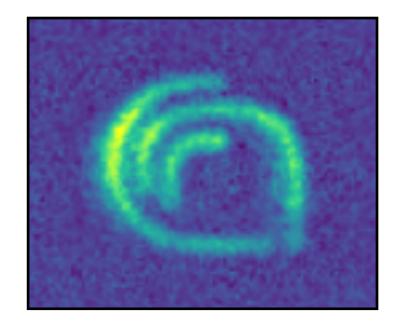
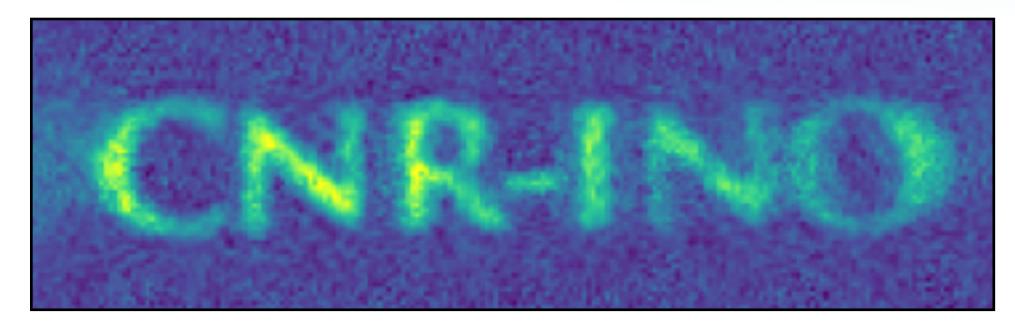
A TUNABLE JOSEPHSON JUNCTION BETWEEN BEC-BCS CROSSOVER SUPERFLUIDS

Francesco Scazza - CNR-INO and LENS, Università di Firenze

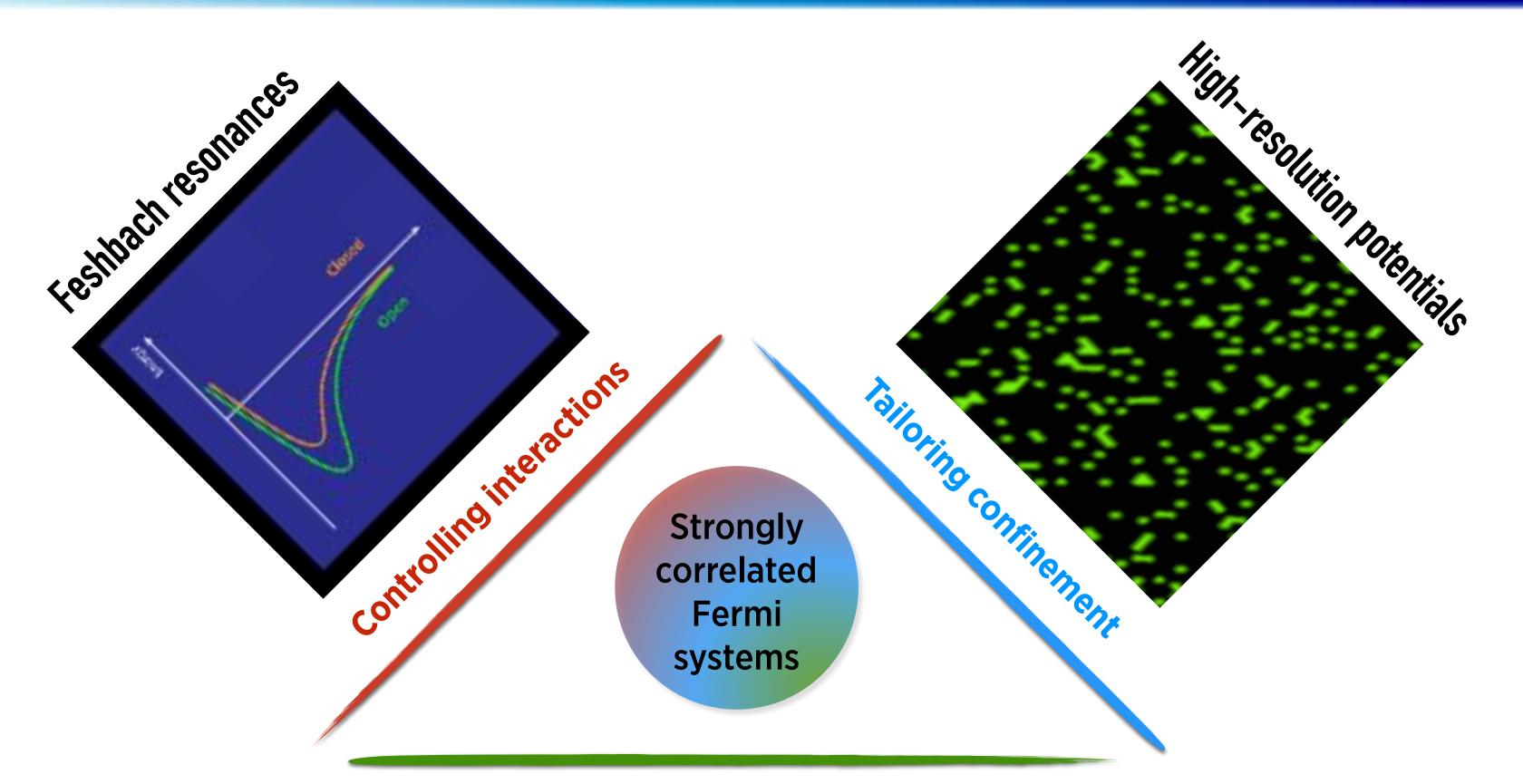
Atomtronics 2019 Centro de Ciencias de Benasque Pedro Pascual - 9 May 2019



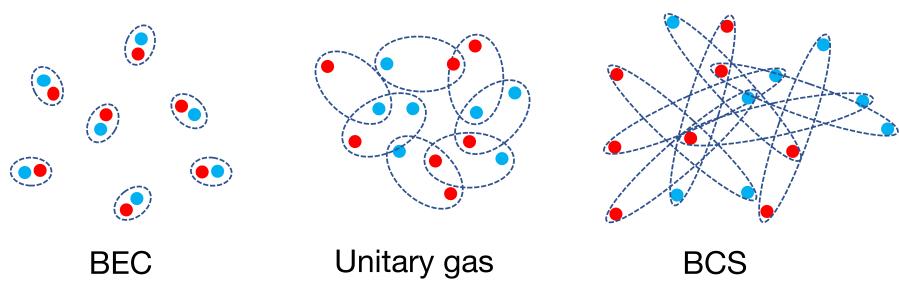




ULTRACOLD ATOMIC FERMI GASES



Tuning particle statistics and correlations

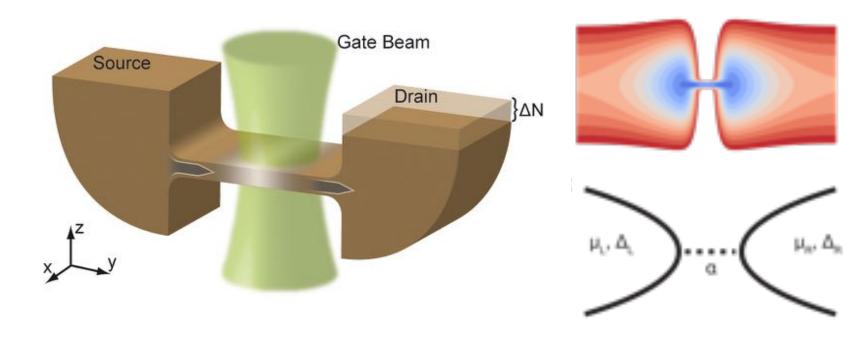






QUANTUM TRANSPORT WITH FERMI GASES

Transport through narrow ballistic channels



ETH, Zürich

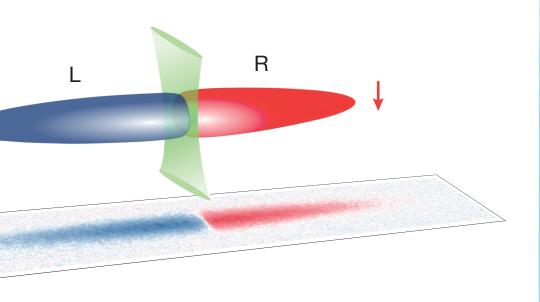
Brantut et al., *Science* **337** (2012) Stadler et al., *Nature* **491** (2012) Krinner et al., Phys. Rev. Lett. 110 (2013) Krinner et al., *Nature* **517** (2015) Husmann et al., *Science* **350** (2015)

100 µm

For a review: Krinner et al., J. Phys.: Condens. Matter 29 (2017)



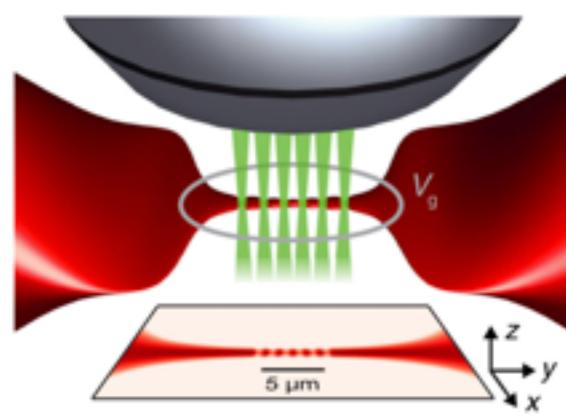
Spin and heat transport



MIT (Boston), Univ. Toronto, LENS (Florence), ETH (Zürich)

```
Sommer et al., Nature 472 (2011)
Brantut et al., Science 342 (2013)
Bardon et al., Science 344 (2014)
Krinner et al., PNAS 113 (2016)
Valtolina et al., Nature Phys. 13 (2017)
Lebrat et al., arXiv:1902.05516 (2019)
```

Tunnelling through mesoscopic structures



ETH (Zürich), LENS (Florence)

Valtolina et al., *Science* **350** (2015) Burchianti et al., Phys. Rev. Lett. 120 (2018) Lebrat et al., *Phys. Rev. X* 8 (2018)



















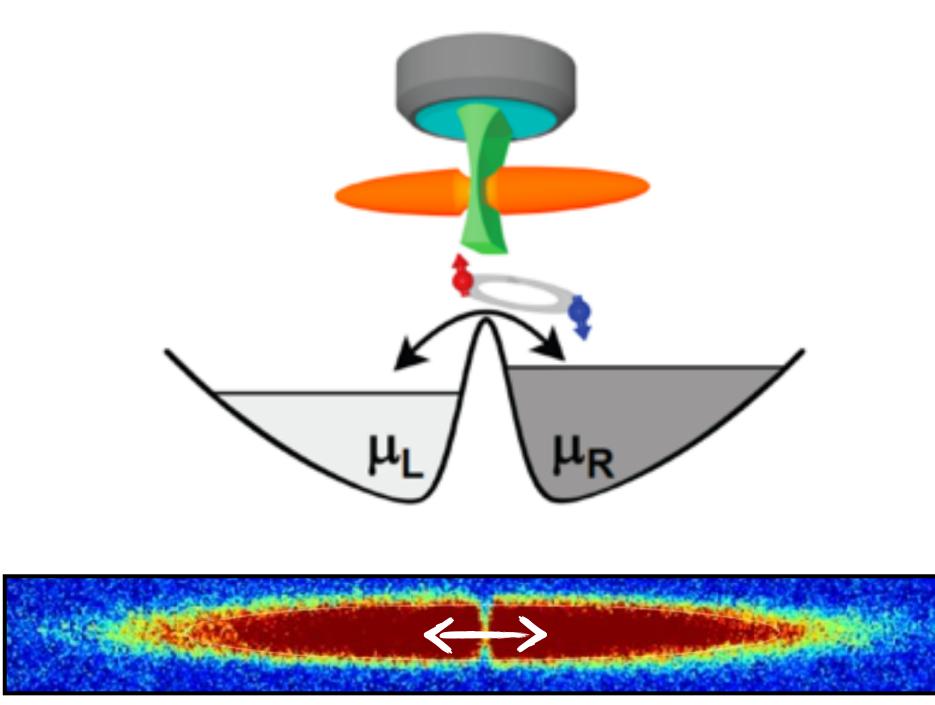






FERMIONIC MANY-BODY DYNAMICS AT LENS

Superfluid transport in tunnel junctions

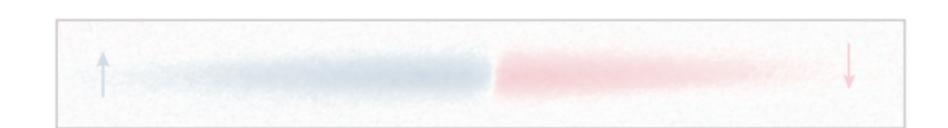


Weak-link geometry between Fermi superfluids → tuneable Josephson junction

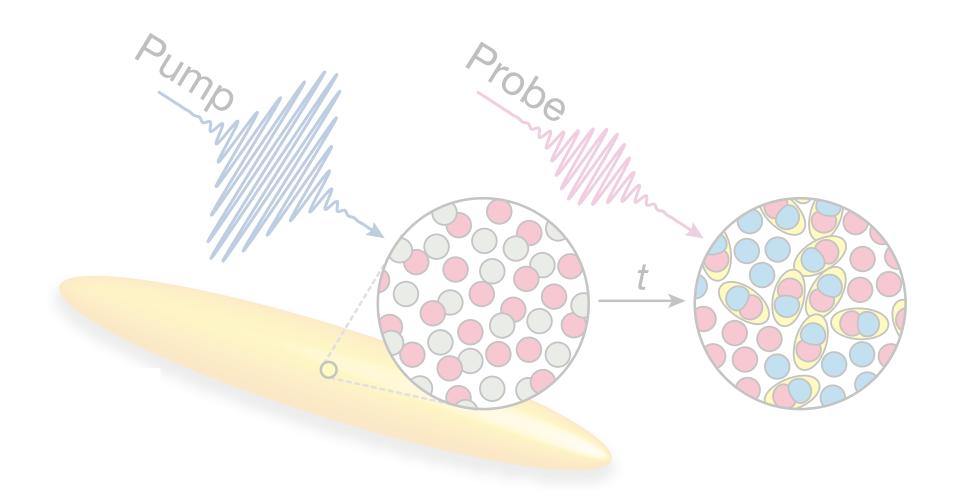
Critical superflow and dissipation mechanisms Valtolina et al., *Science* **350** (2015) Burchianti et al., *Phys. Rev. Lett.* **120** (2018) Kwon et al., in preparation (2019)



Spin dynamics in repulsive Fermi gases



Spin diffusion at an artificial domain wall Valtolina et al., *Nature Phys.* **13** (2017)



Pump-probe spectroscopy of repulsive Fermi gas Scazza et al., Phys. Rev. Lett. 118 (2017) Amico et al., *Phys. Rev. Lett.* **121** (2018)

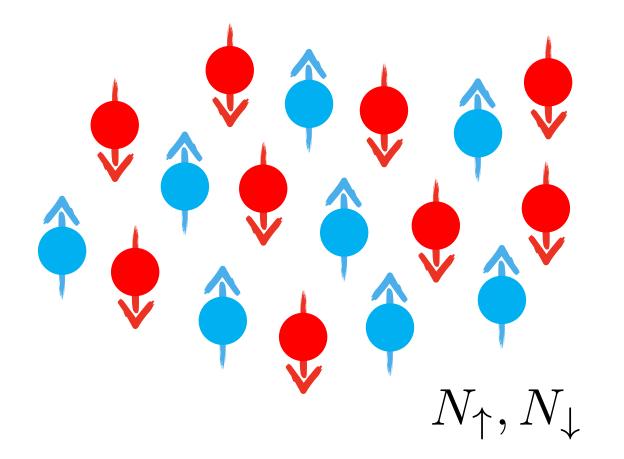
Min

 $\overline{>}$

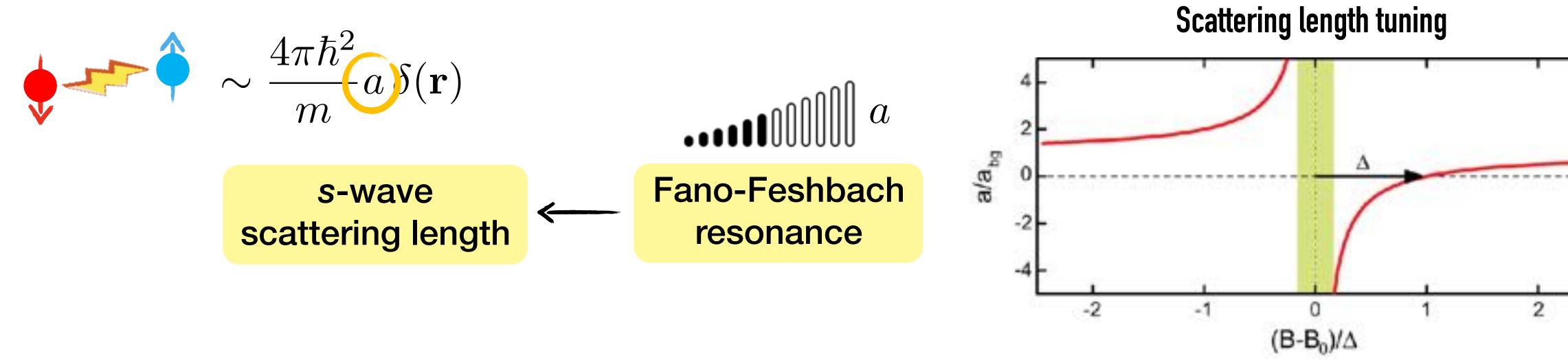




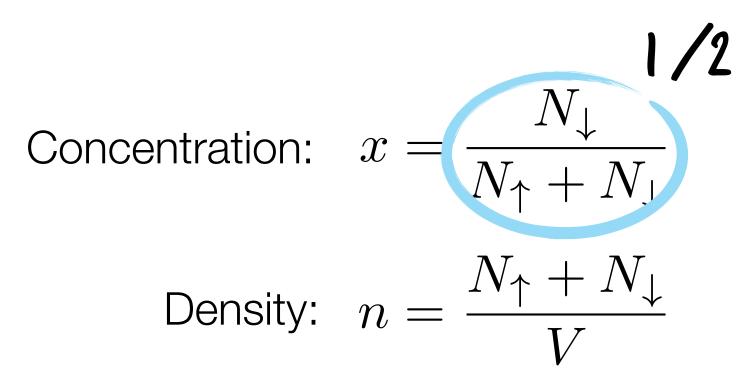
Ultracold Fermi Gases



Two-component Fermi gas with short-range (contact-like) interactions







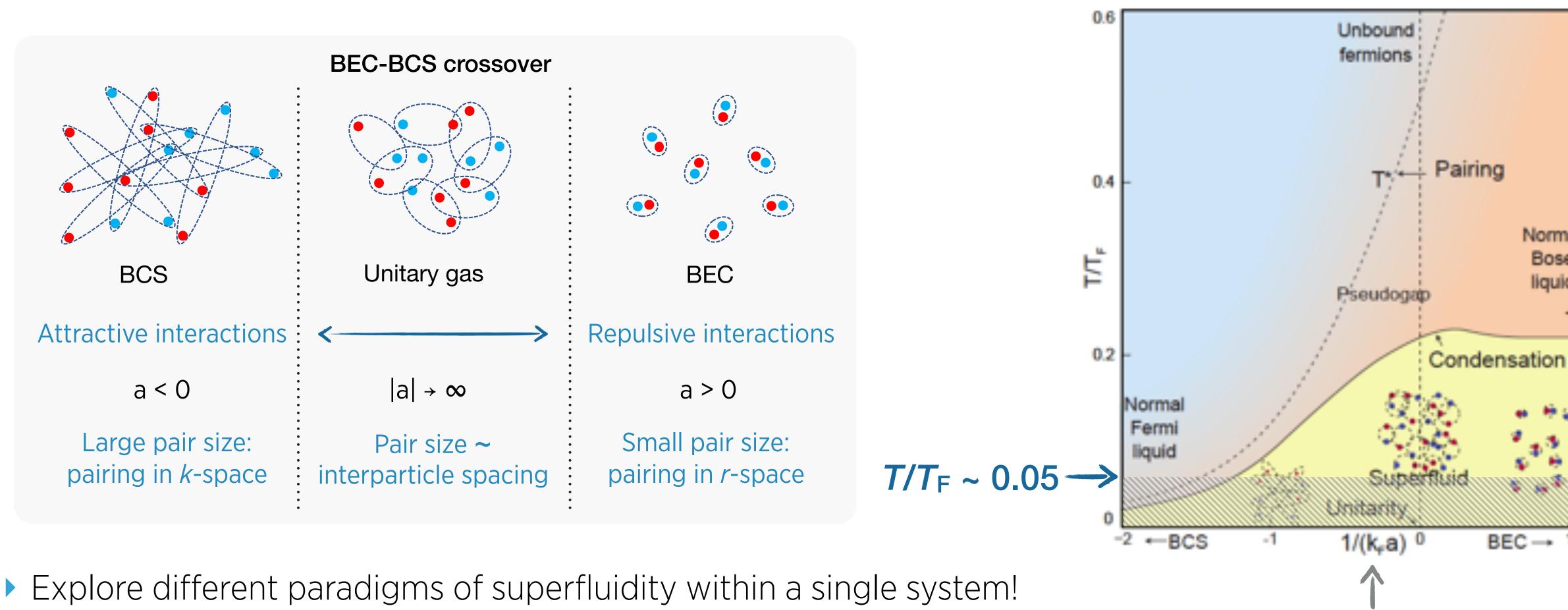
Fermi wavevector: $k_F = (6\pi^2 n)^{1/3}$ Fermi energy: $\varepsilon_F = \frac{\hbar^2 k_F^2}{2m}$





THE BEC-BCS CROSSOVER

Two-component Fermi gas with strong interactions between distinguishable spins: crossover from BEC to BCS superfluidity



The BCS-BEC crossover and the unitary Fermi gas. Lecture notes in physics, 836, Edited by W. Zwerger (Springer, Berlin, 2012).

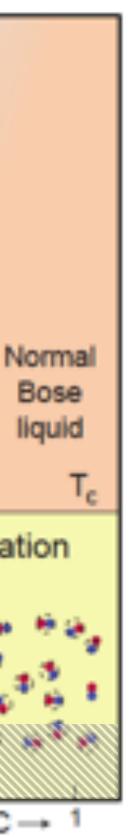


Temperature-interaction phase diagram

Randeria, *Nature Phys.* **6**, 561 (2010)

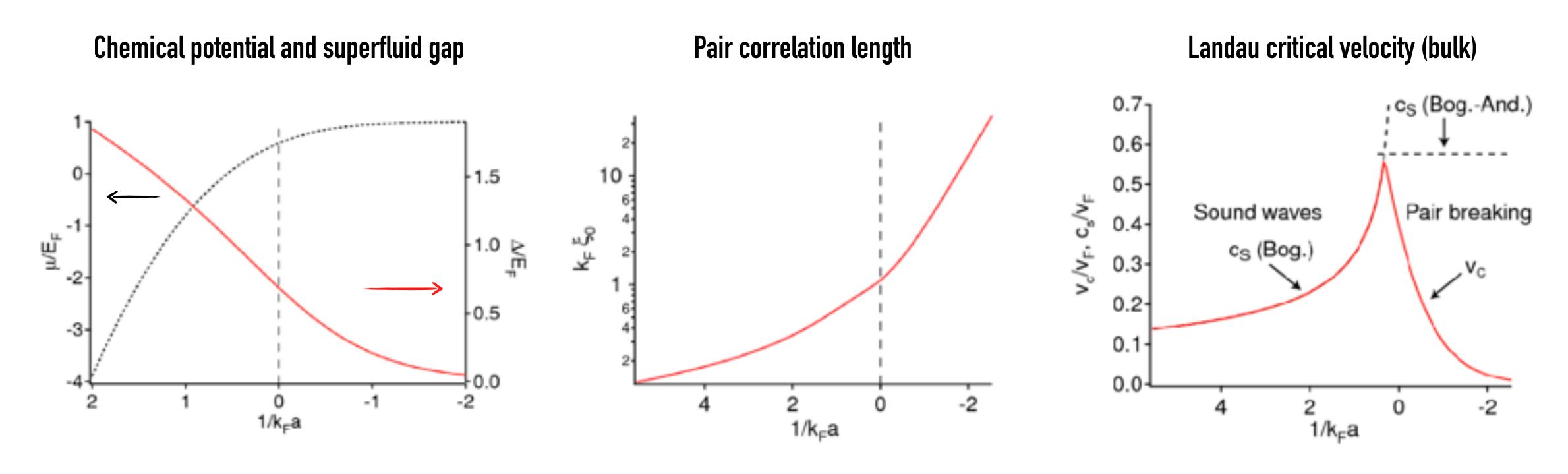
 $k_F a$ (adimensional) quantifies interactions







BEC-BCS CROSSOVER SUPERFLUIDS



Proceedings of the International School of Physics "Enrico Fermi", Course CLXIV, Varenna. Edited by M. Inguscio, W. Ketterle, and C. Salomon (IOS Press, Amsterdam, 2008)

Crossover from two-body to many-body pairing, from tightly bound pairs to Cooper pairs, from **bosonic to fermionic excitations**: binding energy of pairs approaches ε_F near unitarity

▶ Bosonic theories are appropriate for $\epsilon_B \simeq \frac{\hbar^2}{ma^2} \lt$



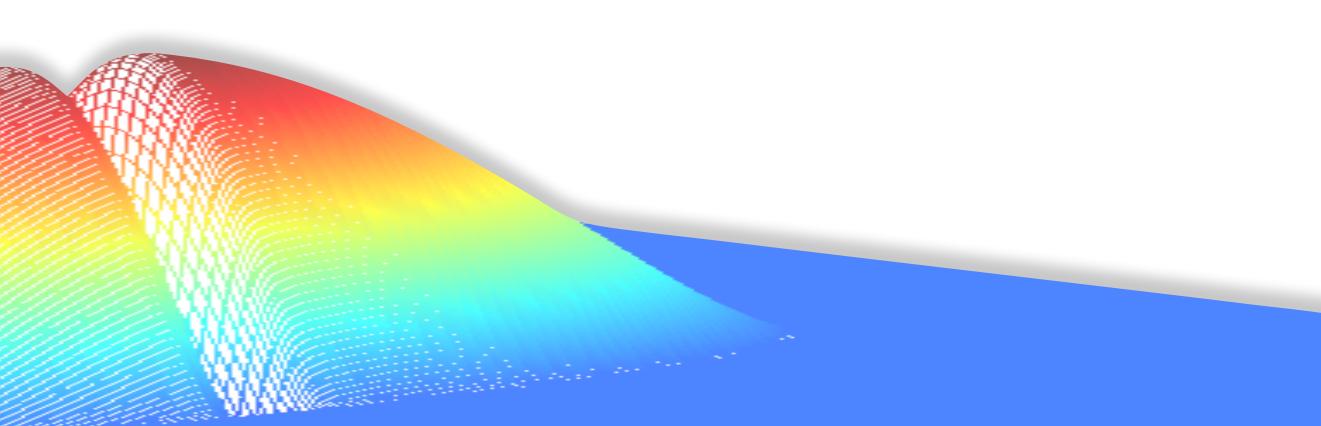
$$\ll \varepsilon_F$$



THE PLAN

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- Our experimental setup: a thin tunable Josephson junction between Fermi superfluids
- Dynamics in **population-biased** junctions: Josephson-plasma oscillations and dissipative flow through vortex nucleation
- Current-driven junctions: probing the critical current via the **DC Josephson** effect
- Outlook: local phase manipulation and quantum transport of two-dimensional gases







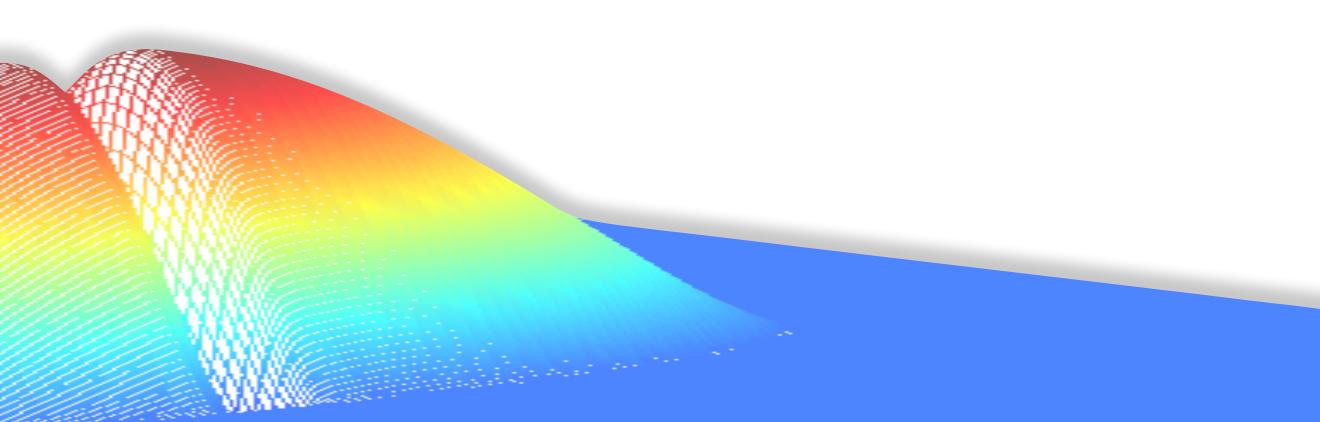
THE PLAN

Introduction: ultracold Fermi gases across the BEC-BCS crossover

Josephson junction basics

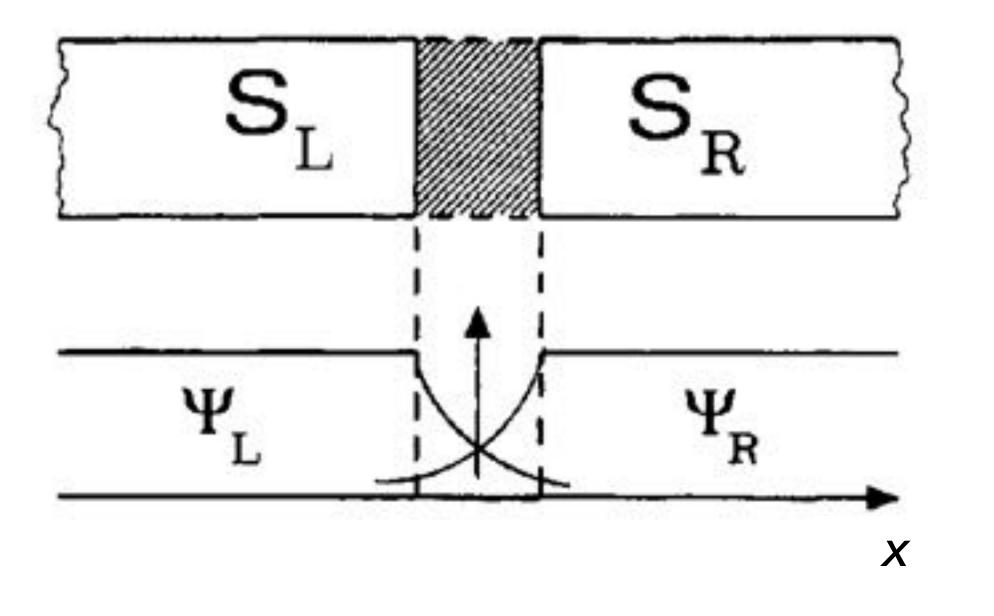
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JOSEPHSON JUNCTION BASICS



- $\psi_L = |\Delta_L| e^{i\phi_L}, \ \psi_R = |\Delta_R| e^{i\phi_L}$ In BEC regime: $|\Delta| \sim \sqrt{n_c}$
- **Relative phase:** $\phi = \phi_L \phi_R$
- Supercurrent induced by phase jump: $v_s = \frac{h}{m} \nabla \phi$





Josephson effect: quantum coherent tunnelling superfluid of order parameter

- → Demonstrating the macroscopic phase coherence of condensed state i.e. superfluids
- → Pin down the order parameter

For sufficiently small **T**

Critical current

- **)** Josephson current: $I(t) = I_c \sin \phi(t) \leftarrow$
- Ambegaokar-Baratoff relation: $I_c \propto \Delta \sim n_c$
- > Josephson-Anderson relation: $\hbar \dot{\phi}(t) = -\Delta \mu = \mu_R \mu_L$

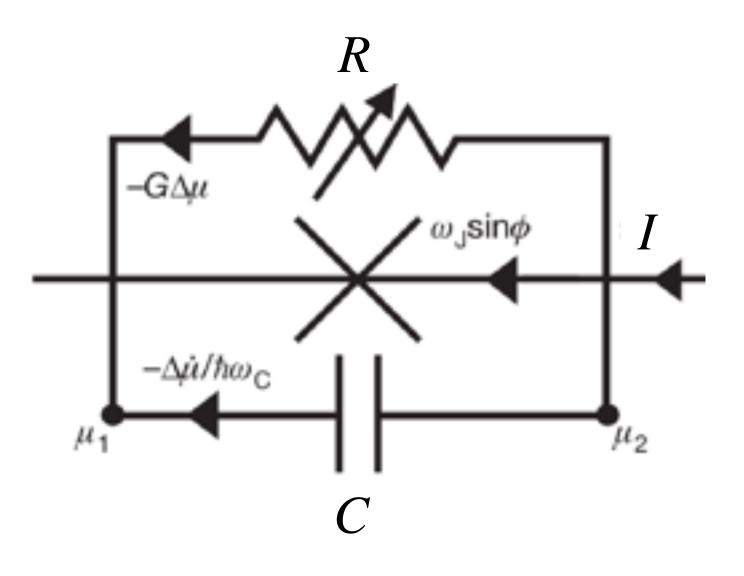
Bias potential

[e.g. population imbalance]



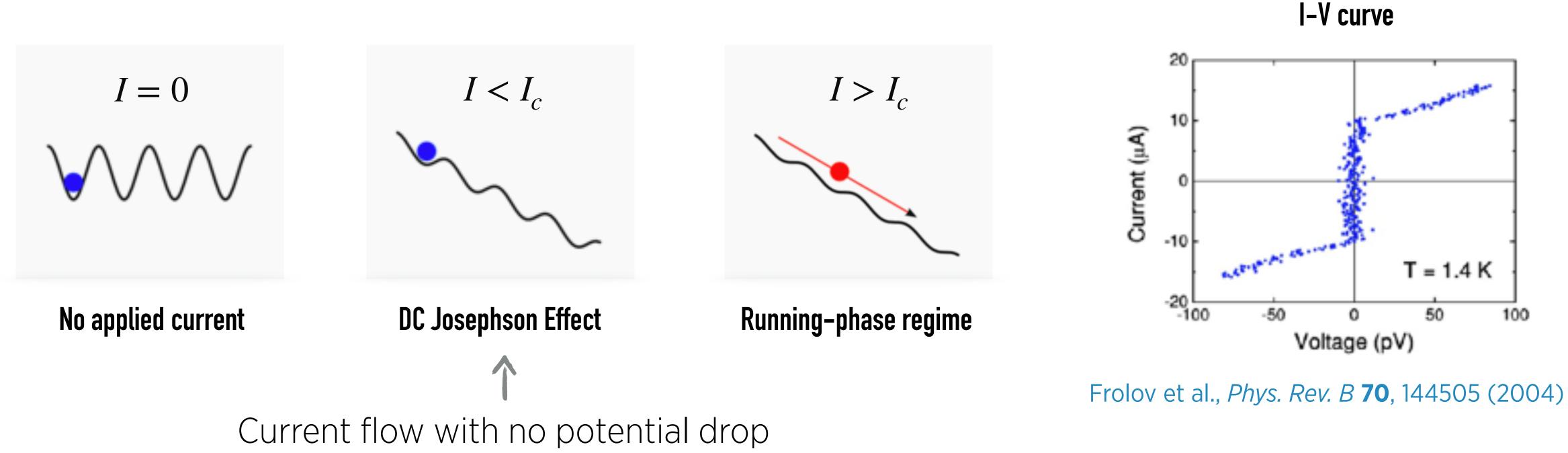


JOSEPHSON JUNCTION BASICS



Flow a current: current-biased junction

- Mass ~ C
- Friction coefficient ~ G = 1/R
- Potential energy ~ $-1/C(I\phi + I_c \cos \phi)$









JOSEPHSON-PLASMA OSCILLATIONS

- Charge the junction: population-biased junction dynamics
- (Forget about resistance for now) **Two relevant energies**:

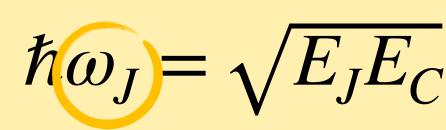
Josephson energy: $E_J \sim J(\mu, V_0, w) N_0$, $E_J > k_B T$

Charging energy: $E_C \sim \frac{\partial \mu}{\partial n} = \frac{1}{\kappa}$ (junction capacity)

Josephson relation ($V_0 \gtrsim \mu$) → Pendulum-like dynamics:

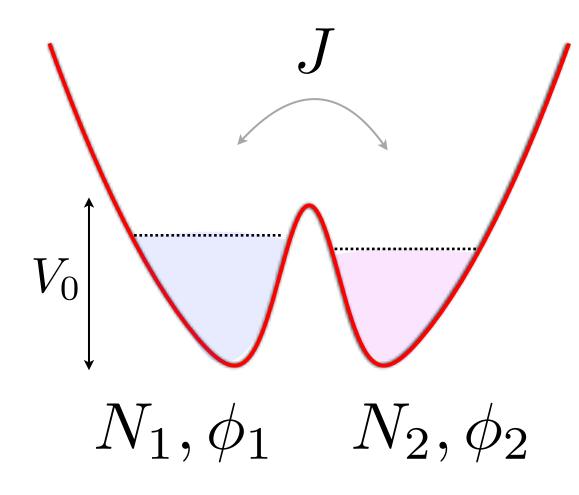
 $\begin{aligned} &\hbar \dot{z} \propto -E_J \sin(\phi) \\ &\dot{h} \dot{\phi} \propto E_C z \end{aligned}$

Josephson-Plasma oscillations:



Josephson-Plasma frequency







Relative imbalance

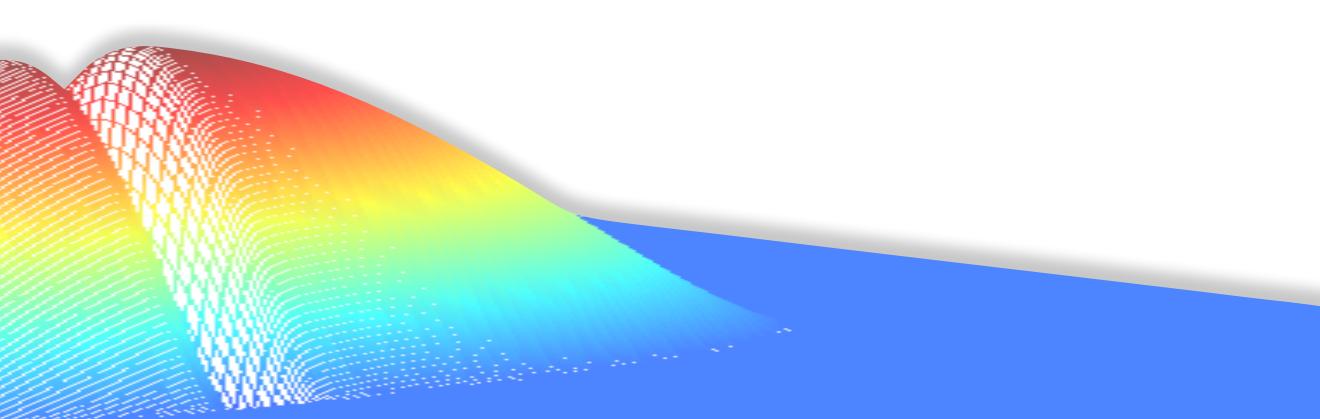
Pendulum-like evolution



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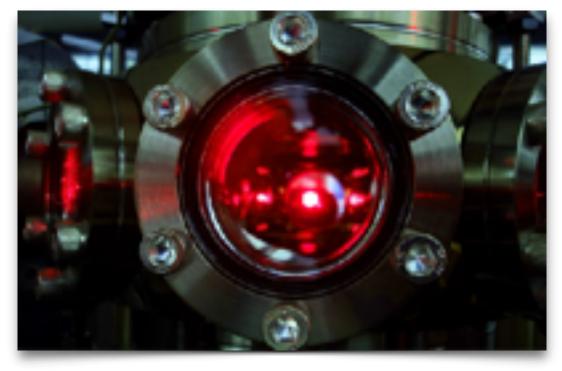


FERMI GASES OF LITHIUM-6

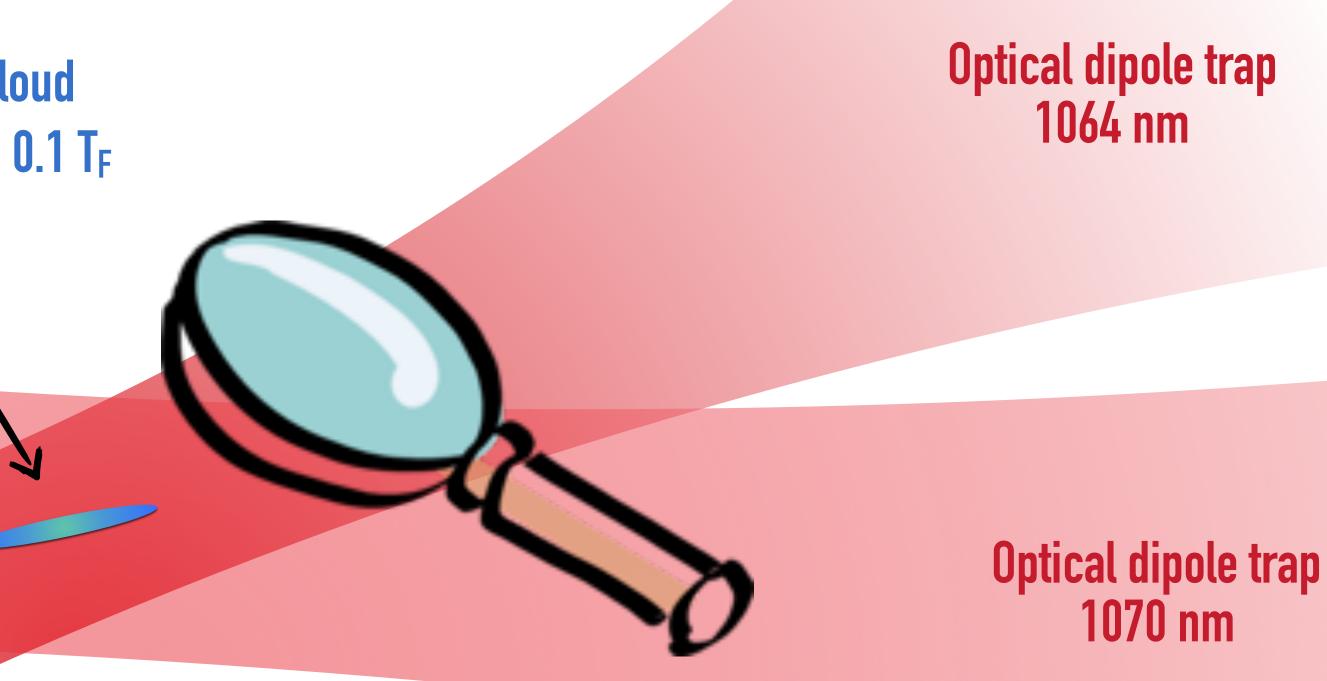
Ultracold lithium-6 cloud $N \sim 10^5$ at T ~ 30 nK < 0.1 T_F

100 µm





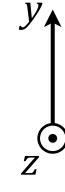




$N \sim 10^8 \text{ at } T \sim 50 \,\mu\text{K}$ Magneto-Optical Trap + D_1 molasses

All-optical preparation of ultracold lithium gases

Burchianti et al., Phys. Rev. A 90 (2014)





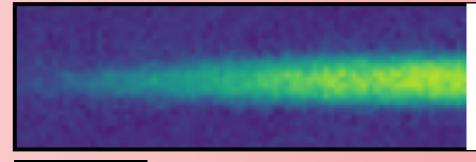




FERMI GASES OF LITHIUM-6

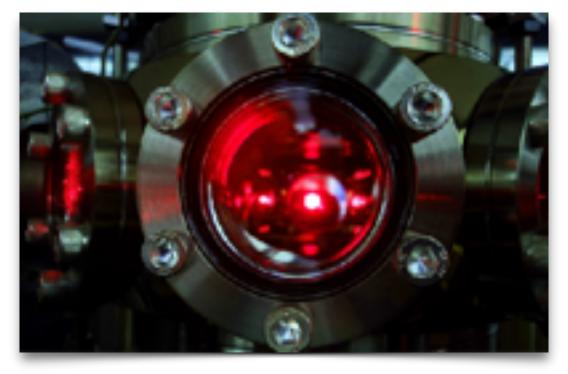
Ultracold lithium-6 cloud $N \sim 10^5$ at T ~ 30 nK < 0.1 T_F

$2\mu m \gtrsim W \gtrsim 0.8\mu m$

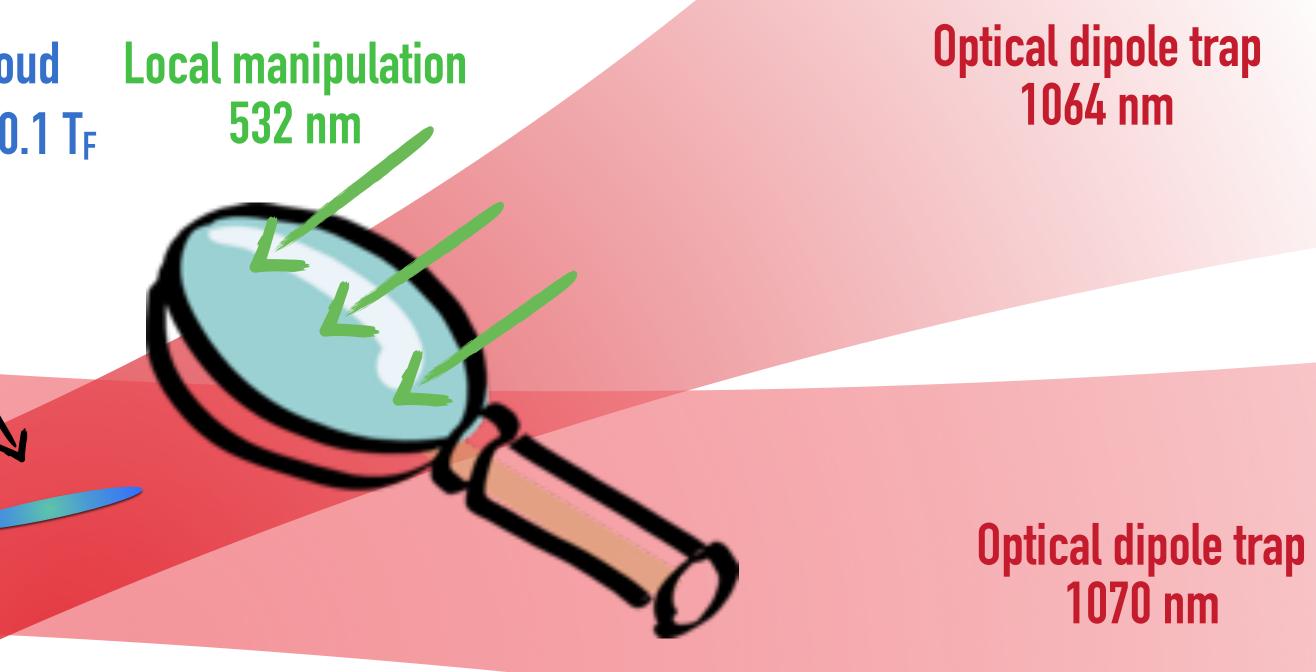


100 µm





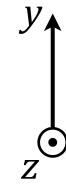




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All-optical preparation of ultracold lithium gases

Burchianti et al., Phys. Rev. A 90 (2014)





OUR JOSEPHSON JUNCTION

Ultracold lithium Fermi gas bisected by thin insulating barrier $w_h \gtrsim 3\xi$

Order parameters: $\psi_i = \sqrt{N_i} e^{-i\phi_i}$

 $\phi = \phi_1 - \phi_2$

 $N_1 N_2$

- Relative phase: $\phi = \phi_1 \phi_2$
- Imbalance: $\Delta N = N_1 N_2$
- Current: $I = (\dot{N}_1 \dot{N}_2)/2$

In situ imaging \rightarrow Current through junction Time-of-flight imaging → Phase diff. across junction



Preparation of tuneable $\Delta \mu$

Step 1

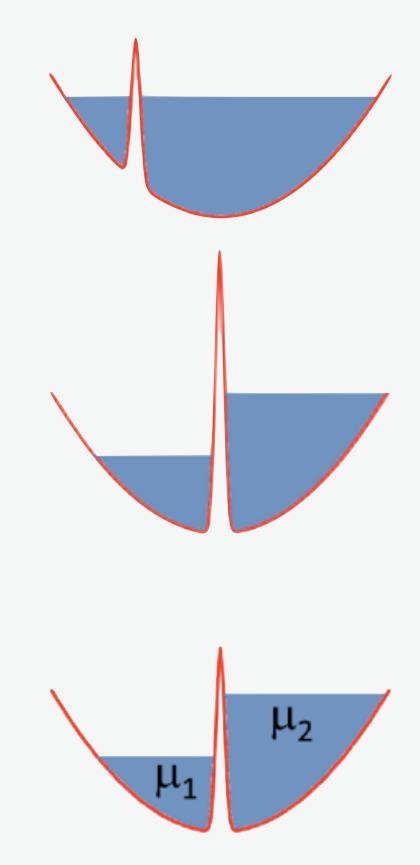
Prepare imbalanced reservoirs at rest

Step 2

Slowly raise barrier and move trap to create imbalance

Step 3

Rapidly lower barrier to target value of V_0





OUR JOSEPHSON JUNCTION

Ultracold lithium Fermi gas bisected by thin insulating barrier $w_h \gtrsim 3\xi$

Order parameters: $\psi_i = \sqrt{N_i} e^{-i\phi_i}$

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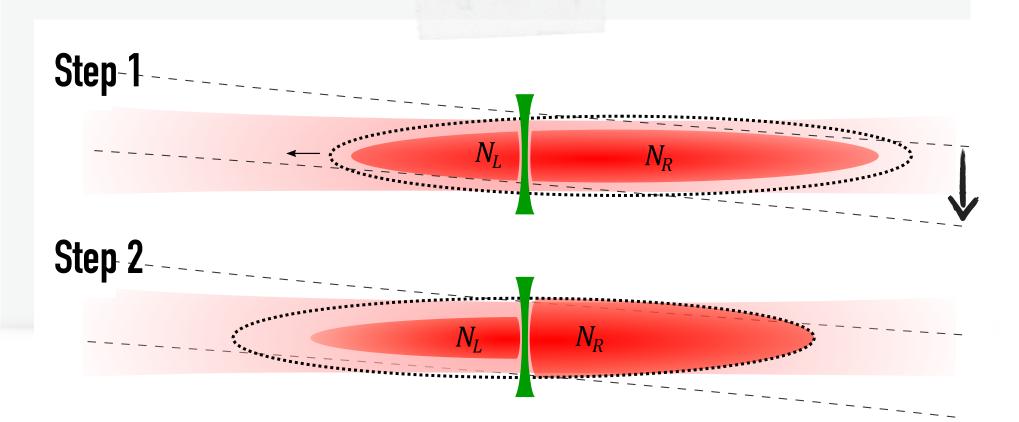


Preparation of tuneable $\Delta \mu$

Step 1 Prepare imbalanced reservoirs at rest

Step 2

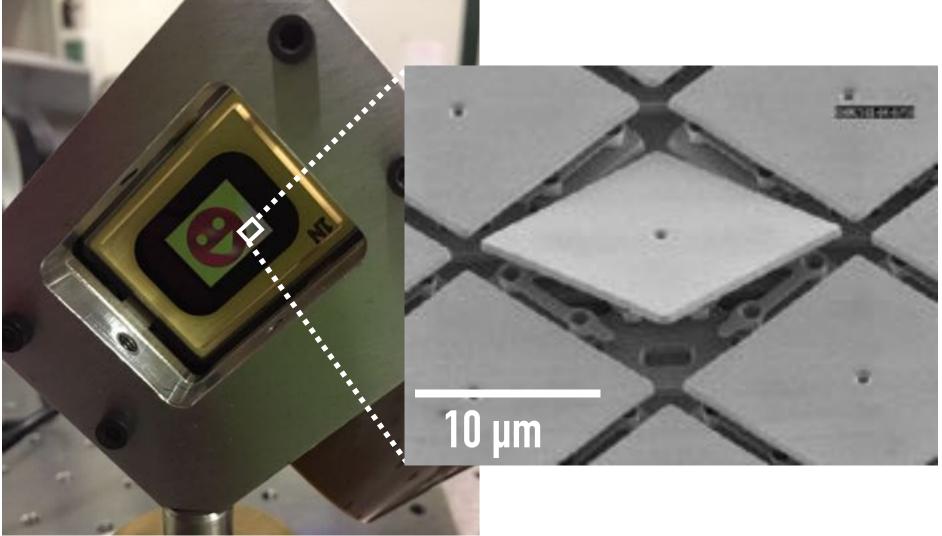
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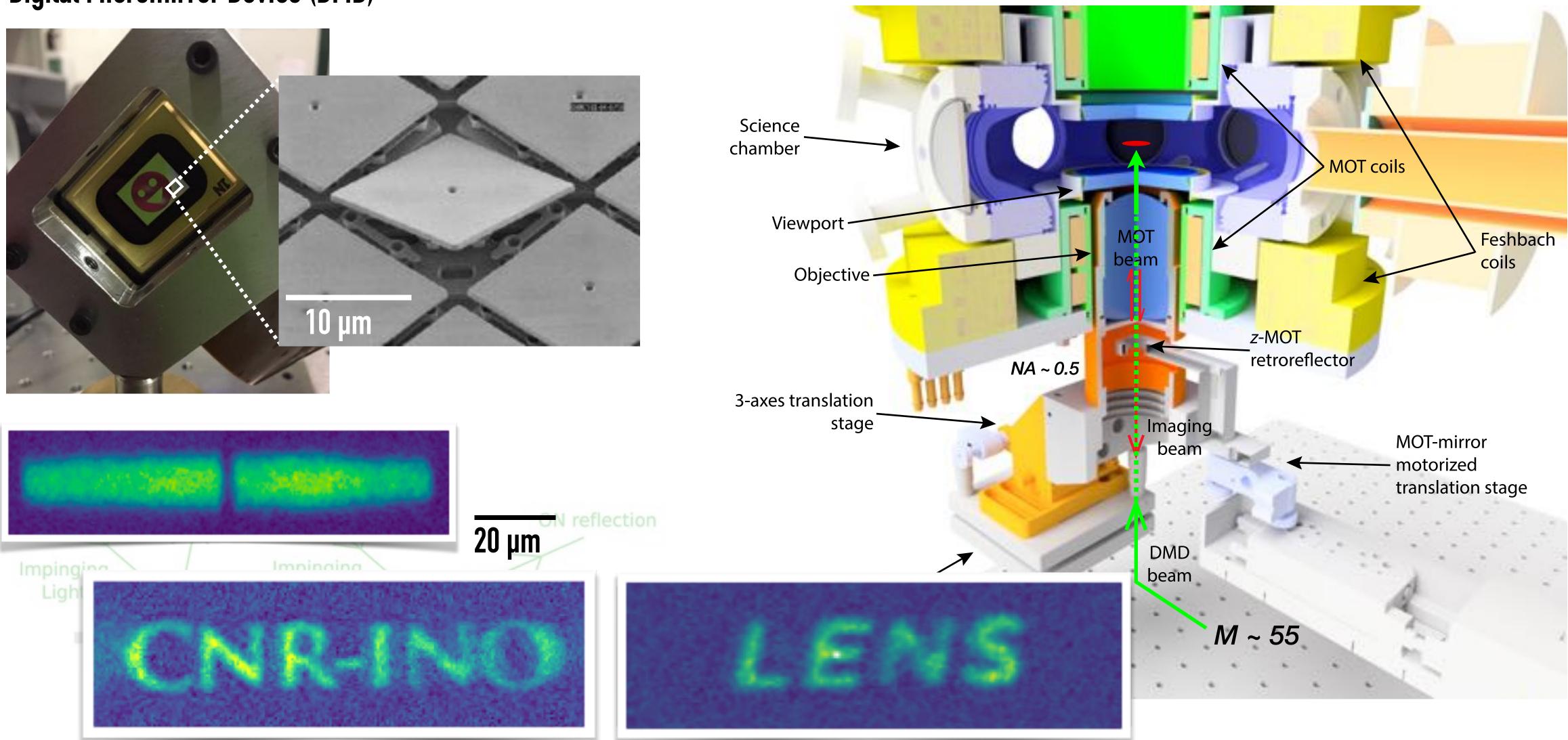




RECENT UPGRADES: OBJECTIVE AND DMD

Digital Micromirror Device (DMD)





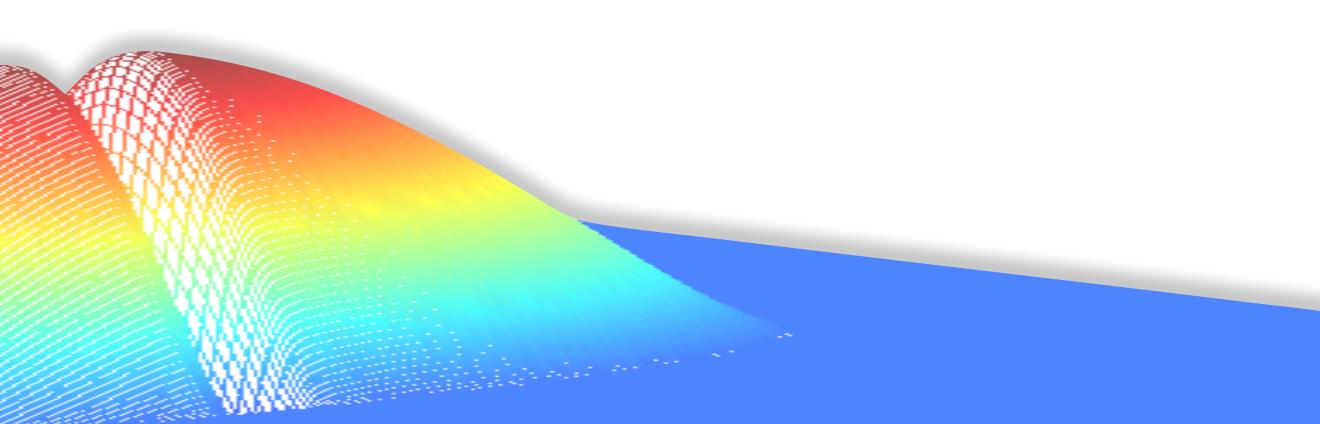




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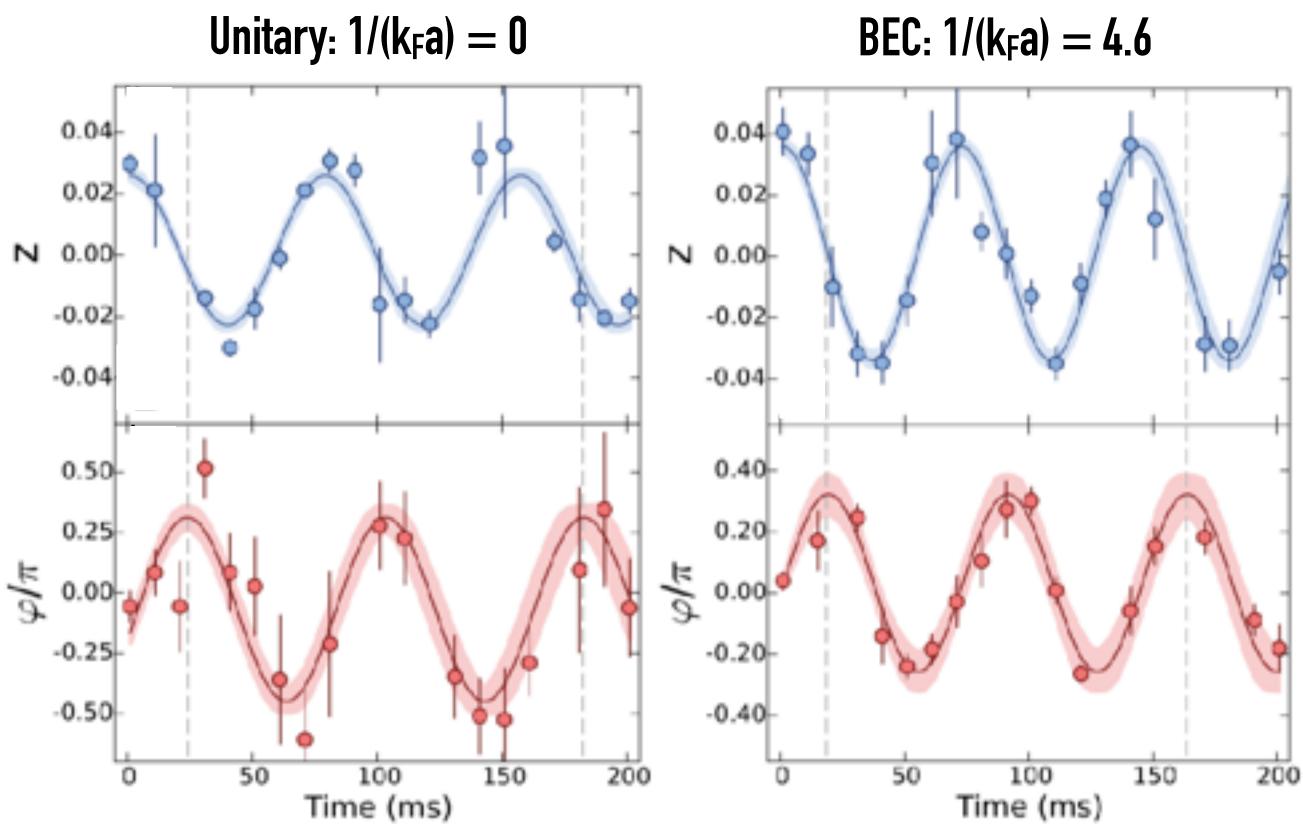


JOSEPHSON-PLASMA REGIME

For small excitations (small population bias): Josephson-Plasma oscillations

 $\dot{h}\phi \propto E_C z \\
\dot{h}\dot{z} \propto -E_J \phi$

Plasma frequency: $\omega_J = \sqrt{E_J E_C}/\hbar$







Universality of Josephson-Anderson relation over **BEC-BCS** crossover

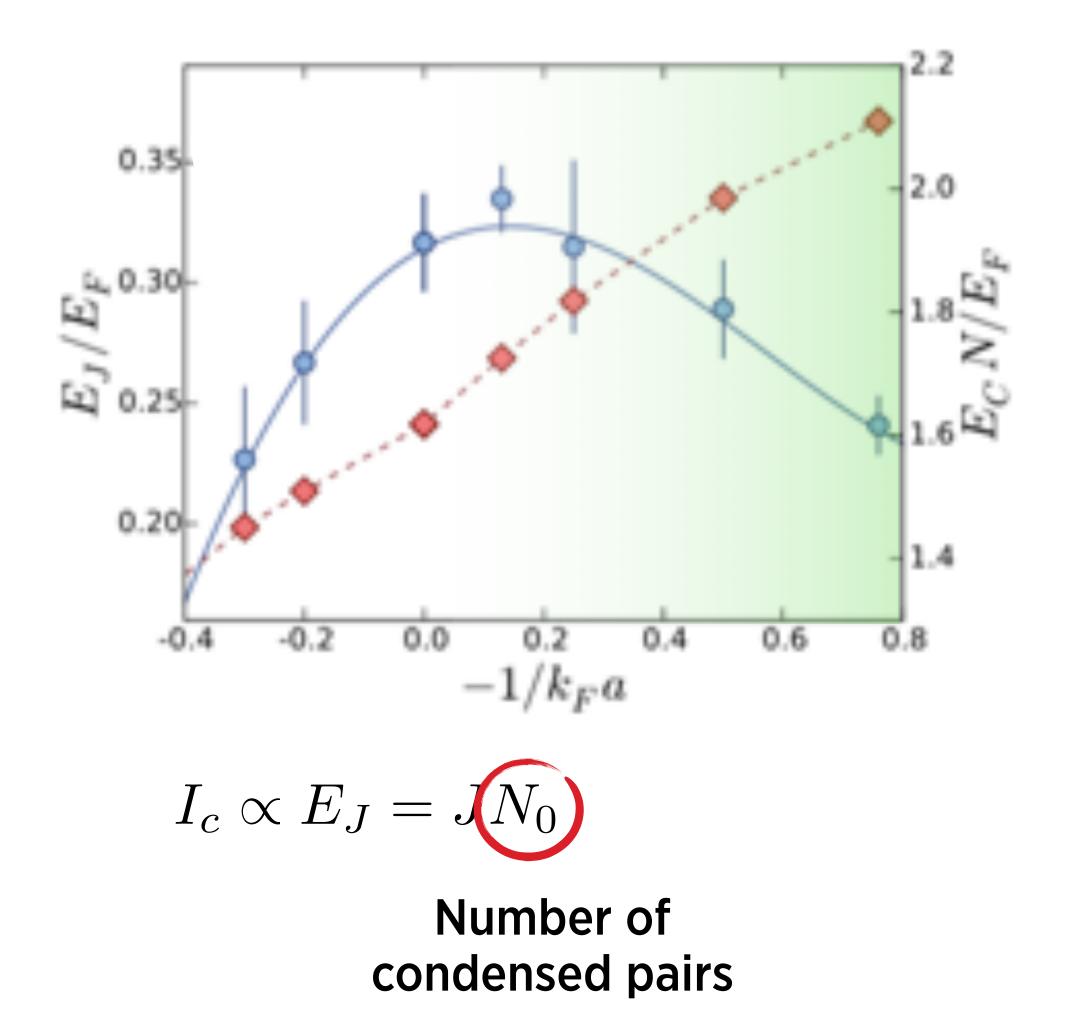
Imbalance and phase oscillate in quadrature → conjugate observables

Valtolina et al., *Science* **350** (2015)



JOSEPHSON-PLASMA REGIME

- Constant barrier height $V_0 > E_F$, varying the interaction strength $1/(k_Fa)$







Use measured Josephson-Plasma frequency to **extract Josephson energy:** $\omega_J = \sqrt{E_J E_C}/\hbar$

Towards BEC side, *Ec* decreases because of decreasing chemical potential

 $E_J^{BCS} \propto \Delta$

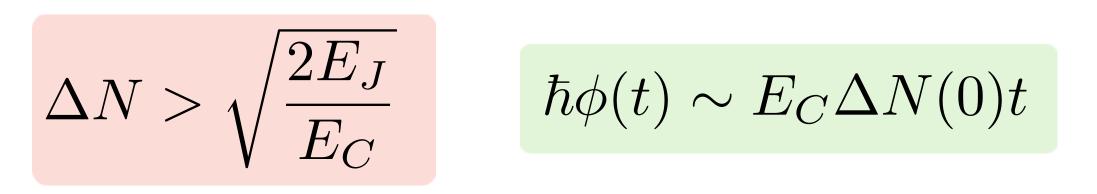
Ambegaokar-Baratoff relation

- Towards BCS side, *Ec* grows but condensed fractions decreases linearly with Δ
- \rightarrow Overall decrease of E_J towards BCS side!
- → Maximum Josephson energy near unitarity!



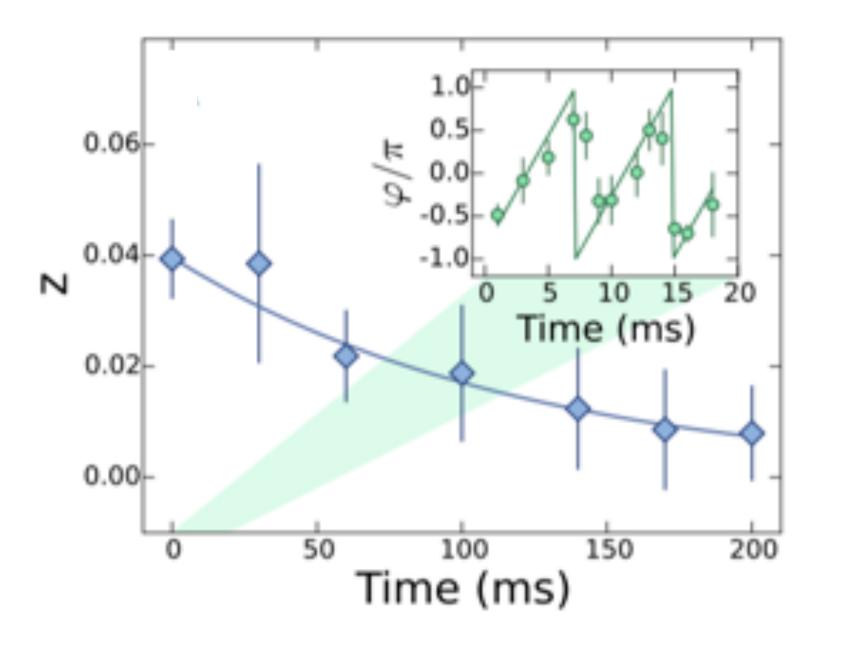
THE RUNNING-PHASE REGIME

If charging energy exceeds Josephson energy: running-phase evolution



Small imbalance oscillation at Josephson frequency $\omega \simeq \Delta \mu_0 / \hbar$

• One way to reach this: raise the barrier to $V_0 \gg \mu$, so as to strongly reduce E_J



Linear phase evolution is observed: phase coherence is clearly there, but large shot-to-shot fluctuations

Population imbalance decays: no Josephson oscillations observed, no "quantum self-trapping" (MQST)

A. Smerzi et al, *Phys. Rev. Lett.* **79**, 4950 (1997) I. Zapata et al., *Phys. Rev. A* 57, R28, (1998)

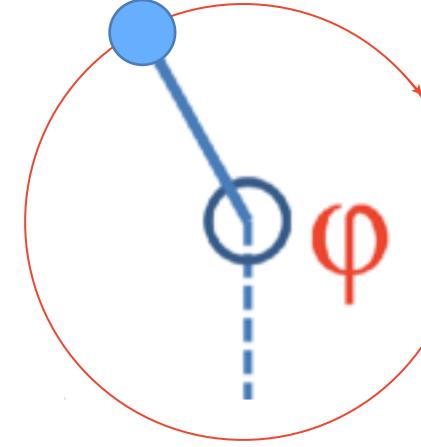
Valtolina et al., *Science* **350** (2015)



What is the origin of incoherent transport?



Running pendulum evolution

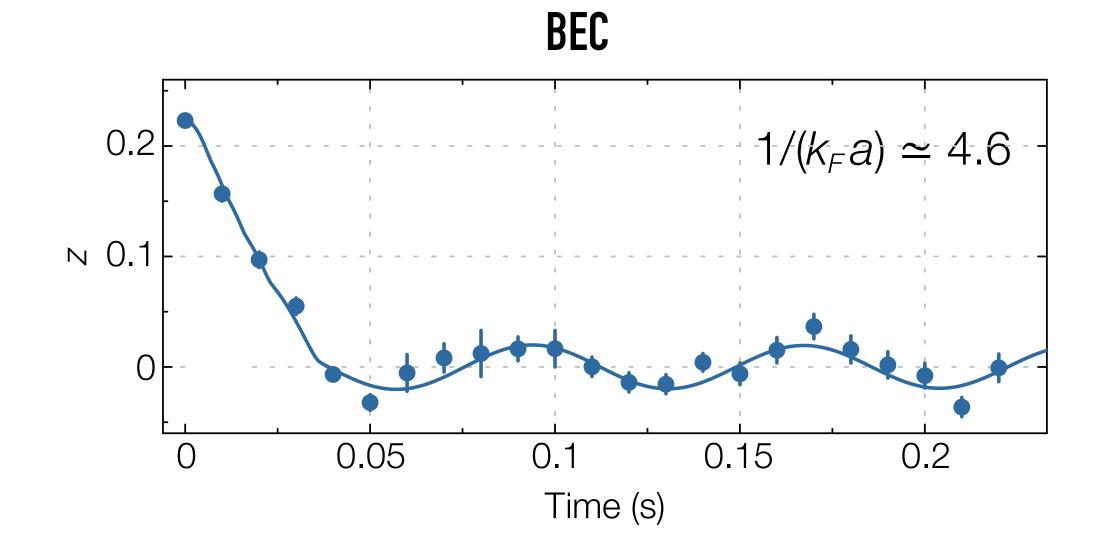






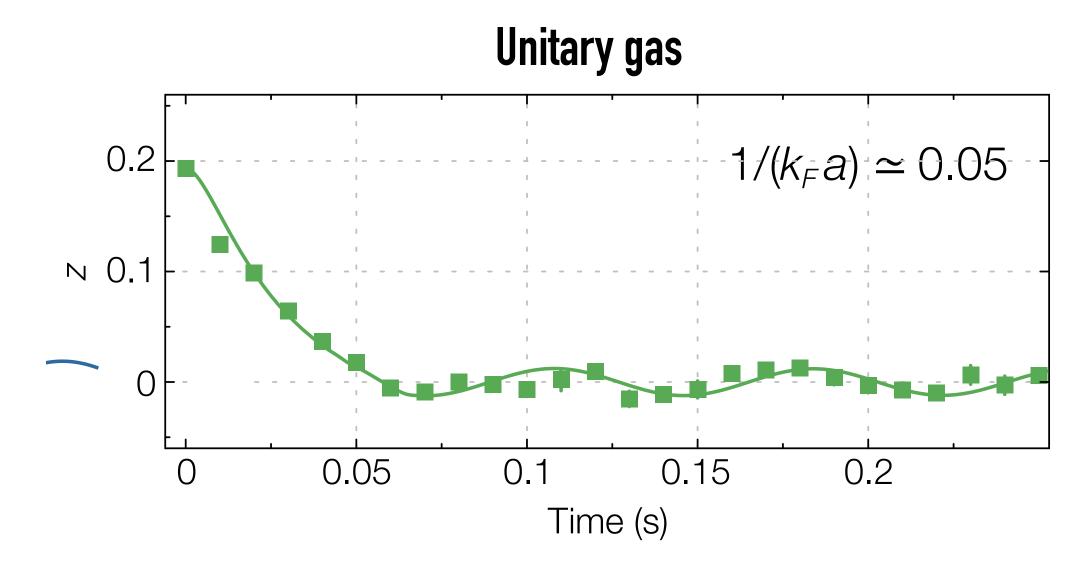
INCREASING THE INITIAL POPULATION BIAS

Increase the initial imbalance while keeping E_{J} constant at $V_{0} \simeq \mu$





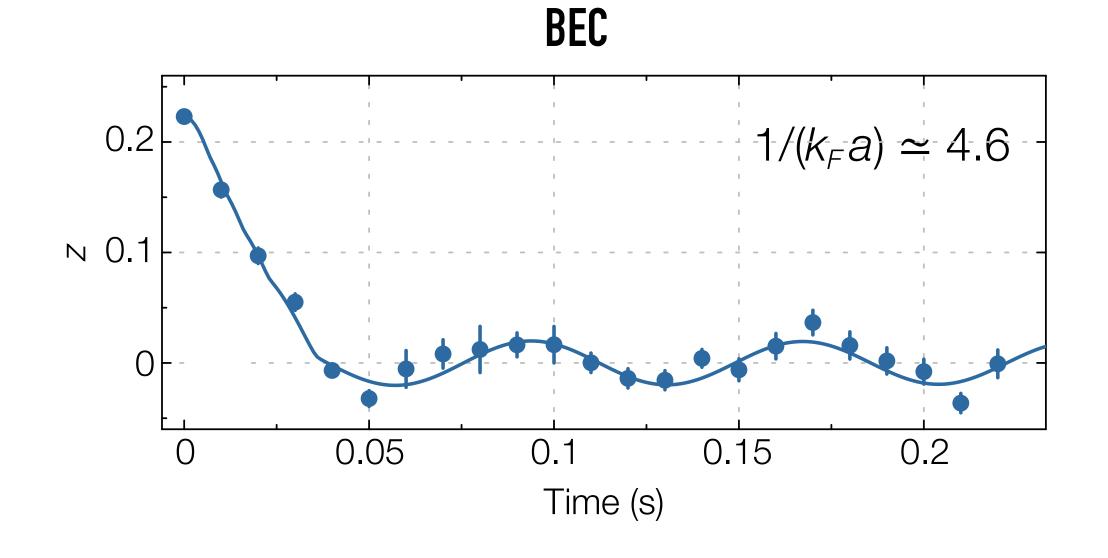
A. Burchianti et al., *PRL* **120** (2018)





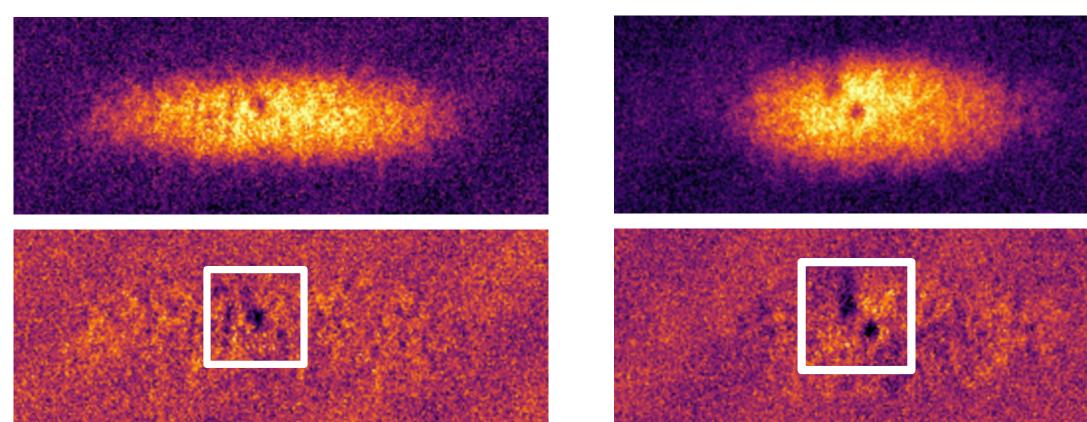
INCREASING THE INITIAL POPULATION BIAS

Increase the initial imbalance while keeping E_J constant at $V_0 \simeq \mu$



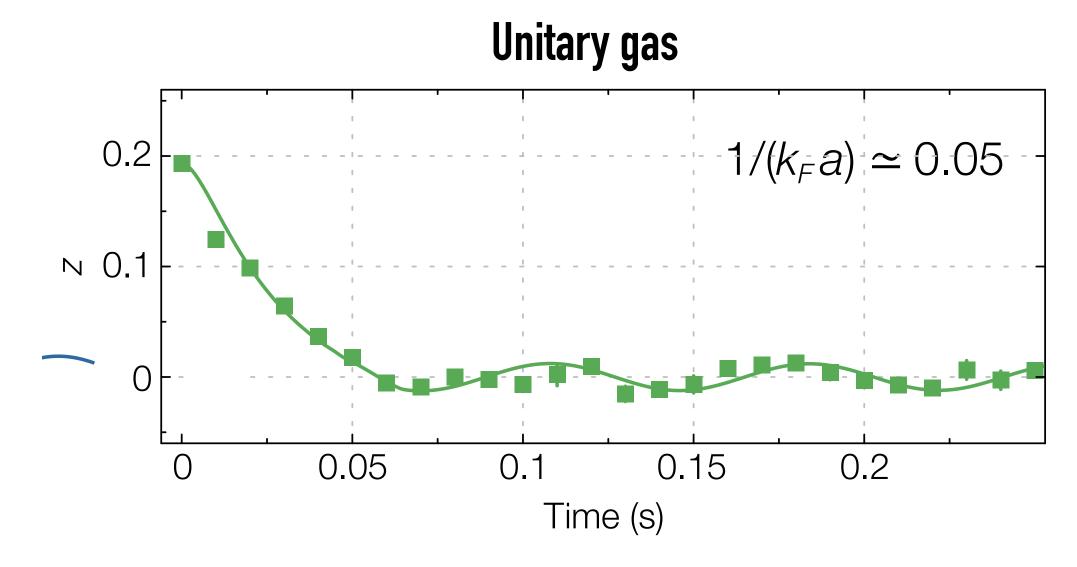
BEC

Unitary gas

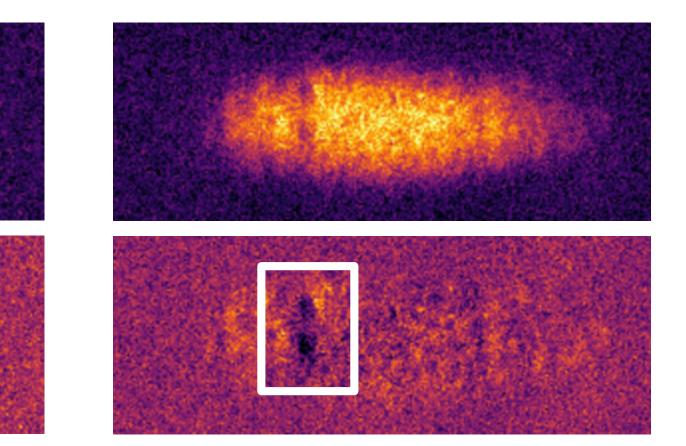




A. Burchianti et al., *PRL* **120** (2018)



BCS



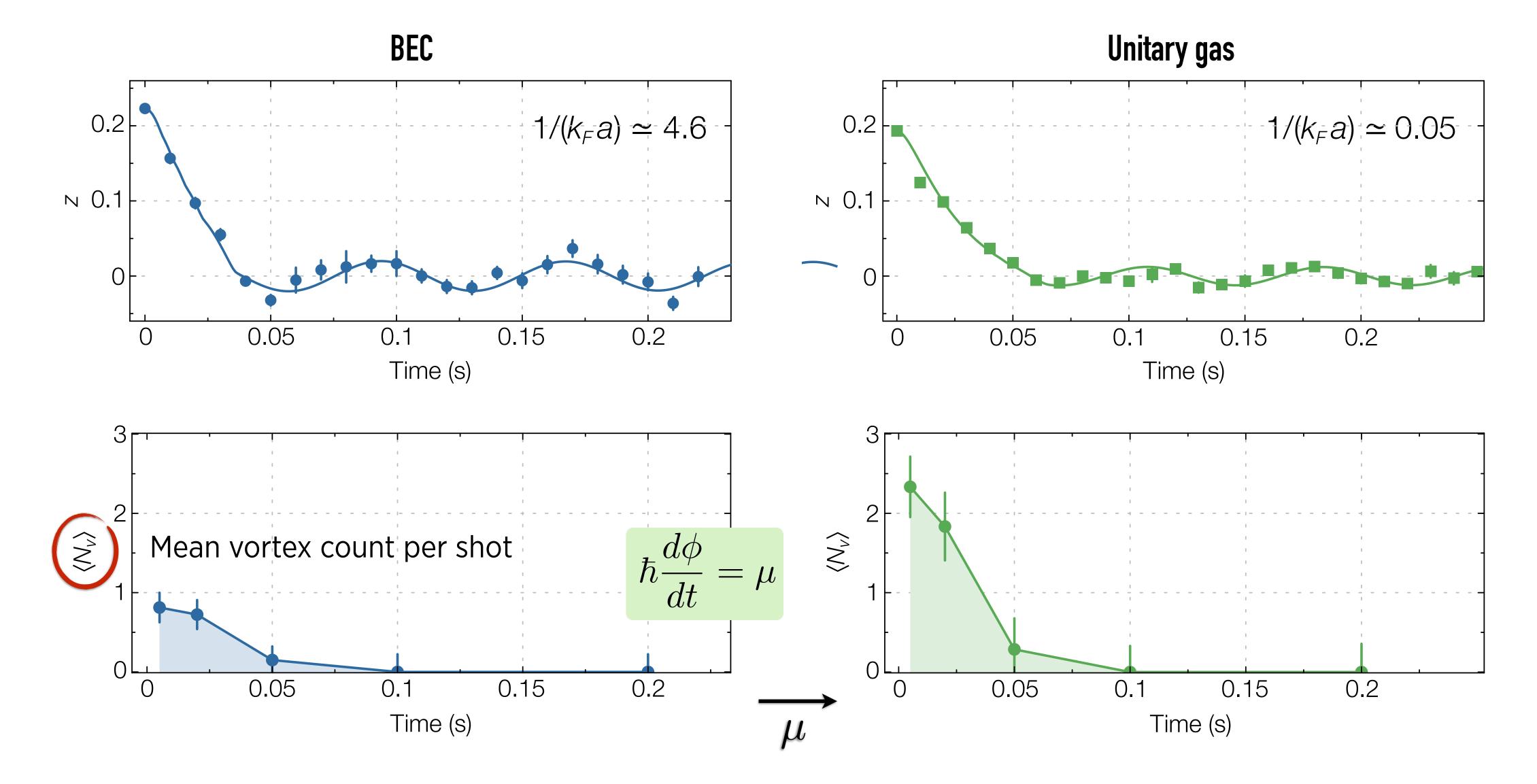
Topological defects are present!





INCREASING THE INITIAL POPULATION BIAS

Increase the initial imbalance while keeping E_{J} constant at $V_{0} \simeq \mu$





A. Burchianti et al., *PRL* **120** (2018)



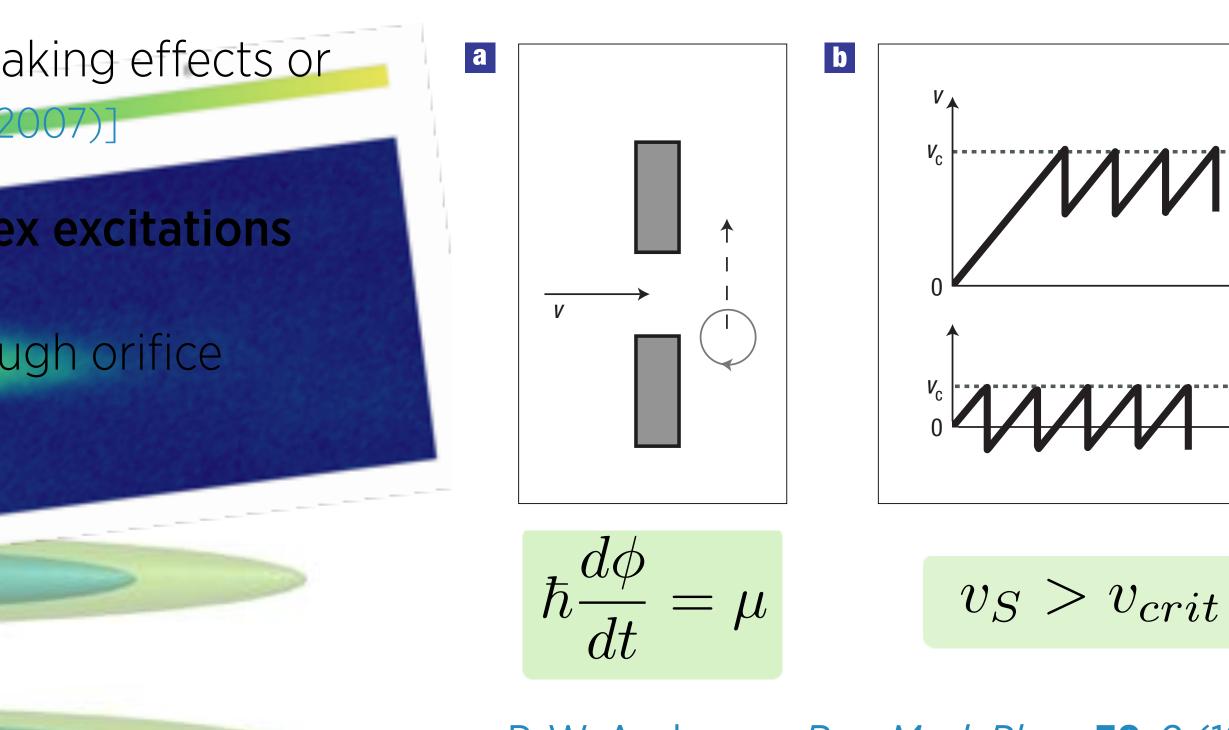
VORTEX NUCLEATION: PHASE-SLIPPAGE

 $t \sim h/\Delta \mu$

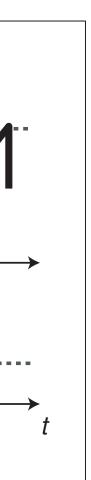
- Phase coherence is preserved, ruling out pair-breaking effects or quasiparticle currents [cf. Levy et al., Nature 449, 579 (2007)]
- **Dissipation** can originate from **(topological) vortex excitations** rather than by (Landau) single-particle excitations -> analogous to phase slippage for liquid 4He through orifice ee also recent work by Gauthier et al., arXiv:1903.04086]

- When a vortex line crosses the superflow, dissipation arises: phase slippage → Energy transfer from the superflow to vortex motion The phase slips and the superfluid velocity jumps
- Our thin 3D junction geometry favours vortex nucleation and shedding into bulk Vortex dynamics affects superflow through junction \rightarrow initial imbalance decay!





P. W. Anderson, *Rev. Mod. Phys.* **38**, 2 (1966) E. Hoskinson et al. Nature Phys. 2, 23 (2006)

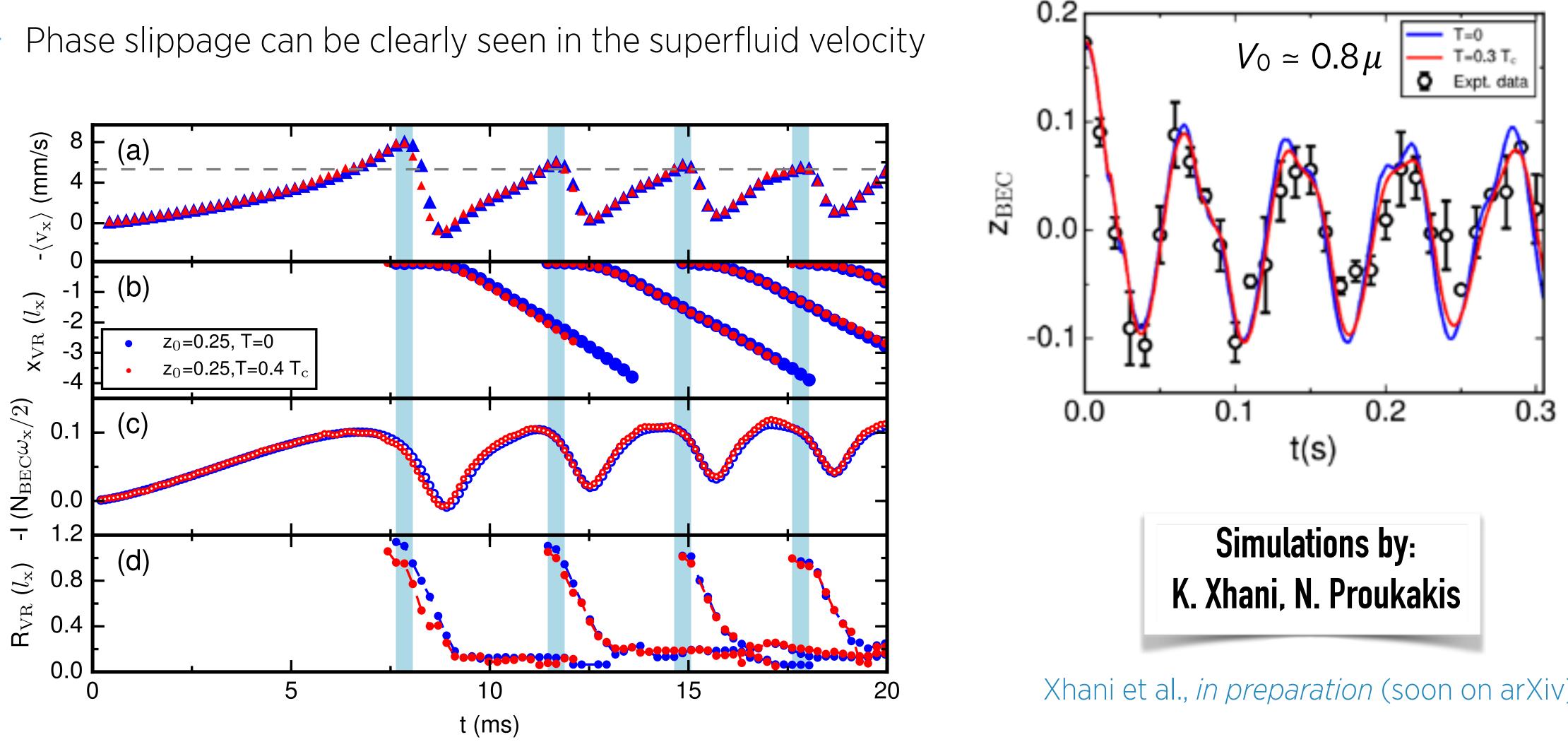






VORTEX NUCLEATION: SIMULATIONS

Phase slippage and vortex shedding is well reproduced by GP simulations of junction dynamics in BEC regime [see also early works e.g. Piazza et al., New J. Phys. 13 (2011)]

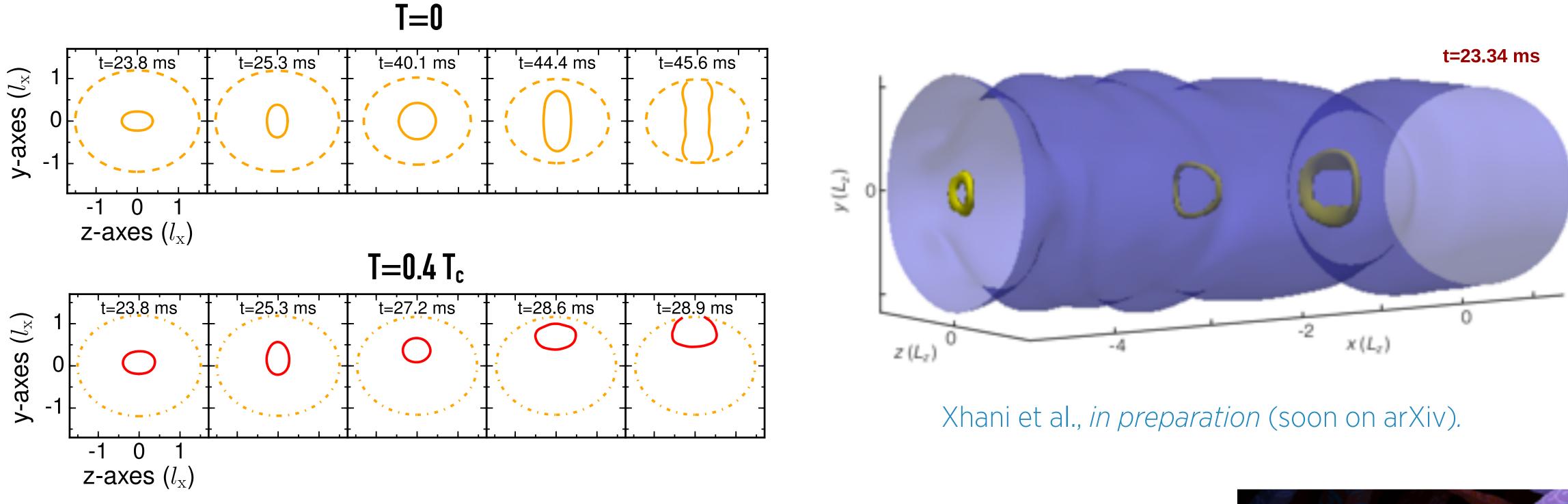




Xhani et al., in preparation (soon on arXiv).



SIMULATIONS OF VORTEX DYNAMICS





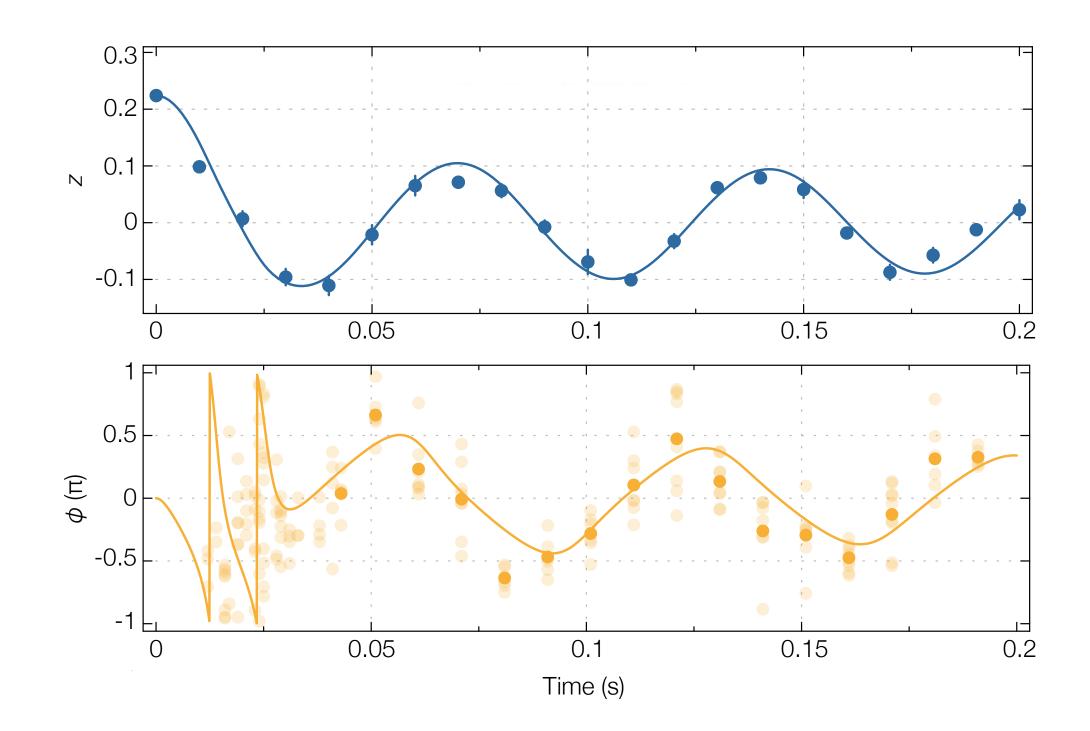




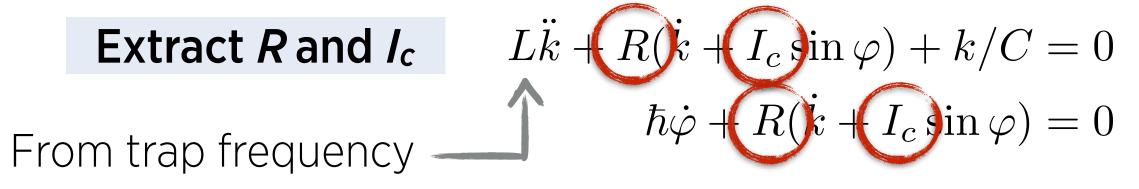


RESISTIVE FLOW AND RSJ CIRCUIT MODEL

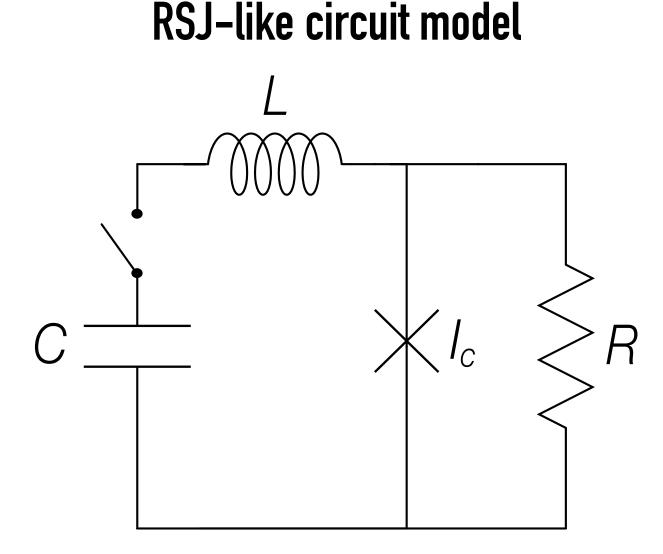
Model the evolution of imbalance and phase with RC-shunted Josephson Junction circuit



Imbalance z(t) and phase $\phi(t)$ evolution well fitted by numerical solution of RLCJ model:





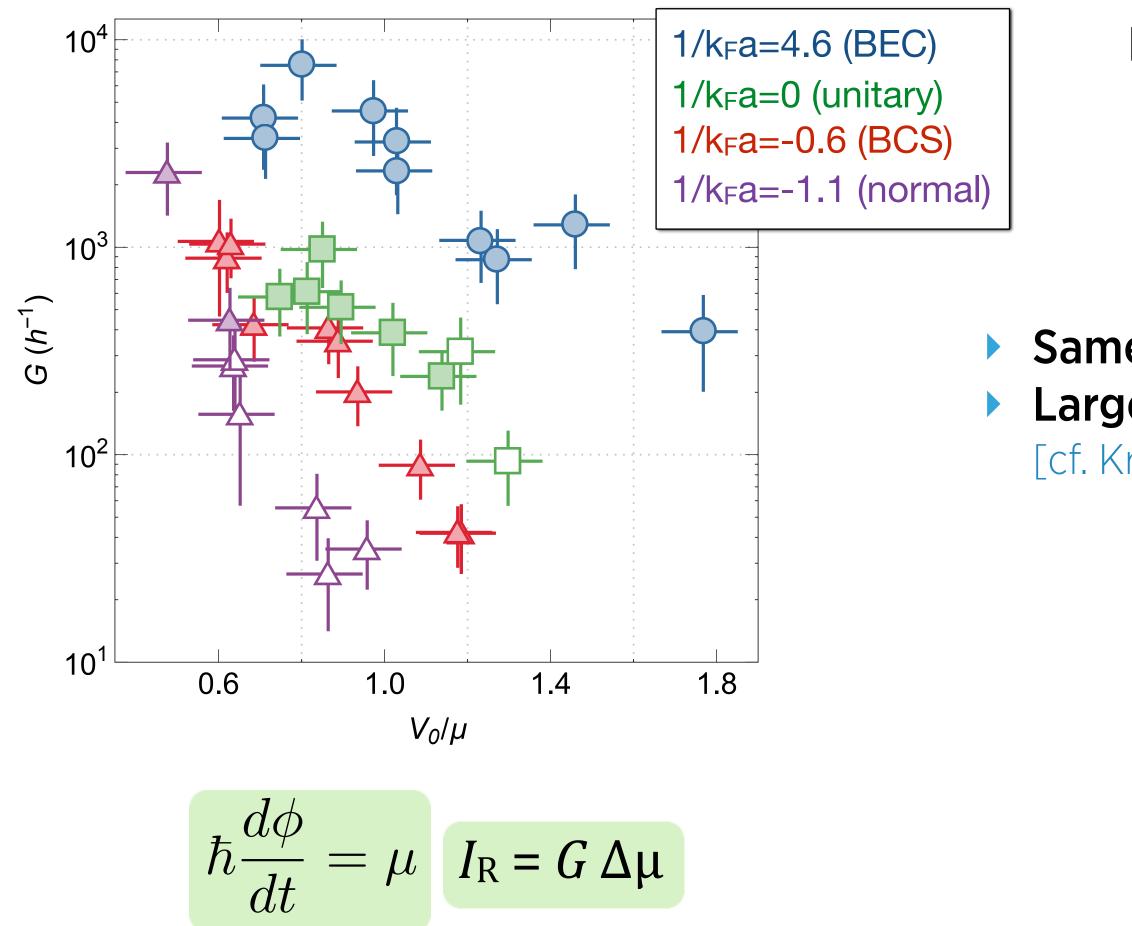


resistively shunted Josephson (RSJ) junction circuit \rightarrow incorporates all Ohmic dissipation into resistor R

Burchianti et al., *Phys. Rev. Lett.* **120** (2018) See also: Bidasyuk et al., J. Phys. B 51 (2018) Gauthier et al., arXiv:1903.04086ì



CONDUCTANCE $G = R^{-1}$



$$I_{\rm R} \propto \gamma N_{\rm ex} = N_{\rm ex} \Delta \mu / h$$
$$\rightarrow G \propto N_{\rm ex} / h \propto n_0$$

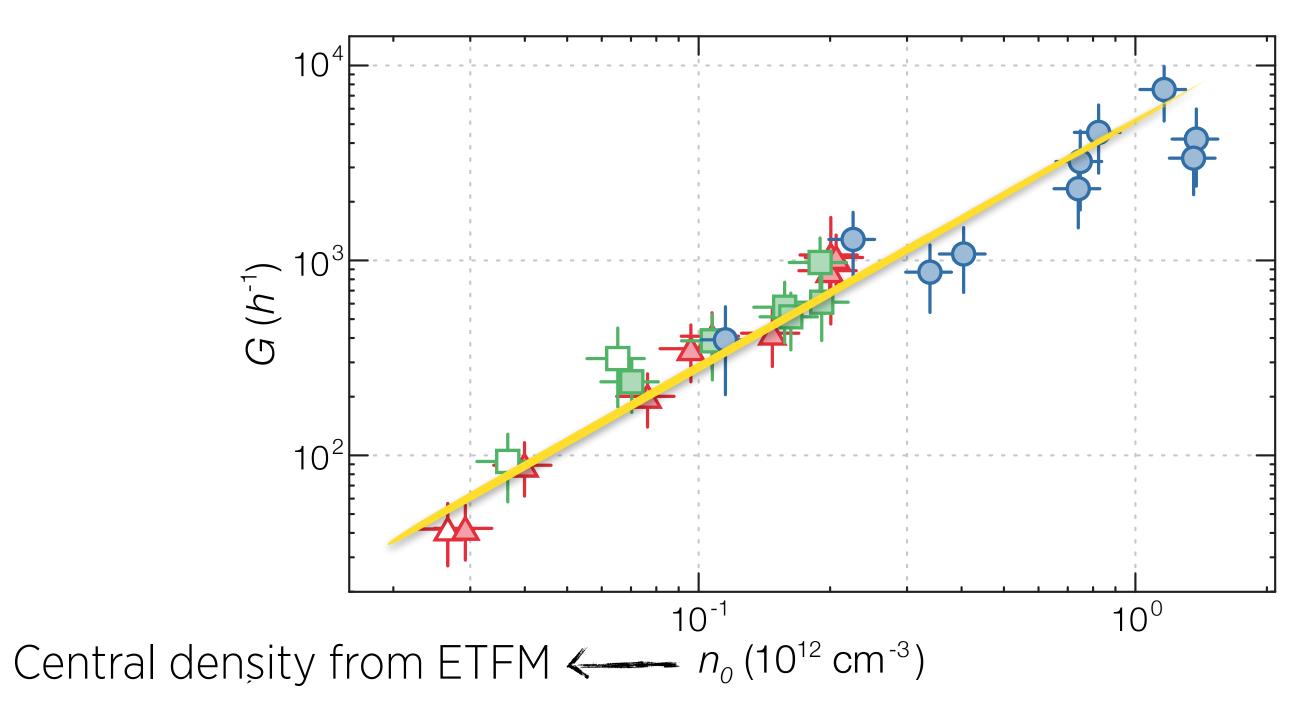
Jendrzejewski et al., *PRL* **113**, 045305 (2014)



Fitting the data with $G \propto n_0^{\alpha}$

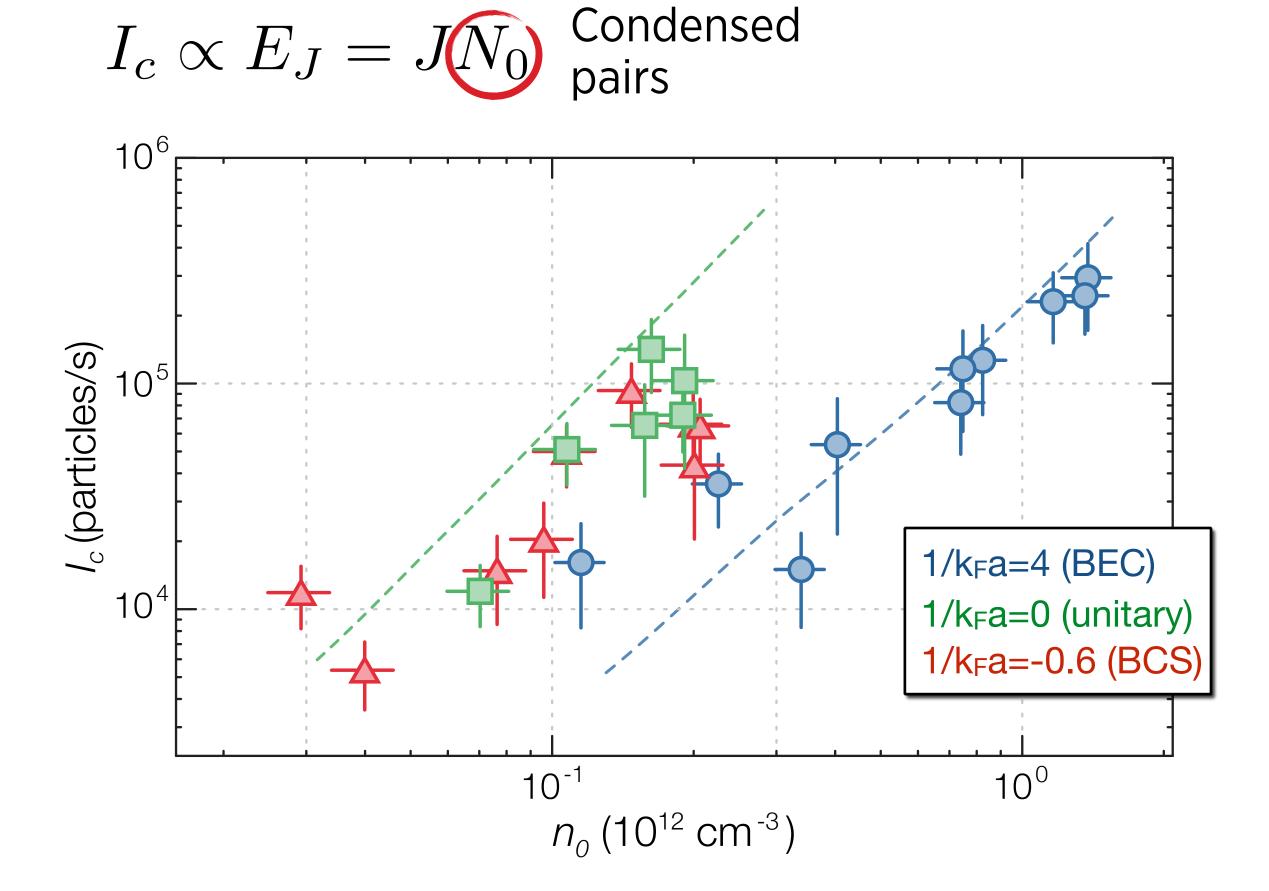
a=1.0(3) BEC $\alpha = 1.2(2)$ Unitary α=1.5(2) BCS (pair breaking?)

Same origin of resistive transport throughout BEC-BCS crossover! • Large $G \rightarrow$ composite "bosonic" nature of the tunneling particles [cf. Krinner et al. *Nature* **517** (2015)]

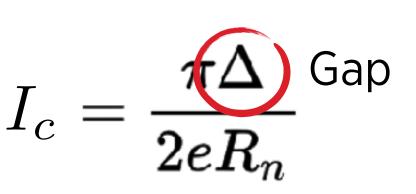




CRITICAL CURRENT Ic



Measure conductance of normal state on BCS side of resonance:





• Calculated upper bound on I_c :

 $I_{\rm c}=n_{\rm 0x}\,c_0$

Inspired by hydrodynamic scenario,
barrier as an obstacle
→ seems ok also for tunnelling regime
Spuntarelli et al., PRL. 99, 040401 (2007)
Watanabe et al., PRA 80, 053602 (2009)

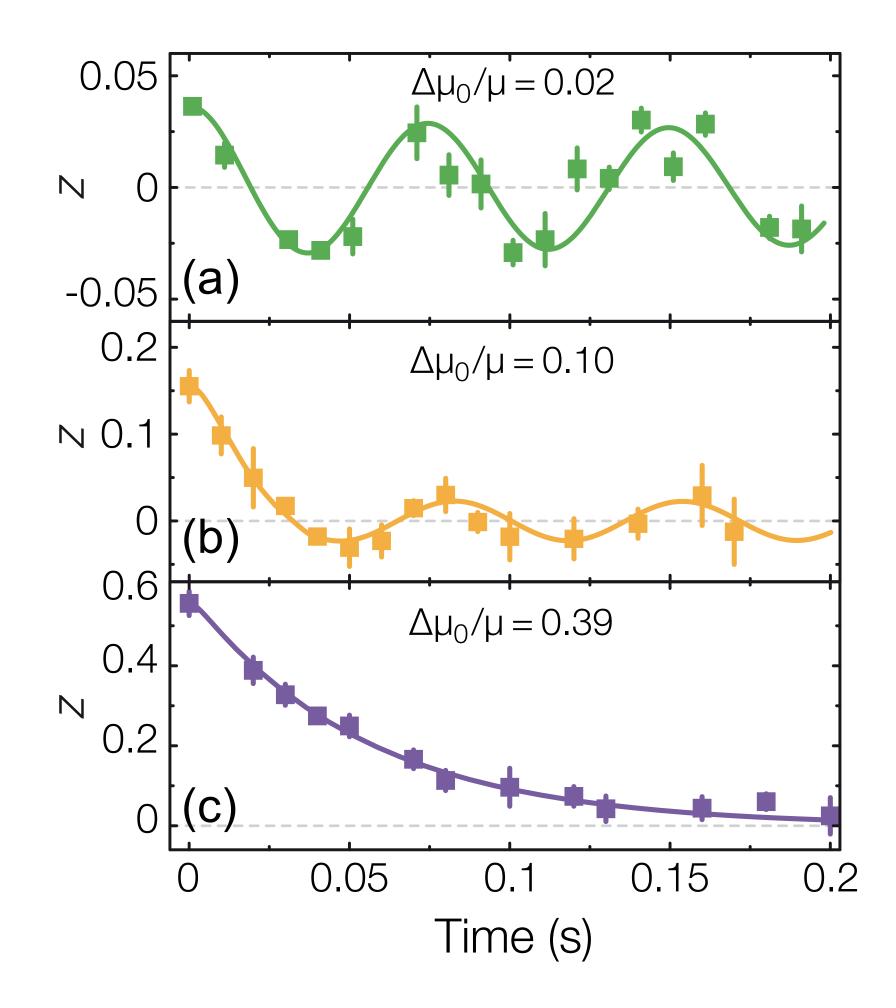
What limits the critical current on BCS side? Pair-breaking or condensate depletion?

Miller et al., *PRL* **99** (2007) Valtolina et al., *Science* **350** (2015)



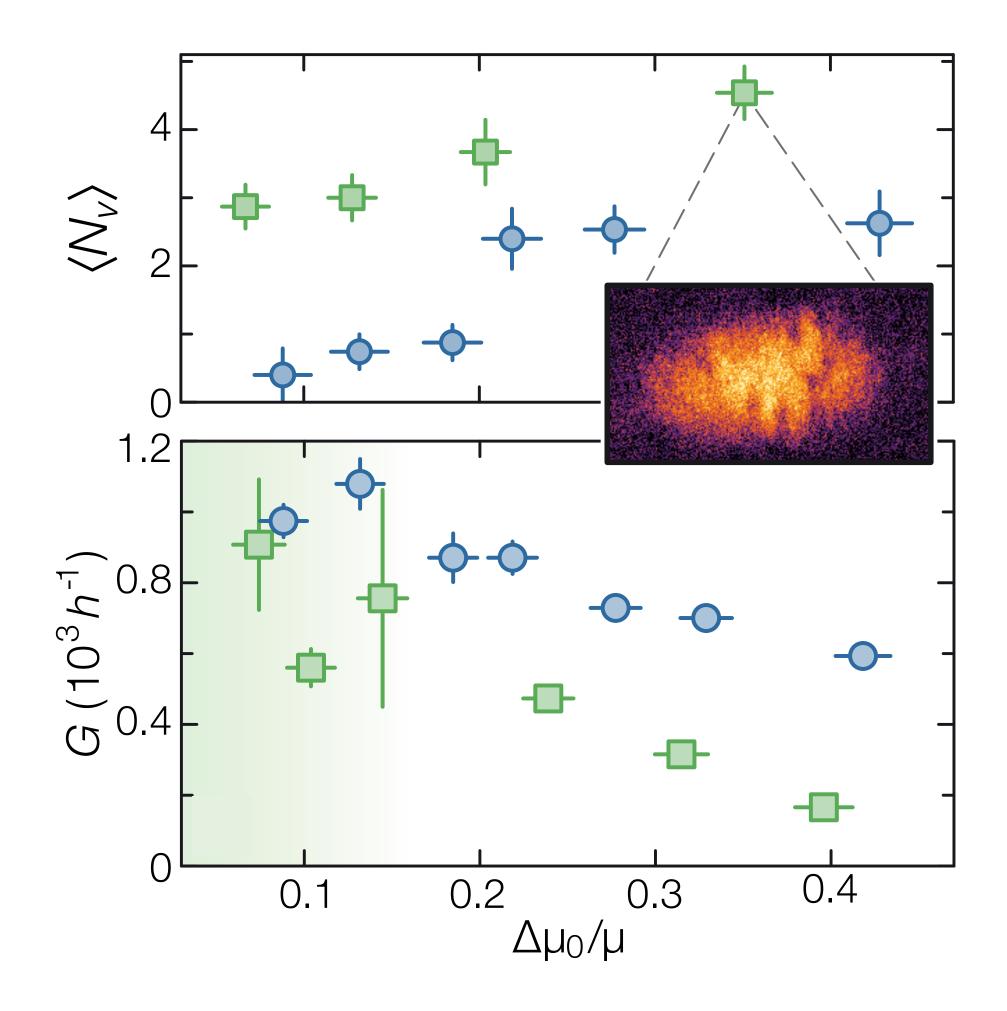
INCOHERENT TUNNELLING REGIME

Increasing the initial imbalance $z_0 > 0.3 \rightarrow$ **Disappearance of coherent oscillations**



Conductance decreases: saturation of phase-slippage rate. What is the cause?



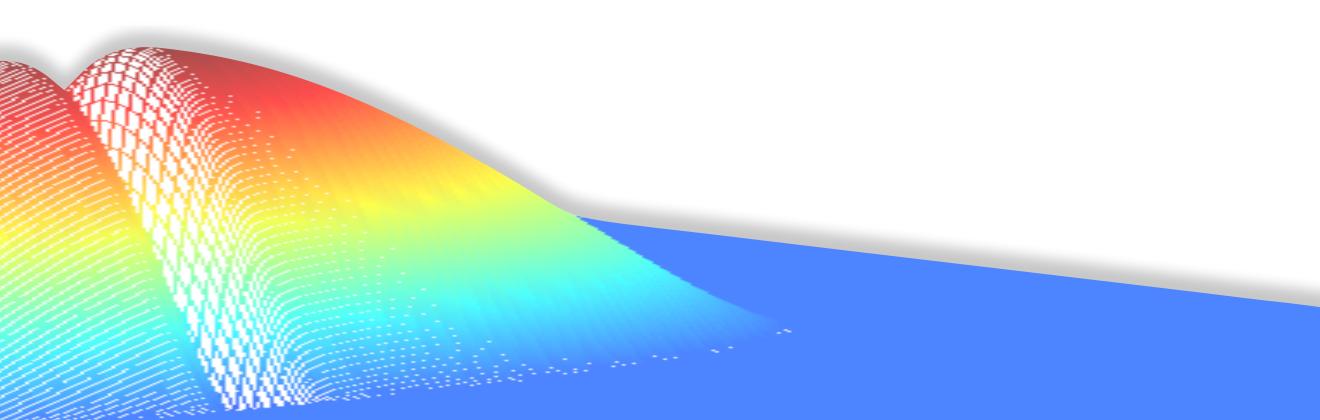




THE PLAN

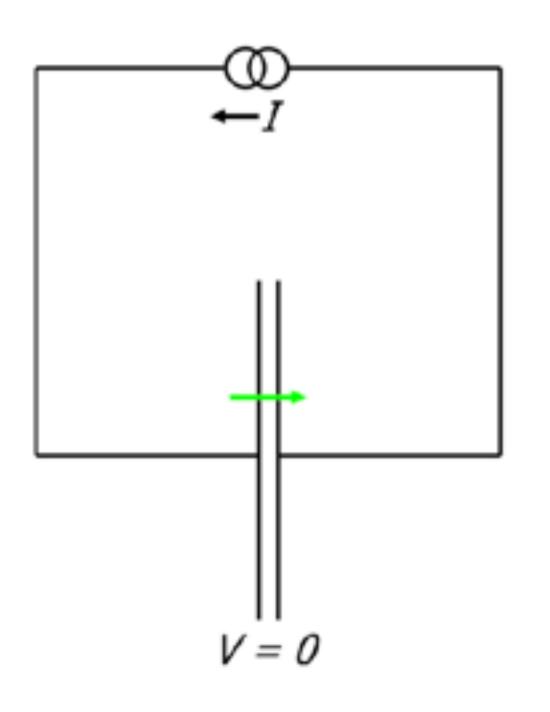
- Introduction: ultracold Fermi gases across the BEC-BCS crossover
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- Current-driven junctions: probing the critical current via the **DC Josephson** effect \rightarrow Ongoing...
- Outlook: local manipulation and quantum transport of two-dimensional gases







CURRENT-BIASED JUNCTION



DC Josephson current

Tunnelling super current without bias $I < I_c$

<u>Ultracold bosons:</u>

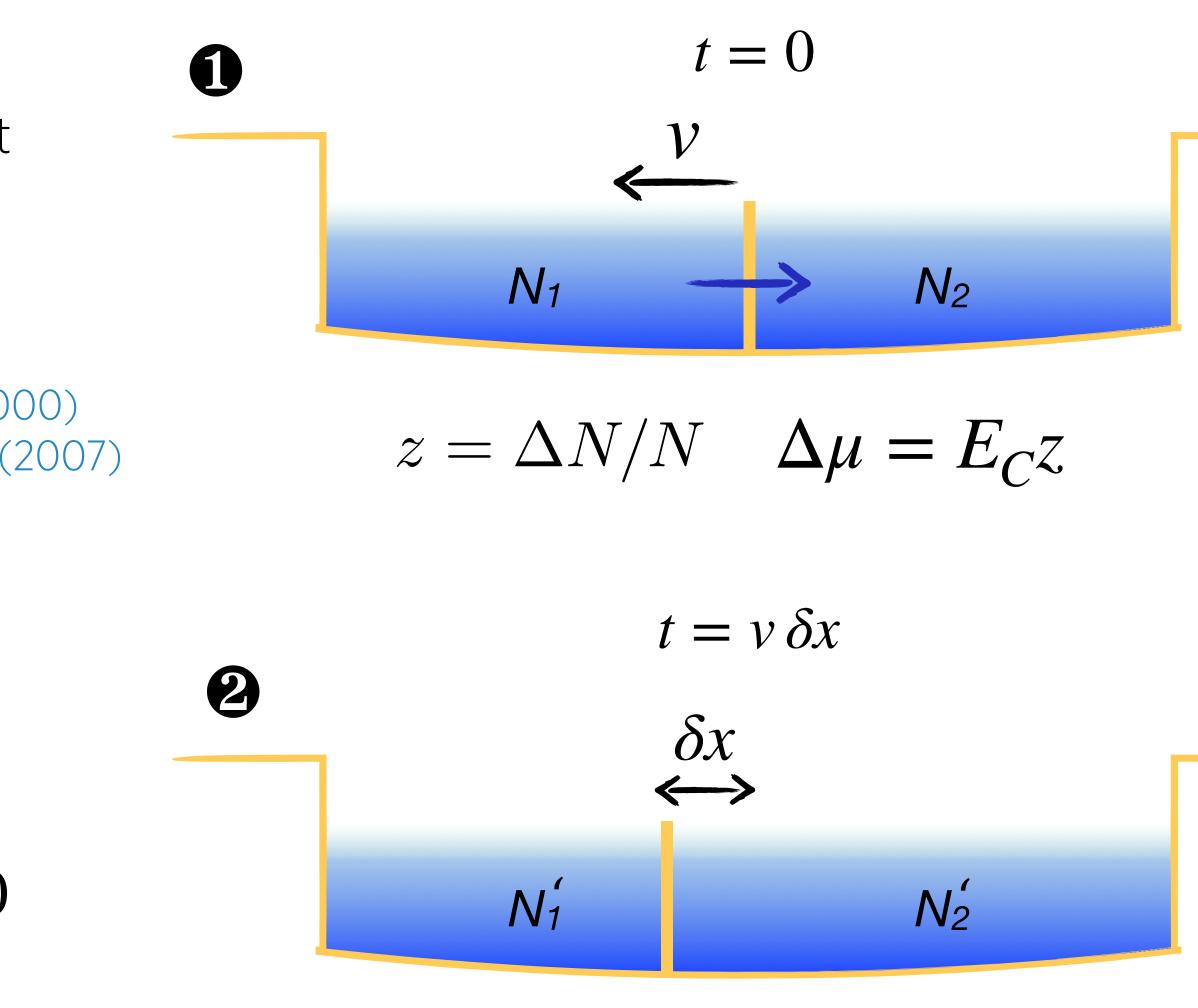
Giovanazzi et al., *PRL* **84** (2000) Levy et al., *Nature* **449**, 579 (2007) Ryu et al., *PRL* **111** (2013)

$$\hbar\dot{\phi}(t) = -\Delta\mu = \mu_R - \mu_L$$

$$I = I_c \sin\phi - G\Delta\mu \quad \overrightarrow{\Delta\mu} = 0$$

$$I < I_c$$

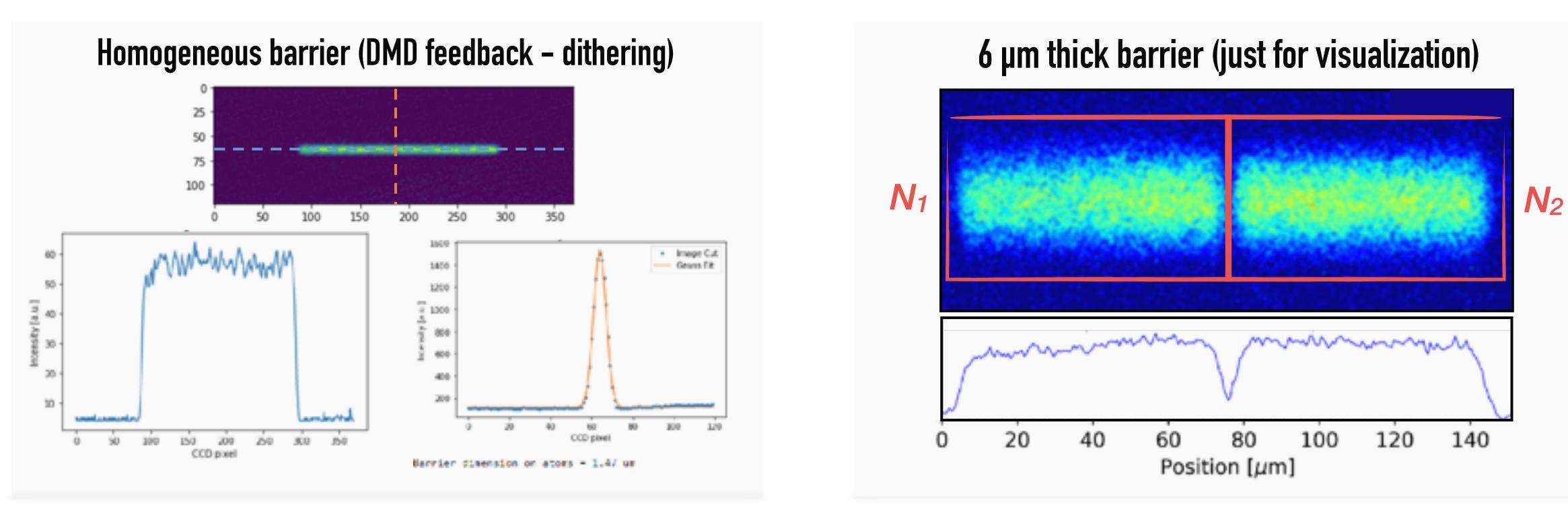


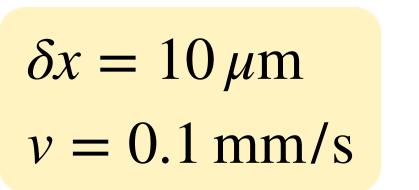


 $\Delta \mu = E_C(z - z_{eq})$



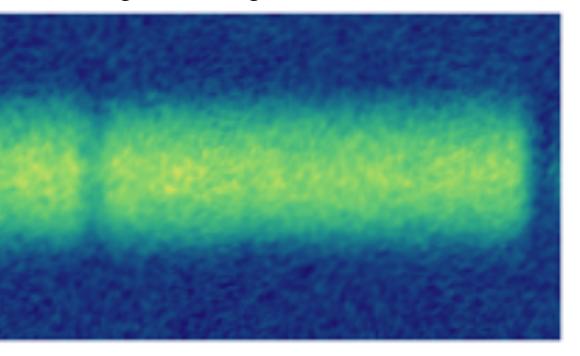
CURRENT-BIASED JUNCTION: EXPERIMENT







Unitary gas (raw images, single shots)

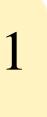


$$V_0/\varepsilon_F \simeq 0.8 \rightarrow V_0/\mu >$$

 $w = 1.5 \,\mu\text{m}, k_F w \approx 3$







DC JOSEPHSON EFFECT

Move barrier through the gas at constant velocity along $10 \, \mu m$ For final off-centered barrier, $z_{eq} \neq 0$ $\Delta \mu = E_C(z - z_{eq}) \longrightarrow |z_{eq}| \simeq 0.15$ for 10 µm movement

 $v \simeq 0.3 \text{ mm/s}$

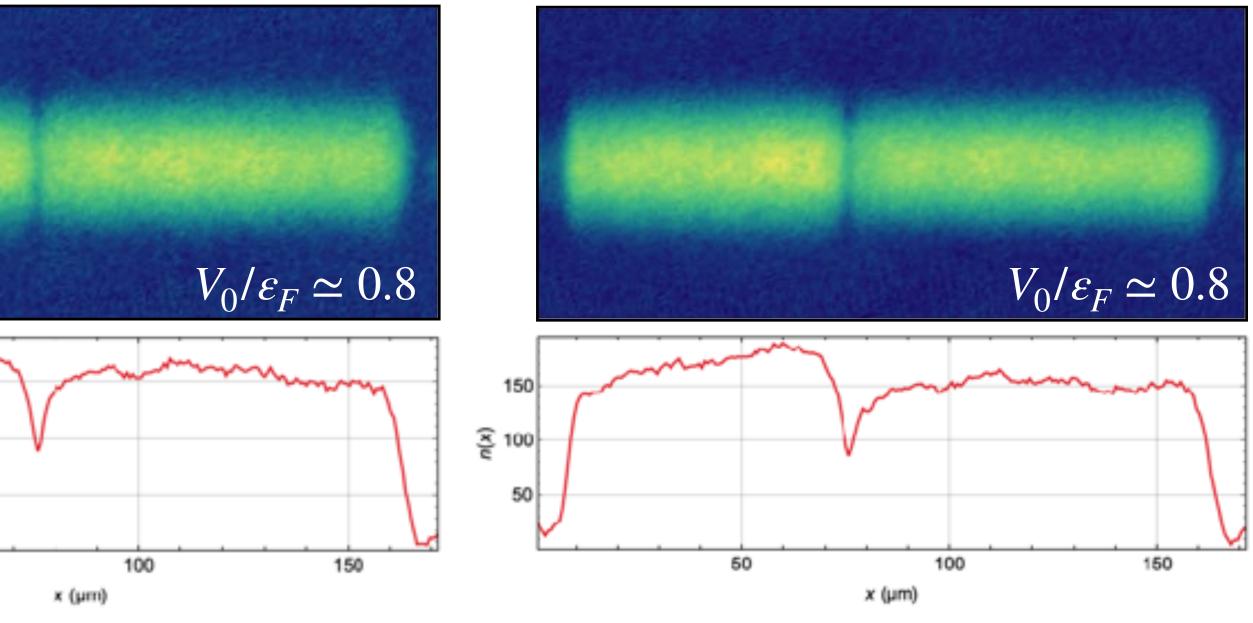
 $V_0/\varepsilon_F \simeq 0.8$ 150 150 2 100 E ~ 100 50 50 150 50 50 100 x (µm)



Sound velocity (bulk): $c \approx 10 \text{ mm/s}$

 $v \simeq 0.8 \text{ mm/s}$

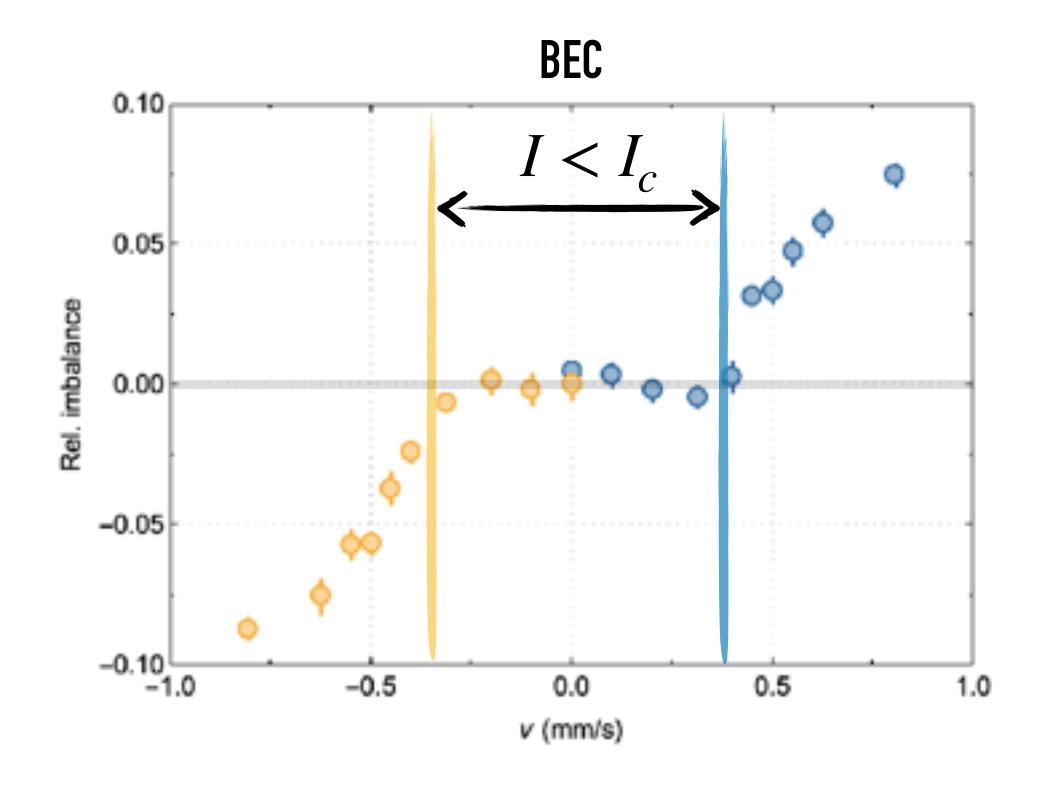




Below critical velocity, superfluid flows entirely through barrier!



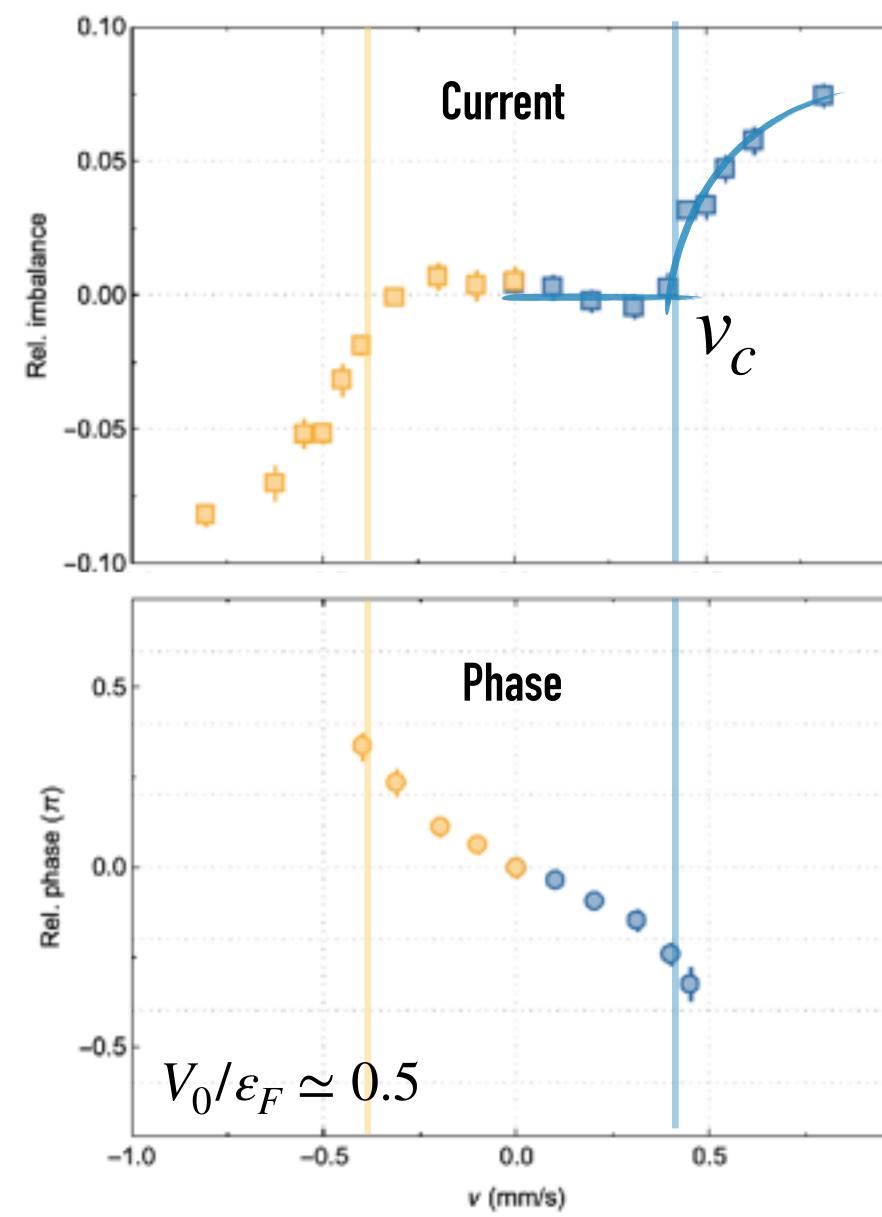
IV CURVE AND CURRENT-PHASE RELATION

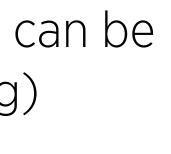


Clear footprint of DC Josephson effect ! Evolution can be modelled by RC-shunted junction circuit (...ongoing)

Above critical current: finite $\Delta \mu$ is created, but smaller than superfluid gap -> no excitation of quasiparticle branch Only AC/MQST branch (unstable)



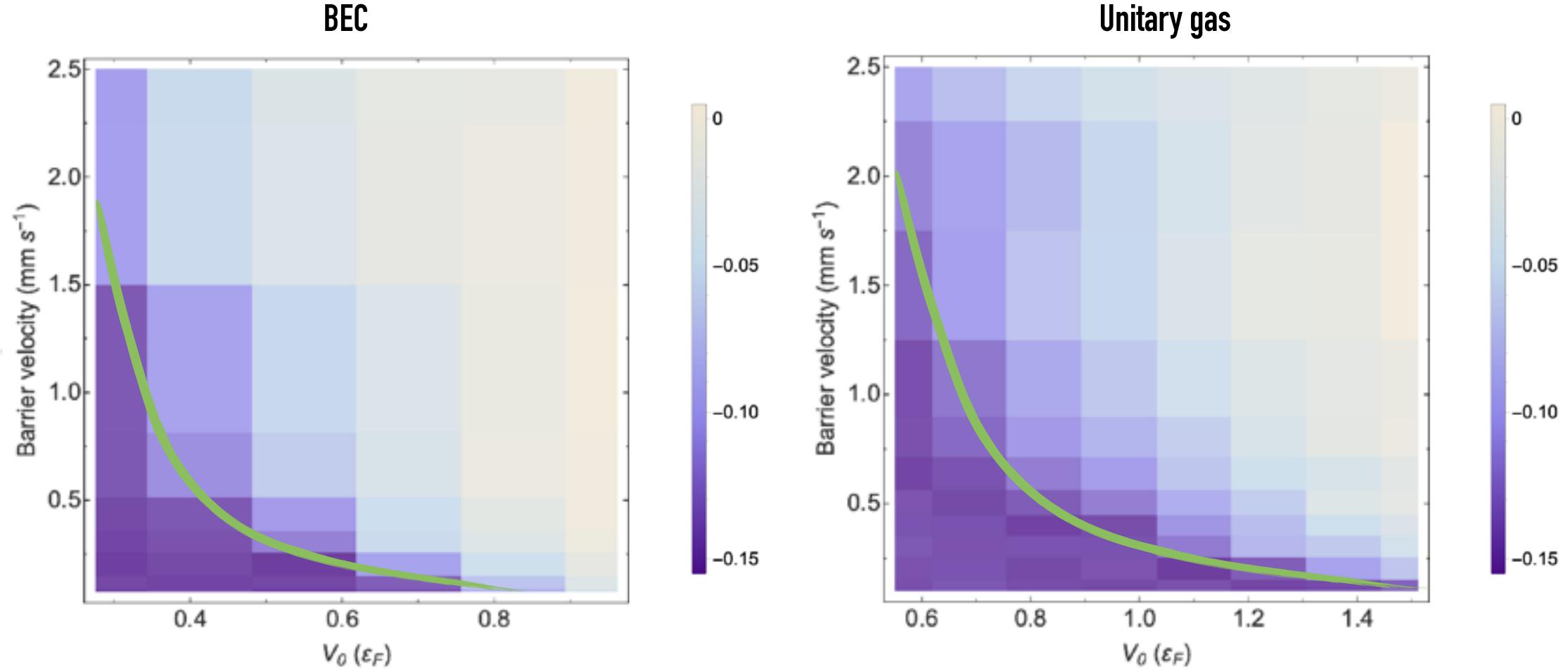






CRITICAL VELOCITY

> Map out imbalance after barrier movement at variable height Vo and speed v



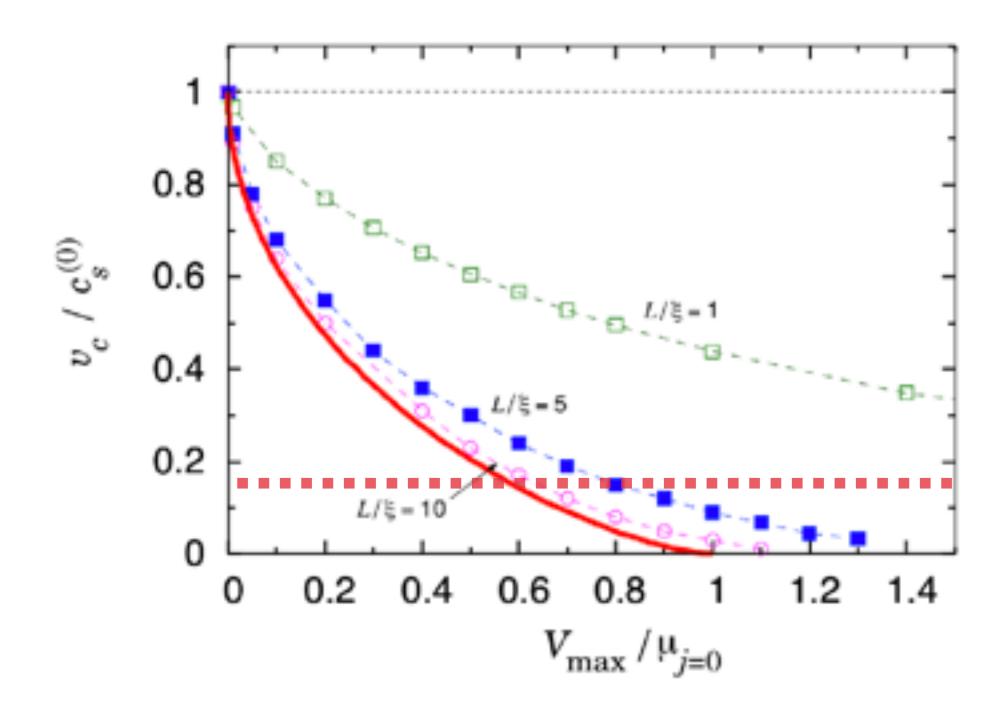




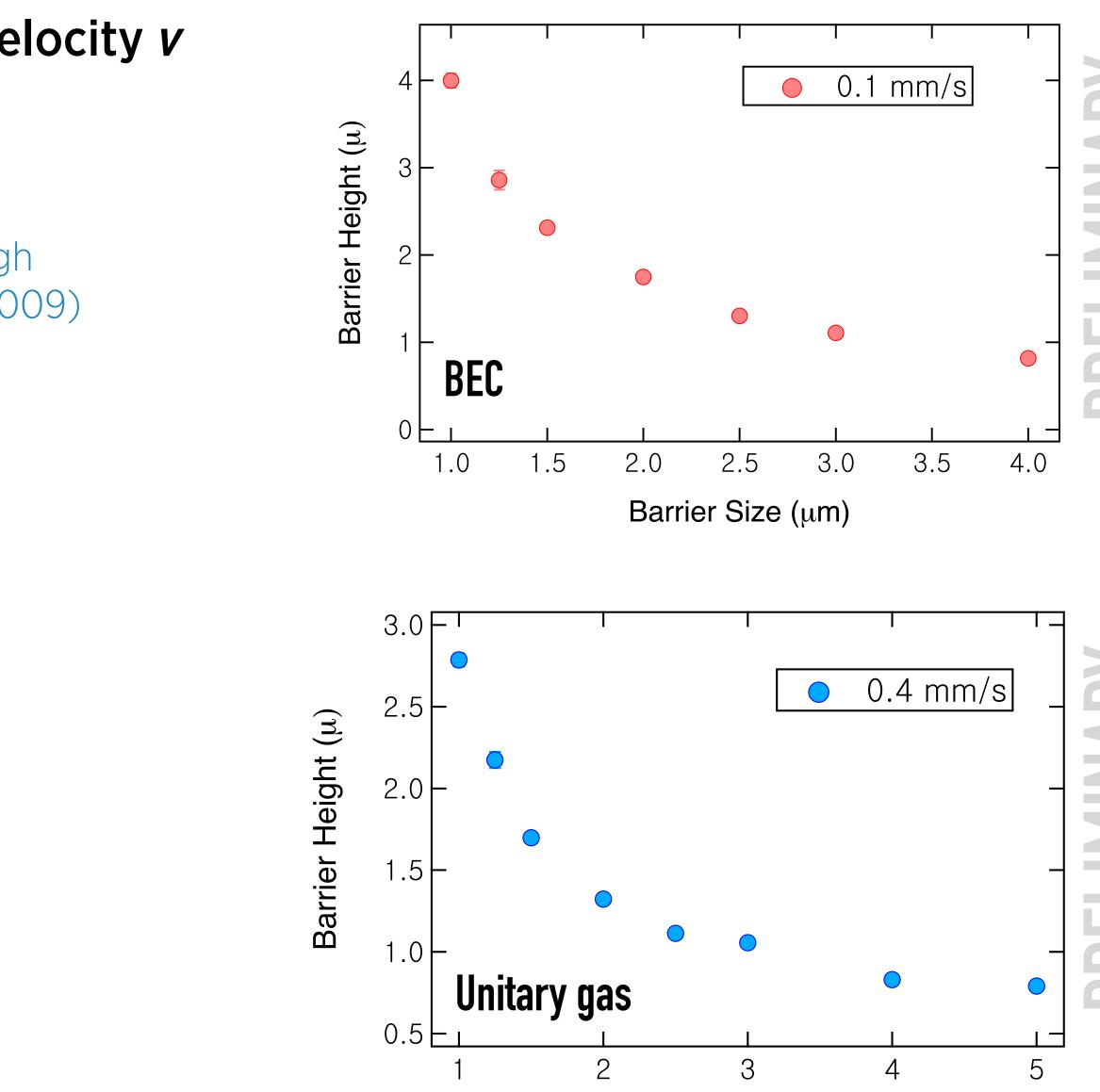
CRITICAL BARRIER HEIGHT VS SIZE

Extract critical barrier height V₀ at constant velocity v
 varying the barrier size

Watanabe et al., "Critical velocity of superfluid flow through single barrier and periodic potentials". *PRA* **80**, 053602 (2009)





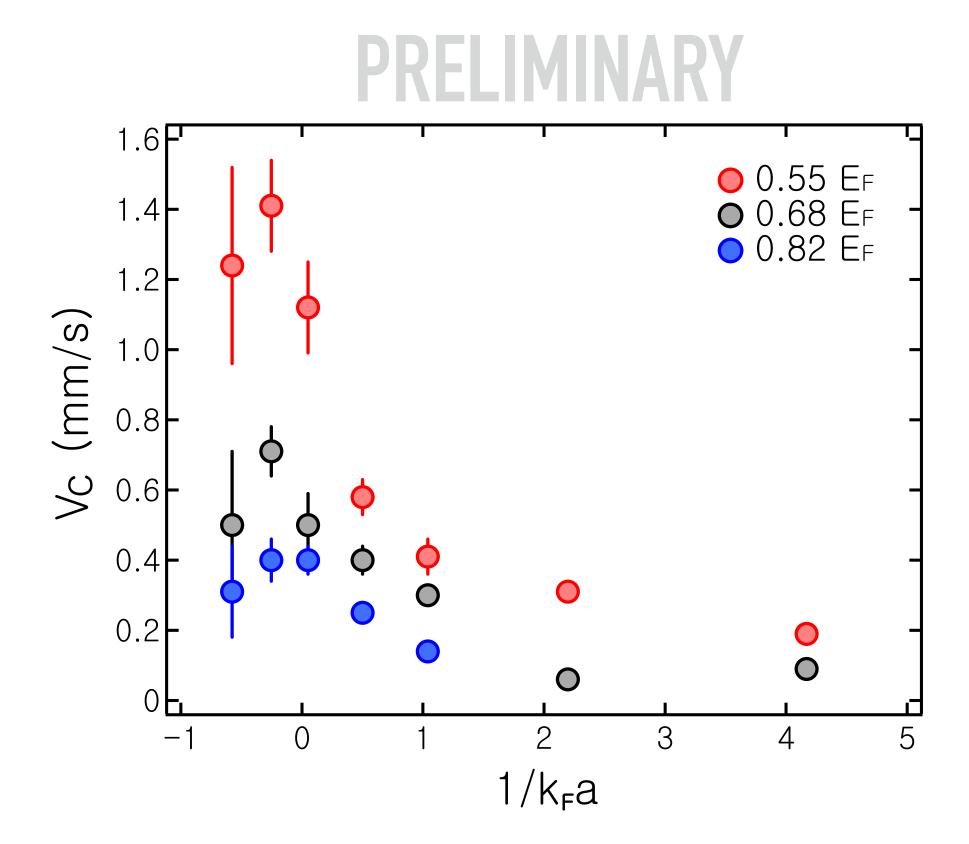


Barrier Size (µm)



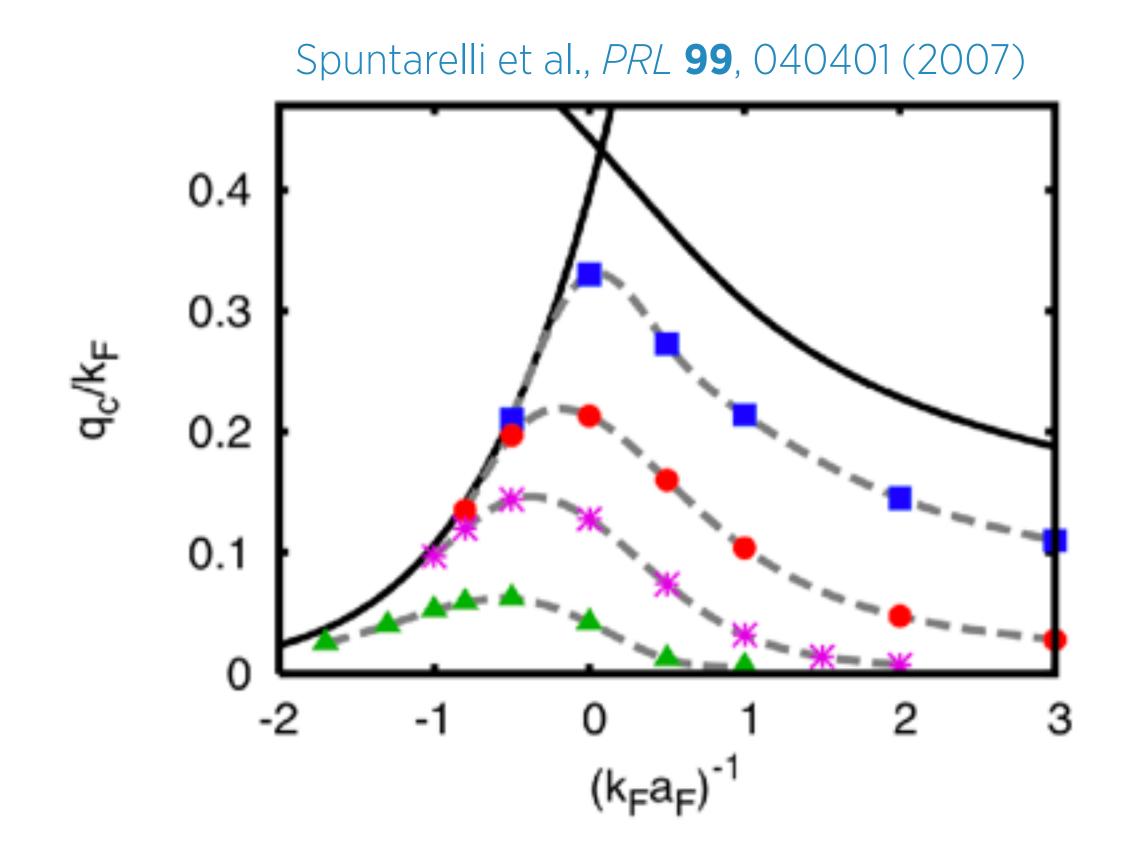
CRITICAL VELOCITY VS INTERACTION STRENGTH

Extract critical velocity as a function of $1/(k_{F}a)$



Maximum critical velocity is located slightly on BCS side of resonance







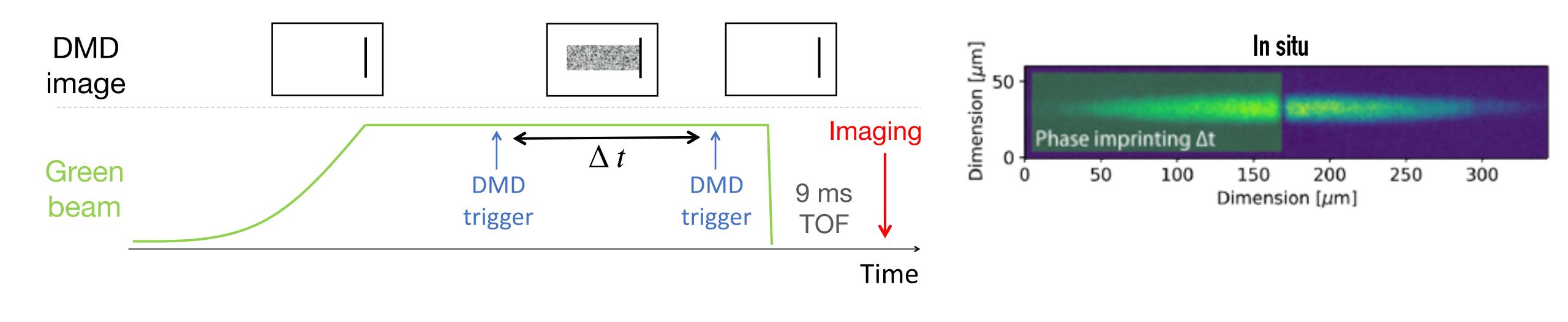
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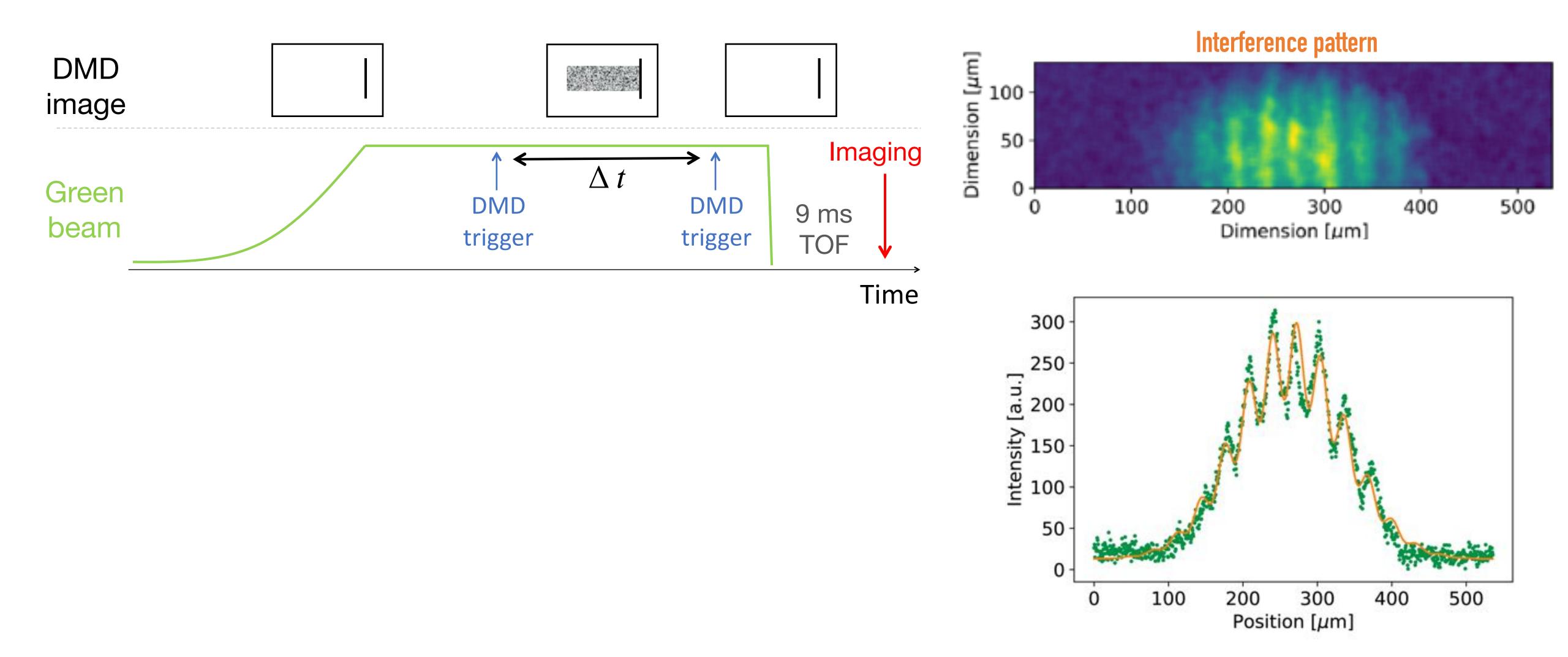
LOCAL PHASE CONTROL: PHASE IMPRINTING







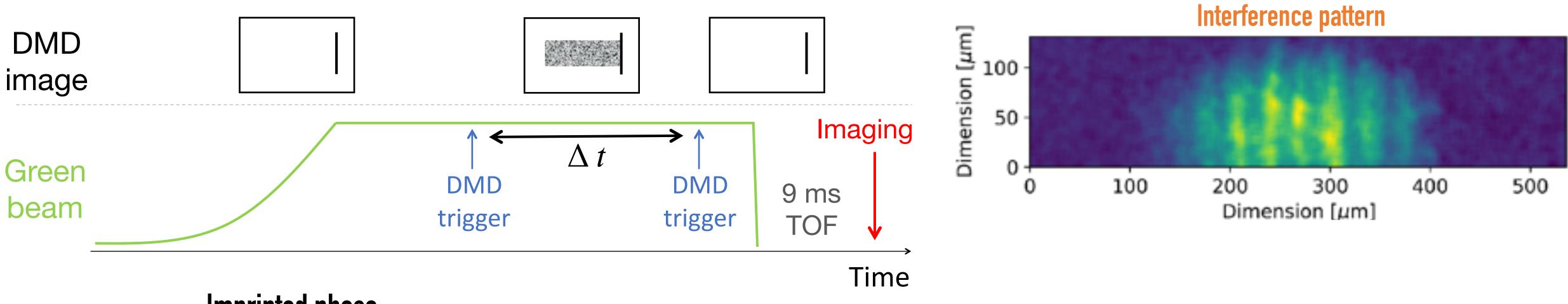
LOCAL PHASE CONTROL: PHASE IMPRINTING



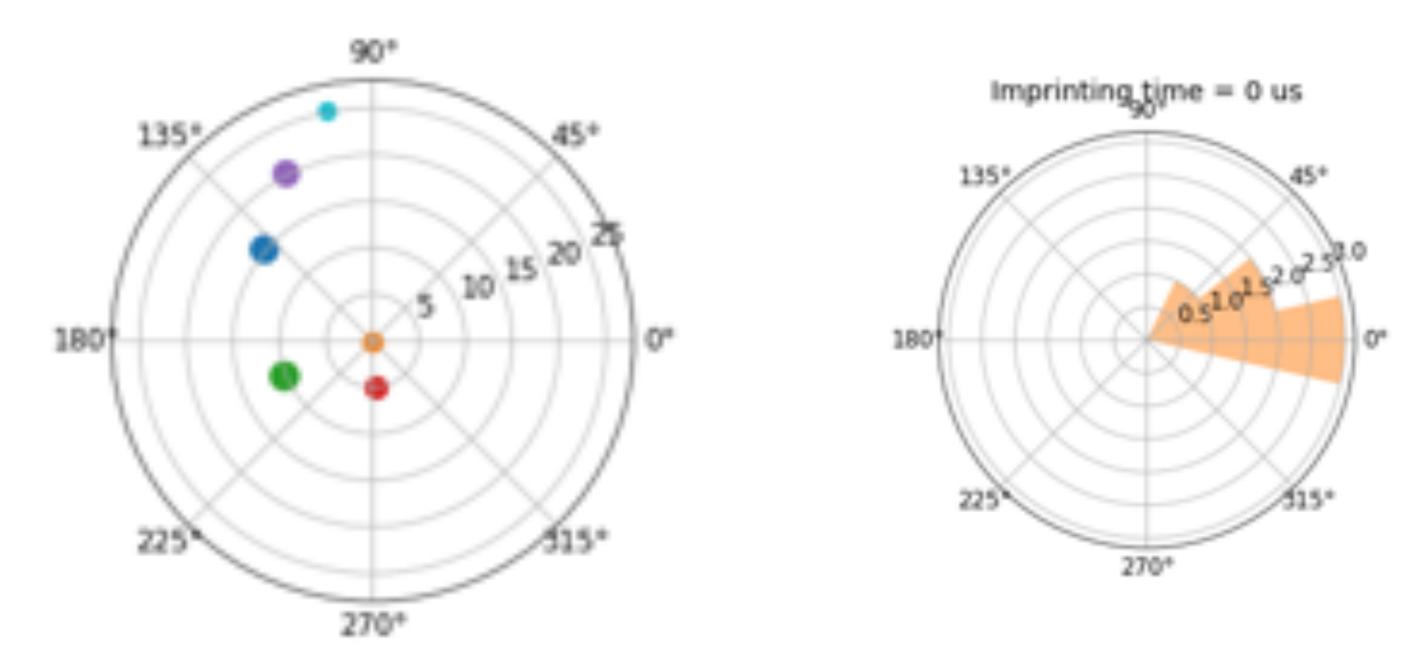




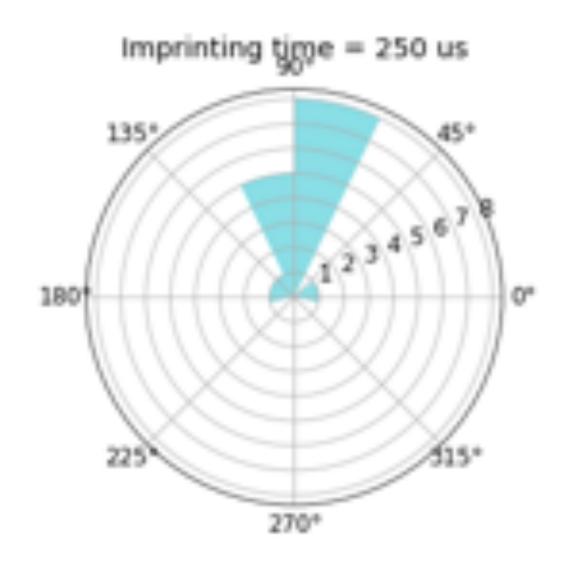
LOCAL PHASE CONTROL: PHASE IMPRINTING



Imprinted phase

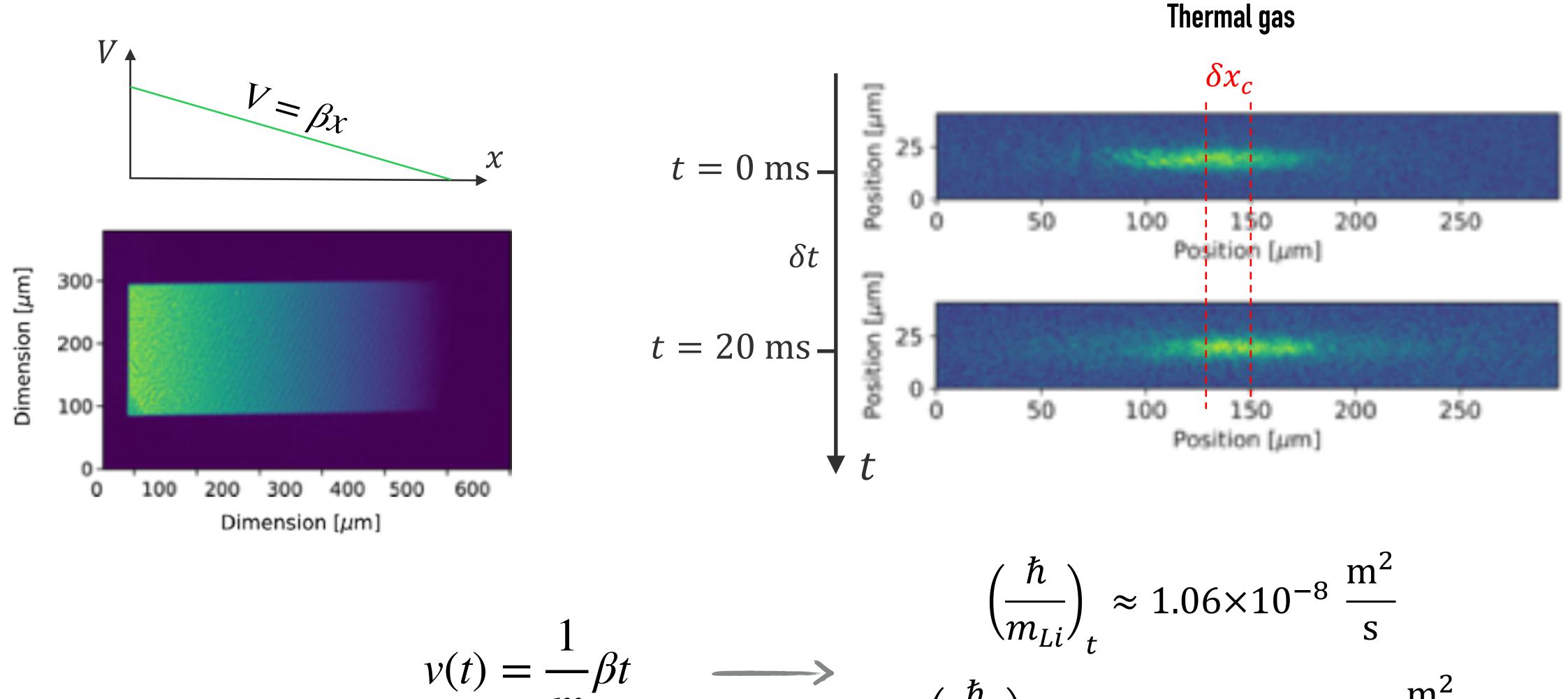








LOCAL PHASE CONTROL: VELOCITY IMPRINTING



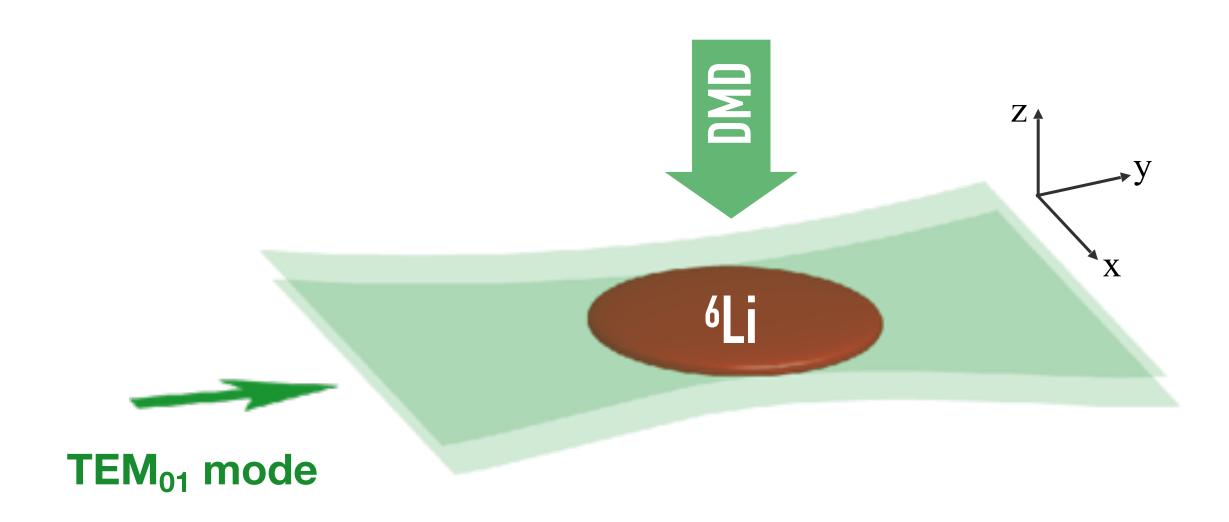
 $v(t) = -\frac{1}{m}\beta t$



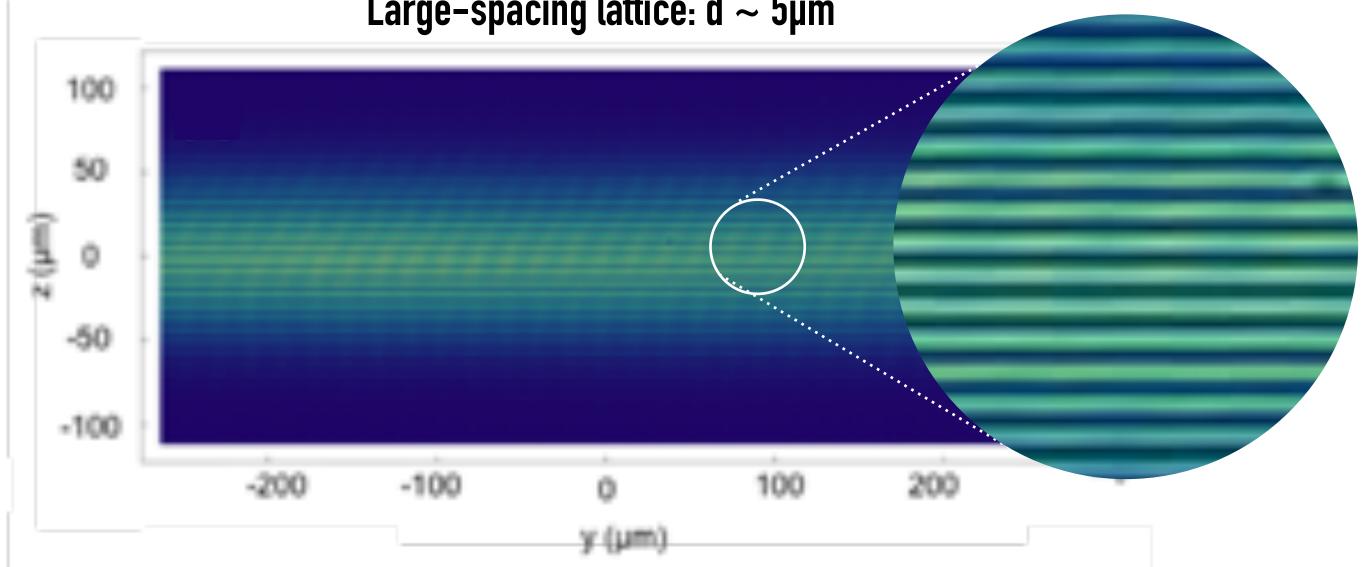
$$\left(\frac{\hbar}{m_{Li}}\right)_{t} \approx 1.06 \times 10^{-8} \frac{\mathrm{m}^{2}}{\mathrm{s}}$$
$$\left(\frac{\hbar}{m_{Li}}\right)_{m} \approx (1.4 \pm 0.2) \times 10^{-8} \frac{\mathrm{m}^{2}}{\mathrm{s}}$$



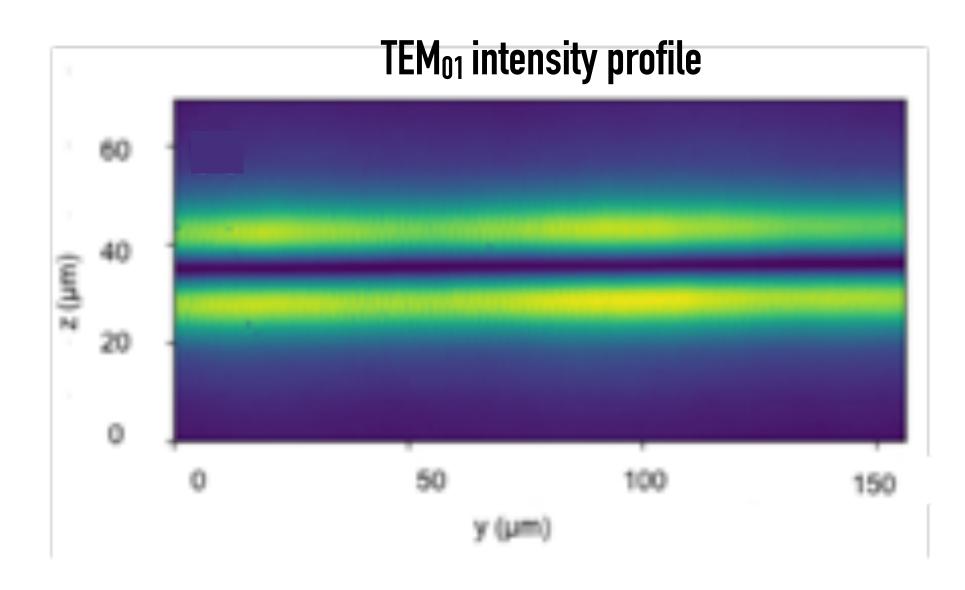
TWO-DIMENSIONAL POTENTIALS

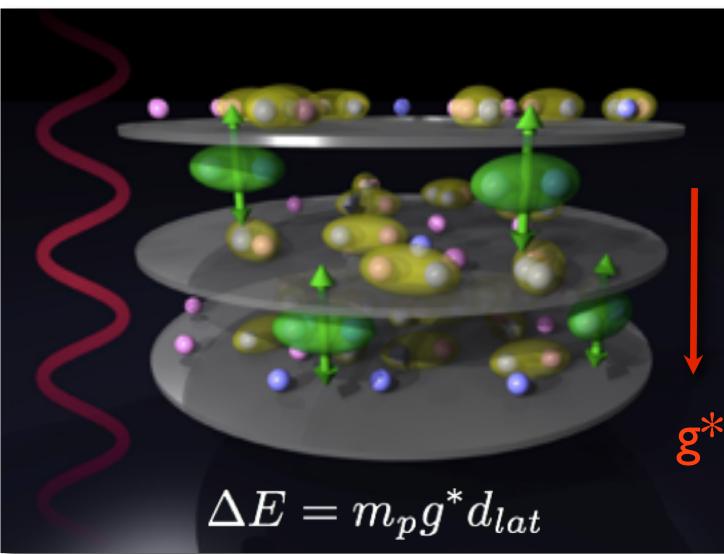


Large-spacing lattice: $d \sim 5 \mu m$













THE LITHIUM LAB AT LENS

















Massimo Inguscio

Collaborators and former members:

Nick Proukakis (Newcastle) Andrea Trombettoni (Trieste) Pietro Massignan (UPC) Wolfgang Ketterle (MIT) Luca Pezzé (CNR-INO)

Giacomo Valtolina (JILA) Alessia Burchianti (CNR-INO) Chiara Fort (University of Florence) Eleonora Lippi (Heidelberg)



Qombs

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