

Unsolved Problems in Dark Energy

a.k.a. Everything



Wayne Hu
Benasque, February 2011

Said the great Spanish physicist **Raul Jimenez** (in Americanized paraphrase):

“Better **Lame** than **Late**”

– circa 24 hrs ago

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“Better **Lame** than **Late**”

– circa 24 hrs ago

or the **A**delayed **S**ession = **C**ut the **F*****ing **T**ime correspondence

Prolific Participants: $p+\bar{p} \rightarrow ?$ Hitoshi says 2 in billion survive!

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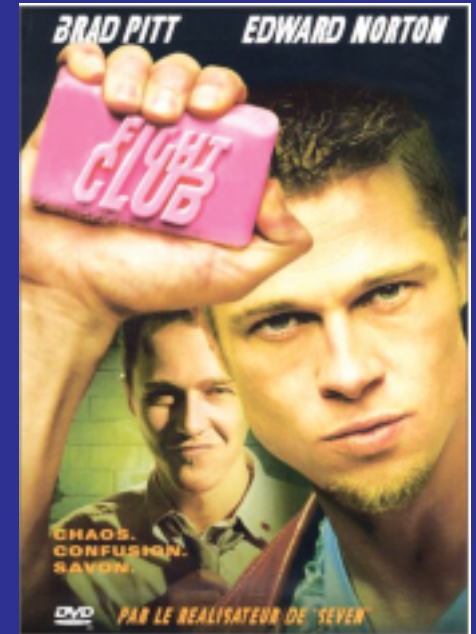
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Observational to Do List

- Just 3 things (from a theorist's perspective)
 1. Falsify (flat) Λ CDM
 2. Falsify (flat) Λ CDM
 3. Falsify (flat) Λ CDM



How to Falsify

Test the **consistency** of Λ CDM in **parameter space**

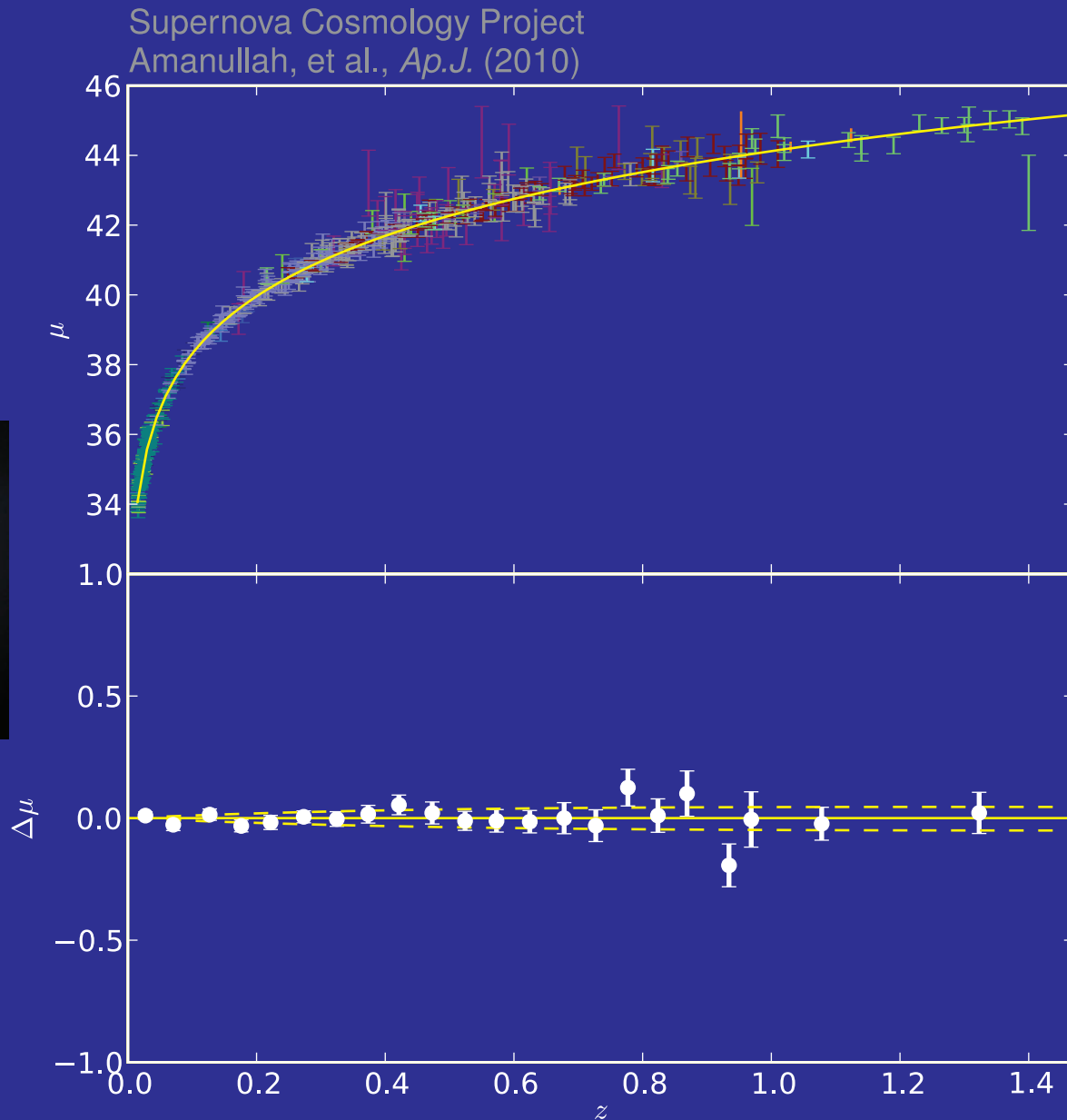
- Expand **parameter space** or take **alternate models**
- MCMC set of parameters, find **evidence** for **tension** with Λ CDM
- Good - well defined, optimal if **models well motivated**
- Bad - there are **no well motivated alternatives** to Λ (cf. Sundrum's IQ Test)
- **FOM** (aka FML) and other elements of the Dark Energy Canon (Andrew Liddle and the New Bayesian Testament)

Test **consistency** in **observable space**

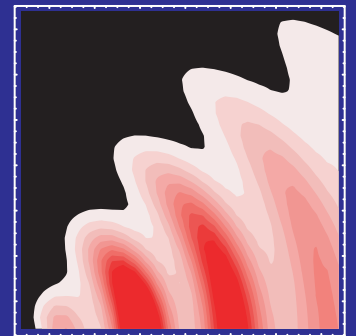
- MCMC in Λ CDM (or other complete paradigm like quintessence) and predict posteriors of **new observables**
- Good - theory says what **best to observe** to falsify Λ CDM
- Bad - **falsify in favor of what?**

Falsifying Λ CDM

- Geometric measures of distance redshift from SN, CMB, BAO



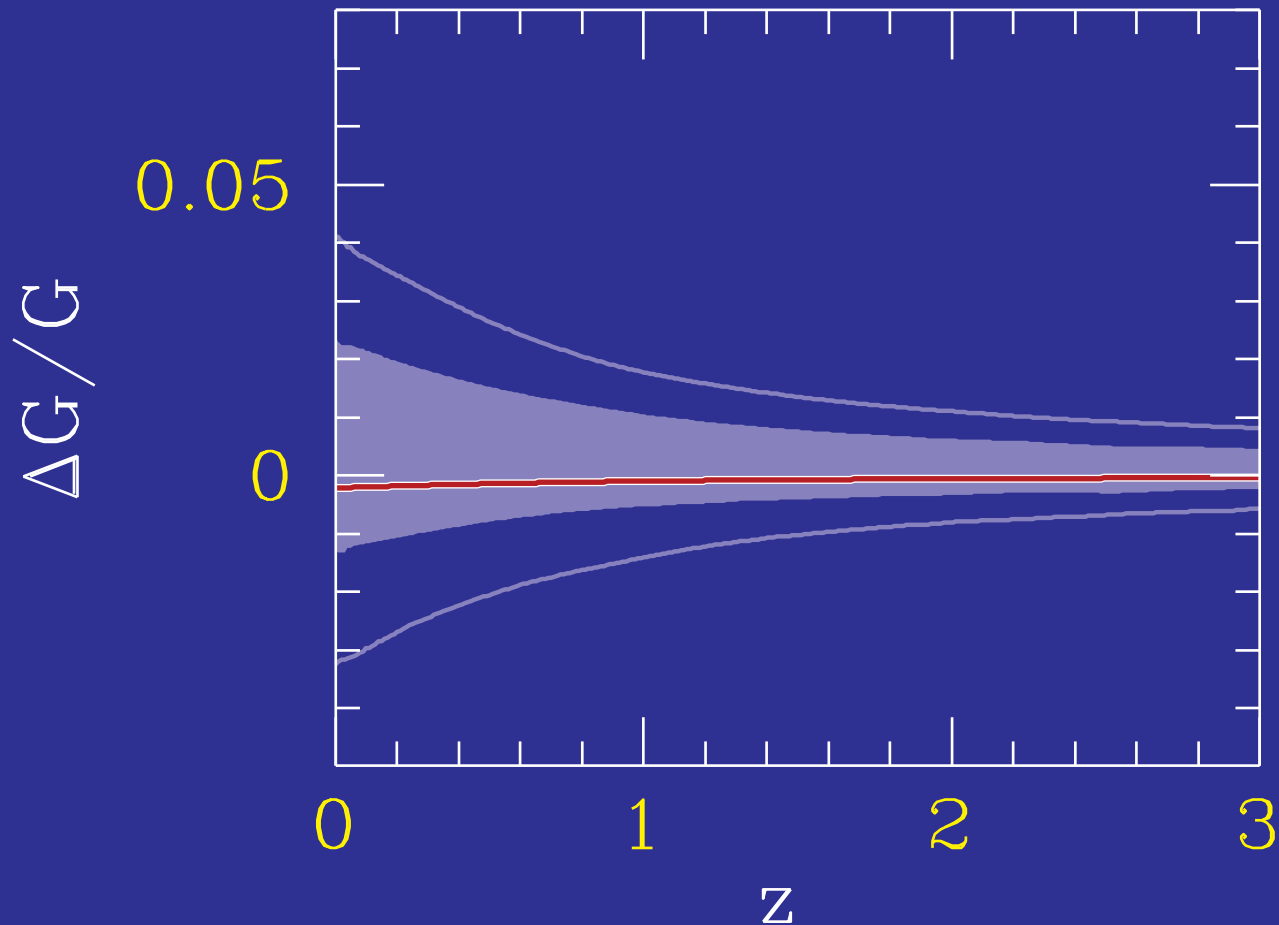
Standard(izable)
Candle
Supernovae
Luminosity ν Flux



Standard Ruler
Sound Horizon
 ν CMB, BAO angular
and redshift separation

Falsifying Λ CDM

- Λ slows growth of structure in highly predictive way



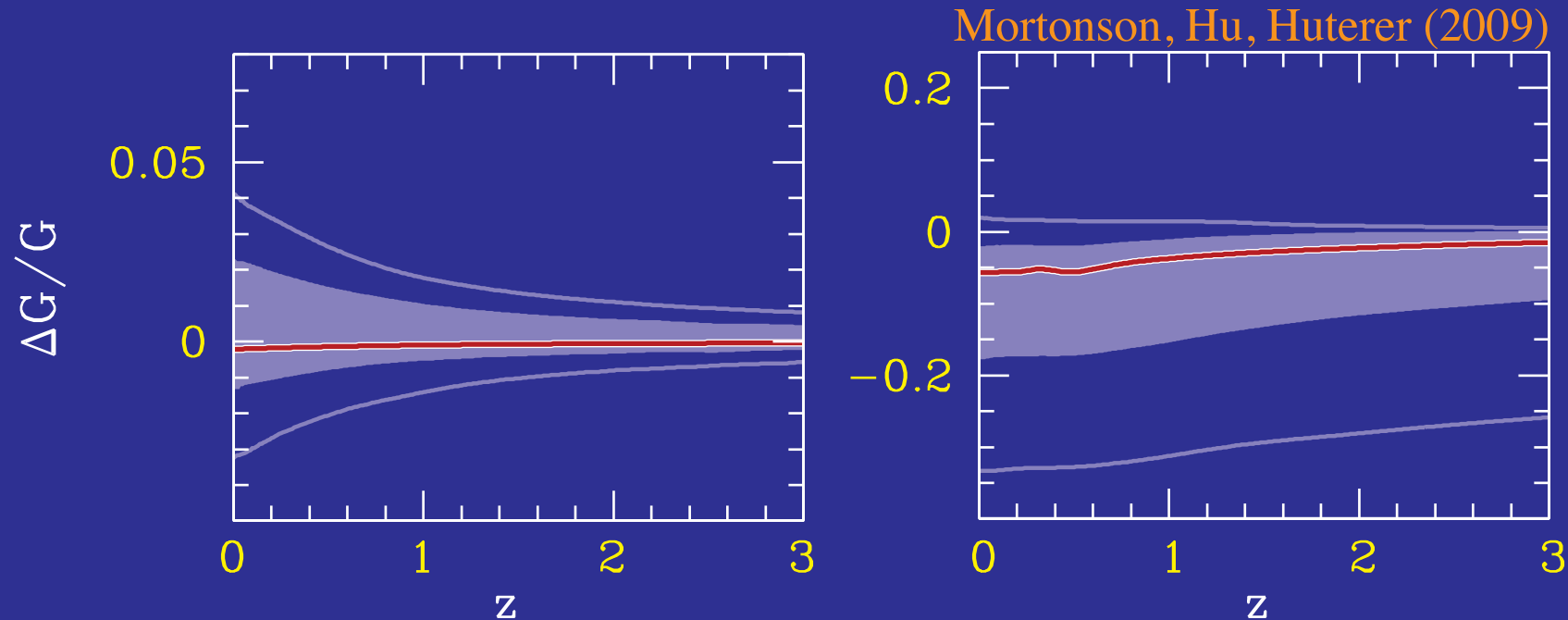
Cosmological Constant

Falsifiability of Smooth Dark Energy

- With the smoothness assumption, dark energy only affects gravitational growth of structure through changing the expansion rate
- Hence geometric measurements of the expansion rate predict the growth of structure
 - Hubble Constant
 - Supernovae
 - Baryon Acoustic Oscillations
- Growth of structure measurements can therefore falsify the whole smooth dark energy paradigm
 - Cluster Abundance
 - Weak Lensing
 - Velocity Field (Redshift Space Distortion)

Falsifying Quintessence

- Dark energy slows growth of structure in highly predictive way



Cosmological Constant

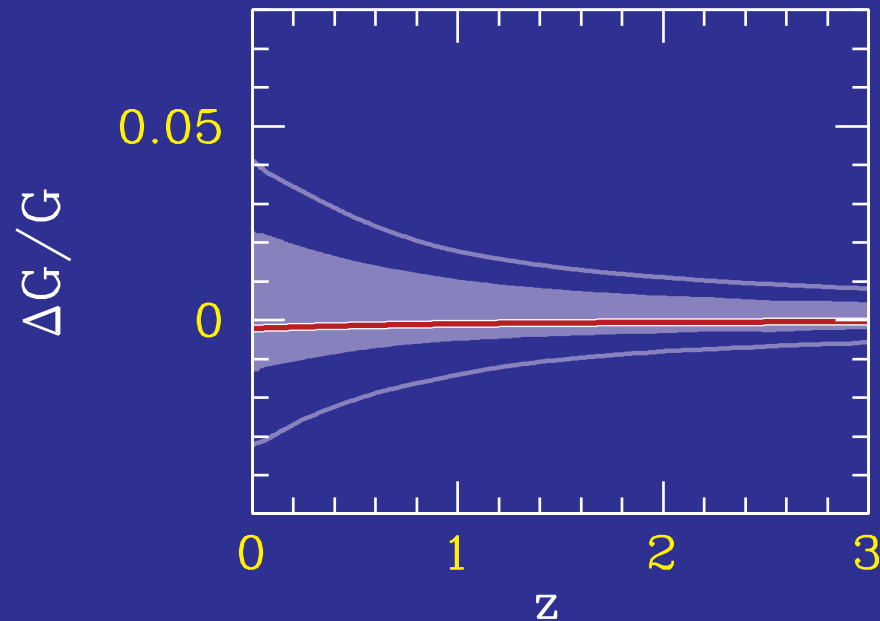
Quintessence

- Deviation significantly $>2\%$ rules out Λ with or without curvature
- Excess $>2\%$ rules out quintessence with or without curvature and early dark energy [as does $>2\%$ excess in H_0]

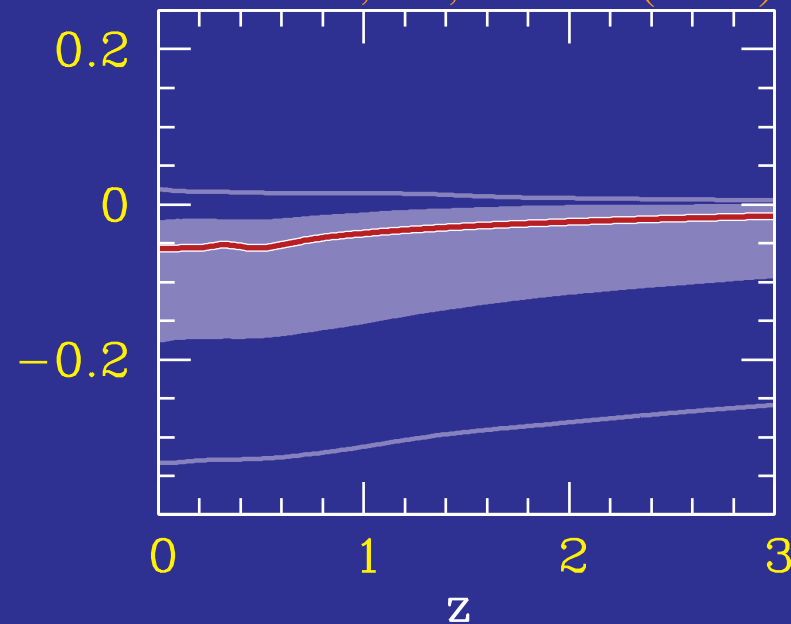
Dynamical Tests of Acceleration

- Dark energy slows growth of structure in highly predictive way

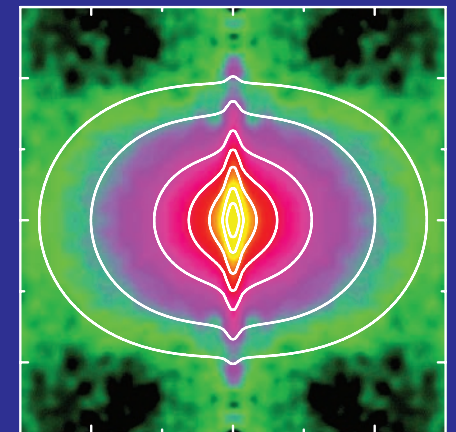
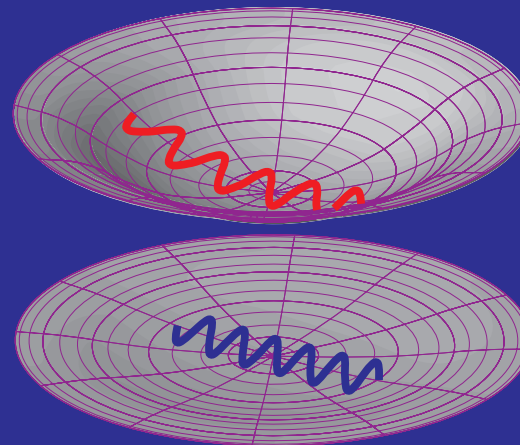
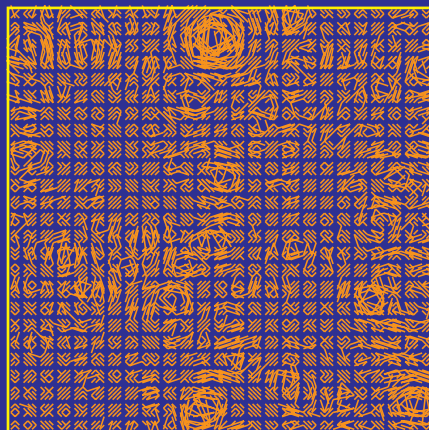
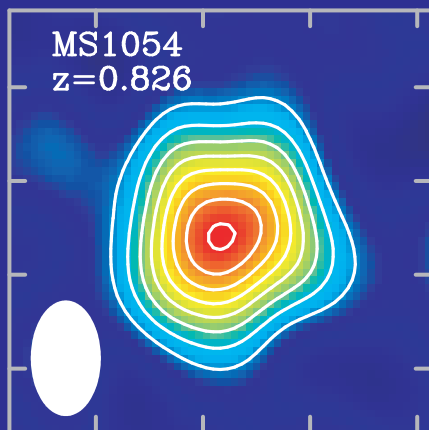
Mortonson, Hu, Huterer (2009)



Cosmological Constant

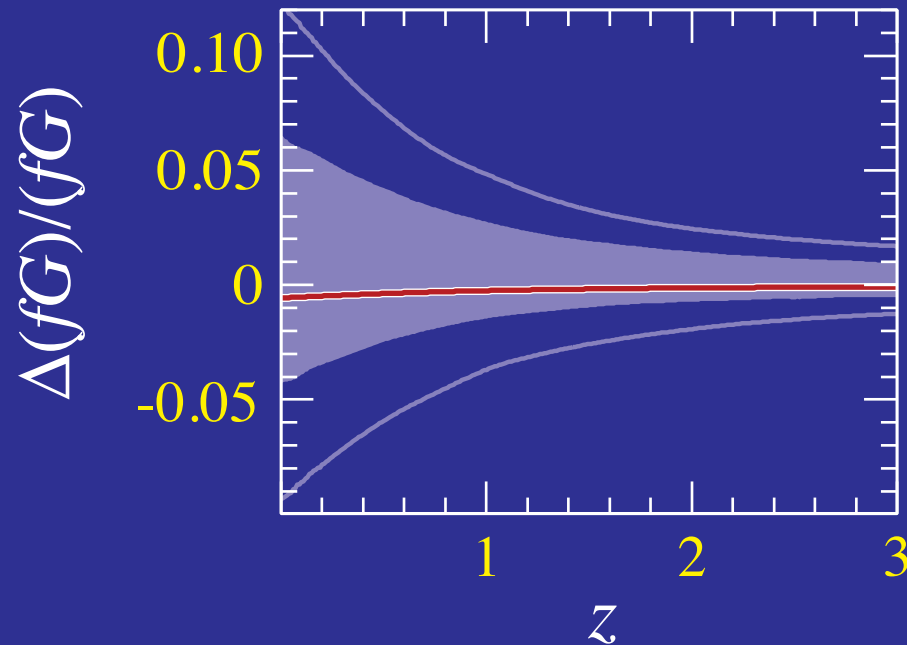


Quintessence

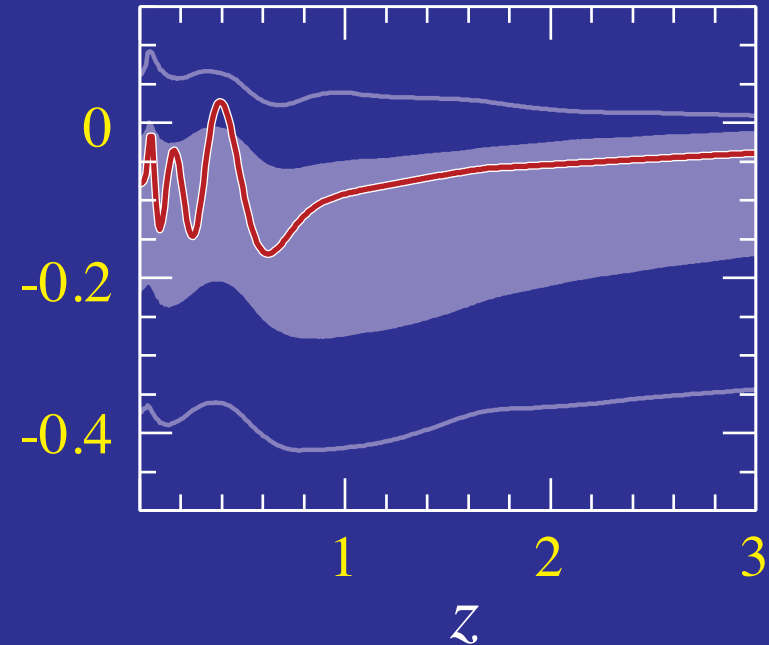


Redshift Space Distortion

- Redshift space distortions measure fG or $f\sigma_8$
- Measurements in excess of $\sim 5\%$ of Λ CDM would rule out quintessence



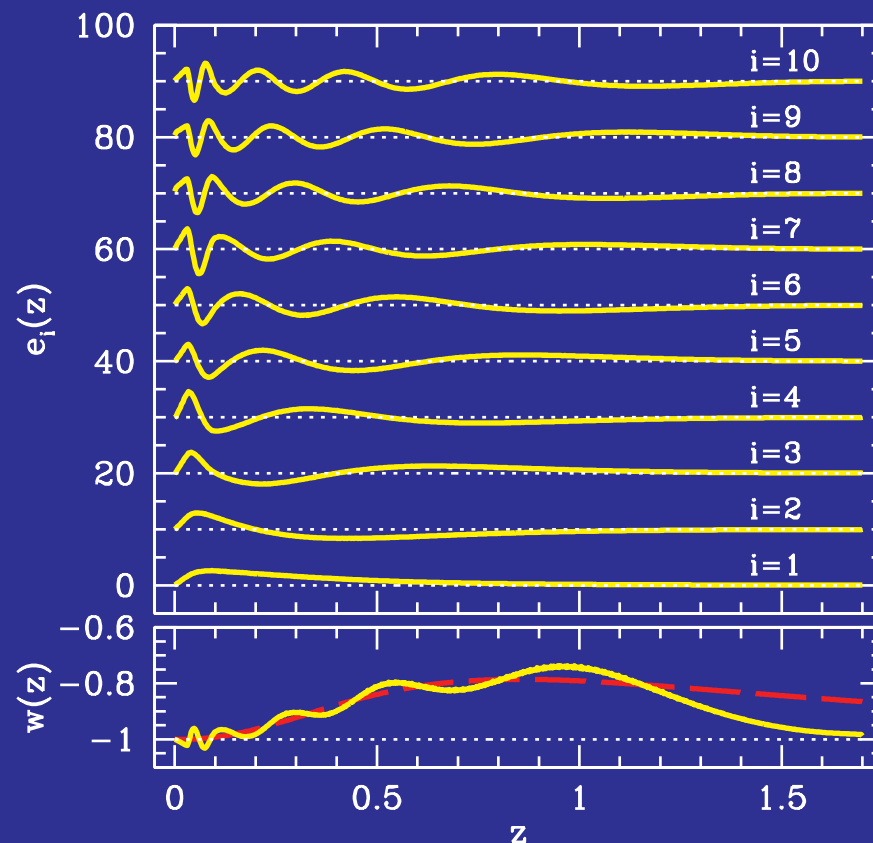
Cosmological Constant



Quintessence

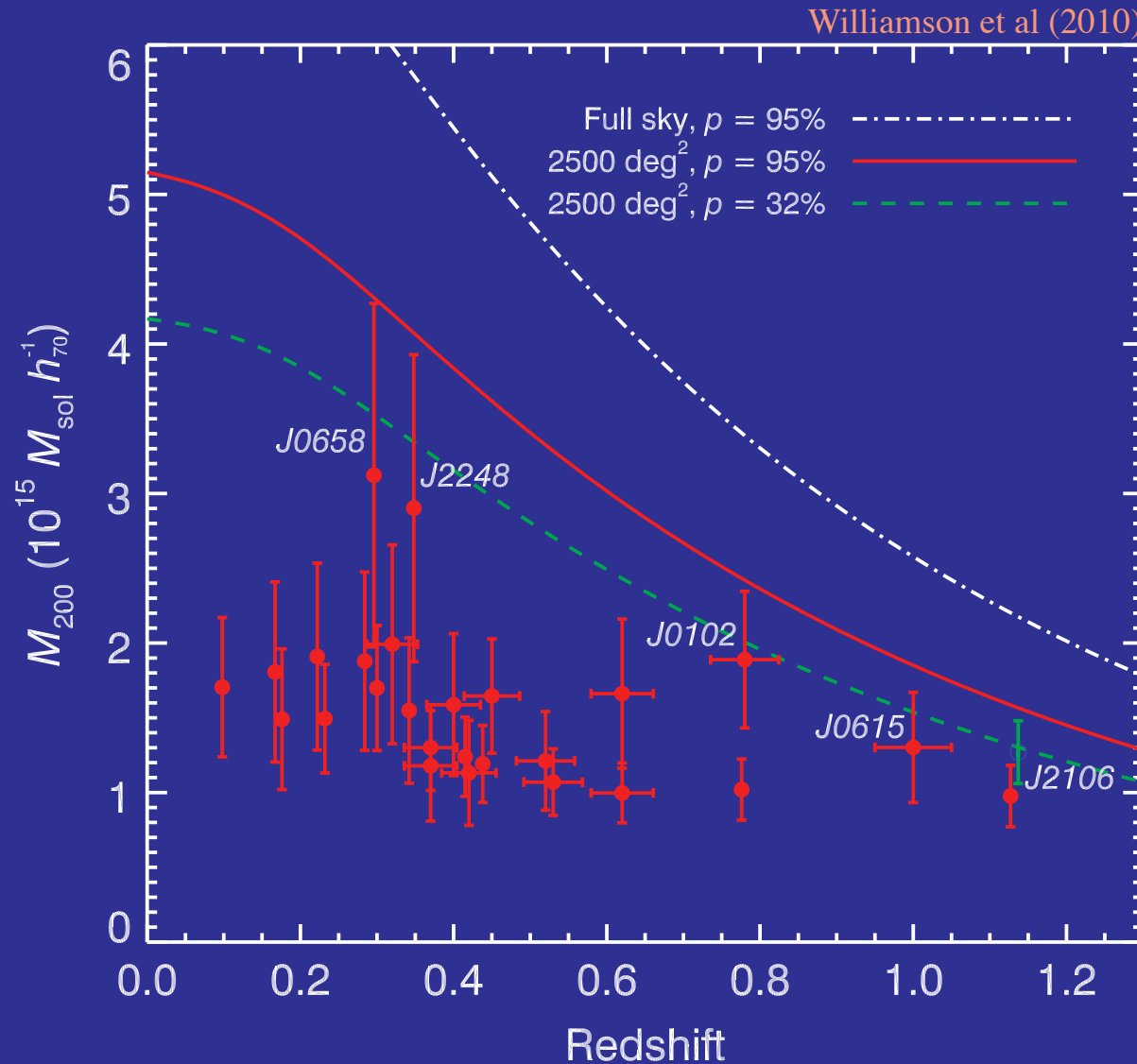
NonPC Caveats on PCs

- Principal component decomposition of $w(z)$ shows many components can in principle be measured (Euclid, LSST, WFirst)
- Yet even models like Albrecht-Skordis (oscillating w) are still dominated by first component - average w or pivot - plus 1-2 weaker
- Should a multidimensional parameterization be the basis for optimizing an experiment?



Pink Elephant Parade

- Too early too soon? SPT catalogue on 2500 sq degrees



Falsification Criteria
Mortonson, Hu, Huterer (2010)
Holz & Perlmutter (2010)

Other Analyses
Hoyle, Jimenez, Verde (2010)
many others...

Systematics, Systematics, Systematics

- E.g.: clusters - mass calibration from X-ray, SZ, optical, lensing

Systematics, Systematics, Systematics

- Coffee talk: discuss amongst yourselves



Phenomenological To Do List

- How best to parameterize consistency tests or define theoretically predicted observables?
- How to treat baryonic effects in the non-linear regime e.g.
 - Galaxy occupation of halos [BAO, velocity field tests]
 - Concentration of clusters for cosmic shear

Extensive simulations + modelling of gas physics including star formation (see Brant, Licia, Volker's talks)

- Calibrate non-linear mean and covariance of dark energy observables as function of cosmological parameters (Volker's talk)
- Simulate alternate models
 - (Kill) inhomogeneous models
 - Interacting dark matter-energy models
 - Modified gravity models

Modified Gravity = Dark Energy?

- Solar system tests of gravity are informed by our knowledge of the local stress energy content
- With no other constraint on the stress energy of dark energy other than conservation, modified gravity is formally equivalent to dark energy

$$F(g_{\mu\nu}) + G_{\mu\nu} = 8\pi G T_{\mu\nu}^{\text{M}}$$

$$-F(g_{\mu\nu}) = 8\pi G T_{\mu\nu}^{\text{DE}}$$

$$G_{\mu\nu} = 8\pi G [T_{\mu\nu}^{\text{M}} + T_{\mu\nu}^{\text{DE}}]$$

and the Bianchi identity guarantees $\nabla^\mu T_{\mu\nu}^{\text{DE}} = 0$

- Distinguishing between dark energy and modified gravity requires closure relations that relate components of stress energy tensor
- For matter components, closure relations take the form of equations of state relating density, pressure and anisotropic stress

Modified Gravity \neq “Smooth DE”

- **Scalar field** dark energy has $\delta p = \delta \rho$ (in constant field gauge) – relativistic sound speed, **no anisotropic** stress
- **Jeans stability** implies that its energy density is **spatially smooth** compared with the **matter** below the **sound horizon**

$$ds^2 = -(1 + 2\Psi)dt^2 + a^2(1 + 2\Phi)dx^2$$

$$\nabla^2(\Phi - \Psi) \propto \text{matter density fluctuation}$$

- **Anisotropic stress** changes the amount of **space curvature** per unit dynamical mass

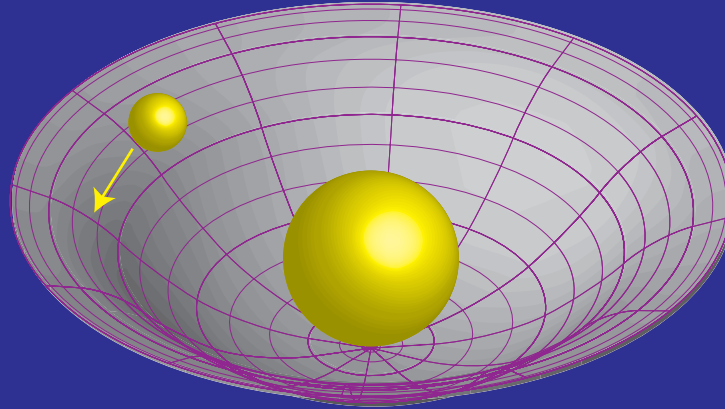
$$\nabla^2(\Phi + \Psi) \propto \text{anisotropic stress}$$

but its absence in a **smooth dark energy** model makes

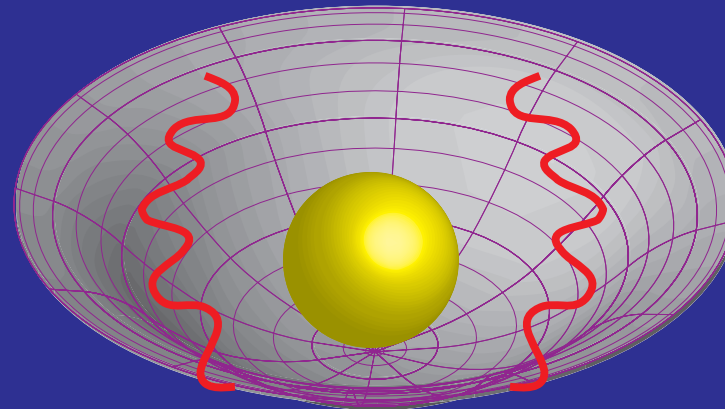
$$g = (\Phi + \Psi)/(\Phi - \Psi) = 0 \text{ for non-relativistic matter}$$

Dynamical vs Lensing Mass

- Newtonian **potential**: $\Psi = \delta g_{00} / 2g_{00}$ which non-relativistic particles feel



- Space **curvature**: $\Phi = \delta g_{ii} / 2g_{ii}$ which also deflects photons

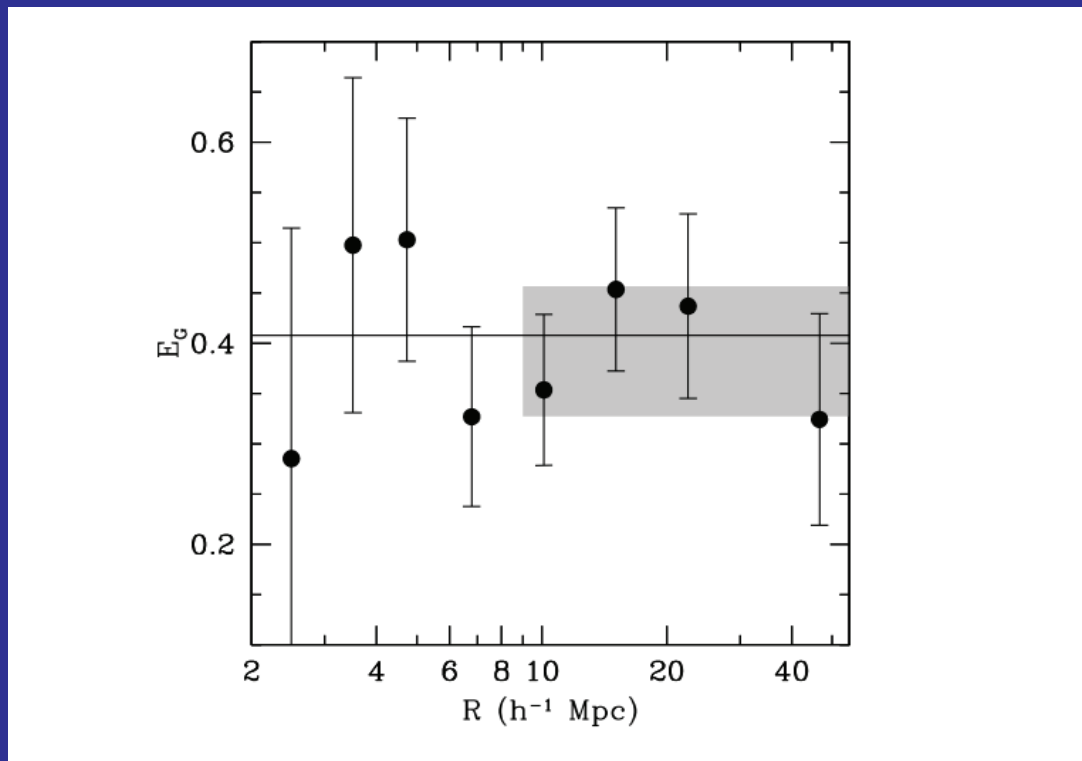


- Most of the **incisive tests** of gravity reduce to testing the **space curvature** per unit **dynamical mass**

Lensing v Dynamical Comparison

- Gravitational lensing around galaxies vs. linear velocity field (through redshift space distortions and galaxy autocorrelation)
- Consistent with GR + smooth dark energy beginning to test interesting models

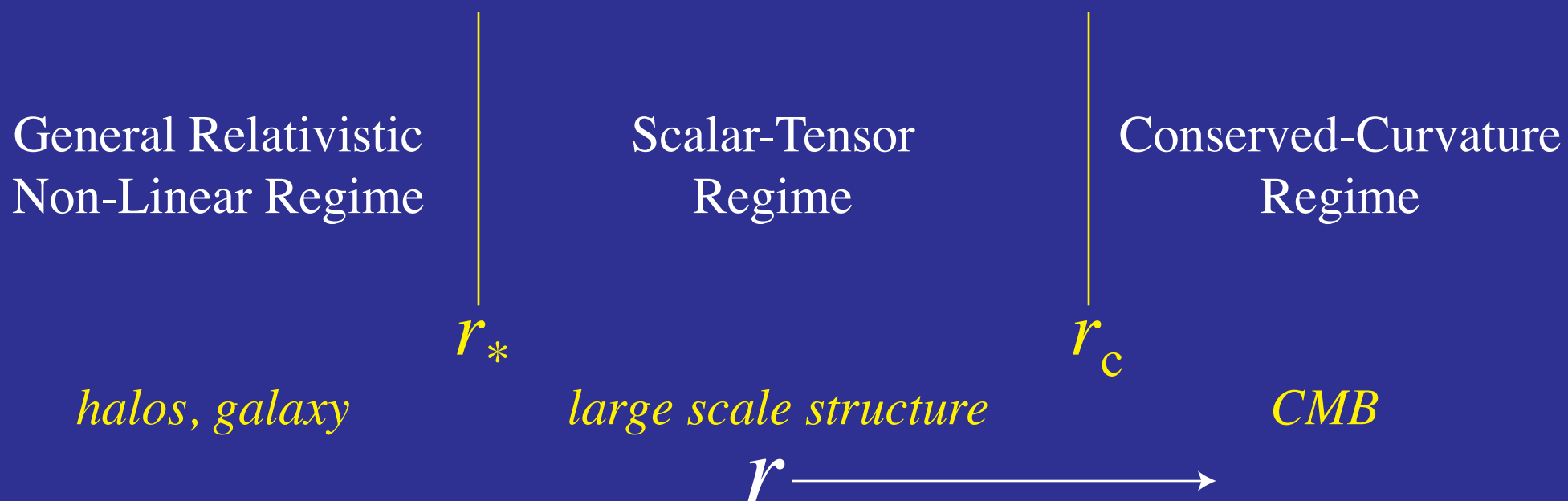
Reyes et al (2010); Lombriser et al (2010)



Zhang et al (2007); Jain & Zhang (2008)

Three Regimes

- Three regimes with different dynamics
- Examples $f(R)$ and DGP braneworld acceleration
- Parameterized Post-Friedmann description
- Non-linear regime return to General Relativity / Newtonian dynamics



Three Regimes

- Fully worked $f(R)$ and DGP examples show 3 regimes
- Superhorizon regime: $\zeta = \text{const.}$, $g(a)$
- Linear regime - closure condition - analogue of “smooth” dark energy density:

$$\begin{aligned}\nabla^2(\Phi - \Psi)/2 &= -4\pi G a^2 \Delta\rho \\ g(a, \mathbf{x}) &\leftrightarrow g(a, k)\end{aligned}$$

G can be promoted to $G(a)$ but conformal invariance relates fluctuations to field fluctuation that is small

- Non-linear regime:

$$\begin{aligned}\nabla^2(\Phi - \Psi)/2 &= -4\pi G a^2 \Delta\rho \\ \nabla^2\Psi &= 4\pi G a^2 \Delta\rho - \frac{1}{2}\nabla^2\phi\end{aligned}$$

Nonlinear Interaction

Non-linearity in the **field equation**

$$\nabla^2 \phi = g_{\text{lin}}(a) a^2 (8\pi G \Delta \rho - N[\phi])$$

recovers linear theory if $N[\phi] \rightarrow 0$

- For $f(R)$, $\phi = f_R$ and

$$N[\phi] = \delta R(\phi)$$

a non-linear function of the field

Linked to **gravitational potential**

- For **DGP**, ϕ is the brane-bending mode and

$$N[\phi] = \frac{r_c^2}{a^4} [(\nabla^2 \phi)^2 - (\nabla_i \nabla_j \phi)^2]$$

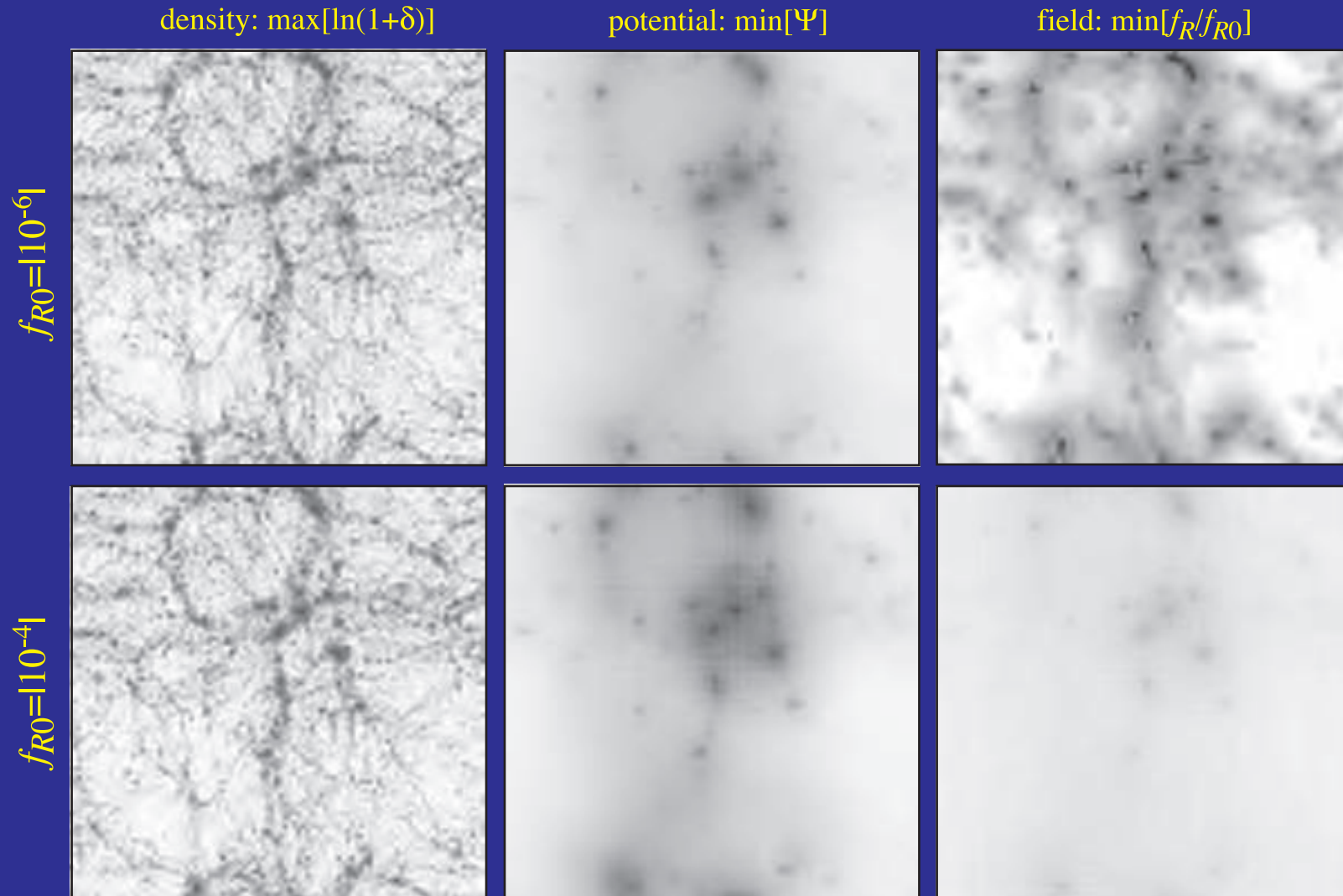
a non-linear function of second derivatives of the field

Linked to **density fluctuation**

Example of **Galileon invariance**

Environment Dependent Force

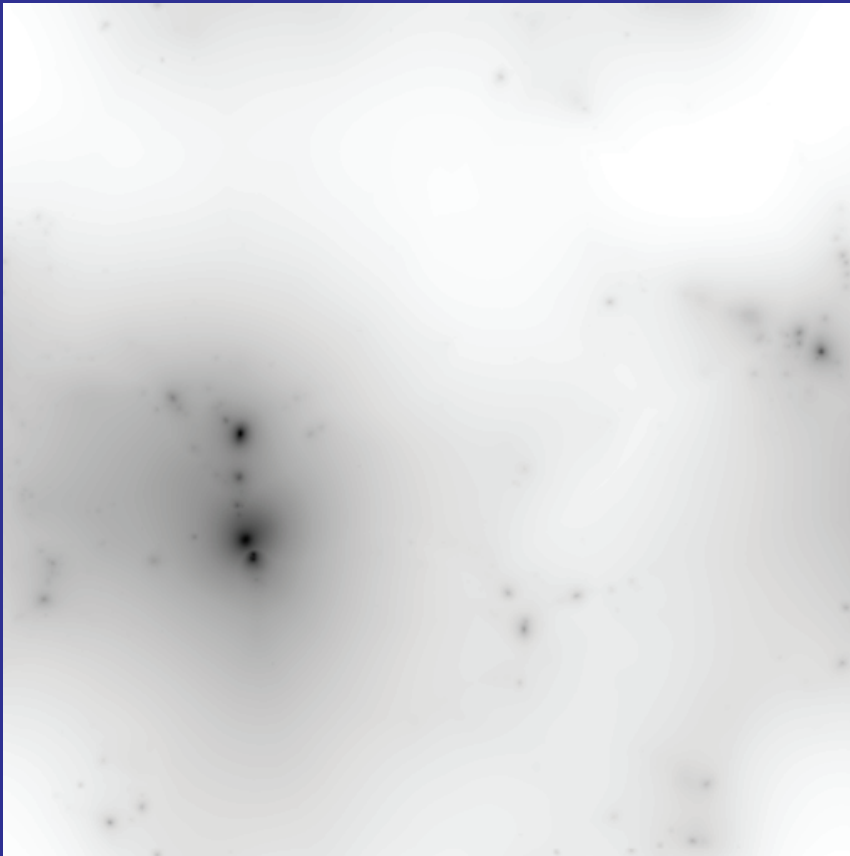
- For large background field, gradients in the scalar prevent the chameleon from appearing



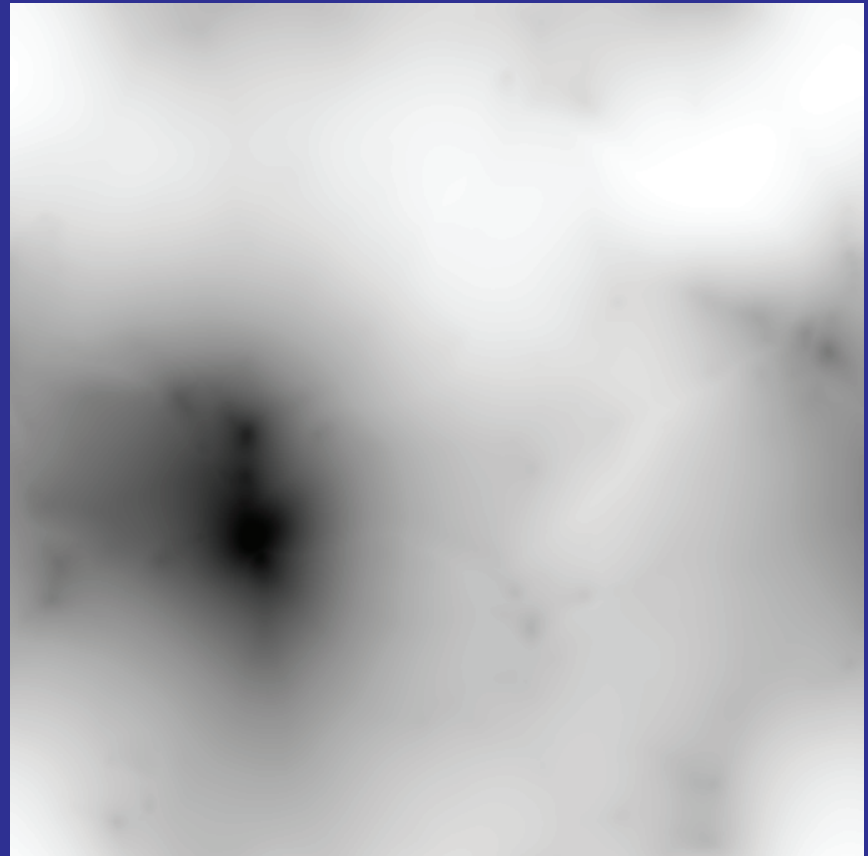
DGP N-Body

- DGP nonlinear derivative interaction solved by relaxation revealing the Vainshtein mechanism

Newtonian Potential

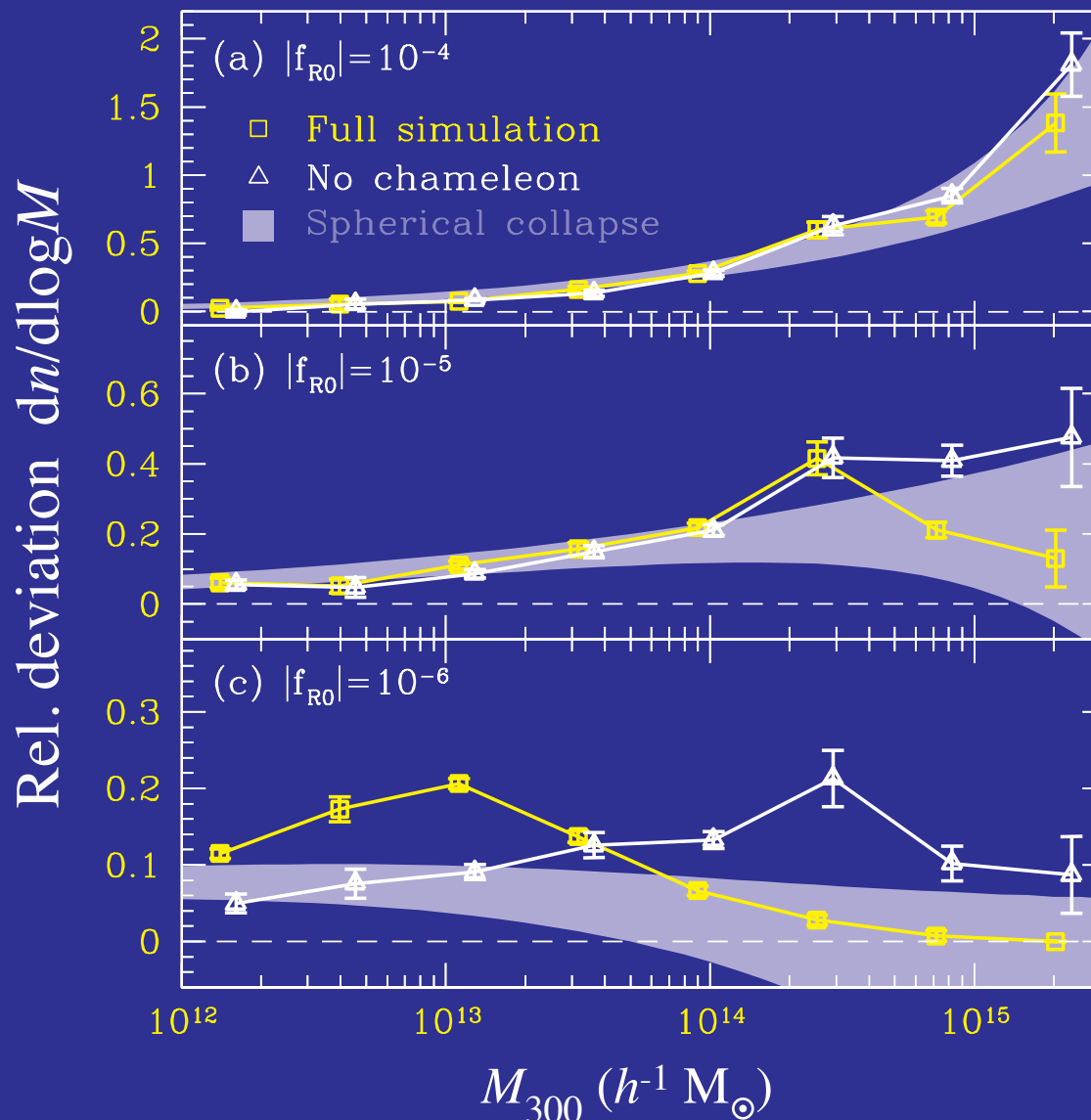


Brane Bending Mode



Mass Function

- Enhanced **abundance** of rare dark matter halos (**clusters**) with extra force goes away as non-linearity increases



Phenomenological To Do List

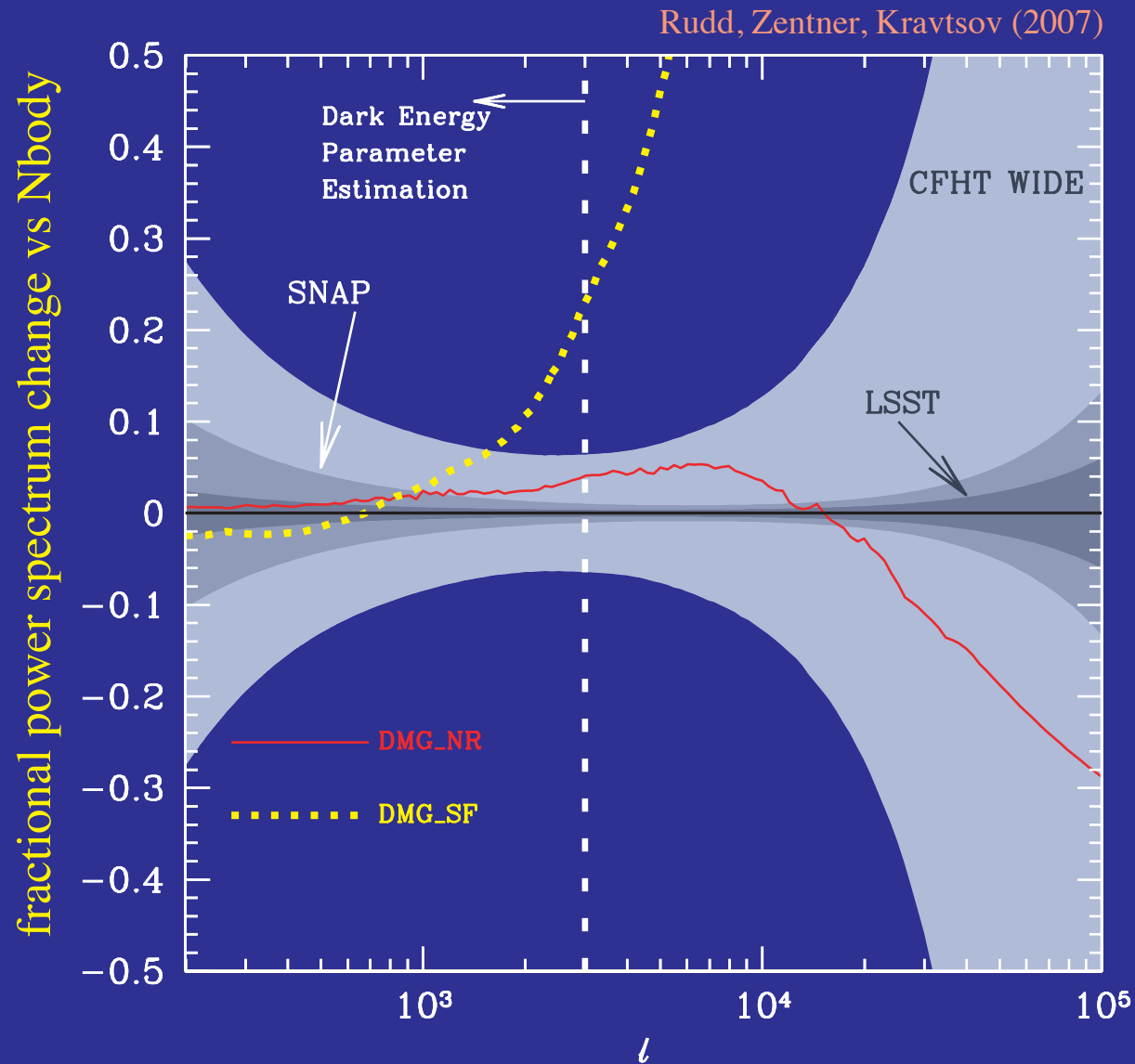
- How best to parameterize consistency tests or define theoretically predicted observables?
- How to treat baryonic effects in the non-linear regime e.g.
 - Galaxy occupation of halos [BAO, velocity field tests]
 - Concentration of clusters for cosmic shear

Extensive simulations + modelling of gas physics including star formation (see Brant, Licia, Volker's talks)

- Calibrate non-linear mean and covariance of dark energy observables as function of cosmological parameters (Volker's talk)
- Simulate alternate models
 - (Kill) inhomogeneous models
 - Interacting dark matter-energy models
 - Modified gravity models

Cooling/Star Formation in Clusters

- Baryonic effects can lead to false falsification of Λ CDM



Theoretical To Do List

- Develop (discuss here) and explore **known alternatives**
- **Dynamical Dark Energy**
 - Quintessence, k-essence, phantom, effective field theoretic quintessence, vanishing sound speed k-essence, extended quintessence, coupled quintessence, electrostatic dark energy, elastically scattering dark energy, and other **venial sins...**
- **Modified Gravity**
 - braneworld, $f(R)$, $f(G)$, cascading gravity, degravitation, galileon, massive gravity, kinetic gravity braiding, TeVeS and **other heresies...**

Theoretical To Do List

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 - Q: e.g. do **massive gravity** and **galileon ideas** for self-acceleration without ghosts make sense beyond the decoupling limit

Theoretical To Do List

- Develop alternatives that are **more than** just illustrative **toy models**

Floor is open to hear about them now!

- If **observationally indistinguishable** from Λ why does it have the **value** it does?

If we fail to find something to argue about in this session we can always try **landscape/anthropic**



Apf tgy 'Nkf f ng"qp'O qf gn'Ugngevkqp

What are we trying to achieve?

Goal: to define the key model tests to be carried and, where possible, to optimize survey strategies to achieve them. First we need to figure out which are the interesting models.

- **Λ CDM**: The current baseline cosmological model.

- **Parameterized dark energy models**, eg CPL $w = w_0 + (1-a) w_a$

The most common candidate alternative for dark energy studies.

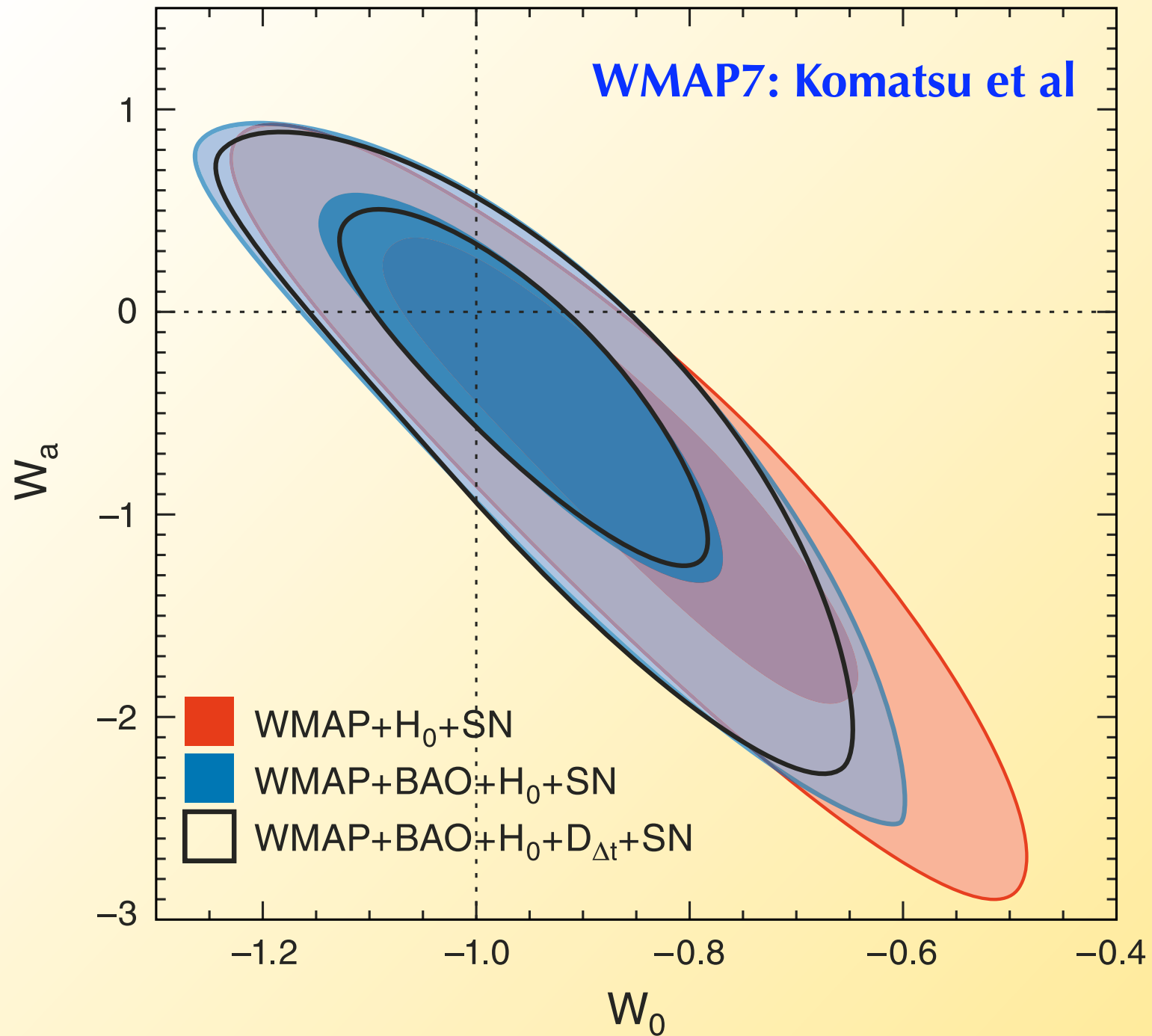
- **Fundamental physics dark energy models**, eg inverse power-laws, Albrecht-Skordis, etc

Many candidate models in the literature though many fail to fit current data. Not clear which are best motivated.

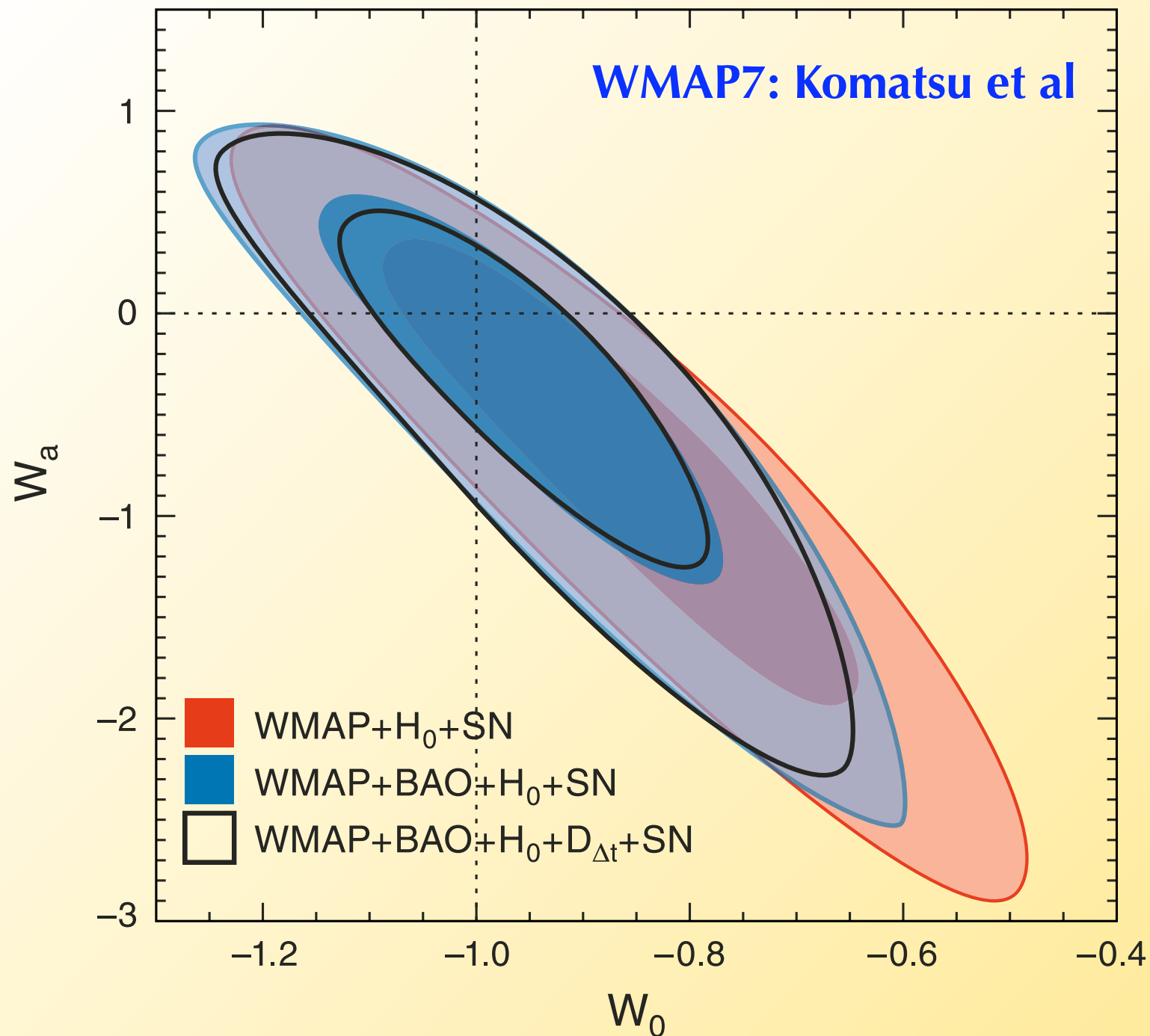
- **Modified gravity models**

Determination of best candidate modified gravity models required.

Parameter estimation tests



Parameter estimation tests



This graph answers the following question:

If we assume that the w_0 - w_a dark energy model is correct, how good will our constraints on those parameters be?

Model tests

However that wasn't the question we wanted to answer, which was:

Between the Λ CDM model and the dark energy model, which is the better description of the data?

[I.e., can one of them be ruled out with respect to the other?]

This question can only be answered with a model-level analysis, e.g. Bayesian model selection.

Model tests

However that wasn't the question we wanted to answer, which was:

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Another way of expressing this: do you think that the *prior* probabilities of $w_0 = -1$ and of $w_0 = -0.9$ are equal?

I would argue that they are not just different in magnitude, but that the former is finite while the latter is infinitesimal.

(Almost) current dark energy data

Liddle, Mukherjee, Parkinson, and Wang, PRD, astro-ph/0610126

CMB shift+BAO(SDSS)+SN

LambdaCDM	data used	
	WMAP+SDSS+	$\Delta \ln E$
	Astier05	0.0
Constant w	Astier05	
	-1.3 ± 0.1	
	Astier05	
w_0-w_a	Astier05	
	-2.0 ± 0.1	
	Astier05	
	Astier05	
	-4.1 ± 0.1	

(Almost) current dark energy data

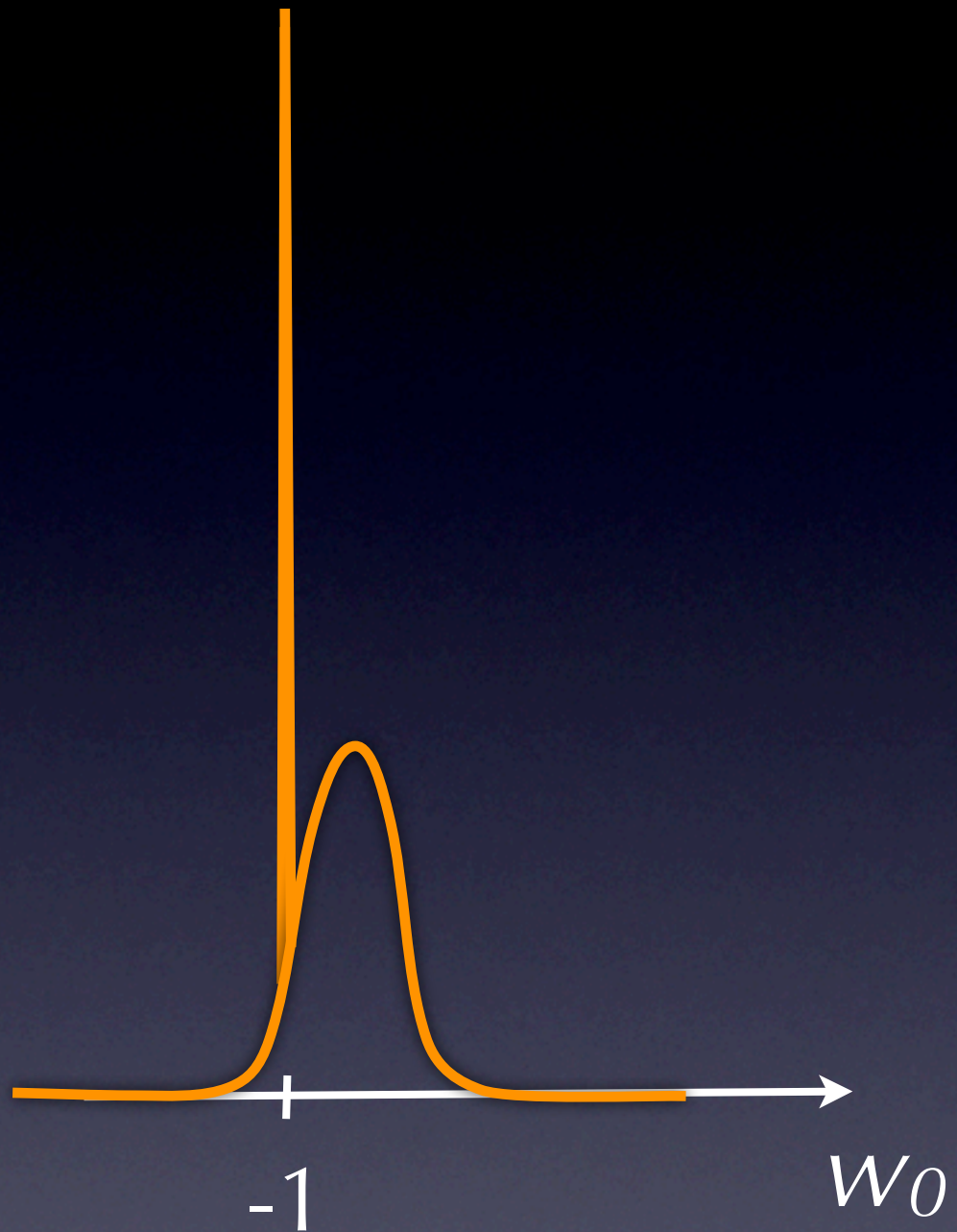
Liddle, Mukherjee, Parkinson, and Wang, PRD, astro-ph/0610126

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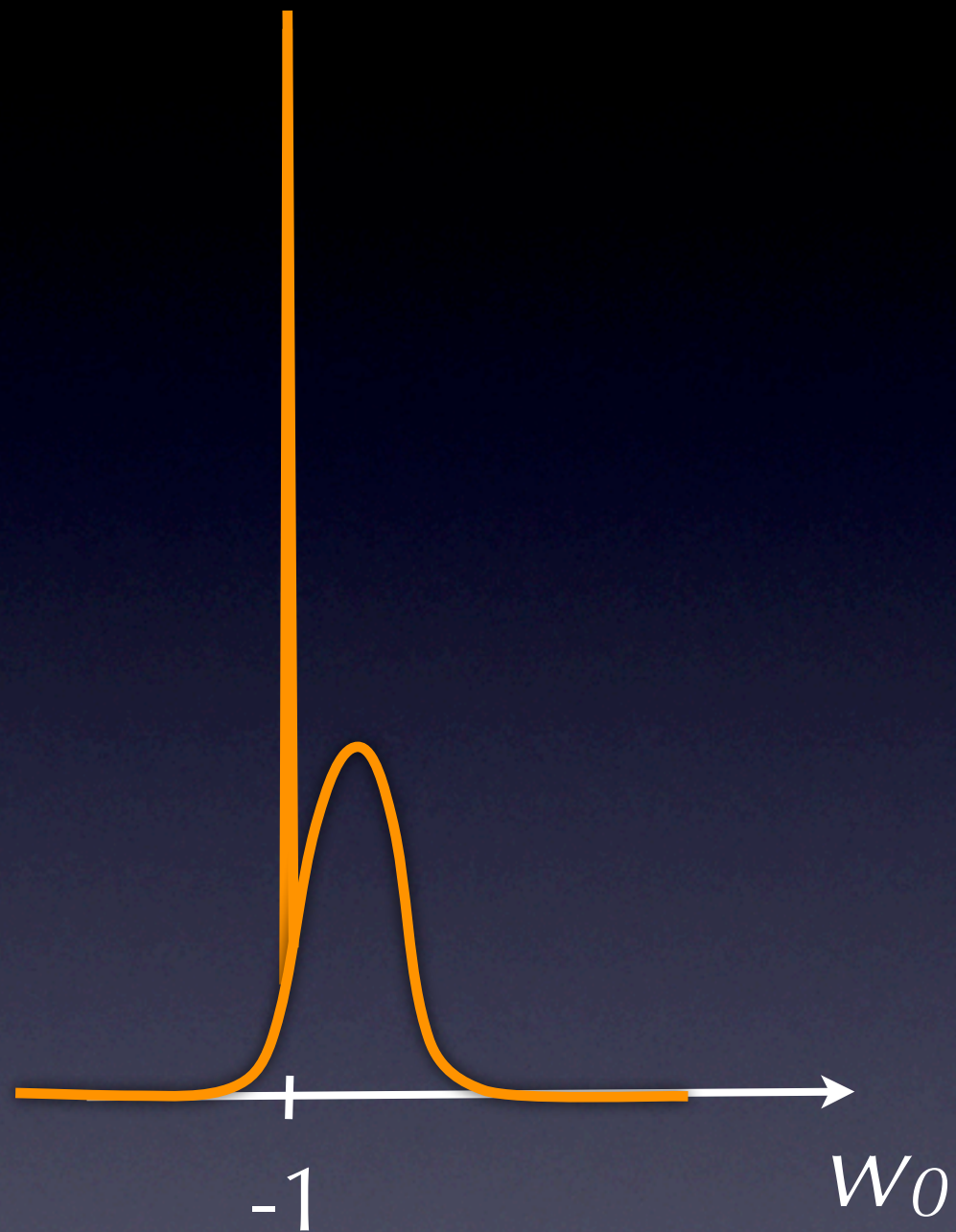
LambdaCDM	data used	
	WMAP+SDSS+	$\Delta \ln E$
Constant W	Astier05	0.0
	Astier05	-1.3 ± 0.1
W ₀ -W _a	Astier05	-1.8 ± 0.1
	Astier05	-2.0 ± 0.1
	Astier05	-4.1 ± 0.1

Conclusion: If the models were originally equally likely, the data now indicates about a 75% chance that Λ CDM is correct.

Likelihood of w_0 given all models

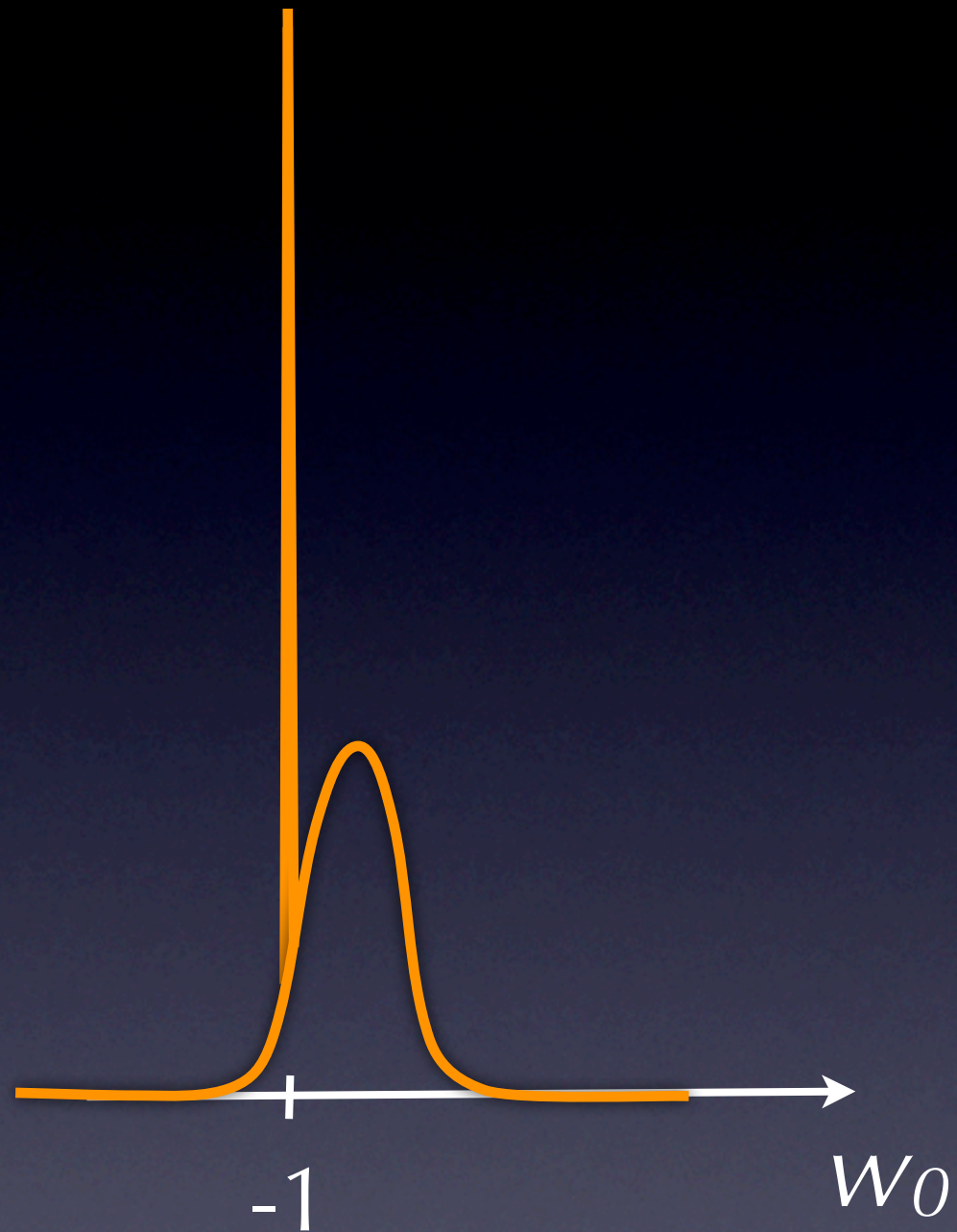


Likelihood of w_0 given all models



Low IQ version

Likelihood of w_0 given all models



Low IQ version



High IQ version

Model tests/inference

Model-level inference can be used at several levels:

- **Model-level tests**

Deploy Bayesian model selection tools to compare model classes.

- **Model selection forecasting**

Evaluate the capability of proposed experiments to answer model selection questions, by defining model selection FoMs. Explore outcomes contingent on each model class (including Λ CDM) being correct.

- **Survey optimization**

Vary survey configurations in order to optimize ability to carry out identified model test priorities.