

The heavy-ion programme at the LHC

“Taller d'Altes Energies” 2010

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CERN

Unsolved questions in particle physics

1. Mass generation problem : What is the origin of the SM elementary particle masses ? Higgs boson ? other mechanism ?
2. Hierarchy / fine-tuning problem: What stabilizes m_{Higgs} up to m_{Planck} (10^{16} orders-of-magnitude !?) ? SUSY ? extra-dimensions ? ...?
3. Dark matter problem : $\sim 1/4$ universe = invisible matter. SUSY ? ...?
4. Flavour problem : Origin of matter-antimatter asymmetry in the Universe ? Why so many types of matter particles ?
5. QCD in strongly-interacting regime : Why quark confinement ? high-energy hadronic x-sections ? Gauge-String duality (AdS/CFT) ?
6. Highest-energy cosmic-rays : Sources/nature of CRs at 10^{20} eV ?

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my topic today
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Solving the unsolved at the LHC: 7 experiments

1. Mass generation problem:

(Higgs boson)



2. Hierarchy, fine tuning:



3. Dark matter problem:

(SUSY, Beyond SM)

4. Flavour problem:

(CP-violation, B-physics)



5. non-perturbative QCD:

(QGP, total x-section, ...)



6. Highest-energy cosmic-rays:



Overview

■ Introduction:

- High-energy nucleus-nucleus collisions: Physics motivations
- Experiments: RHIC (Au-Au@200 GeV), LHC (Pb-Pb@5.5 TeV)

■ Probes of many-body quantum chromo (thermo)dynamics:

Observable (type)	Medium property	Theoretical tool
dN/dη multiplicity (soft)	gluonic struct. $xG(x, Q^2)$	Color-Glass-Condensate
dN/dp _T spectra (soft)	Equation-of-State $P(V, T)$	(Hydro), Lattice QCD
dN/dΔφ elliptic flow (soft)	shear viscosity η	(Hydro), AdS/CFT
Jet quenching (hard)	transport coefficient $\langle \hat{q} \rangle$	(Hydro), pQCD
γ enhancement (intermed.)	critical temperature T_{crit}	(Hydro), Lattice QCD
Q̄Q suppression (hard)	critical energy density ϵ_{crit}	(Hydro), Lattice QCD

■ Summary

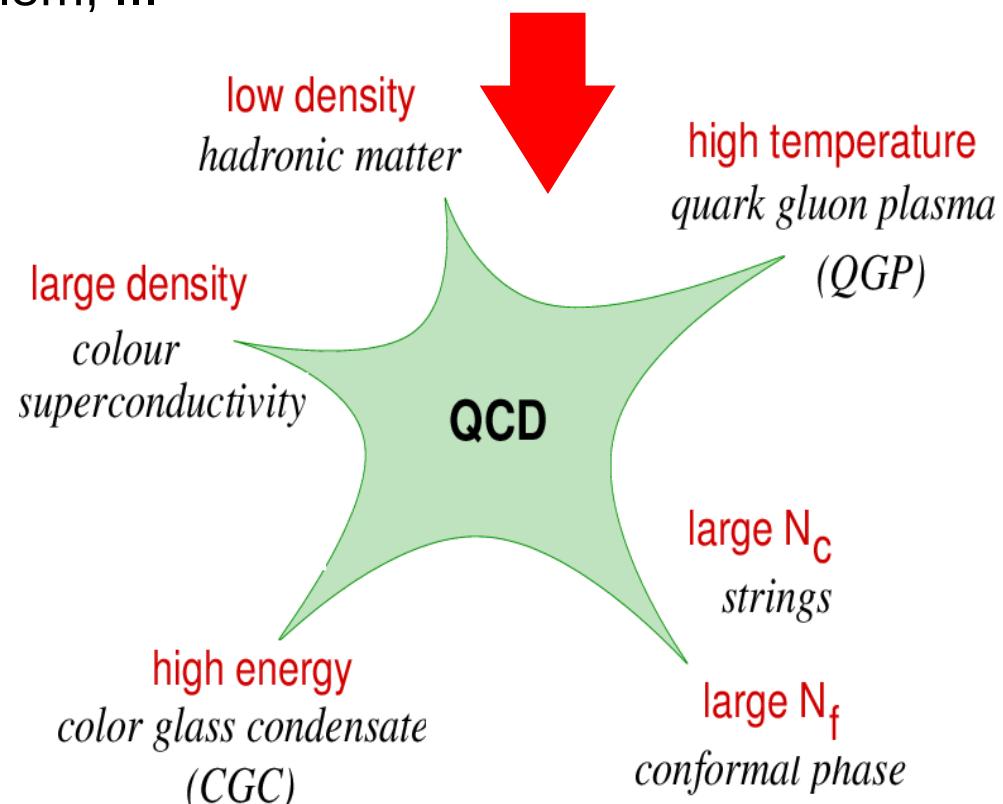
Many-body dynamics of quarks & gluons

- QCD = Quantum-field theory with **very rich dynamical** content: asymptotic freedom, confinement, (approx.) χ -symmetry, non-trivial vacuum, $U_A(1)$ anomaly, CP-problem, ...

$$\mathcal{L} = \frac{1}{4g^2} G_{\mu\nu}^\alpha G_{\mu\nu}^\alpha + \sum_i \bar{q}_i (\not{D}_\mu + m_i) q_i$$

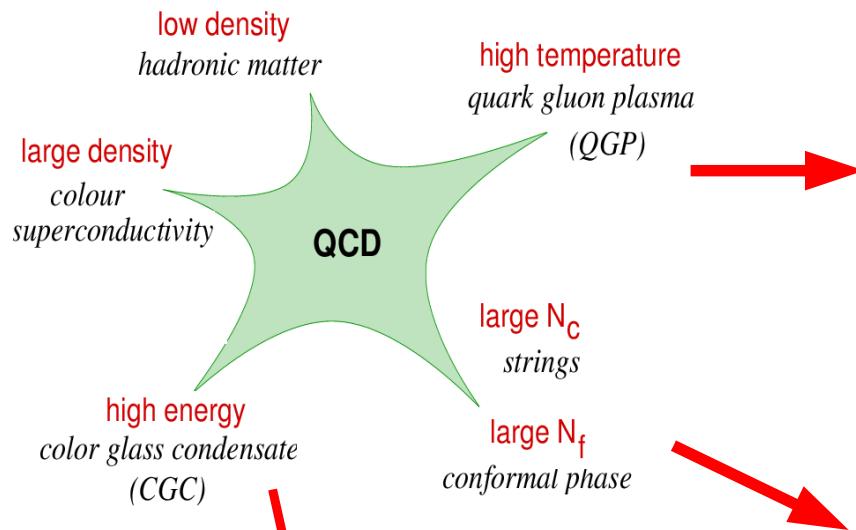
where $G_{\mu\nu}^\alpha = \partial_\mu A_\nu^\alpha - \partial_\nu A_\mu^\alpha + \epsilon_{abc} F_{\mu\nu}^b A_\nu^c$
and $\not{D}_\mu = \partial_\mu + i t^a A_\mu^a$

$$g^2(Q^2) \sim 4\pi / [\beta_0 \log(Q^2/\Lambda^2)], \quad \Lambda \sim 0.2 \text{ GeV}$$

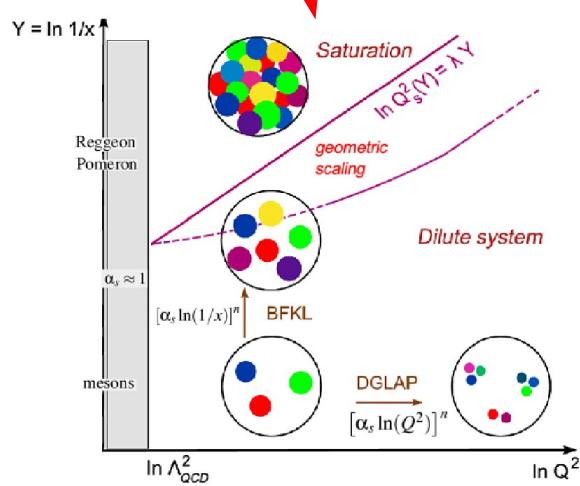


- QCD = the only sector of SM whose **collective behaviour** can be studied in the lab: **phase transition(s)**, **thermalization** of fundamental fields, ...
- QCD = very diverse **many-body phenomenology** at various limits:

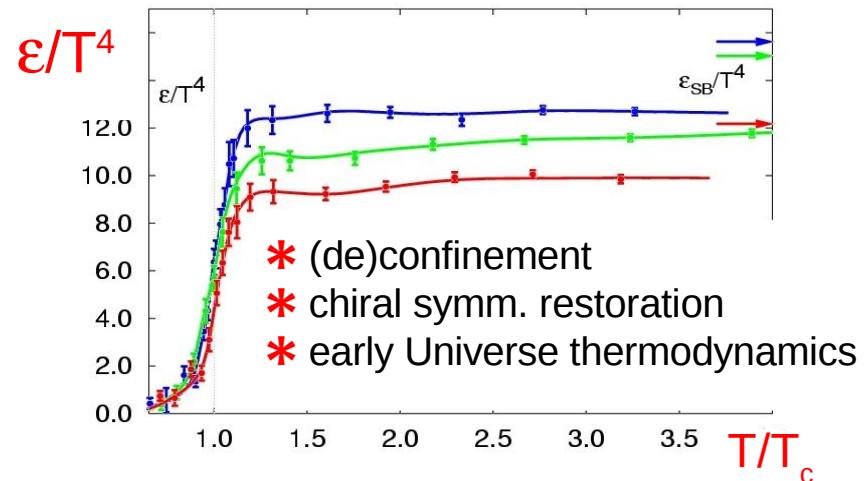
QCD matter: physics menu



■ High-density QCD at small-x: CGC



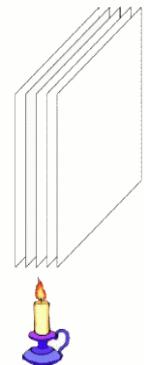
■ Lattice QCD at high-T: QGP



■ Gauge-gravity duality: AdS/CFT

$$\mathcal{L} = \frac{1}{2g_{YM}^2} \text{Tr}(F_{\mu\nu}F^{\mu\nu}) + i \text{Tr}(\bar{\psi}\gamma^\mu D_\mu \psi) \quad \leftrightarrow \quad ds^2 = \frac{r^2}{R^2}(-dt^2 + dx^2) + \frac{R^2}{r^2}d\Omega_5^2$$

$\mathcal{N}=4$ SYM
plasma in 4-D



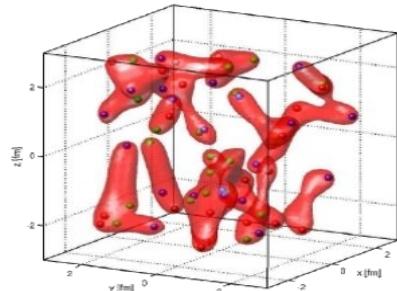
Black-hole
in 5-D

* QGP transport coeffs: viscosity, diffusivity, ...

Topic I: Study of (bulk) deconfinement ...

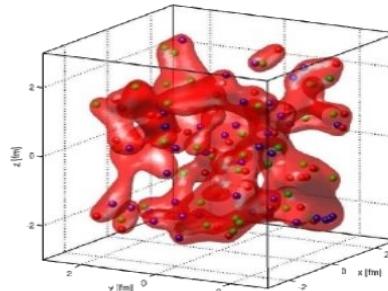
- Increase of parton # density (n) \Rightarrow bulk deconfined state:

$$n = 0.5 \text{ fm}^{-3}$$



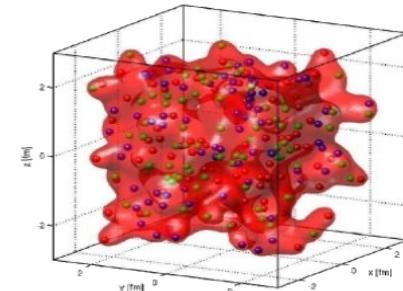
Color-neutral clusters

$$n = 1.0 \text{ fm}^{-3}$$



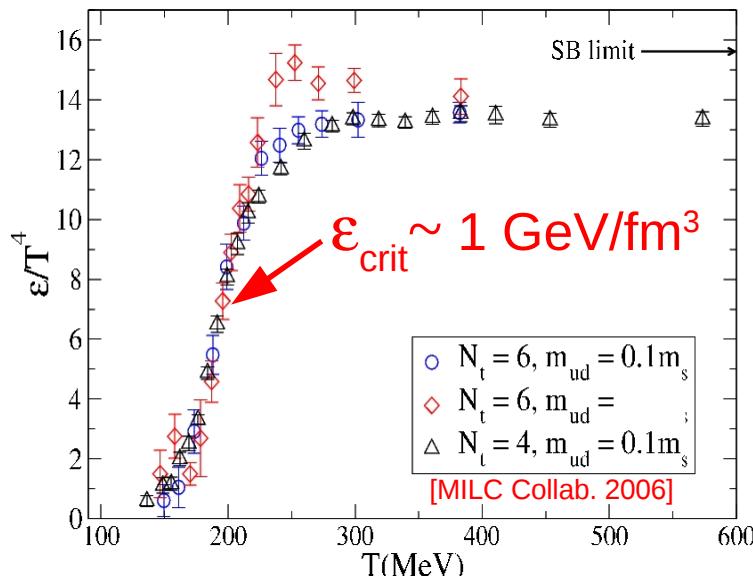
Increasing overlap with n

$$n = 2.0 \text{ fm}^{-3}$$



Color-connected system at n_{crit}

- Energy density vs. temperature (lattice QCD Equation-of-State):

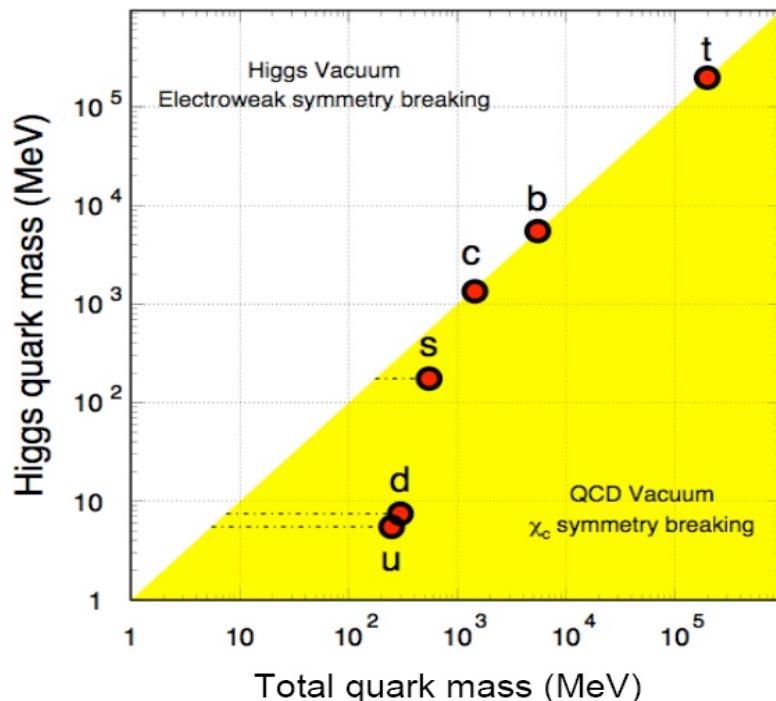


Deconfinement transition:

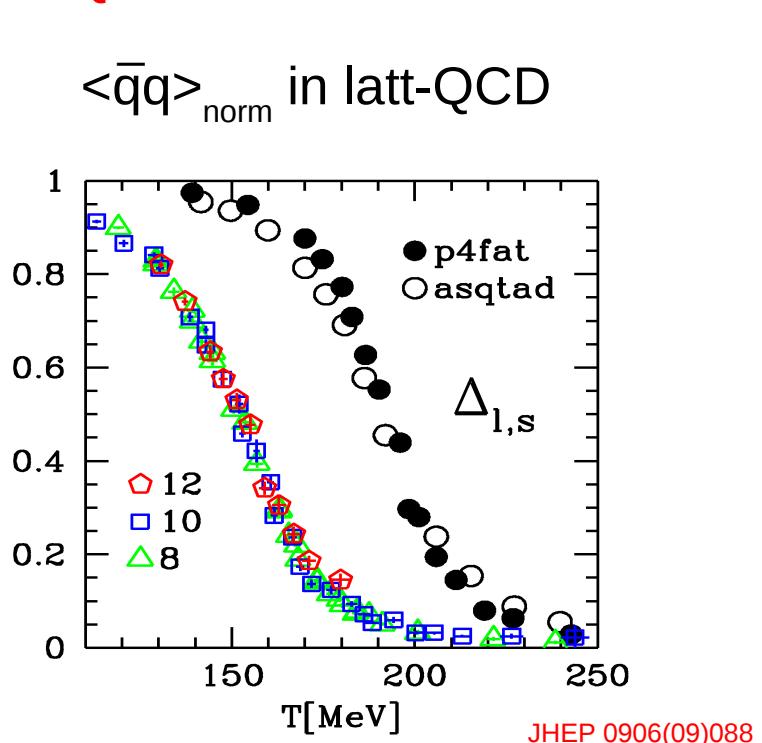
- Sharp rise of ϵ at $T_{\text{crit}} \sim 0.2 \text{ GeV}$
- Sudden increase of degrees of freedom:
 $\epsilon \propto g_{\text{eff}} T^4$
 $g_{\text{eff}} (\text{hadrons}) = 3$ (pions)
 $g_{\text{eff}} (\text{QGP}) \sim 47$ (gluons, quarks)
 $= 2(\text{spin}) * 8(\text{color}) + (7/8) * [2 * 3(\text{flavour}) * 3(\text{color}) * 2(\text{spin})]$

Topic I: ... and origin of (visible) mass

- QCD (= χ -symm breaking) not (!) Higgs (= EWK-symm breaking) is truly responsible for the “origin of (baryon) mass” (~4% of all mass in Univ.):
- Quark masses at T=0:
- Quark masses at T \neq 0:



~98% of the u,d masses generated dynamically (gluons) in the QCD confining potential



Chiral transition: light-q recover bare mass at T_{crit} ~0.15-0.2 GeV

Topic 2: Gluon saturation

- Gluons dominate **low-x** hadronic wave-function:

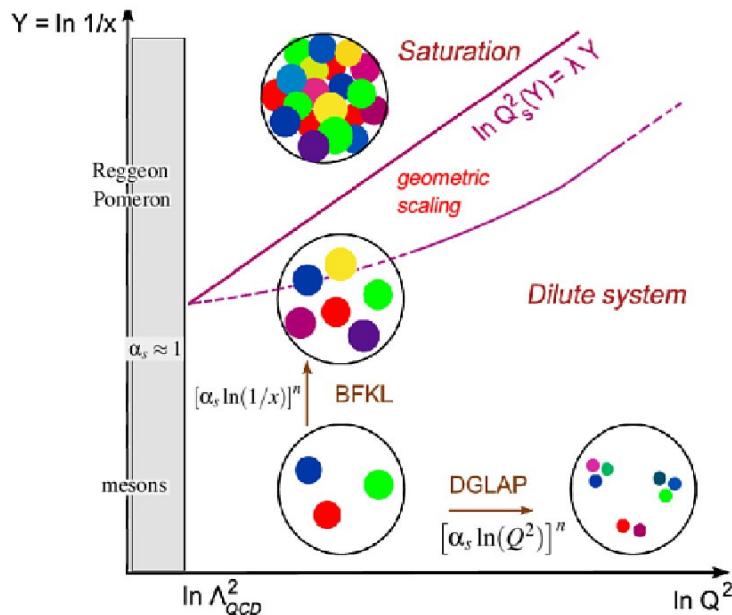
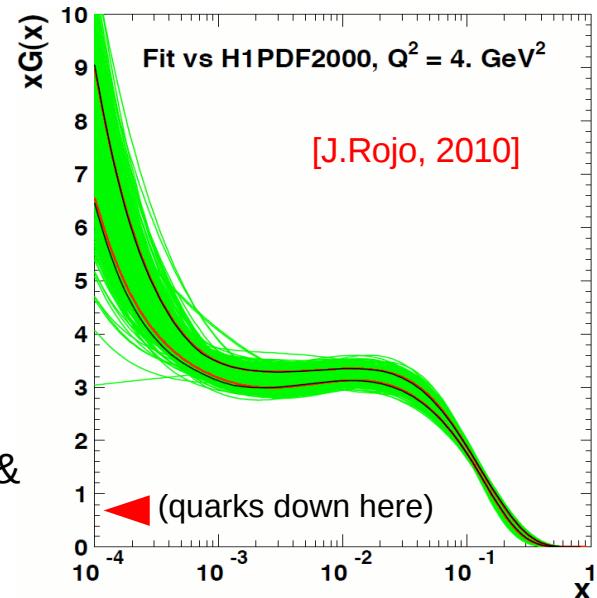
- Radiation controlled by QCD evolution eqs.:

Q^2 - DGLAP: $F_2(Q^2) \sim \alpha_s \ln(Q^2/Q_0^2)^n$, $Q_0^2 \sim 1 \text{ GeV}^2$

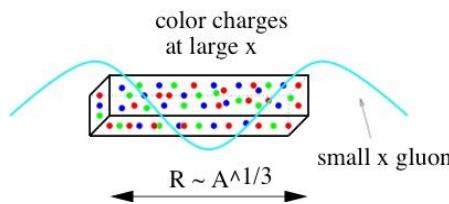
x - BFKL: $F_2(x) \sim \alpha_s \ln(1/x)^n$

Linear eqs. (single parton radiation/splitting) **cannot work**

at very low-x: Unitarity violated (even for $Q^2 \gg \Lambda^2$), collinear & k_T factorization breakdown.



- Gluons overlap below “saturation scale” $Q_s(x)$
- Color Glass Condensate = EFT describes hadrons as **classical fields** below Q_s
- Saturation effects **enhanced in nuclei**:



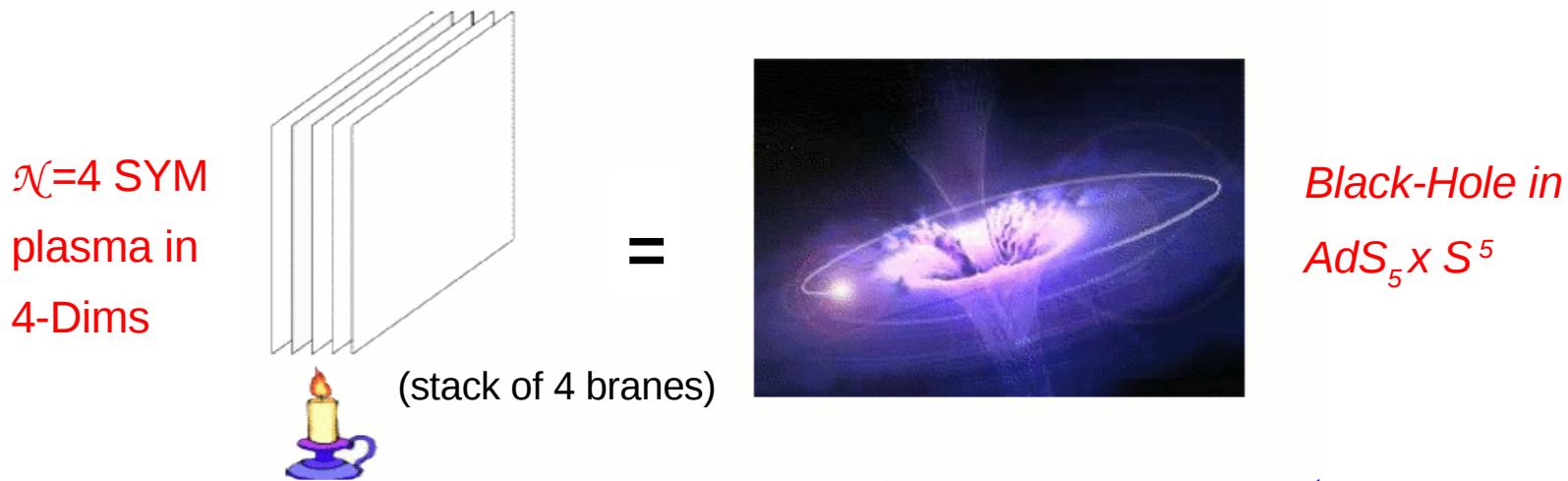
Large # of partons per transverse area

$$Q_s^2 \sim A^{1/3} \sim 6$$

Topic 3: AdS/CFT correspondence

- Strongly-coupled 4-D theories (QCD-like) can be studied analytically from eqs-of-motion/thermodynamics in simpler 5-D gravity duals.

$$\mathcal{L} = \frac{1}{2g_{\text{YM}}^2} \text{Tr}(F_{\mu\nu}F^{\mu\nu}) + i\text{Tr}(\bar{\psi}\gamma^\mu D_\mu\psi) \quad \longleftrightarrow \quad ds^2 = \frac{r^2}{R^2}(-dt^2 + d\vec{x}^2) + \frac{R^2}{r^2}d\Omega_5^2$$



Duality between couplings: $g_{\text{SYM}}^2 = 4\pi g_{\text{st}}$ $g_{\text{SYM}}^2 N_c = \left(\frac{R}{l_{\text{st}}}\right)^4$

- Guess the holography “dictionary” that relates both sides of duality for a given observable, e.g. BH Hawking T \Leftrightarrow QGP T ($T_H = r_0/4\pi R^2$)
- Large differences between QCD & SYM (extra SUSY degrees of freedom, no running-coupling, no confinement) “wash out” at finite-T.

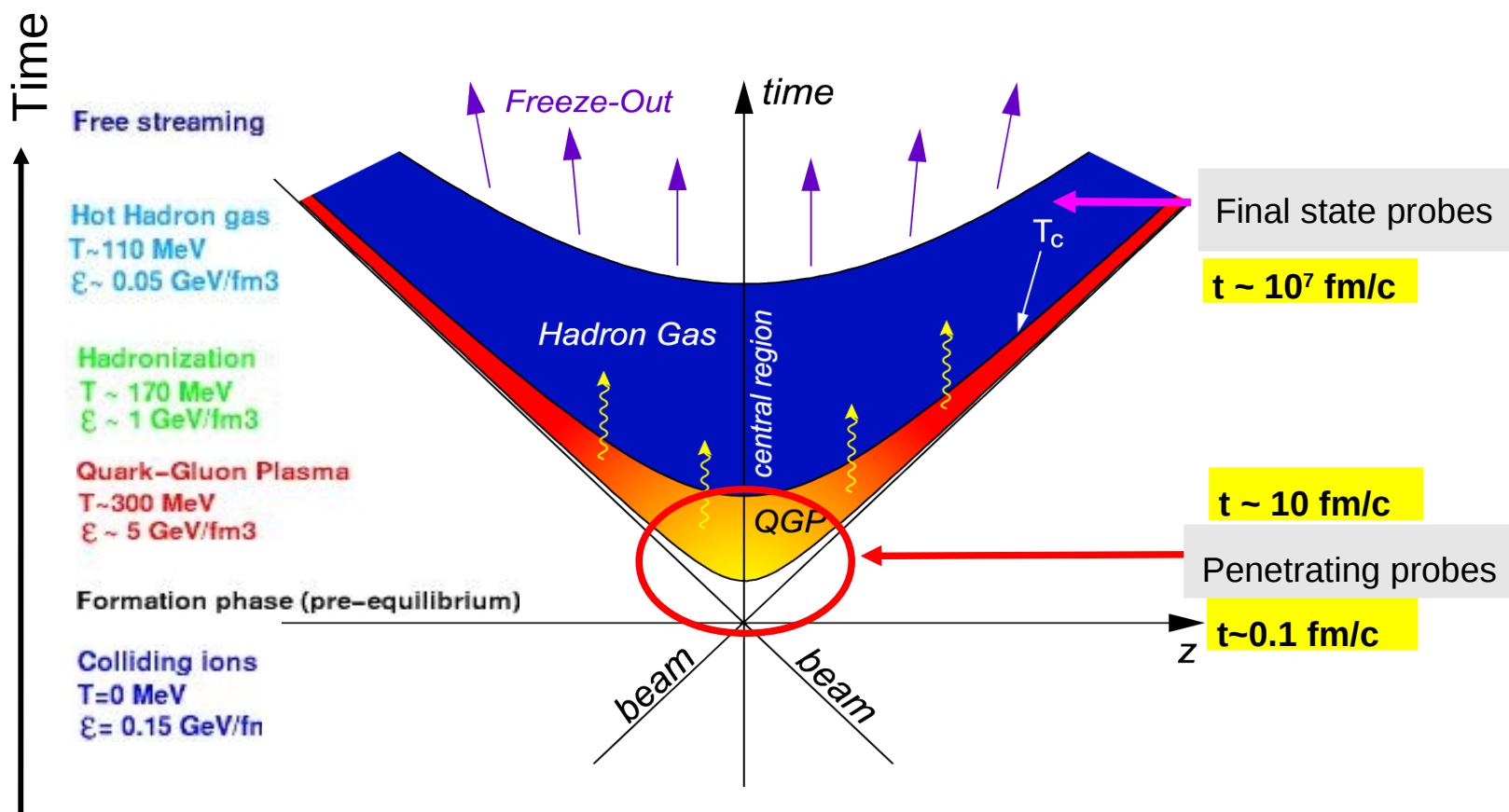
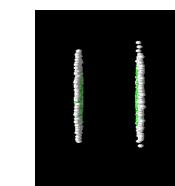
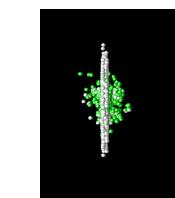
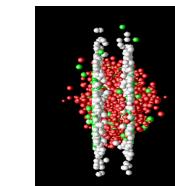
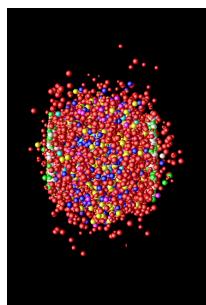
QCD matter studies via heavy-ion collisions

The "Little Bang" in the lab.

High-energy **nucleus-nucleus collisions**: fixed-target ($\sqrt{s}=20$ GeV, SPS) or colliders ($\sqrt{s}=200$ GeV, RHIC; $\sqrt{s}=5.5$ TeV, LHC)

Expanding QGP: volume $\sim O(10^3 \text{ fm}^3)$ for times $\sim 0.1\text{-}10 \text{ fm}/c$

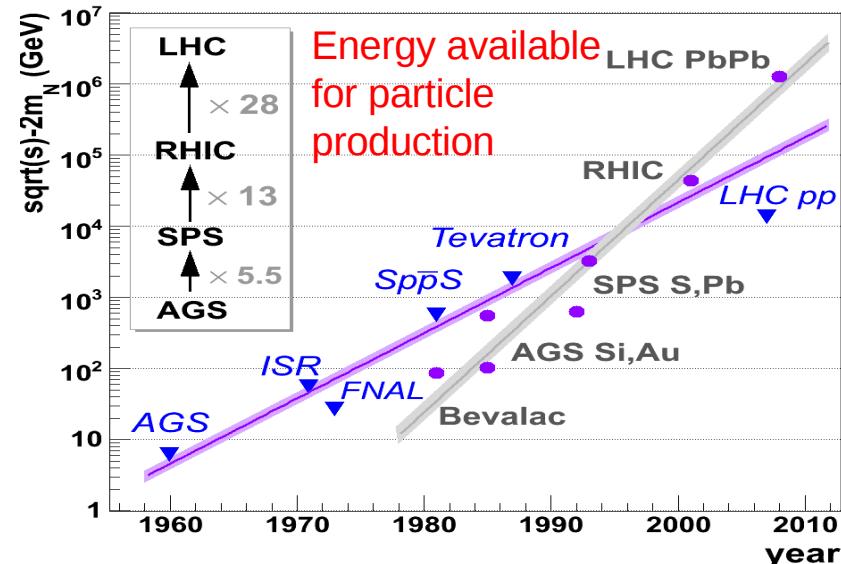
Collision dynamics: Diff. observables sensitive to diff. reaction stages



Energy densities in A-A collisions

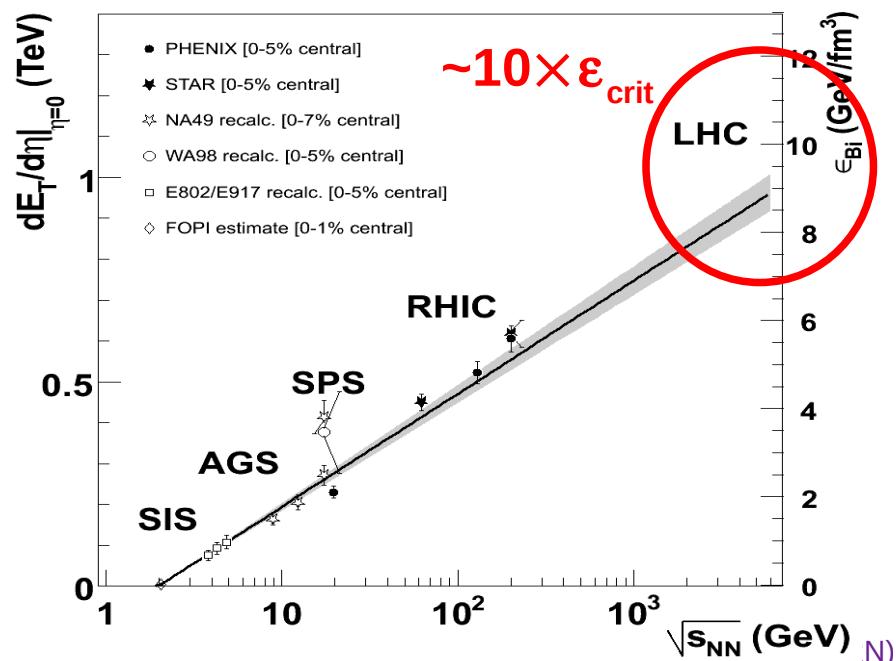
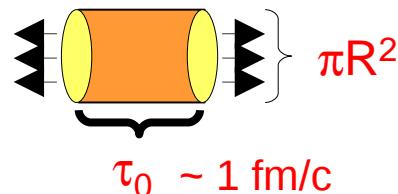
■ T.D. Lee [Rev. Mod. Phys. 47 (1975) 267]:

"In HEP we've concentrated on experiments in which we distribute a higher & higher amount of energy into a region with smaller & smaller dimensions. In order to study the question of 'vacuum' (...) we should investigate 'bulk' phenomena by distributing high energy over a relatively large volume."



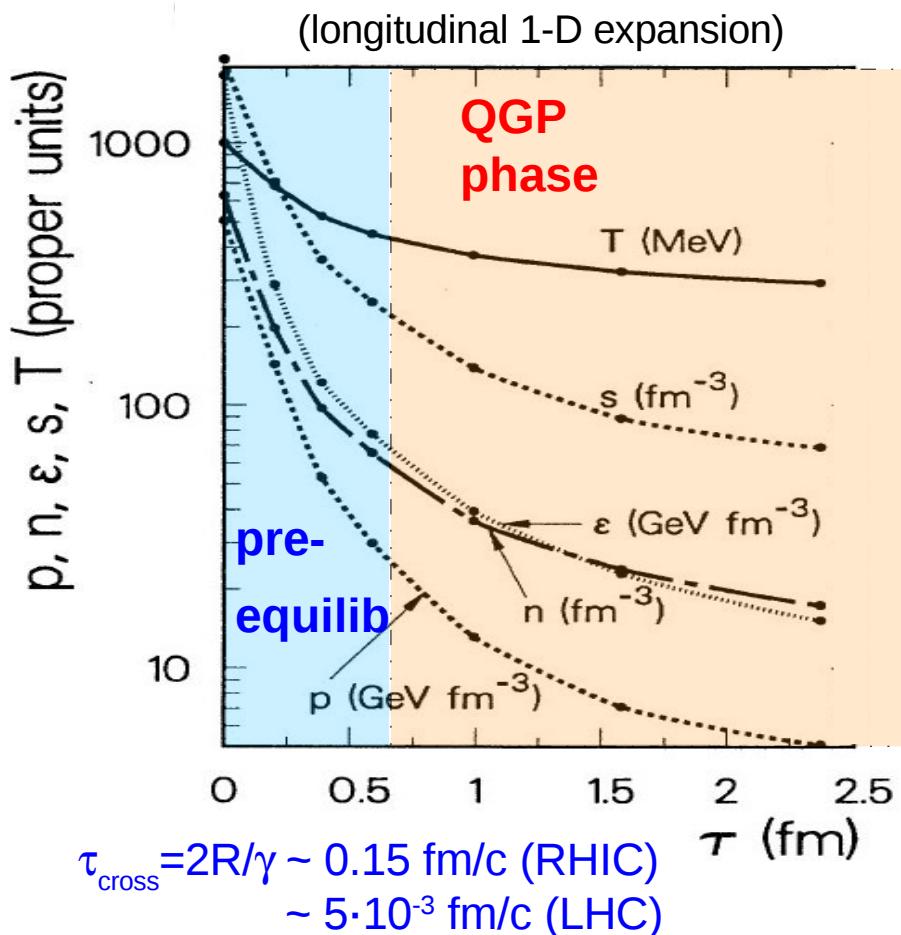
■ Energy density “Bjorken estimate”
(longitudinally expanding plasma):

$$\epsilon_{Bj} = \frac{dE_T}{dy} \frac{1}{\tau_0 \pi R^2}$$



QCD fluid-dynamics

- After collision, medium **expands** ($\beta_L \approx 1$, $\beta_T > 0.5$) & cools within $\tau \sim 15$ fm/c.
- Power-law evolution of thermo-dynamical properties: $T \sim 1/\tau^{1/3}$, $\varepsilon \sim 1/\tau^{4/3}, \dots$



- Relativistic fluid-dynamics needed to extract initial QGP properties:
Local conservation of **energy-momentum tensor** & other currents:

$$\partial_\mu T^{\mu\nu} = 0$$

$$\partial_\mu N_i^\mu = 0, \quad i = B, S, \dots$$

Ideal (non-viscous) **fluid** tensor & charges:

$$T^{\mu\nu} = (\epsilon + P)u^\mu u^\nu - Pg^{\mu\nu}$$

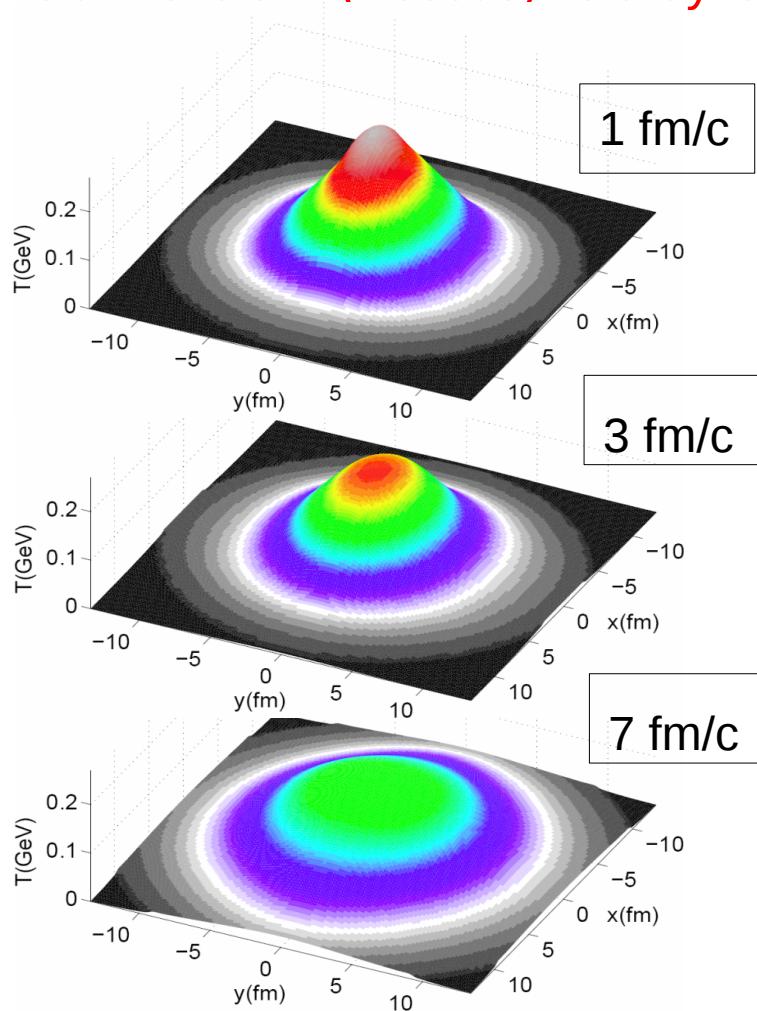
$$N^\mu = n u^\mu \quad (\text{u}^\mu: \text{fluid velocity})$$

Equation-of-State (parton relativ. gas):

$$\varepsilon = 3 \cdot P \propto g_{\text{eff}} \cdot T^4 \quad (\text{Stefan-Boltzmann})$$

3-D viscous QCD fluid-dynamics

- After collision, medium **expands** ($\beta_L \approx 1$, $\beta_T > 0.5$) & cools within $\tau \sim 15$ fm/c.
- Relativistic 3-D (viscous) fluid-dynamics needed to extract initial QGP properties



Local conservation of **energy-momentum tensor** & other currents:

$$\begin{aligned}\partial_\mu T^{\mu\nu} &= 0 \\ \partial_\mu N_i^\mu &= 0, \quad i = B, S, \dots\end{aligned}$$

Viscous fluid tensor & charges:

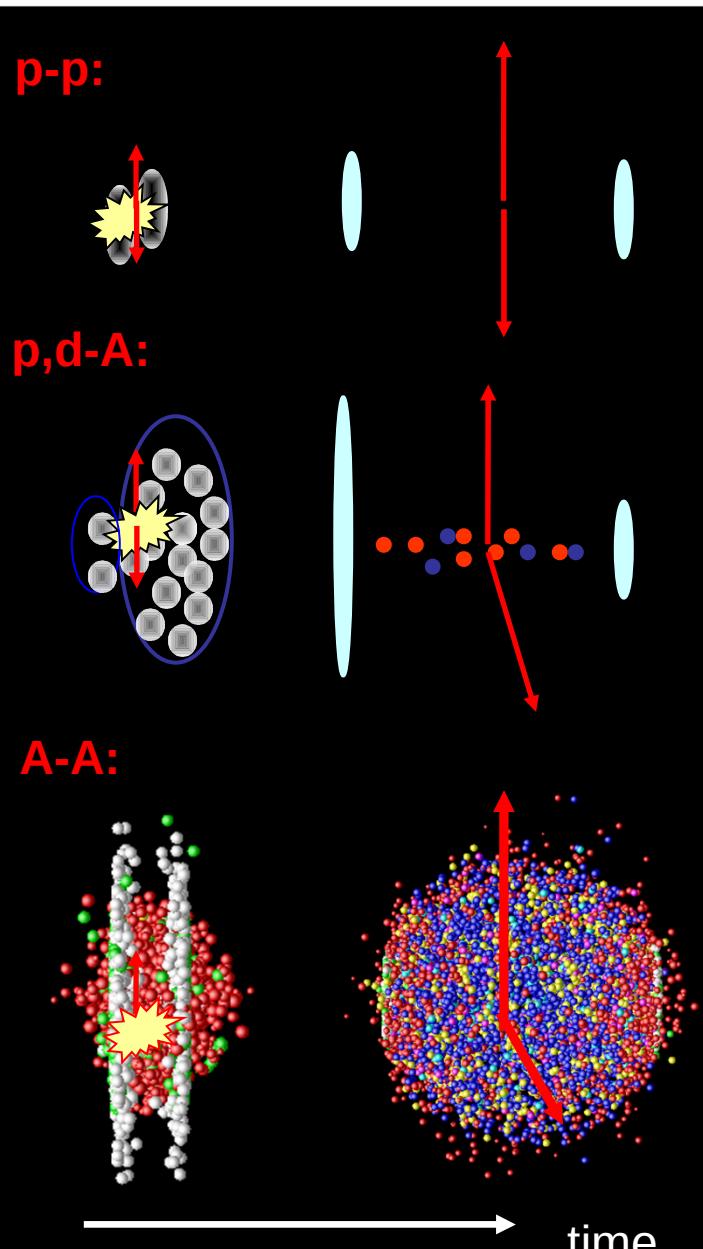
$$\begin{aligned}T^{\mu\nu} &= (\epsilon + p)u^\mu u^\nu - pg^{\mu\nu} + \Pi^{\mu\nu} \\ N^\mu &= n u^\mu \quad (\Pi^{\mu\nu}: \text{shear-stress})\end{aligned}$$

Equation-of-State (parton relativ. gas):

$$\varepsilon = 3 \cdot P \propto g_{\text{eff}} \cdot T^4 \quad (\text{Stefan-Boltzmann})$$

Heavy-Ion Experiments

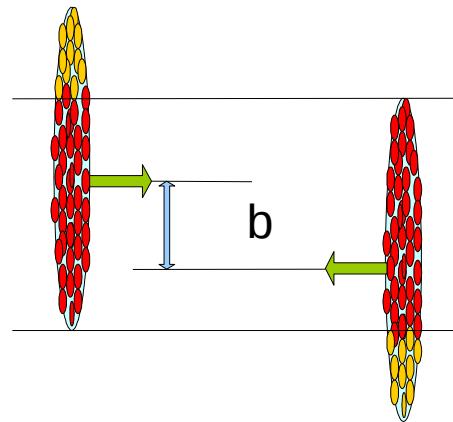
proton-proton & proton-nucleus baselines



p-p = “QCD vacuum” (reference)

p,d-A = “cold QCD medium” (control)

A-A = “hot & dense QCD matter”



Plasma volume
dialed varying
impact parameter b
 (“centrality”)

Relativistic Heavy-Ion Collider (RHIC) @ BNL

- Specifications:

3.83 km circumference

2 independent rings:

- 120 bunches/ring
- 106 ns crossing time

A-A collisions @ $(\sqrt{s}_{NN})_{max} = 200 \text{ GeV}$

Lumi: $\sim 10^{27} \text{ cm}^{-2} \text{ s}^{-1}$ ($\sim 6 \text{ kHz}, \sim 6 \text{ mo./year}$)

p-p @ $\sqrt{s}_{max} = 500 \text{ GeV}$

p,d-A @ $\sqrt{s}_{max} = 200 \text{ GeV}$

- 4 experiments:

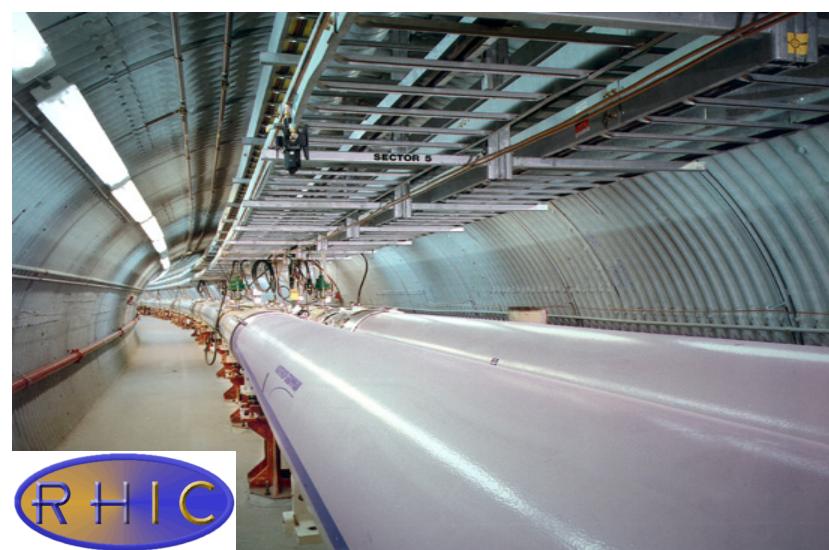
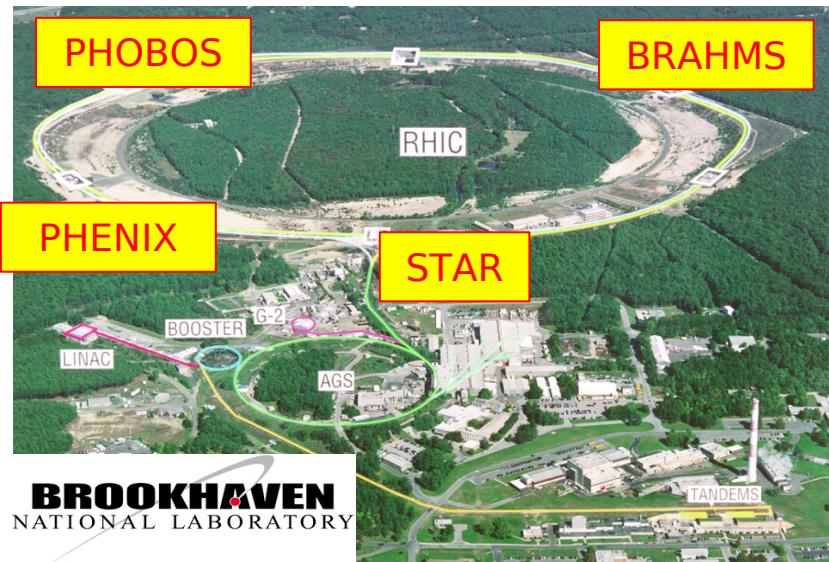
PHENIX, STAR (BRAHMS, PHOBOS)

- Runs 1 - 7 (2000 – 2010):

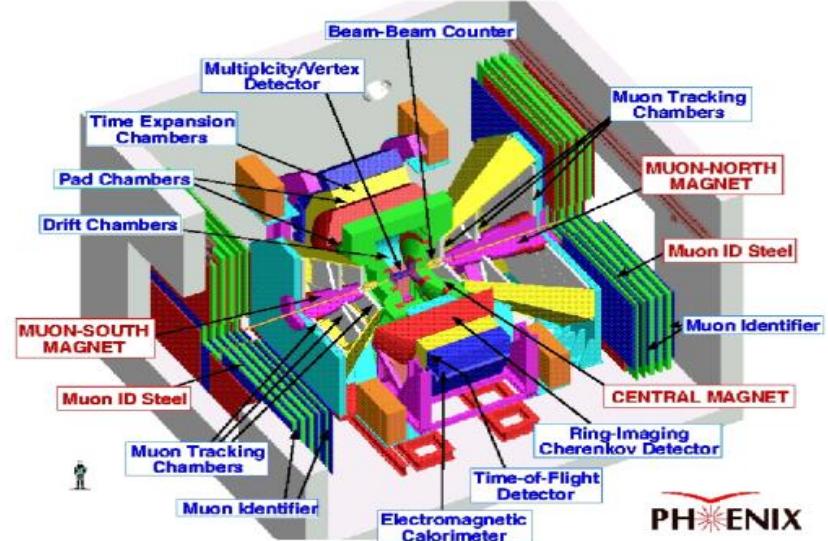
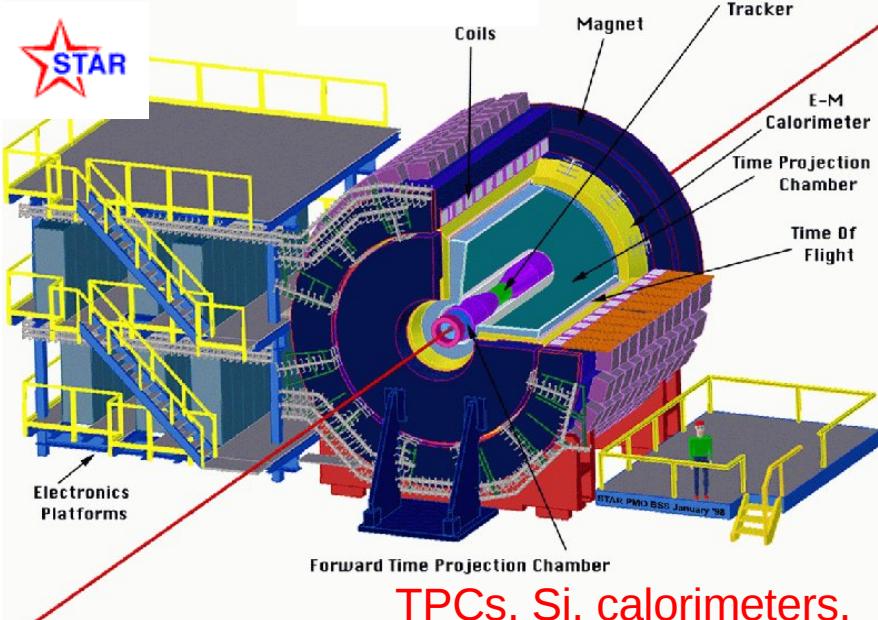
Au-Au,Cu-Cu @ $\sqrt{s}_{NN} = 4 – 200 \text{ GeV}$

d-Au @ $\sqrt{s}_{NN} = 200 \text{ GeV}$

p-p, p \uparrow -p \uparrow @ $\sqrt{s} = 22 – 500 \text{ GeV}$



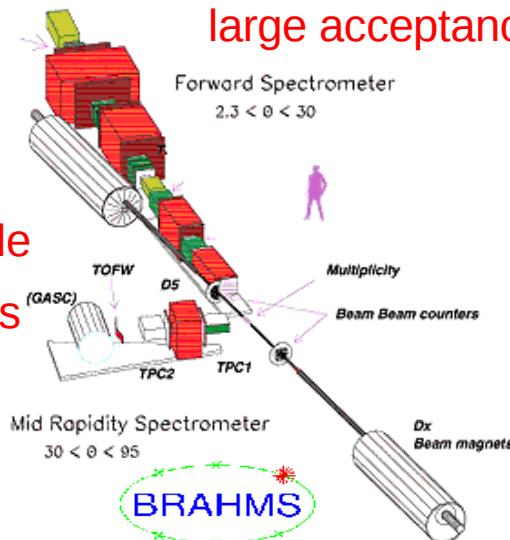
RHIC experiments



Hadrons, e, μ , γ . High-rate DAQ.
Rare & penetrating probes

Heinz Pernegger for


2 magn. dipole spectrometers in “fix-target” config.

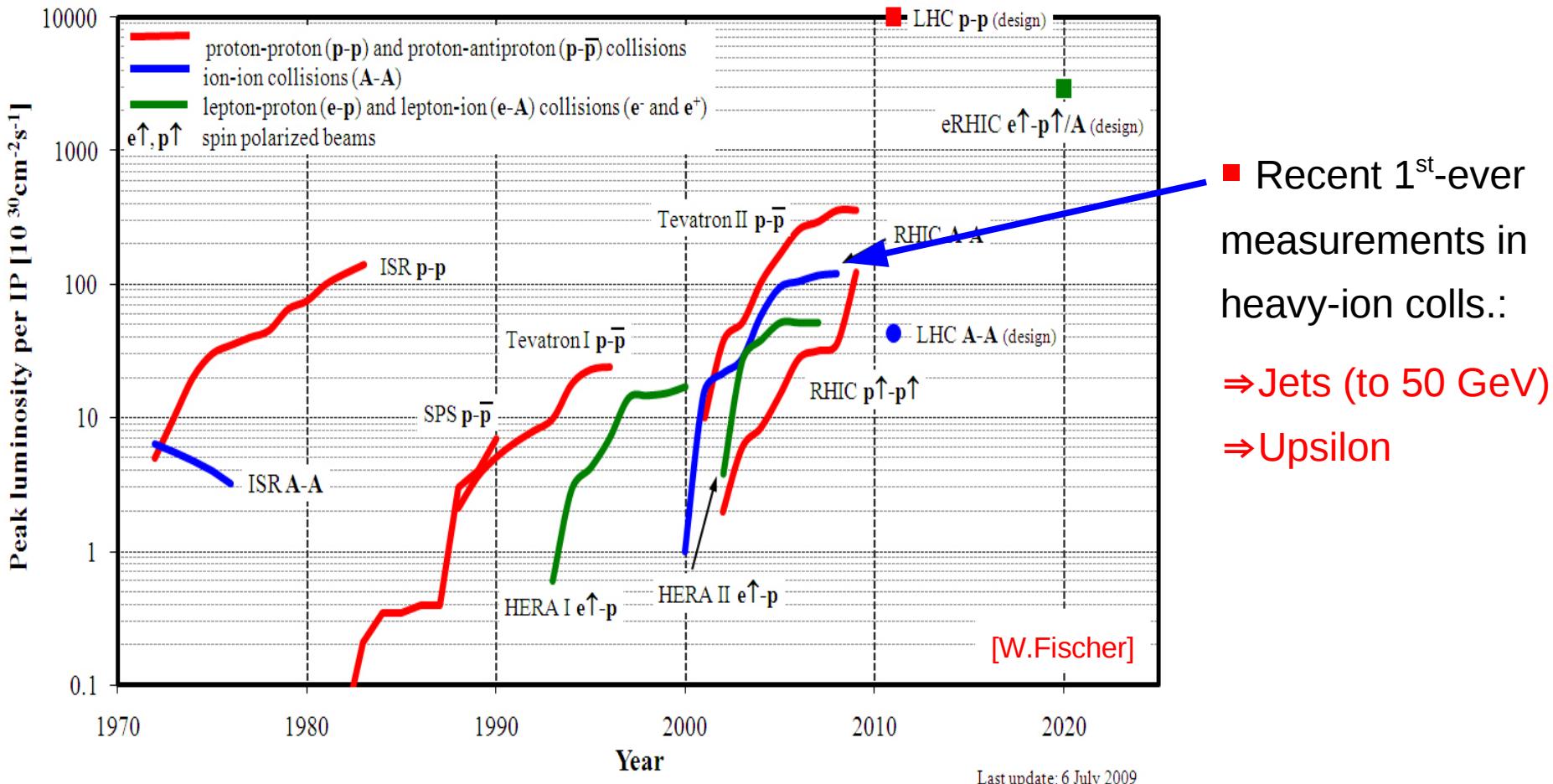


Si-strip tracking
PMT-based TOF

David d'Enterria (CERN)

RHIC luminosities

- Peak luminosities: $\mathcal{L}_{\text{equiv-pp}} = A^2 \times \mathcal{L}_{\text{AA}} \sim 200^2 \times 10^{27} \text{ cm}^{-2}\text{s}^{-1} \sim 10^{32} \text{ cm}^{-2}\text{s}^{-1}$
- Max. integrated luminosities: $\int \mathcal{L} dt \sim 400 \text{ pb}^{-1}$ (A-A), 150 pb^{-1} ($p\uparrow-p\uparrow$)



Large Hadron Collider (LHC) @ CERN

- Specifications:

- 1 ring: **26.7 km** circumference

- 8.33 T superconducting coils

- 25 ns crossing time

- Pb-Pb @ $\sqrt{s_{NN}} = 5.5 \text{ TeV}$

- Lumi: $10^{27} \text{ cm}^{-2} \text{ s}^{-1}$ ($\sim 7 \text{ kHz}$, 1mo./year)

- p-p collisions @ $\sqrt{s_{NN}} = 14 \text{ TeV}$

- Lumi: $10^{34} \text{ cm}^{-2} \text{ s}^{-1}$ ($\sim 600 \text{ MHz}$, 8 mo./year)

- p,d-Pb @ $\sqrt{s_{NN}} = 8.8 \text{ TeV}$

- 3 experiments:

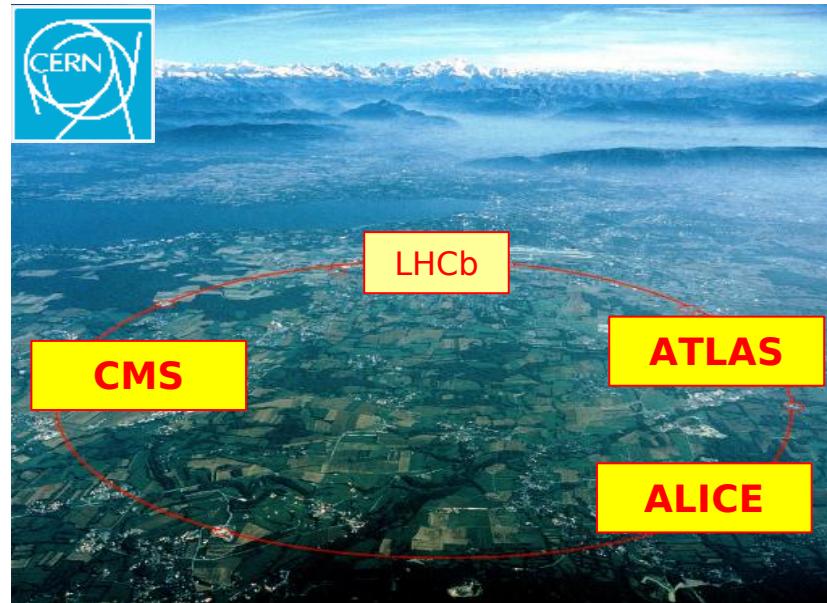
- ALICE, ATLAS, CMS**

- Run planning:

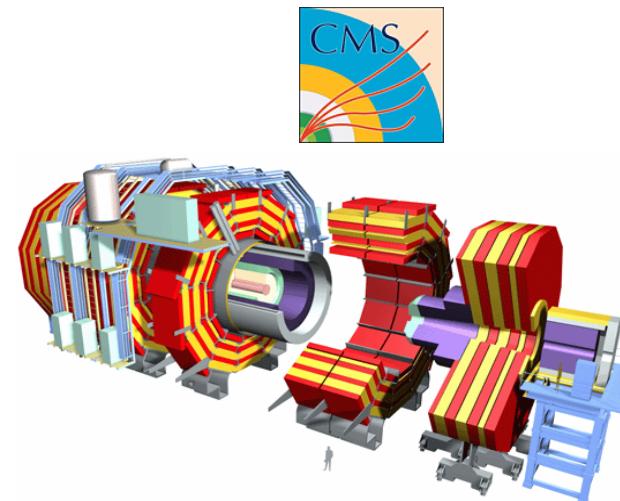
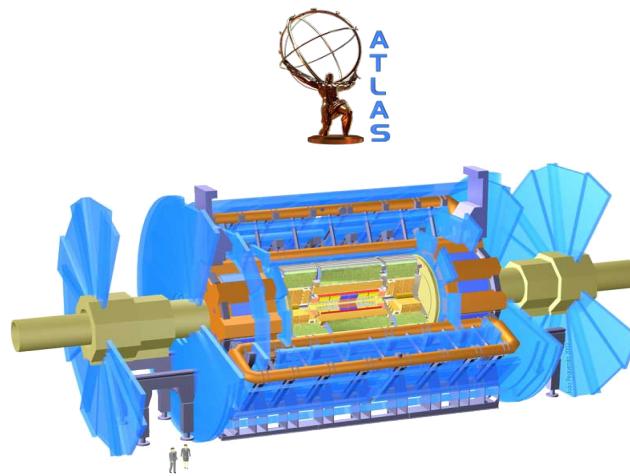
- p-p @ 7-14 TeV (2010, ...)

- Pb-Pb @ 2.76-5.5 TeV (2010, ...)

- p-Pb @ 8.8 TeV (2015?)



LHC heavy-ion experiments



ALICE: dedicated HI experiment

People: largest community (~1000)

$|\eta| < 1$: Tracking (TPC+ITS+TRD)

Calorimetry (EMCal, PHOS)

$\eta = 2.5-4$: Muon spectrometer.

0.5 T solenoid magnet

Strongest capabilities:

low- p_T , light-quark PID, ...

ATLAS & CMS: multipurpose (pp+HI) program

People: ~50/2000 (ATLAS), ~120/2500 (CMS)

$|\eta| < 2.5$: Tracking, muons

$|\eta| < 5$: EM/HAD Calorimetry

$\eta = 5-6.6$: Forward calorimetry (CMS)

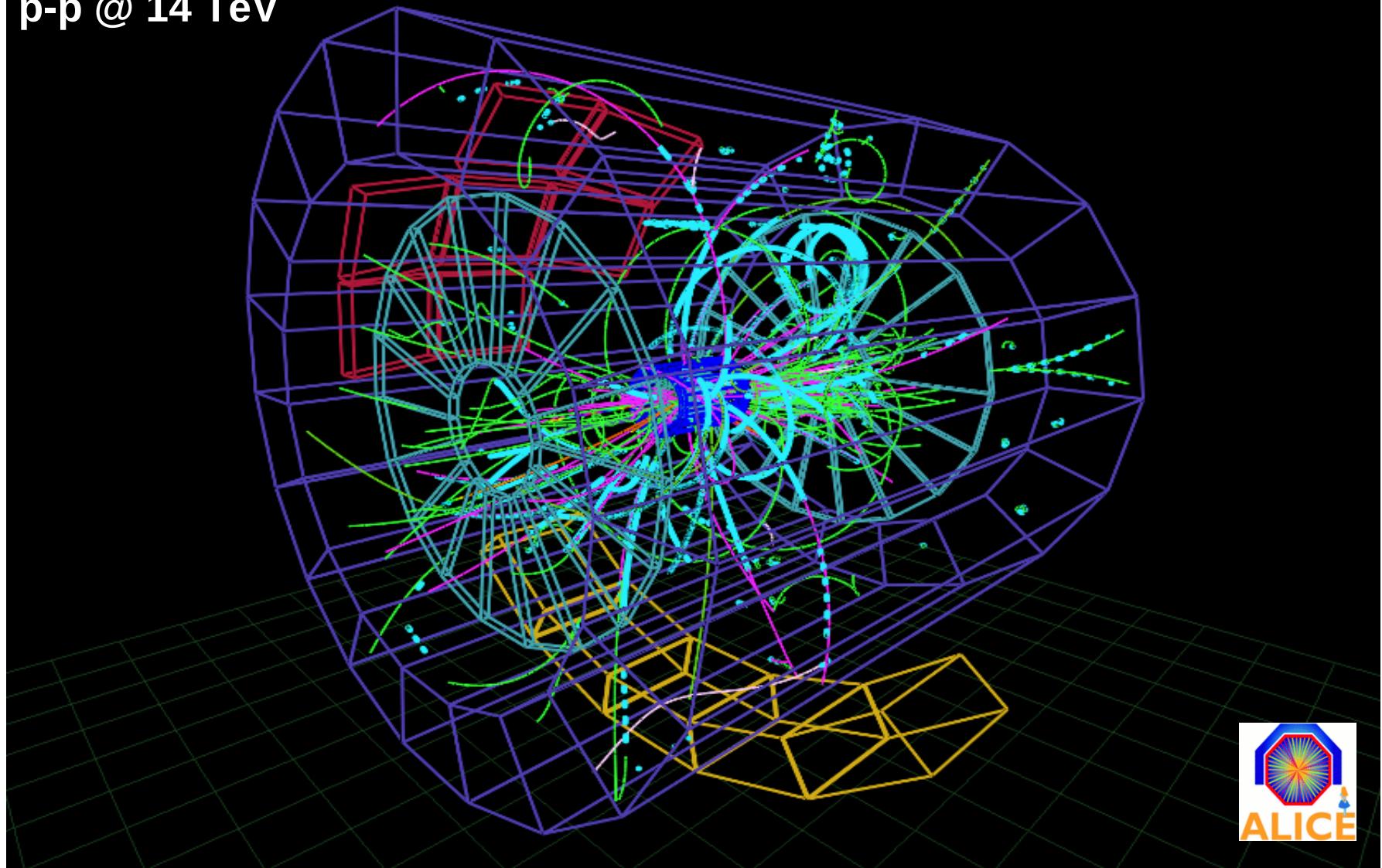
4 T (CMS), 2 T (ATLAS) mag. field

Strongest capabilities:

hard-probes, full jet reco, heavy-Q jet PID

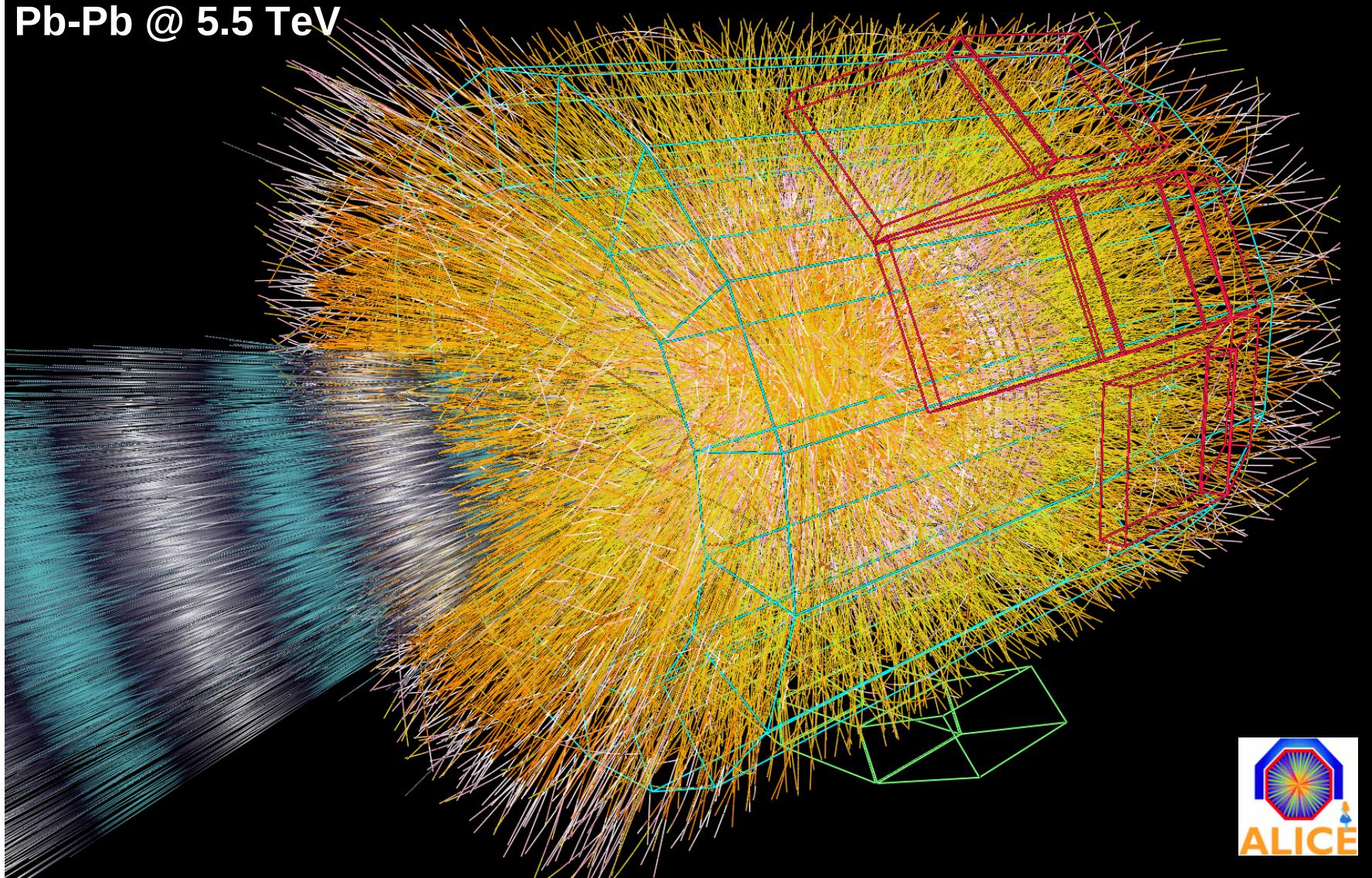
ALICE event display: p-p @ 14 TeV

p-p @ 14 TeV



ALICE event display: Pb-Pb @ 5.5 TeV

Pb-Pb @ 5.5 TeV



Quark-gluon matter probes:

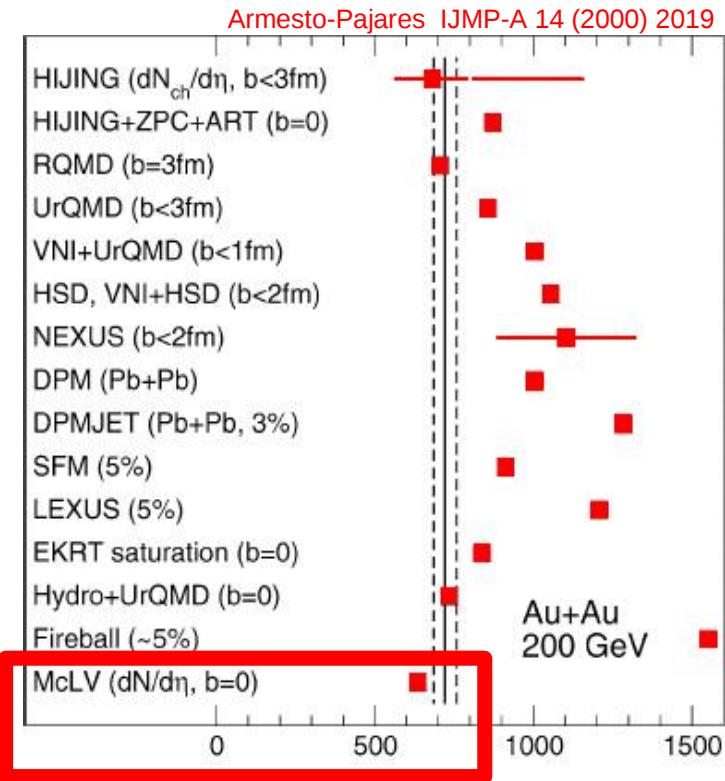
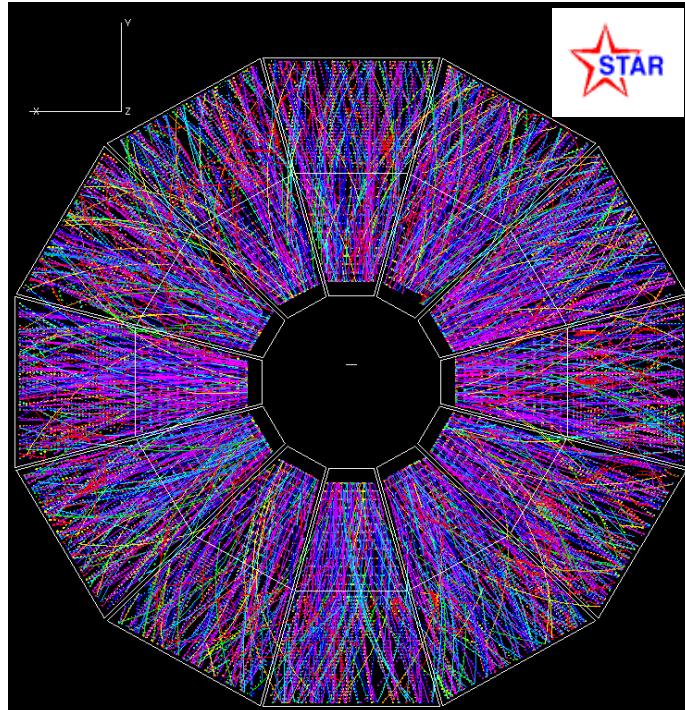
Observable (type)	Medium property	Theoretical tool
dN/dη multiplicity (soft)	gluonic struct. $xG(x,Q^2)$	Color-Glass-Condensate
dN/dp _T spectra (soft)	Equation-of-State $P(V,T)$	(Hydro), Lattice QCD
dN/dΔφ elliptic flow (soft)	shear viscosity η	(Hydro), AdS/CFT
Jet quenching (hard)	transport coefficient $<\!q\!>$	(Hydro), pQCD,AdS/CFT
γ enhancement (intermed.)	critical temperature T_{crit}	(Hydro), Lattice QCD
QQ suppression (hard)	critical energy density ε_{crit}	(Hydro), Lattice QCD

Quark-gluon matter probes (1)

Observable (type)	Medium property	Theoretical tool
dN/dη multiplicity (soft)	gluonic struct. $xG(x,Q^2)$	Color-Glass-Condensate
dN/d p_T spectra (soft)	Equation-of-State $P(V,T)$	(Hydro), Lattice QCD
dN/d $\Delta\phi$ elliptic flow (soft)	shear viscosity η	(Hydro), AdS/CFT
Jet quenching (hard)	transport coefficient $\langle q \rangle$	(Hydro), pQCD,AdS/CFT
γ enhancement (intermed.)	critical temperature T_{crit}	(Hydro), Lattice QCD
QQ suppression (hard)	critical energy density $\varepsilon_{\text{crit}}$	(Hydro), Lattice QCD

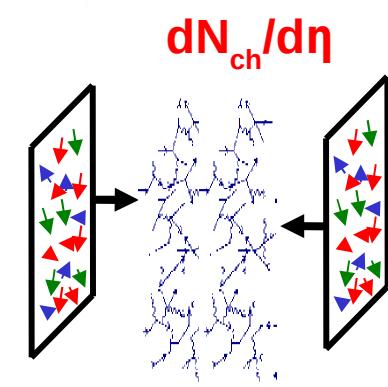
Total Au-Au hadron multiplicity (RHIC)

- AuAu (200 GeV) 0-5% central collisions:



~ 650 charged hadrons per unit rapidity at $y=0$

- Most hadrons from semihard partons w/ $Q_s \sim 1.5$ GeV
- Low multiplicity predicted by saturation models due to reduced incoming parton flux ($gg \rightarrow g$)

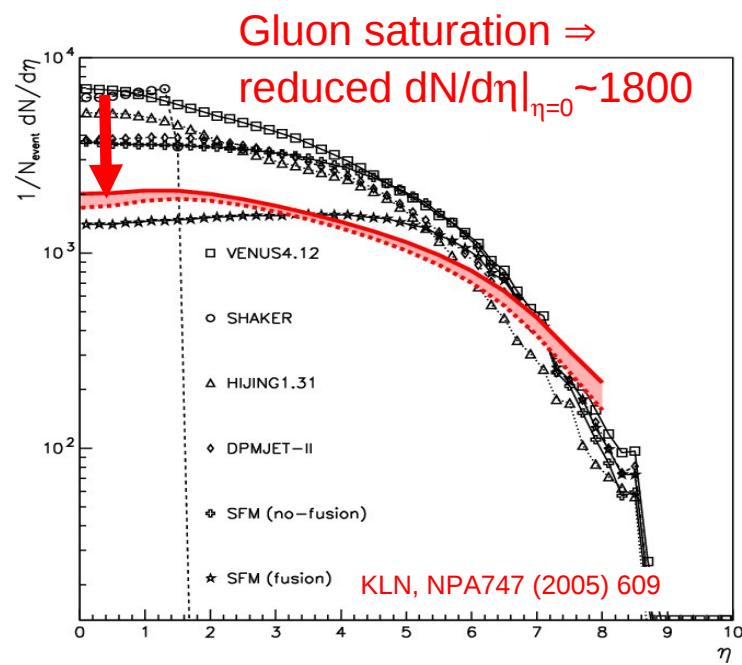
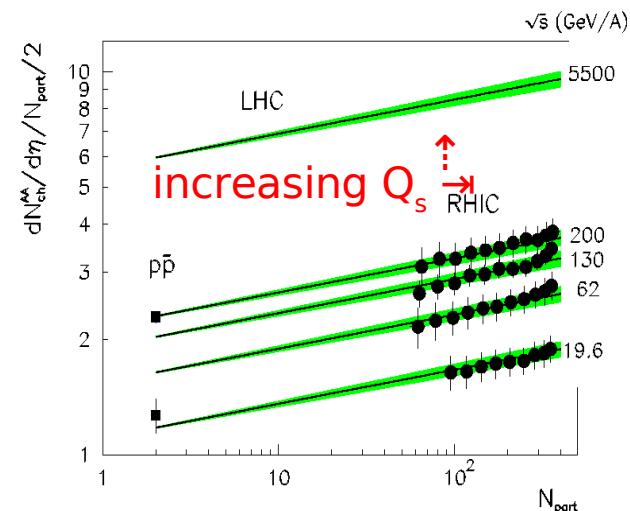
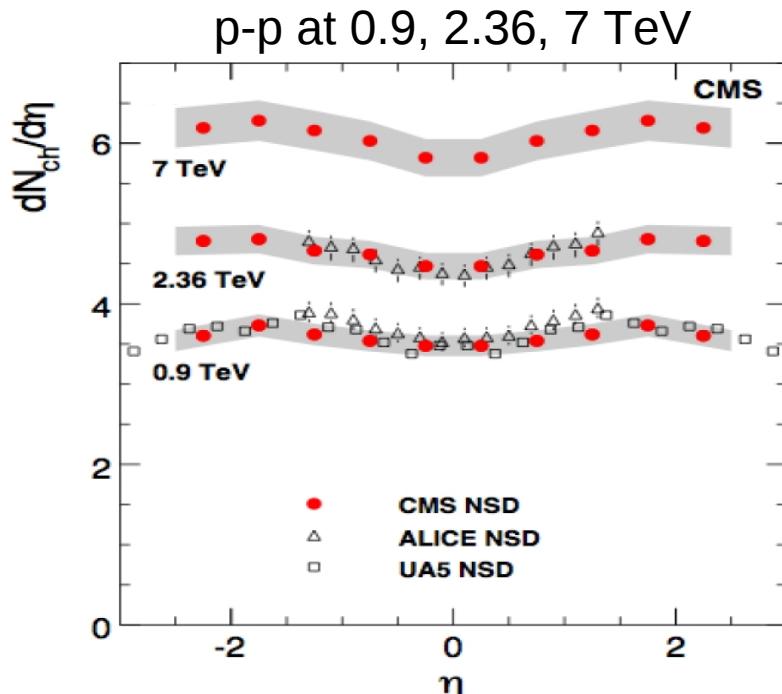


Total Pb-Pb hadron multiplicity (LHC)

- Final A-A hadron multiplicity \propto Initial # of released gluons with $p_T \sim Q_s \propto xG \propto A^{1/3} \times (\sqrt{s})^\lambda$:

CGC: $dN_{ch}/d\eta \propto A^{1/3} \times (\sqrt{s})^\lambda$, with $\lambda \sim 0.25$

- $dN_{ch}/d\eta$: 1st LHC measurement (Si trackers):

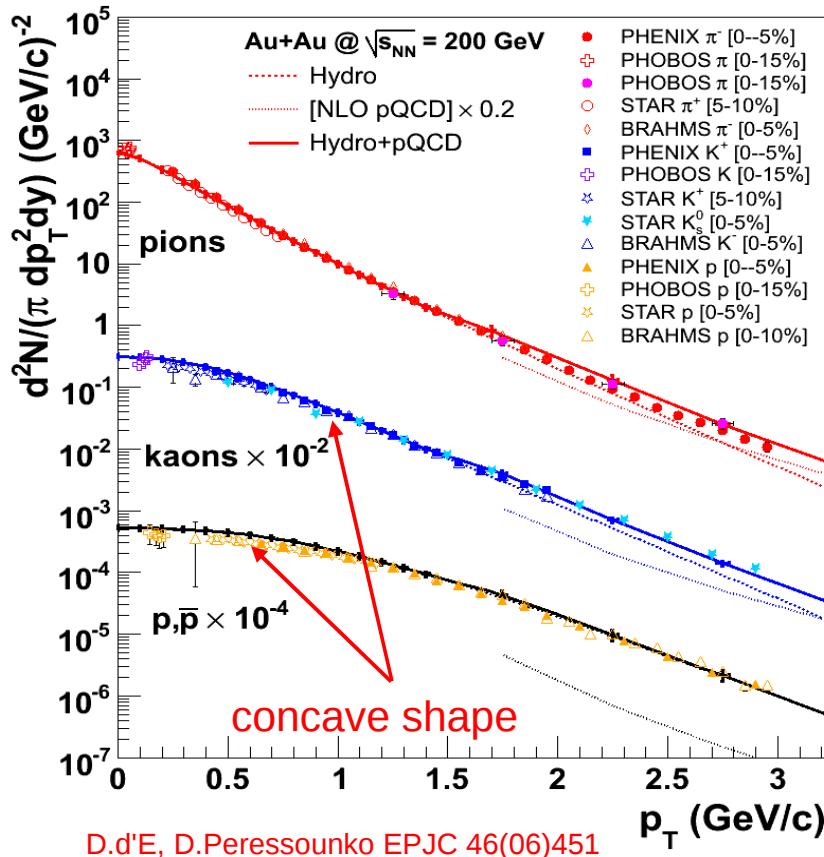


Quark-gluon matter probes (2)

Observable (type)	Medium property	Theoretical tool
dN/dη multiplicity (soft)	gluonic struct. $xG(x, Q^2)$	Color-Glass-Condensate
dN/dp_T spectra (soft)	Equation-of-State $P(V,T)$	(Hydro), Lattice QCD
dN/d $\Delta\phi$ elliptic flow (soft)	shear viscosity η	(Hydro), AdS/CFT
Jet quenching (hard)	transport coefficient $\langle q \rangle$	(Hydro), pQCD, AdS/CFT
γ enhancement (intermed.)	critical temperature T_{crit}	(Hydro), Lattice QCD
QQ suppression (hard)	critical energy density ϵ_{crit}	(Hydro), Lattice QCD

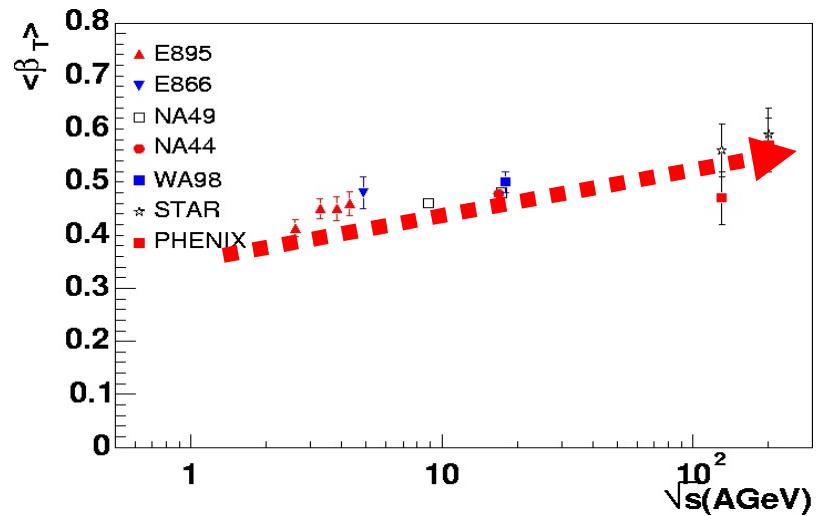
Soft hadron spectra (RHIC)

- Single hadron (π^\pm , K^\pm , p, pbar) p_T spectra up to ~ 2 GeV/c boosted for increasing centrality, with a (mass-dependent) collective radial flow:



- “Explosive” behaviour reproduced in hydro:

QGP EoS ($\varepsilon_0 \sim 30$ GeV/fm 3) & fast thermalization ($\tau_0 \sim 0.6$ fm/c)

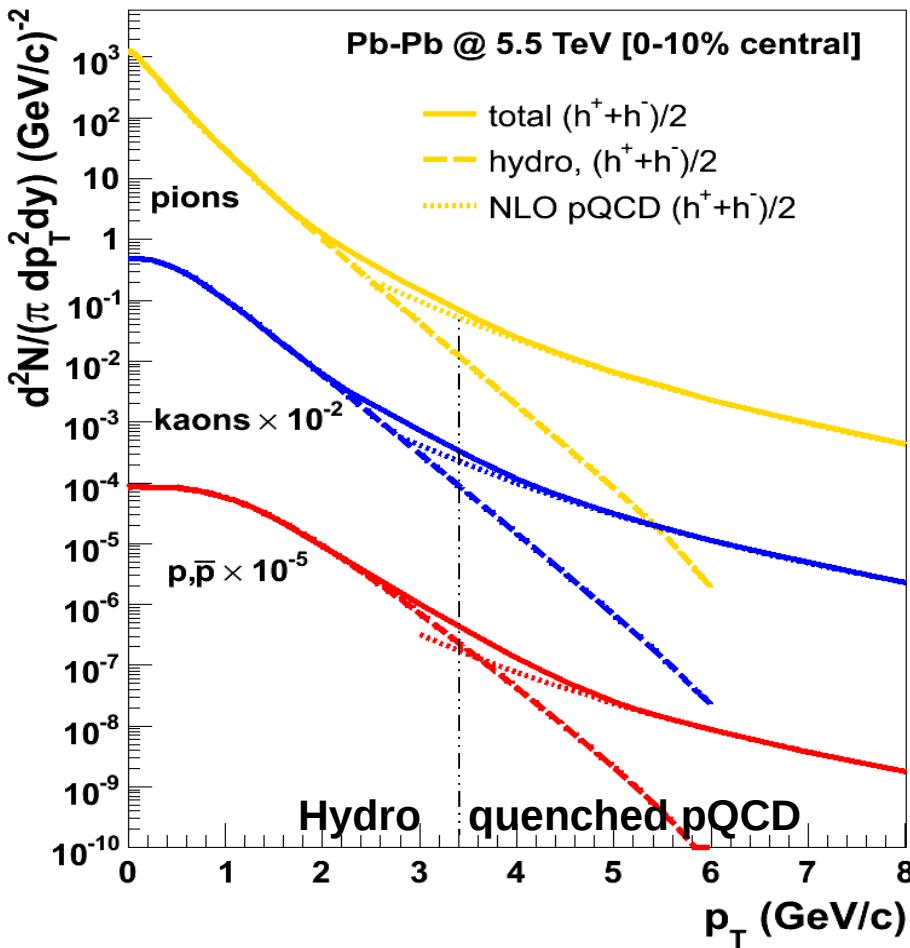


Expansion rate depends on EoS:

$$\frac{\partial u^\mu}{\partial t} = \frac{c_s^2}{1 + c_s^2} \cdot \frac{\nabla^\mu \varepsilon}{\varepsilon} \quad \text{with} \quad c_s^2 = \frac{\partial P}{\partial \varepsilon} = \frac{1}{3}$$

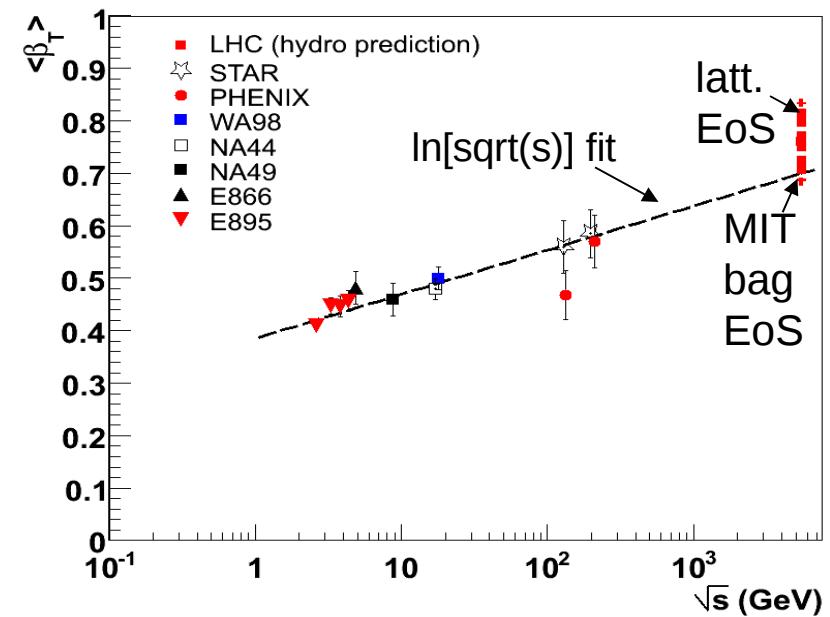
Soft hadron spectra (LHC)

- LHC plasma starts hotter & denser: Larger transverse pressure expected
- “Hydrodynamics” predictions for $\varepsilon_0 \sim 650 \text{ GeV/fm}^3$ at $\tau_0 \sim 0.1 \text{ fm/c}$:



Arleo-DdE-Peressounko JPG 35 (08)054001

Collective expansion velocity of inclusive hadrons: $\langle \beta_T \rangle \approx 0.75$

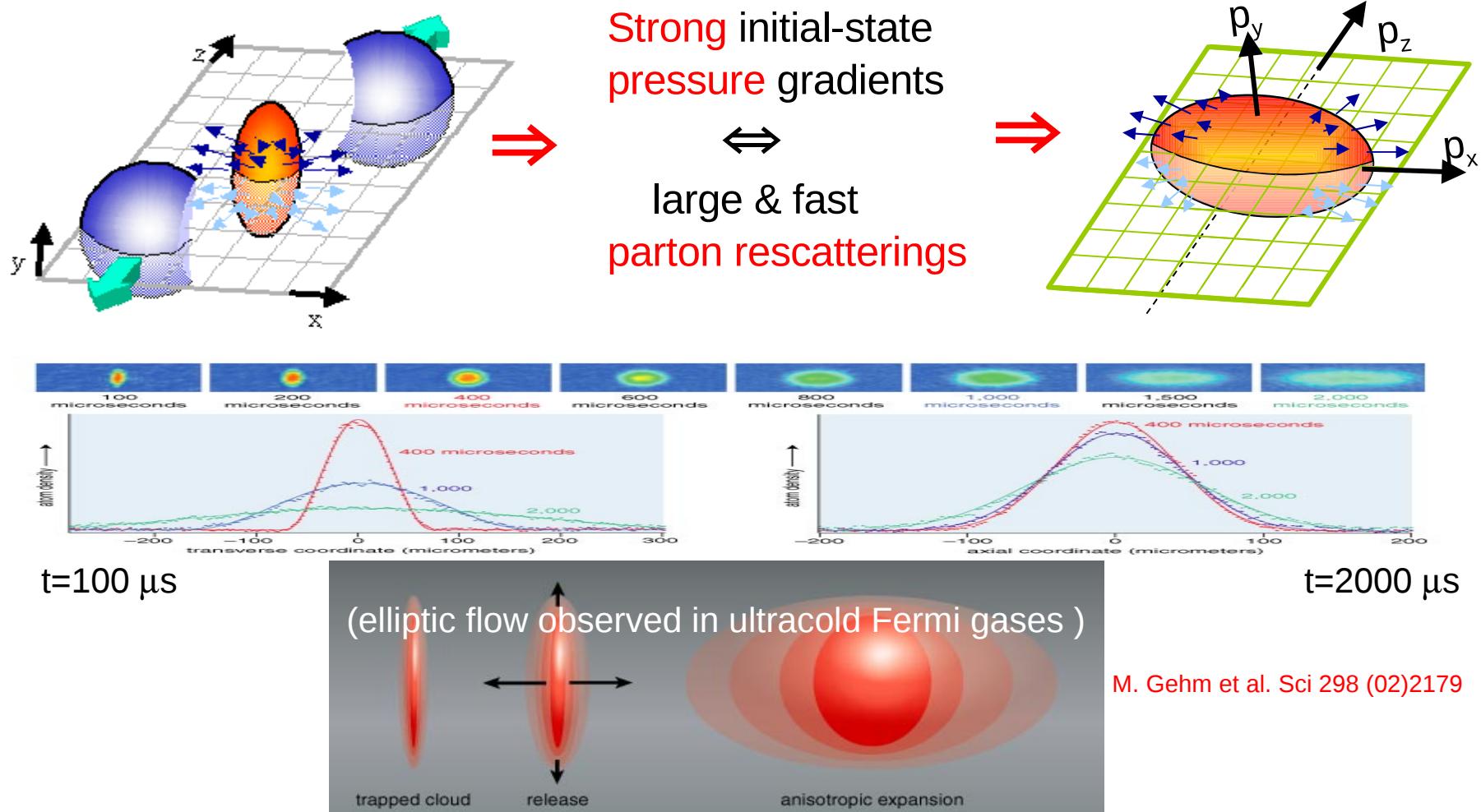


Quark-gluon matter probes (3)

Observable (type)	Medium property	Theoretical tool
dN/dη multiplicity (soft)	gluonic struct. $xG(x, Q^2)$	Color-Glass-Condensate
dN/d p_T spectra (soft)	Equation-of-State $P(V, T)$	(Hydro), Lattice QCD
dN/d$\Delta\phi$ elliptic flow (soft)	shear viscosity η	(Hydro), AdS/CFT
Jet quenching (hard)	transport coefficient $\langle q \rangle$	(Hydro), pQCD, AdS/CFT
γ enhancement (intermed.)	critical temperature T_{crit}	(Hydro), Lattice QCD
QQ suppression (hard)	critical energy density $\varepsilon_{\text{crit}}$	(Hydro), Lattice QCD

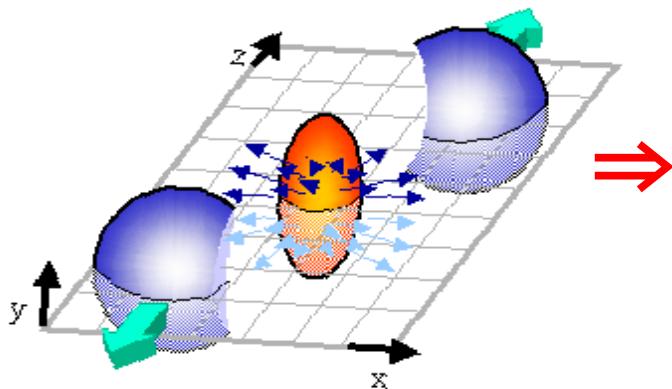
Elliptic flow: azimuthal anisotropies

- Lens-shaped spatial anisotropy (overlap) in non-central collisions translates into boosted momentum along reaction plane:

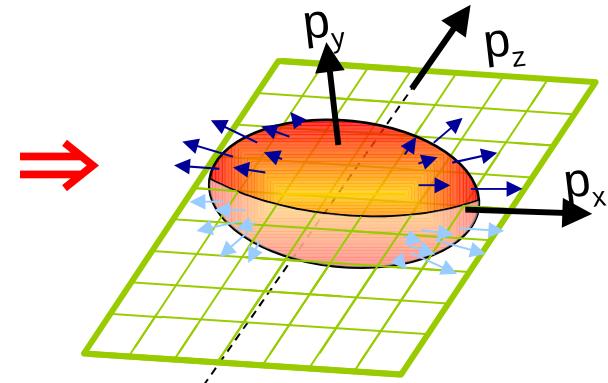


Elliptic flow: azimuthal anisotropies

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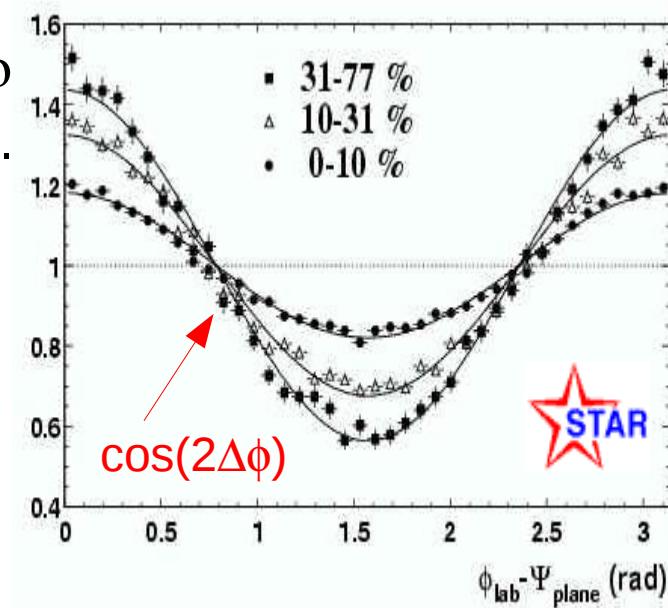
Strong initial-state pressure gradients
↔
large & fast parton rescatterings



- Elliptic flow $v_2 = 2^{\text{nd}}$ Fourier coeff. azimuth distrib.

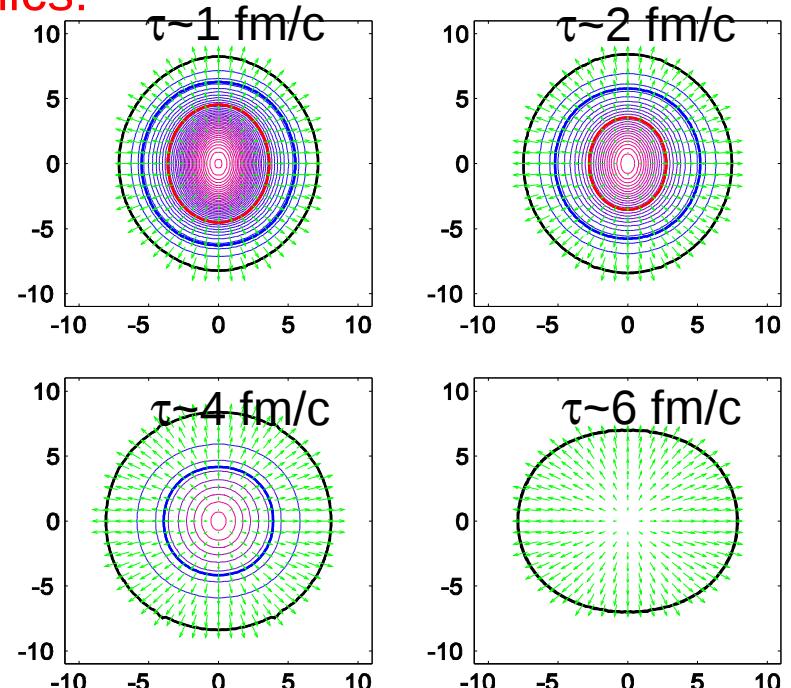
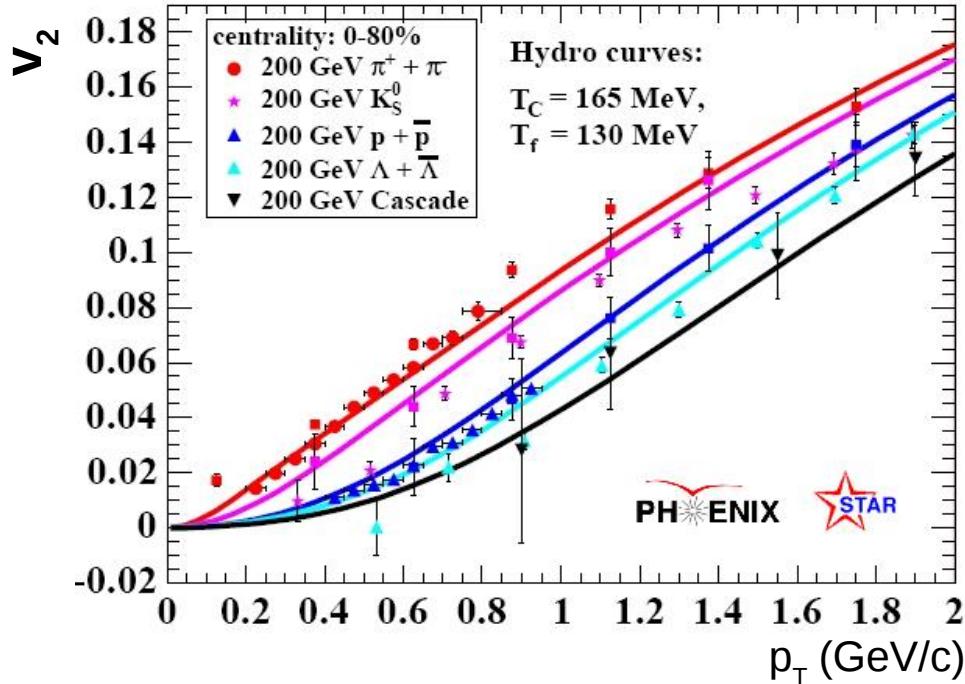
$$E \frac{d^3N}{d^3p} = \frac{1}{2\pi} \frac{d^2N}{p_T dp_T dy} \left(1 + 2 \sum_{n=1}^{\infty} v_n \cos[n(\phi - \Phi_{RP})] \right)$$

- v_2 is very sensitive to medium viscosity



Strong elliptic flow (RHIC): QGP = perfect fluid ?

- Large v_2 signal (~20%) for all hadrons well described by “perfect fluid” (= non-viscous) relativistic hydrodynamics:



⇒ Initial conditions: $\tau_0 = 0.6 \text{ fm/c}$, $\varepsilon_0 \sim 30 \text{ GeV/fm}^3$

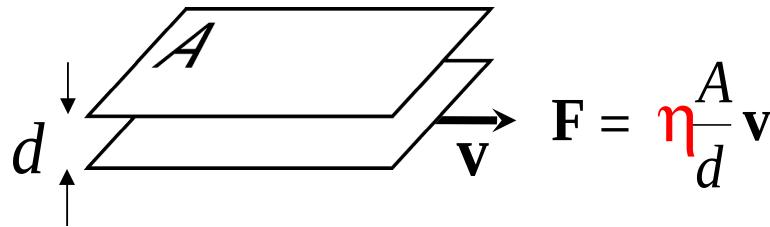
Kolb-Heinz,Huovinen,Teaney, ...

⇒ Lattice QCD (QGP → hadron gas) Equation-of-State

⇒ Zero viscosity (no “internal dissipation”) term in equations.

Minimum universal viscosity from AdS/CFT

- (Shear) Viscosity \sim “internal friction” of a fluid: $\eta \sim 1/(\text{fluidity})$:



η : resistance to flow gradients



Microscopically: $\eta = \frac{1}{T} \int d^4x \langle T_{xy}(x)T_{xy}(0) \rangle$ (hard to compute in lattQCD !)

- Minimum viscosity/entropy ratio possible:

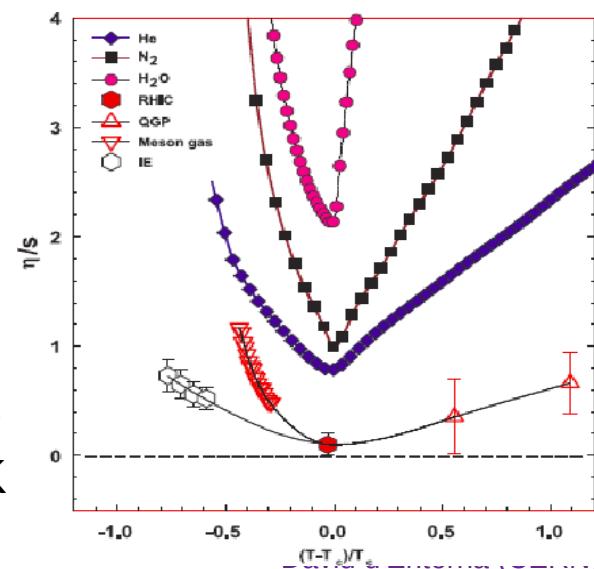
$$\eta/s \geq 1/4\pi(\hbar/k_B)$$

AdS/CFT “universal bound” (see next slide)

[Kovtun-Starinets-Son, PRL94,111601(2005)]

- Only 3 classes of quantum fluids known to have $\eta/s < (\hbar/k_B)$!

- Strongly-coupled Bose fluids (liquid ${}^4\text{He}$) $T_{\text{crit}} \sim 5 \text{ K}$
- Strongly-correlated ultracold Fermi gases $T_{\text{crit}} \sim 10^{-6} \text{ K}$
- Quark-Gluon-Plasma $T_{\text{crit}} \sim 10^{12} \text{ K}$



Viscosity from AdS/CFT correspondence

- Certain gauge-theories in Minkowski space can be obtained as limits in the 4-D boundary of simpler 5-D string dual theories:

- Duality relation between couplings: $g_{\text{SYM}}^2 = 4\pi g_{\text{st}}$ $g_{\text{SYM}}^2 N_c = \left(\frac{R}{l_{\text{st}}}\right)^4$
 - “Easy” case: strongly-coupled QFT \leftrightarrow classical gravity



- Dual thermodynamics: BH Hawking $T \Leftrightarrow$ SYM plasma: $T_H = r_0 \hbar / \pi R^2$
 - Dual transport coeffic.: Graviton BH $\sigma_{\text{absorption}} \Leftrightarrow$ SYM viscosity/entropy
 - KSS “universal bound”: $\eta/s \geq 1/4\pi(\hbar/k_B)$

Kovtun-Starinets-Son, PRL94(05)111601

Viscous relativistic fluid-dynamics

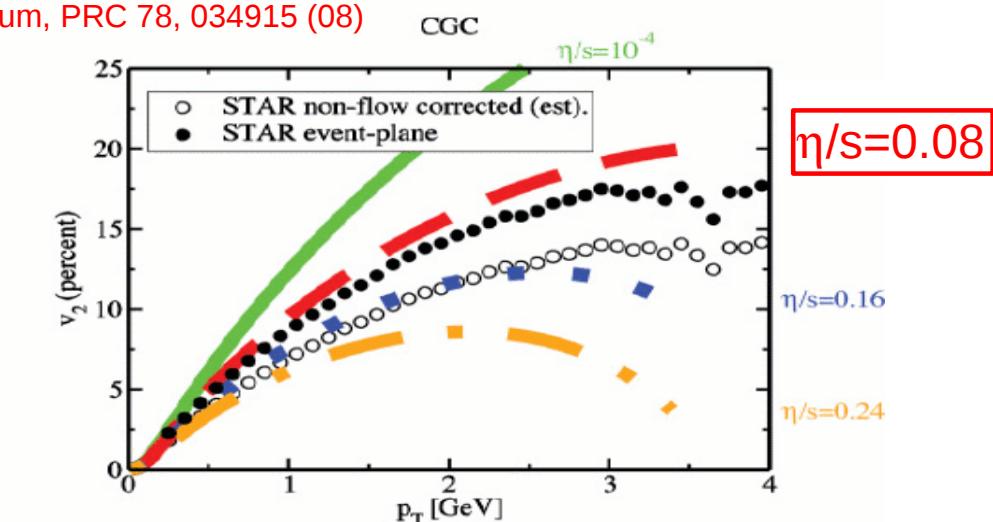
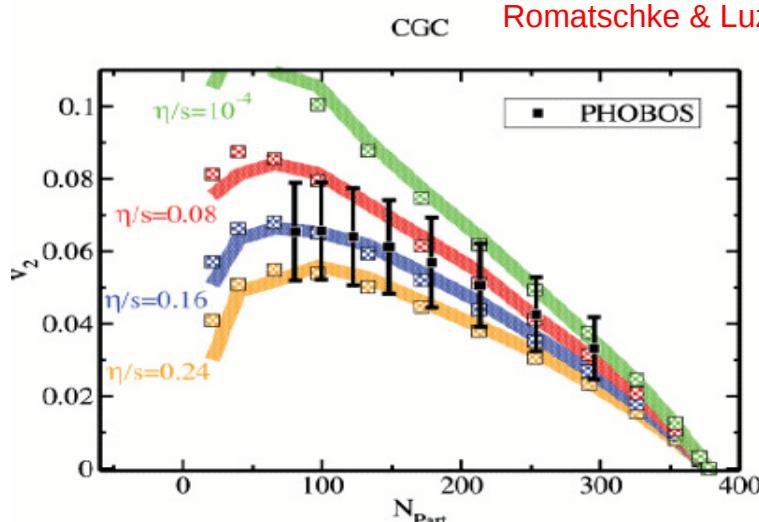
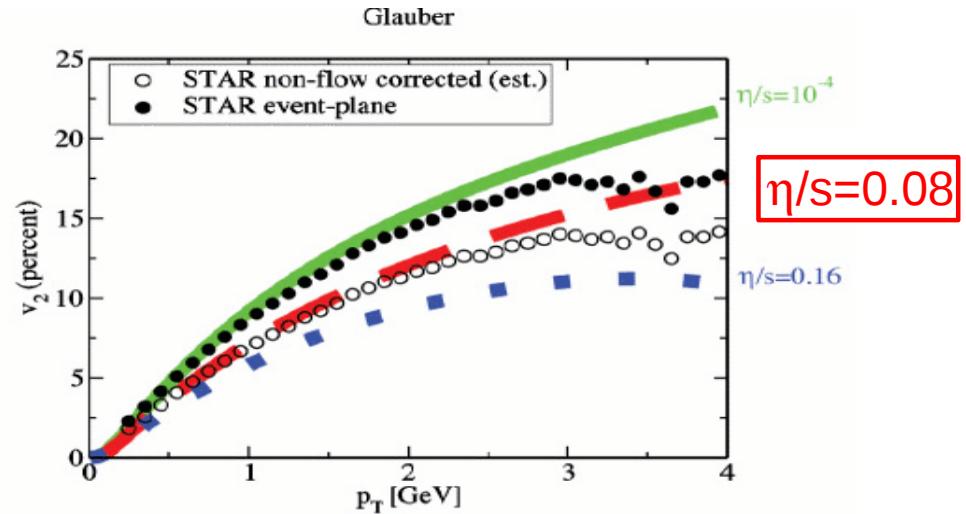
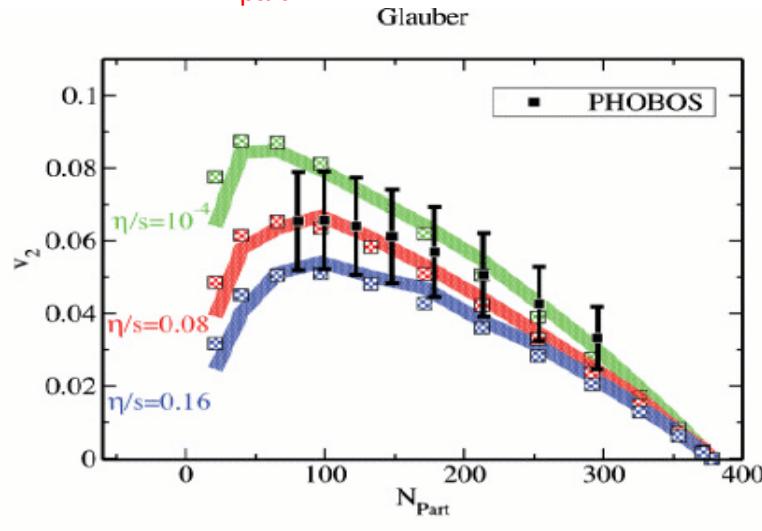
- Relativistic hydrodynamics equations with non-zero viscosity η
(theoretical “tour de force”) ...

$$\begin{aligned}\tau_\Pi \dot{\Pi} + \Pi &= \Pi_{\text{NS}} + \tau_{\Pi q} q \cdot \dot{u} - \ell_{\Pi q} \partial \cdot q - \zeta \hat{\delta}_{0,1} \Pi \theta \\ &\quad + \lambda_{\Pi q} q \cdot \nabla \alpha + \lambda_{\Pi \pi} \pi^{\mu\nu} \sigma_{\mu\nu} + \hat{\delta}_{0,2} \Pi^2 + \hat{\epsilon}_0 q \cdot q + \hat{\eta}_0 \pi^{\mu\nu} \pi_{\mu\nu} \\ \tau_q \Delta^{\mu\nu} \dot{q}_\nu + q^\mu &= q_{\text{NS}}^\mu - \tau_{q\Pi} \Pi \dot{u}^\mu - \tau_{q\pi} \pi^{\mu\nu} \dot{u}_\nu \\ &\quad + \ell_{q\Pi} \nabla^\mu \Pi - \ell_{q\pi} \Delta^{\mu\nu} \partial^\lambda \pi_{\nu\lambda} + \tau_q \omega^{\mu\nu} q_\nu - \frac{\kappa}{\beta} \hat{\delta}_{1,1} q^\mu \theta \\ &\quad - \lambda_{qq} \sigma^{\mu\nu} q_\nu + \lambda_{q\Pi} \Pi \nabla^\mu \alpha + \lambda_{q\pi} \pi^{\mu\nu} \nabla_\nu \alpha \\ &\quad + \hat{\delta}_{1,2} \Pi q^\mu + \hat{\eta}_1 \pi^{\mu\nu} q_\nu \\ \tau_\pi \dot{\pi}^{<\mu\nu>} + \pi^{\mu\nu} &= \pi_{\text{NS}}^{\mu\nu} + 2 \tau_{\pi q} q^{<\mu} \dot{u}^{\nu>} \\ &\quad + 2 \ell_{\pi q} \nabla^{<\mu} q^{\nu>} + 2 \tau_\pi \pi_\lambda^{<\mu} \omega^{\nu>\lambda} - 2 \eta \hat{\delta}_{2,1} \pi^{\mu\nu} \theta \\ &\quad - 2 \tau_\pi \pi_\lambda^{<\mu} \sigma^{\nu>\lambda} - 2 \lambda_{\pi q} q^{<\mu} \nabla^{\nu>} \alpha + 2 \lambda_{\pi\Pi} \Pi \sigma^{\mu\nu} \\ &\quad + \hat{\delta}_{2,2} \Pi \pi^{\mu\nu} - \hat{\eta}_2 \pi_\lambda^{<\mu} \pi^{\nu>\lambda} - \hat{\epsilon}_2 q^{<\mu} q^{\nu>}\end{aligned}$$

P.Romatschke-Baier, D.Teaney, U.Heinz-Song, A.Muronga ...

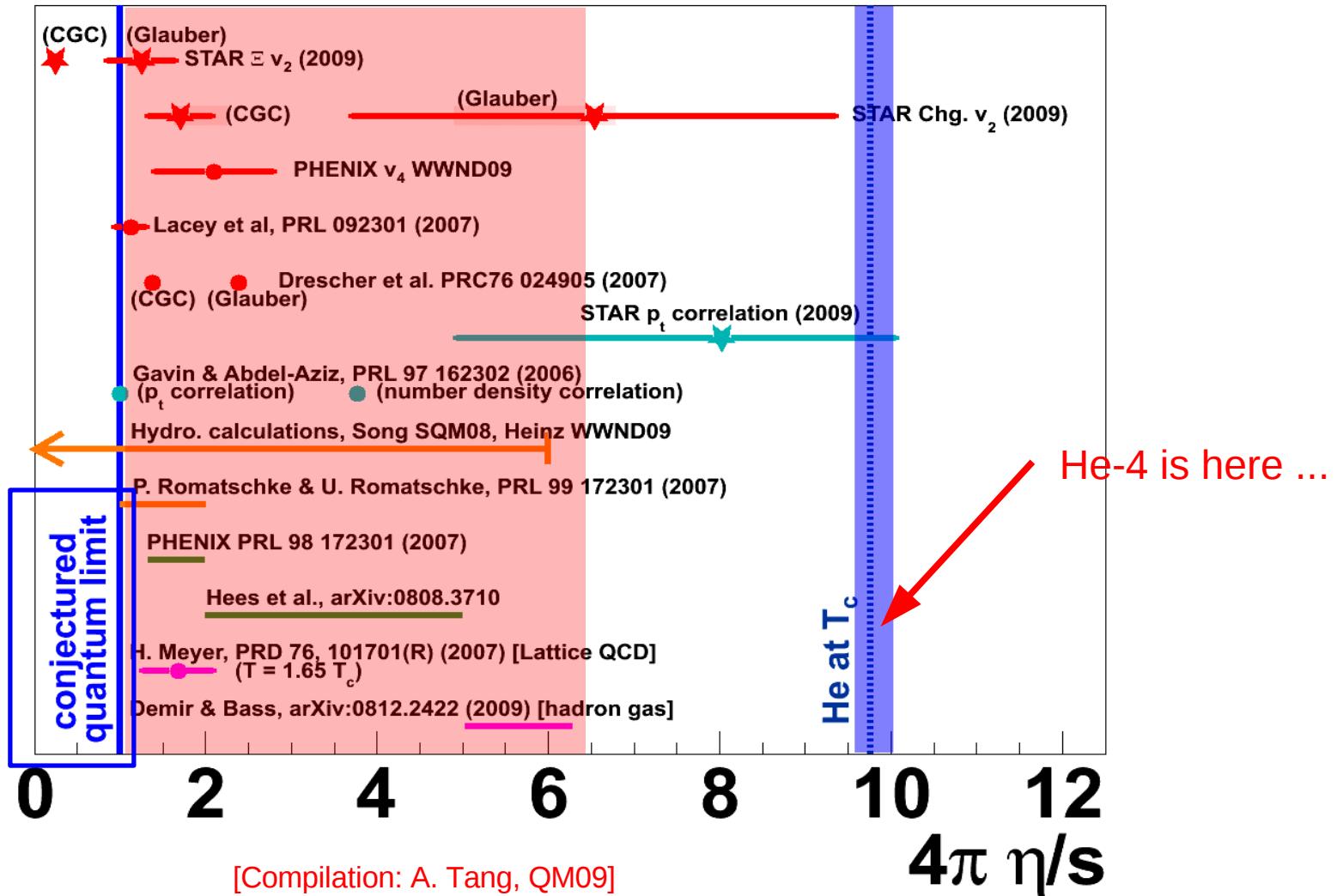
Elliptic flow: very small viscosity

- Inclusion of shear stress, $T^{\mu\nu} = T_0^{\mu\nu} + \eta(\nabla^\mu u^\nu)$ modifies expansion rate:
 $v_2(p_T, N_{\text{part}})$ strongly reduced !



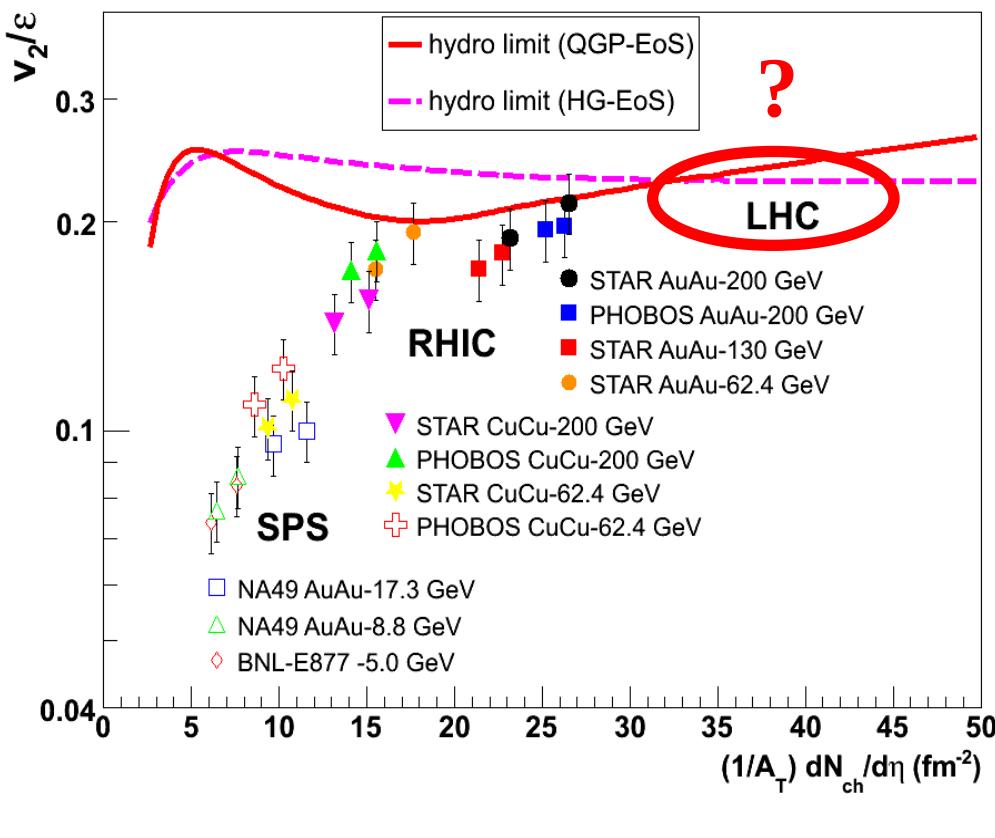
QGP viscosity constraints from RHIC data

- QGP is the **best** perfect-fluid known ! $\eta/s < 6 \cdot (\hbar/k_B)/4\pi$

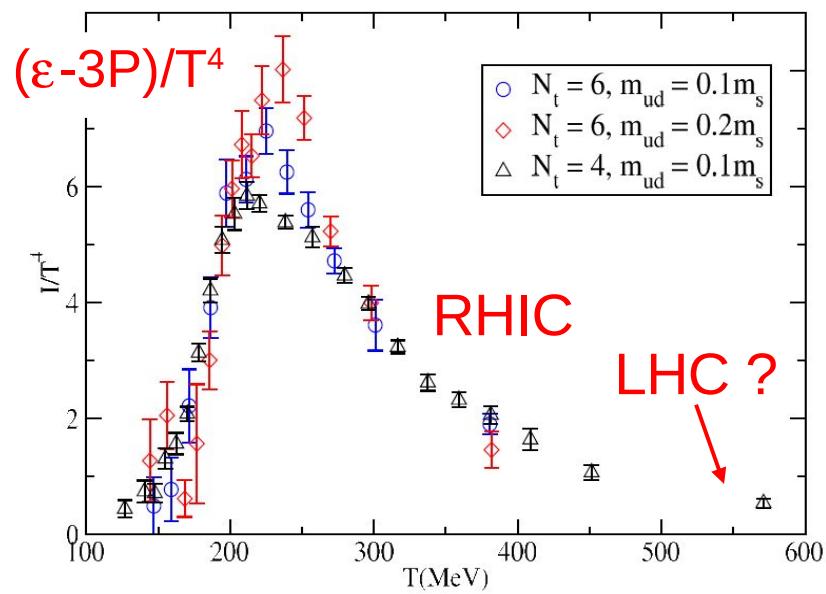


Elliptic flow (LHC)

■ Collective azimuthal anisotropy (v_2 parameter) in Pb-Pb 5.5 TeV ?



- ◆ null-viscosity fluid as at RHIC ?
⇒ AdS/CFT applicable ...
- ◆ weakly interacting (high viscosity)
quark-gluon “gas” from latt.-QCD ?

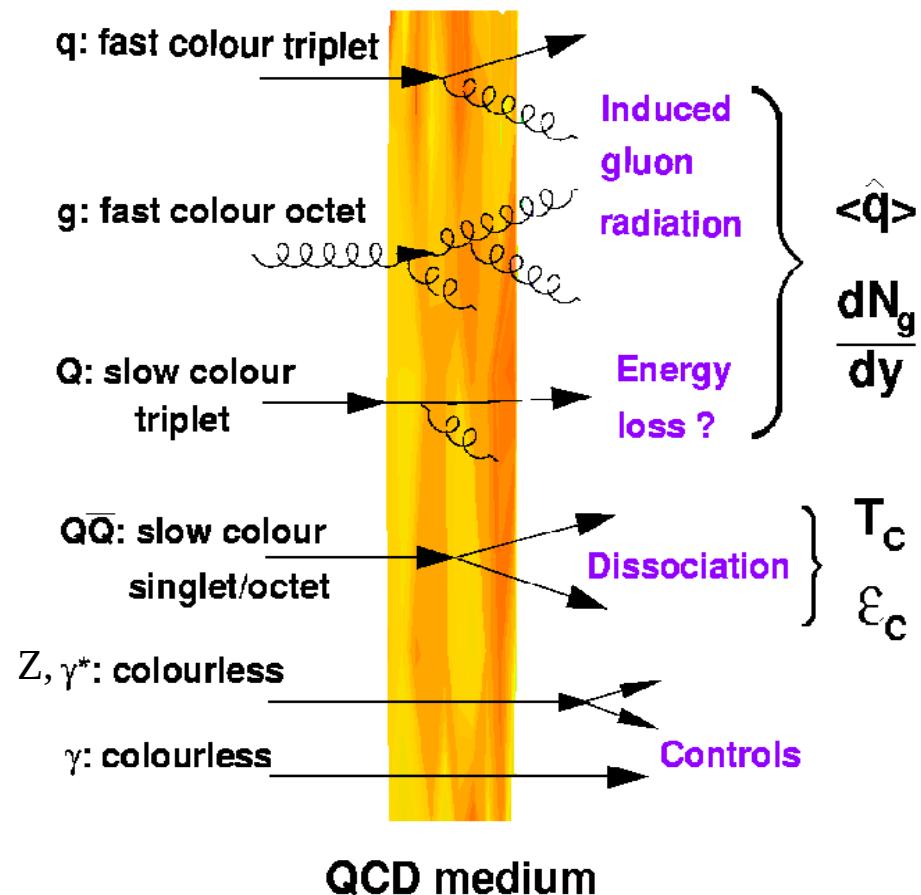
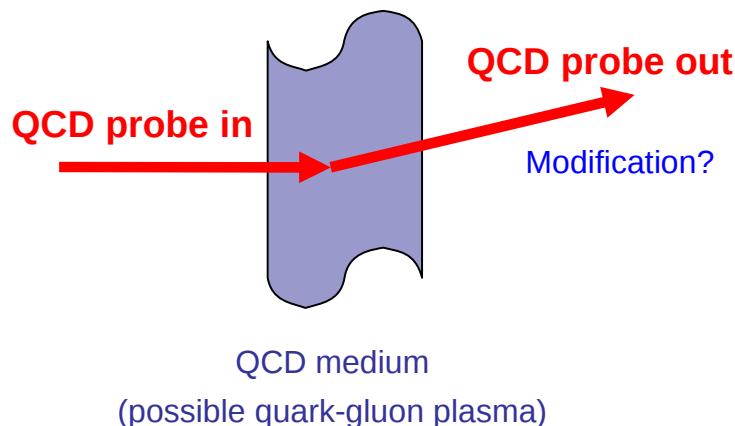


Hard QGP probes

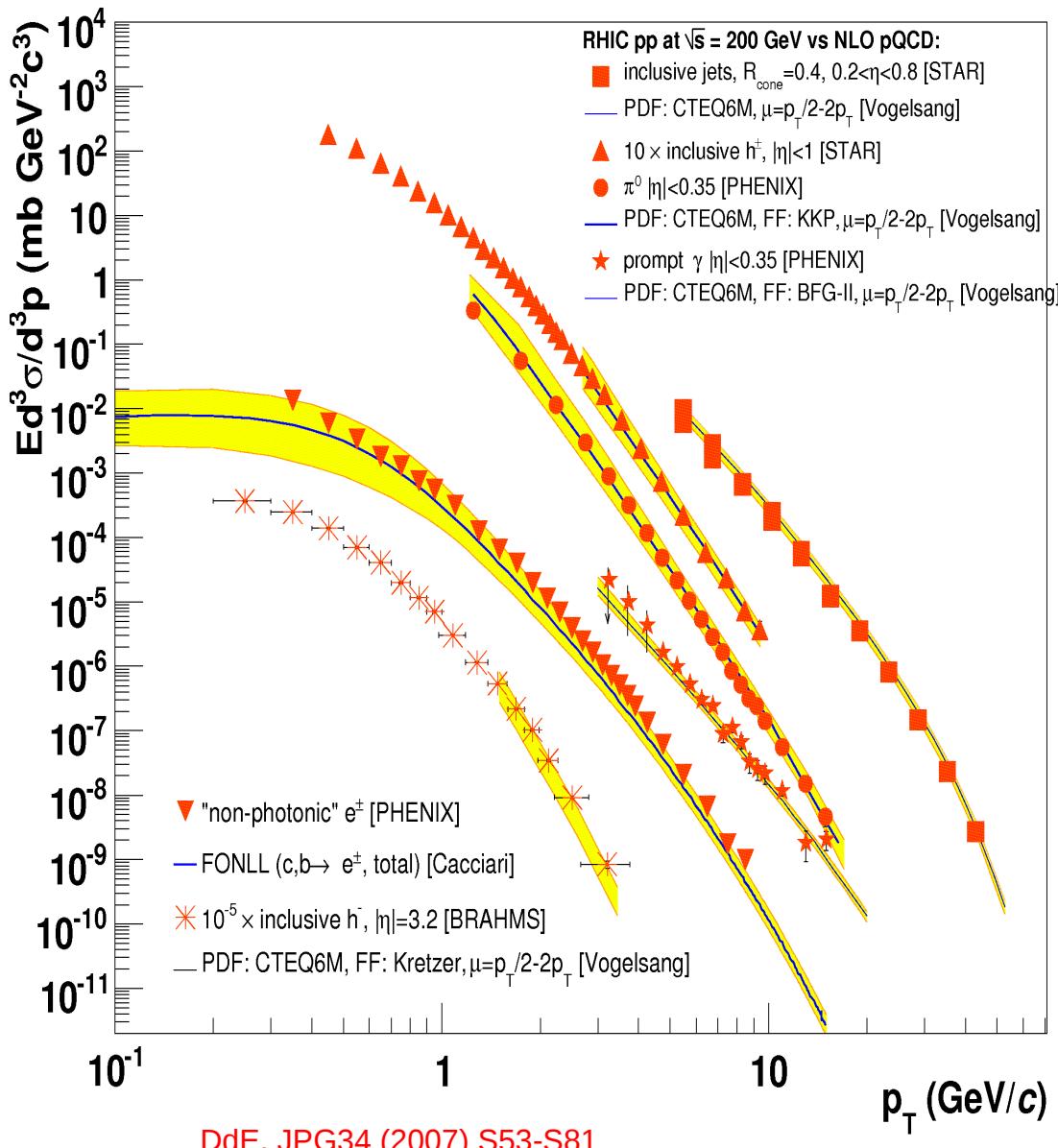
Hard “tomographic” probes of QCD matter

■ Hard-probes of QCD matter:

- ◆ jets, γ , $Q\bar{Q}$... well controlled experimentally & theoretically (pQCD)
- ◆ self-generated in collision at $\tau < 1/Q \sim 0.1$ fm/c,
- ◆ tomographic probes of hottest
& densest phases of medium .



RHIC “QCD vacuum” (p-p) references vs. pQCD



$p_{\text{T}} \Rightarrow X, \sqrt{s}=200$ GeV

■ Jets, high- p_{T} hadrons,
prompt- γ , heavy-Q ...
High-quality
measurements
within $p_{\text{T}} \sim 2-45$ GeV/c

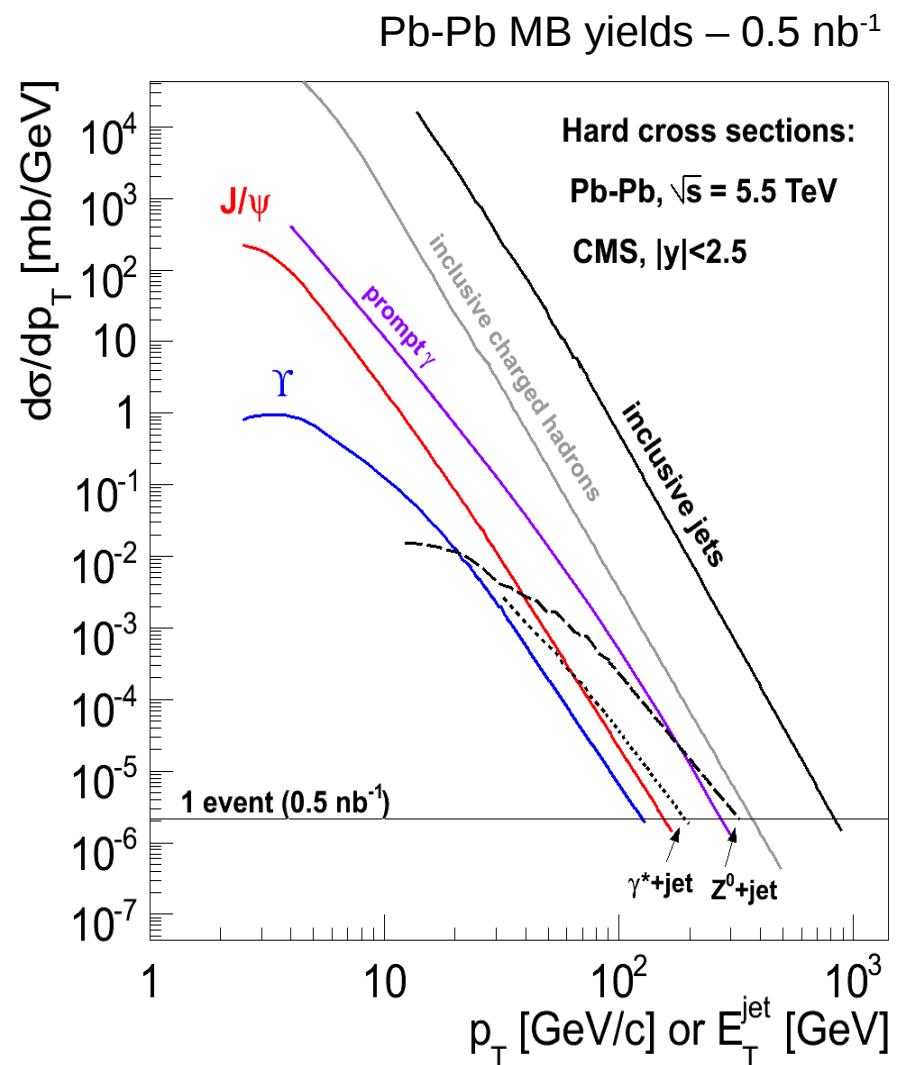
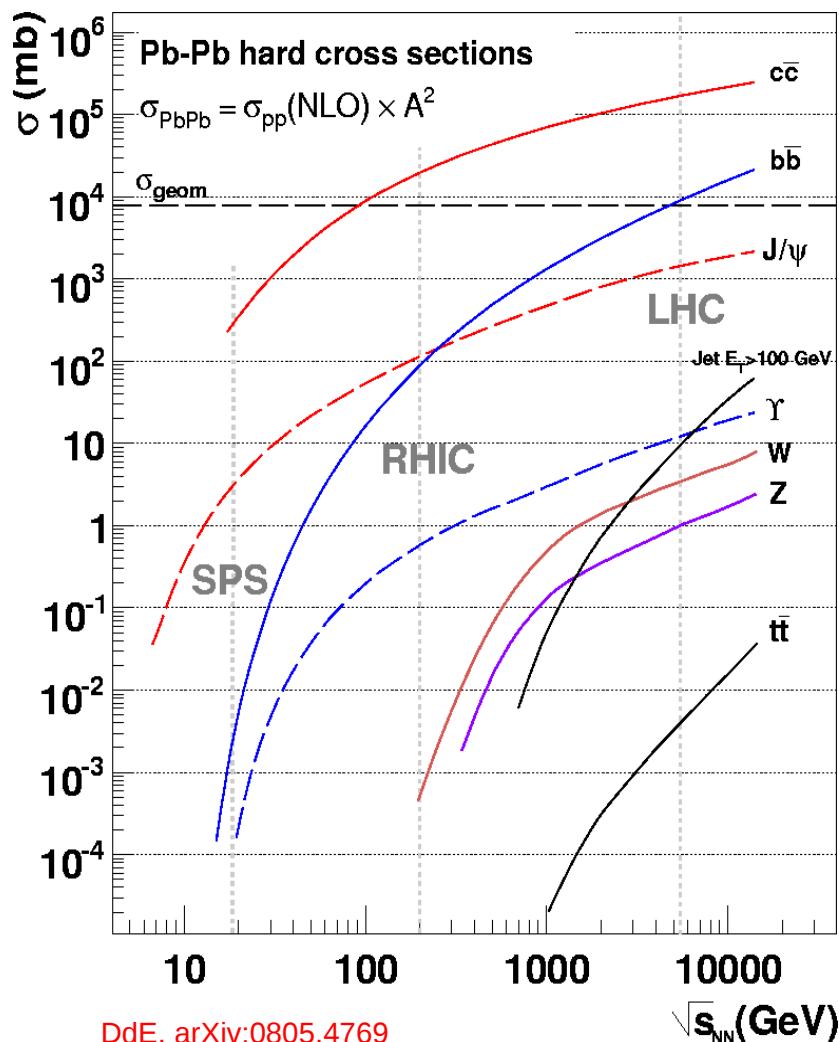
■ NLO [1], NLL [2] pQCD
+ recent PDFs, FFs
in good agreement
with all data.

[1] W. Vogelsang *et al.*

[2] M. Cacciari *et al.*

Hard probes cross-sections (LHC)

- Huge cross-sections (large statistics & p_T reach) at the LHC:

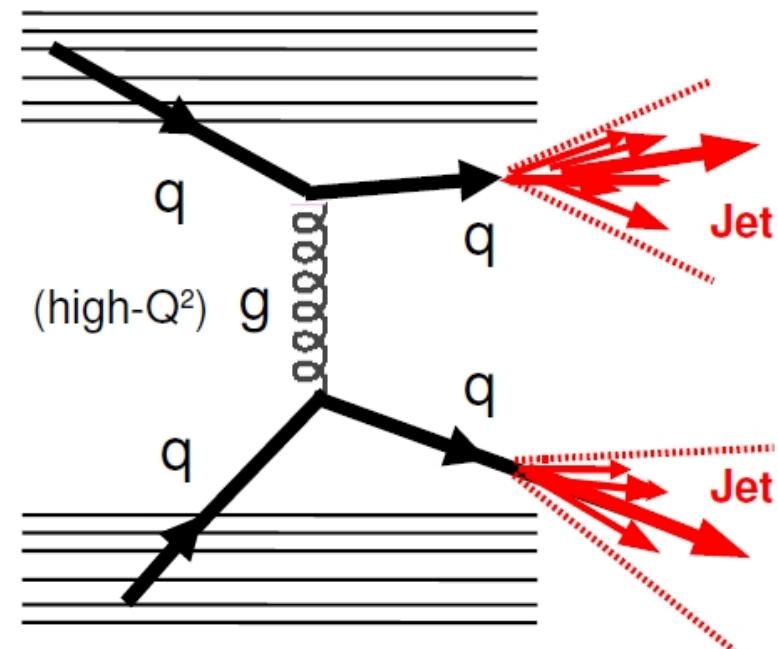
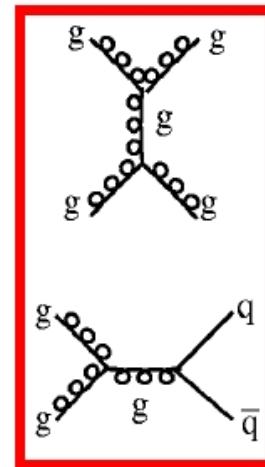
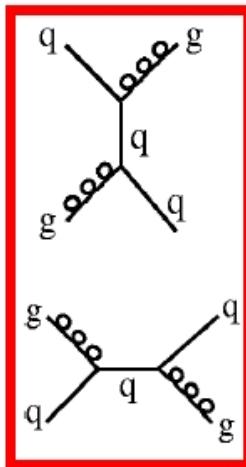
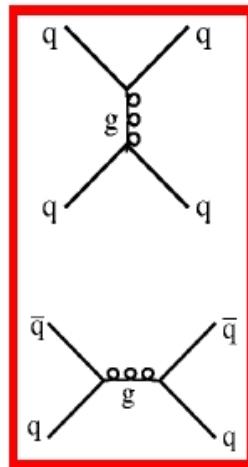


Quark-gluon matter probes (4)

Observable (type)	Medium property	Theoretical tool
dN/dη multiplicity (soft)	gluonic struct. $xG(x, Q^2)$	Color-Glass-Condensate
dN/d p_T spectra (soft)	Equation-of-State $P(V, T)$	(Hydro), Lattice QCD
dN/d $\Delta\phi$ elliptic flow (soft)	shear viscosity η	(Hydro), AdS/CFT
Jet quenching (hard)	transport coefficient $\langle q \rangle$	(Hydro), pQCD
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QQ suppression (hard)	critical energy density ϵ_{crit}	(Hydro), Lattice QCD

Jets in hadronic collisions

- Jet = high- p_T parton (quark, gluon) produced in a **hard scattering** process: $q\bar{q}$, qg , gg (or in the decay of a heavy particle)
- Jet **production processes** (leading order):

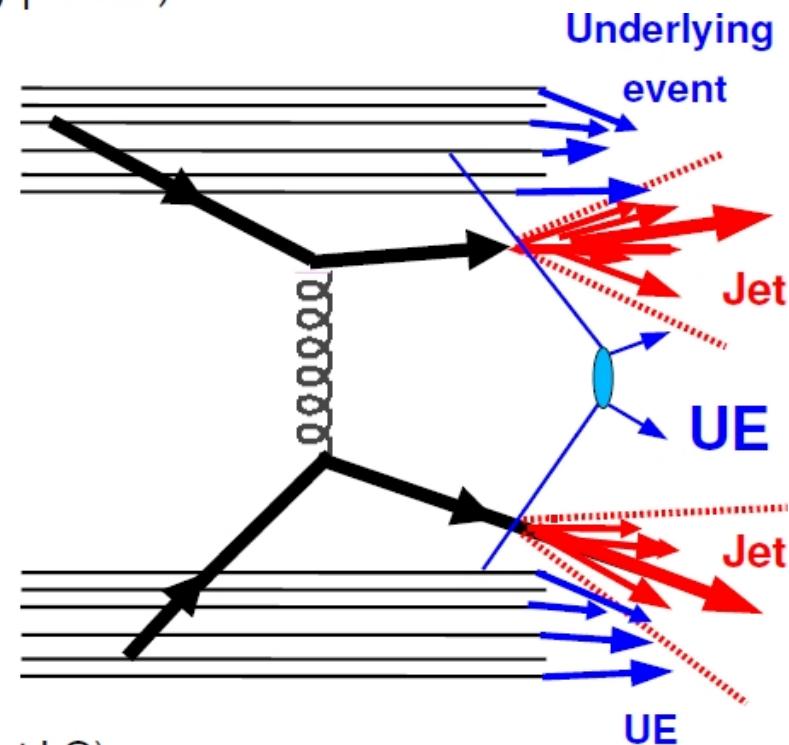
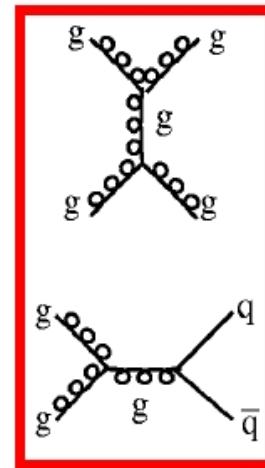
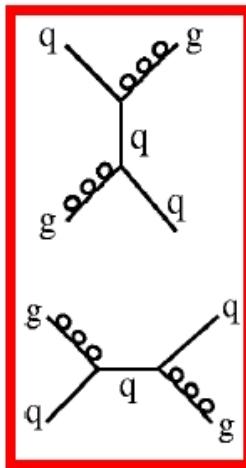
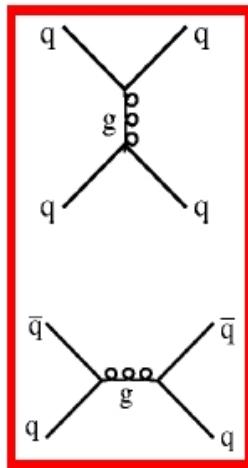


Jet **balanced back-to-back** by another jet, a prompt γ , ... (at LO).

- Jet **(real life)**: Collimated **spray of hadrons** in a cone ($R = \sqrt{\Delta\eta^2 + \Delta\phi^2} \sim 0.4\text{-}1.$) with total 4-momentum of original fragmenting parton.

Jets in hadronic collisions

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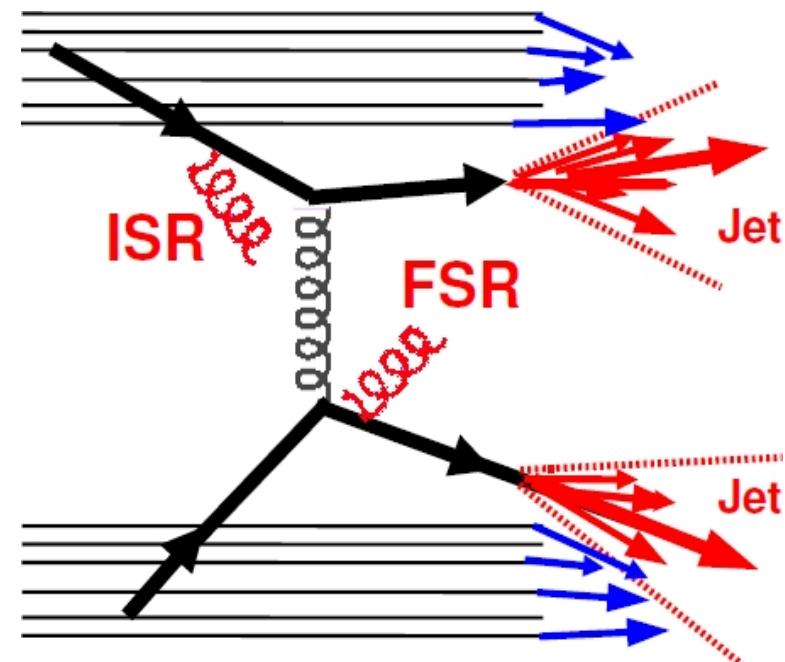
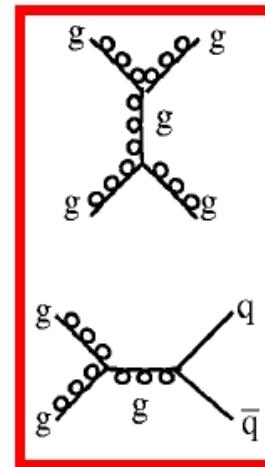
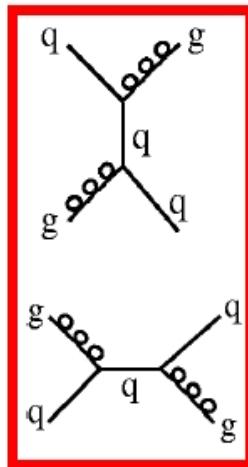
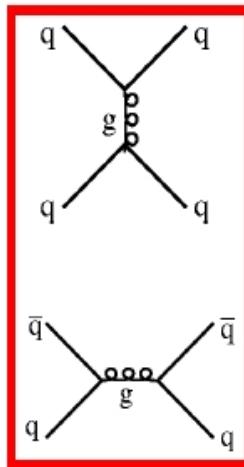


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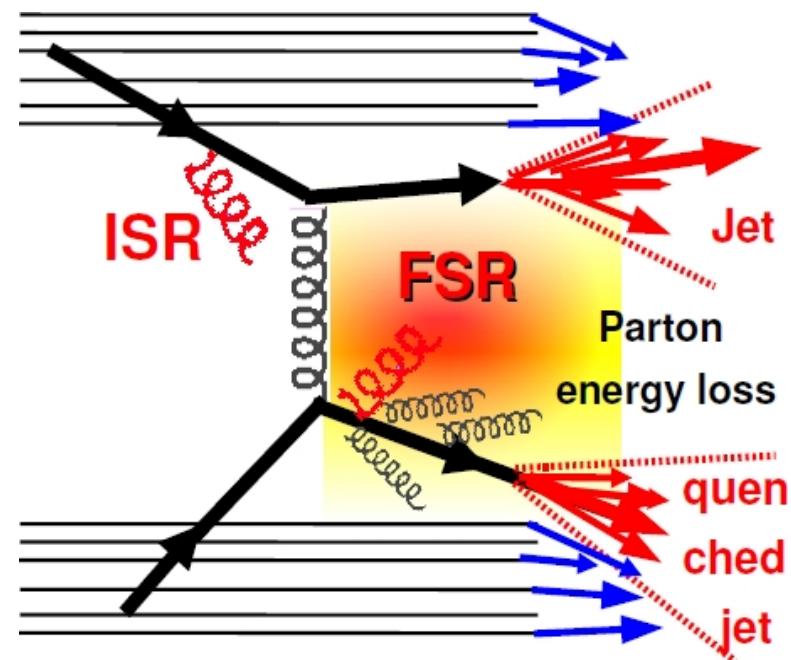
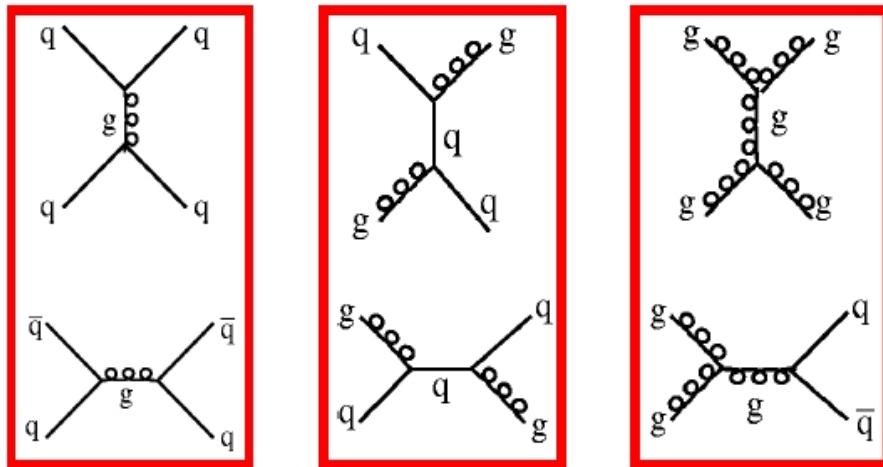


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- Jet (**real life**): Collimated **spray of hadrons** in a cone ($R = \sqrt{\Delta\eta^2 + \Delta\phi^2} \sim 0.4\text{-}1.$) with total 4-momentum of original fragmenting parton.

Jets in nuclear collisions

- Jet = high- p_T parton (quark, gluon) produced in a **hard scattering** process: $q\bar{q}$, qg , gg (or in the decay of a heavy particle)
- Jet **production processes** (leading order):



Jet **balanced back-to-back** by another jet, a prompt γ , ... (at LO).

- Jet (**real life**): Collimated **spray of hadrons** in a cone ($R = \sqrt{\Delta\eta^2 + \Delta\phi^2} \sim 0.4\text{-}1.$) with total 4-momentum of original fragmenting parton.

“Jet quenching” = tomographic QGP probe

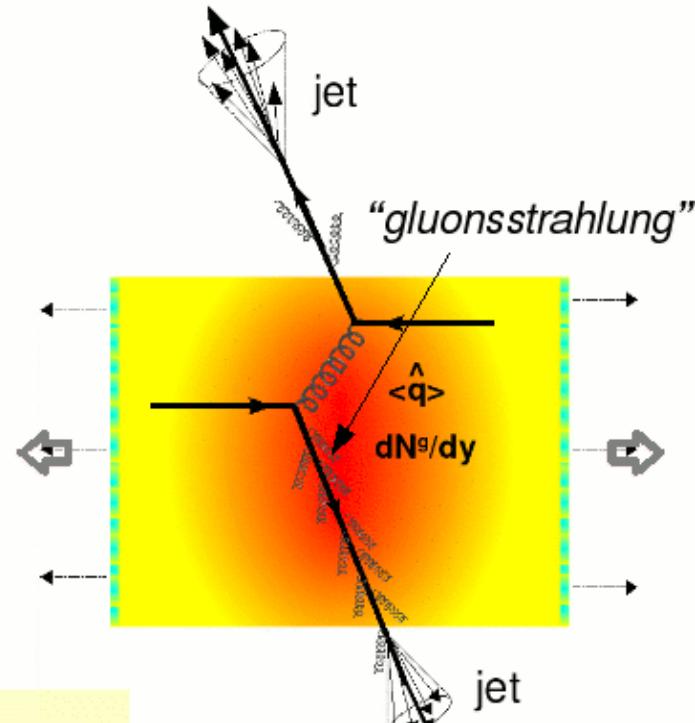
- Parton radiative energy loss: multiple gluon radiation off the produced hard parton induced by the dense QCD medium:

- Energy loss \rightarrow Medium properties:

$$\Delta E_{\text{GLV}} \propto \alpha_s^3 C_R \frac{1}{A_\perp} \frac{dN^g}{dy} L$$

$$\langle \Delta E \rangle \propto \alpha_s C_R \langle \hat{q} \rangle L^2$$

$\propto (\hat{q}, \text{gluon density}, L^{(2)})$



- \hat{q} transport coefficient:

medium “scattering power”

$$\hat{q} \equiv m_D^2 / \lambda = m_D^2 \rho \sigma$$

parton-parton x-section
medium density
Debye mass $\sim gT$

- Flavour-dependent energy loss:

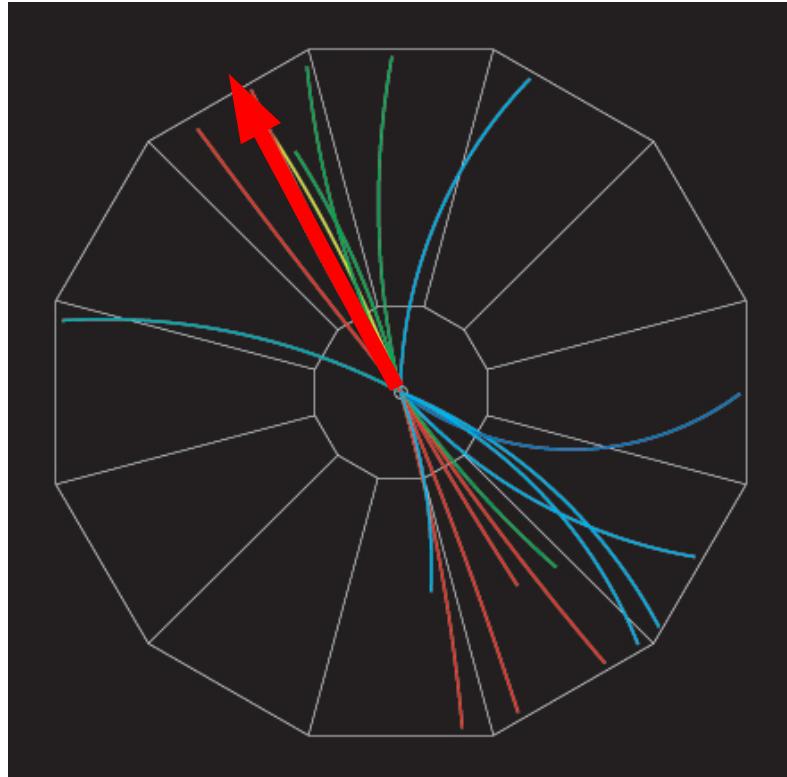
$$\Delta E_{\text{loss}}(\text{g}) > \Delta E_{\text{loss}}(\text{q}) > \Delta E_{\text{loss}}(\text{Q})$$

(color factor)

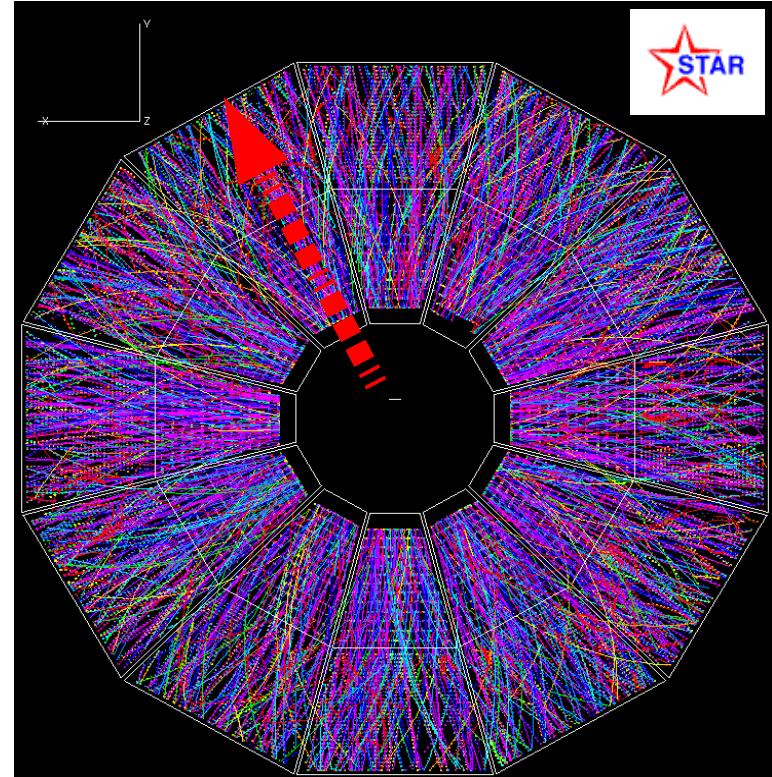
(dead-cone effect)

Jet quenching at RHIC (I): high- p_T hadrons

- Study **energy modifications** suffered by the high p_T hadrons (“**leading** **hadron** of the jet) in A-A compared to p-p:



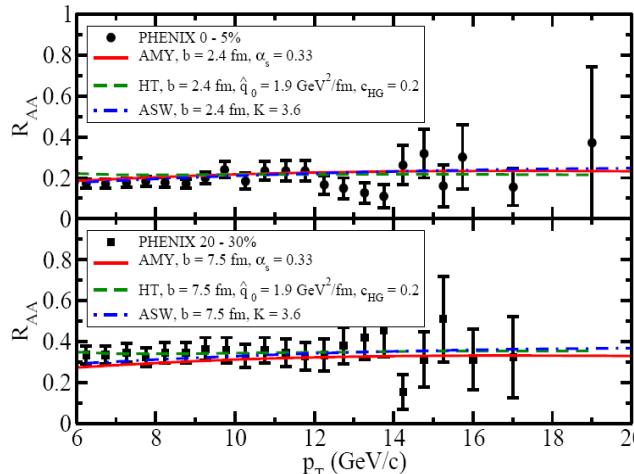
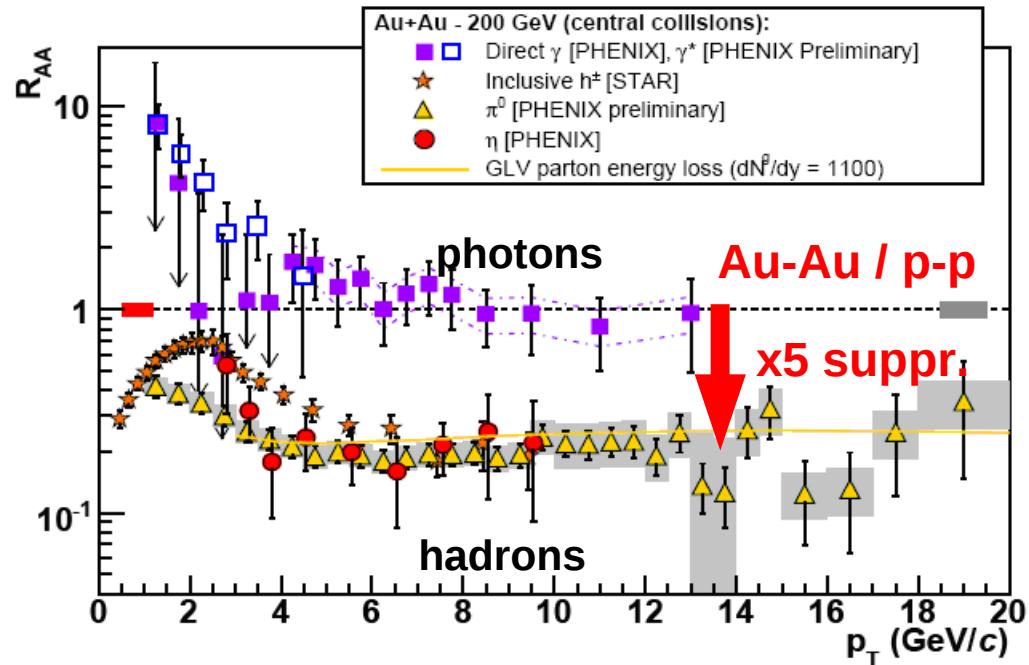
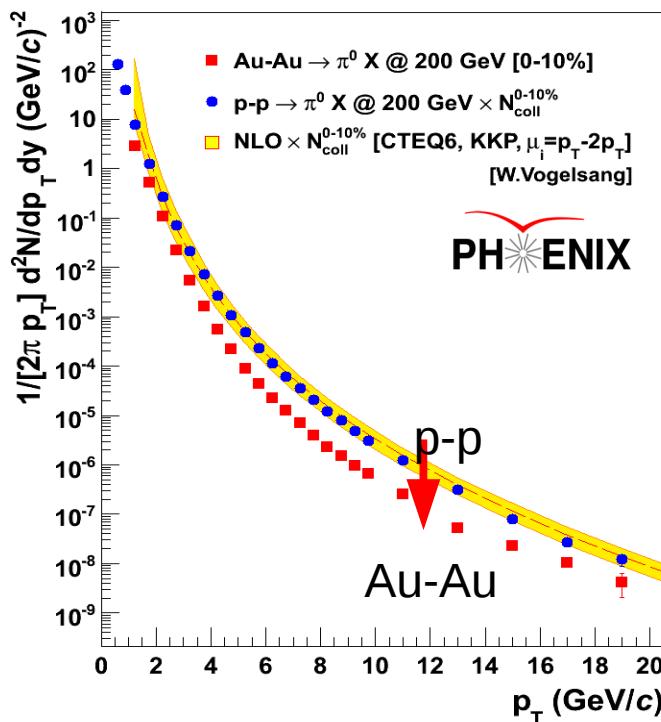
$p+p \rightarrow \text{jet+jet}$ [$\sqrt{s} = 200 \text{ GeV}$]



$\text{Au+Au} \rightarrow X$ [$\sqrt{s_{\text{NN}}} = 200 \text{ GeV}$]

Jet quenching at RHIC (II): high- p_T hadrons

- All high- p_T hadrons quenched (but not photons) !



S. Bass et al.
PRC79 (2009)024901

David d'Enterria (CERN)

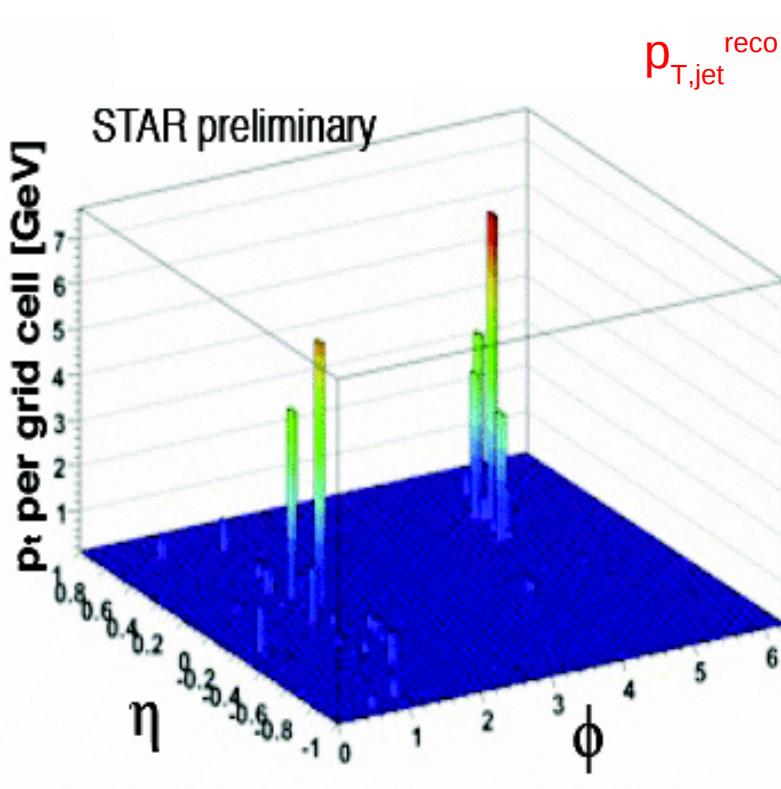
Jet quenching at RHIC (III): full jet reconstruction

- Study jet modifications (energy, shape, FFs) in A-A compared to p-p:

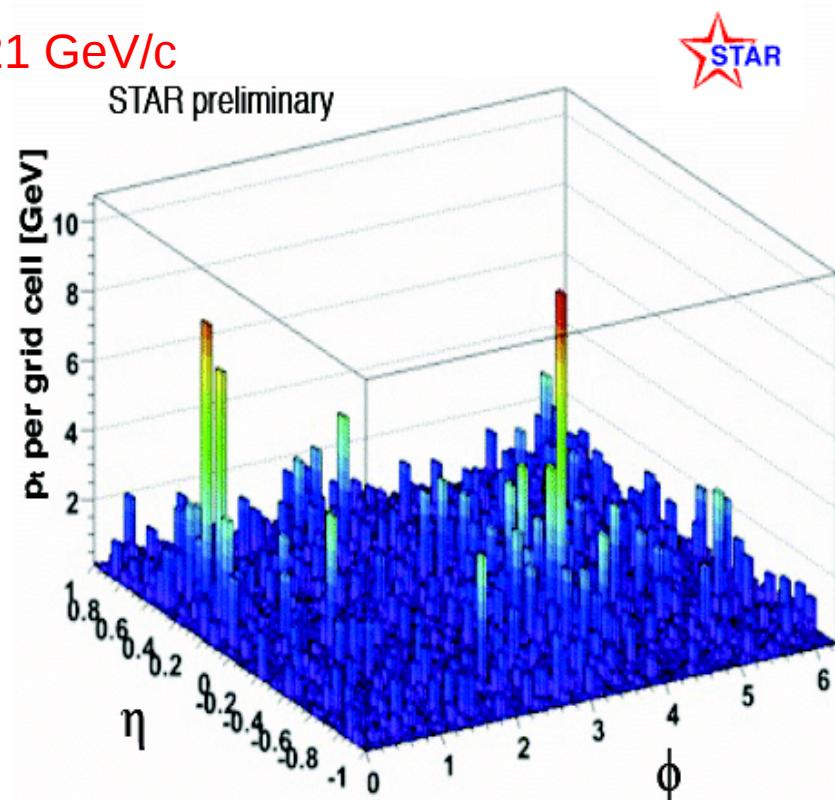
$p+p \rightarrow \text{jet+jet}$

$[\sqrt{s}_{\text{NN}} = 200 \text{ GeV}]$

$\text{Au+Au} \rightarrow \text{jet+jet}$



$p_{T,\text{jet}}^{\text{reco}} = 21 \text{ GeV/c}$

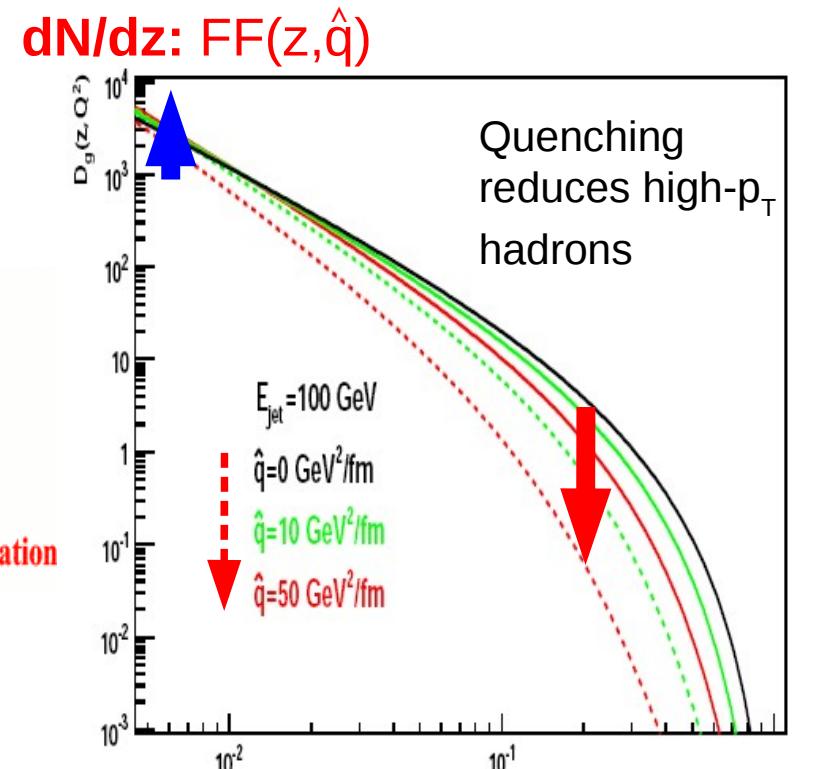
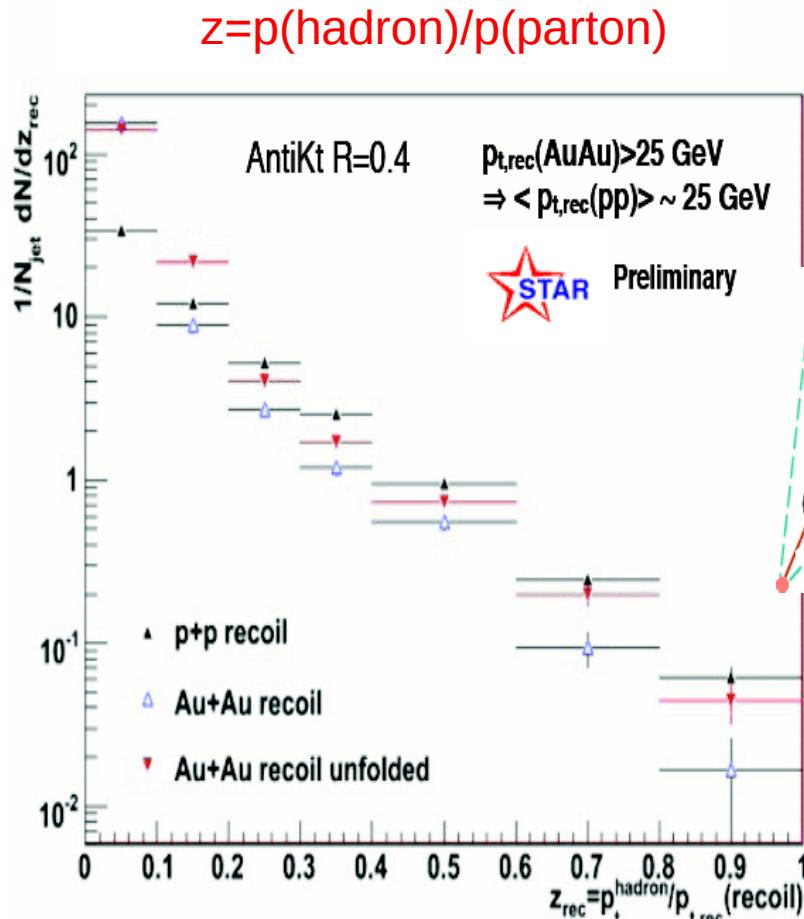


- Full jet reco complicated (but feasible): huge A-A underlying evt.:

$\langle p_T^{\text{bkg}} \rangle \sim 45 \text{ GeV}$ in $R=0.4$ cone (S/B~0.5 for a $p_T=20 \text{ GeV}$ jet)

Jet quenching at RHIC (IV): fragmentation functions

- Detailed studies of medium-modified fragmentation fcts. accessible.
- Radiative E_{loss} shifts partons from high-z to low-z: sensitive to $\langle \hat{q} \rangle$



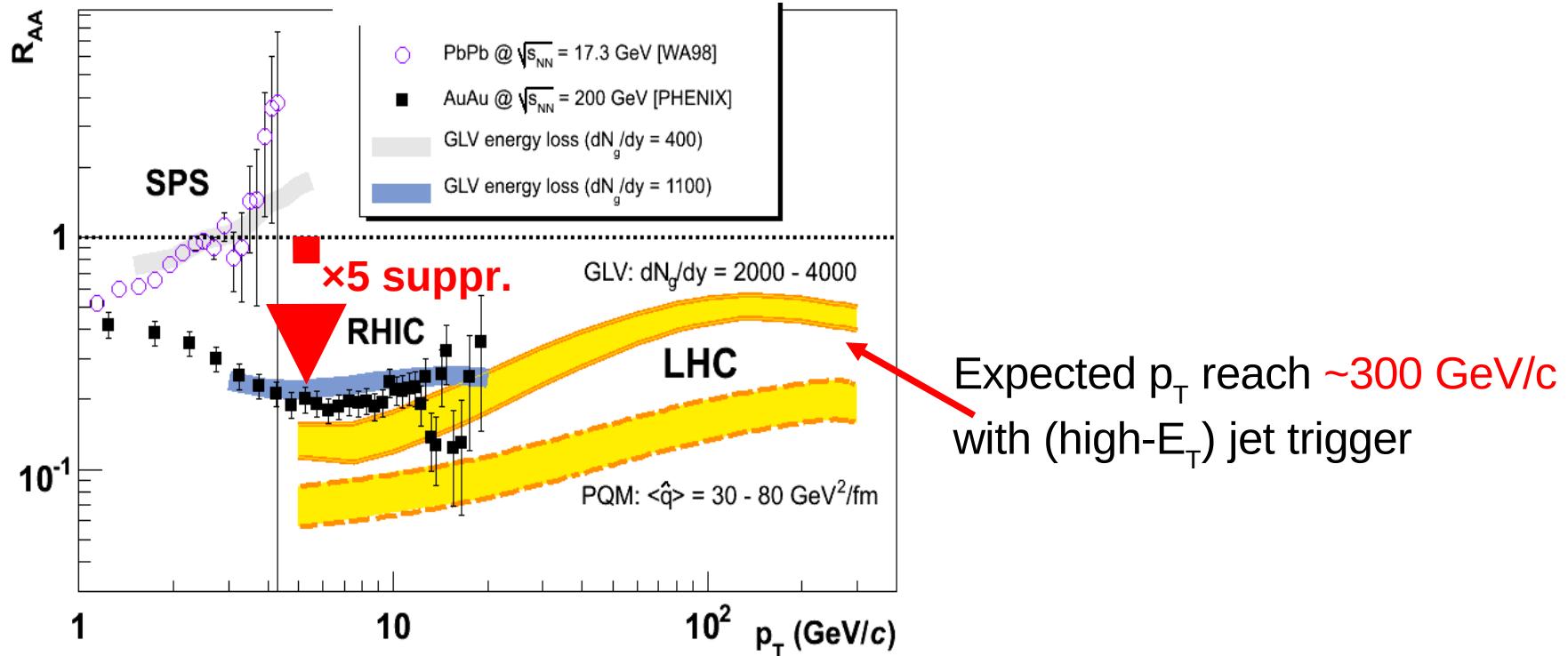
Quenching increases low-p_T hadrons

Armesto et al.
arXiv:0710.3073

Putschke, Salur, Ploskon, Bruna, QM'09

High- p_T hadron suppression (LHC)

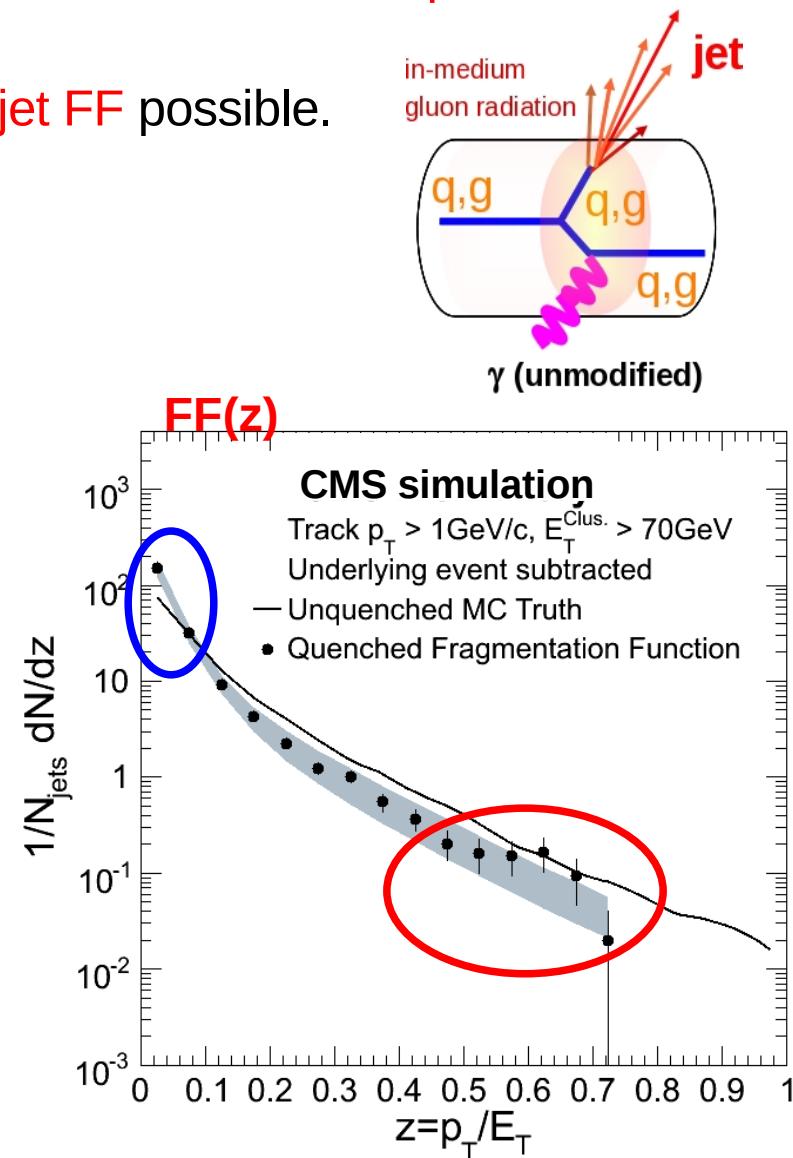
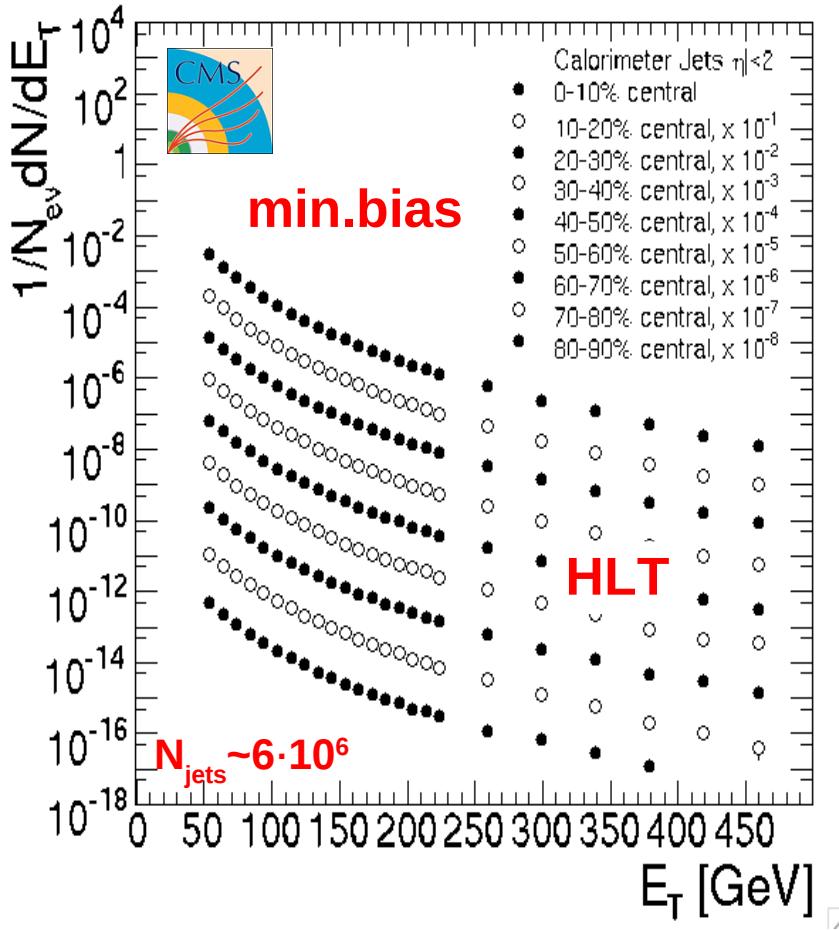
- Nuclear modification factor (= AA-yield / pp-yield) at the LHC:



- Strong **discrimination power** for parton energy loss models:
 - Initial parton medium density: $dN_g/dy \sim O(2-4 \cdot 10^3)$
 - Medium transport coefficient: $\langle \hat{q} \rangle \sim O(10-100)$ GeV 2 /fm

Jet, γ - jet reconstruction (LHC)

- Jet reconstruction, backg-subtraction & corrections: **complicated but doable**
- Jet spectra up to $E_T \sim 0.5$ TeV
- γ - jet: medium-modified (**quenched**) jet FF possible.

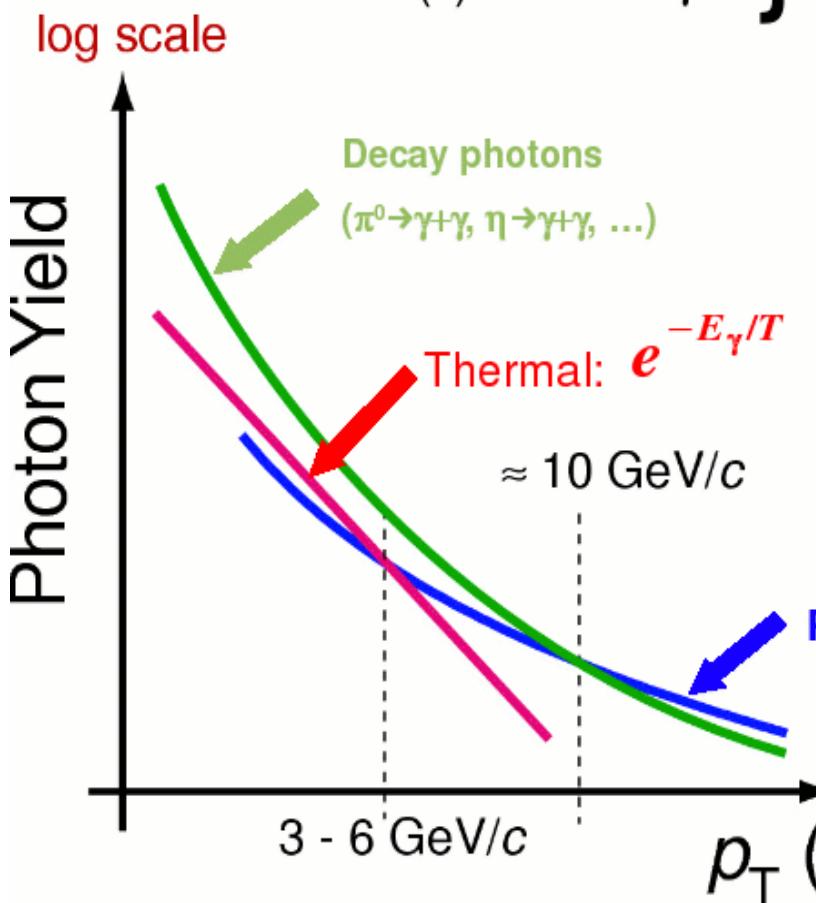
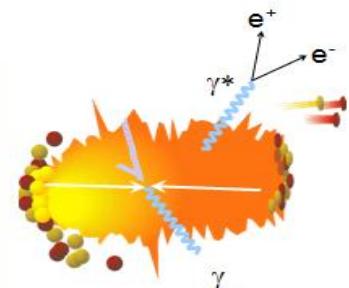


Quark-gluon matter probes (5)

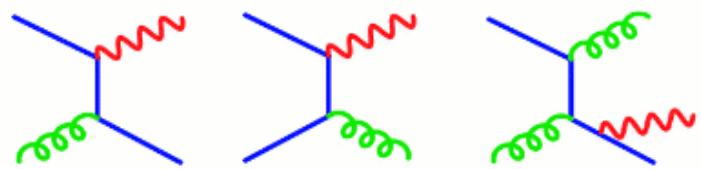
Observable (type)	Medium property	Theoretical tool
dN/dη multiplicity (soft)	gluonic struct. $xG(x, Q^2)$	Color-Glass-Condensate
dN/d p_T spectra (soft)	Equation-of-State $P(V, T)$	(Hydro), Lattice QCD
dN/d $\Delta\phi$ elliptic flow (soft)	shear viscosity η	(Hydro), AdS/CFT
Jet quenching (hard)	transport coefficient $\langle q \rangle$	(Hydro), pQCD
γ enhancement (intermed.)	critical temperature T_{crit}	(Hydro), Lattice QCD
QQ suppression (hard)	critical energy density ϵ_{crit}	(Hydro), Lattice QCD

Thermal photon radiation = QGP temperature

- Three sources: (i) Hadron decay $\gamma \rightarrow$ Background
- (ii) **Prompt** γ
- (ii) **Thermal** γ



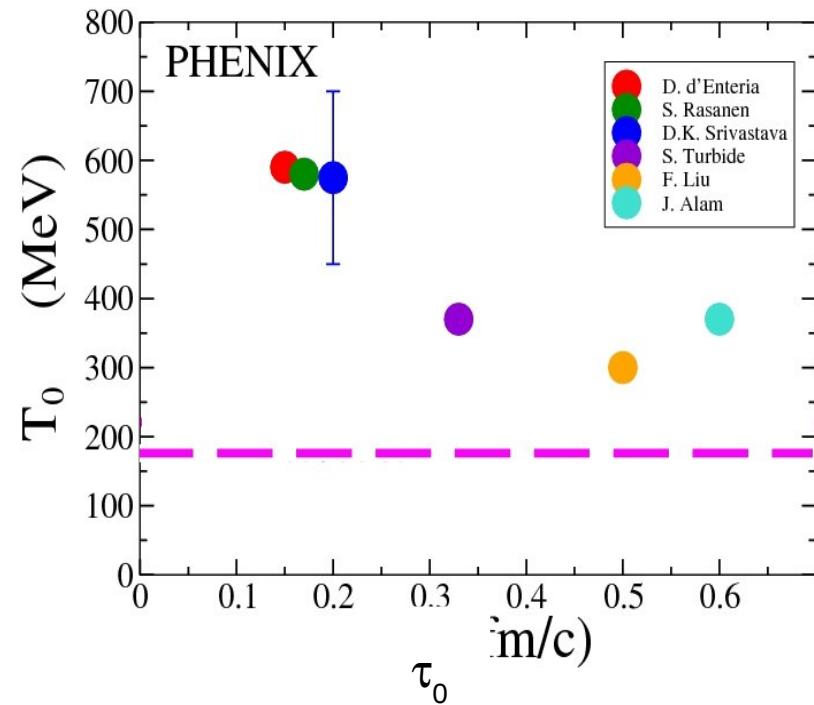
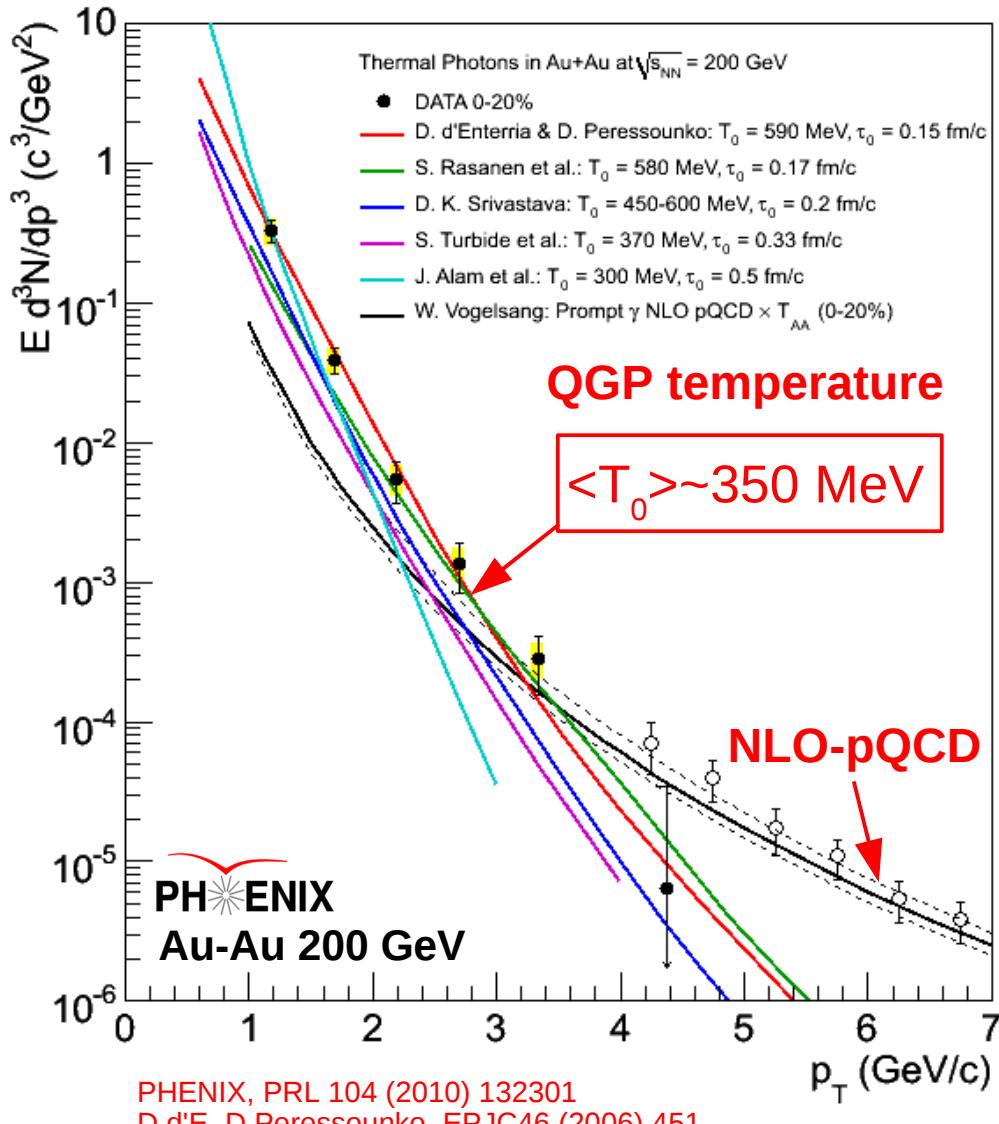
- Direct measure of the medium T
- Hydro model needed to relate expo slope to temperature.



- Initial parton-parton colls.
- Measurable in p-p.
- Computable in pQCD.

Thermal photon radiation from QGP

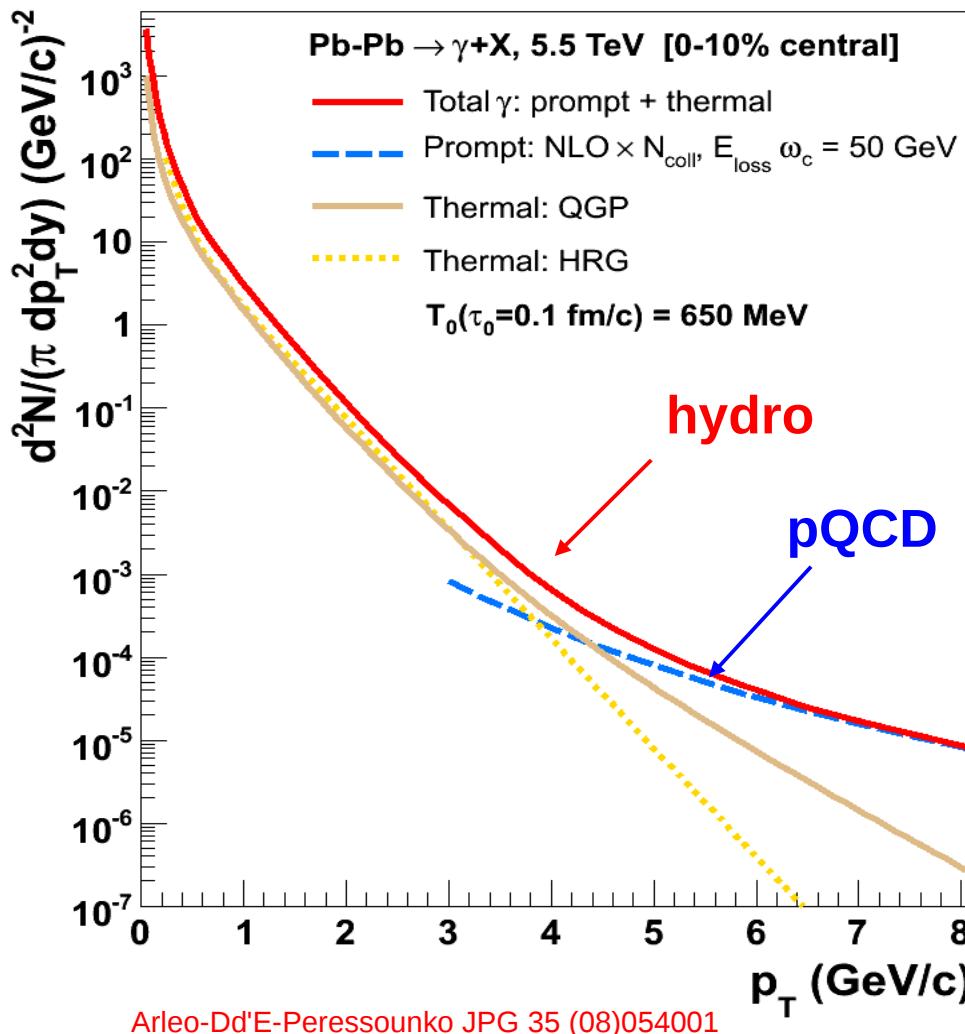
■ Hydrodynamical models vs. Au-Au γ, γ^* excess over p-p & pQCD:



■ Initial derived temperatures:
 $T_0 = 0.3-0.6$ GeV well above
 latt. QCD $T_{\text{crit}} \sim 0.17-0.19$ GeV

Thermal+Prompt photon (LHC)

- Photon spectra: hydro + NLO pQCD predictions:



Pb-Pb @ 5.5 TeV ($\langle b \rangle \sim 3 \text{ fm}$)

$$\epsilon_0 \propto S_0^{4/3} \sim 650 \text{ GeV/fm}^3$$

$$T_0 = 770 \text{ MeV} (\langle T_0 \rangle \sim 500 \text{ MeV})$$

$$\tau_0 = 0.1 \text{ fm}/c$$

- Thermal photon radiation dominates at $p_T \sim 1-5 \text{ GeV}/c$.

Quark-gluon matter probes (6)

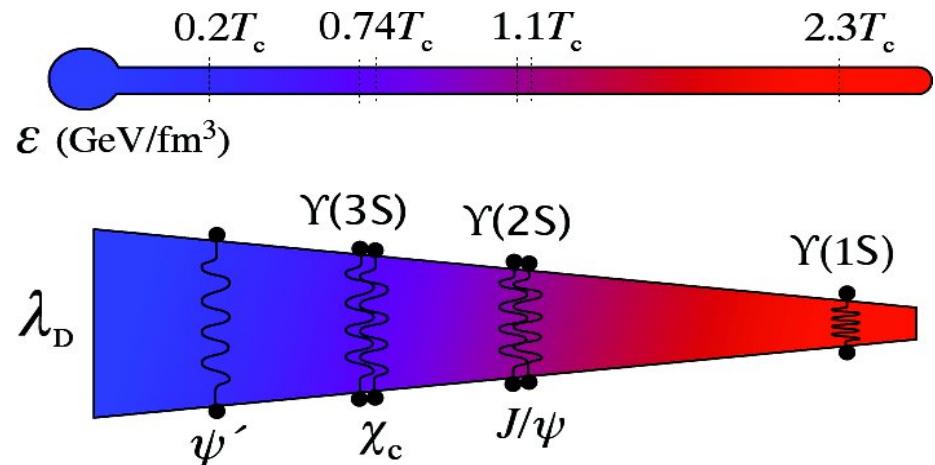
Observable (type)	Medium property	Theoretical tool
dN/dη multiplicity (soft)	gluonic struct. $xG(x, Q^2)$	Color-Glass-Condensate
dN/d p_T spectra (soft)	Equation-of-State $P(V, T)$	(Hydro), Lattice QCD
dN/d $\Delta\phi$ elliptic flow (soft)	shear viscosity η	(Hydro), AdS/CFT
Jet quenching (hard)	transport coefficient $\langle q \rangle$	(Hydro), pQCD
γ enhancement (intermed.)	critical temperature T_{crit}	(Hydro), Lattice QCD
QQ suppression (hard)	critical energy density ϵ_{crit}	(Hydro), Lattice QCD

QQbar suppression = Color screening

■ Heuristic argument [Matsui-Satz 1986]:

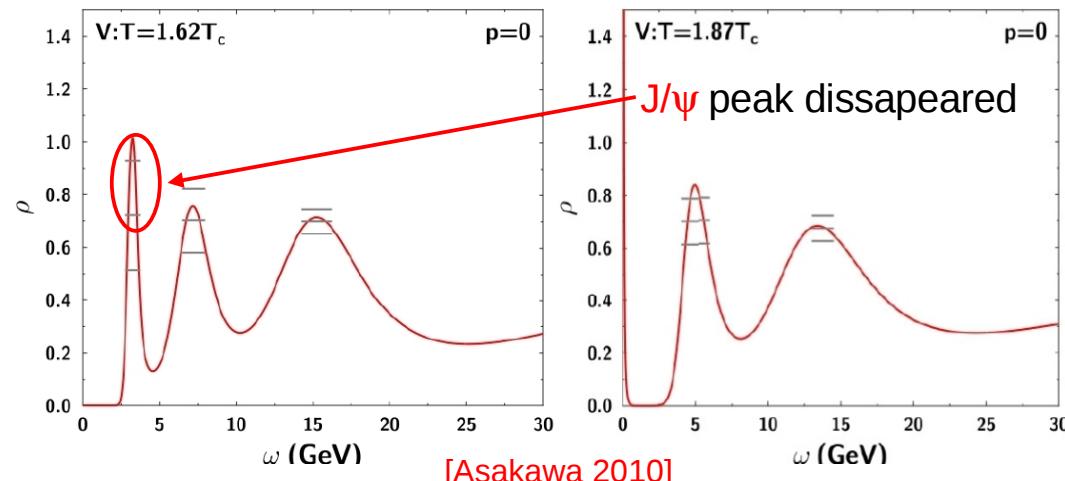
- Colour screening in a deconfined plasma dissolves QQbar.
- Different bound states “melt” at different temperatures due to their different binding radius:
QQbar: QGP “thermometer”

Screening Debye length λ_D vs. T:



■ Lattice QCD calculations (quarkonia spectral functions):

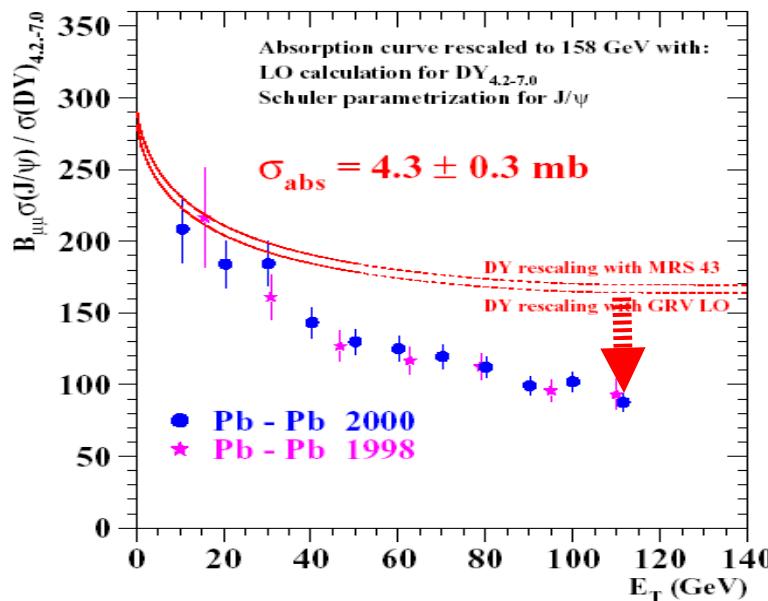
ψ' , χ_c dissolve around T_c
 J/ψ dissolves at $\sim 1.5-2T_c$
 Υ survives up to $\sim 4T_c$



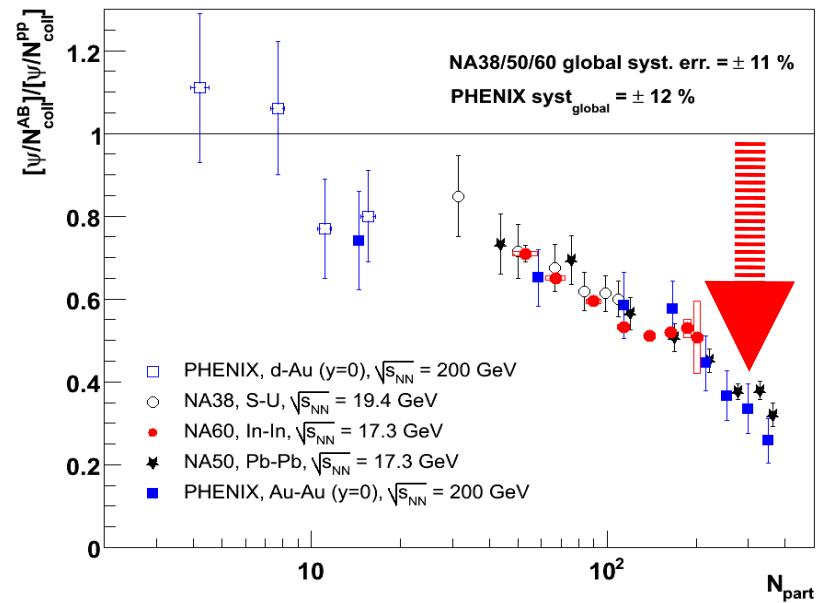
J/ψ suppression (SPS, RHIC)

- J/ψ suppression vs. collision centrality (N_{part}):

SPS: $\sqrt{s} \sim 20$ GeV



RHIC: $\sqrt{s} = 200$ GeV



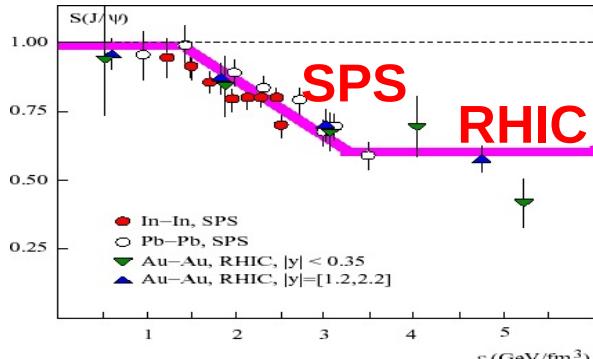
- Same suppression observed at RHIC ($T \sim 400$ MeV) & SPS ($T \sim 200$ MeV) !?

Charm recombination ? ccbar regeneration (~10 ccbar pairs in central AuAu) compensates for screening

Sequential dissociation ? Only ψ' and χ_c (~40% feed-down J/ψ) suppressed.
Direct J/ψ survives at RHIC $\Rightarrow T_0 < 2 \cdot T_c$

J/ ψ , Υ suppression (LHC)

■ J/ ψ : enhancement or suppression ?

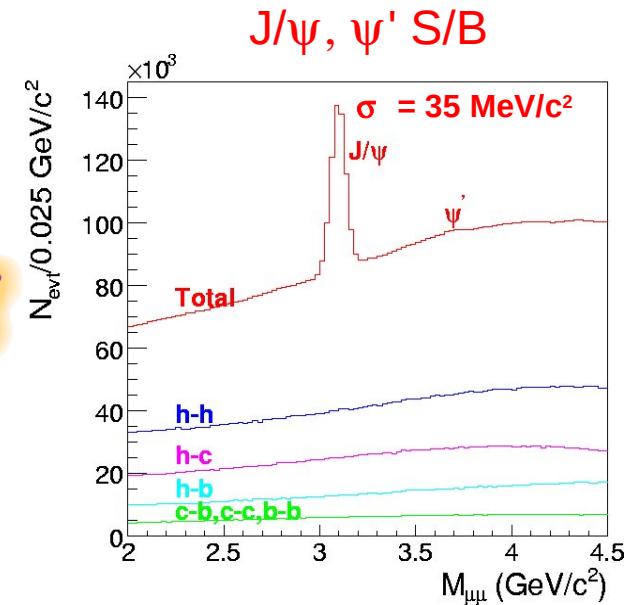


regeneration ?

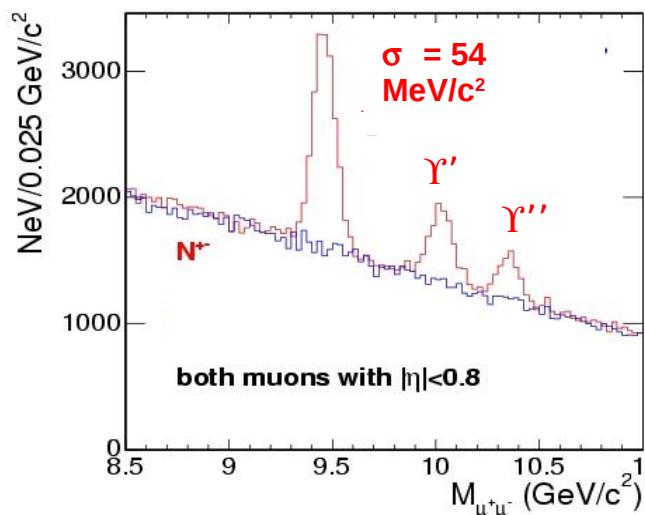
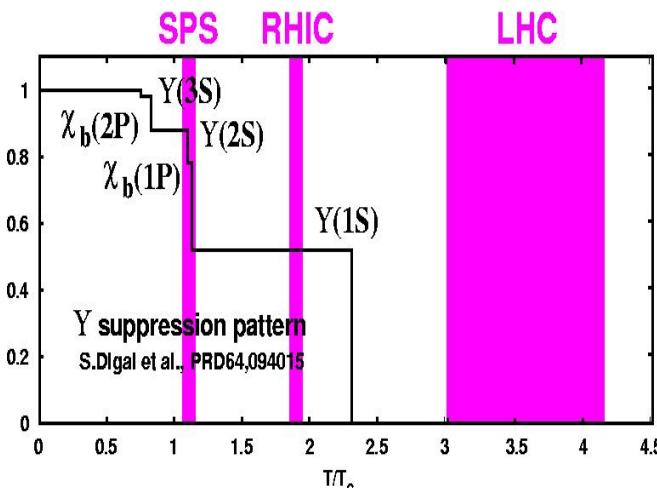
LHC

suppression ?

Energy density



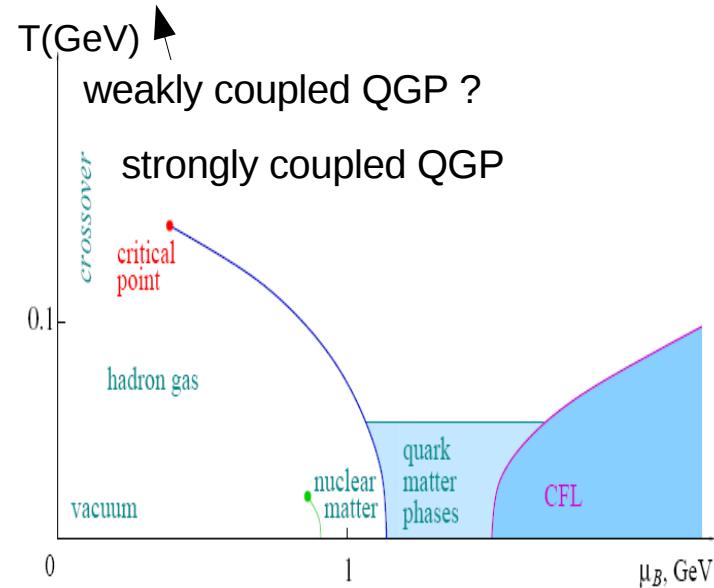
■ Bottomonia: sequential suppression ?



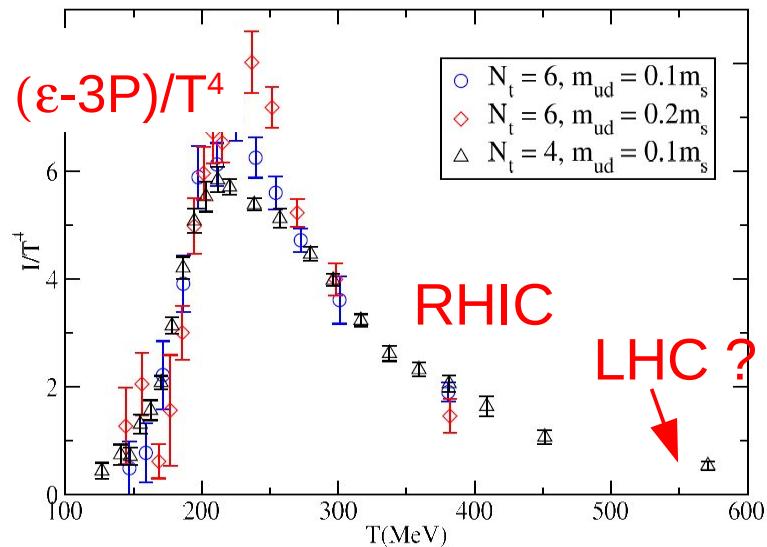
- Large stats. available:
- $O(10^5)$ J/ ψ
- $O(10^4)$ Υ

Summary

- High-energy heavy-ion collisions study
QCD in extreme conditions ($\rho, T, \text{small-}x$)
- SPS: close to phase boundary ($T_0 \sim 200$ MeV)
 J/Ψ suppressed, (ρ broadened, ...)
- RHIC: Initial-state = saturated gluon xG (CGC)
Strongly-coupled QGP (large partonic flows):
lowest viscosity/entropy $< 6/4\pi$
Very dense system ("jet quenching"):
 $dN_g/dy \sim 1000$, $\langle \hat{q} \rangle \sim 10$ GeV $^2/fm$
Hot medium (J/Ψ suppressed, thermal γ)
 $T_0 \sim 2 \cdot T_c \sim 400$ MeV
- LHC: Hottest/densest matter in the lab ever.
weakly-coupled QGP ?
stronger CGC effects ? ...



LattQCD interaction measure:



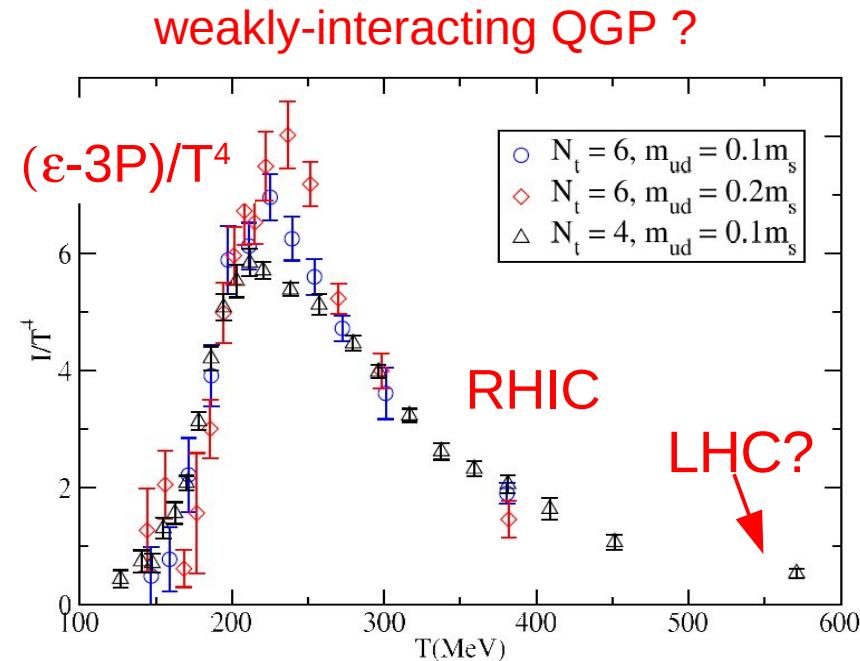
Backup slides

LHC: new frontier for QGP/CGC studies

- QGP: hotter, denser, bigger, longer-lived

	SPS	RHIC	LHC
\sqrt{s}_{NN} (GeV)	17	200	5500
dN_{ch}/dy	500	650	1500
τ^0_{QGP} (fm/c)	1	0.2	0.1
T/T_c	1.1	1.9	3.0-4.2
ϵ (GeV/fm ³)	~5	~10	~20
τ_{QGP} (fm/c)	≤ 2	2-4	≥ 10
τ_f (fm/c)	~ 10	20-30	30-40
V_f (fm ³)	few 10^3	few 10^4	few 10^5

X 28
 x 2-3
 faster
 hotter
 denser
 longer
 bigger



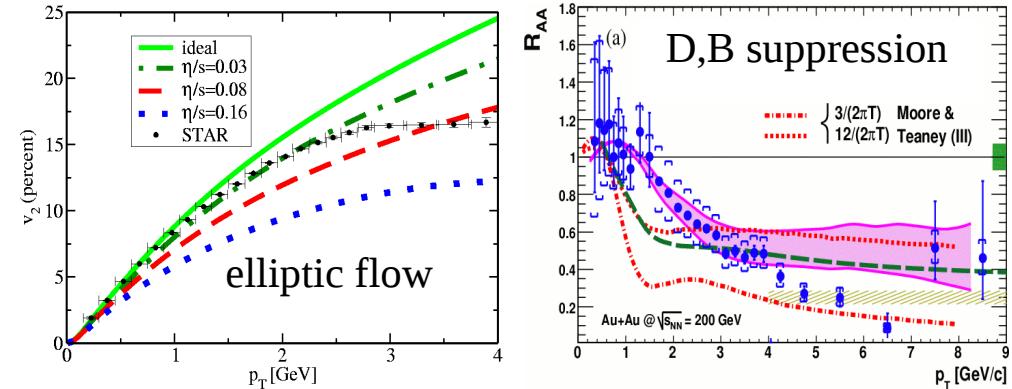
- Very large pQCD cross-sections (copious “tomographic” QGP probes).
 - Very low- $x = 2p_T/\sqrt{s} \cdot e^y \sim 10^{-4}-10^{-5}$ (30-45 times smaller than @ RHIC).
- Saturation scale (Q_s) x4 larger

AdS/CFT: QGP applications

- The Quark-Gluon-Plasma @ RHIC is “strongly coupled”:

Strong parton flows consistent w/ ideal hydro (**viscosity $\eta \sim 0$**)

Large heavy-Q (& light-q) E_{loss}
(**very opaque medium**)



- AdS/CFT gives access to **real-time (transport) QCD** quantities.
- Large **differences between QCD & SYM** “wash out” at finite-T:

- Universal shear **viscosity η** bound ($\sim \sigma_{\text{abs}}$ of soft gravitons in BH): $\eta/s > 1/4\pi$

[Kovtun&Son&Starinets, PRL94:111601,2005]

- **Quenching parameter \hat{q}** (Wilson loop from strings): $\hat{q}_{\text{SYM}} \approx 26.69 \sqrt{\alpha_{\text{SYM}} N_c} T^3$

[Liu&Rajagopal&Wiedemann, PRL97, 182301, 2006]

- **Heavy-Q diffusion coefficient D** (Wilson loop from strings): $D_{\text{SYM}} \simeq \frac{6.0}{2\pi T} \left(\frac{1.5}{\alpha_s N_{pQCD}} \right)^2$

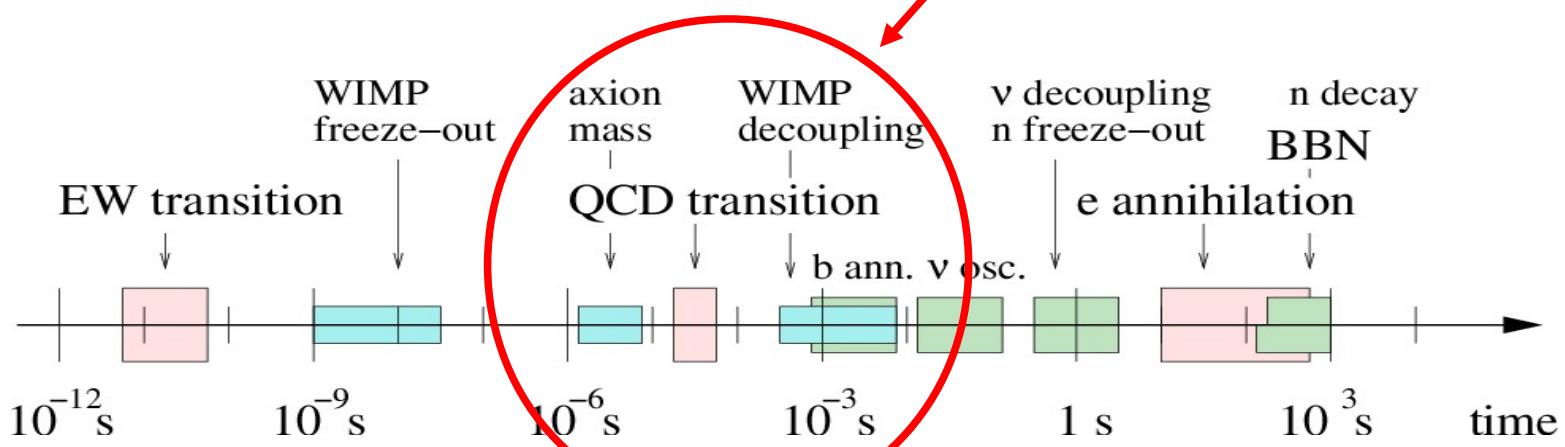
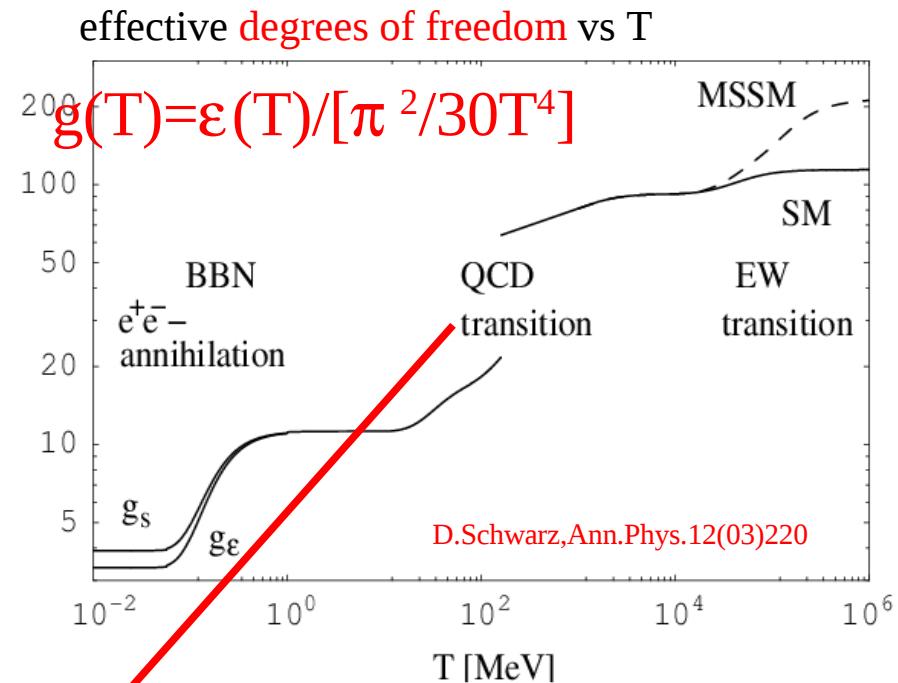
[Herzog, Gubser, Casalderrey-Solana, ...]

- **virtual/real γ emission rates** (thermal spectral functions), ...

[Kovtun, Teaney, ...]

QCD transition in the primordial Universe

- The QGP was already produced ~13.7 (-10 μ s) Gyears ago:
Most important event between EW (or SUSY) transition and Big-Bang Nucleosynthesis:
- QCD phase-transition = backgd. role for most of DM relic densities



“AdS/QGP” connection: basics

■ Anti-de-Sitter(AdS)/Conformal-Field-Theory(CFT) correspondence

Strongly-coupled gauge theories in 4-D brane (CFT in our flat space)

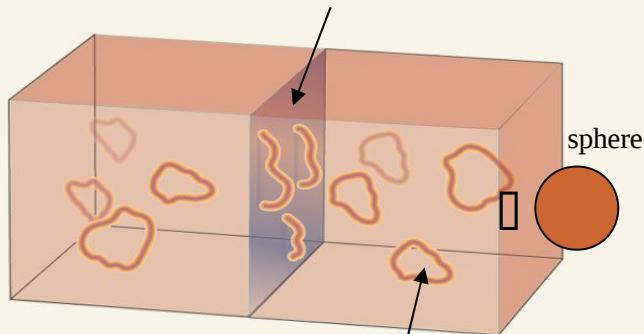
EQUIVALENT to

weakly-coupled gravity theories in 5-D neg. curved space-time (AdS)

■ Maldacena's holographic conjecture,1998:

4-D $\mathcal{N}=4$ SUSY Yang-Mills $SU(N_c)$ \Leftrightarrow IIB string theory (supergravity) in $AdS_5 \times S^5$

Gauge: fields (open strings) in 4-D brane



Dual: closed strings in 5-D $AdS_5 \times S^5$ space

Conjecture: Gauge (AdS boundary/horizon) & dual are same theory seen at diff. values of coupling (radial dir. r)

“Technicalities”:

- Gauge sector: 2 params. (g_{YM}, N_c), large 't Hooft coupling ($g_{YM}^2 N_c \gg 1$), conformal (no runn. coupling), supersymm. (gauge field, 4 Weyl fermions, 6 real scalars), $\mathcal{N}=4$ (four copies of D=4 brane)
- Gravity dual: SUGRA (supersymm. to match gauge side), fields (massless: gravitons, ...; massive string excitats.), 5 extra scalars (S^5 sphere), 2 parameters (string tension $1/\ell_s^2$, string coupling g_{st}), small curvature limit ($R/\ell_s \gg 1$, classical Einstein GR)

QCD versus N=4 SYM

	QCD	$N=4$ SYM
$T=0$	$N_c = 3 = N_f$, confinement, discrete spectrum, scattering,	N_c large, N_f/N_c small, deconfined, conformal, supersymmetric,
	very different !!	
$T > T_c$	strongly-coupled plasma of gluons & fundamental matter deconfined, screening, finite corr. lengths, . . .	strongly-coupled plasma of gluons & adjoint and fundamental matter deconfined, screening, finite corr. lengths, . . .
	very similar !!	
$T \gg T_c$	runs to weak coupling	remains strongly-coupled
	very different !!	

[from Myers and Vazquez 08]

Heavy-ion experiments @ LHC

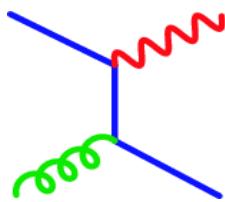


γ – jet, Z-jet (LHC)

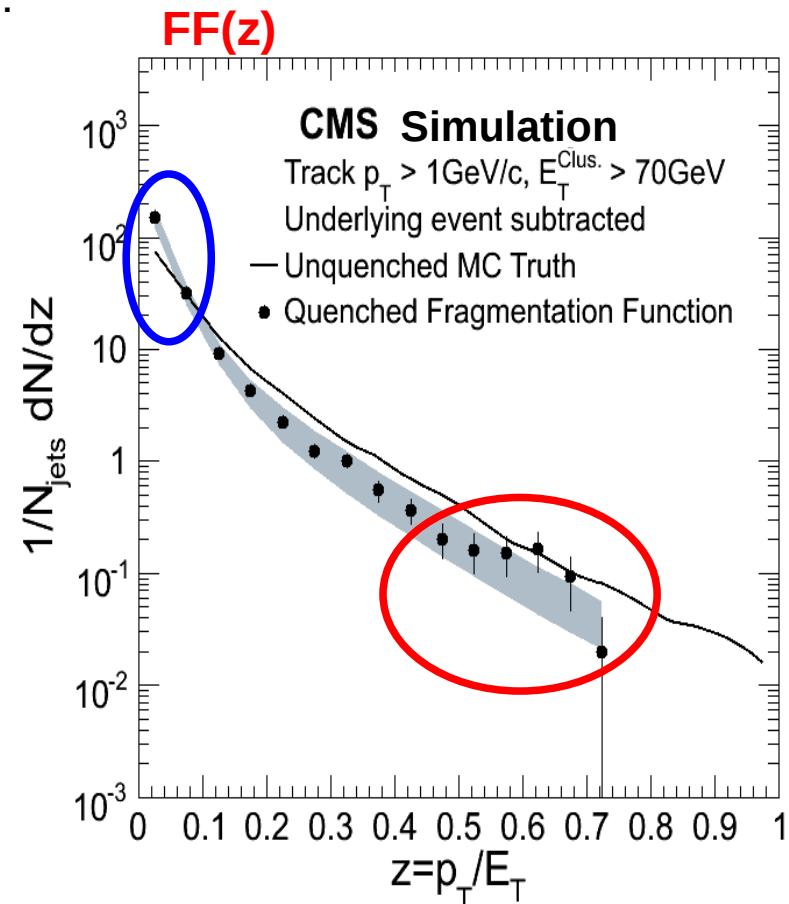
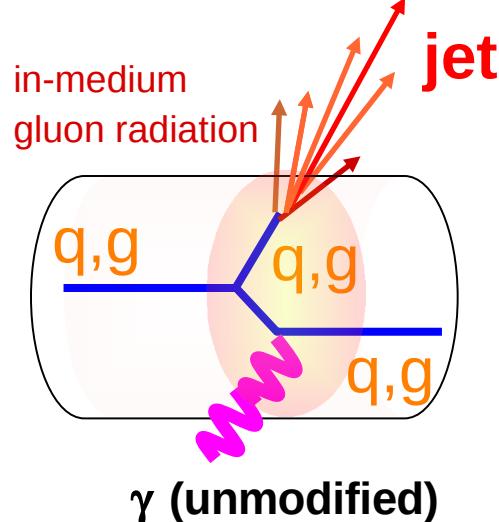
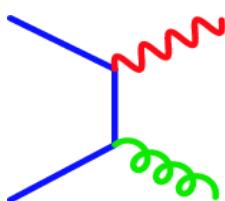
- Jet-energy loss & Frag. Functions via jet balanced with gauge bosons:

Photon-jet LO diagrams (back-to-back):

Compton



Annihilation



Pb-Pb reaction centrality

- Centrality = crucial parameter to determine PbPb collision **overlap: volume, particle/energy density** of “fireball”.
- E_{tot}, E_T in CASTOR or HF = **monotonic functions of impact parameter (b)**

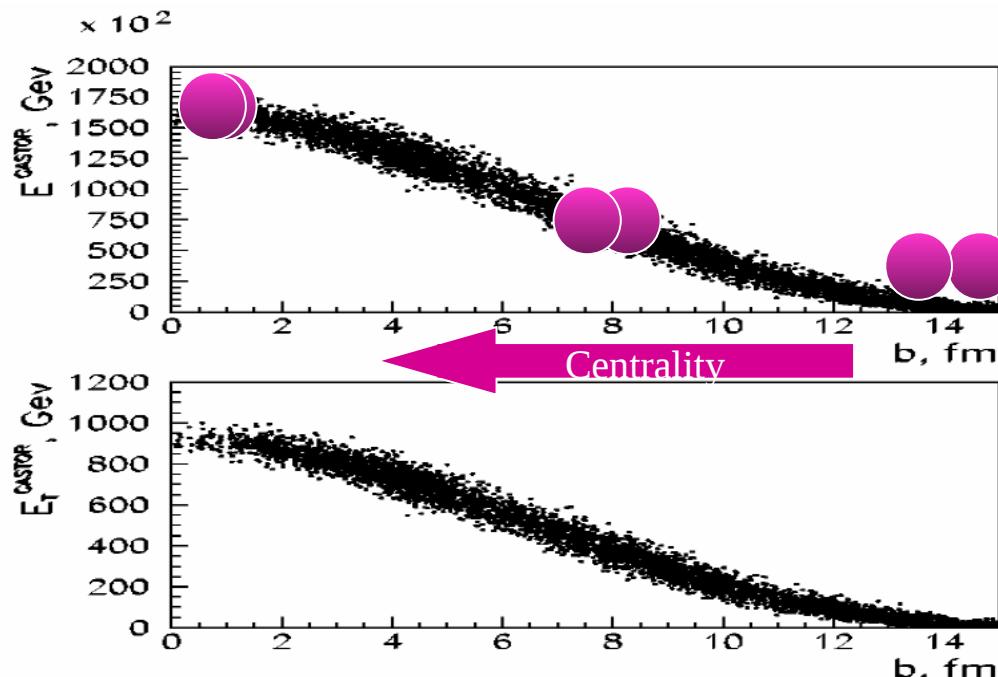
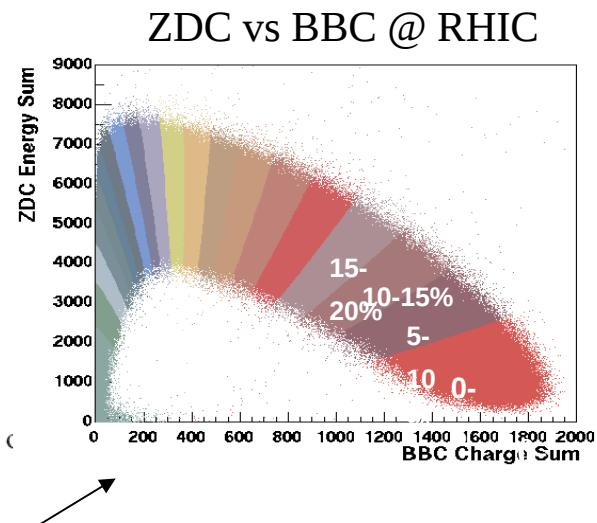


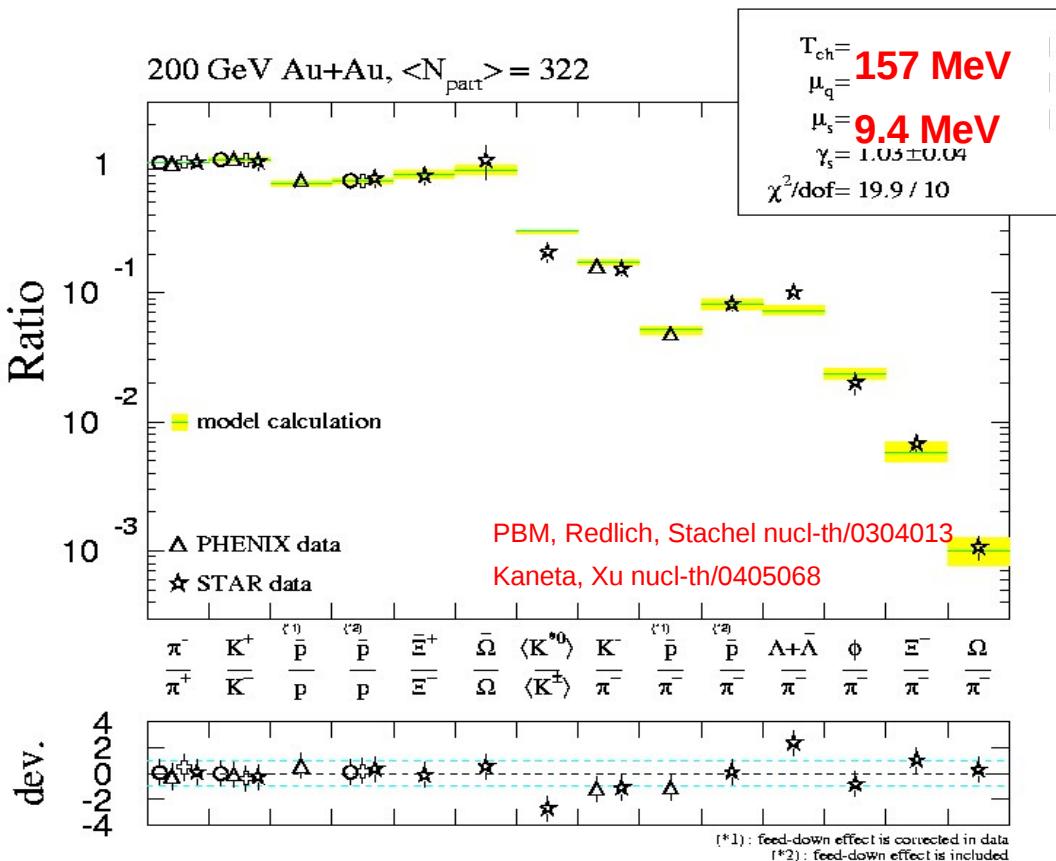
Figure 3: The distributions of energy and transverse energy deposited in CASTOR as a function of the impact parameter, b , for the highest energy Pb-Pb collisions at the LHC.



- NB: Correlation of **CASTOR E_{tot}** with **ZDC E_{tot}** will provide yet more accurate determination of the event centrality (default method at RHIC).

Ratios of particle yields

- Ratios of hadron yields consistent w/ system at **chemical equilibrium** at hadronization ($T_{\text{chem.freeze-out}} \sim T_{\text{crit}}$) :



- Hadron composition (even for strange had., $\gamma_s=1$) “fixed” at hadronization
All other hadronic yields and ratios predicted

- Assume grand canonical distrib. described by T and μ :

$$dN \sim e^{- (E - \mu)/T} d^3p$$

- 1 ratio (e.g. p/p_0) determines $\mu/T = e^{-2\mu/T}$

- 2nd ratio (e.g. K/π) provides T, μ