



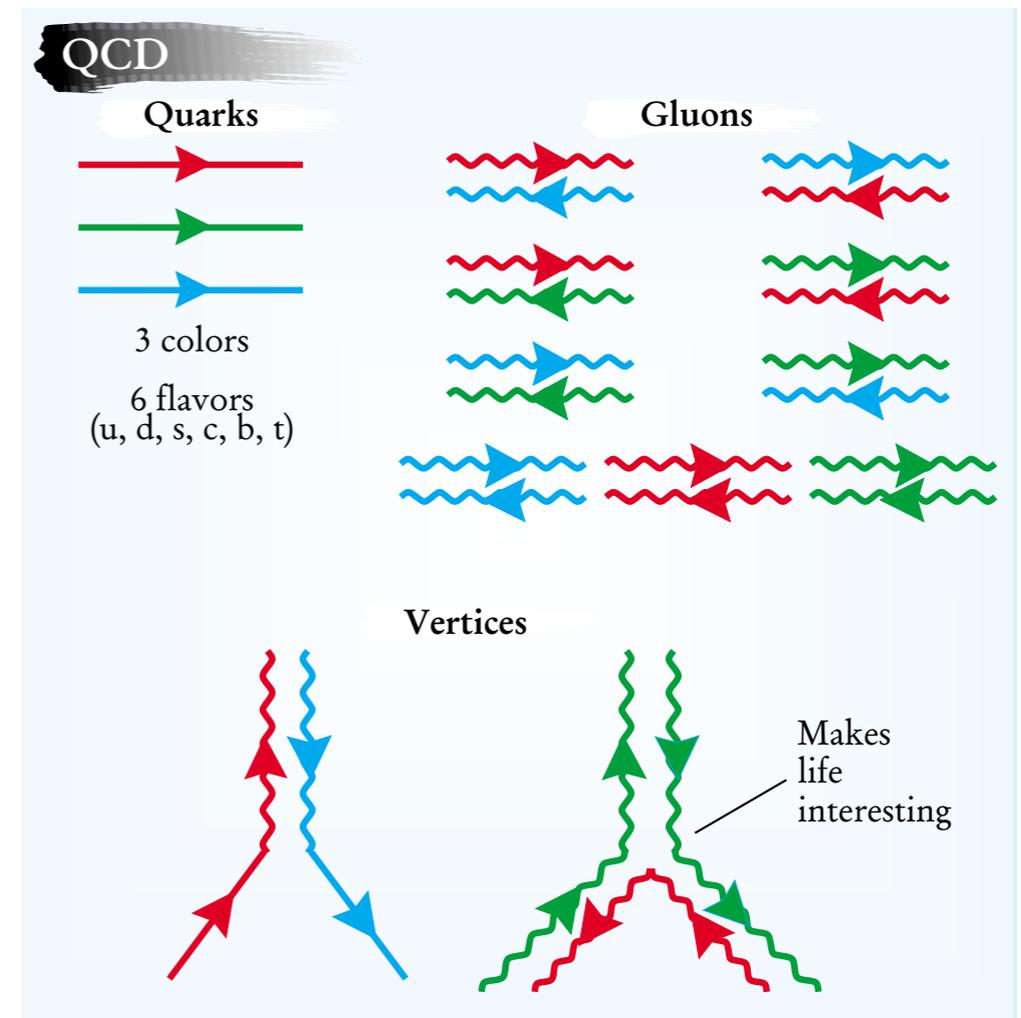
HEAVY IONS

Konrad Tywoniuk

Taller de Altas Energias 2014, Sep 14 - 27, Benasque

The strong nuclear interaction

- a theory of strongly interaction quarks & gluons
 - never observed directly
 - indirect measurements in experiments
- non-Abelian: gluons interact amongst themselves



A snapshot of a proton

A conundrum: how can QCD particles be aware of the fact that “physical” (long-distance) particles only interact with **integer** electric charge?

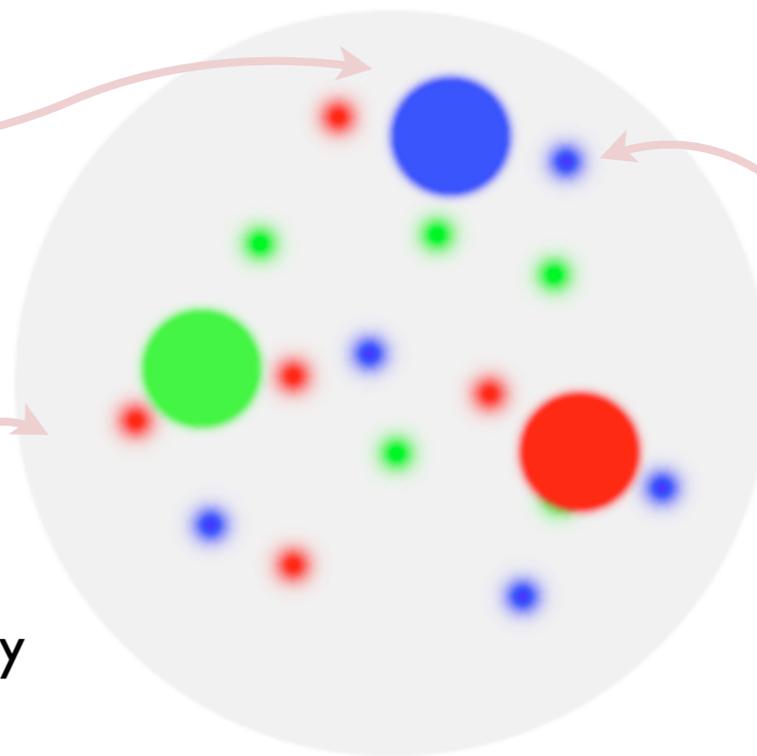
“fractional charge”

2/3 e: up, charm and top

1/3 e: down, strange and bottom

confinement

the quarks are tightly bound by the gluons inside “colorless” objects, so called **hadrons**



“fuzziness”

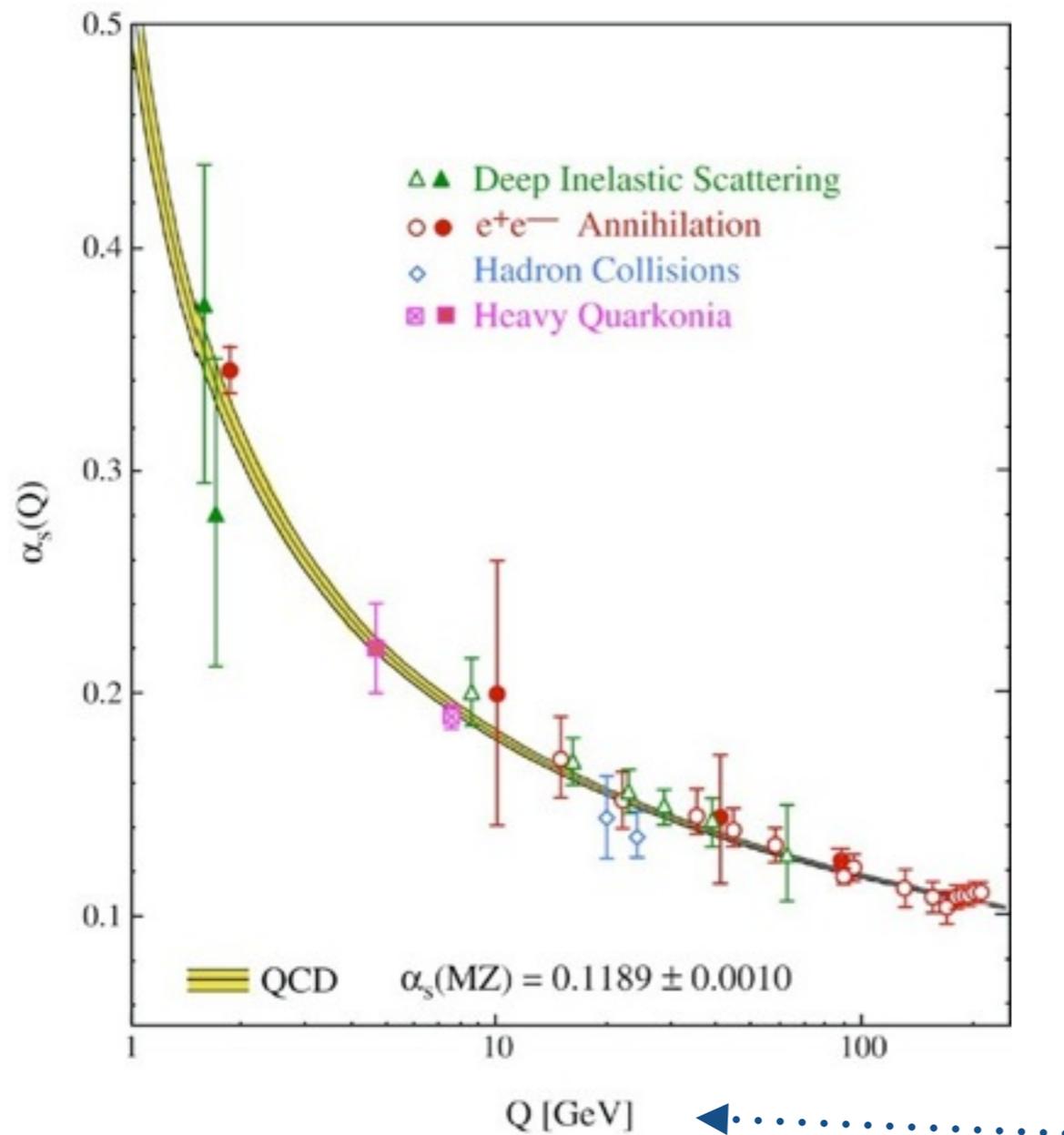
QCD is a **quantum field theory** (creation & annihilation of particles)

$$\Delta x \Delta p \gtrsim h$$

Millennium Prize Problem #7

Yang–Mills Existence and Mass Gap. Prove that for any compact simple gauge group G , a non-trivial quantum Yang–Mills theory exists on \mathbb{R}^4 and has a mass gap $\Delta > 0$. Existence includes establishing axiomatic properties at least as strong as those cited in [45, 35].

Asymptotic freedom

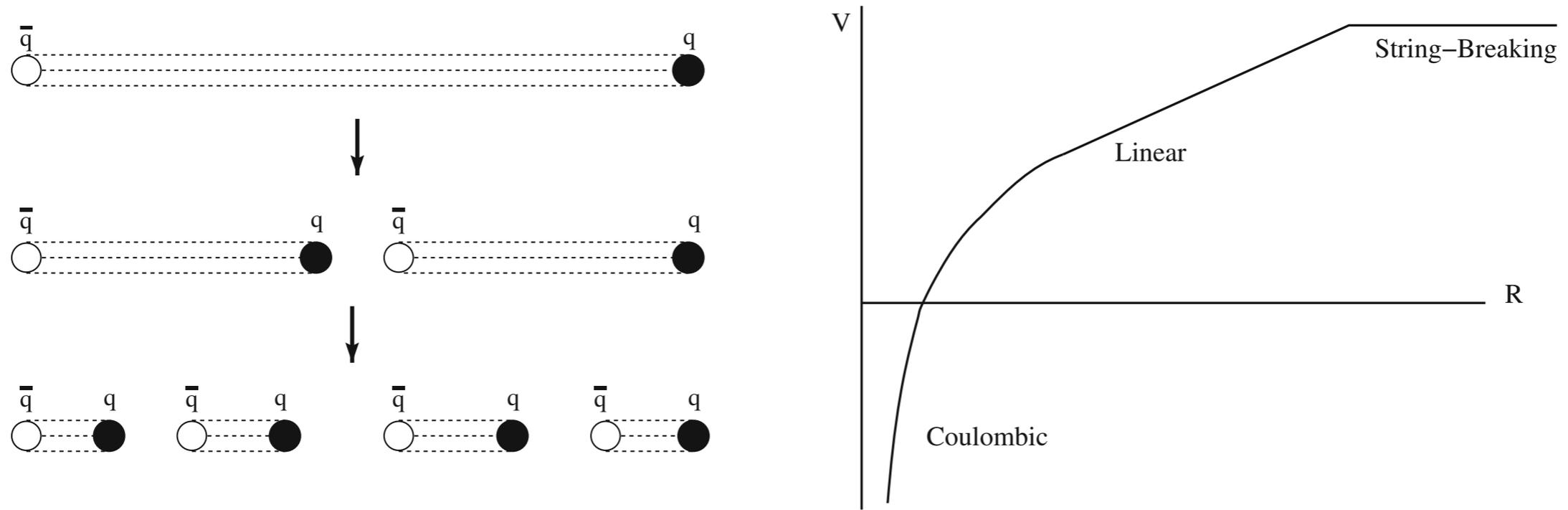


- QCD is weakly coupled at small distances — strongly coupled at large distances
- can use perturbation theory when there is a large scale in the problem
- unfortunately, in many interesting situations this is not the case...

In heavy-ions you also have to consider medium scales, such as T , geometry ($1/L$)...

multi-scale problem!

String breaking mechanism

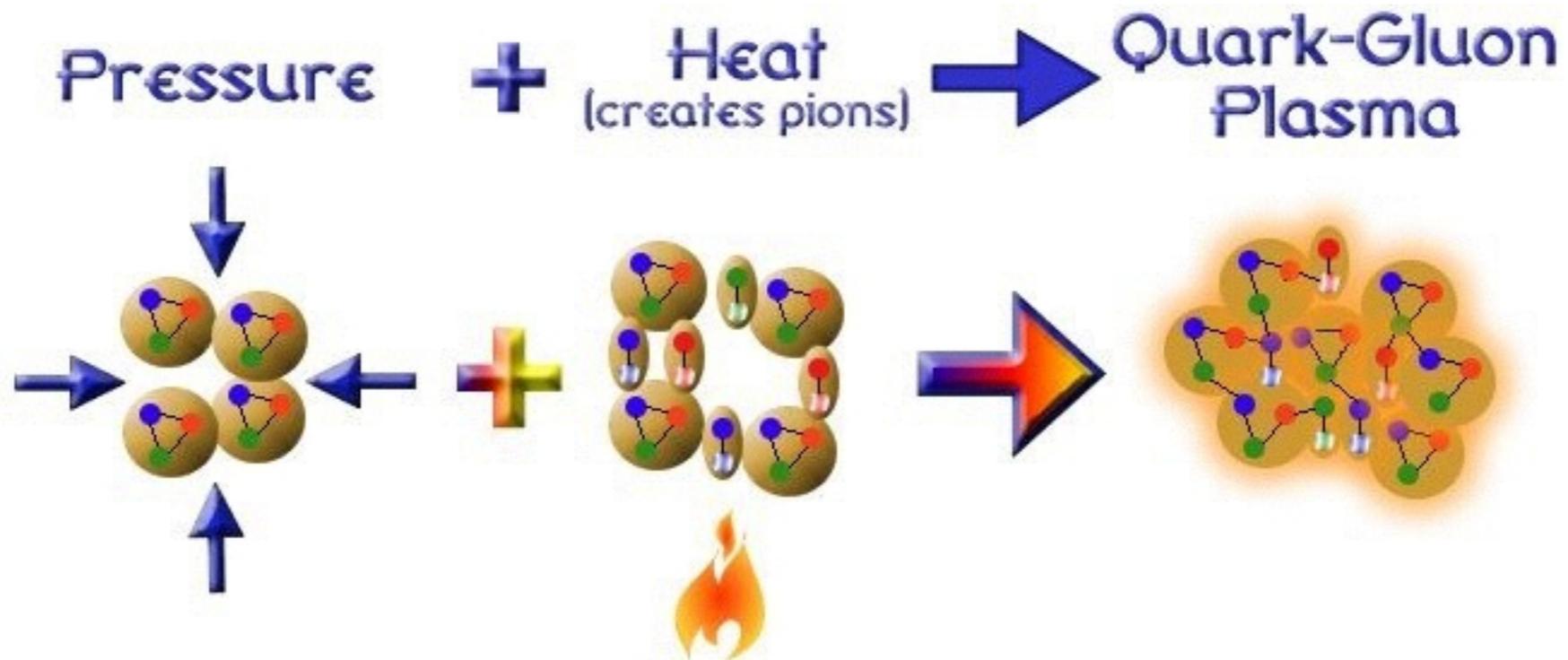


Energy stored in the tube is σL with $\sigma = \int d^2x_{\perp} \frac{1}{2} E_k^a(x) E_k^a(x)$

$$V(r) = -\frac{\alpha}{r} + \sigma r$$

- short-distance regime: Coulomb interaction
- $E_k = F_{0k}$ is the (color) electrical flux
- $\sqrt{\sigma} = 420$ MeV is the so-called string tension
- string breaks due to light quarks!

Changing the dynamics

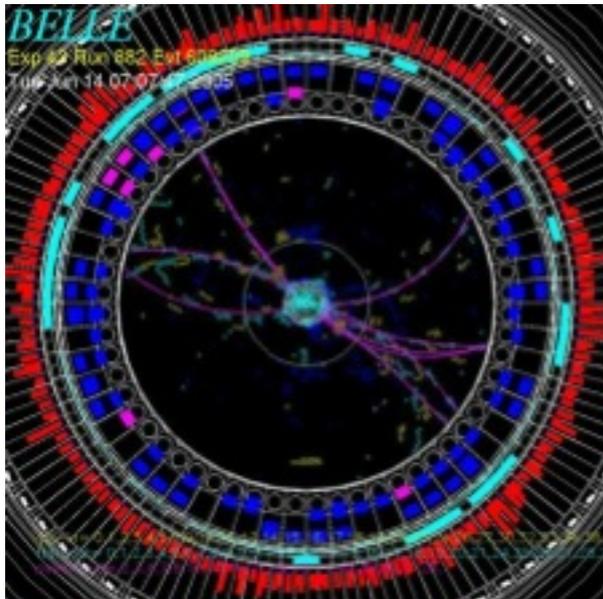


Lecture I

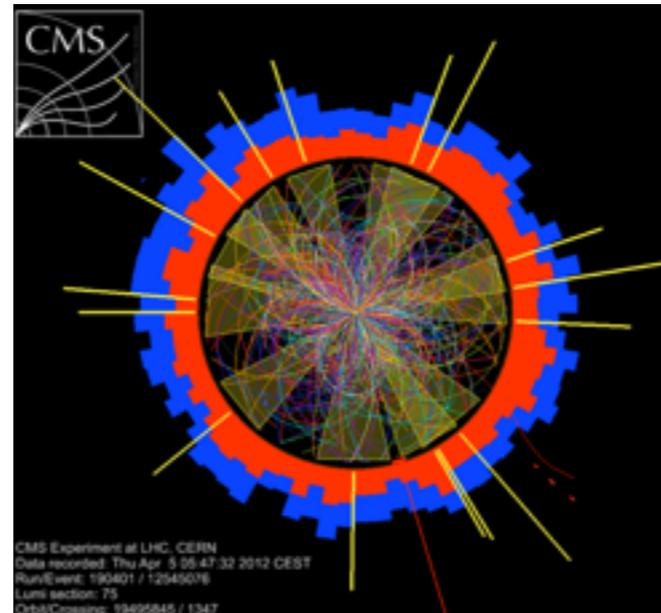
- thermal properties of QCD
- two paradigms: gas or fluid
- do we measure nucleons or gluons?

Heavy-ion collisions probe the strong interaction in highly dynamical and complex conditions.

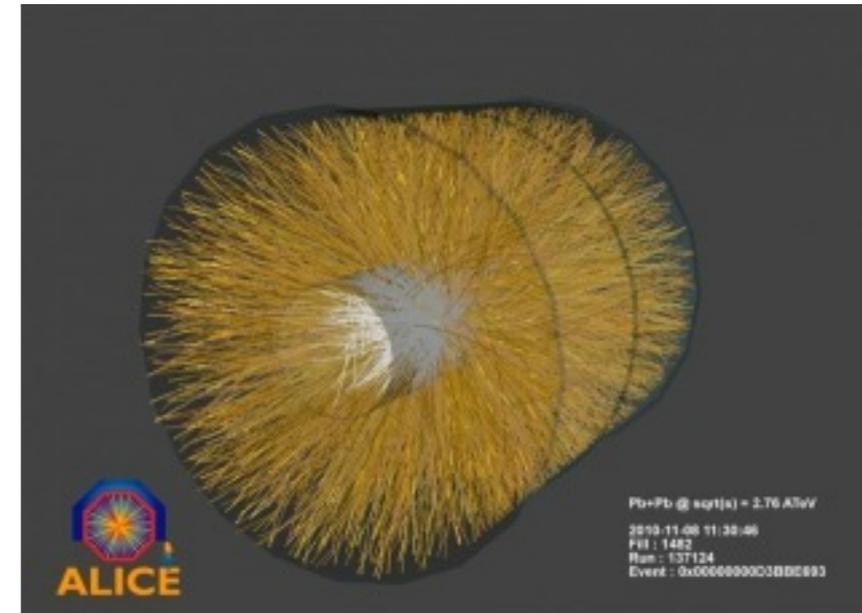
Collisions & colliders



e^+e^-

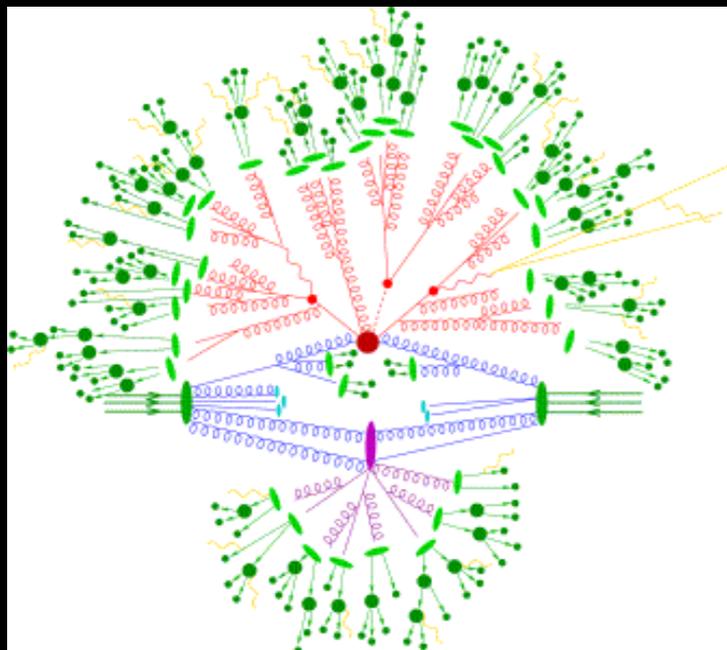
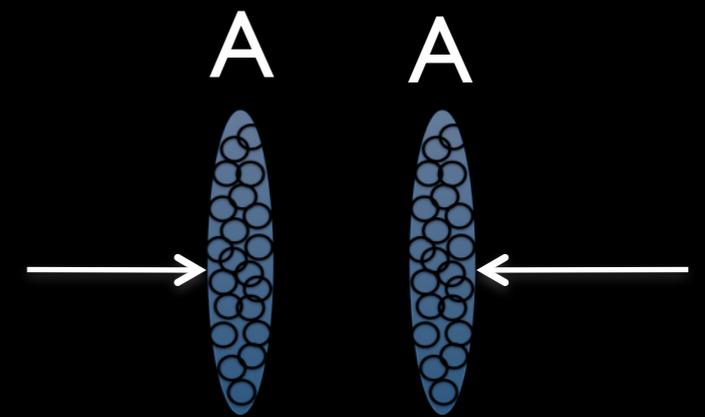
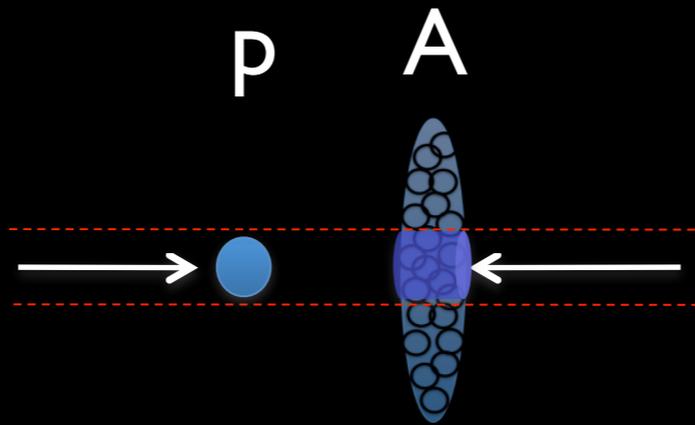


$p+p$

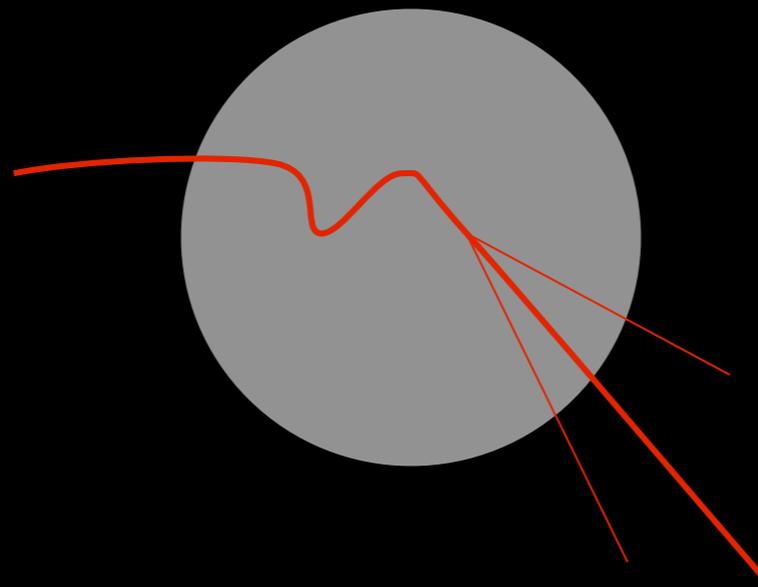


A+A

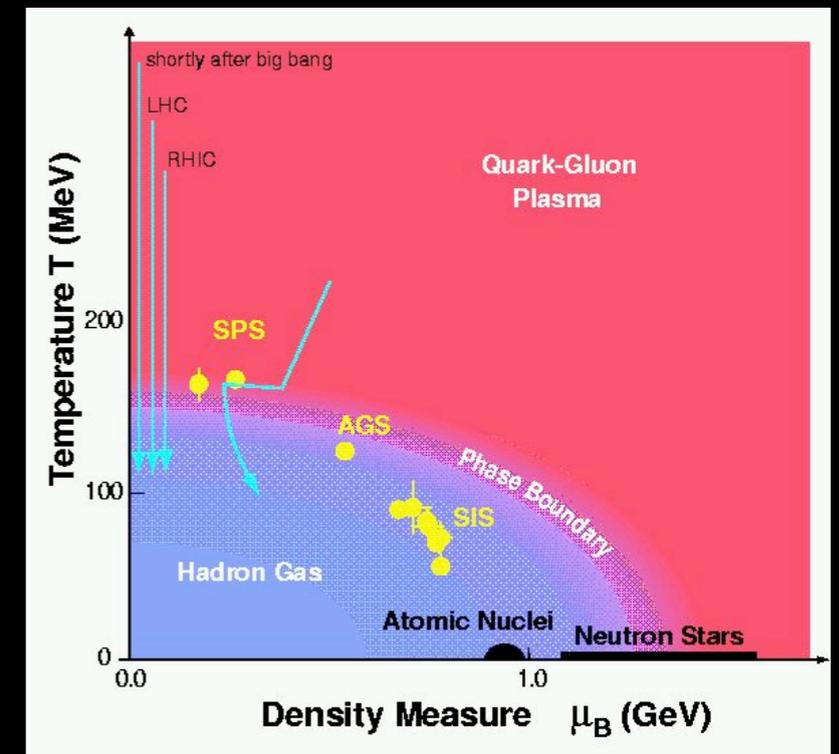
Names	Start-up	Energy ($\sqrt{s_{NN}}$)	Colliding system
Alternating Gradient Synchrotron (AGS)	mid 1980's	2-5 GeV	variety of beams
CERN Super Proton Synchrotron (SPS)	Pb since 1994	≤ 17 GeV	variety of beams
BNL Relativistic Heavy-Ion Collider (RHIC)	2000	≤ 200 GeV	$p+p$, $d+Au$, $Au+Au$, $Cu+Cu$, ...
CERN Large Hadron Collider (LHC)	2010	2.75 TeV, 4 TeV (?)	$p+p$, $Pb+Pb$, $p+Pb$



Local structure of QCD vacuum



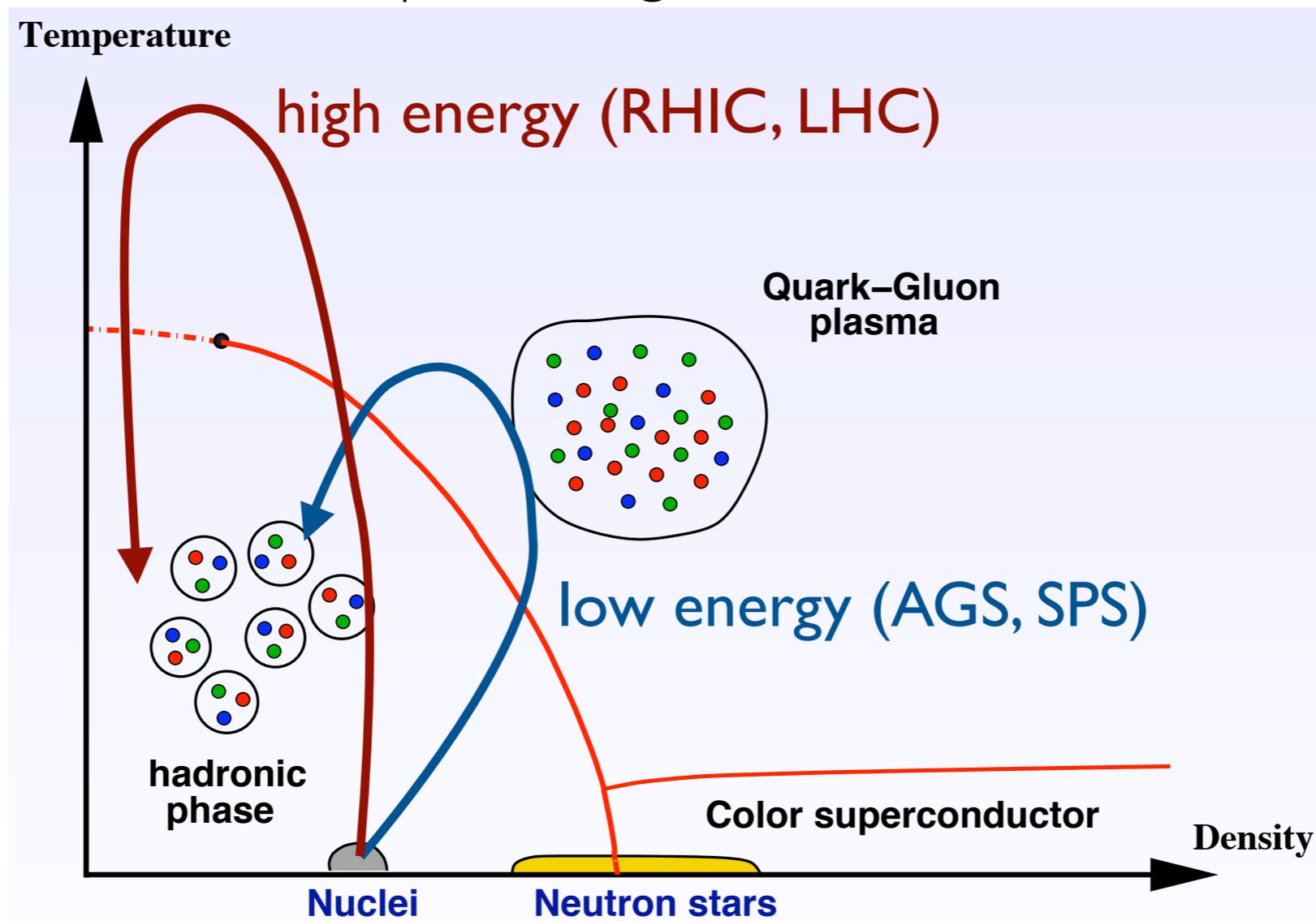
Local QCD + initial state/cold nuclear matter



Local QCD + initial state/cold nuclear matter + Quark-Gluon Plasma

Turning on the temperature

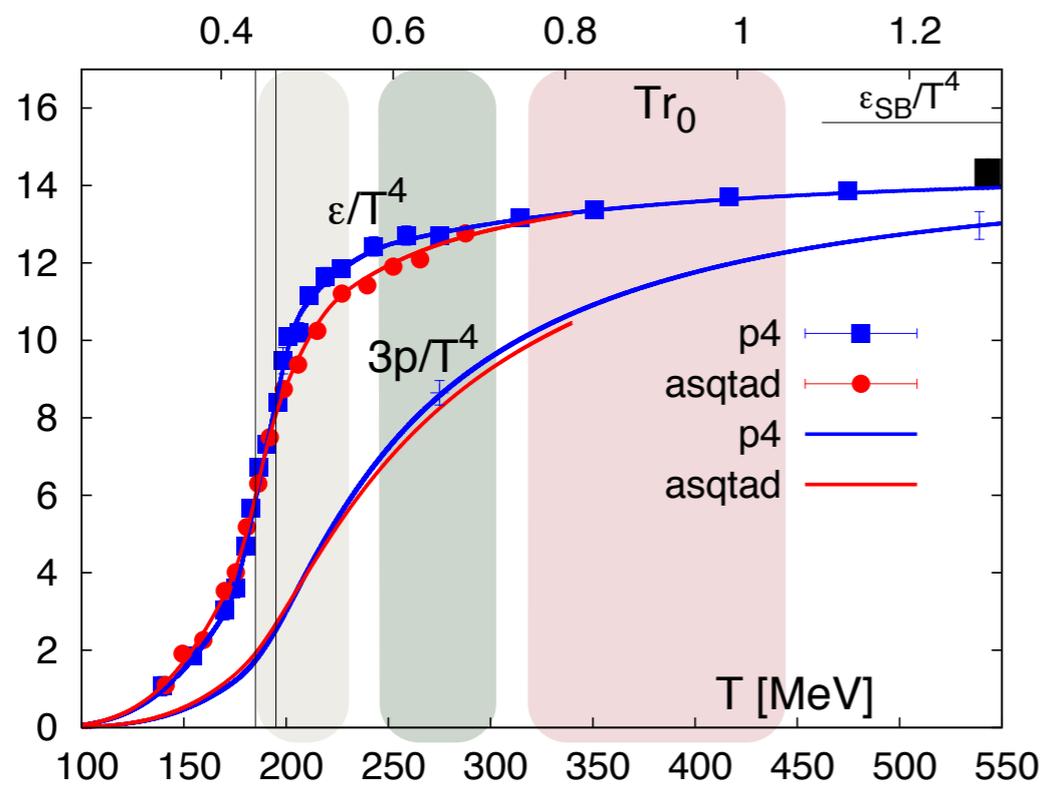
The phase diagram of QCD



$\mu_B = \text{net baryon density}$

QCD thermodynamics

A rapid rise of energy density (pressure, entropy etc) is observed ($\mu_B=0$).



Bazavov et al., PRD 80 (2009) 014504

Energy regimes: **SPS**, **RHIC** & **LHC**

Number of pions ($d_\pi=3$):
$$n_\pi = d_\pi \int \frac{d^3\mathbf{p}}{(2\pi)^3} \frac{1}{e^{E_{\mathbf{p}}/T} - 1}$$

Free parton gas:

$$e_{SB} = e_{\text{glue}} + e_{\text{quark}}$$

$$e_{\text{glue}} = d_{\text{glue}} \int \frac{d^3\mathbf{p}}{(2\pi)^3} \frac{E_{\mathbf{p}}}{e^{E_{\mathbf{p}}/T} - 1}$$

$$e_{\text{quark}} = d_{\text{quark}} \int \frac{d^3\mathbf{p}}{(2\pi)^3} \frac{E_{\mathbf{p}}}{e^{E_{\mathbf{p}}/T} + 1}$$

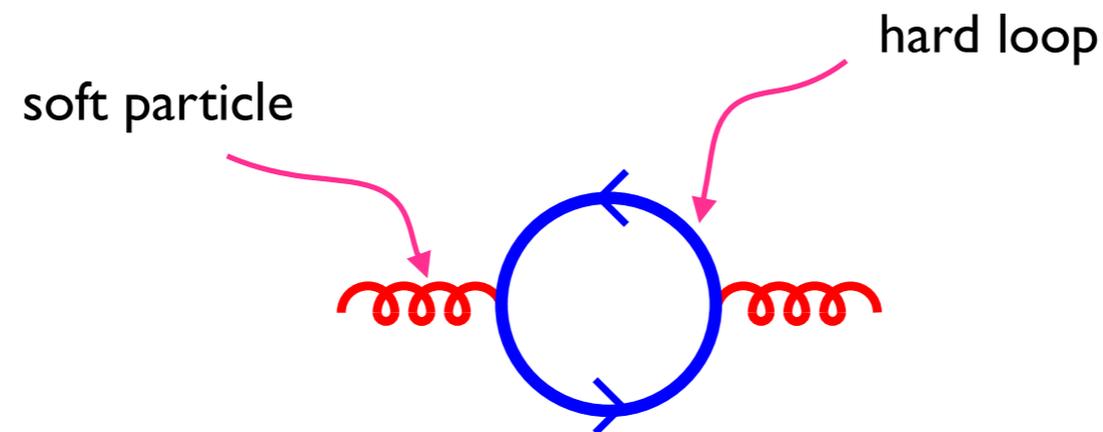
$$d_{\text{glue}} = 2 \times 8 \quad \text{spin, color}$$

$$d_{\text{quark}} = 2 \times 2 \times 3 \times 3 \quad \text{spin, quark/antiquark, color, flavor}$$

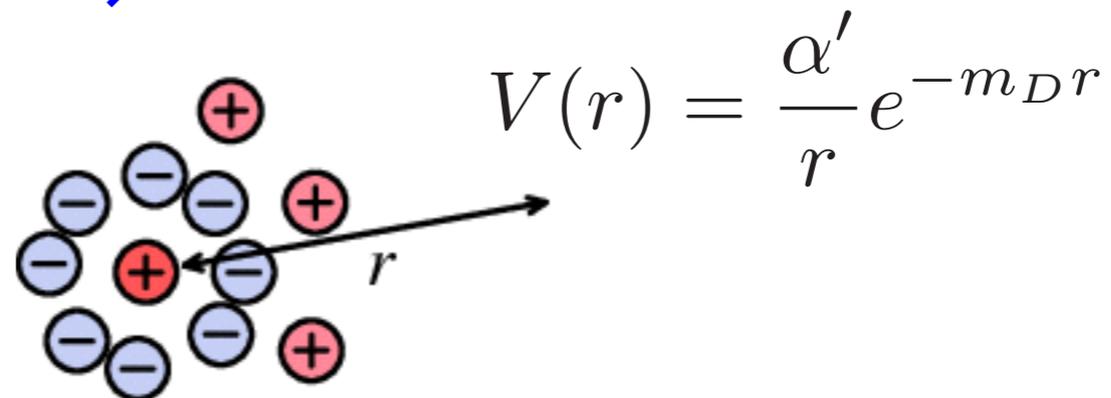
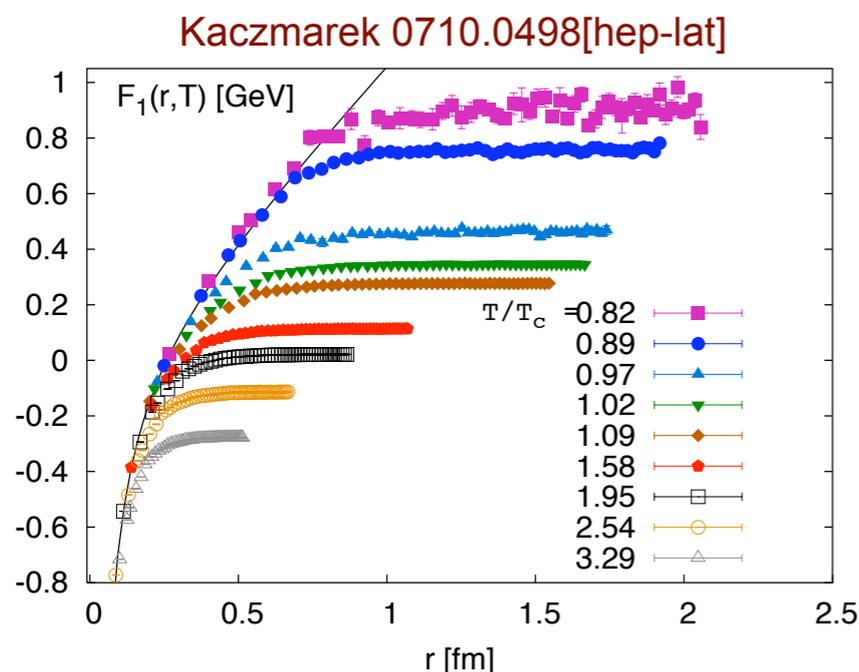
Do not reach Stefan-Boltzman limit — interactions survive!

Debye screening

At asymptotically high T ($g \ll 1$): plasma particles with soft momenta ($\sim gT$) are dressed by fluctuations ($\sim T$).



$$m_D = \# gT$$



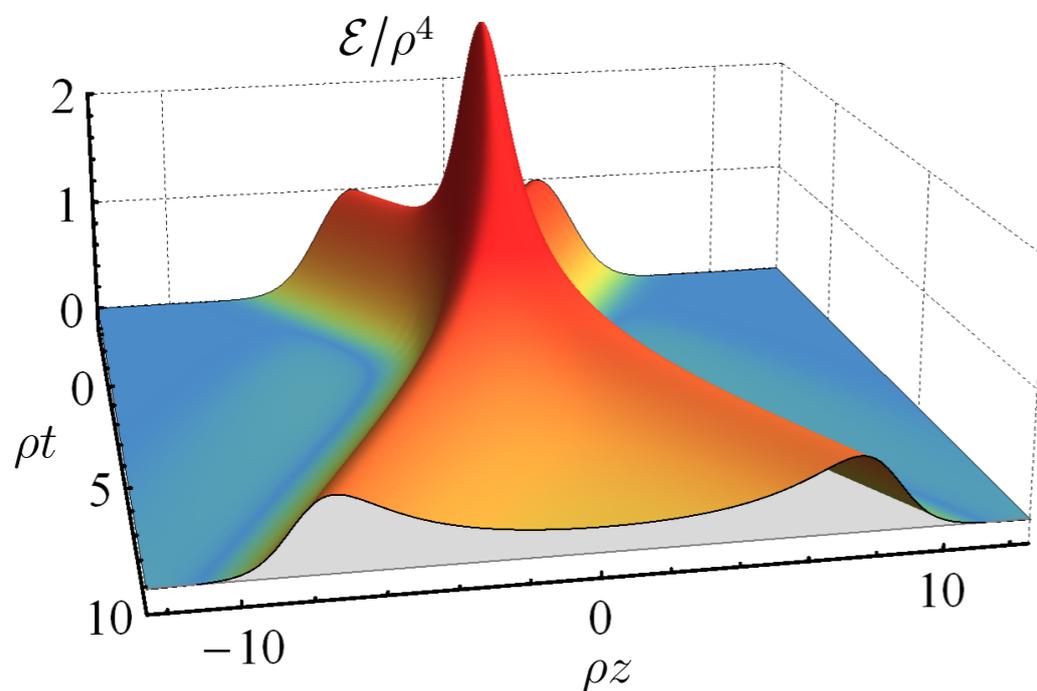
$$V(r) = \frac{\alpha'}{r} e^{-m_D r}$$

- color interactions have limited range
- gauge bosons get dressed :: longitudinal gluons
- Hard-Thermal-Loop effective field theory

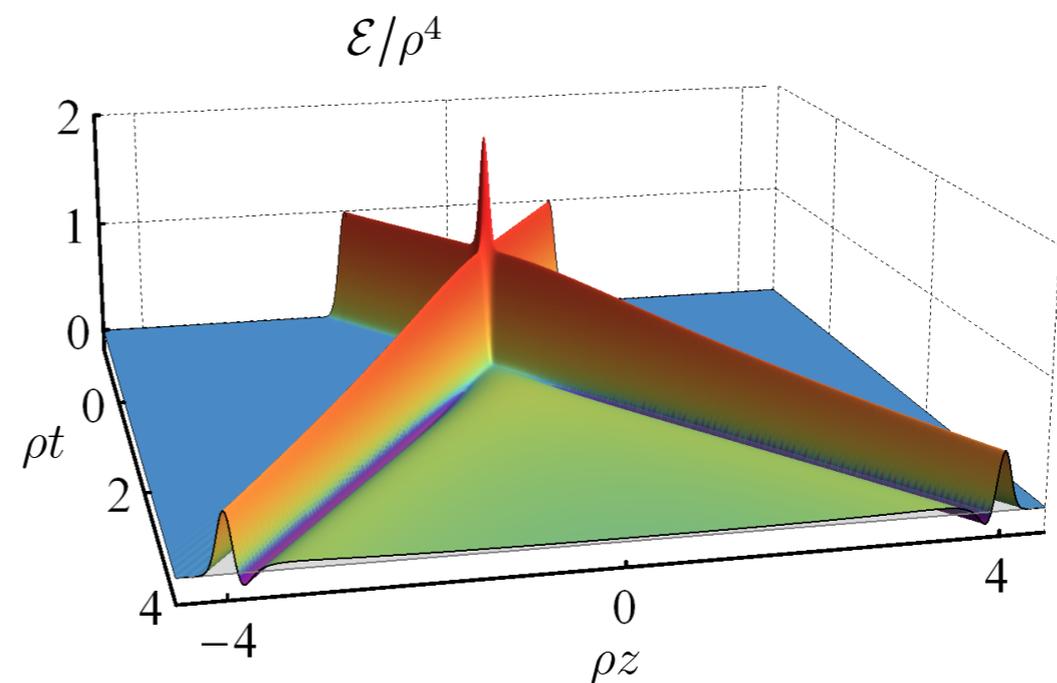
Strong-coupling approach

Gauge-gravity (AdS/CFT) duality: the strong-coupling limit of the gauge theory (N=4 SYM) is described by a weakly-coupled gravitational system in 4D AdS space.

System becomes “hydro-like” (no quasi-particles) on very short timescales and is characterized by the universal $\eta/s = 1/4\pi$.



Thick shock (low energy)



Thin shock (high energy)

QCD transport properties

Real-time dynamics \Leftrightarrow thermodynamics

Euclidean space and thermal fields:

$$t \rightarrow i\tau$$
$$0 \leq \tau \leq \beta$$
$$\beta = 1/(k_B T)$$

Schematically:

Spectral function ρ connects to the Euclidean correlator

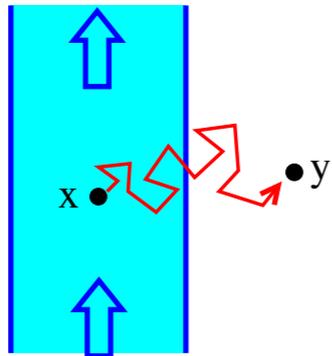
$$G_E(t) = \int_0^\infty d\omega \rho(\omega) \frac{\cosh \omega(\beta/2 - t)}{\sinh \omega\beta/2}$$

Kubo formula:

$$\eta = \pi \lim_{\omega \rightarrow 0} \lim_{\mathbf{k} \rightarrow 0} \frac{\rho(\omega, \mathbf{k})}{\omega}$$

Transport properties encode the long-wave length, long-time features of the underlying theory. This probes the E-correlator in the infrared sector — hard to control on the lattice!

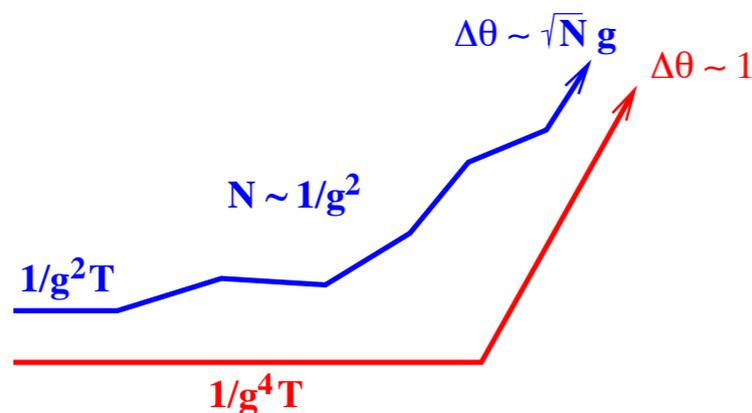
The shear viscosity



Dissipation

rate $\propto \eta \sim$ (mean free path) \times (energy-momentum density)

$$\frac{\eta}{s} \sim \tau_R T \sim \frac{\hbar}{k_B} \frac{\tau_R}{\tau_{\text{quant}}} \quad \text{what is the relaxation time?}$$



$$\sigma \sim \frac{g^4}{p^2}$$

$$\tau \sim (n\sigma v)^{-1} \sim (T^3 \sigma)^{-1}$$

1. typical collisions $p \sim m_D \sim gT$ with small deflection $\Delta\theta \sim p/E \sim g$
 - need to wait for a long time so to experience N kicks!
2. rare collisions $p \sim T$ with large deflection

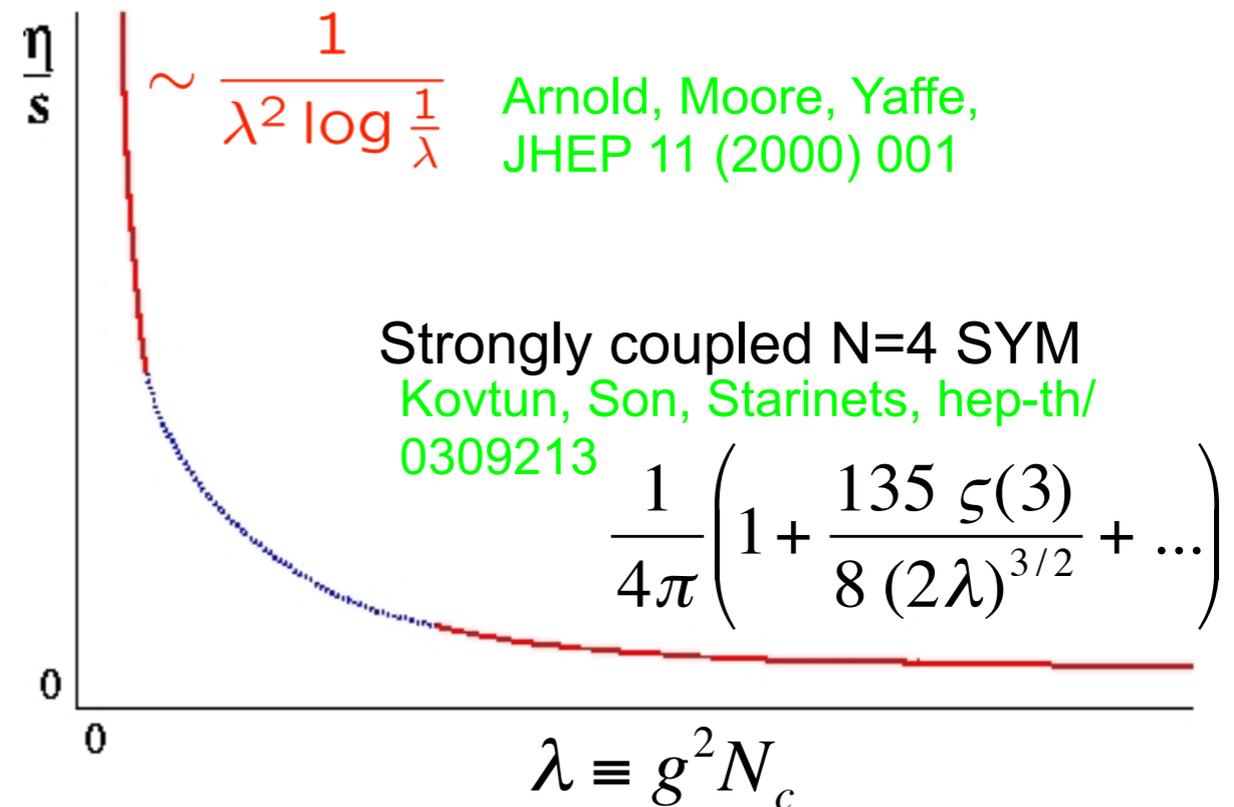
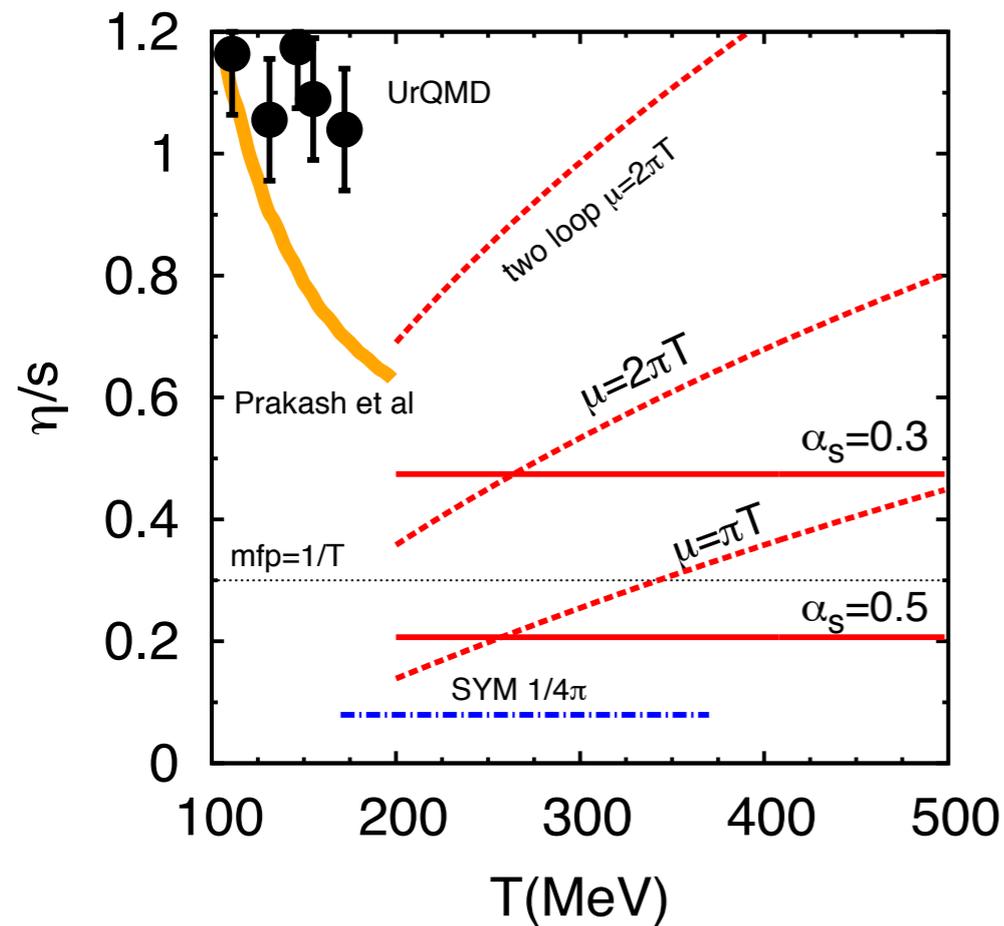
In both cases: $\tau_{\text{rand}} \sim \frac{1}{g^4 T \ln(1/g)}$

Measure of “fluidity”

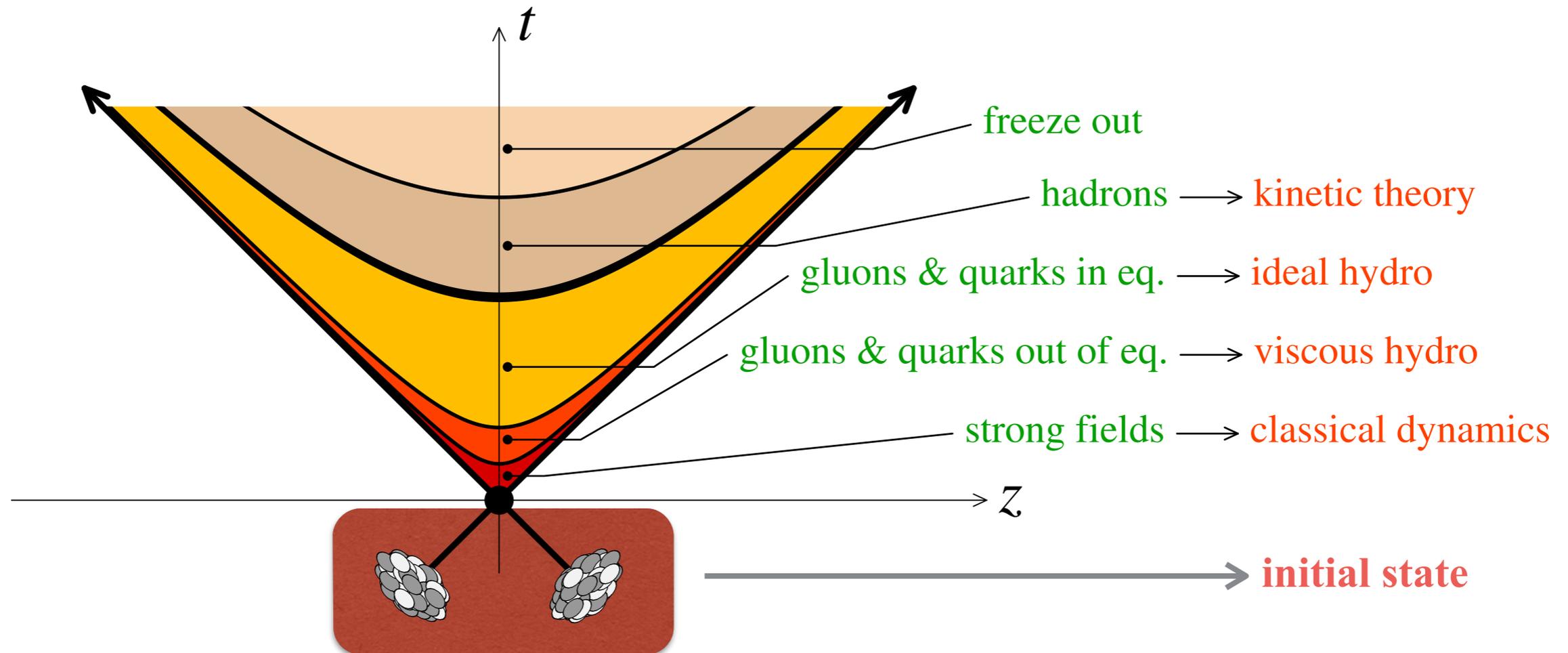
Leading log result from pert theory:

$$\eta \simeq \frac{T^3}{g^4 \ln(1/g)} f(\ln(1/g))$$

getting this log piece is difficult and involves the LPM effect (next lecture)!



Collision evolution



Formation time: $1 \text{ fm}/c$ ($3 \cdot 10^{-24} \text{ s}$)

Lifetime of QGP: $10 \text{ fm}/c$

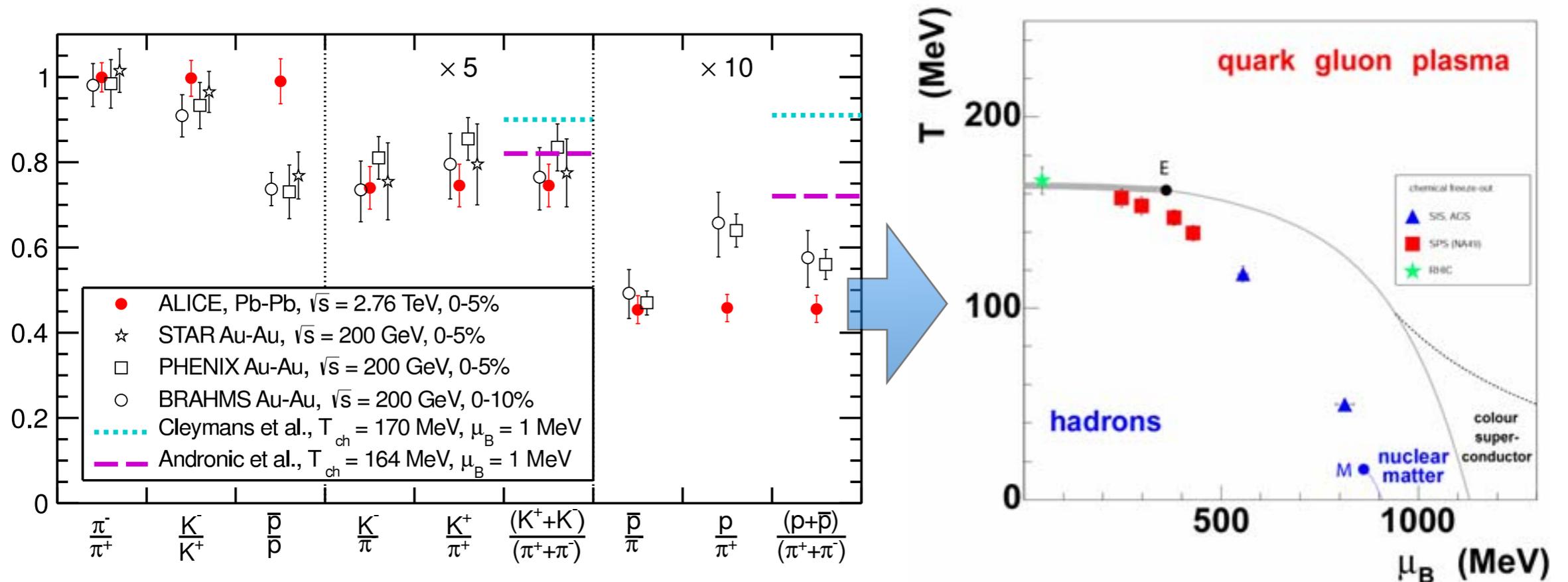
How does thermalization arise??

Statistical model

Grand canonical partition function $\ln Z_i(V, T, \mu_Q, \mu_B, \mu_S) = \pm(2s_i + 1) \frac{V}{2\pi^2} \int_0^\infty dp p^2 \ln [1 \pm \lambda_i \exp(-\beta\omega_i)]$

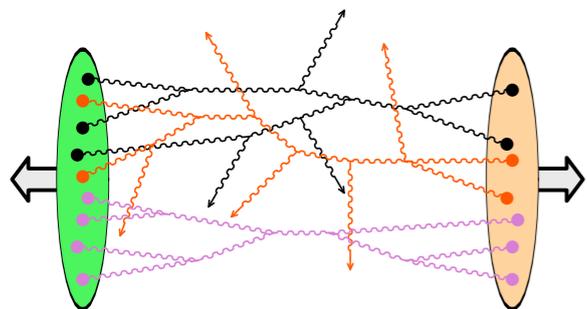
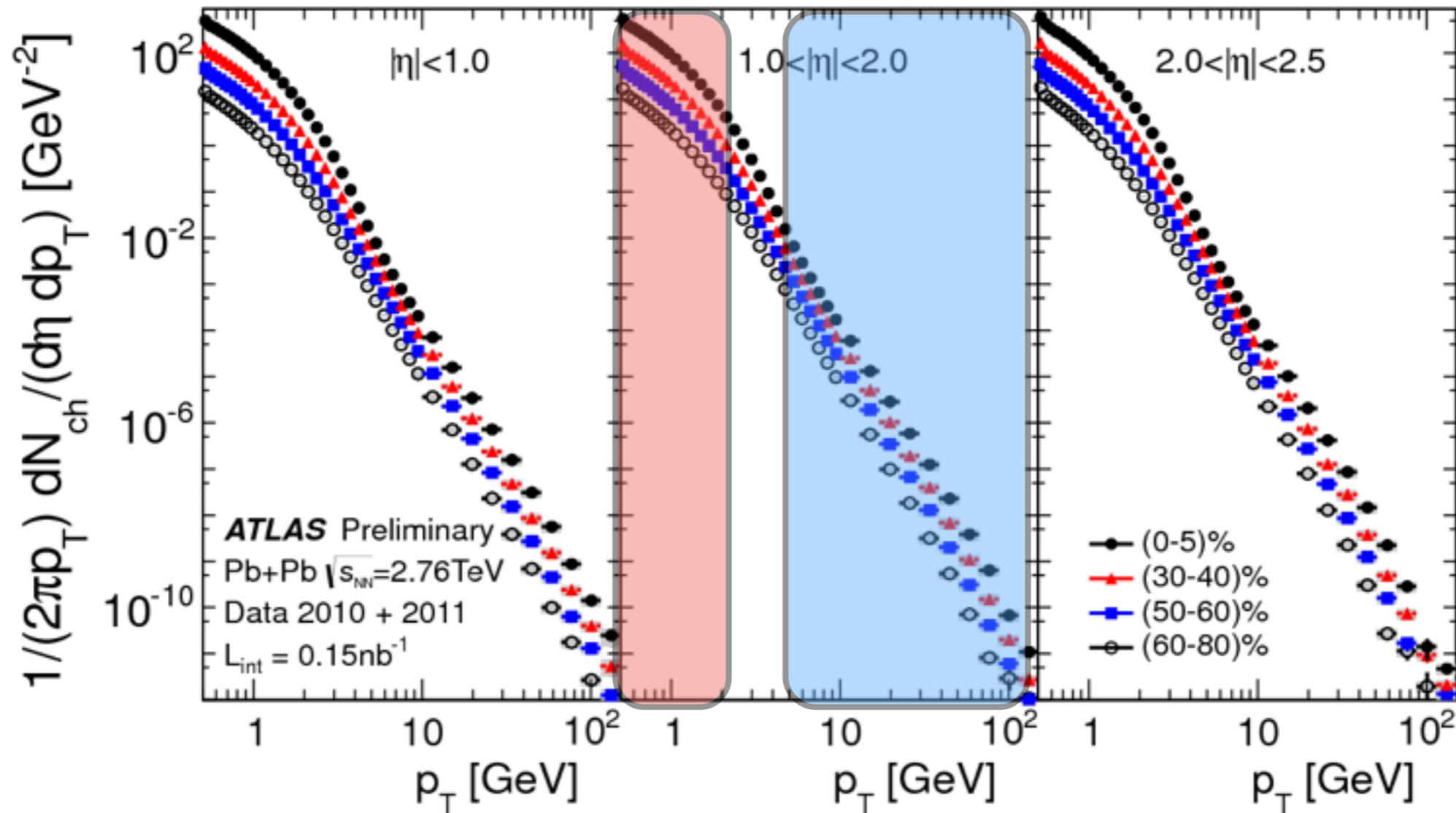
Fugacities:

$$\lambda_i(T, \mu_Q, \mu_B, \mu_S) = \exp [\beta(\mu_Q Q_i + \mu_B B_i + \mu_S S_i)]$$



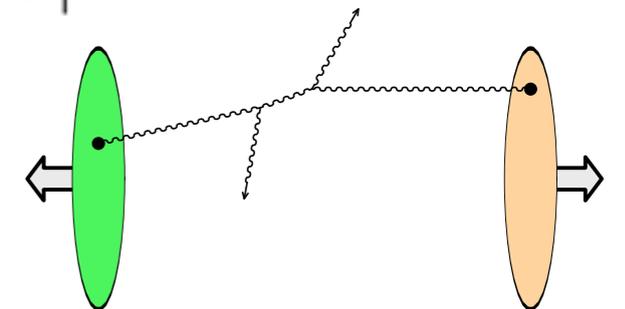
Thermal properties at the freeze-out surface.
Hadron yields are in chemical equilibrium.

Charged particle spectrum

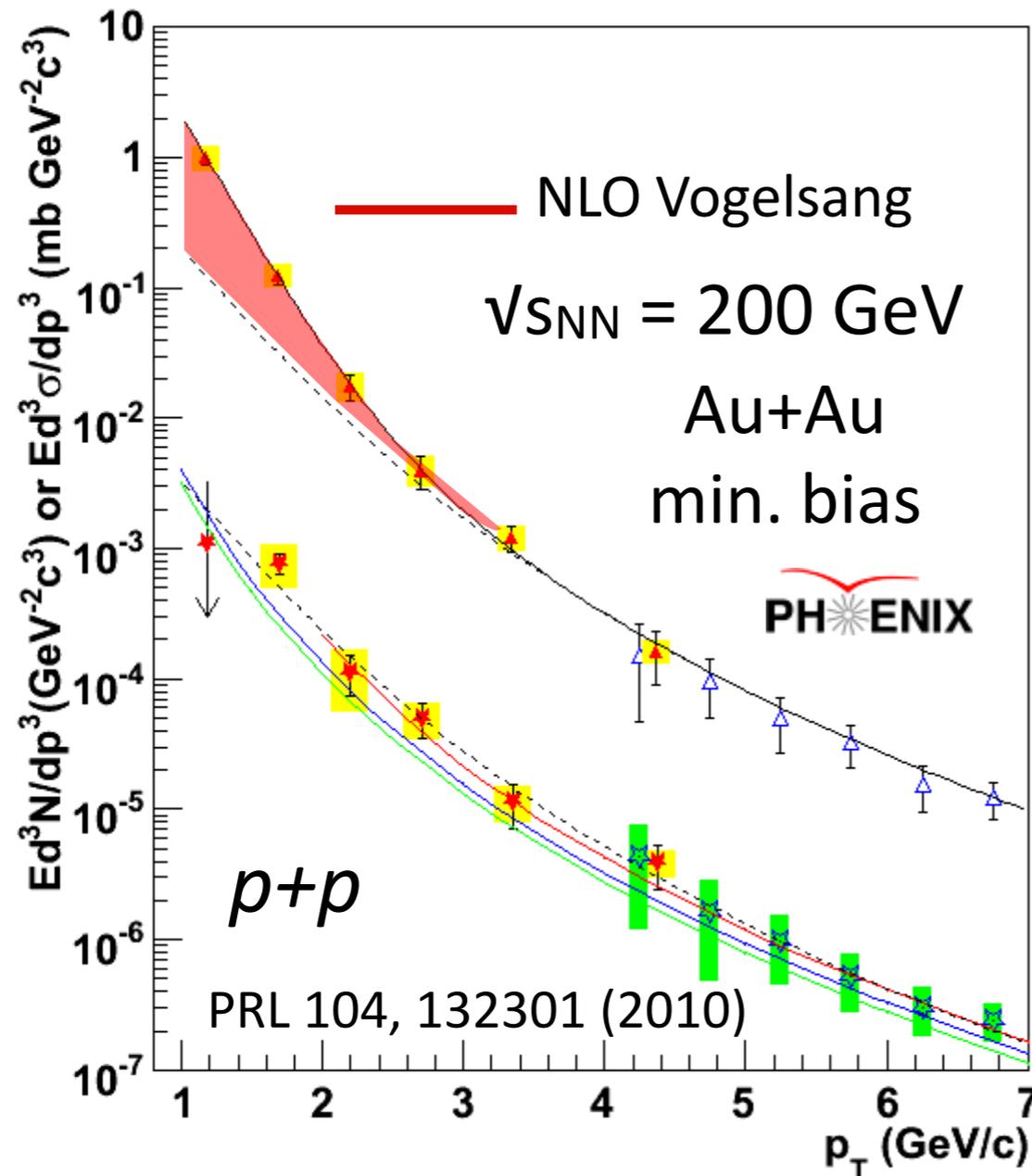


soft probes
 dense regime
 exponential

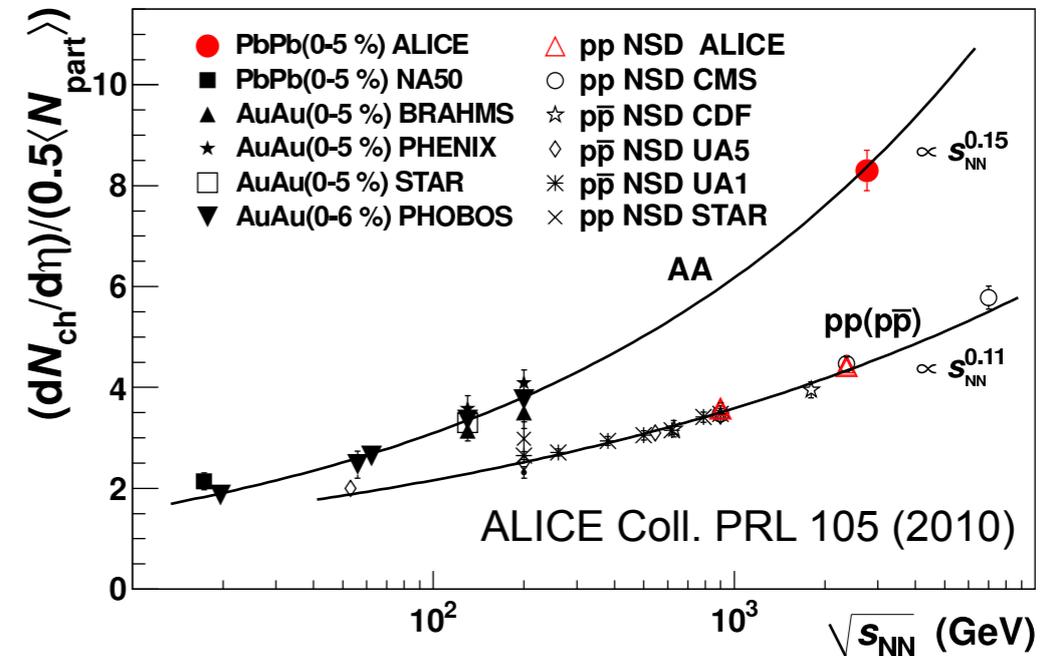
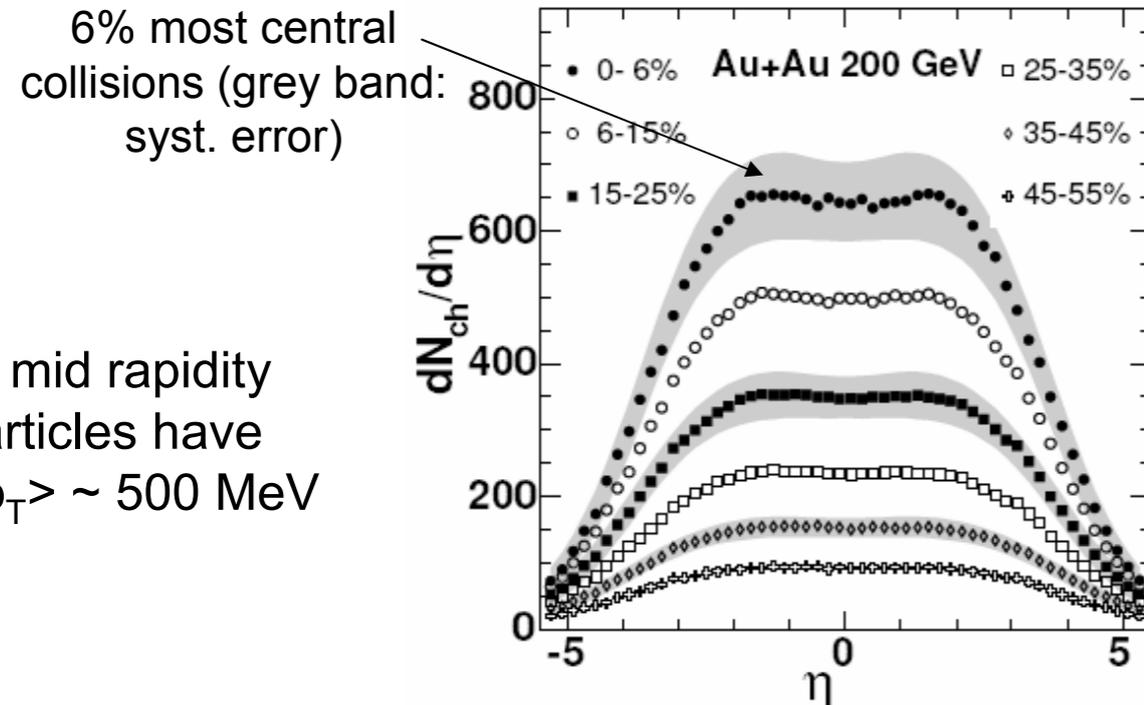
hard probes
 dilute regime
 power-like



Photon spectra



Deposited energy



- particle density is a measure of energy density
- almost flat distribution in pseudo-rapidity
- factor of 2 from SPS to RHIC and another from RHIC to LHC

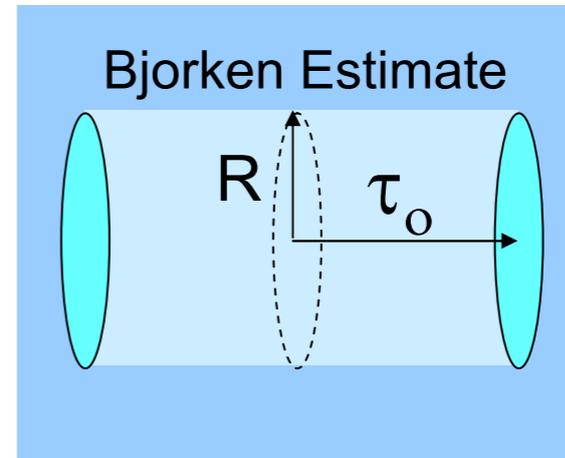
$$\frac{dE}{d\eta} \simeq \langle E \rangle \frac{dN_{ch}}{d\eta} \times \frac{3}{2} \simeq 6 - 12 \times 0.5 \text{ GeV} \times \frac{N_{part}}{2}$$

$$\frac{N_{part}}{2} \sim 170$$

Bjorken energy density estimate

At high energies most the matter is mostly transparent;
QGP is formed in the wake.

$$\eta_s = \frac{1}{2} \log \frac{t+z}{t-z} \simeq \frac{1}{2} \log \frac{p+p_z}{p-p_z} = \eta$$



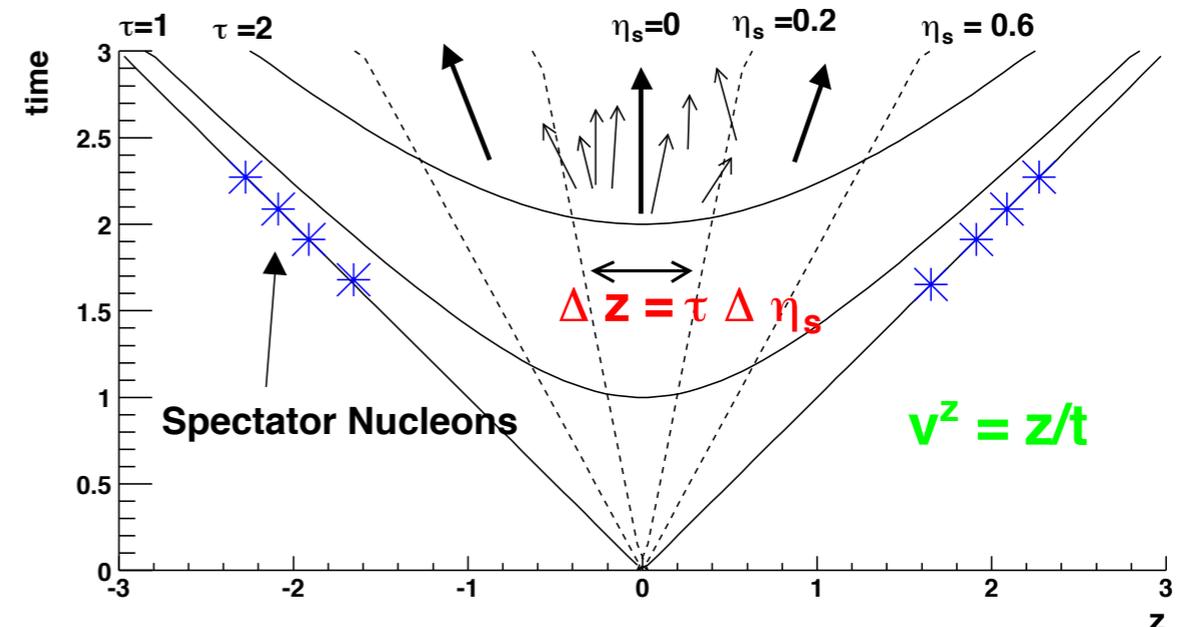
Matter at certain rapidity are created in the
same space-time slice.

$$\epsilon_{\text{Bj}} \simeq \frac{1}{\pi R^2} \frac{\Delta E}{\Delta z} \simeq \frac{1}{\pi R^2 \tau_0} \frac{\Delta E}{\Delta \eta}$$

- using $\tau_0 = 1$ fm and $R = 6$ fm

$$\epsilon_{\text{Bj}} \sim 5 - 10 \frac{\text{GeV}}{\text{fm}^3}$$

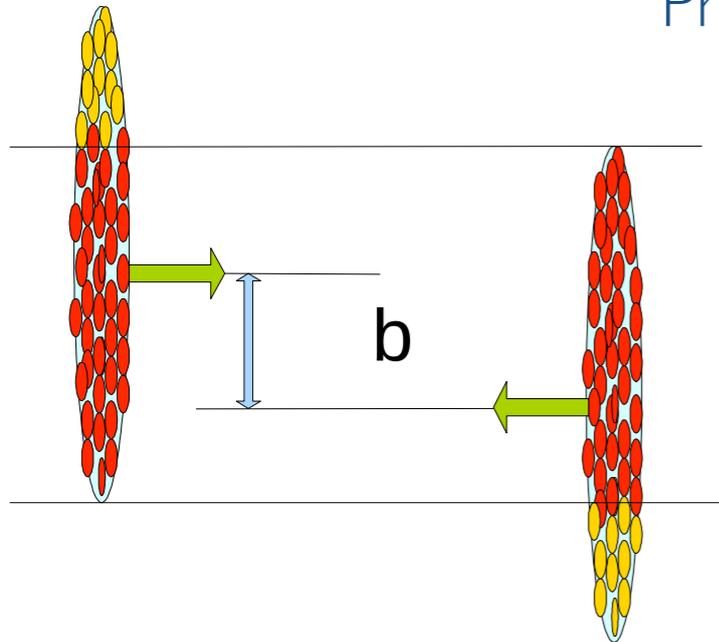
$$\rho_{\text{cold}} = 0.15 \frac{\text{GeV}}{\text{fm}^3}$$



Enough energy density to melt the nucleons!

The Glauber model

Probabilistic model of the collision.



Nuclear thickness: $T_A(\mathbf{b}) = \int_{-\infty}^{\infty} dz \rho(z, \mathbf{b})$

Optical approximation:

$$\int ds T_A(\mathbf{b}) T_B(\mathbf{b} - \mathbf{s}) \sigma_{NN}^{\text{inel}} \equiv T_{AB}(\mathbf{b}) \sigma_{NN}^{\text{inel}}$$

Probability of n scatterings at impact parameter b :

$$P(n, \mathbf{b}) = \binom{AB}{n} [1 - T_{AB}(\mathbf{b}) \sigma_{NN}^{\text{inel}}]^{AB-n} [T_{AB}(\mathbf{b}) \sigma_{NN}^{\text{inel}}]^n$$

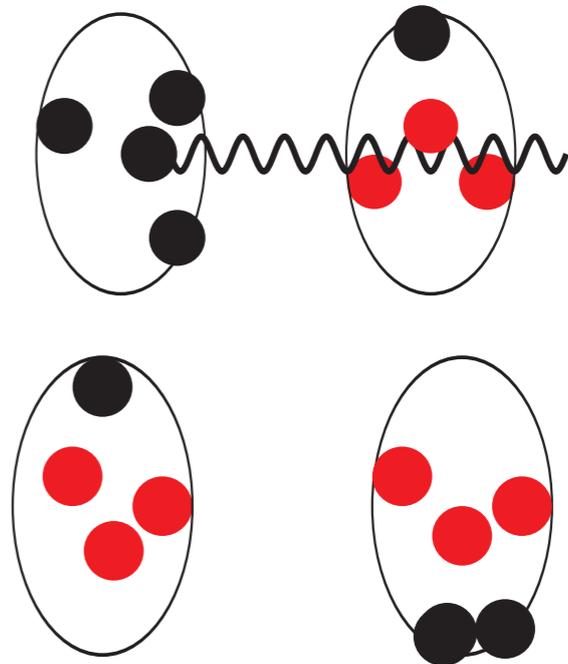
Sum over probabilities
= cross section:

$$\begin{aligned} \sigma_{AB}^{\text{inel}} &= \int d^2b [1 - (1 - T_{AB}(\mathbf{b}) \sigma_{NN}^{\text{inel}})^{AB}] \\ &\simeq \int d^2b \{1 - \exp[-AB T_{AB}(\mathbf{b}) \sigma_{NN}^{\text{inel}}]\} \end{aligned}$$

Centrality determination

Number of collisions:

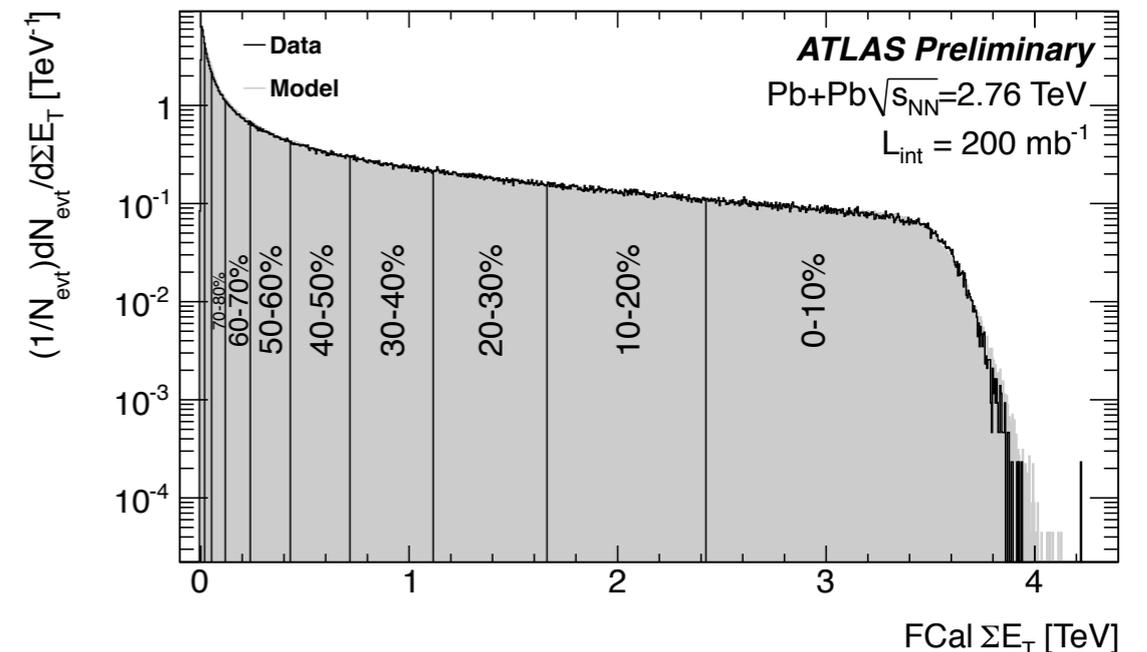
$$N_{\text{coll}}^{AB}(\mathbf{b}) = \sum_{n=0}^A n P(n, \mathbf{b}) = AB T_{AB}(\mathbf{b}) \sigma_{NN}^{\text{inel}}$$



Number of participants:

$$\begin{aligned} N_{\text{part}}^A(\mathbf{b}) &= \int ds B T_B(\mathbf{s}) \sigma_{pA}^{\text{inel}}(\mathbf{b} - \mathbf{s}) \\ &= \int ds B T_B(\mathbf{s}) \exp[-AT_A(\mathbf{b} - \mathbf{s}) \sigma_{NN}^{\text{inel}}] \end{aligned}$$

- events are (typically) categorized
 - soft :: N_{part}
 - hard :: N_{coll}
- how does energy or entropy scale with N_{part} & N_{coll} — not clear



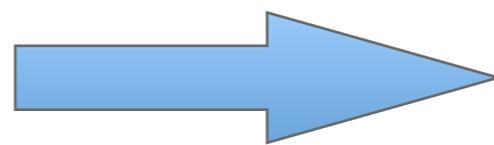
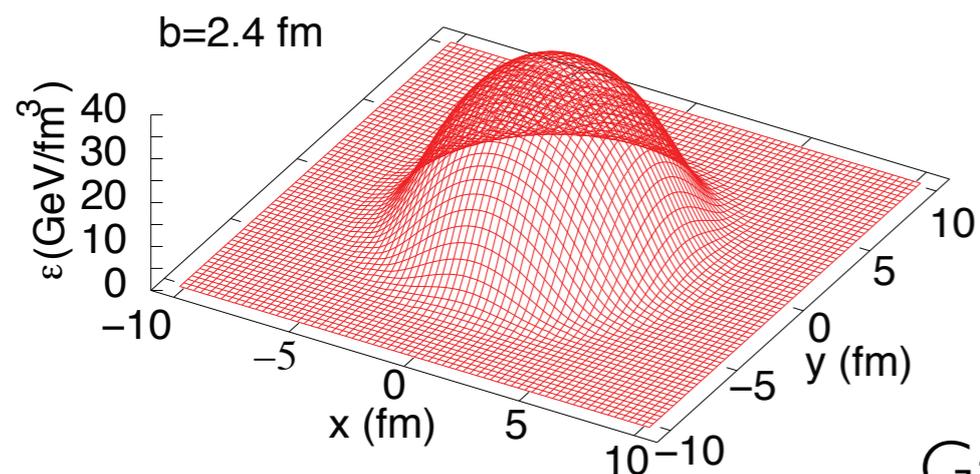
Initial conditions

Smooth distribution of wounded nucleons (participants)

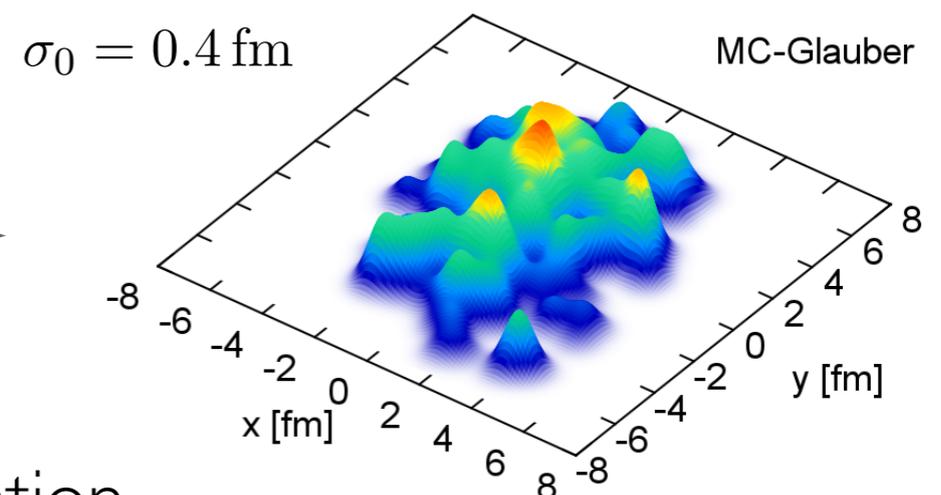
$$N_{\text{part}}(x, y, b) = T_A(x + b/2, y) \left[1 - (1 - \sigma_{\text{inel}}^{NN} T_B(x - b/2, y))^B \right] \\ + T_B(x - b/2, y) \left[1 - (1 - \sigma_{\text{inel}}^{NN} T_A(x + b/2, y))^A \right]$$

Binary collisions per area: $N_{\text{coll}}(x, y, b) = \sigma_{\text{inel}}^{NN} T_A(x + b/2, y) T_B(x - b/2, y)$

$$\epsilon \propto \frac{dN_{\text{ch}}}{d\eta} = \alpha N_{\text{part}} + \beta N_{\text{coll}}$$

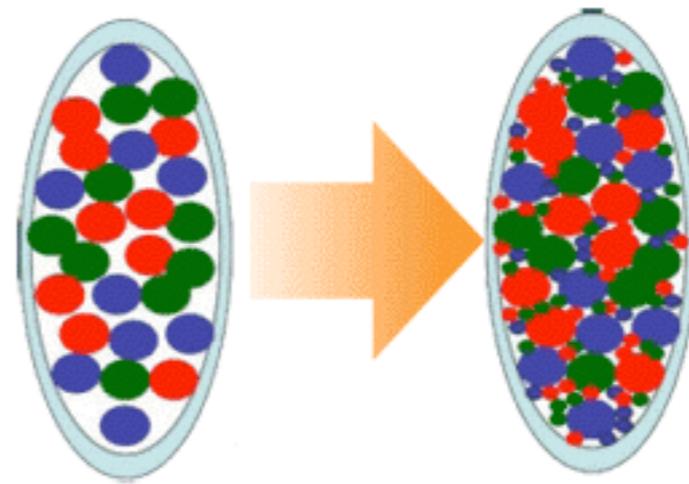


Gaussian randomization

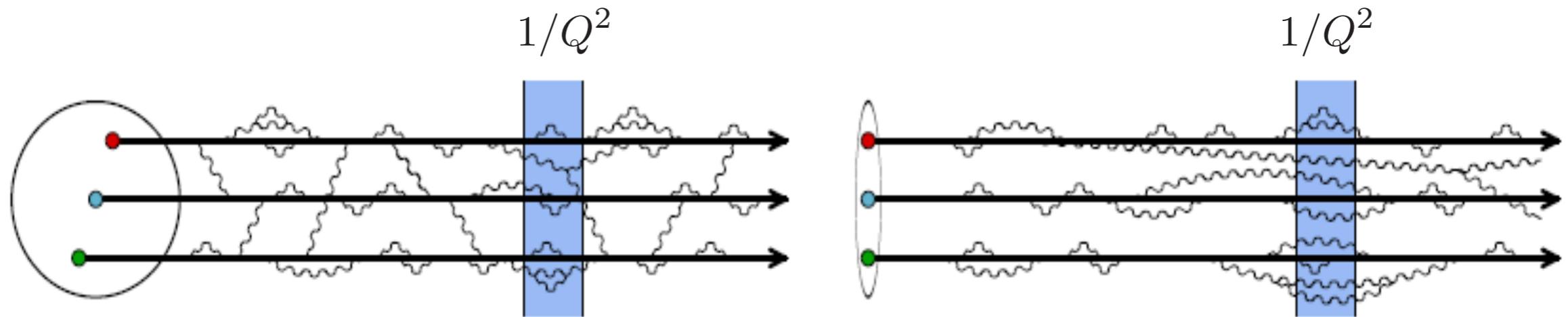


Inner life of nucleons

- the structure of the hadrons changes with energy
- partonic degrees of freedom starts taking over
- space-time picture changes
- related to the physics of infrared & collinear divergences

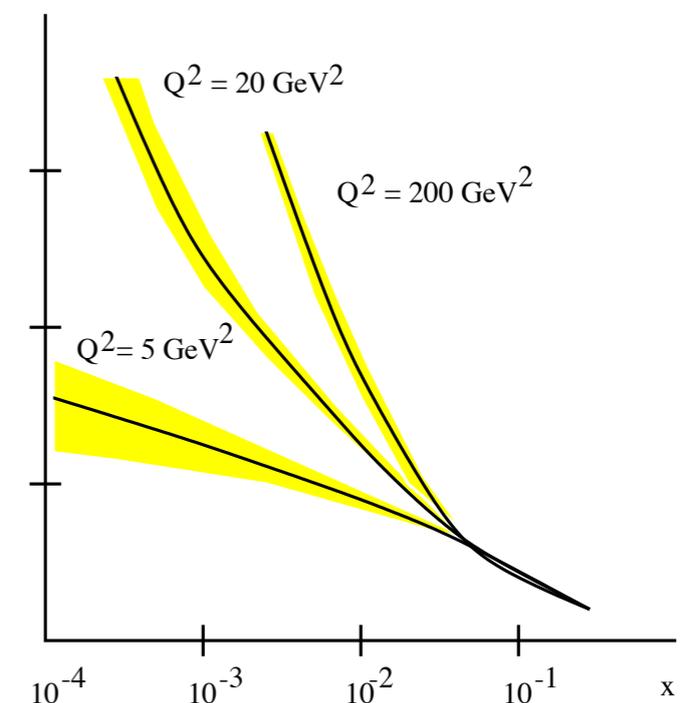


Digging out gluons

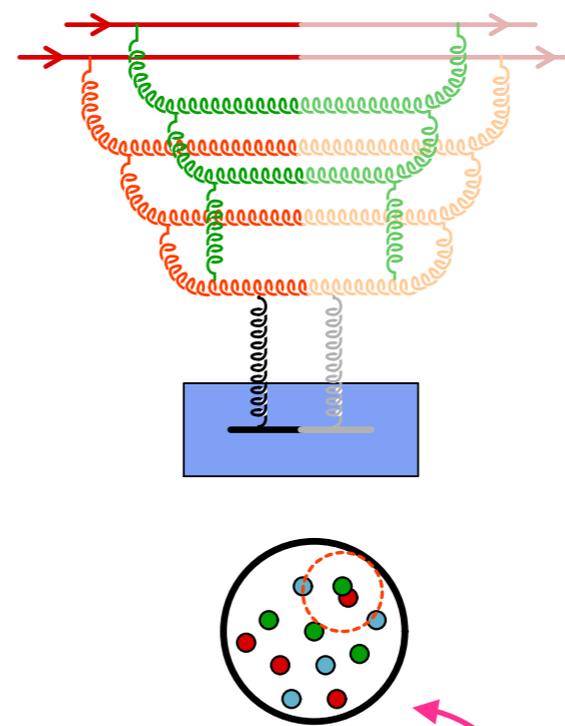
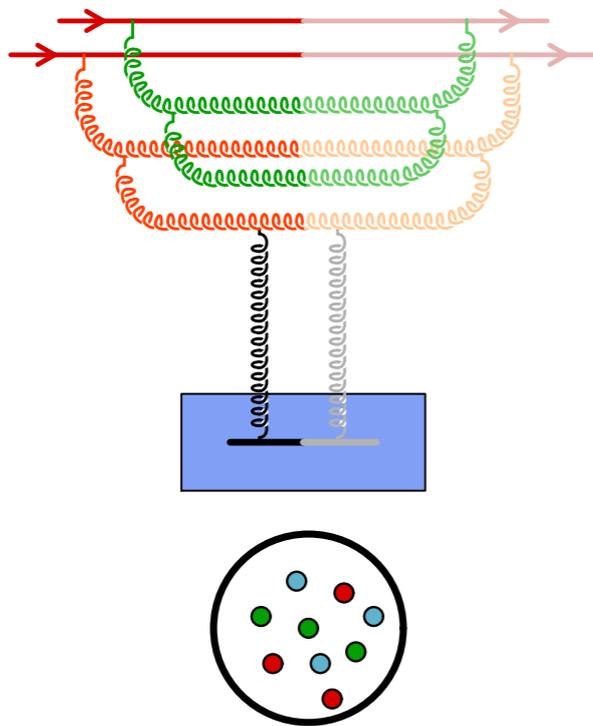


$$\begin{aligned}
 \Delta E &= -p_z + \sqrt{x^2 p_z^2 + k_\perp^2} + \sqrt{(1-x)^2 p_z^2 + k_\perp^2} \\
 &\approx \frac{k_\perp^2}{2x(1-x)p_z} \approx \frac{k_\perp^2}{2k_z}
 \end{aligned}$$

Lorentz time dilation: soft fluctuations can live over long timescales.
Lifetime vs. interaction time.



Dense environment



Number of gluons:

$$N(x, k_{\perp}) \sim \frac{xg(x, k_{\perp})}{\pi R^2}$$

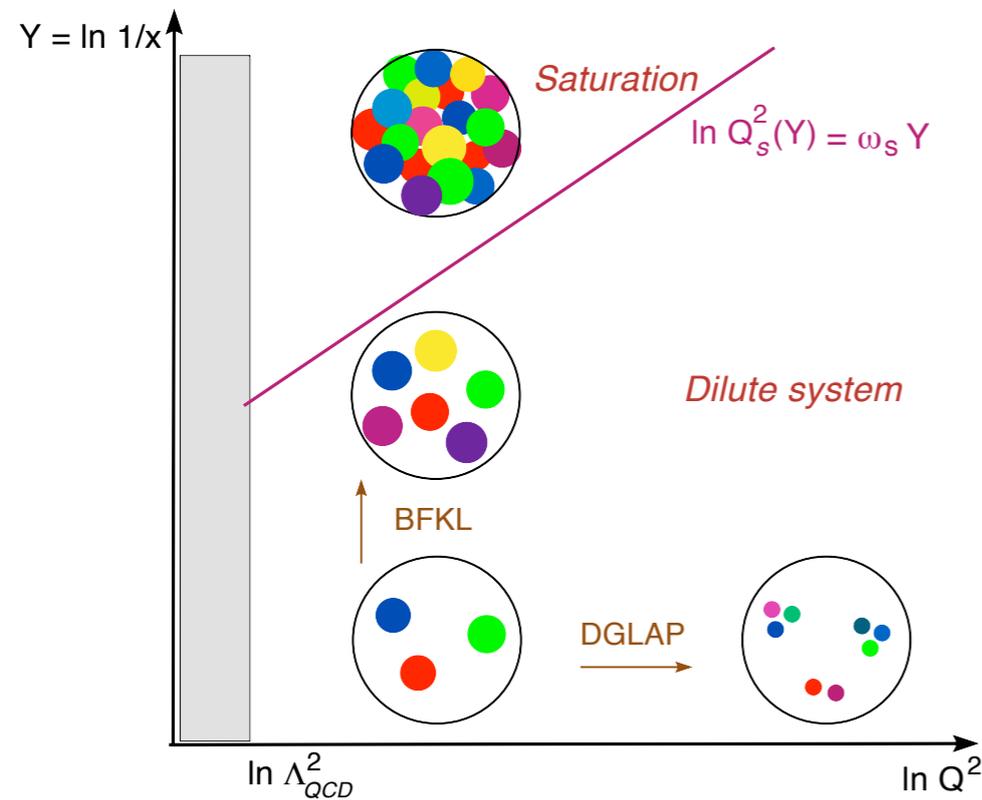
$$N\sigma_{\text{rec}} \geq 1 \Rightarrow k_{\perp} \leq Q_s(x)$$

Interaction cross-section:

$$\sigma_{\text{rec}} \sim \frac{\alpha_s}{k_{\perp}^2}$$

Saturation scale: $Q_s^2(x) \sim \frac{\alpha_s xg(x, Q_s)}{\pi R^2}$

One scale to rule them all



Hard scale of the problem ($Q_s \gg \Lambda_{\text{QCD}}$), governs particle production:

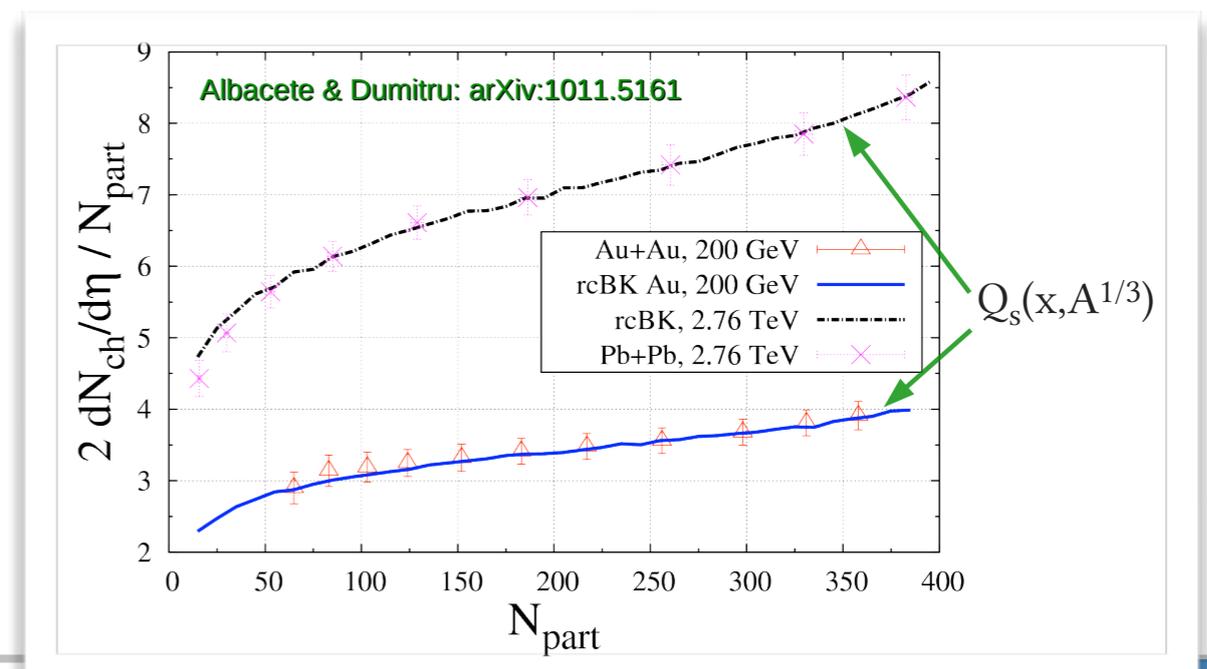
$$Q_s^2(x) \sim A^{1/3} x^{-\lambda}$$

Kinematics: $x_{1,2} = \frac{M_{\perp}}{\sqrt{s}} e^{\pm Y}$

$x \sim 10^{-2}$ at RHIC ($\sqrt{s} = 200$ GeV)

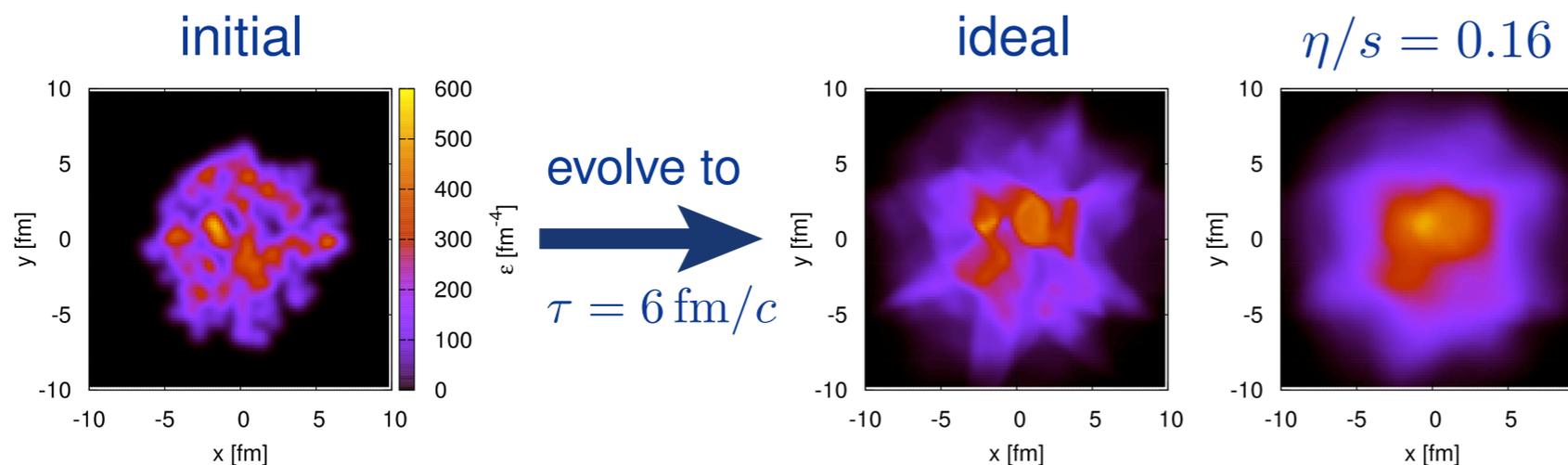
$x \sim 4 \times 10^{-4}$ at LHC ($\sqrt{s} = 5.5$ TeV)

State-of-the-art: Gluon distribution found from solving the Balitsky-Kovchegov equation with running coupling effects.

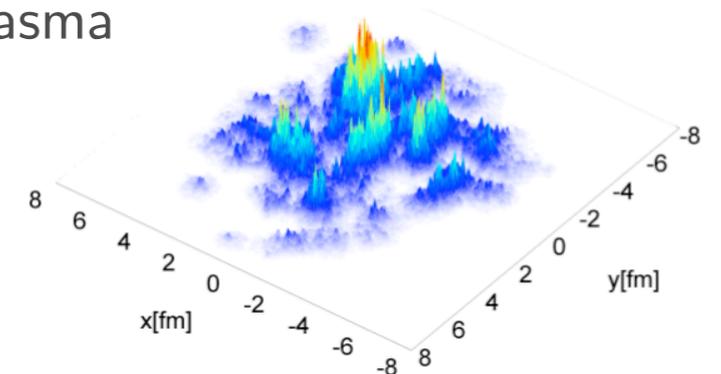


Evolving the state

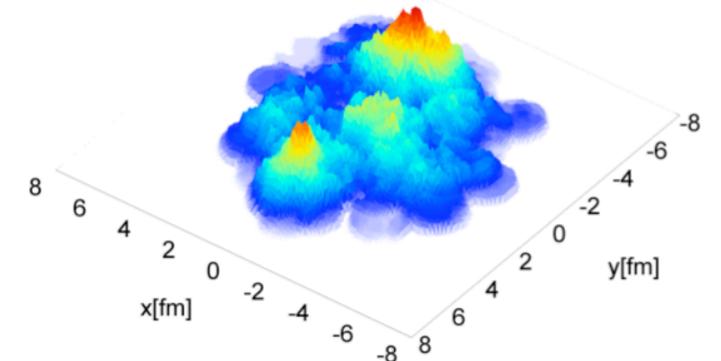
- initial color charge & energy density: sensitivity to size of initial-state fluctuations
- provides initial conditions for hydrodynamics
- can pin down the shear viscosity from observables



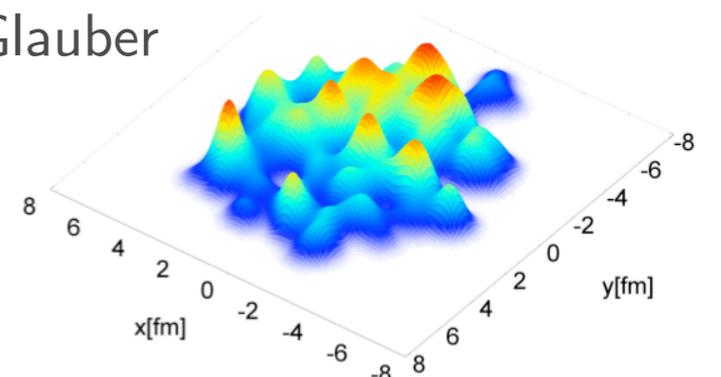
IP-Glasma



MC-KLN



MC-Glauber

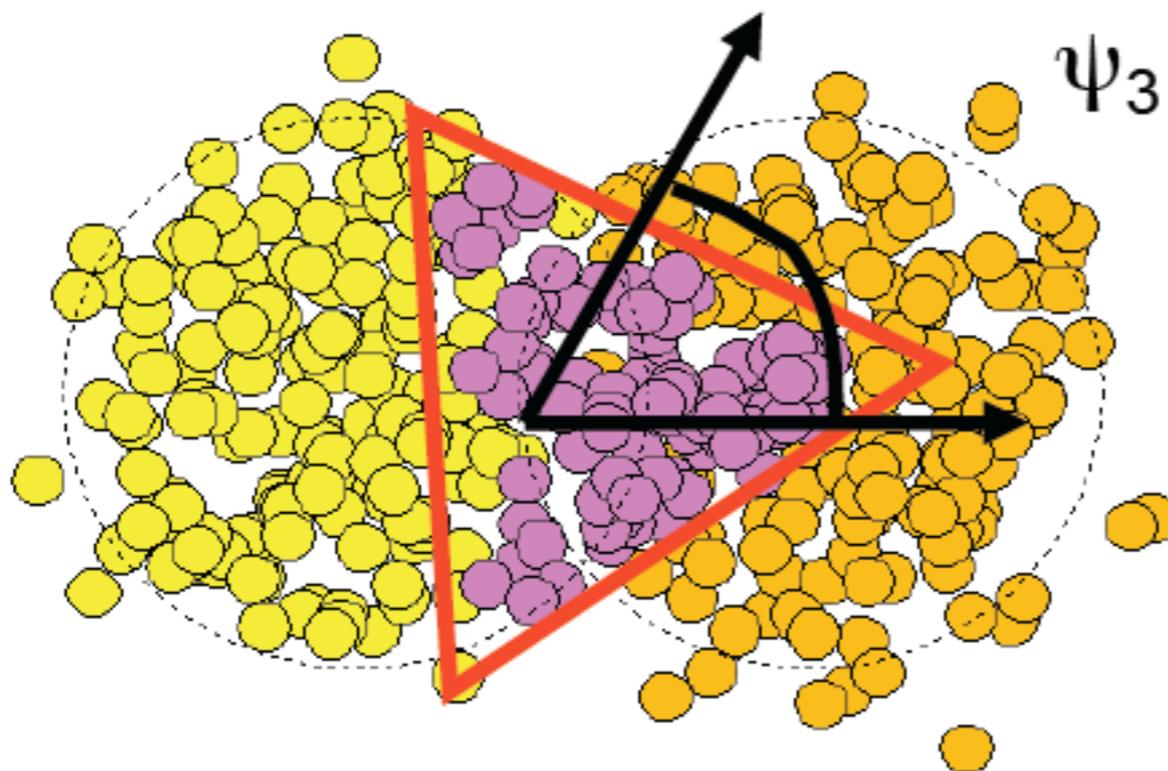


MUSIC B. Schenke, S. Jeon, C. Gale, Phys. Rev. C82, 014903 (2010); Phys.Rev.Lett.106, 042301 (2011)

Schenke, Tribedy, Venugopalan
1206.6805. PRL 108 (2012)

Non-central collisions

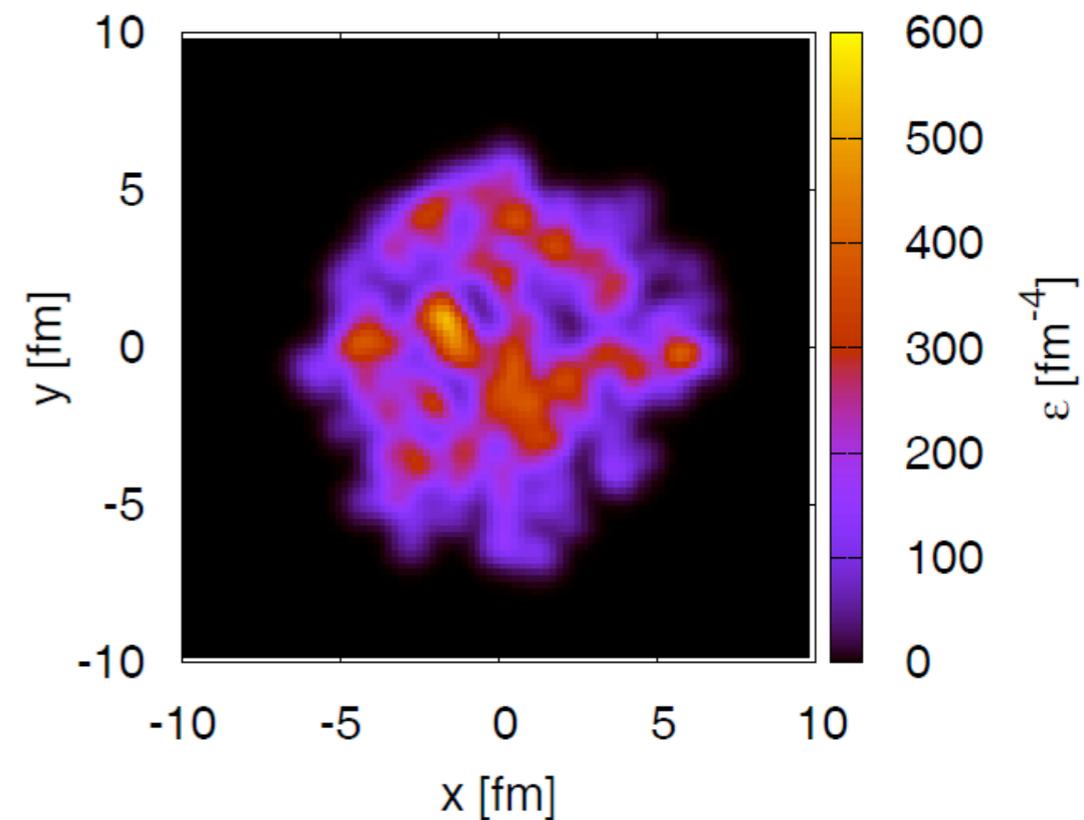
Glauber Model



B. Alver, G. Roland, PRC81 (2010) 054905

Viscous Hydro.

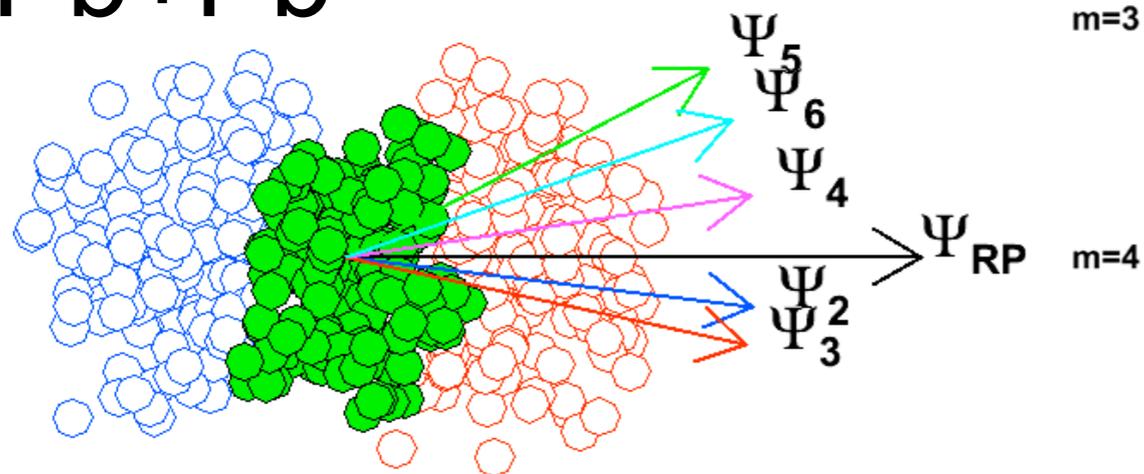
$\tau=0.4$ fm/c



B. Schenke, S. Jeon, C. Gale PRL 106, 042301

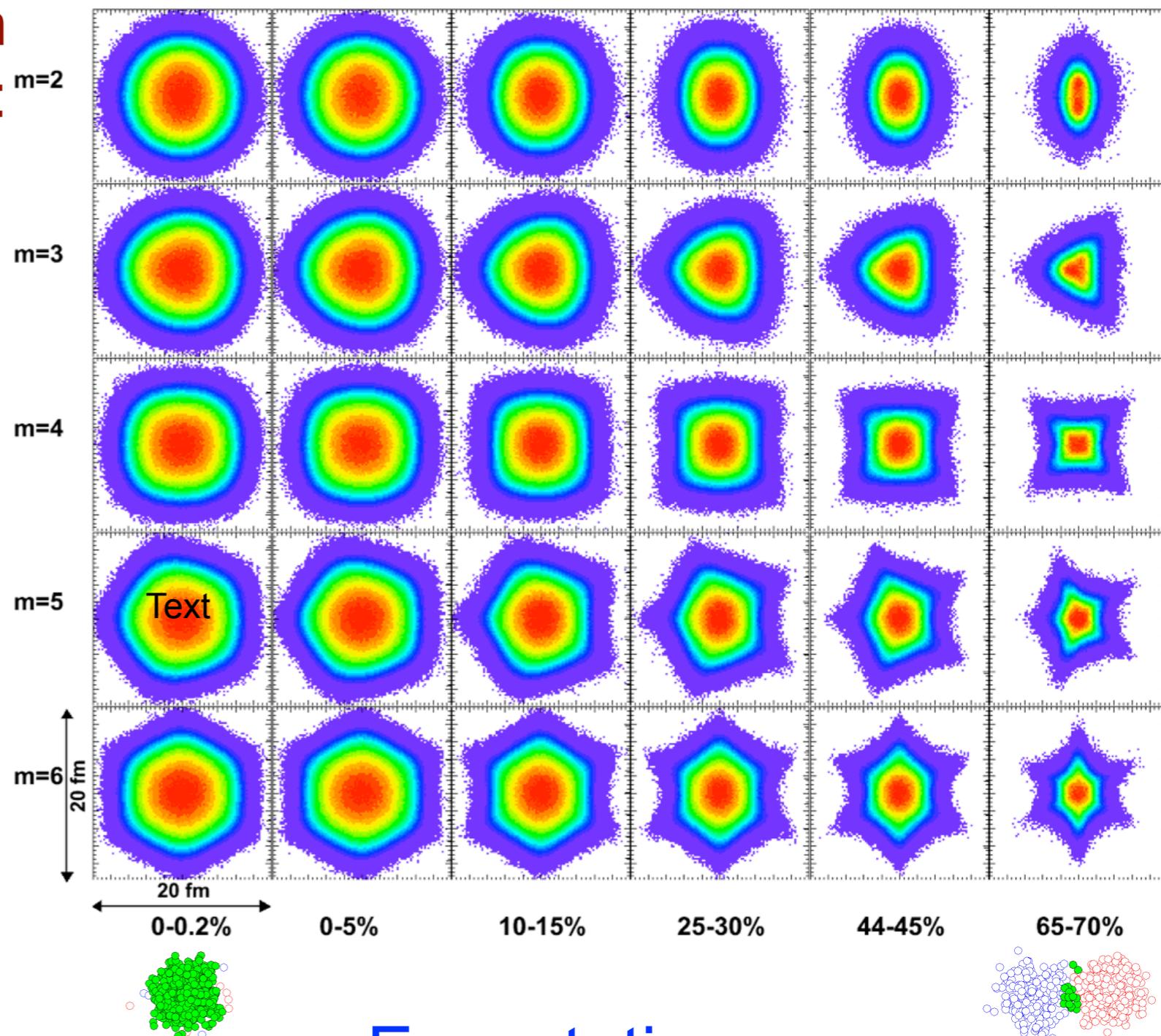
Participant densities with respect to participant plane:

Pb+Pb



Centrality $\propto 35\%$

$$\Psi_m^{pp} = \frac{1}{m} \tan^{-1} \left\{ \frac{\sum_{i=1}^{N_{part}} (r_i')^m \sin(m\phi_i')}{\sum_{i=1}^{N_{part}} (r_i')^m \cos(m\phi_i')} \right\} - \frac{\pi}{m}$$



Measure:

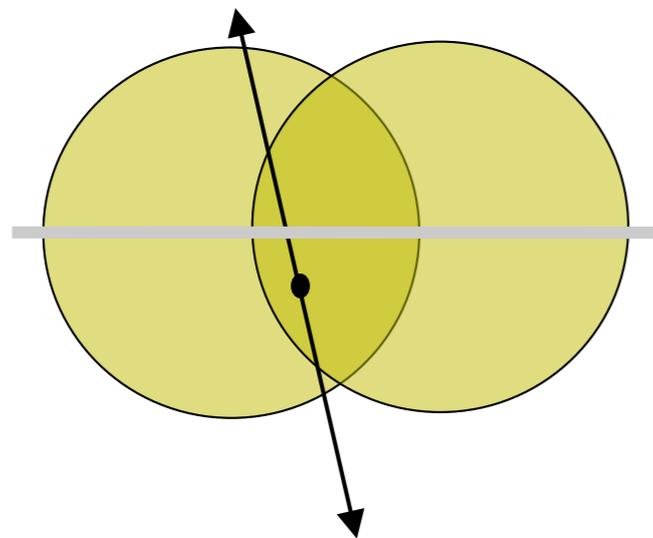
$$\frac{dN}{d(\phi - \Psi_m)} \propto 1 + \sum_{n \geq m} 2v_n^{\text{obs}} \{ \Psi_m \} \cos[n(\phi - \Psi_m)]$$

Expectation:

$$v_n = (\text{medium evolution}) \times \varepsilon_n$$

$$\Psi_m \approx \Psi_m^{pp}$$

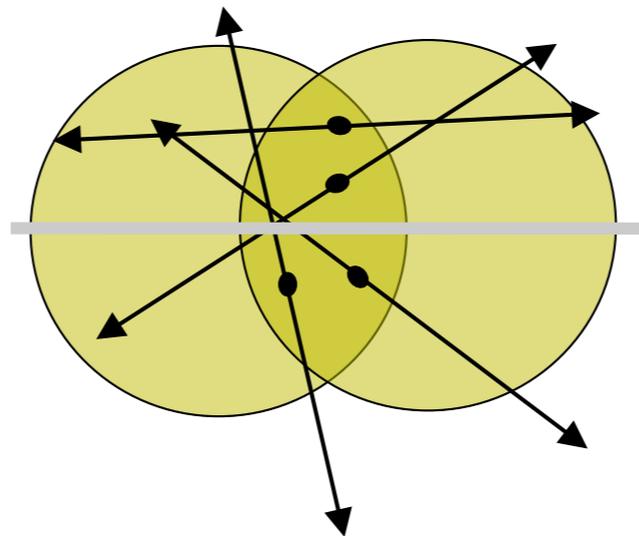
Azimuthal asymmetries



dilute case

YES

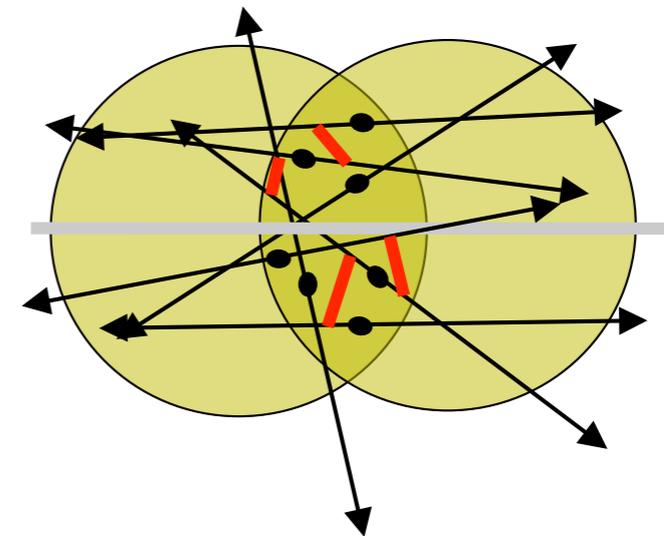
NO



free streaming

YES (smaller $\sim 1/\sqrt{N}$)

NO

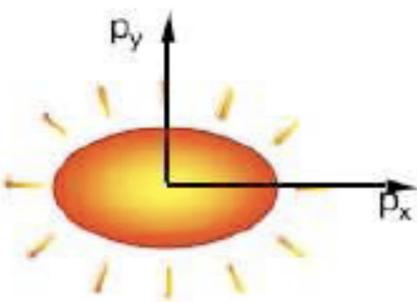
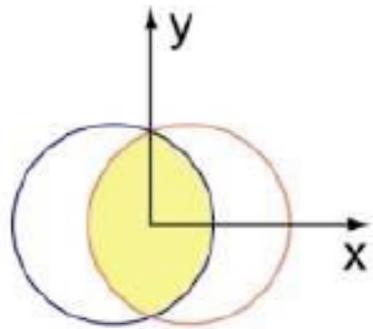


final-state interactions

YES

YES (collective component)

courtesy:
U.A. Wiedemann
(Spätind 2012)



- degree of final state interactions determine how effectively spatial asymmetries transform to momentum asymmetries

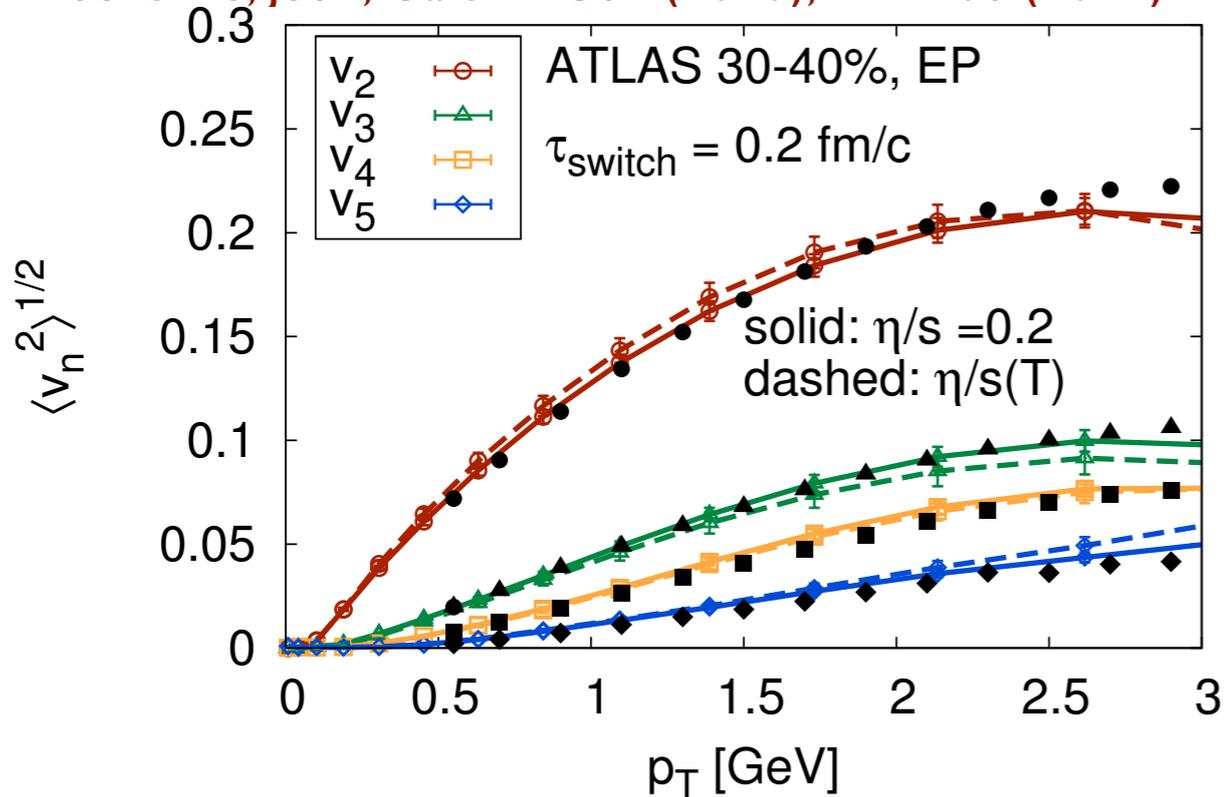
- limit $\sigma \rightarrow \infty$: hydrodynamical limit

$$v_n = \langle \cos [n(\phi - \psi_n)] \rangle$$

reaction plane

The QGP flows

Schenke, Jeon, Gale PRC82 (2010), PRL 106 (2011)



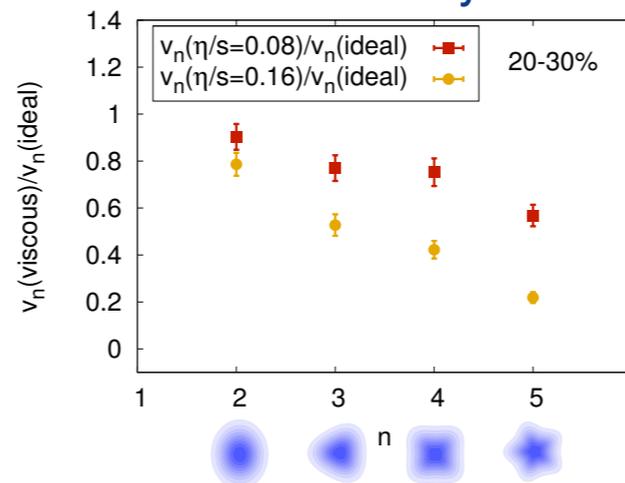
- transport coefficients can be found
- hierarchy of v_n coefficients consistent with almost perfect liquid

$$0.07 \leq \eta/s \leq 0.43$$

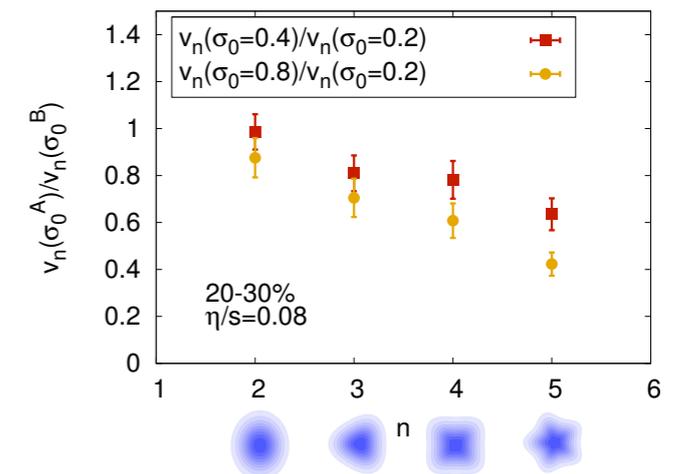
Luzum, Ollitrault et al.

- higher harmonics are more sensitive to viscosity and granularity

viscosity



initial state granularity



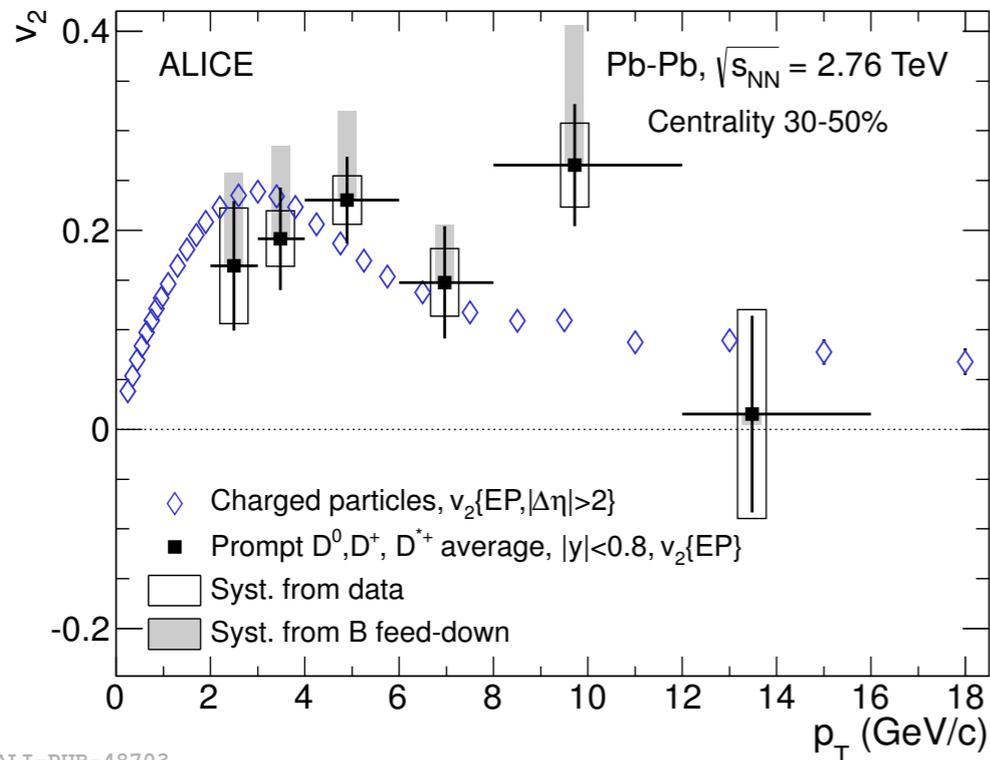
RHIC Scientists Serve Up "Perfect" Liquid

New state of matter more remarkable than predicted -- raising many new questions

April 18, 2005

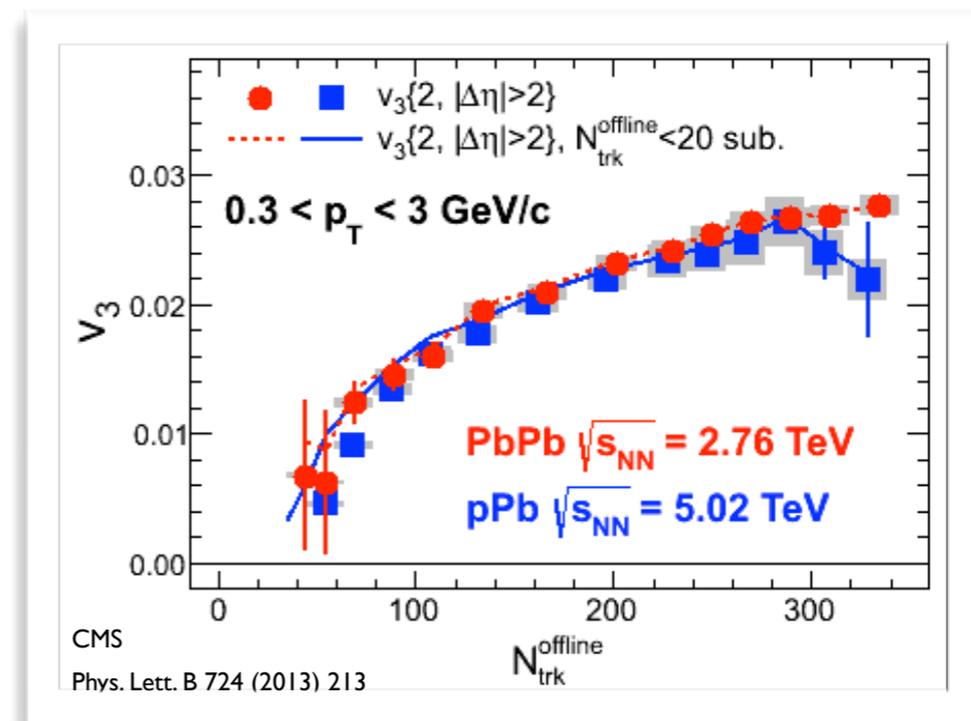
TAMPA, FL -- The four detector groups conducting research at the [Relativistic Heavy Ion Collider](#) (RHIC) -- a giant atom "smasher" located at the U.S. Department of Energy's Brookhaven National Laboratory -- say they've created a new state of hot, dense matter out of the quarks and gluons that are the basic particles of atomic nuclei, but it is a state quite different and even more remarkable than had been predicted. In [peer-reviewed papers](#) summarizing the first three years of RHIC findings, the scientists say that instead of behaving like a gas of free quarks and gluons, as was expected, the matter created in RHIC's heavy ion collisions appears to be more like a *liquid*.

Further puzzles



Small system (p+Pb) shows very similar features — are we completely dominated by fluctuations?

- D meson (= u,d + c)
- mass hierarchy follows from perturbation theory
- in HIC, heavy-quarks behave (flow etc) very similarly to the light quarks
- $T_{\text{eff}} \sim m_Q$? strong-coupling dynamics?



Summary: QCD fluid in HIC

- perturbative techniques give fundamental insight
- experimental features point to fluid-like features of the formed plasma — good description of data!
- solutions of AdS/CFT shares many of the same features (thermalization, small viscosity)
- what is the gravity dual of “real” QCD? how can we access the strong-coupling regime of QCD otherwise?