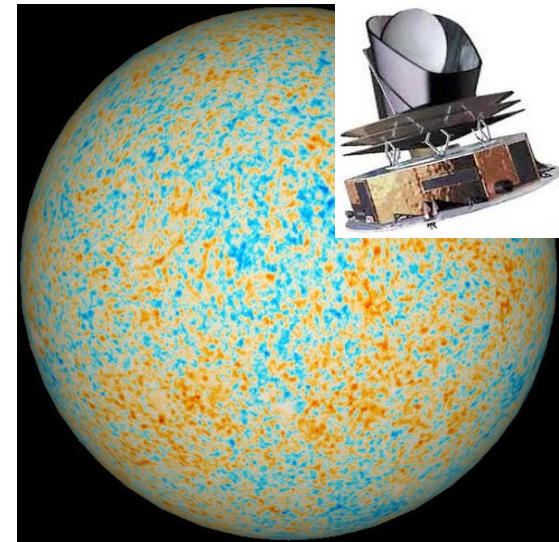
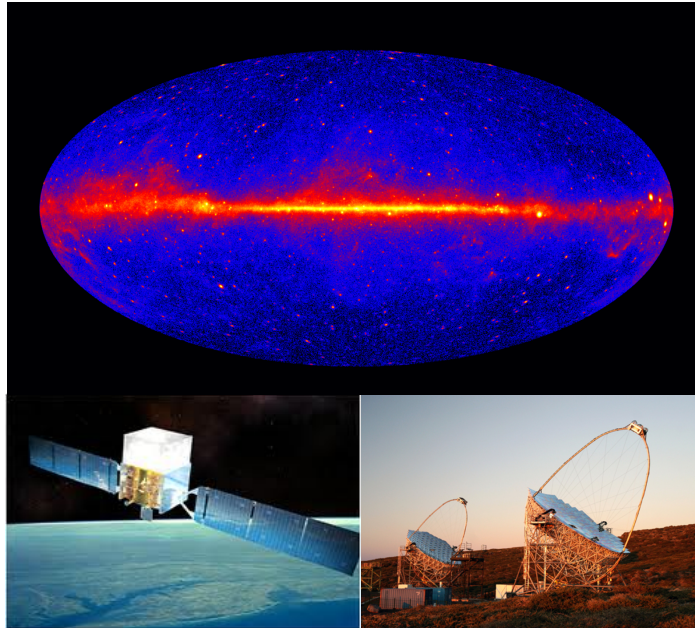
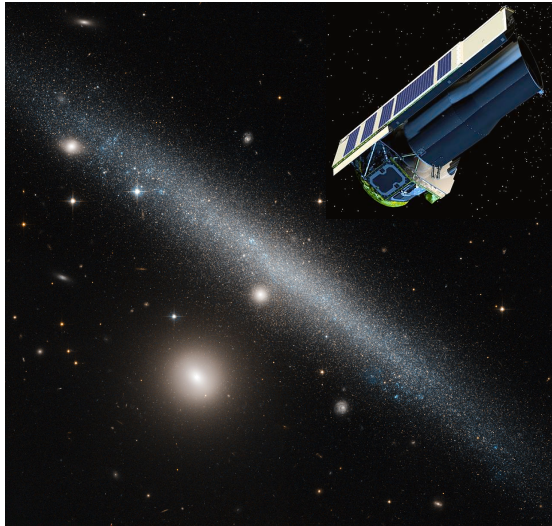
1 TeV

$100 M_{\odot} \sim 10^{68}$ eV

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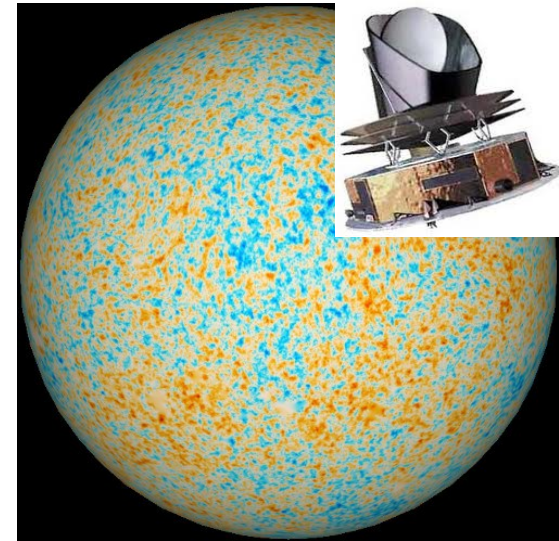
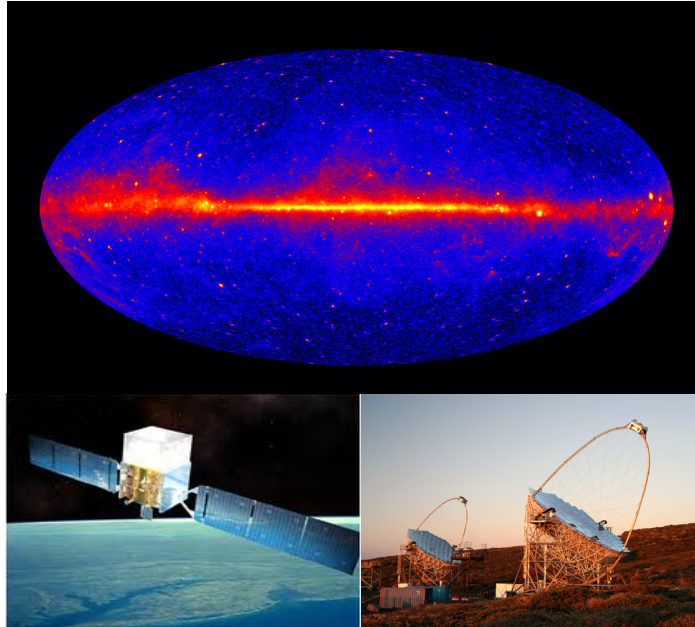
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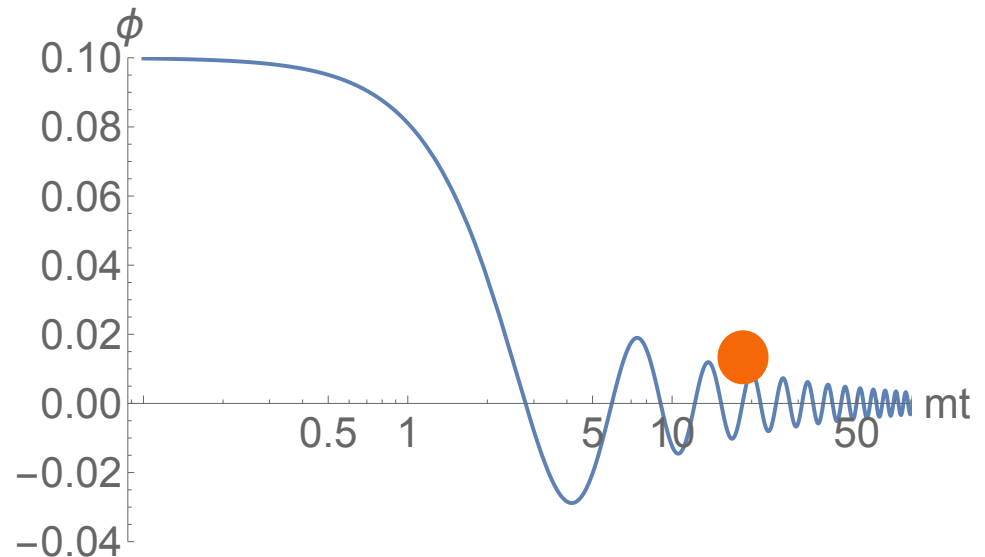
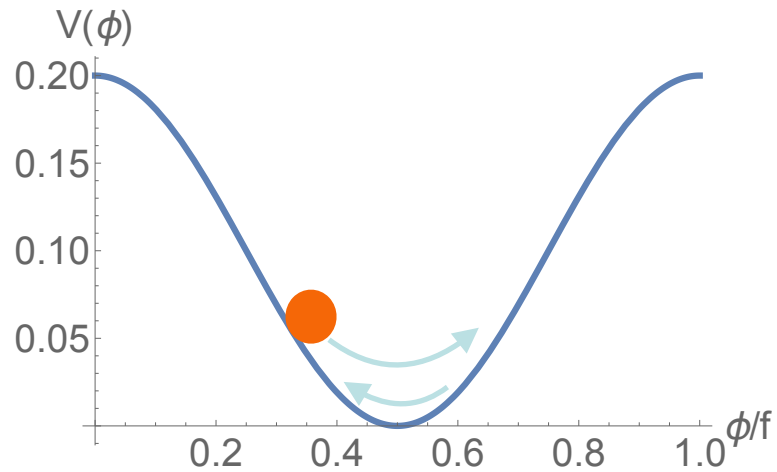
Primordial black holes



Light (pseudo-)scalar fields featured in many UV models, as PNGBs of spontaneously broken symmetries.

Initially displaced from a minimum of its potential during the early cosmological history, the field begins to oscillate around the minimum when $H \sim m$.

Correct cosmological equation of state for dark matter.

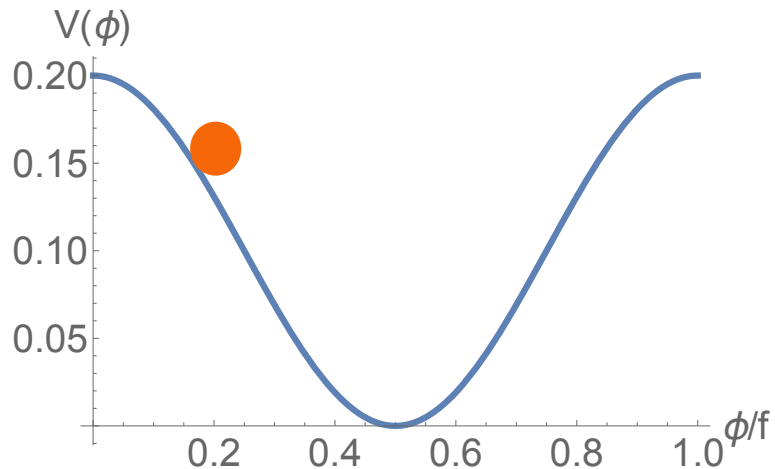


Relic abundance set by initial conditions.

Natural initial condition: $\phi \sim f$

Assuming potential exists
before end of inflation,
contribution to energy density today:

$$\Omega_m \sim 0.1 \left(\frac{m}{10^{-22} \text{ eV}} \right)^{\frac{1}{2}} \left(\frac{f}{10^{17} \text{ GeV}} \right)^2$$



Ultra-light dark matter (ULDM)

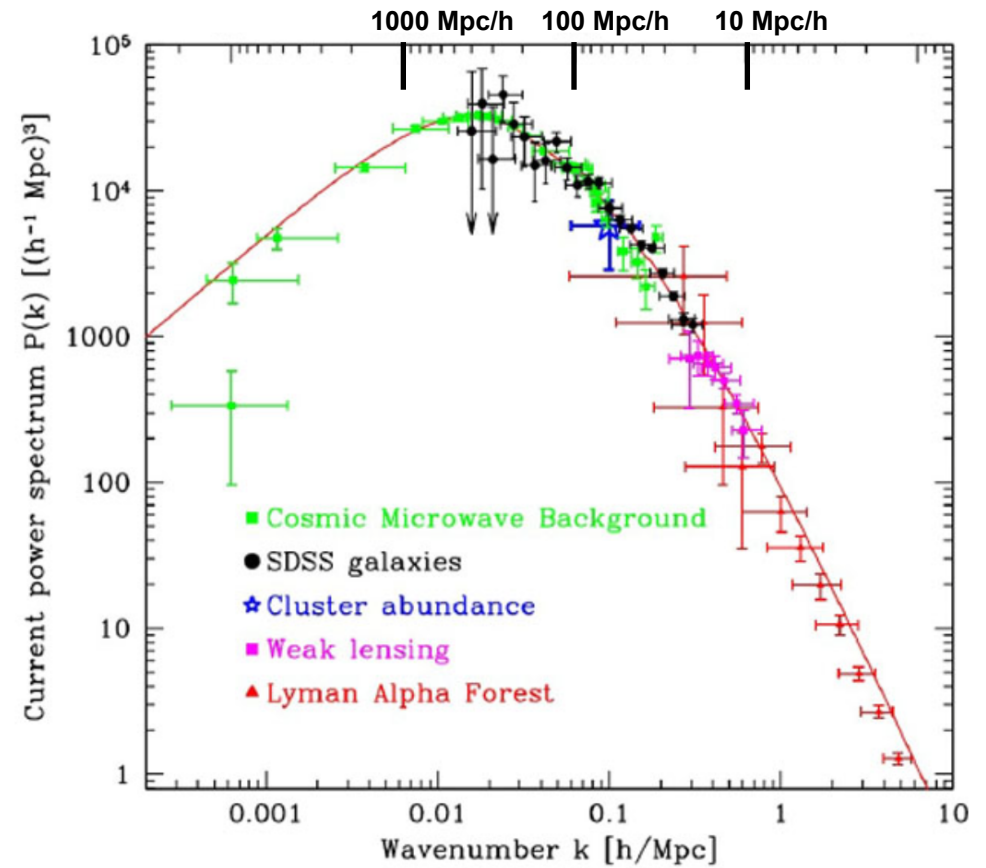
- [1] W. Hu, R. Barkana, and A. Gruzinov, “Cold and fuzzy dark matter,” Phys. Rev. Lett. **85** (2000) 1158–1161, [arXiv:astro-ph/0003365](#) [[astro-ph](#)].
- [2] A. Arbey, J. Lesgourgues, and P. Salati, “Quintessential haloes around galaxies,” Phys. Rev. **D64** (2001) 123528, [arXiv:astro-ph/0105564](#) [[astro-ph](#)].
- [3] J. Lesgourgues, A. Arbey, and P. Salati, “A light scalar field at the origin of galaxy rotation curves,” New Astron. Rev. **46** (2002) 791–799.
- [4] P.-H. Chavanis, “Mass-radius relation of Newtonian self-gravitating Bose-Einstein condensates with short-range interactions: I. Analytical results,” Phys. Rev. **D84** (2011) 043531, [arXiv:1103.2050](#) [[astro-ph.CO](#)].
- [5] P. H. Chavanis and L. Delfini, “Mass-radius relation of Newtonian self-gravitating Bose-Einstein condensates with short-range interactions: II. Numerical results,” Phys. Rev. **D84** (2011) 043532, [arXiv:1103.2054](#) [[astro-ph.CO](#)].
- [6] D. J. E. Marsh and A.-R. Pop, “Axion dark matter, solitons and the cusp-core problem,” Mon. Not. Roy. Astron. Soc. **451** no. 3, (2015) 2479–2492, [arXiv:1502.03456](#) [[astro-ph.CO](#)].
- [7] S.-R. Chen, H.-Y. Schive, and T. Chiueh, “Jeans Analysis for Dwarf Spheroidal Galaxies in Wave Dark Matter,” Mon. Not. Roy. Astron. Soc. **468** no. 2, (2017) 1338–1348, [arXiv:1606.09030](#) [[astro-ph.GA](#)].
- [8] L. Hui, J. P. Ostriker, S. Tremaine, and E. Witten, “Ultralight scalars as cosmological dark matter,” Phys. Rev. **D95** no. 4, (2017) 043541, [arXiv:1610.08297](#) [[astro-ph.CO](#)].
- [9] H.-Y. Schive, T. Chiueh, and T. Broadhurst, “Cosmic Structure as the Quantum Interference of a Coherent Dark Wave,” Nature Phys. **10** (2014) 496–499, [arXiv:1406.6586](#) [[astro-ph.GA](#)].
- [10] H.-Y. Schive, M.-H. Liao, T.-P. Woo, S.-K. Wong, T. Chiueh, T. Broadhurst, and W. Y. P. Hwang, “Understanding the Core-Halo Relation of Quantum Wave Dark Matter from 3D Simulations,” Phys. Rev. Lett. **113** no. 26, (2014) 261302, [arXiv:1407.7762](#) [[astro-ph.GA](#)].

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Ultra-light dark matter (ULDM)

...

On scales much larger than de Broglie wavelength, **ULDM** behaves like WIMP DM.



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Early structure formation:

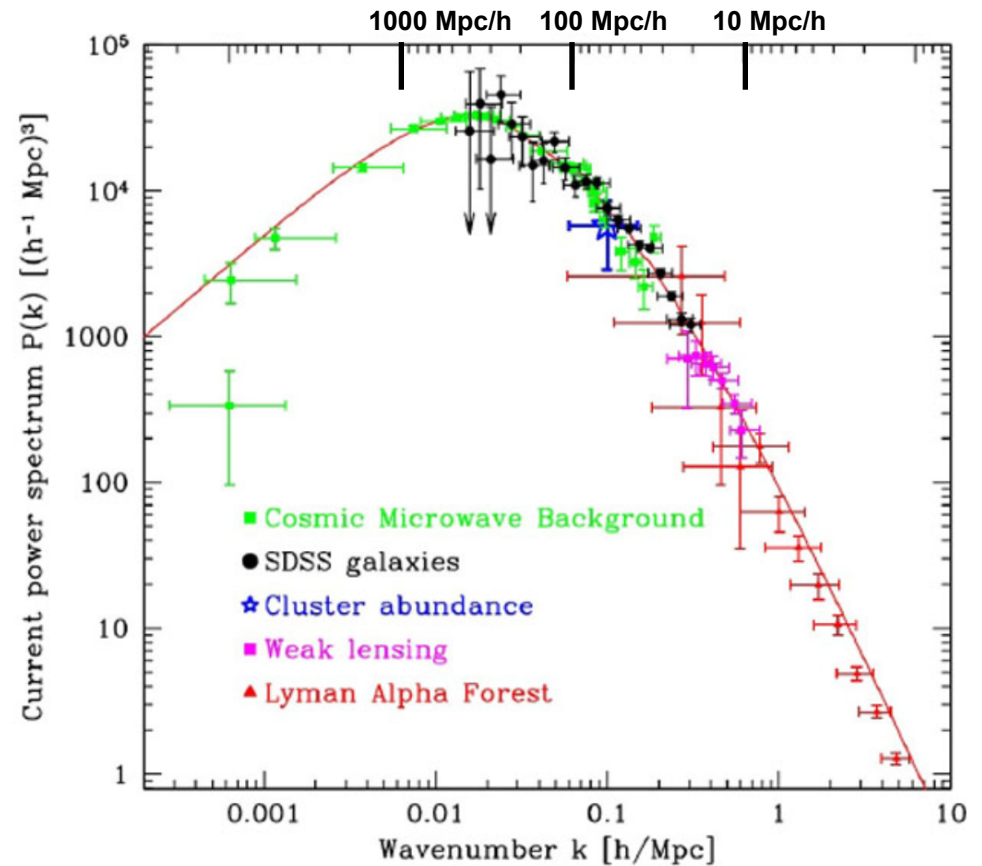
DM EoS achieved when $H \sim m$:

$$T \sim (m M_{pl})^{\frac{1}{2}}$$

$$\sim \left(\frac{m}{10^{-22} \text{ eV}} \right)^{\frac{1}{2}} \text{ keV}$$

$$z \sim 10^6 \left(\frac{m}{10^{-22} \text{ eV}} \right)^{\frac{1}{2}}$$

Mpc scales enter the horizon.

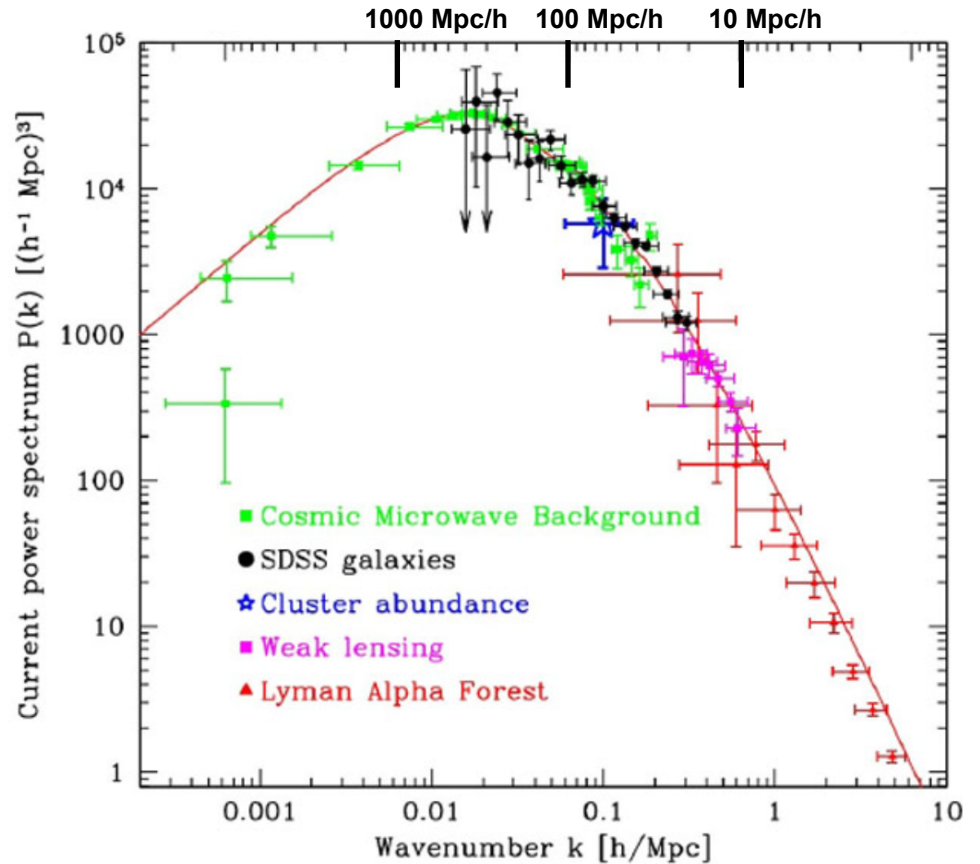


On scales of order de Broglie wavelength, **ULDM** is markedly different than **WIMPs**.

dB length for self-gravitating perturbation (“Jeans scale”):

$$v^2 = \frac{GM}{R} = \frac{4\pi}{3} G \delta\rho \left(\frac{\lambda_{dB}}{2} \right)^2$$

$$\lambda_{dB} = \frac{2\pi}{mv}$$



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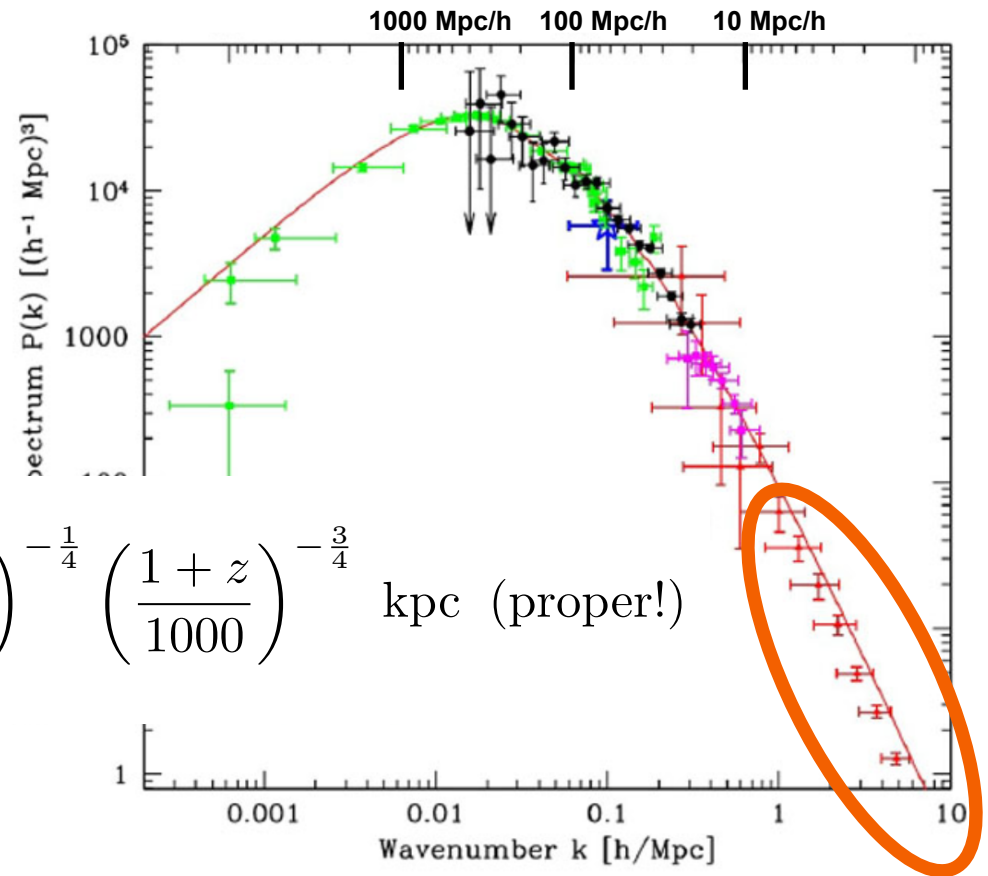
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$$= \left(\frac{G \delta\rho m^2}{12\pi}\right)^{-\frac{1}{4}}$$

$$\approx 5.8 \left(\frac{m}{10^{-22} \text{ eV}}\right)^{-\frac{1}{2}} \left(\frac{\delta\rho/\rho}{10^{-5}}\right)^{-\frac{1}{4}} \left(\frac{1+z}{1000}\right)^{-\frac{3}{4}} \text{ kpc (proper!)}$$



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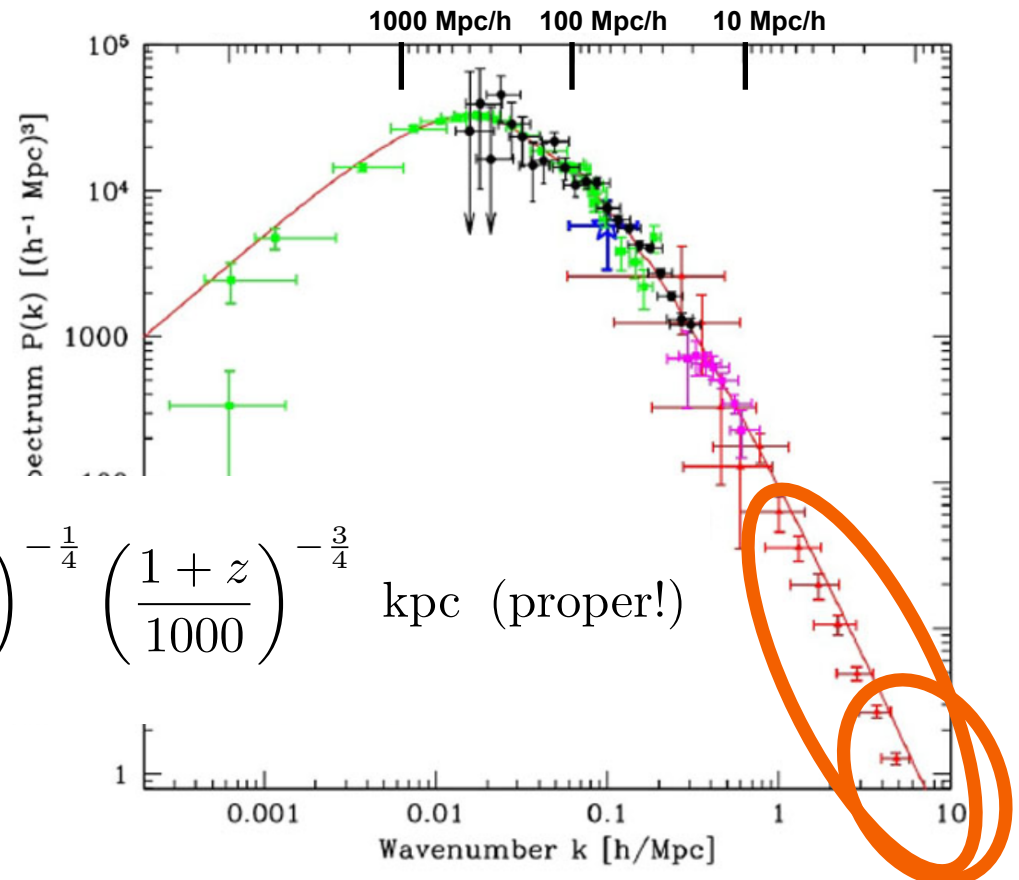
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Ly-alpha Forest:

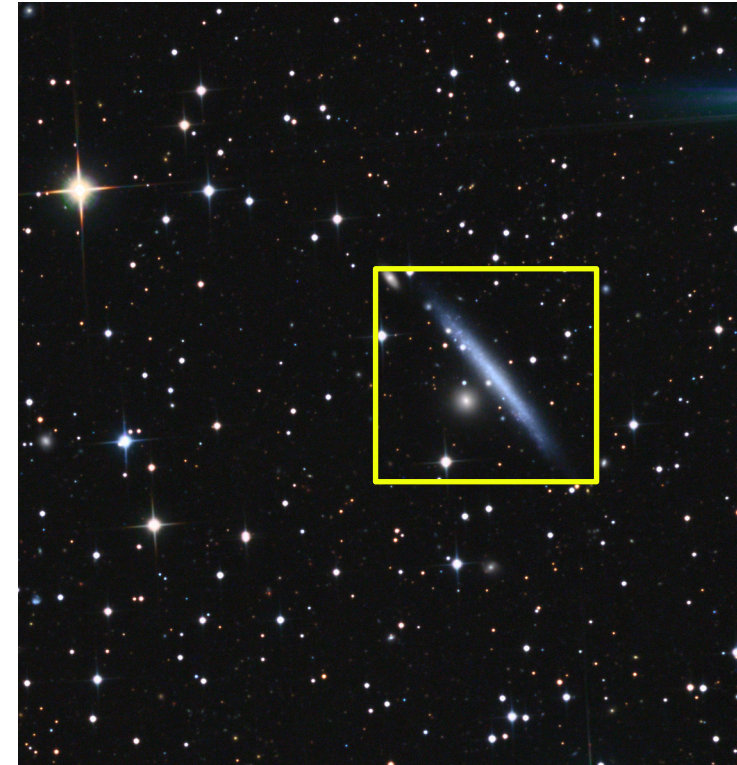
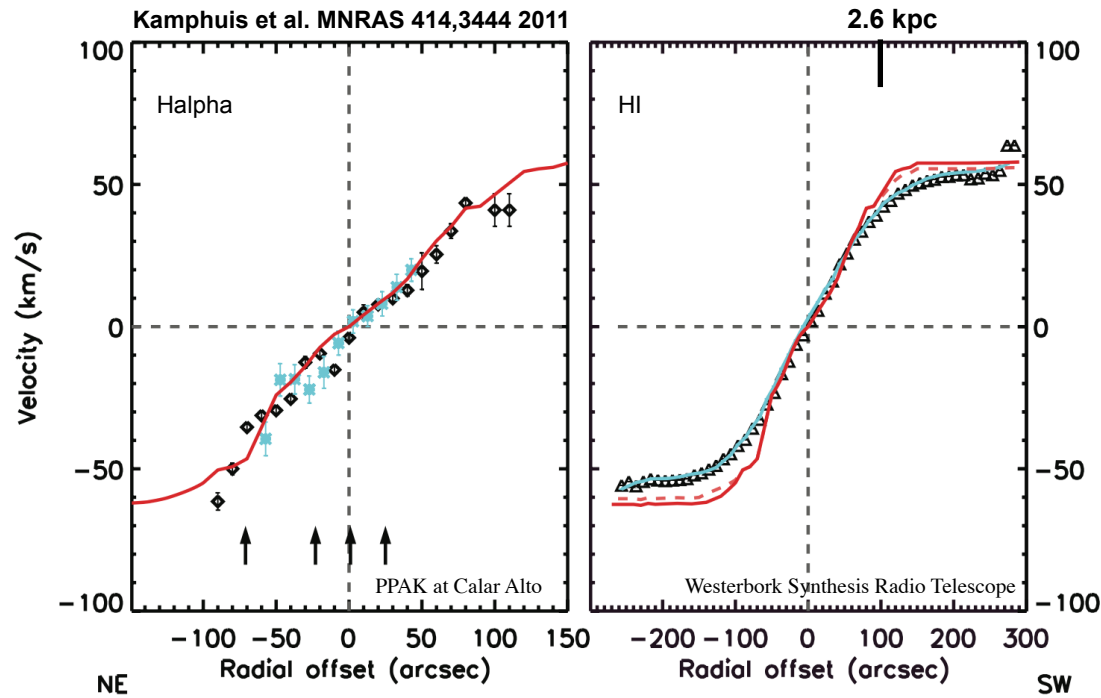
$$m \gtrsim 10^{-21} \text{ eV}$$

- Armengaud (1703.09126),
- Irsic (1703.04683),
- Zhang (1708.04389),
- Kobayashi (1708.00015)

...

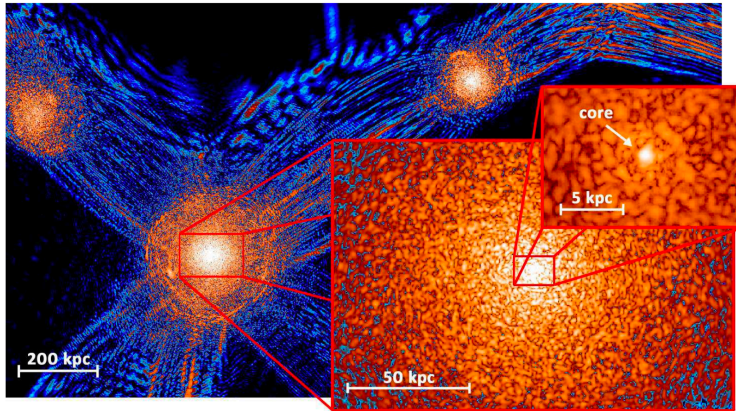
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dB length \sim kpc for $m \sim 10^{-22}$ eV

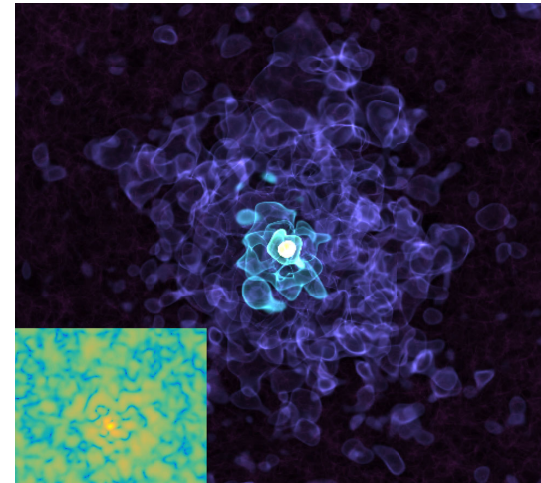


ULDM in galaxies

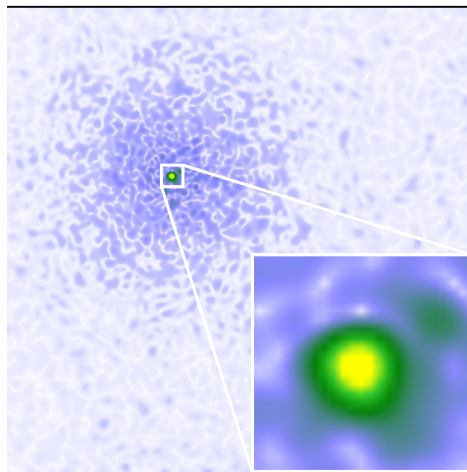
Progress in numerical simulations



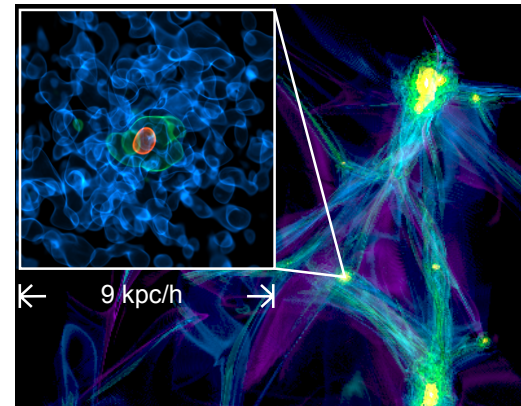
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Mocz et al, MNRAS. 471 (2017) 4559-4570

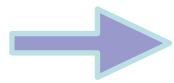


Levkov, Panin, Tkachev,
Phys.Rev.Lett. 121 (2018) 151301

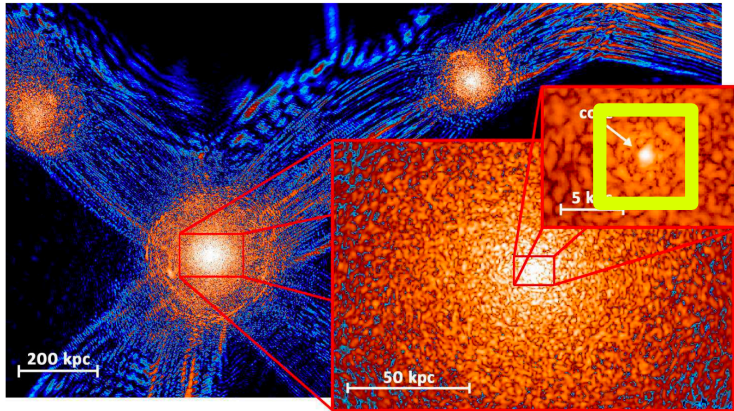


Veltmaat, Niemeyer, Schwabe,
Phys.Rev. D98 (2018) 043509

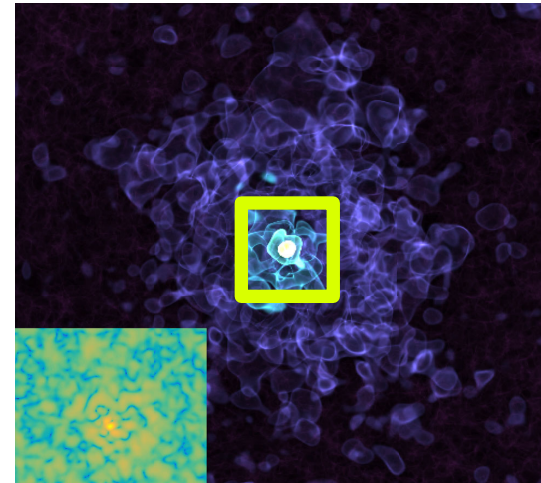
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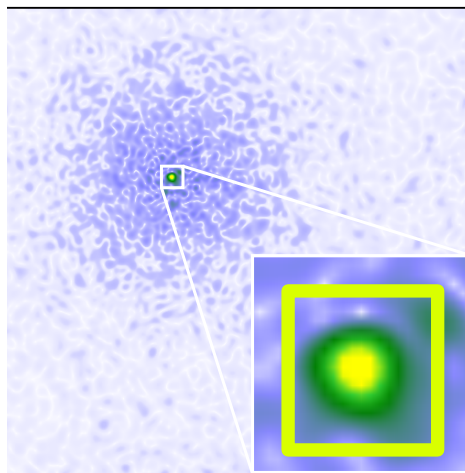
Inner part of simulated galaxies forms a core



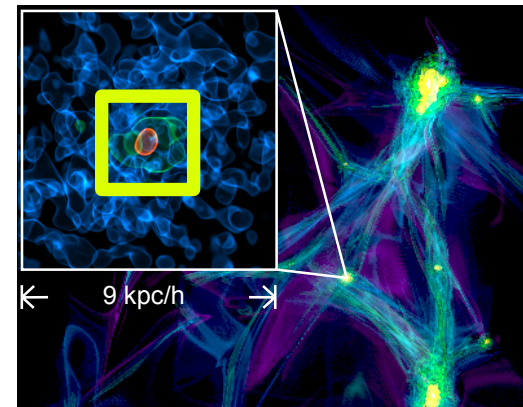
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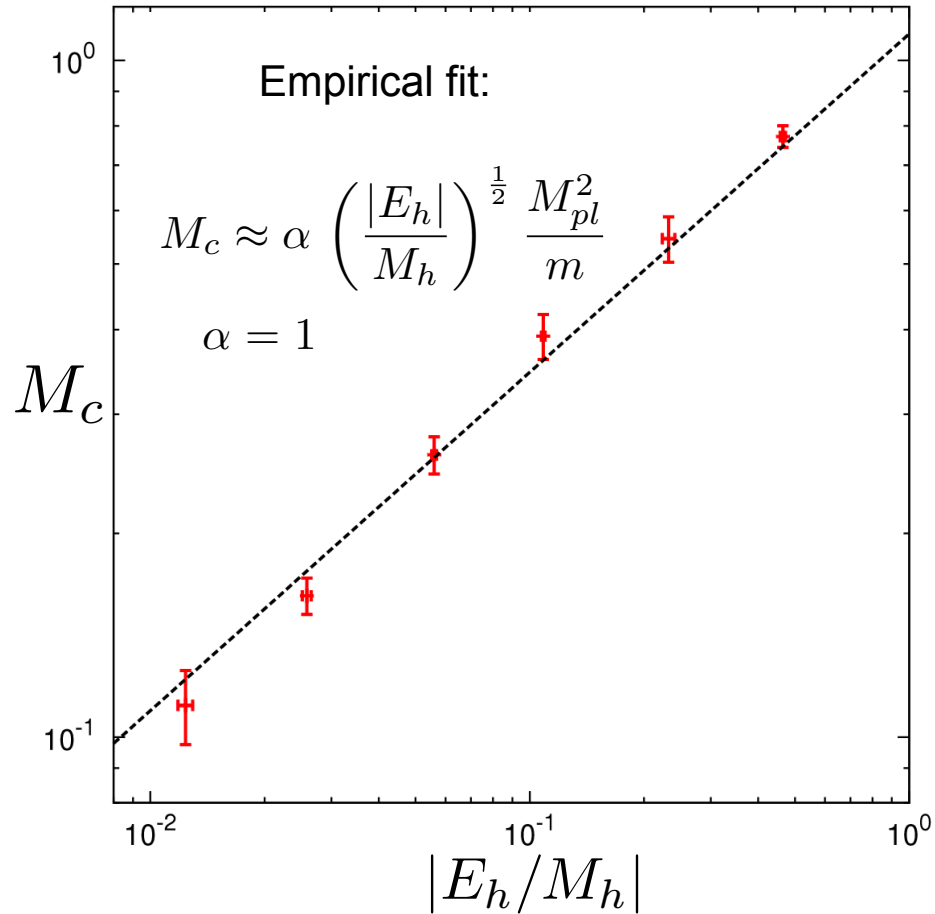
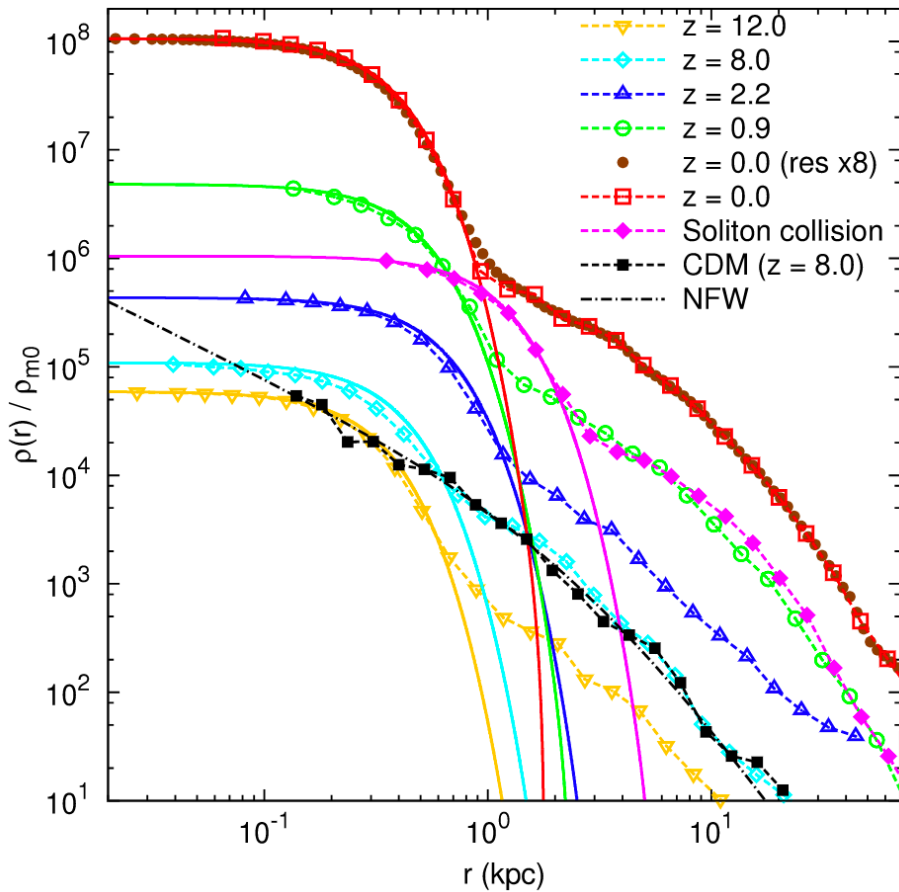
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A soliton — host halo relation?

Schive et al 1406.6586
 Schive et al 1407.7762
 Veltmaat et al 1804.09647



Mocz 1705.05845 find a different relation?
 (Xtra material in this talk)

Some facts about solitons

Real, free, KG field

$$i\partial_t\psi = -\frac{1}{2m}\nabla^2\psi + m\Phi\psi,$$

$$\nabla^2\Phi = 4\pi G|\psi|^2.$$

$$\phi(x, t) = \frac{1}{\sqrt{2m}}e^{-imt}\psi(x, t) + cc$$

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On scales of order de Broglie wavelength:

$$\psi(x, t) = \left(\frac{m M_{pl}}{\sqrt{4\pi}} \right) e^{-i\gamma m t} \chi(x)$$



$$\begin{aligned} \partial_r^2 (r\chi) &= 2r (\Phi - \gamma) \chi, \\ \partial_r^2 (r\Phi) &= r\chi^2. \end{aligned}$$

Some facts about solitons

Continuous family of ground state solutions,
characterised by one parameter

Let $\chi_1(r)$ be defined to satisfy $\chi(0) = 1$, vanishing at infinity w/ no nodes.

$$M_1 = \frac{M_{pl}^2}{m} \int_0^\infty dr r^2 \chi_1^2(r)$$
$$\approx 2.79 \times 10^{12} \left(\frac{m}{10^{-22} \text{ eV}} \right)^{-1} M_\odot$$

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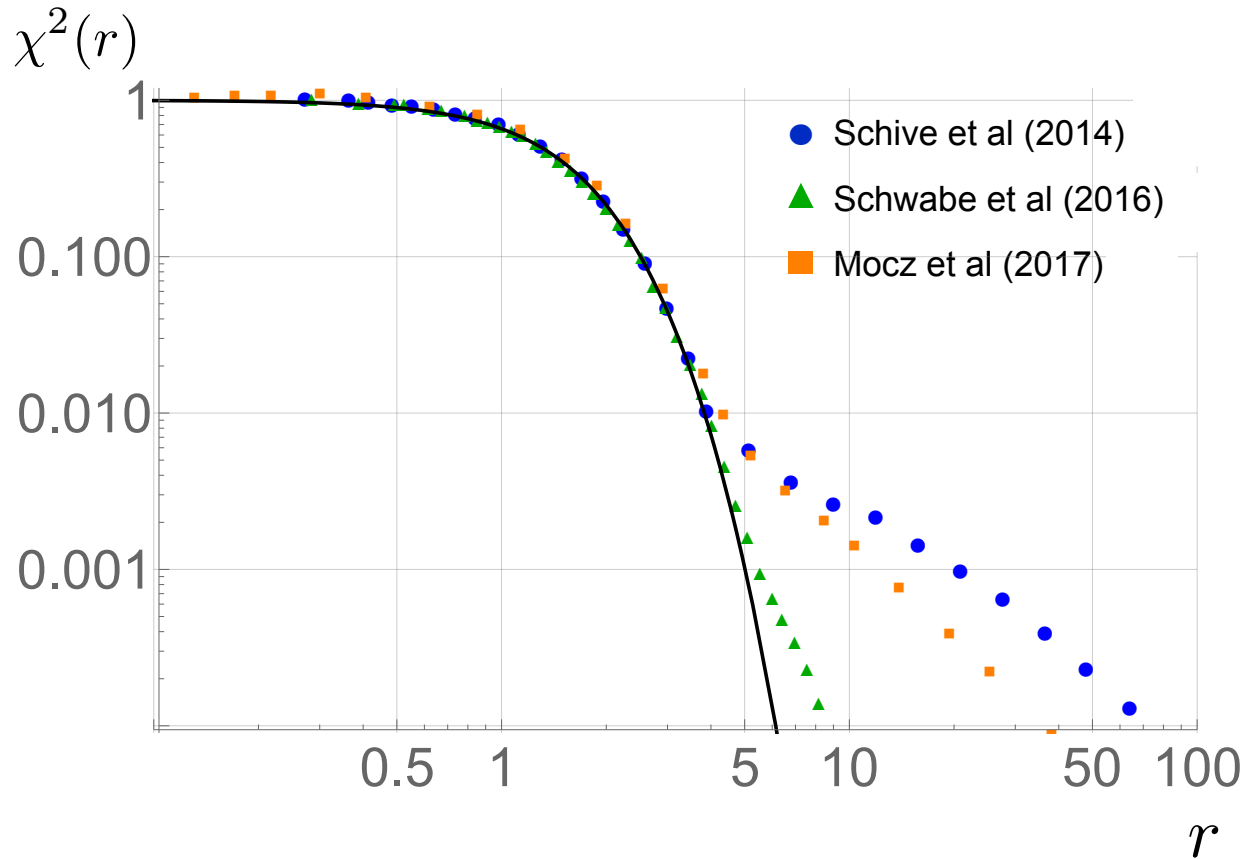
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Other solutions obtained by scaling

$$\chi_\lambda(r) = \lambda^2 \chi_1(\lambda r),$$
$$\Phi_\lambda(r) = \lambda^2 \Phi_1(\lambda r),$$
$$\gamma_\lambda = \lambda^2 \gamma_1,$$

$$M_\lambda = \lambda M_1,$$
$$x_{c\lambda} = \lambda^{-1} x_{c1}$$

Numerical simulations of galaxy formation w/ ULDM find proper solitons* in the centre of galactic halos

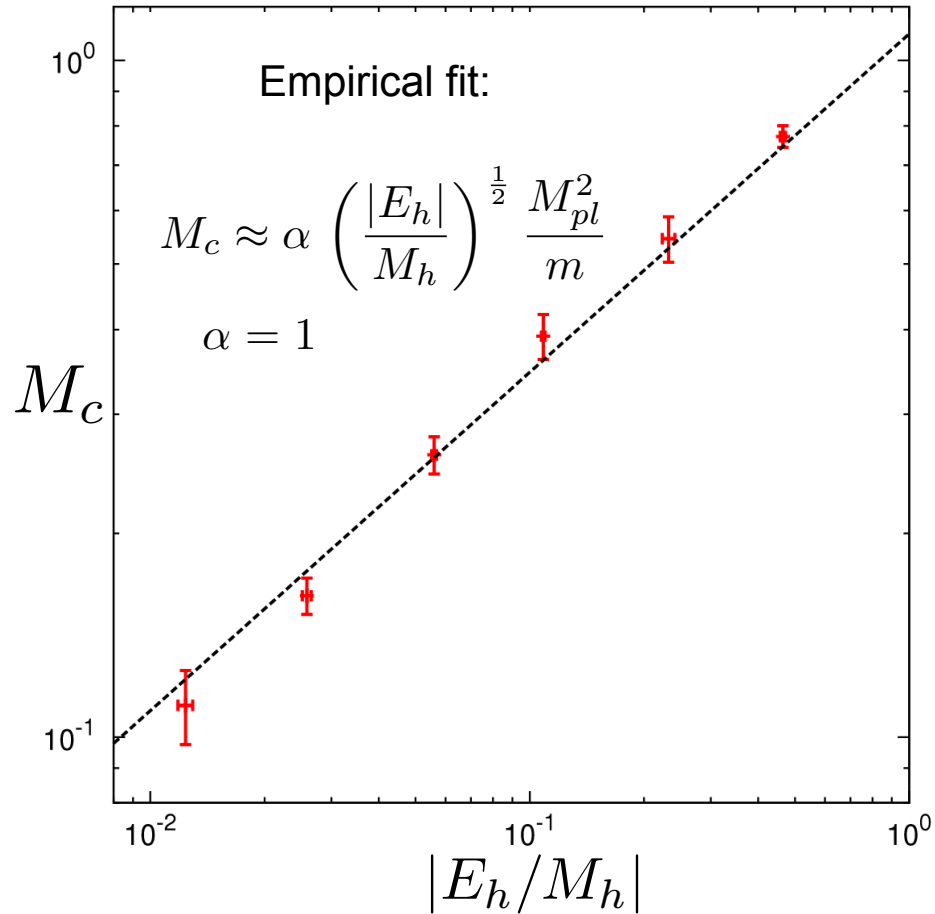
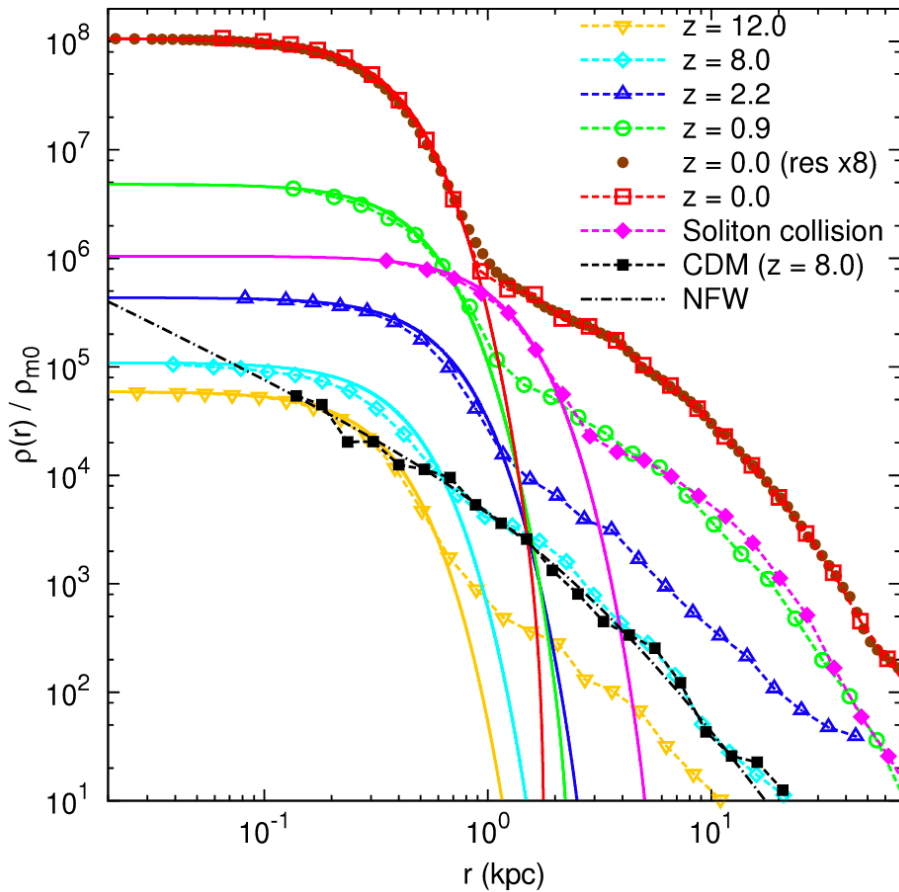


Bar, Blas, KB, Sibiryakov; 1805.00122

* Oscillatons? oscillons?

A soliton — host halo relation?

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Mocz 1705.05845 find a different relation?
 (Xtra material in this talk)

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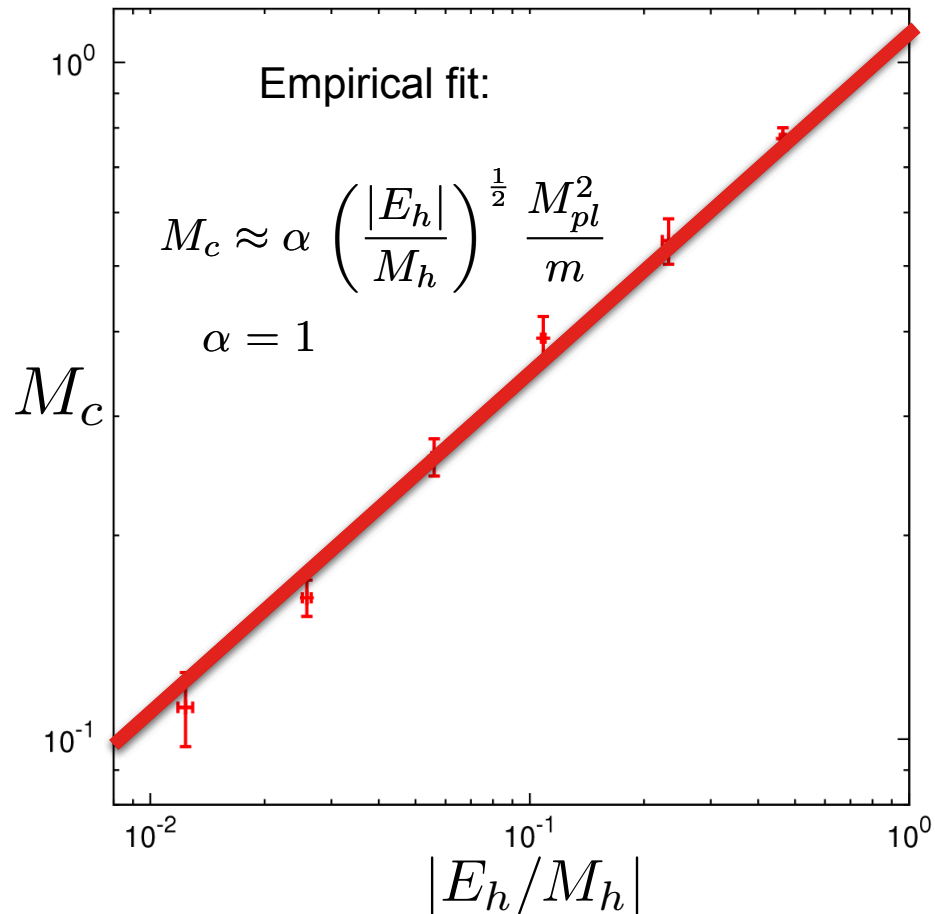
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soliton—halo relation equivalent to:

$$\left. \frac{K}{M} \right|_{\text{soliton}} = \left. \frac{K}{M} \right|_{\text{halo}}$$

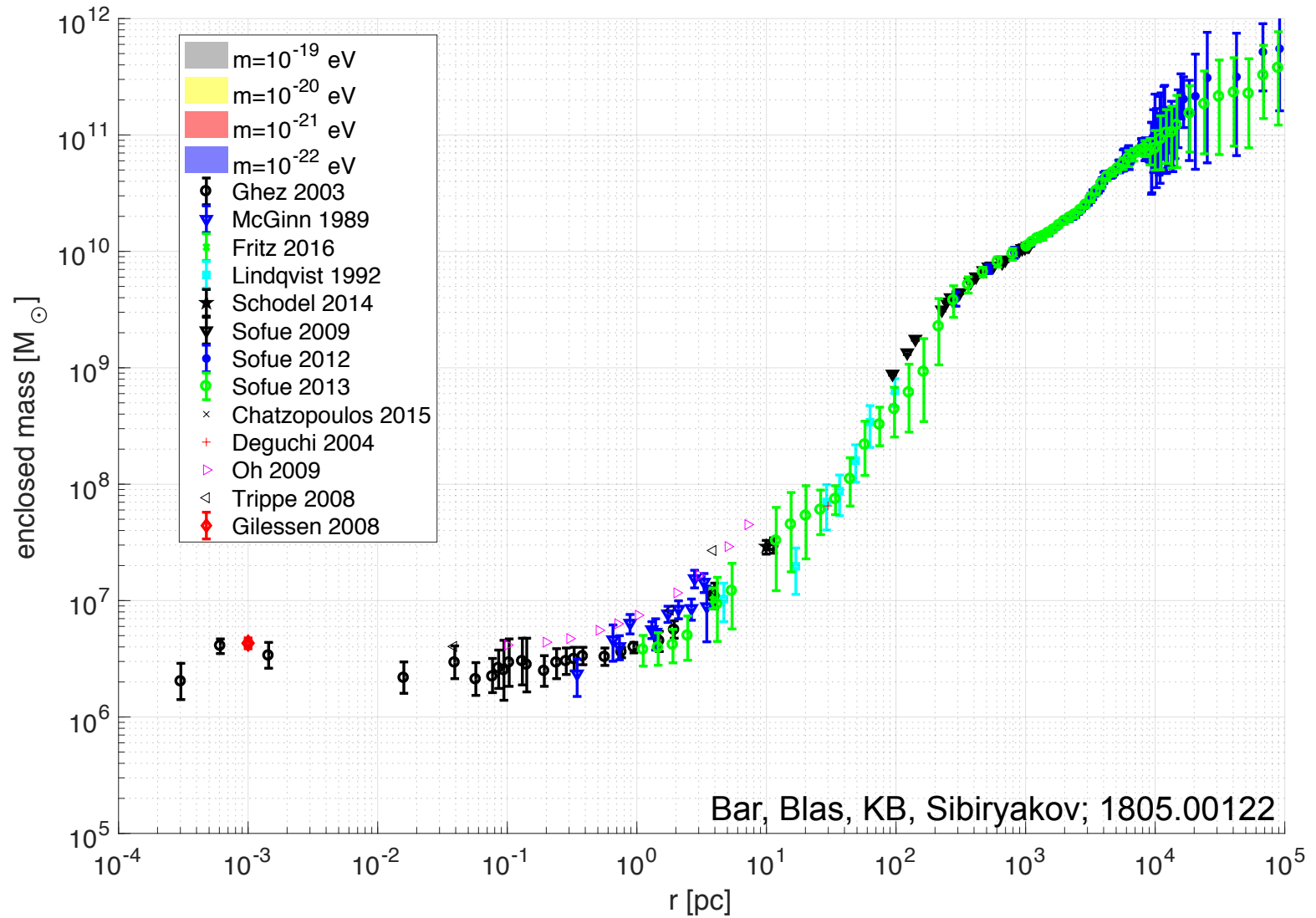
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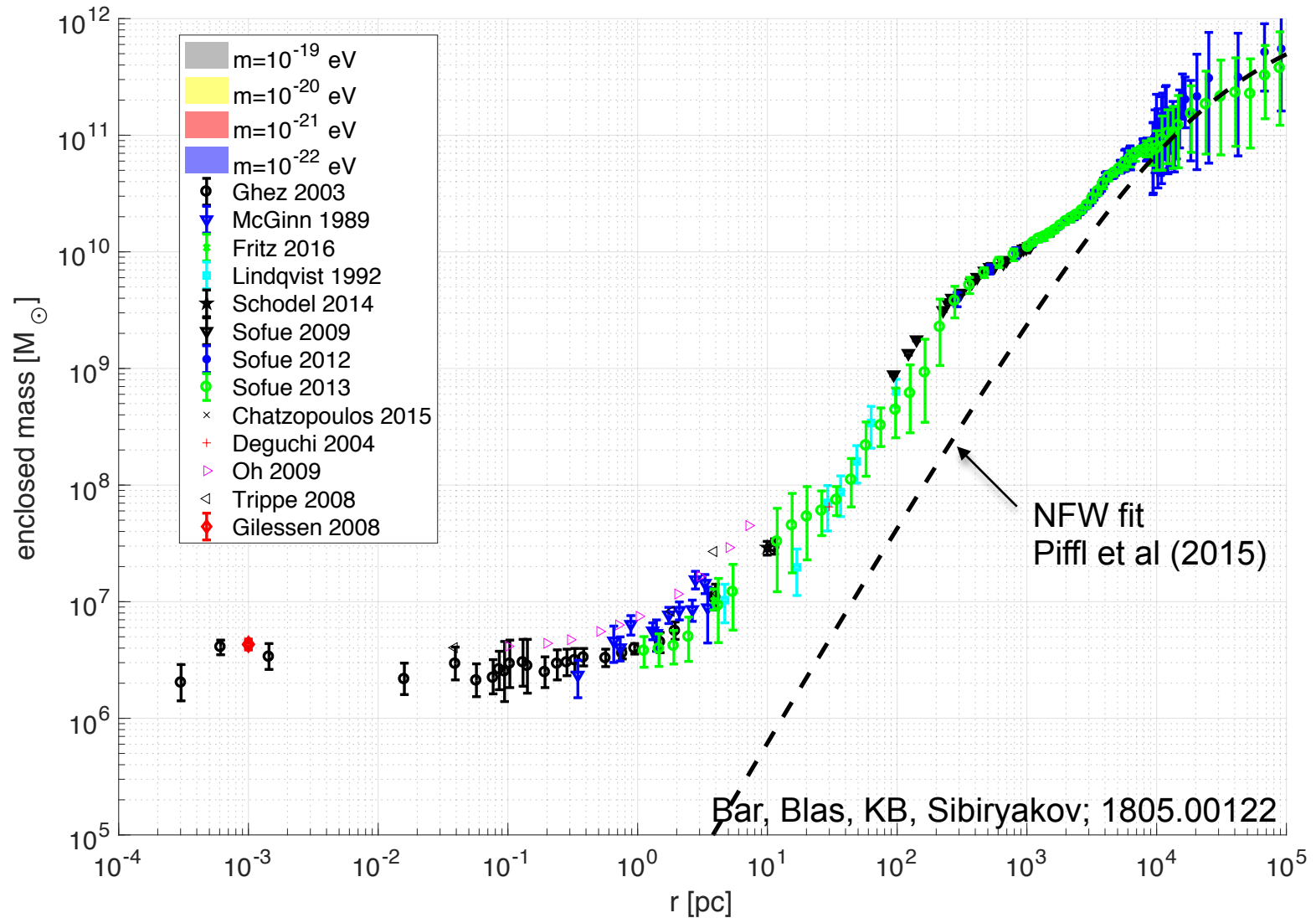
Mocz 1705.05845 find a different relation?
(Xtra material in this talk)

(estimated) radially-averaged mass profile of the Milky Way



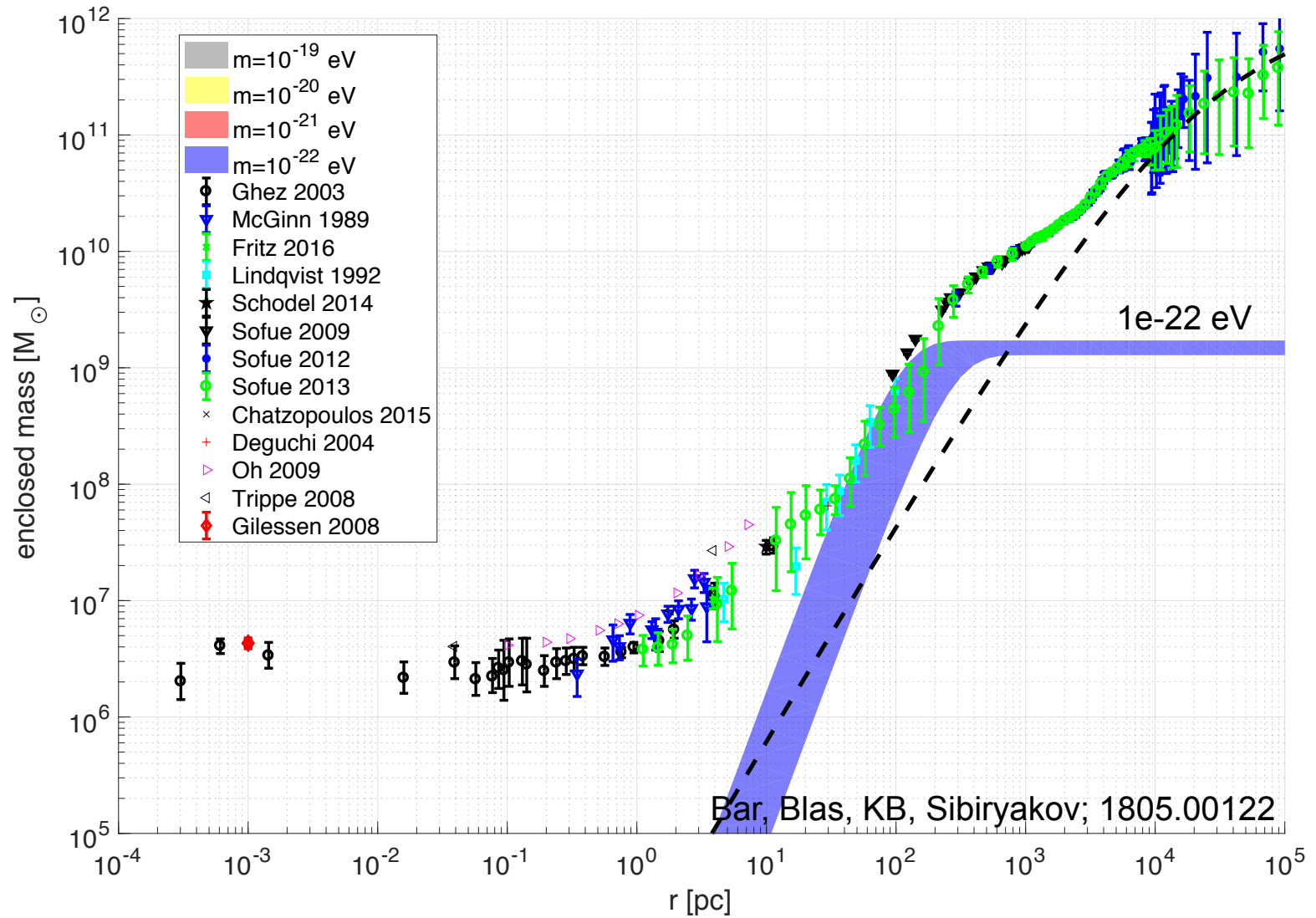
WIMP dark matter:

thought to affect outer part of rotation curve



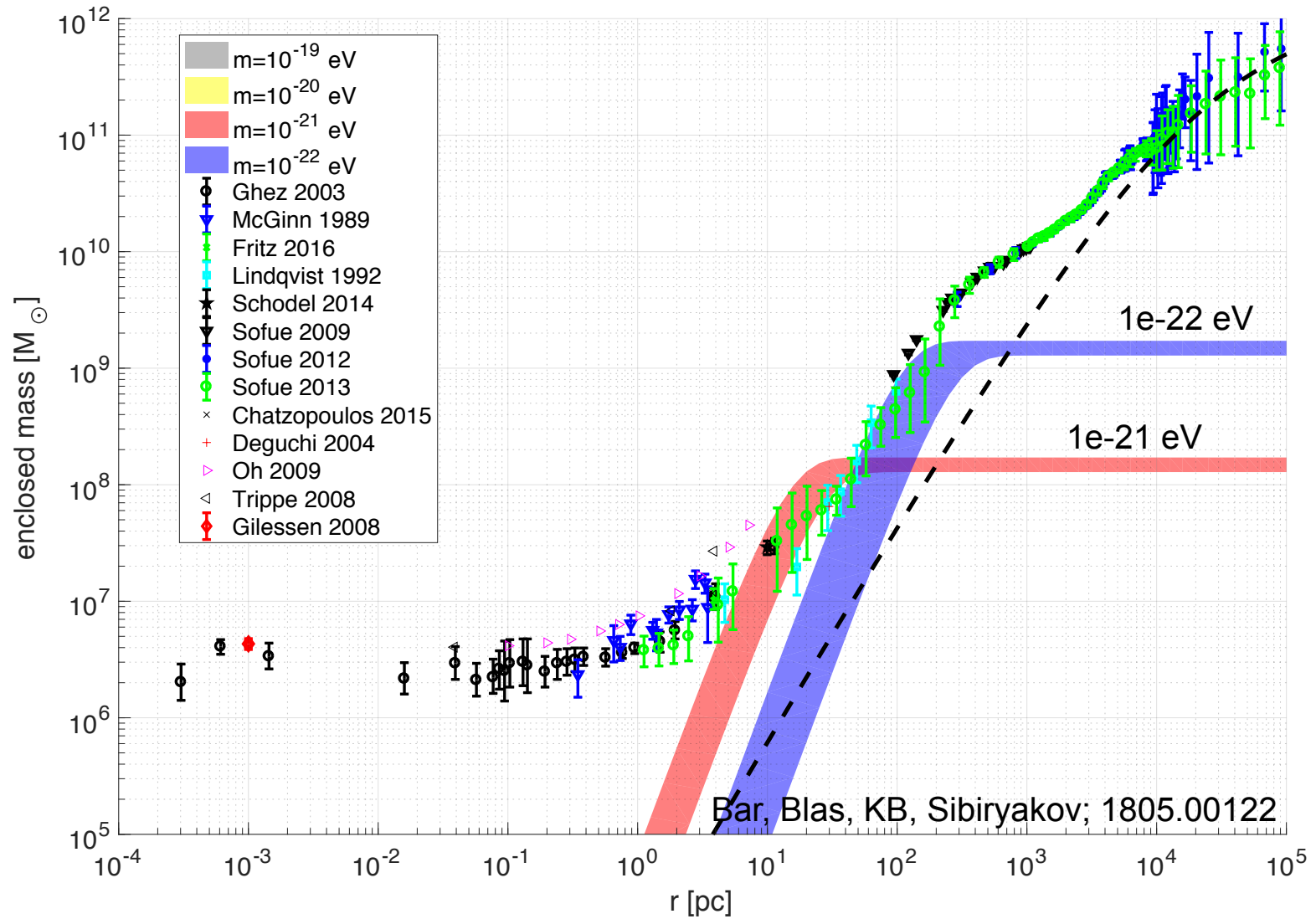
ULDM:

Affects the inner part of rotation curve



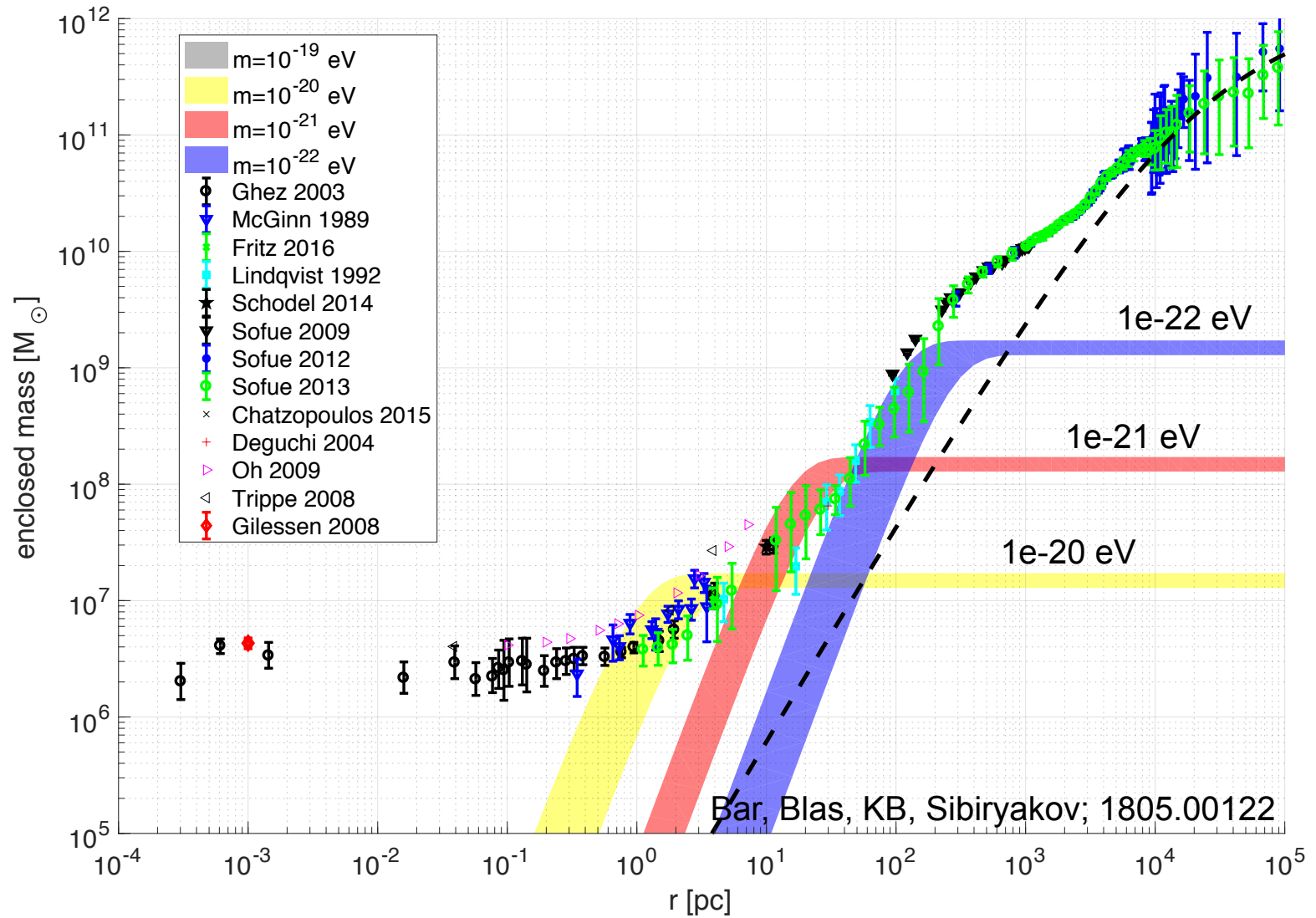
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Affects the inner part of rotation curve



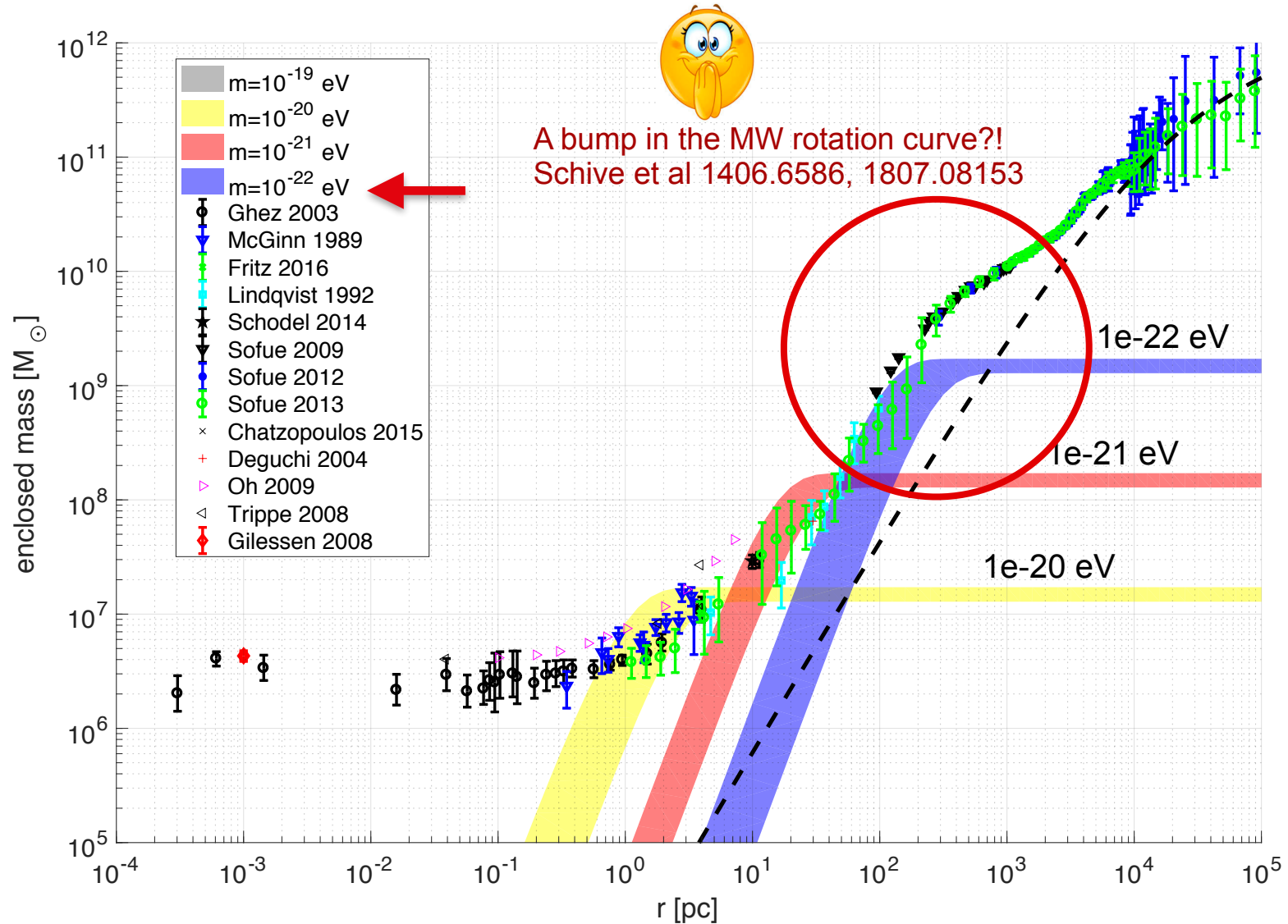
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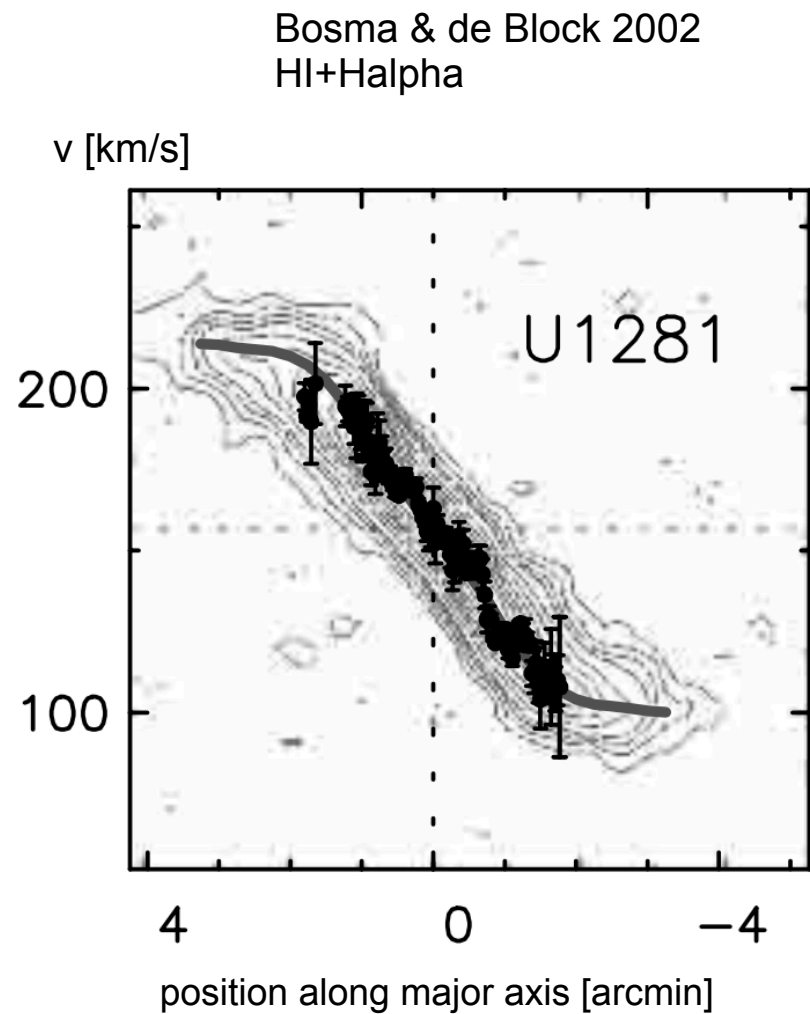
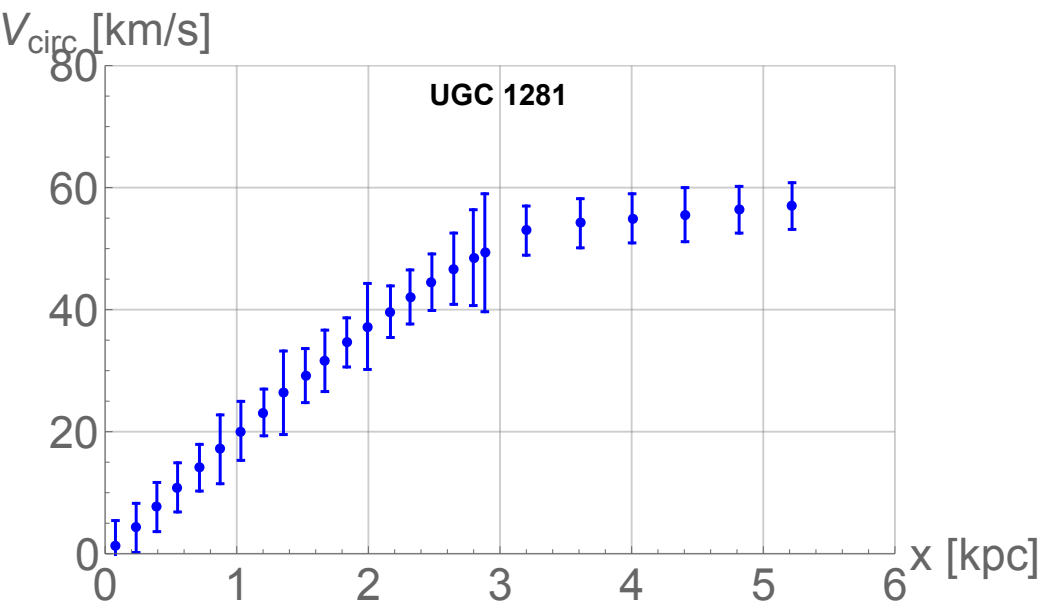
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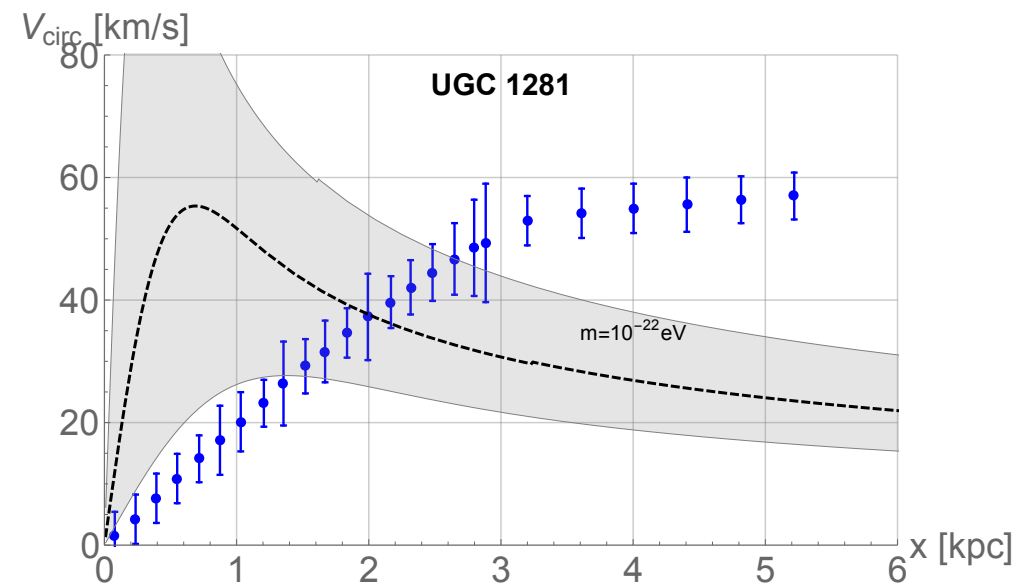


UGC 1281

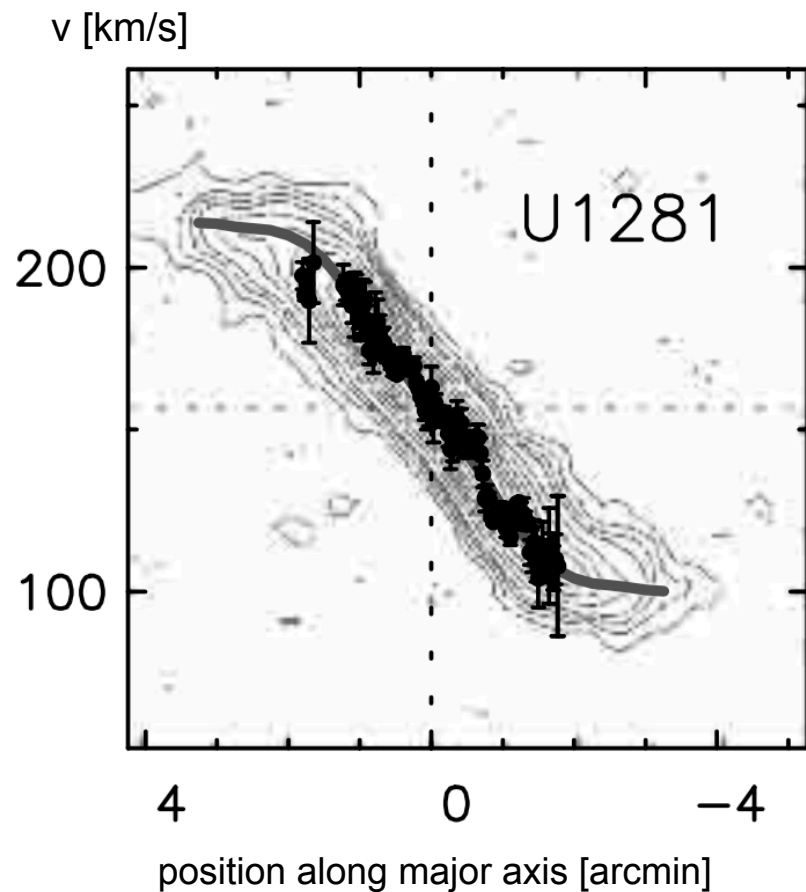




$$m = 10^{-22} \text{ eV}$$

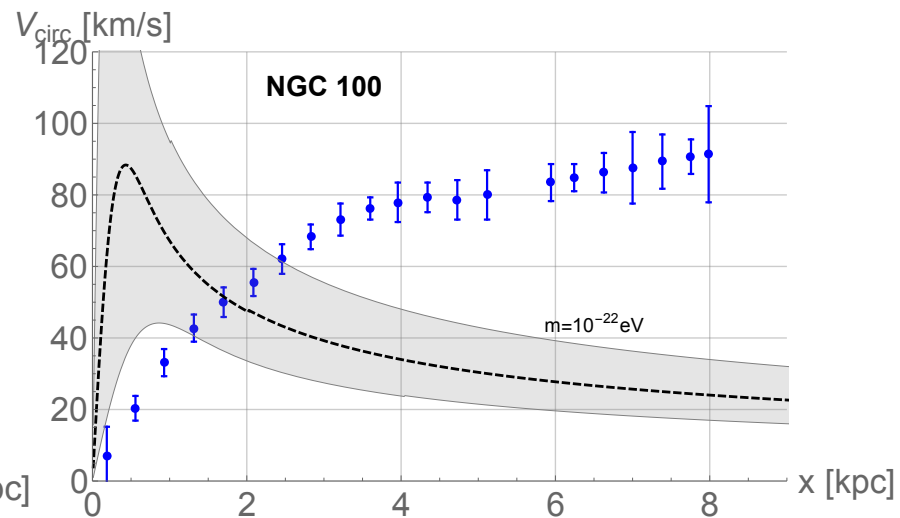
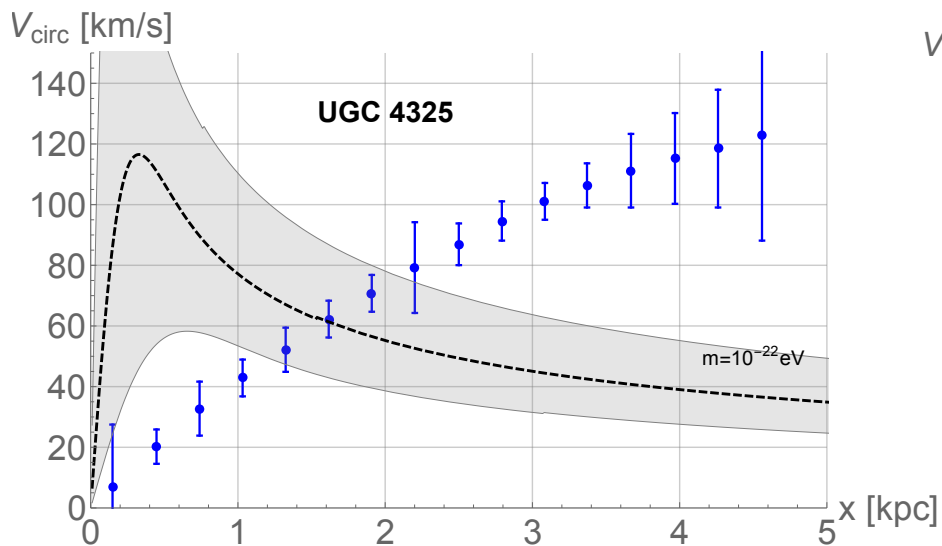
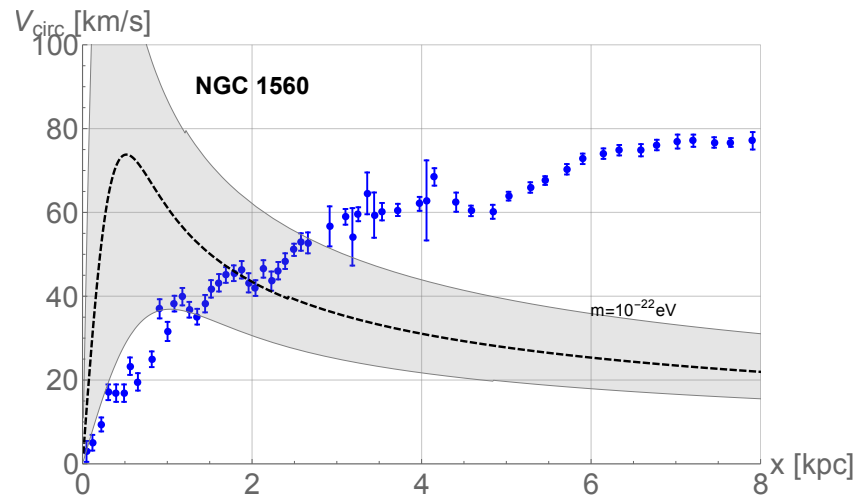
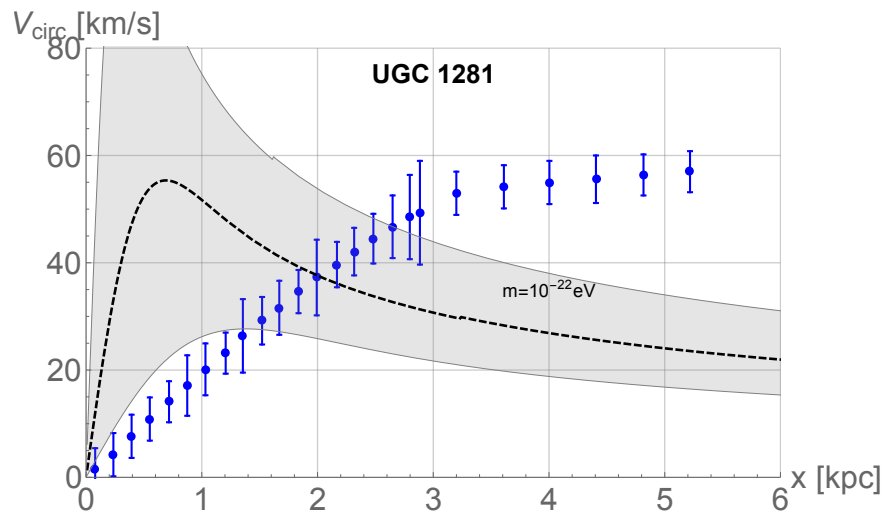


Bosma & de Blok 2002
HI+H α

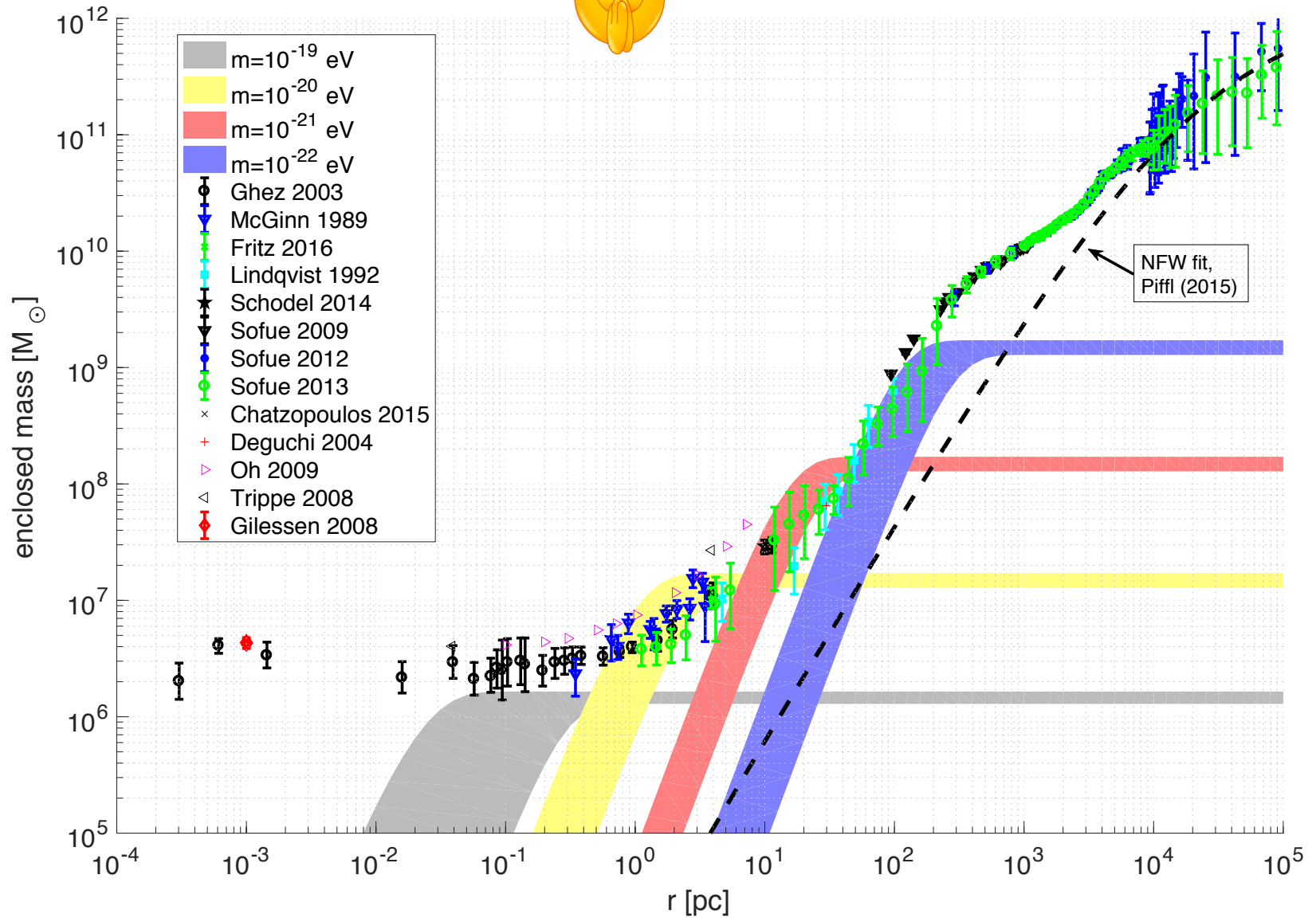


$$m = 10^{-22} \text{ eV}$$

(dozens of other galaxies look similar)



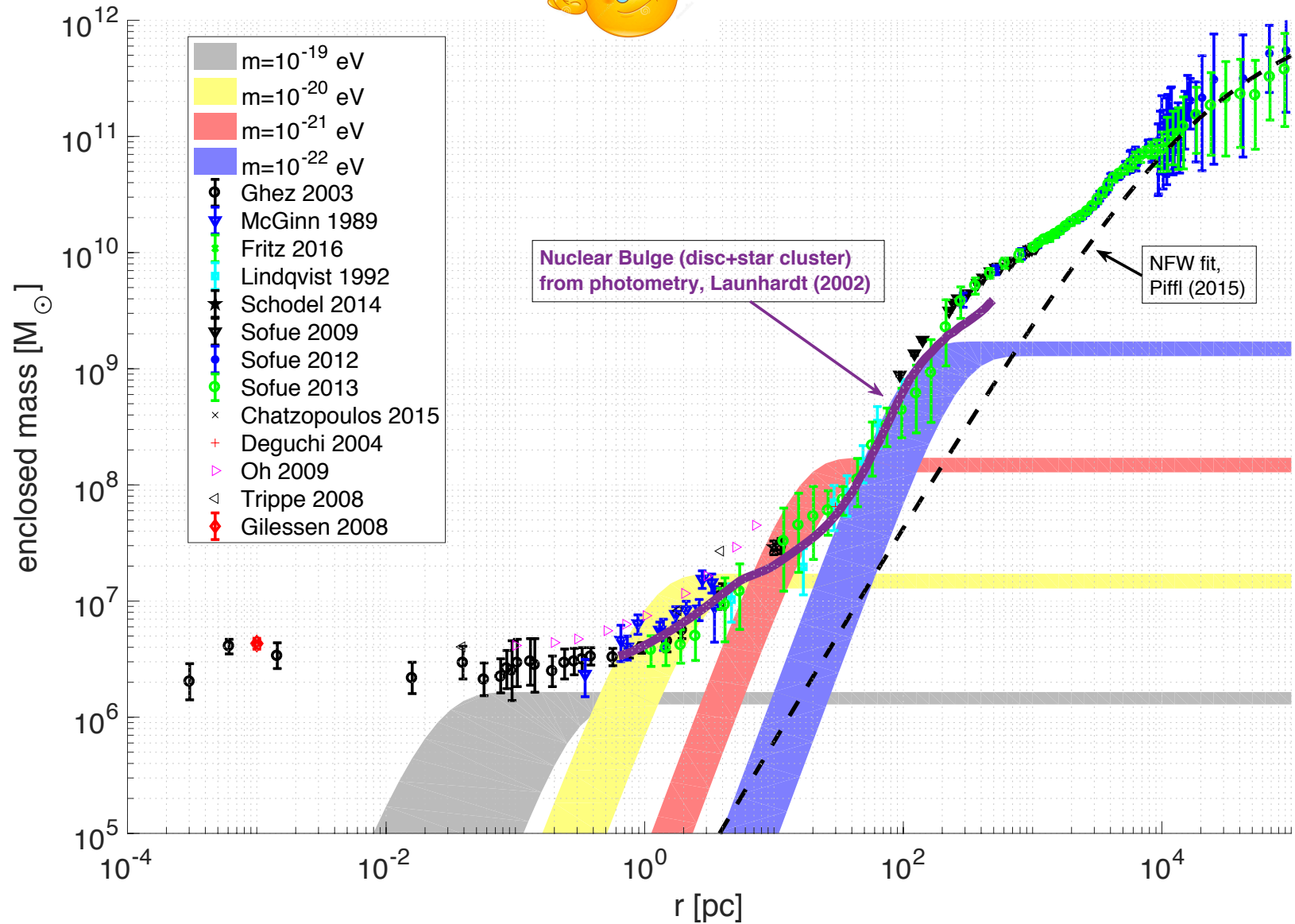
The Milky Way: nuclear bulge vs. soliton



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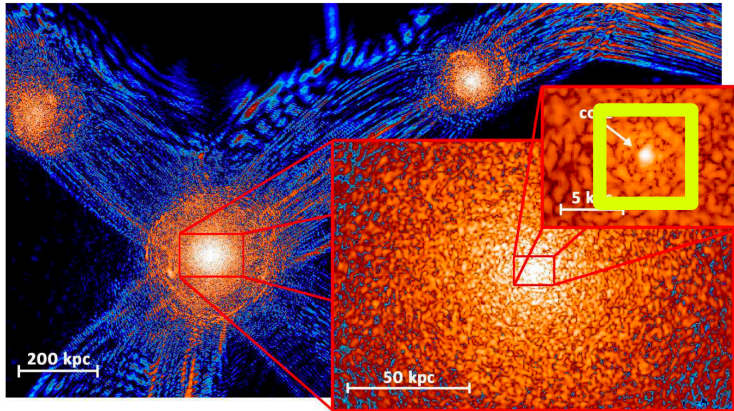
there are *probably* about 10^9 stars in there...



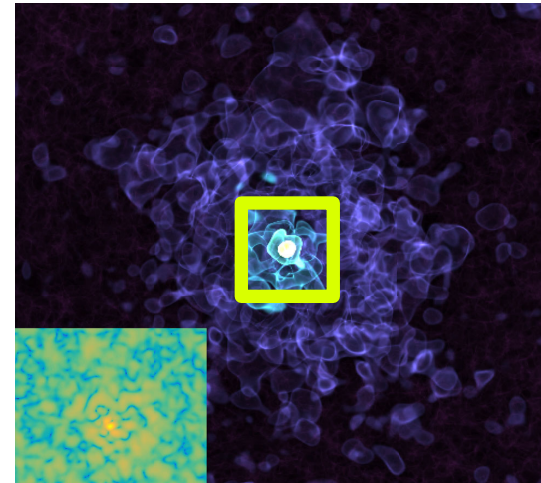
ULDM in galaxies



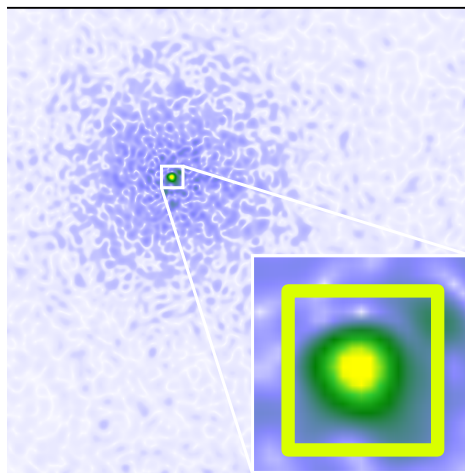
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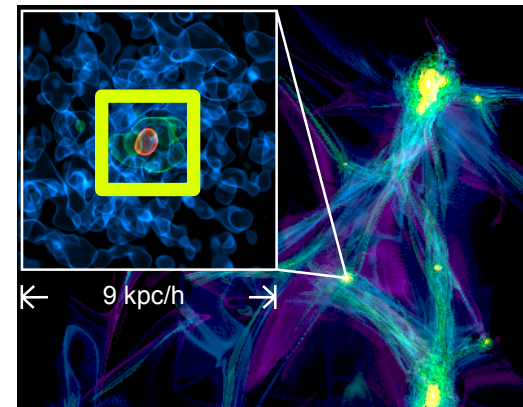
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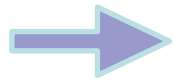


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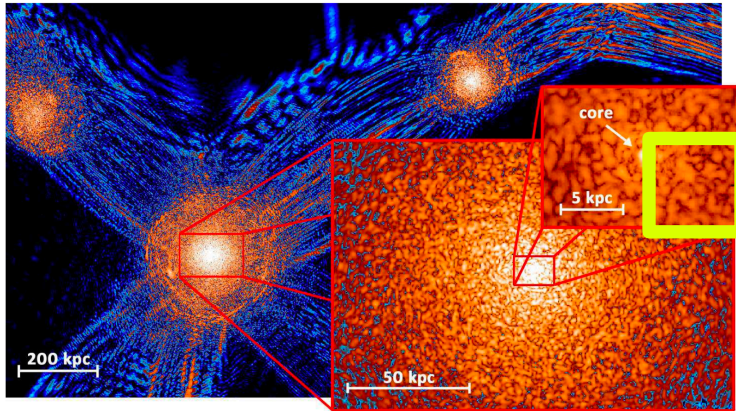
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ULDM in galaxies

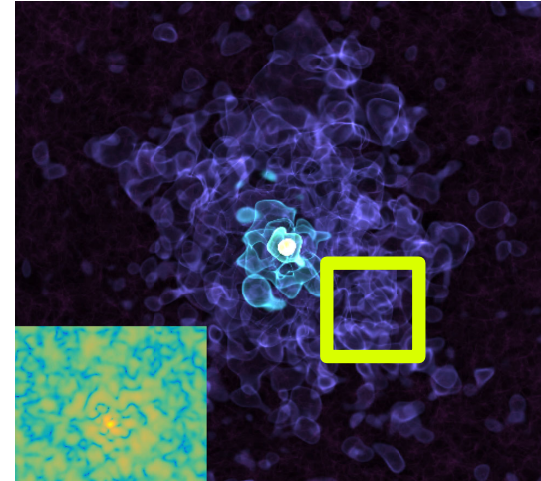


ULDM has more (unbound) substructure than CDM

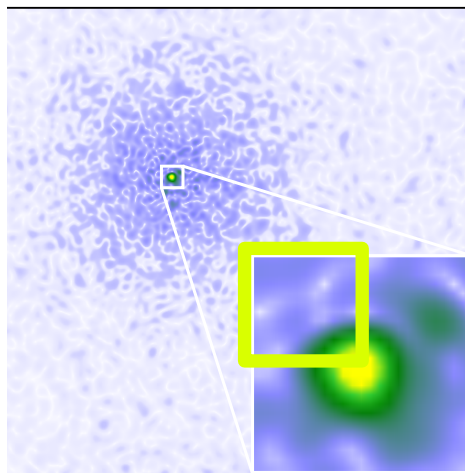
Hui et al, PRD95 (2017) no.4, 043541
Bar-Or, Fouvry, Tremaine,
Astrophys.J. 871 (2019) no.1, 28



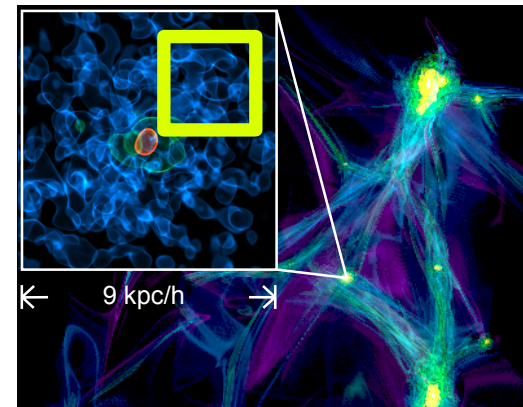
Schive et al, Nature Phys. 10 (2014) 496-499



Mocz et al, MNRAS. 471 (2017) 4559-4570



Levkov, Panin, Tkachev,
Phys.Rev.Lett. 121 (2018) 151301



Veltmaat, Niemeyer, Schwabe,
Phys.Rev. D98 (2018) 043509

ULDM in galaxies



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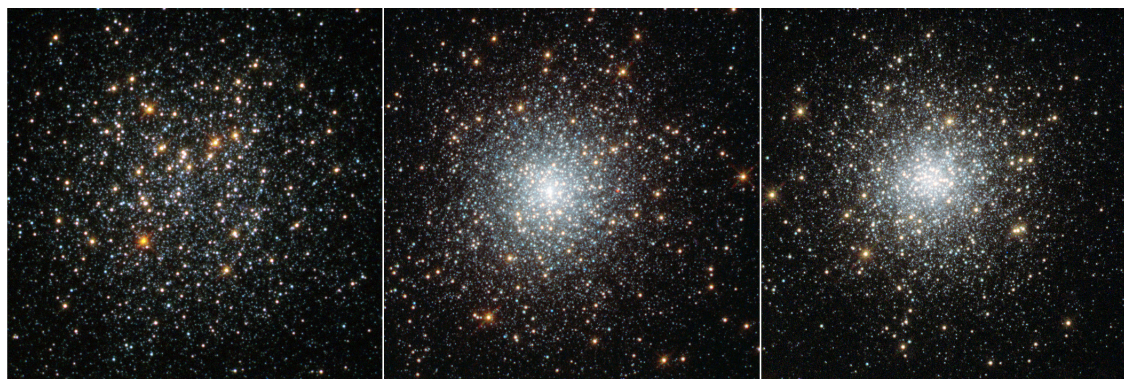
Hui et al, PRD95 (2017) no.4, 043541

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Astrophys.J. 871 (2019) no.1, 28

Orbital decay times for the globular clusters in Fornax for cold dark matter (CDM) and fuzzy dark matter (FDM)

n	projected radius	cluster mass	CDM		FDM		
	r_{\perp} (kpc)	$m_{\text{cl}} (M_{\odot})$	C	τ (Gyr)	kr	C	τ (Gyr)
1	1.6	3.7×10^4	4.29	112	8.90	2.46	215
2	1.05	1.82×10^5	3.32	9.7	5.04	1.88	12
3	0.43	3.63×10^5	2.45	0.62	0.97	0.29	2.2
4	0.24	1.32×10^5	2.50	0.37	0.31	0.033	10
5	1.43	1.78×10^5	3.46	21.3	7.79	2.32	31



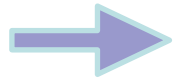
FORNAX 2

FORNAX 3

FORNAX 5

NASA, ESA, S. Larsen (Radboud University, the Netherlands)

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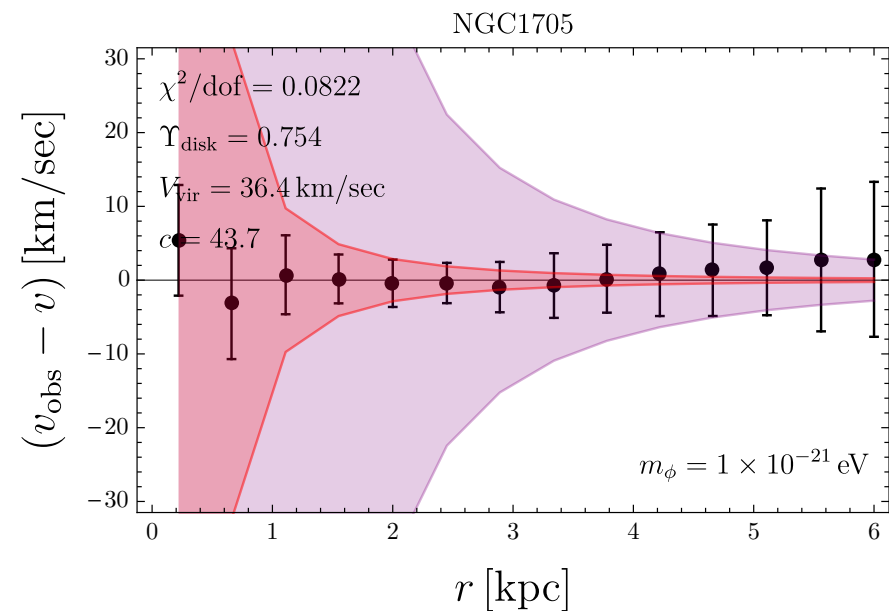
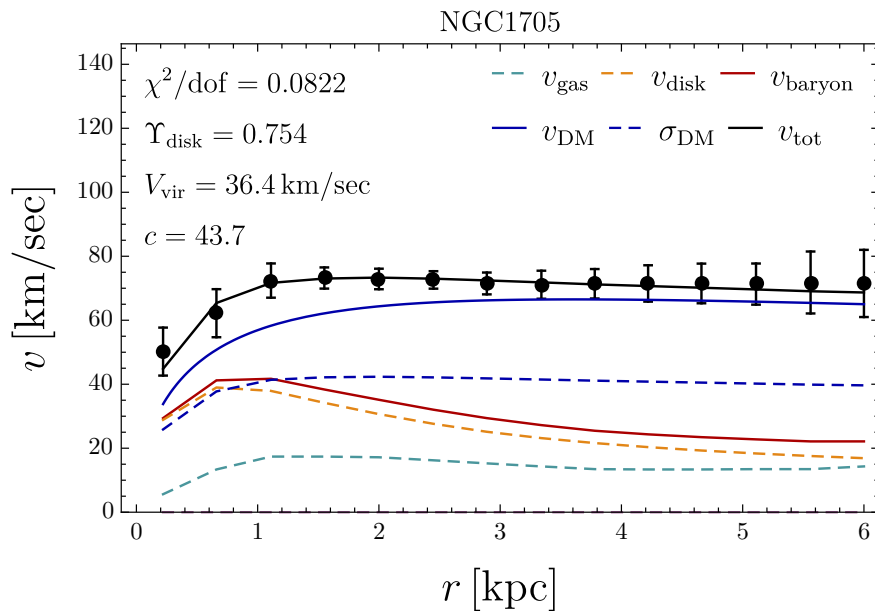
Hui et al, PRD95 (2017) no.4, 043541

Bar-Or, Fouvy, Tremaine,

Astrophys.J. 871 (2019) no.1, 28

In progress: ULDM vs. velocity dispersion in DSph and LSB galaxies

KB, Josh Eby, Hyungjin Kim, *in prep*



Summary

- * ULDM exhibits wave dynamics on scales \sim de Broglie wavelength.
- * Lends itself to analytic understanding (*nothing like this for WIMPs*).
- * Predicts features in inner kinematics of galaxies.

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As far as we could see, the core isn't there:

$m < 1e-21$ eV in tension with observations.

(disfavours ULDM from addressing small-scale puzzles of DM.)

Comparable independent constraints from Ly-alpha Forest

Armengaud (1703.09126), Irsic (1703.04683), Zhang (1708.04389), Kobayashi (1708.00015)

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Questions / work in progress:

Is the soliton—host halo relation correct? (or spurious effect of numerical simulations?)

If yes, what is the dynamical reason for it?

More observational tests of particle nature of dark matter, based on gravity alone?

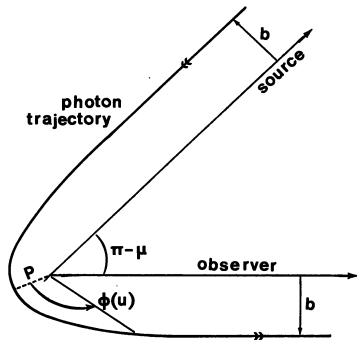
Xtra

Hui et al, Phys.Rev. D95 (2017) no.4, 043541
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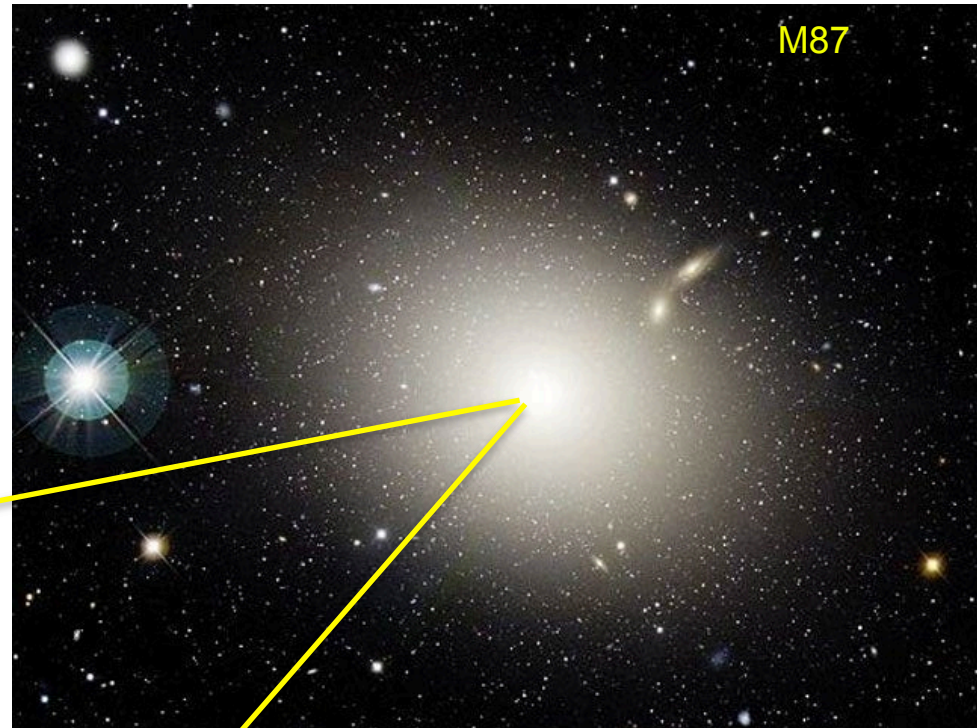


ESO and NASA/Canada-France-Hawaii Telescope, J.-C. Cuillandre (CFHT)

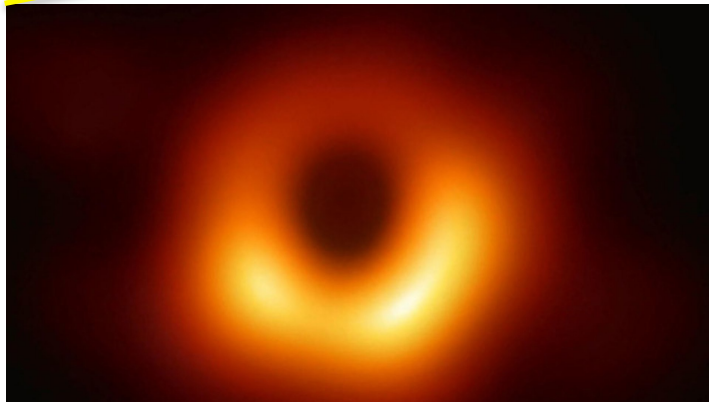
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J.-P. Luminet, Astron.Astrophys. 75 (1979) 228-235



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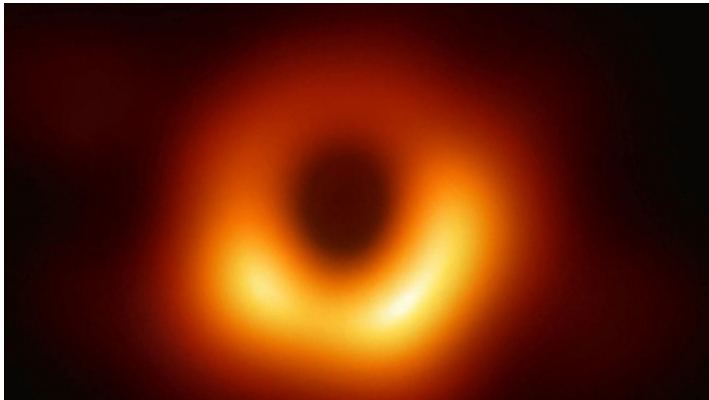


Event Horizon Telescope, Astrophys.J. 875 (2019) no.1, L6

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BH shadow **~ 0.00062 pc**

$$\frac{GM_{\text{BH}}}{c^2 D} = 3.8 \pm 0.4 \mu\text{arcsec}$$



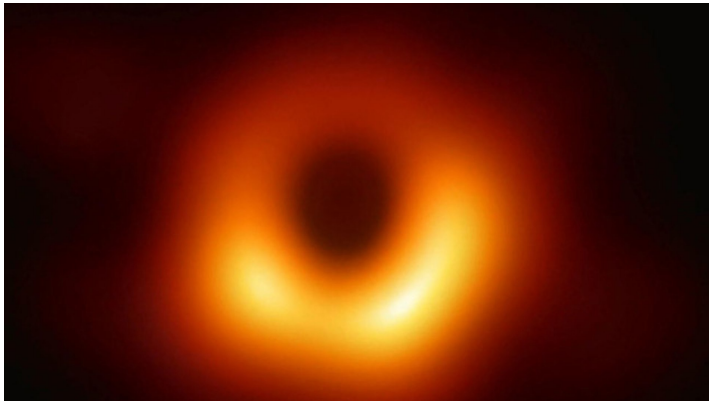
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➔ With EHT 2019, that's no longer plausible

BH shadow ~ 0.00062 pc

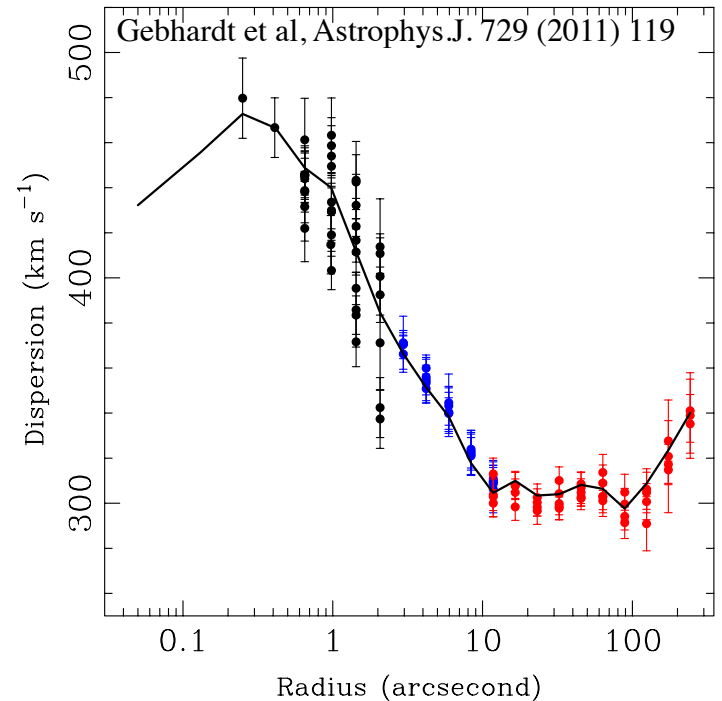
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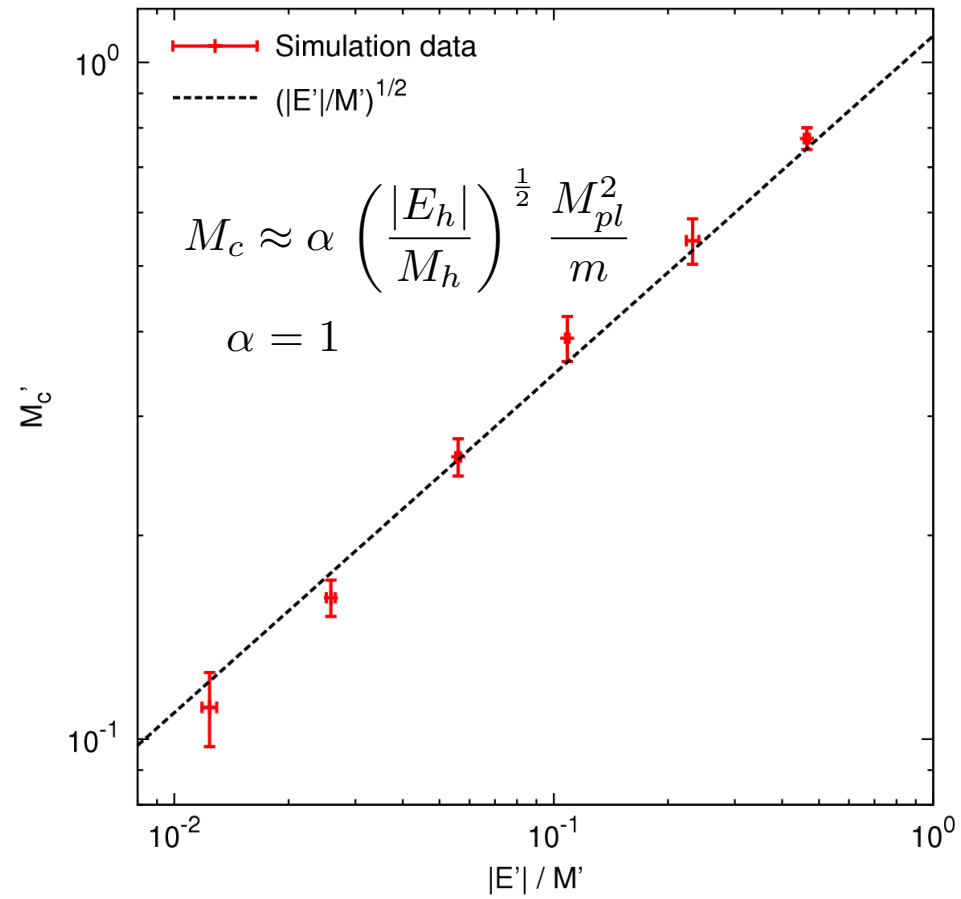
Stellar velocity dispersion ~ 500 pc

$$\frac{GM(\theta_*)}{c^2 D} = 3.6 \pm 0.2 \mu\text{arcsec}$$



Let's consider
numerical simulation results

Schive et al 1406.6586
Schive et al 1407.7762



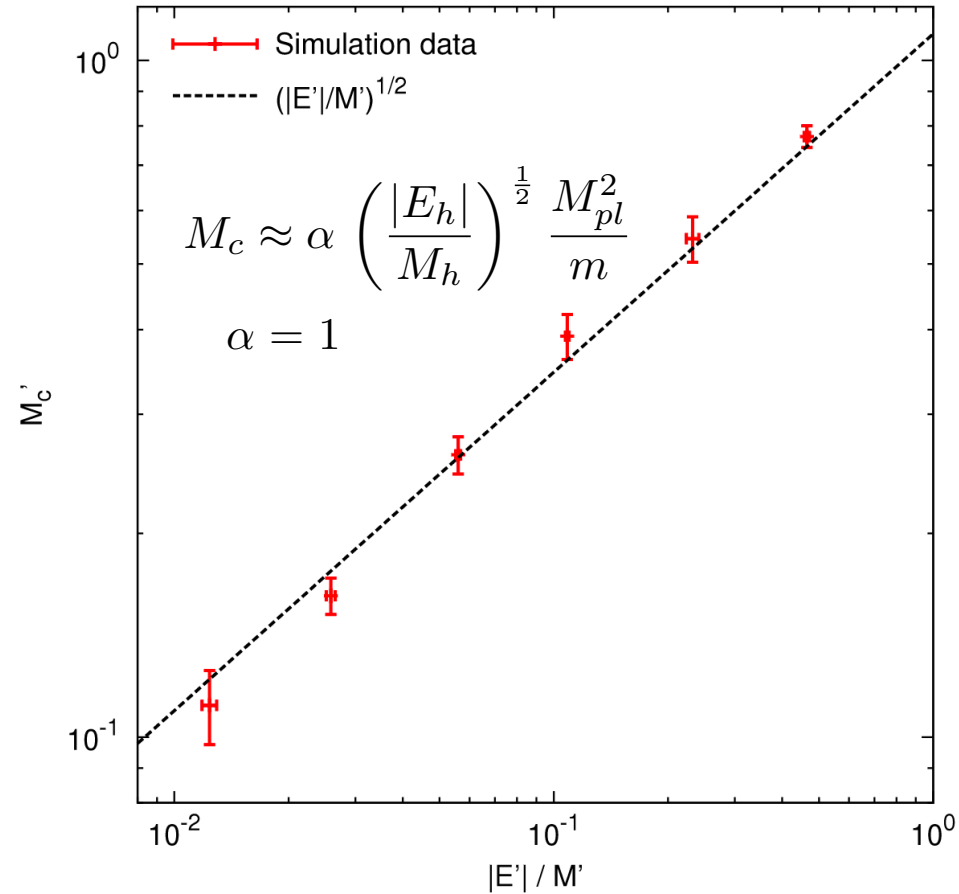
$$E = \int d^3x \left(\frac{|\nabla\psi|^2}{2m^2} + \frac{\Phi |\psi|^2}{2} \right)$$

Schive et al 1406.6586
Schive et al 1407.7762

$$E_\lambda \approx -0.476 \lambda^3 \frac{M_{pl}^2}{m},$$

$$M_\lambda \approx 2.06 \lambda \frac{M_{pl}^2}{m}.$$

➔
$$M_\lambda \approx 4.3 \left(\frac{|E_\lambda|}{M_\lambda} \right)^{\frac{1}{2}} \frac{M_{pl}^2}{m}$$



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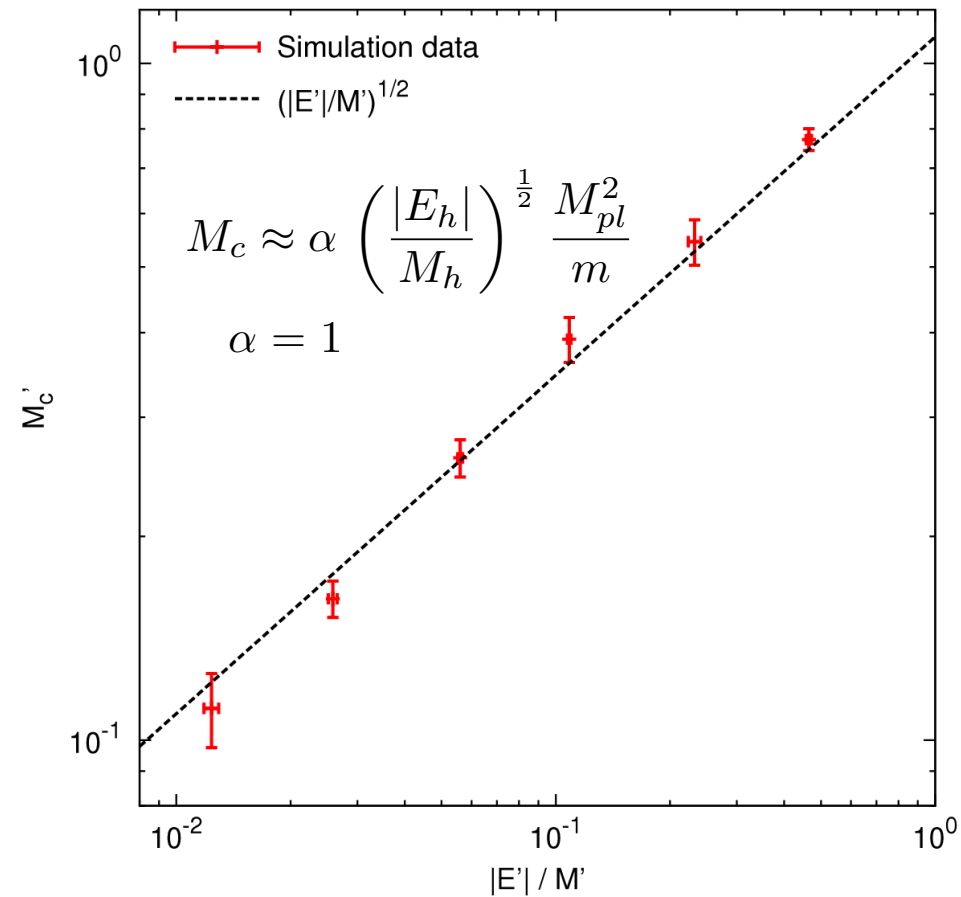
Schive et al 1407.7762

$$E_\lambda \approx -0.476 \lambda^3 \frac{M_{pl}^2}{m},$$

$$M_\lambda \approx 2.06 \lambda \frac{M_{pl}^2}{m}.$$

$$M_{c\lambda} \approx 0.236 M_\lambda$$

➔
$$M_{c\lambda} \approx 1.02 \left(\frac{|E_\lambda|}{M_\lambda} \right)^{\frac{1}{2}} \frac{M_{pl}^2}{m}$$



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Schive et al 1406.6586

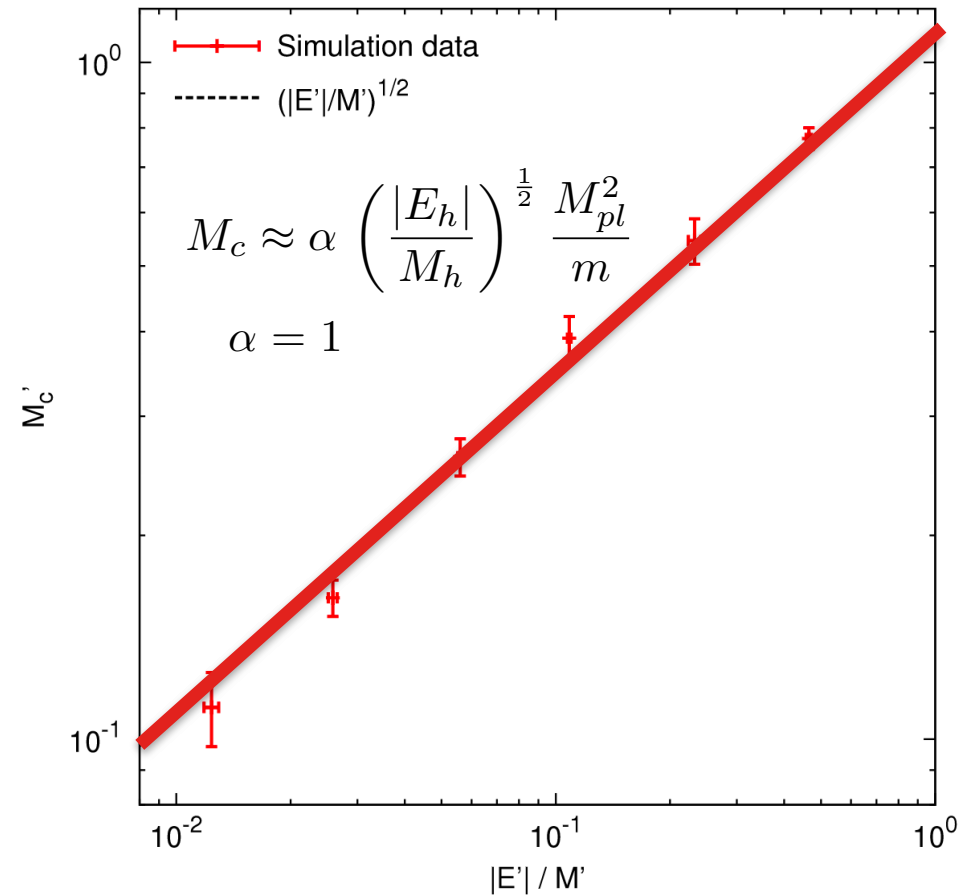
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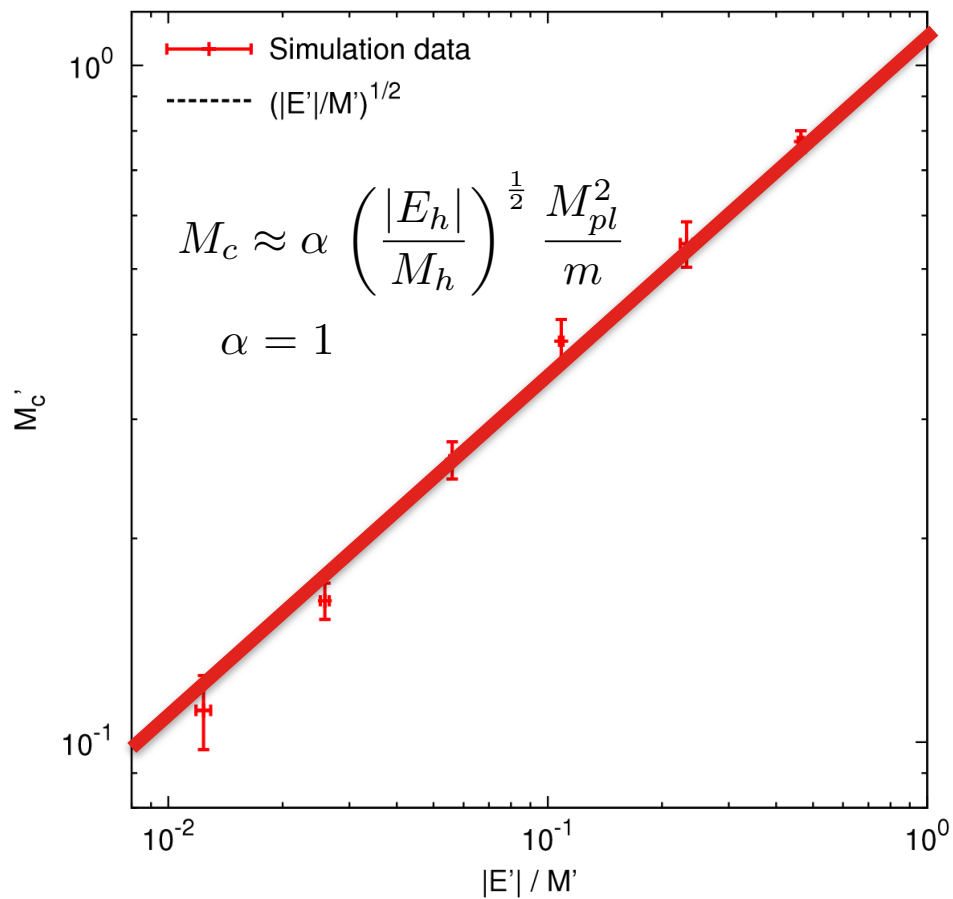


This is equivalent to:

$$\frac{E}{M} \Big|_{\text{soliton}} \approx \frac{E}{M} \Big|_{\text{halo}}$$

Bar, Blas, KB, Sibiryakov; 1805.00122

Schive et al 1406.6586
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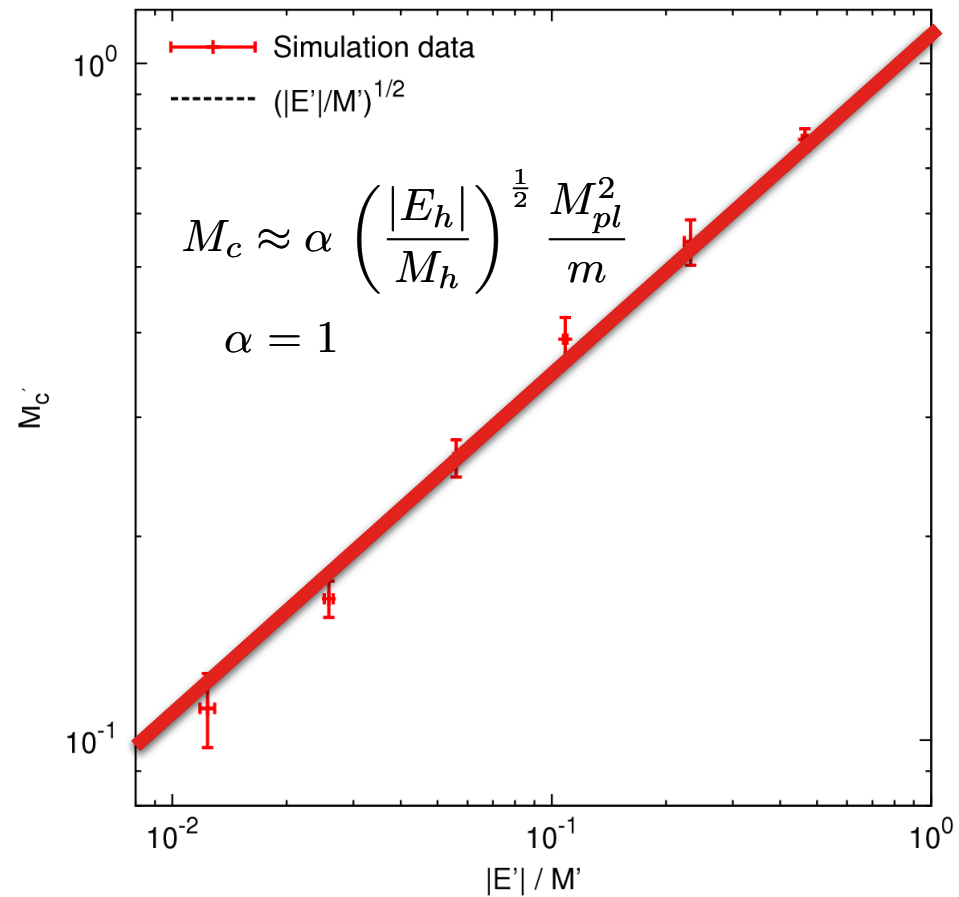
$$\frac{K}{M} \Big|_{\text{soliton}} = \frac{K}{M} \Big|_{\text{halo}}$$

Bar, KB, Sato, Eby; 1903.03402

K/M: kinetic energy/mass.

Schive et al 1406.6586

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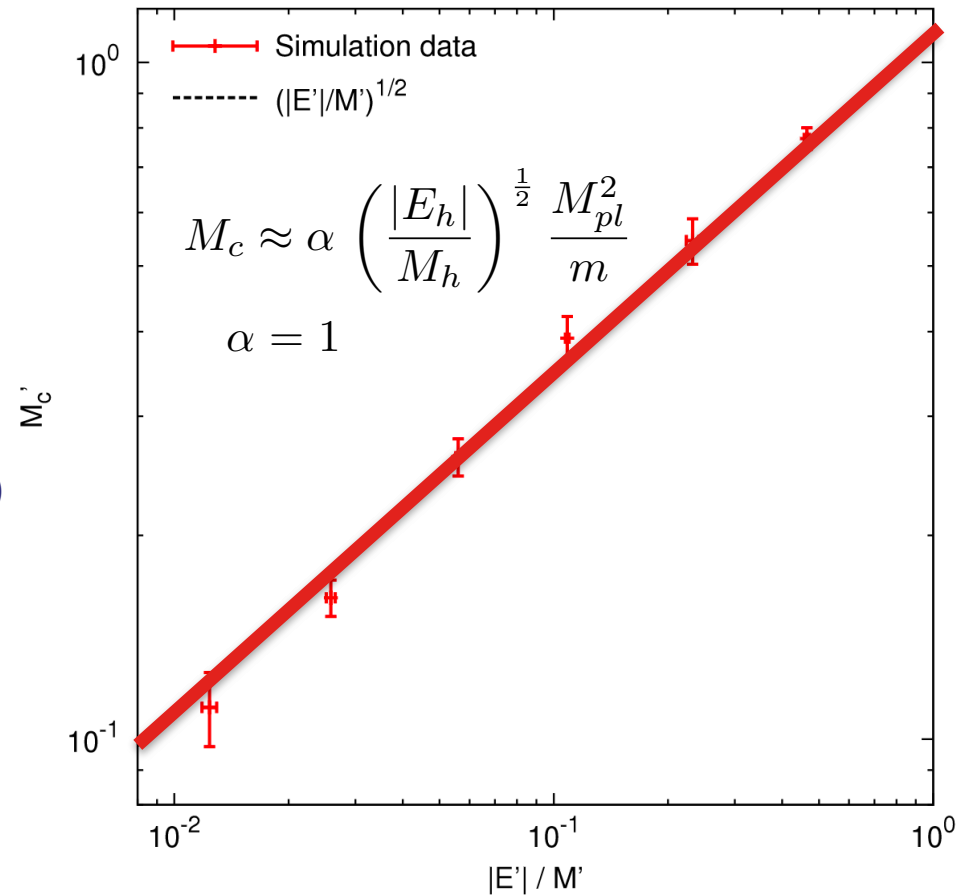
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Open questions

1. Is this actually true? (more simulations?)
2. If it is true, why?

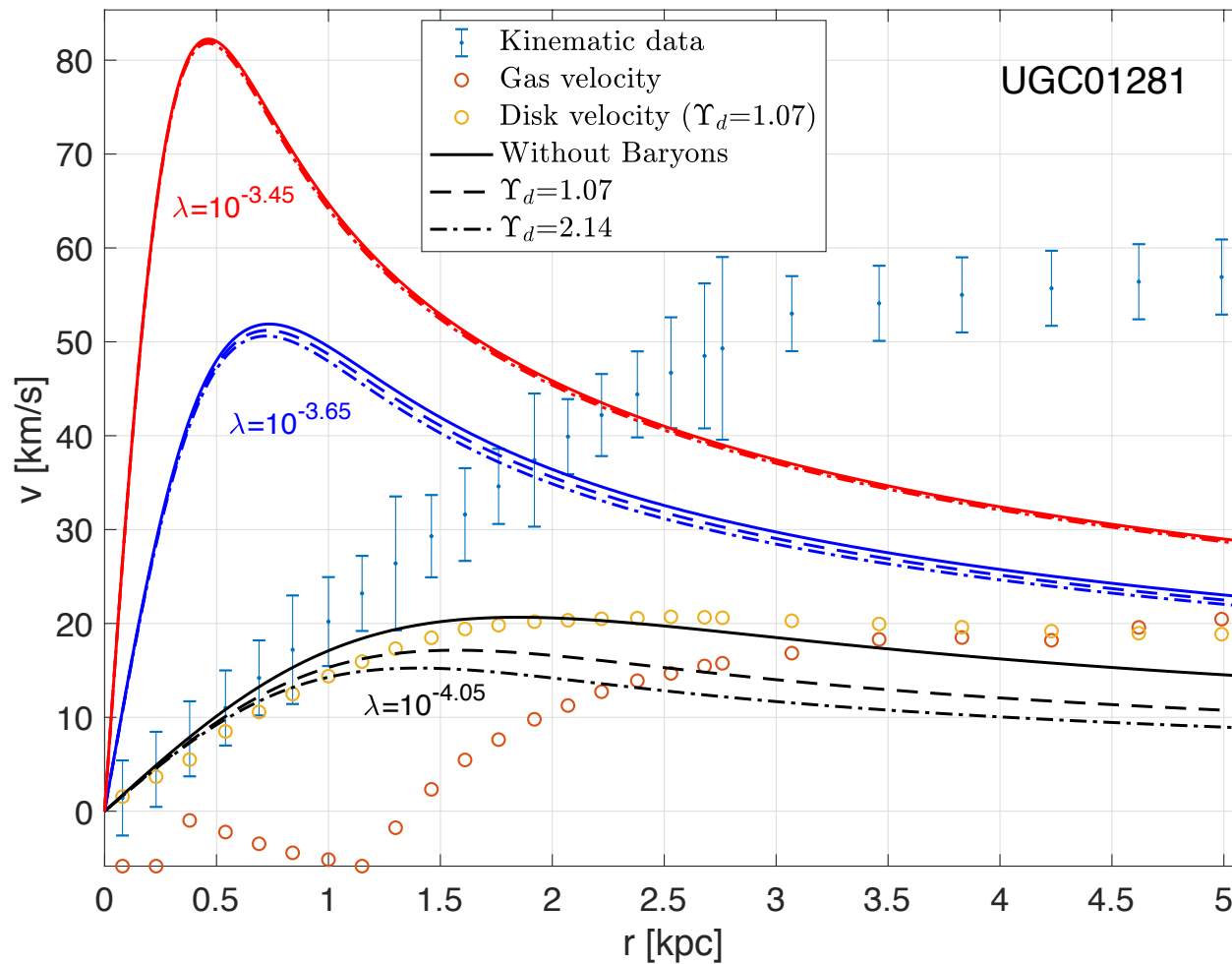
Schive et al 1406.6586

Schive et al 1407.7762



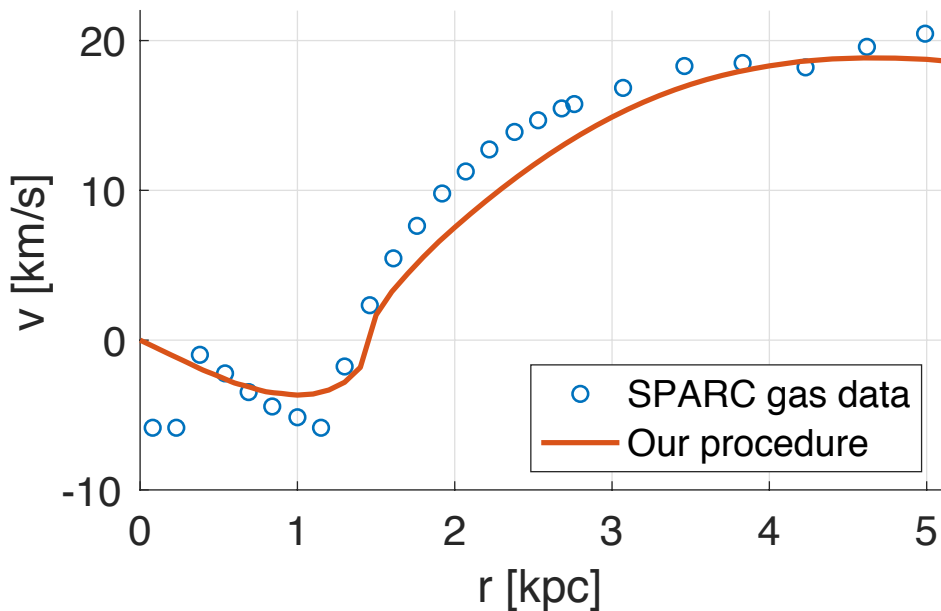
This galaxy is a relatively clean, low surface-brightness object.
From photometric+kinematic data, we can bound stellar+gas effects on K/M

Bar, KB, Sato, Eby; 1903.03402

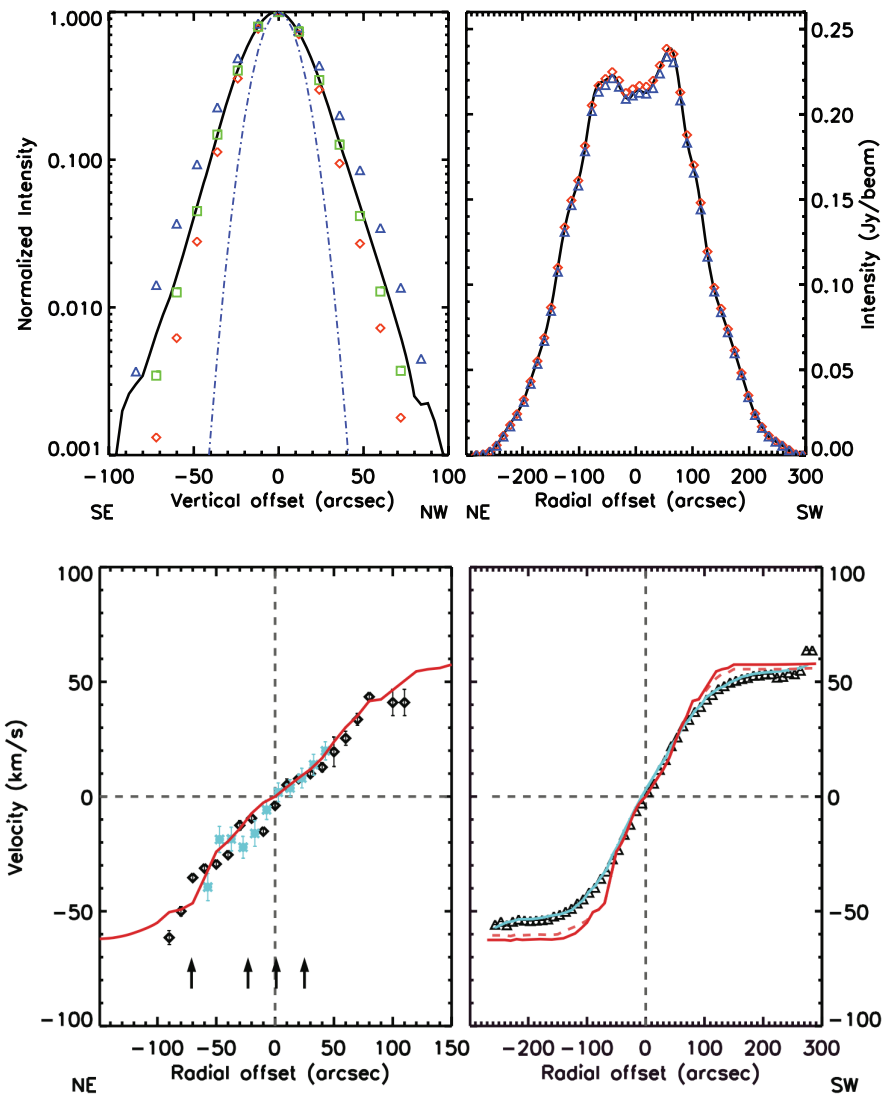


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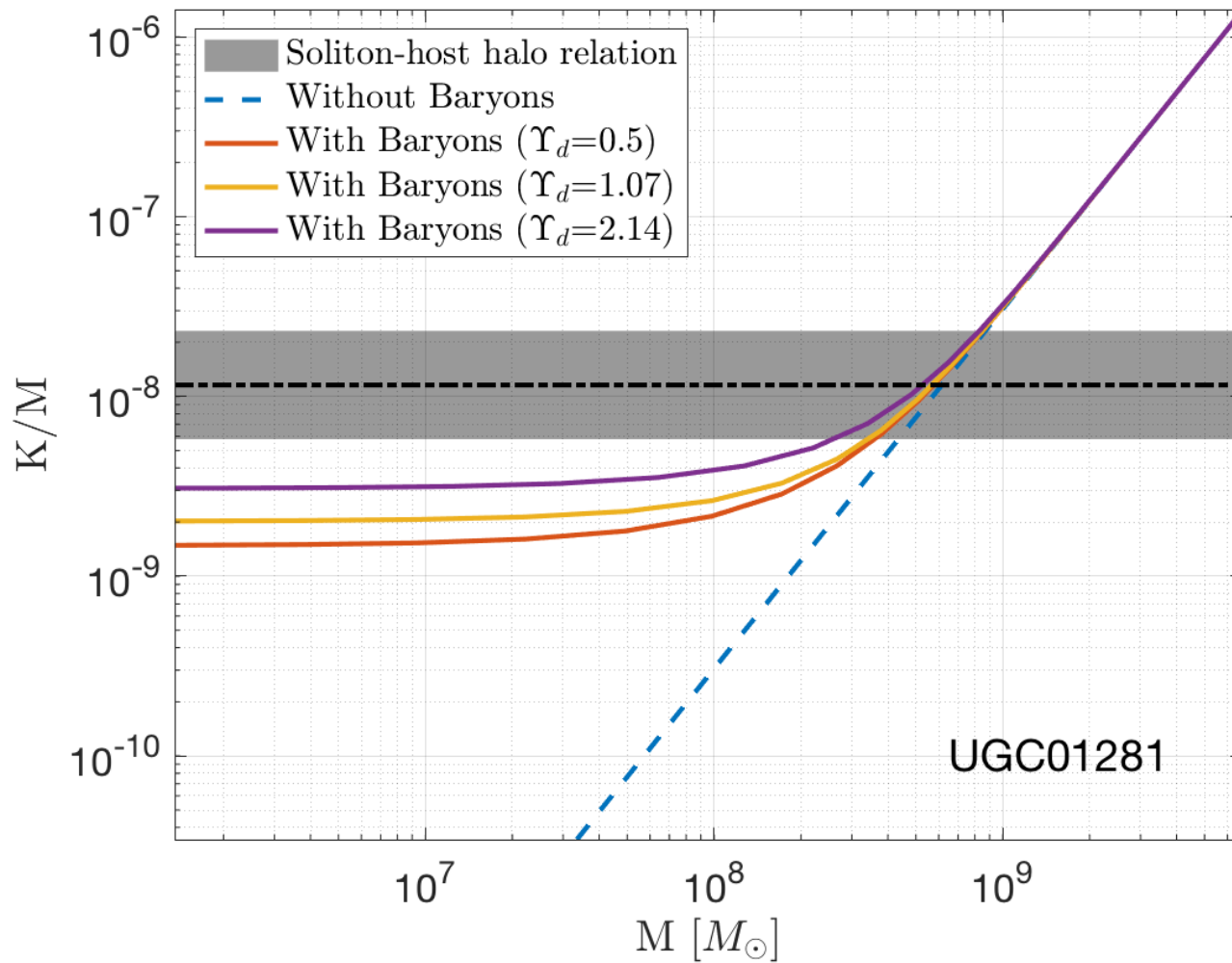
Bar, KB, Sato, Eby; 1903.03402



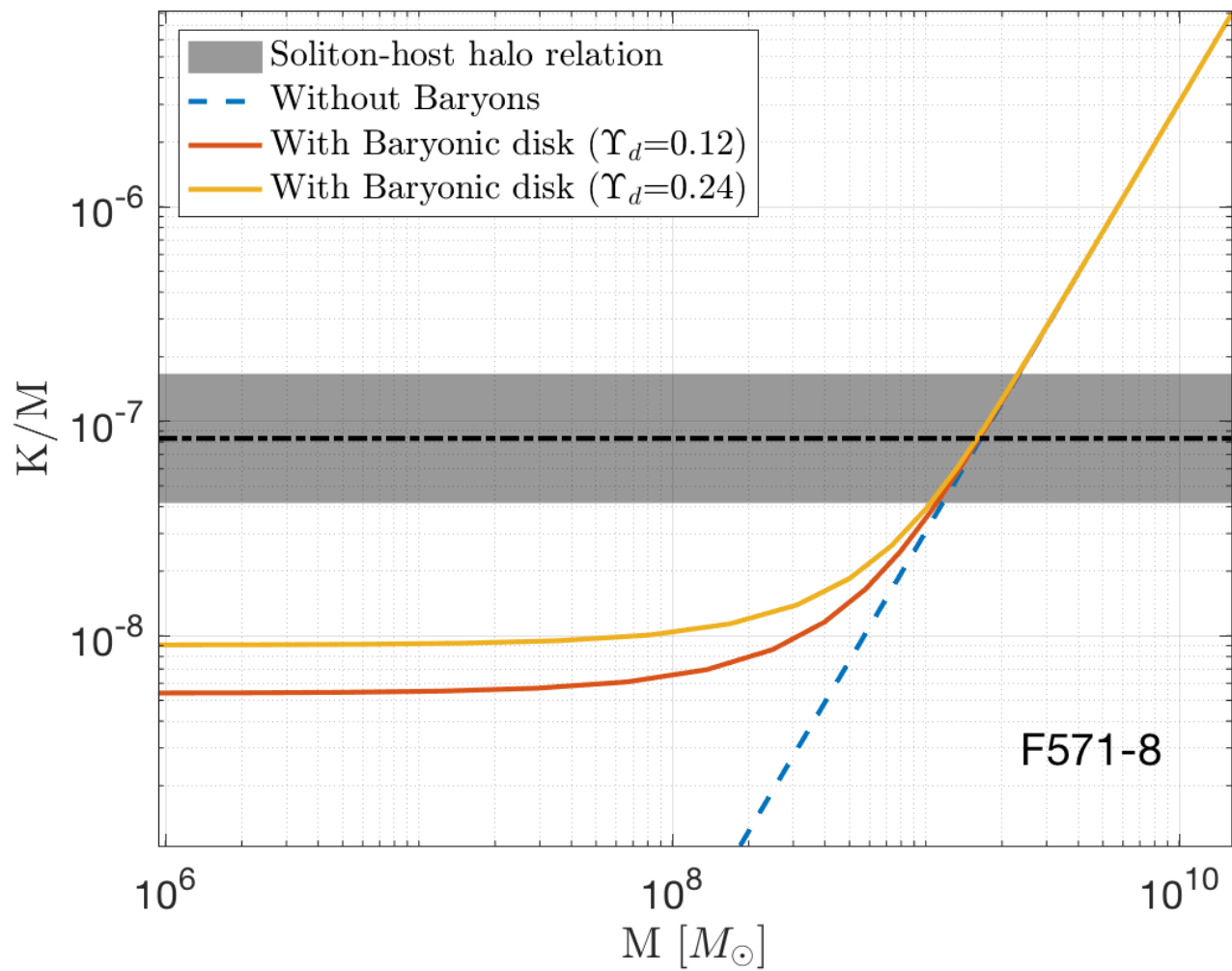
Kamphuis et al. MNRAS 414,3444 2011



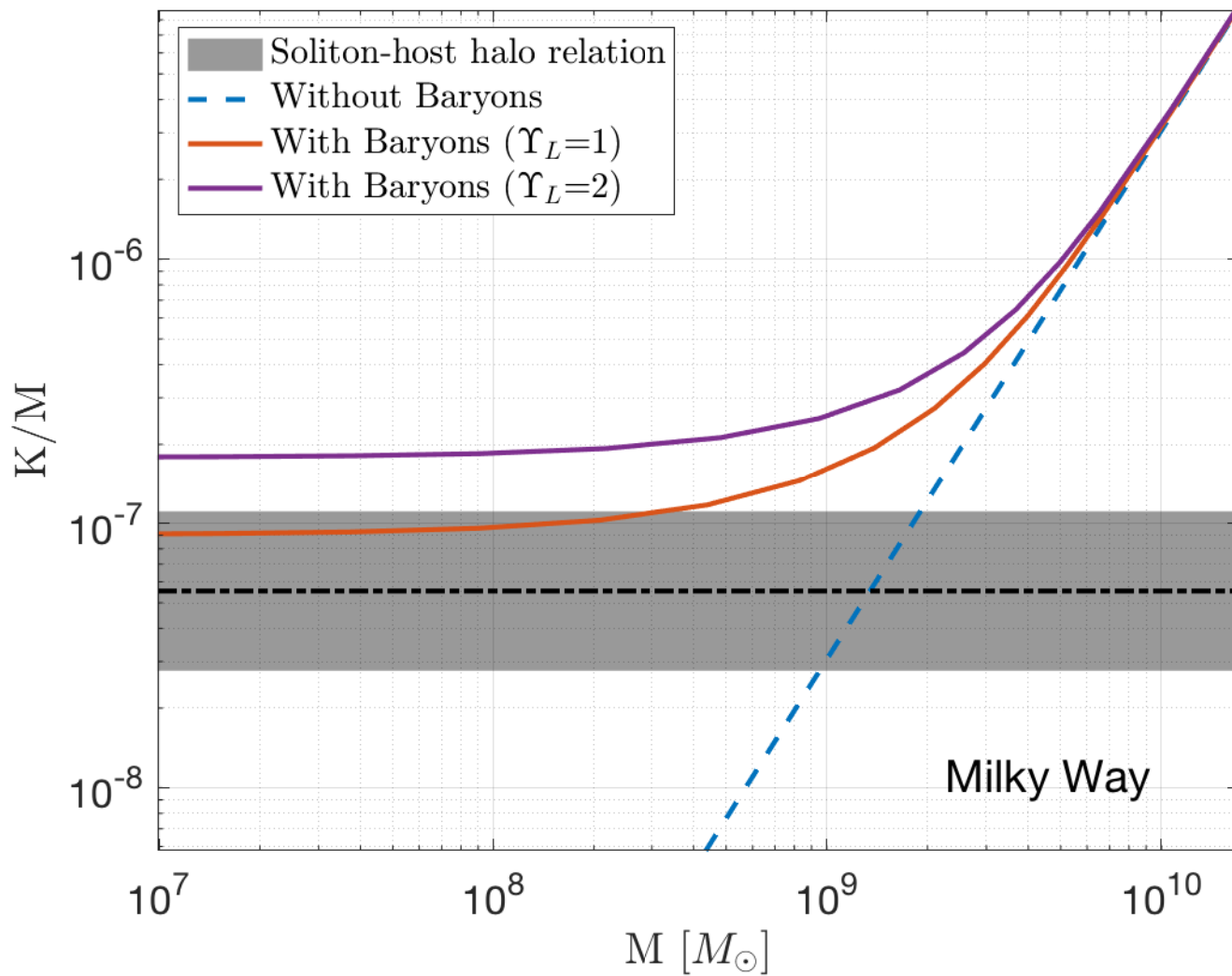
$m=1e-22$ eV

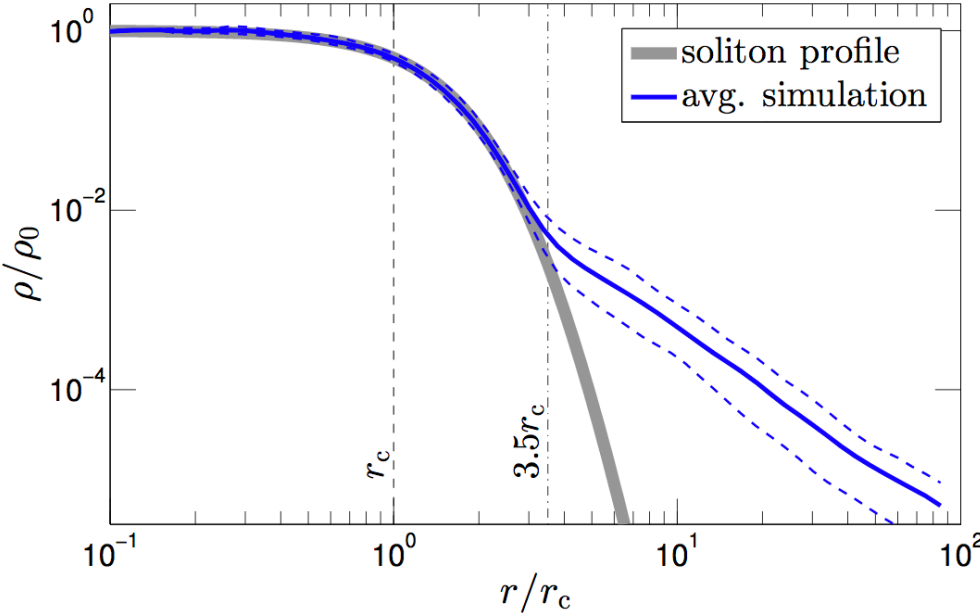
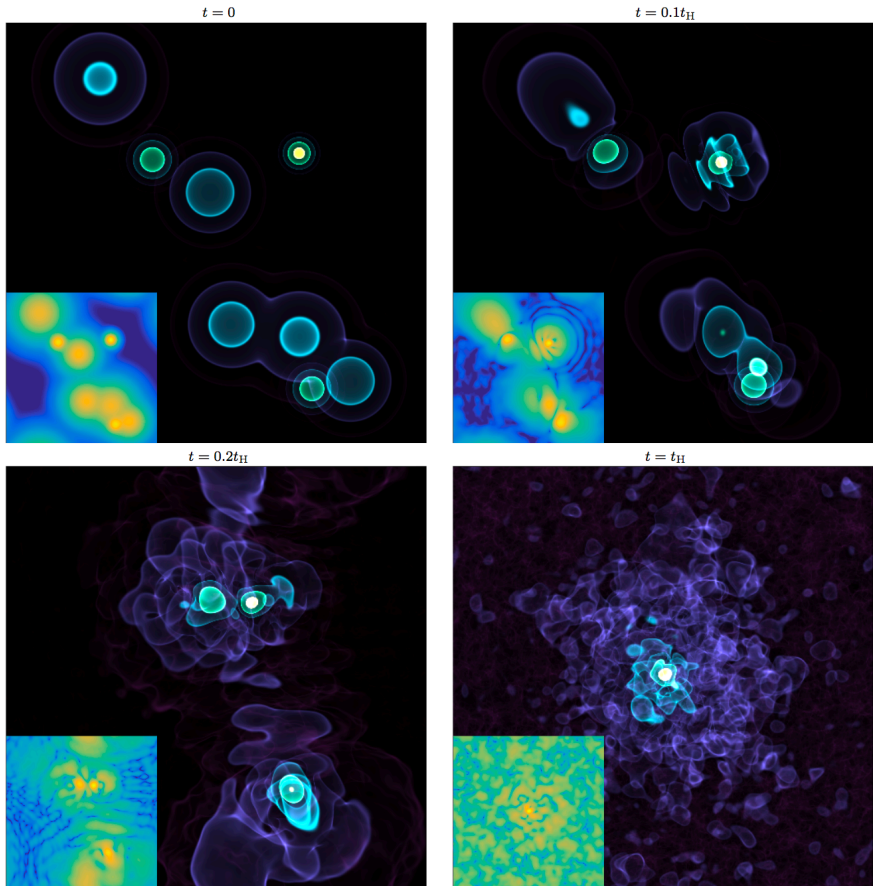


$m=1e-22$ eV



The Milky Way is much more difficult

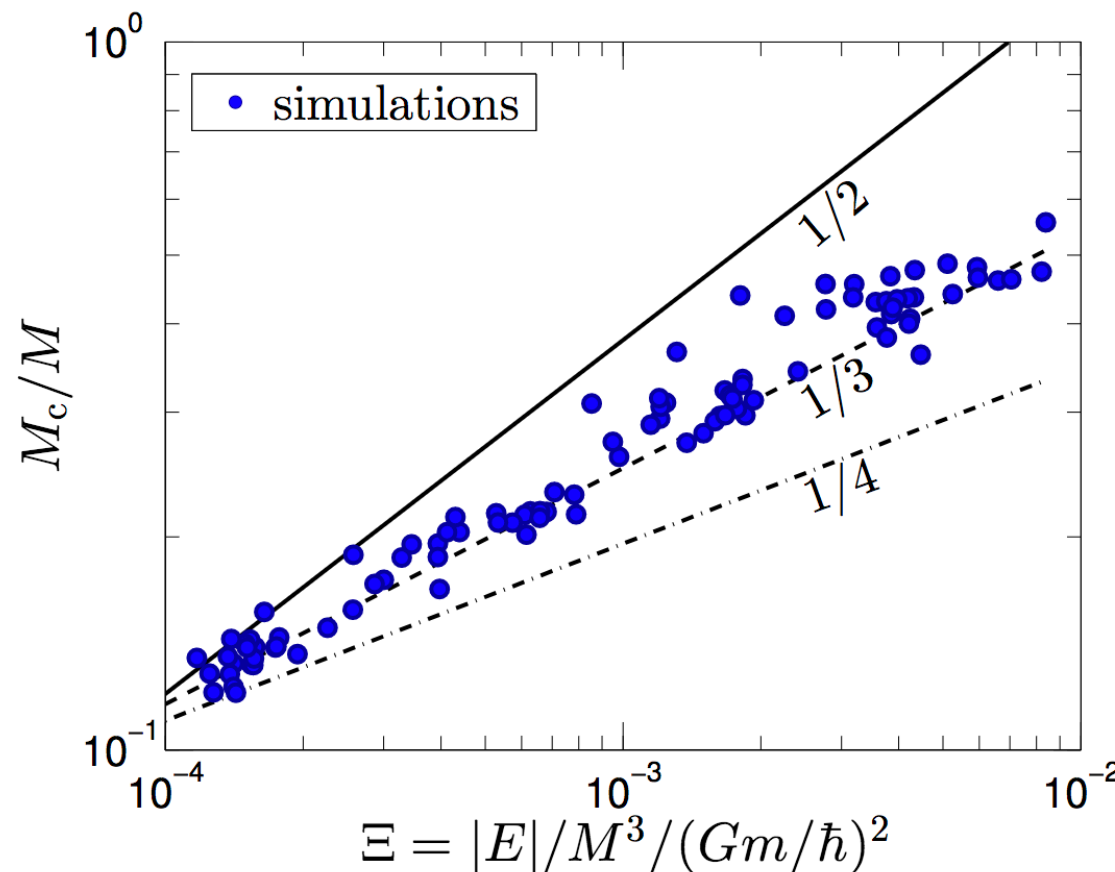




In our 100 simulations of virialized multi-body mergers, essentially characterised by a single parameter $\Xi \equiv |E|/M^3/(Gm/\hbar)^2$ set by the initial mass and energy (we have assumed no net angular momentum), we do find a fundamental relation between core mass M_c and Ξ .

$$M_c/M \simeq 2.6\Xi^{1/3} = 2.6\left(\frac{|E|}{M^3(Gm/\hbar)^2}\right)^{1/3}, \quad (32)$$

which reproduces our simulations spanning two orders of magnitude in E , as shown in Fig. 4. More precisely, a nu-



Analytic soliton:

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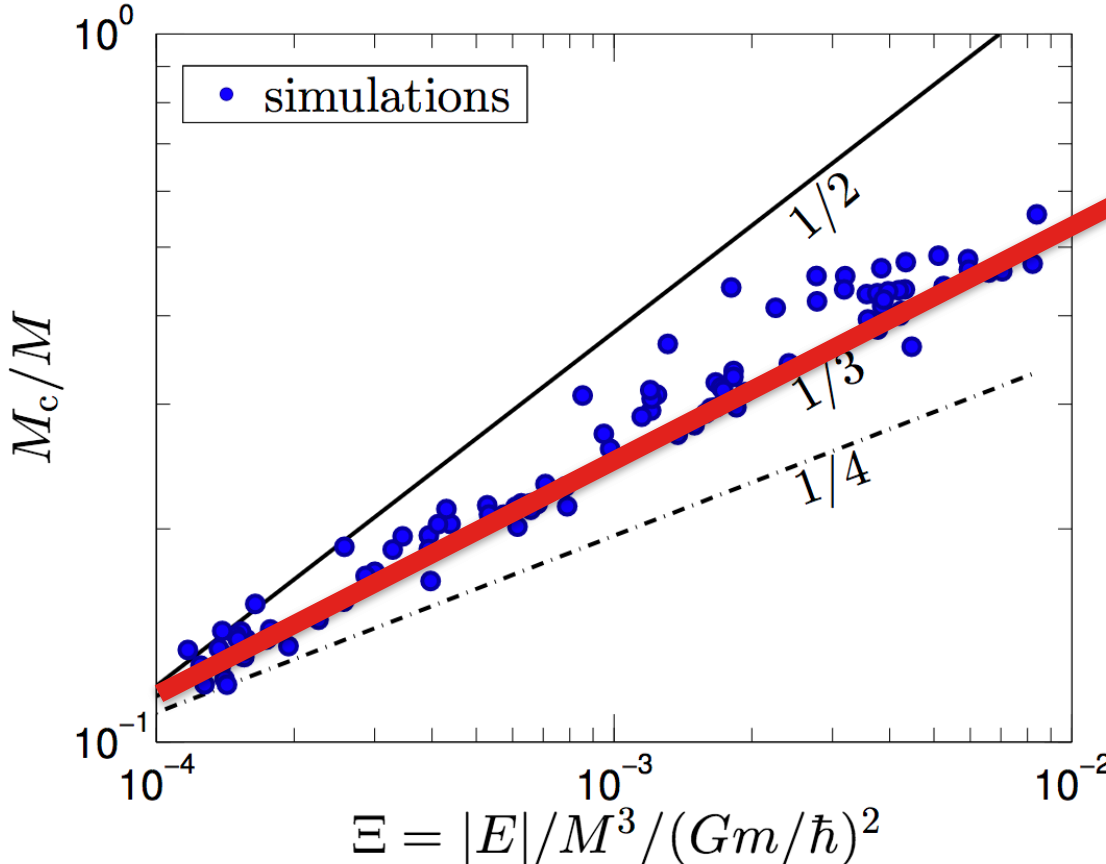
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Mocz et al 1705.05845

This means that the total energy in the simulation box was eaten up by 1 soliton.

Should not apply to real galaxies above $\sim 1e8$ Msol

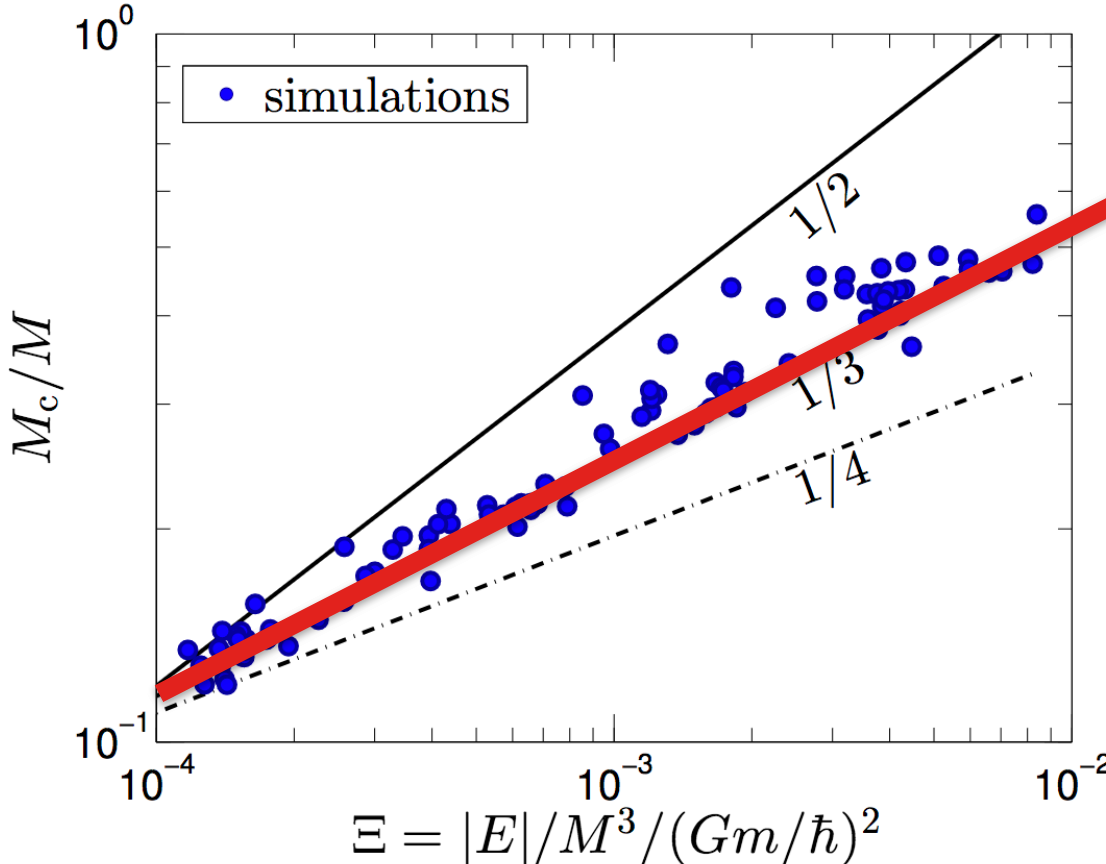
(initial conditions?)

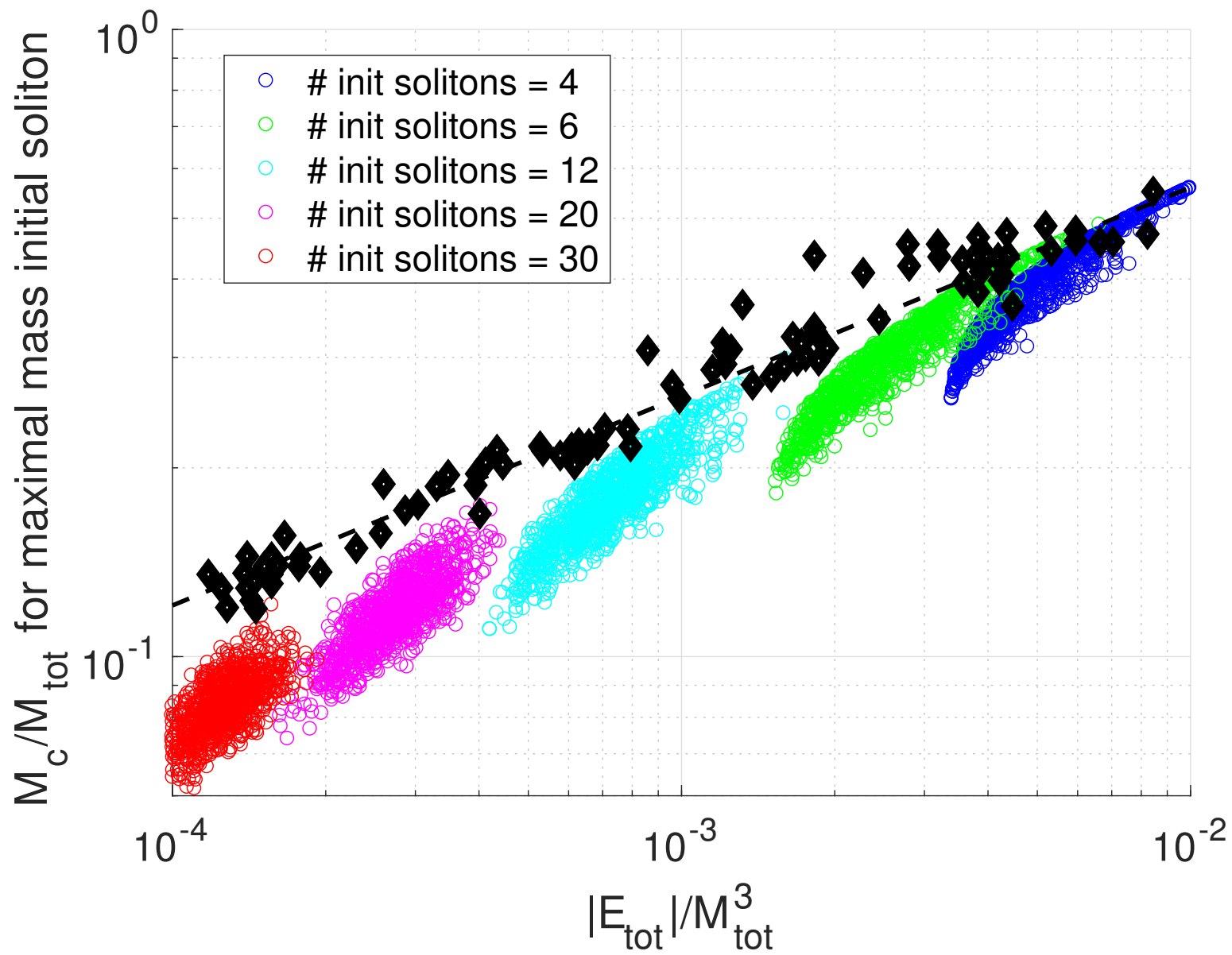
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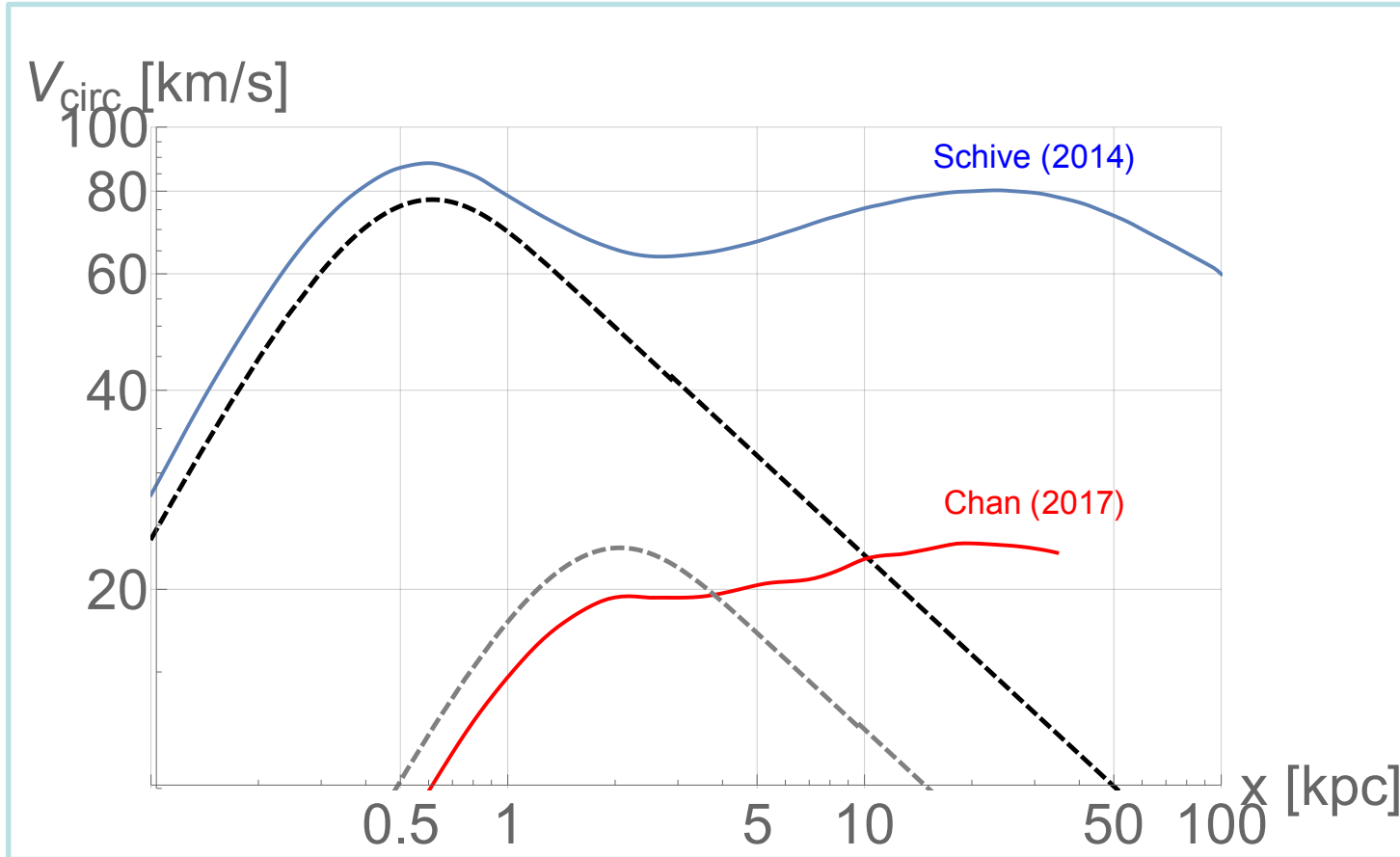
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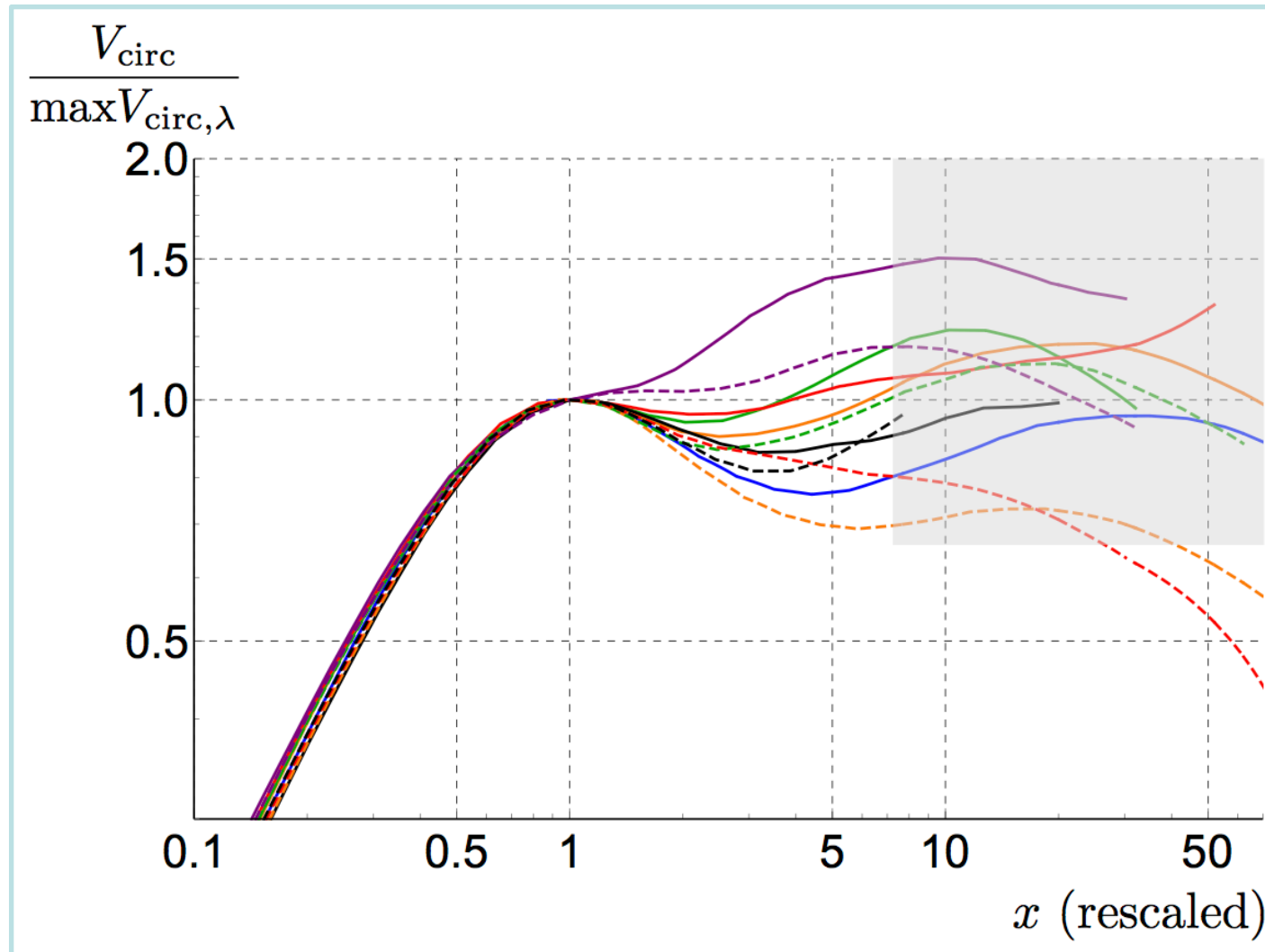
Rotation curves from simulations:

Soliton/halo equal specific kinetic energy ==> equal characteristic velocity



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Soliton/halo equal specific kinetic energy ==> equal characteristic velocity



Non-gravitational interactions

$$\delta V(\phi) = \frac{\kappa \phi^4}{4}$$

$$|\kappa| < \frac{2m^2}{x_{c\lambda}^2 \rho_{c\lambda}} \quad \longrightarrow \quad |\kappa| < 4 \times 10^{-93} \left(\frac{m}{10^{-22} \text{eV}} \right)^2 \left(\frac{M_h}{10^{12} M_\odot} \right)^{-\frac{2}{3}}$$

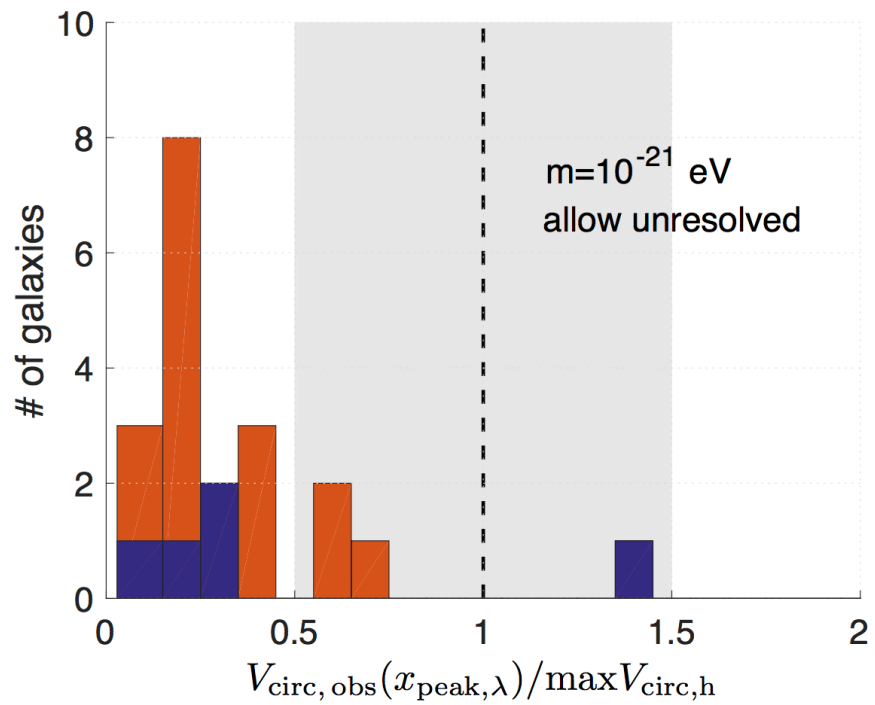
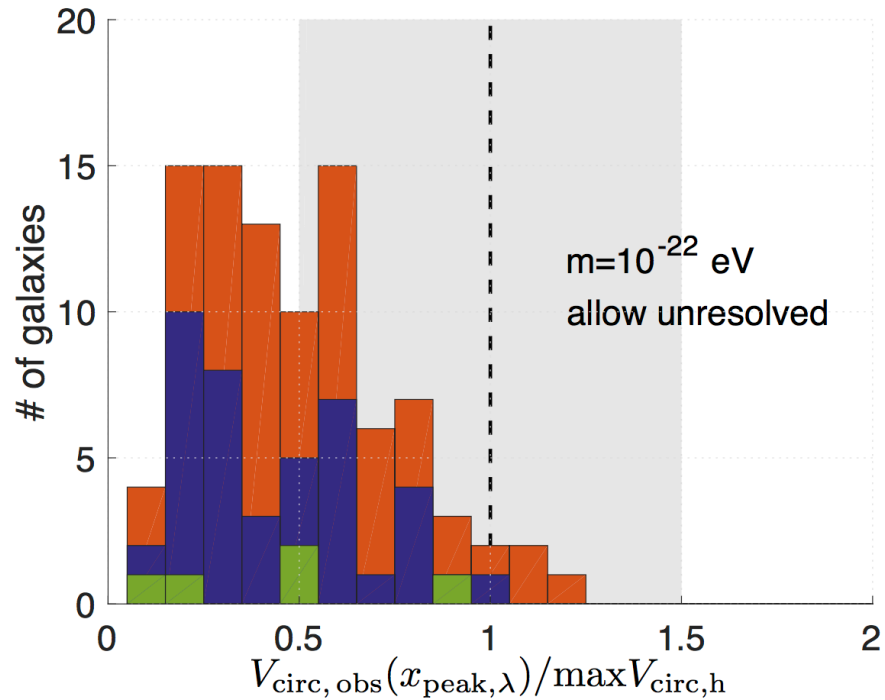
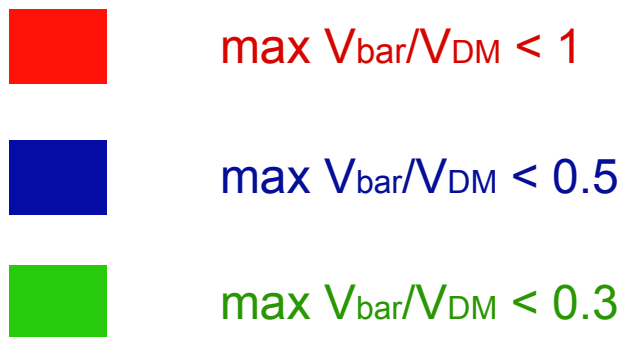
$$V(\phi) = m^2 f^2 (1 - \cos(\phi/f))$$

$$\longrightarrow \quad \kappa = -\frac{m^2}{6f^2} \\ \approx -1.7 \times 10^{-97} \left(\frac{m}{10^{-22} \text{eV}} \right)^2 \left(\frac{f}{10^{17} \text{GeV}} \right)^{-2}$$

SPARC Lelli et al, 1606.09251

175 rotation curves

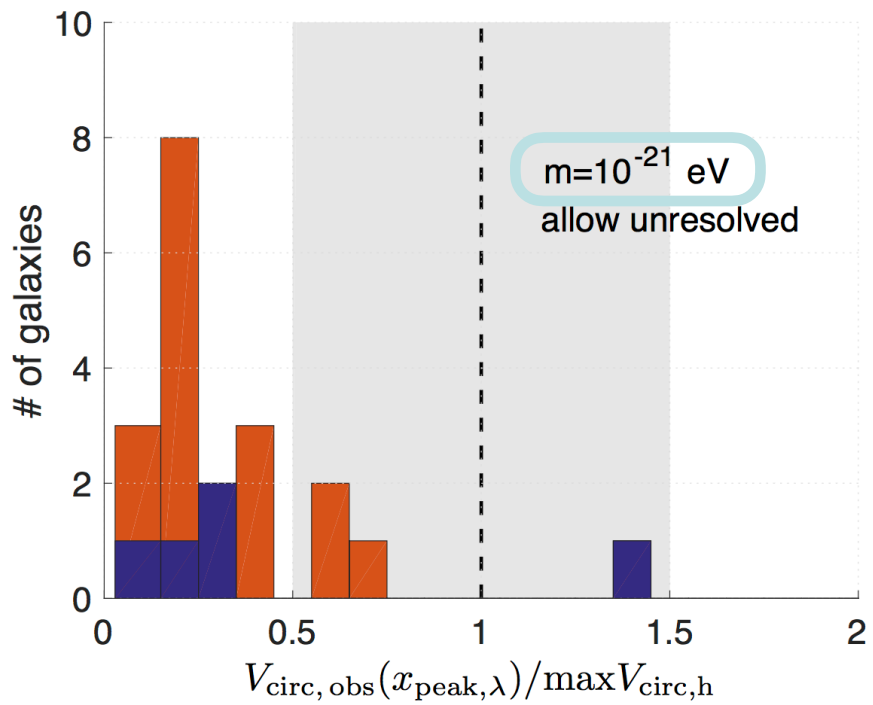
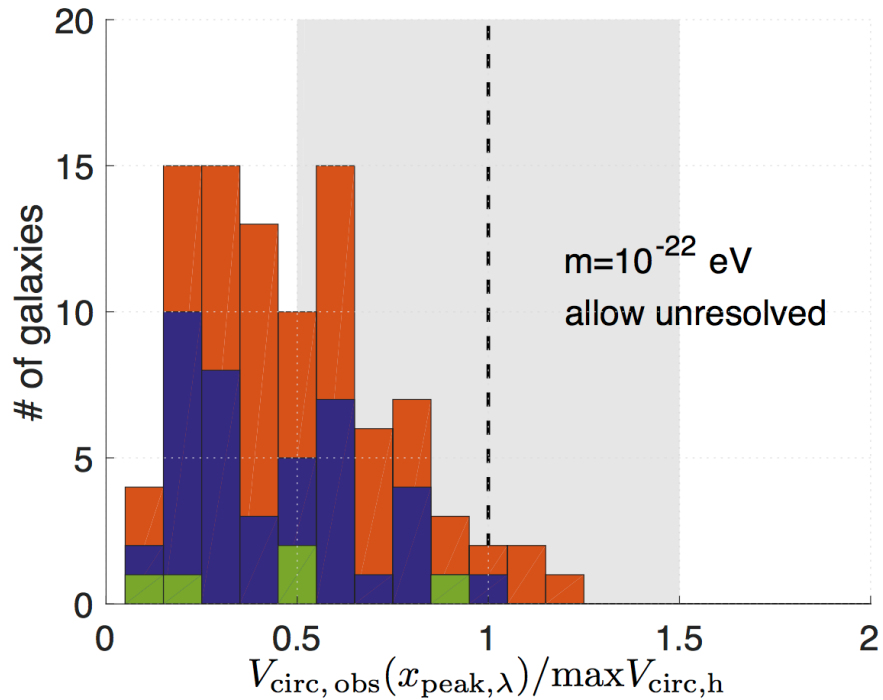
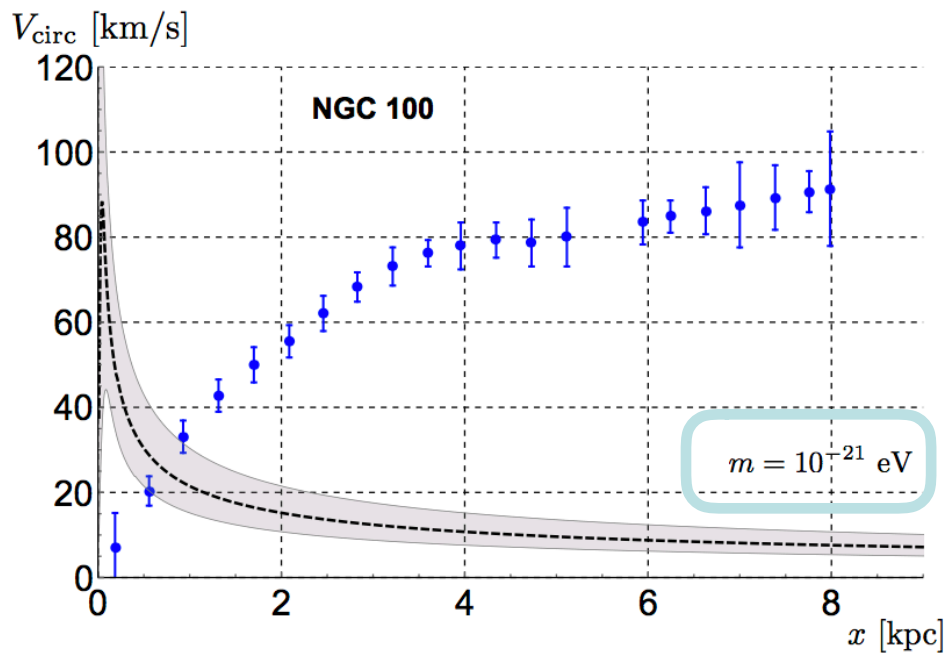
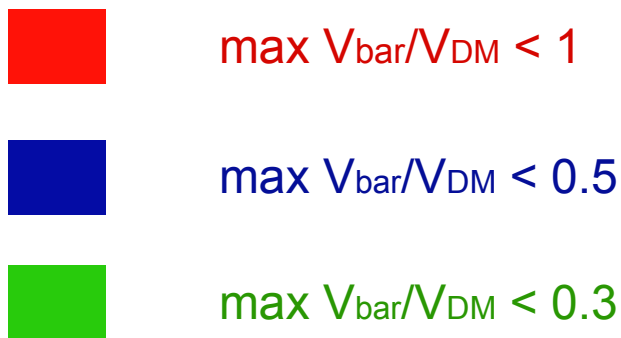
- * 3.6um
- * HI + Halpha rotation curves



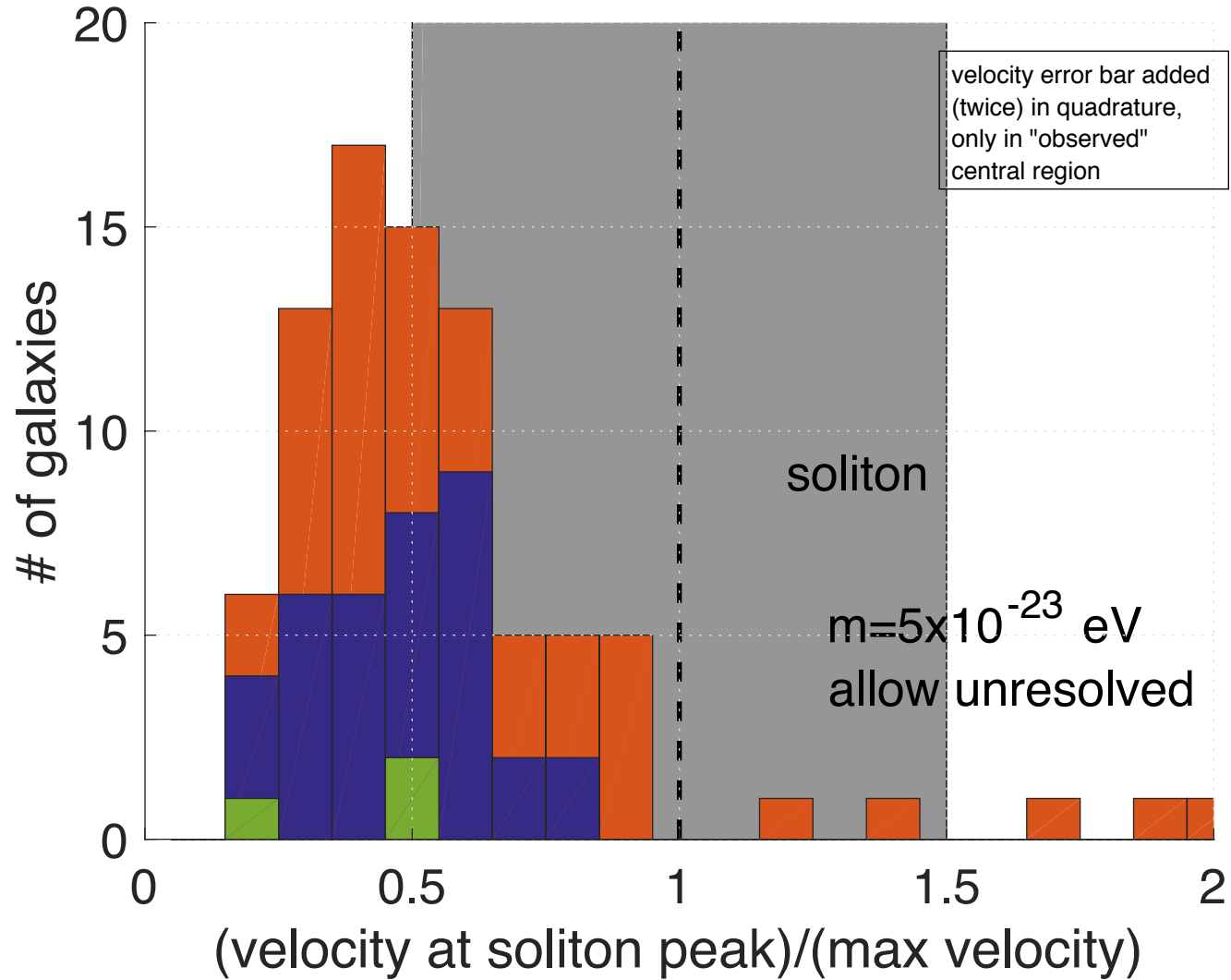
SPARC Lelli et al, 1606.09251

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$m = 5 \times 10^{-23} \text{ eV}$



Consider a halo with an NFW density profile

$$\rho_{NFW}(x) = \frac{\rho_c \delta_c}{\frac{x}{R_s} \left(1 + \frac{x}{R_s}\right)^2},$$

where

$$\rho_c(z) = \frac{3H^2(z)}{8\pi G}, \quad \delta_c = \frac{200}{3} \frac{c^3}{\ln(1+c) - \frac{c}{1+c}}.$$

$$\frac{E}{M} \Big|_{\text{halo}} \approx \frac{\tilde{c}}{4} \Phi_h,$$

$$\tilde{c} = \frac{c - \ln(1+c)}{(1+c) \ln(1+c) - c}$$

NFW halo gravitational potential:

$$\Phi_{NFW}(x) = -\frac{4\pi G \rho_c \delta_c R_s^3}{x} \ln \left(1 + \frac{x}{R_s}\right)$$

$$\Phi_{NFW}(x \ll R_s) \approx \Phi_h$$

soliton—host halo relation says:

$$\frac{E_\lambda}{M_\lambda} \approx \frac{\tilde{c}}{4} \Phi_h$$

$$\left. \frac{E}{M} \right|_{\text{halo}} \approx \frac{\tilde{c}}{4} \Phi_h,$$

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soliton—host halo relation says:

$$-0.23 \lambda^2 \approx \frac{E_\lambda}{M_\lambda} \approx \frac{\tilde{c}}{4} \Phi_h$$

Which fixes the soliton scale parameter.

$$\frac{E}{M} \Big|_{\text{halo}} \approx \frac{\tilde{c}}{4} \Phi_h,$$

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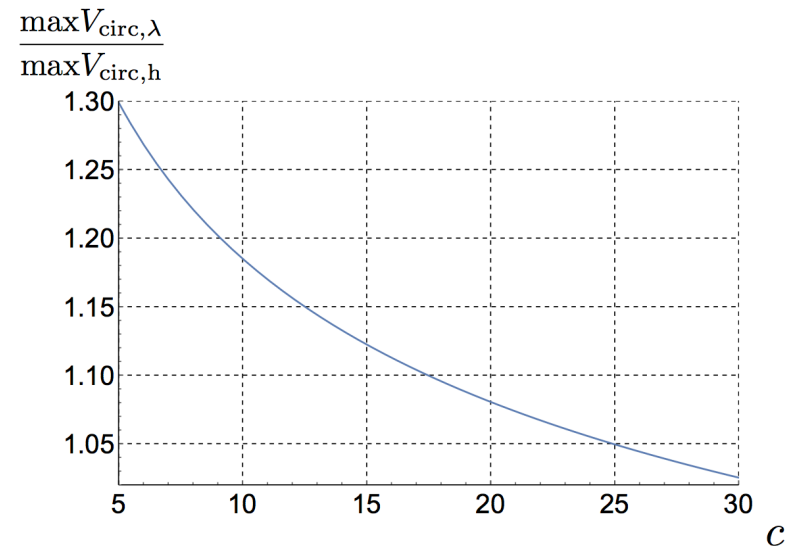
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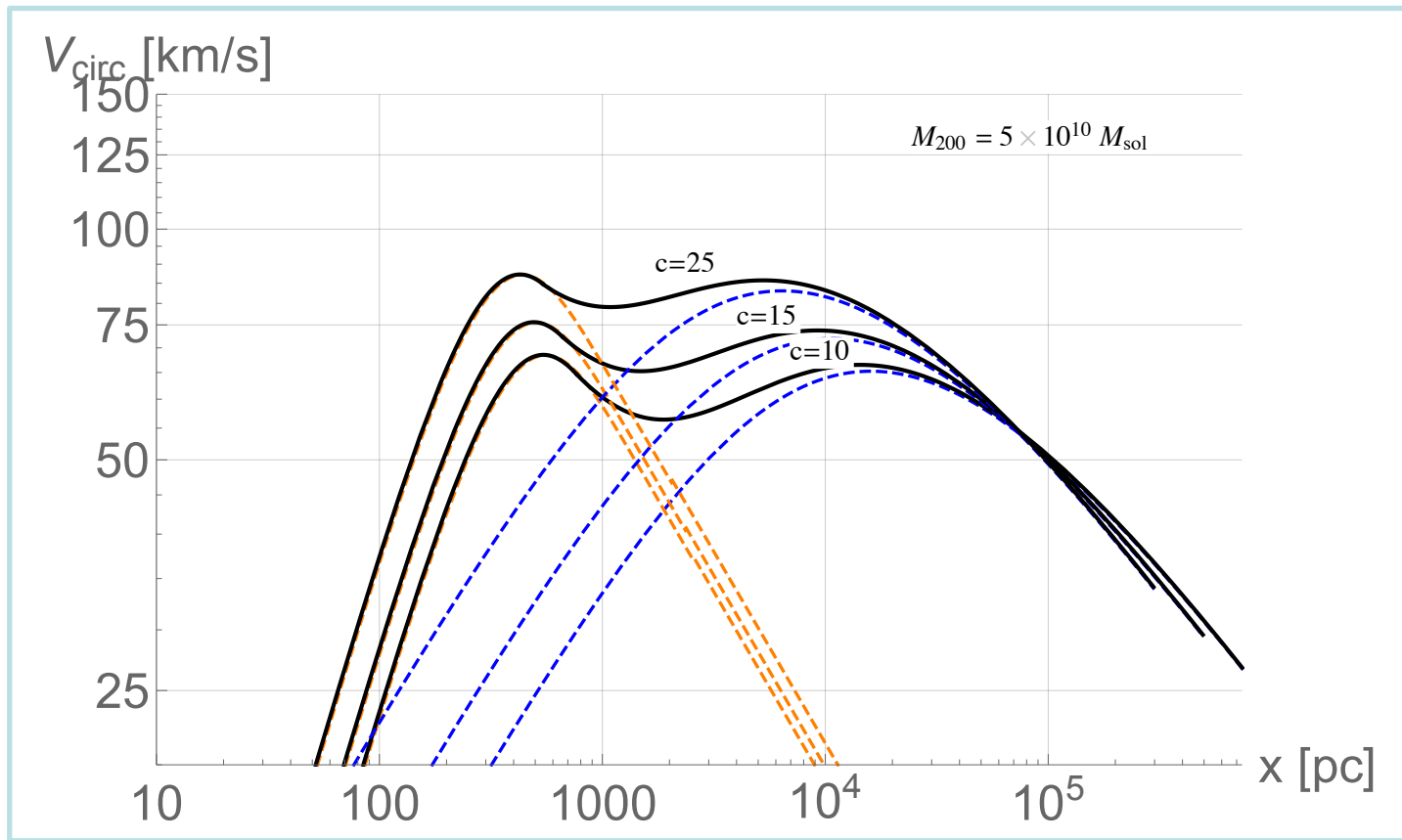
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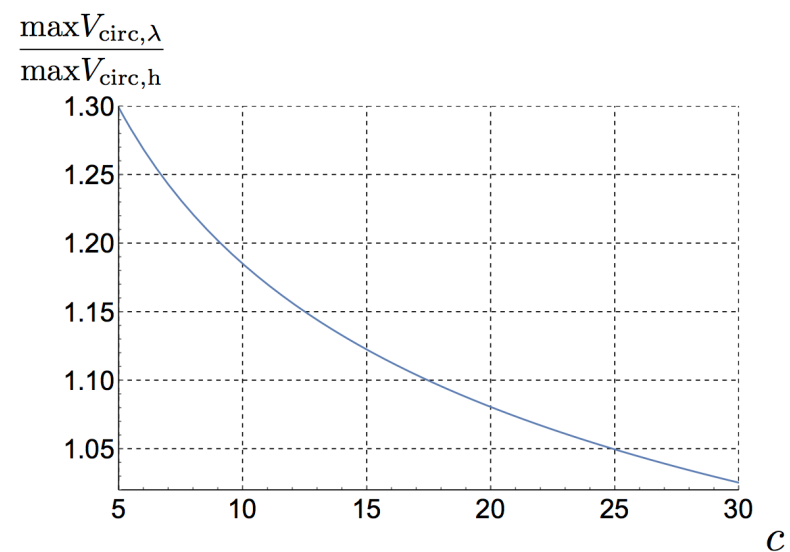
Equal specific energy ==> equal specific kinetic energy
 ==> ~equal peak rotation velocity

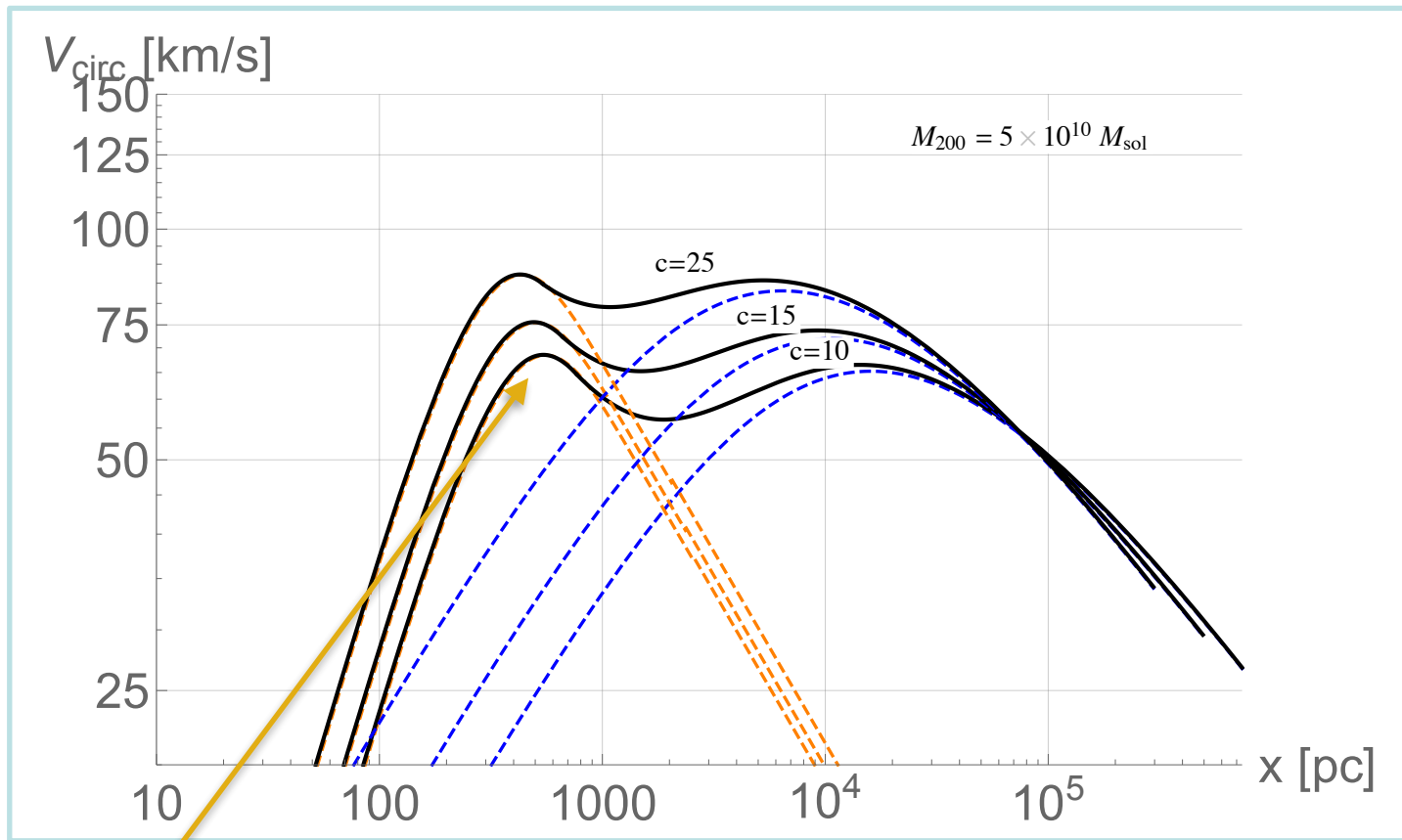
$$\frac{\max V_{\text{circ},\lambda}}{\max V_{\text{circ},h}} \approx 1.1 \left(\frac{\tilde{c}}{0.4} \right)^{\frac{1}{2}}$$



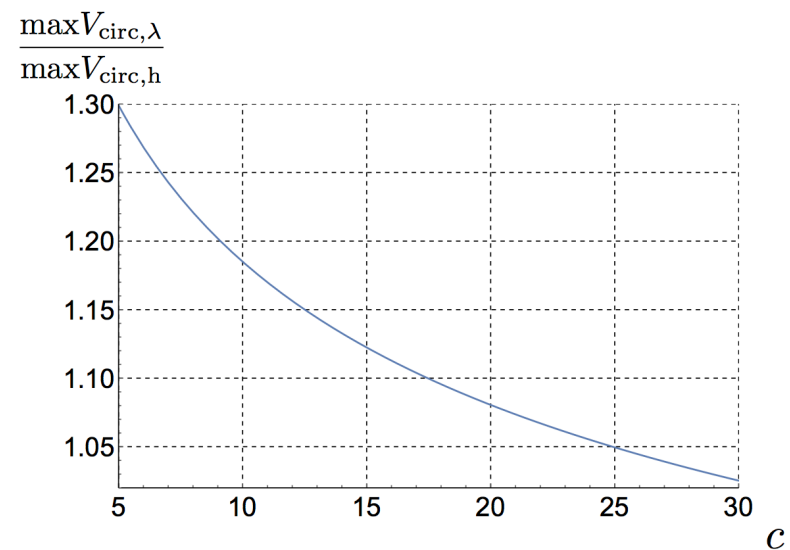


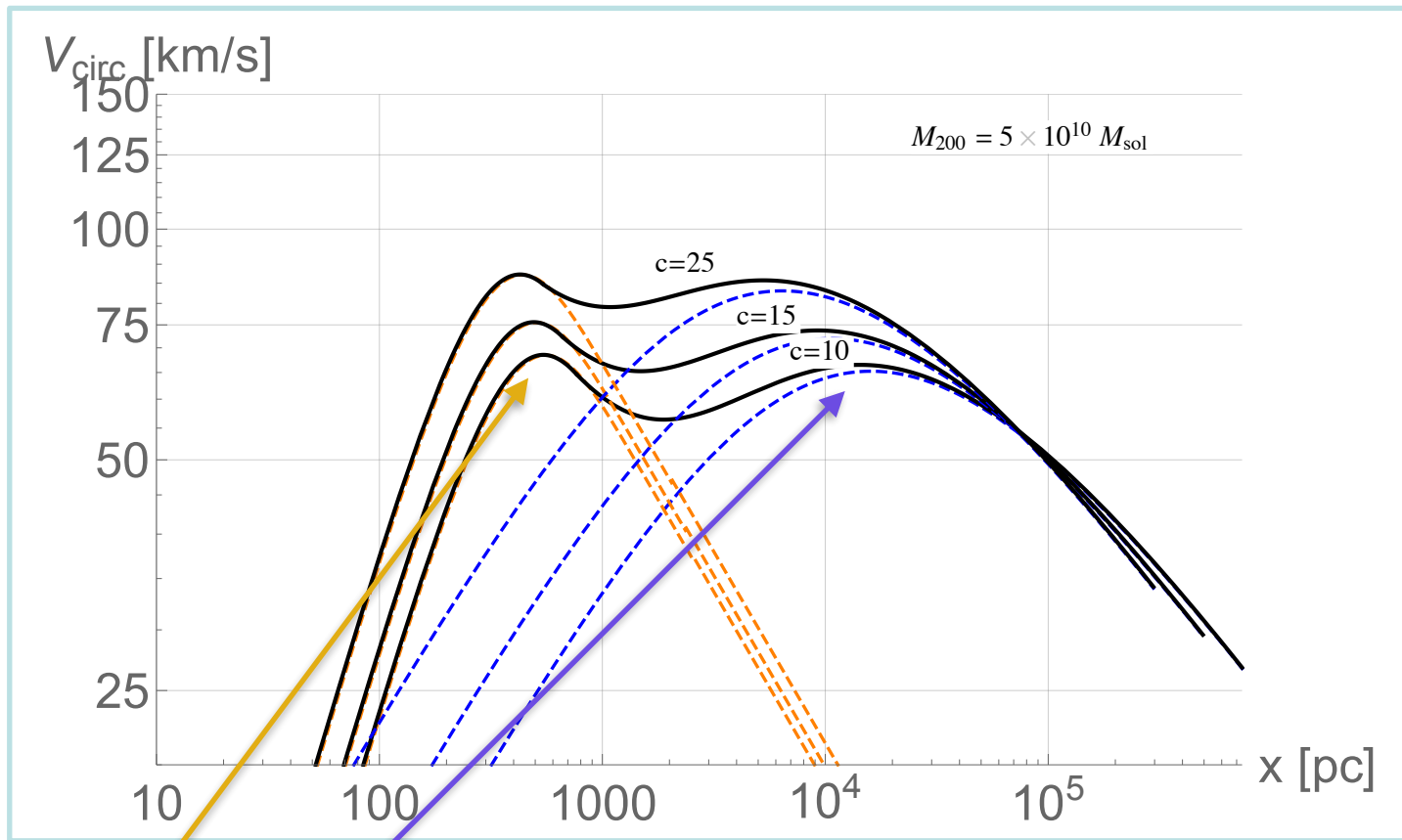
$$\frac{\max V_{\text{circ},\lambda}}{\max V_{\text{circ},h}} \approx 1.1 \left(\frac{\tilde{c}}{0.4} \right)^{\frac{1}{2}}$$



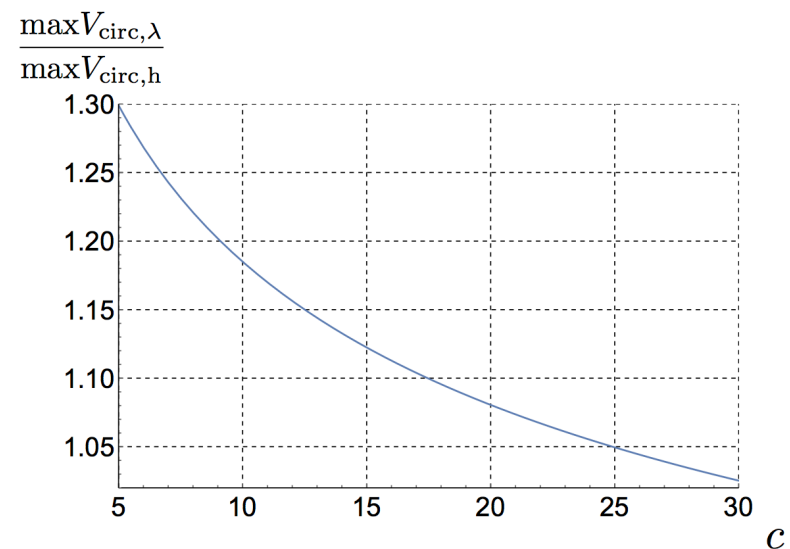


$$\frac{\max V_{\text{circ},\lambda}}{\max V_{\text{circ},h}} \approx 1.1 \left(\frac{\tilde{c}}{0.4} \right)^{\frac{1}{2}}$$





$$\frac{\max V_{\text{circ},\lambda}}{\max V_{\text{circ},h}} \approx 1.1 \left(\frac{\tilde{c}}{0.4} \right)^{\frac{1}{2}}$$



Evidence for DM is gravitational: a huge problem. Naturally, our efforts are diverging.

