

$$\rho_d = \sum_{i,j=1}^d S_d(i,j) |i\rangle \langle i| \otimes |j\rangle \langle j|$$