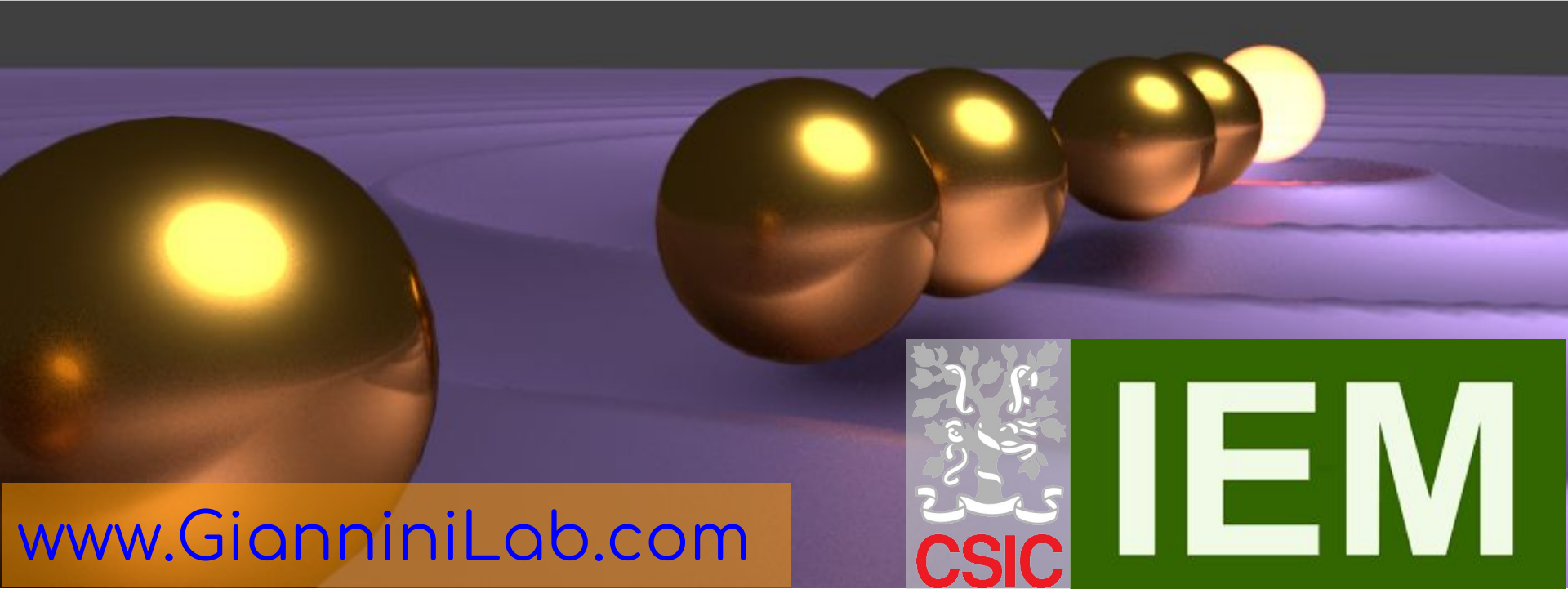


TOPOLOGICAL NANOPHOTONICS

VINCENZO GIANNINI



www.GianniniLab.com







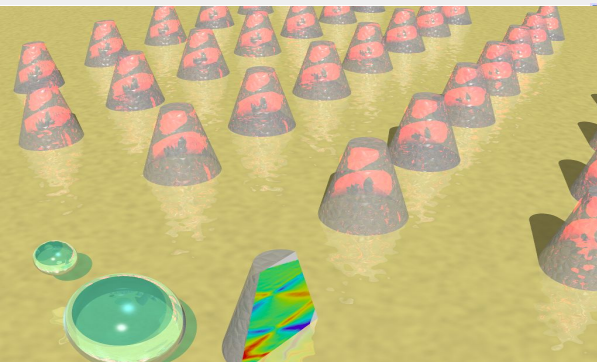
Derek Lee



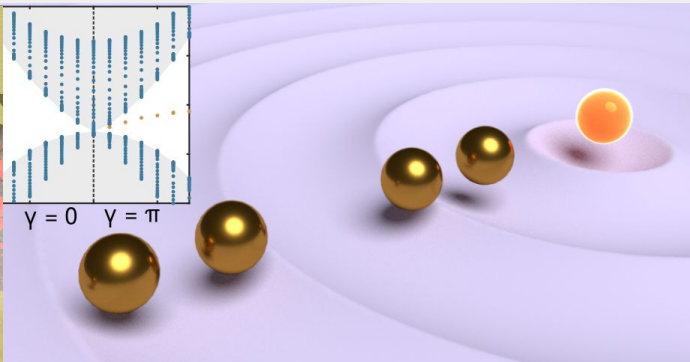
Peter Haynes



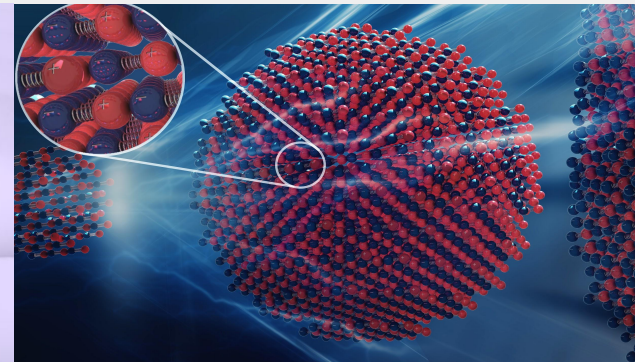
Paloma Arroyo Huidobro



Phonon Polaritons



Topological
Nanophotonics

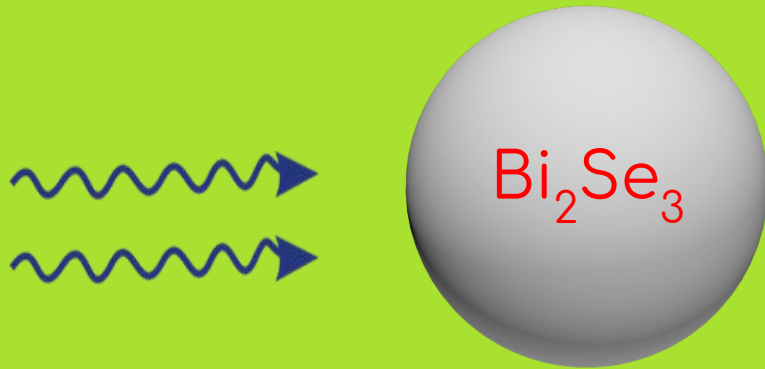


Quantum Plasmonics

Condensed Matter Theory

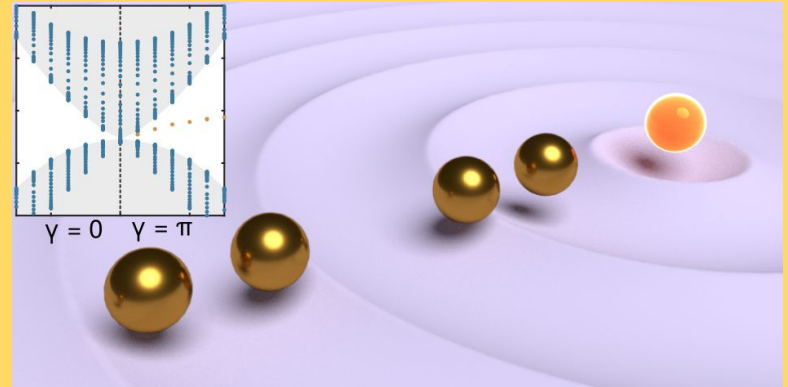
TOPOLOGICAL NANOPHOTONICS

Topological Quantum Dots



Experimental
evidences

Topological Plasmonic Chain



Protected
Hot-Spots

MOTIVATIONS

Robustness of subwavelength modes against:

1. Unidirectional light propagation
2. Low threshold lasing
3. No scattering from sharp bending
4. Disordered domain

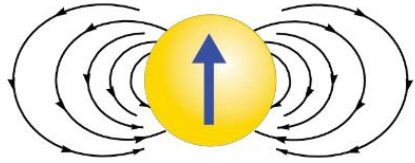
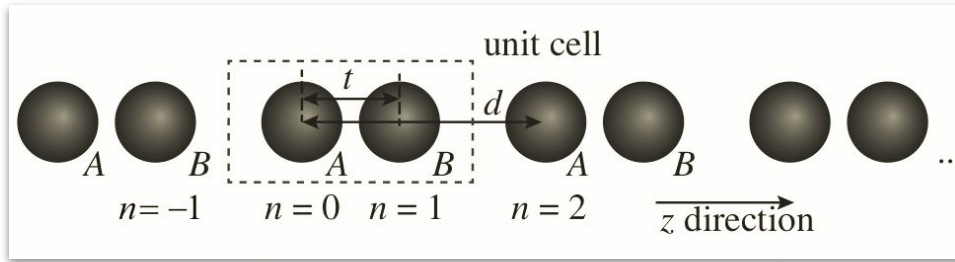
Journal of
Applied Physics

PERSPECTIVE

scitation.org/journal/jap

**A perspective on topological nanophotonics:
Current status and future challenges**

TOPOLOGICAL PLASMONIC CHAIN...



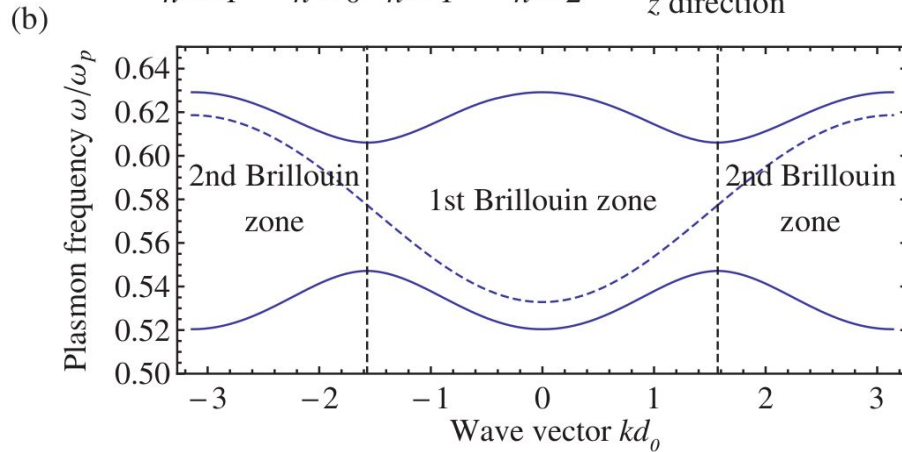
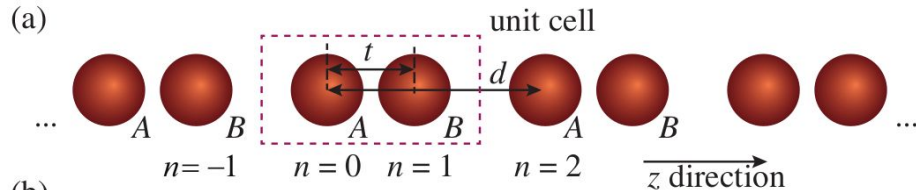
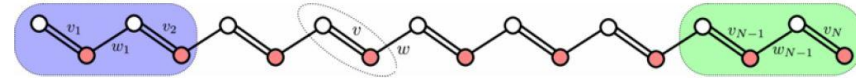
$$\frac{1}{\alpha(\omega)} \mathbf{p}_n = \sum_{j=1}^N G(\mathbf{r}_n, \mathbf{r}_j) \mathbf{p}_j$$

$$G_{\text{long}}(r_{nj}, \omega) = \frac{2e^{ikr_{nj}}}{4\pi\epsilon_0} \left(\frac{1}{r_{nj}^3} - \frac{ik}{r_{nj}^2} \right)$$

$$G_{\text{trans}}(r_{nj}, \omega) = \frac{-e^{ikr_{nj}}}{4\pi\epsilon_0} \left(\frac{1}{r_{nj}^3} - \frac{ik}{r_{nj}^2} - \frac{k^2}{r_{nj}} \right)$$

SSH MODEL: PLASMONIC CHAIN

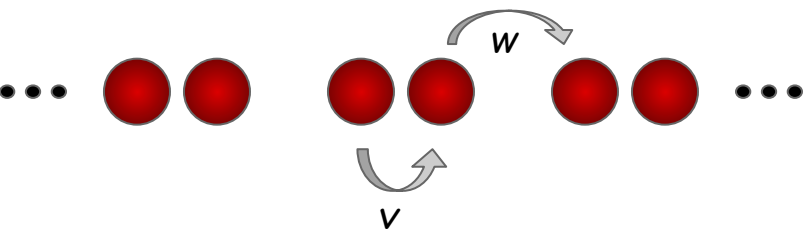
Su-Schrieffer-Heeger



$$\alpha^{-1} p_n = \begin{cases} \frac{2}{4\pi\epsilon_0} \left[\frac{p_{n-1}}{(d-t)^3} + \frac{p_{n+1}}{t^3} \right], & \text{for } n \text{ is even} \\ \frac{2}{4\pi\epsilon_0} \left[\frac{p_{n-1}}{t^3} + \frac{p_{n+1}}{(d-t)^3} \right], & \text{for } n \text{ is odd} \end{cases}$$

$$p_n(k) = \begin{cases} p_A(k) e^{ik \frac{n}{2} d}, \\ p_B(k) e^{ik (\frac{n-1}{2} d)} \end{cases}$$

SSH MODEL: PLASMONIC CHAIN



$$|m, \alpha\rangle \rightarrow |m\rangle \otimes |\alpha\rangle \in \mathcal{H}_{\text{external}} \otimes \mathcal{H}_{\text{internal}}$$

Chiral Symmetry

$$\sigma_z H \sigma_z^{-1} = -H$$

$$\sigma_z = \begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix}$$

$$\begin{bmatrix} p_A \\ p_B \end{bmatrix}$$

Eigenvector with
eigenvalue E



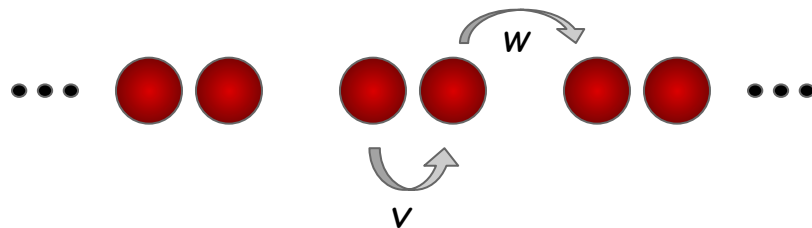
$$\begin{bmatrix} p_A \\ -p_B \end{bmatrix}$$

Eigenvector with
eigenvalue $-E$

SSH MODEL: PLASMONIC CHAIN

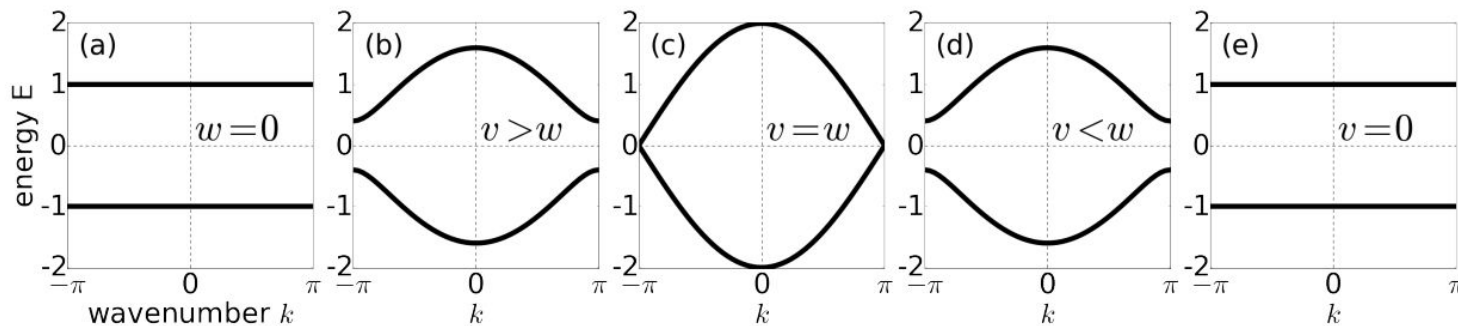
Edge states

$$H = \begin{pmatrix} 0 & v & 0 & 0 & 0 & 0 & 0 & 0 \\ v & 0 & w & 0 & 0 & 0 & 0 & 0 \\ 0 & w & 0 & v & 0 & 0 & 0 & 0 \\ 0 & 0 & v & 0 & w & 0 & 0 & 0 \\ 0 & 0 & 0 & w & 0 & v & 0 & 0 \\ 0 & 0 & 0 & 0 & v & 0 & w & 0 \\ 0 & 0 & 0 & 0 & 0 & w & 0 & v \\ 0 & 0 & 0 & 0 & 0 & 0 & v & 0 \end{pmatrix}$$



Chiral Symmetry

$$\sigma_z H \sigma_z^{-1} = -H$$



TOPOLOGICAL PLASMONIC CHAIN



✓ Cite This: *ACS Photonics* 2018, 5, 2271–2279



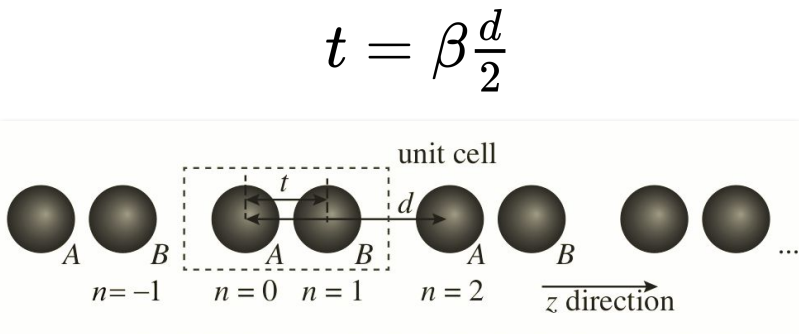
Article

Topological Plasmonic Chain with Retardation and Radiative Effects

Simon R. Pocock,^{*,†} Xiaofei Xiao,[†] Paloma A. Huidobro,[†] and Vincenzo Giannini^{†,‡,§}

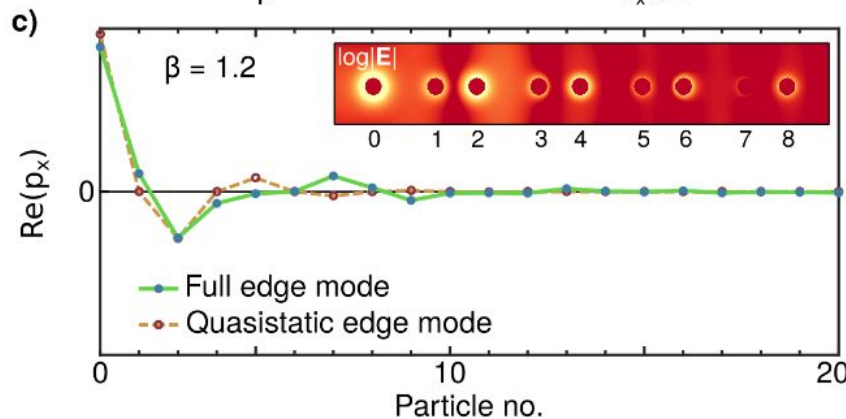
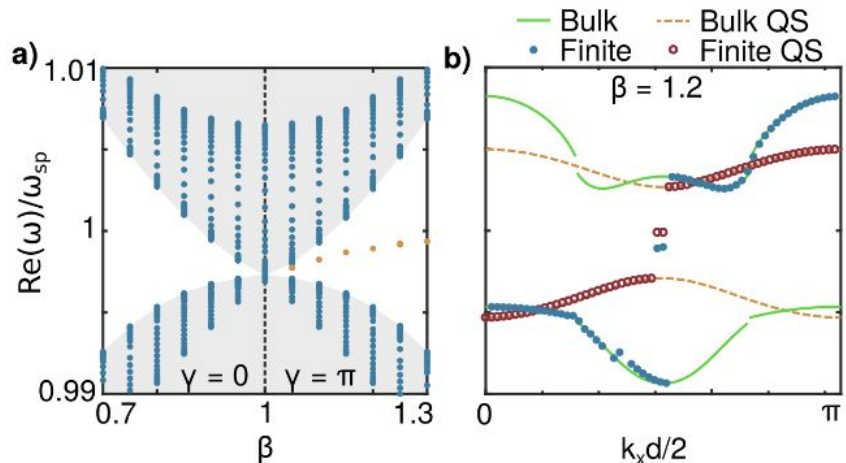
- TE and TM are different
- Long range interaction break the chiral symmetry
- Not Hermitian Hamiltonian
- Band are complex
- *Retardation Induced Phase Transitions*

TOPOLOGICAL PLASMONIC CHAIN



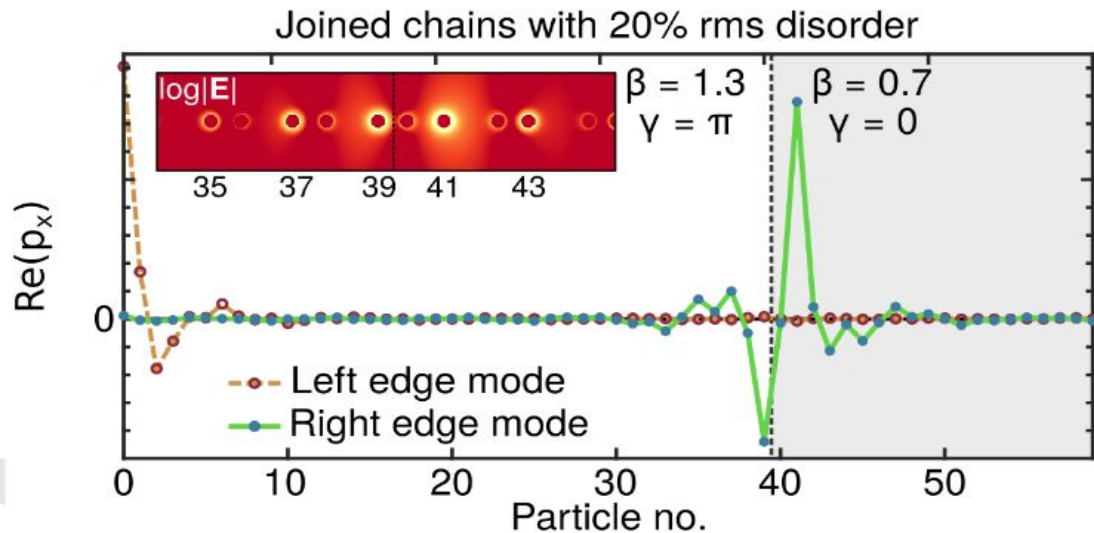
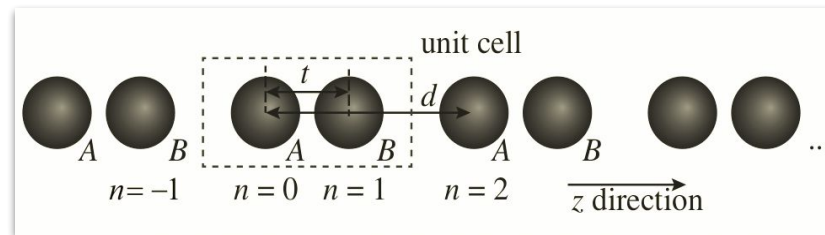
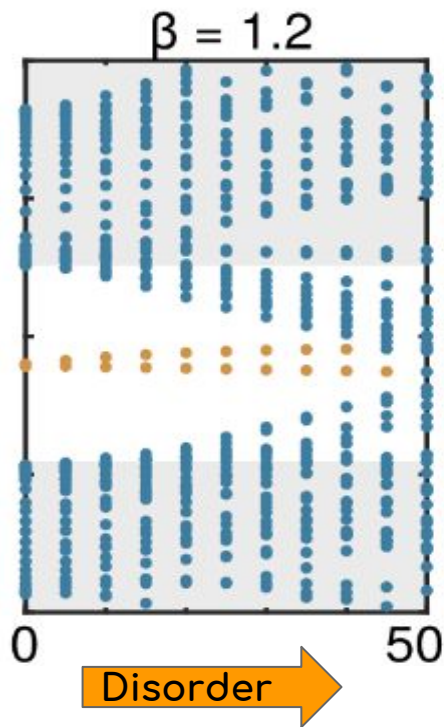
$$t = \beta \frac{d}{2}$$

Longitudinal finite 60 particle chains, $d = 250\text{nm}$, $a = 20\text{nm}$



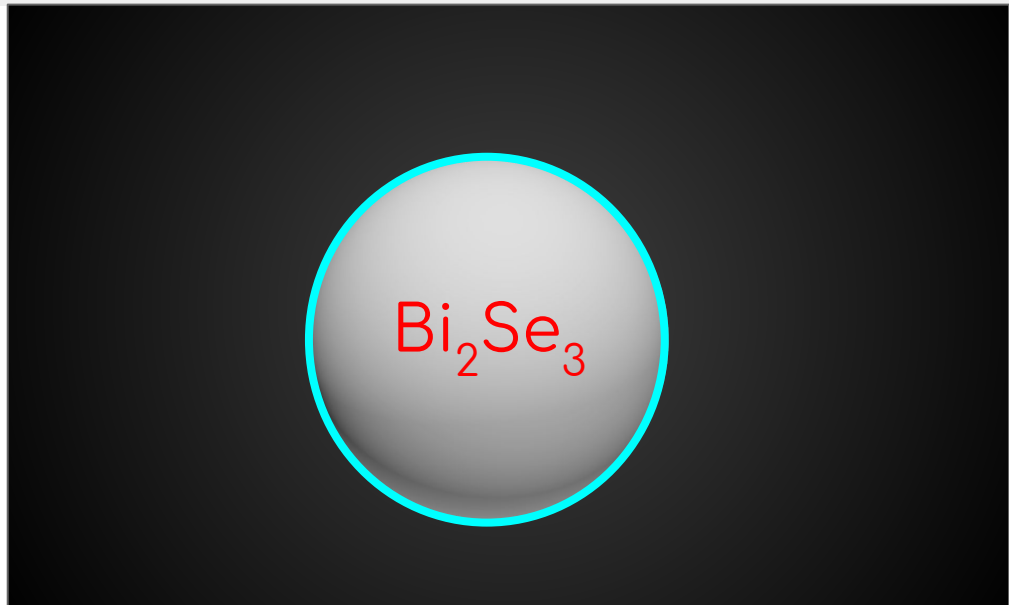
Pocock et al., ACS Phot. 5, 2271 (2018)

TOPOLOGICAL PLASMONIC CHAIN



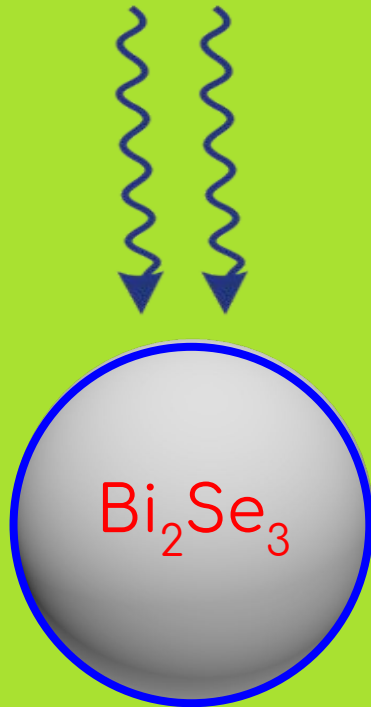
PLASMONICS WITH TOPOLOGICAL INSULATORS

Light
+
Topological
Insulator
Nanoparticle



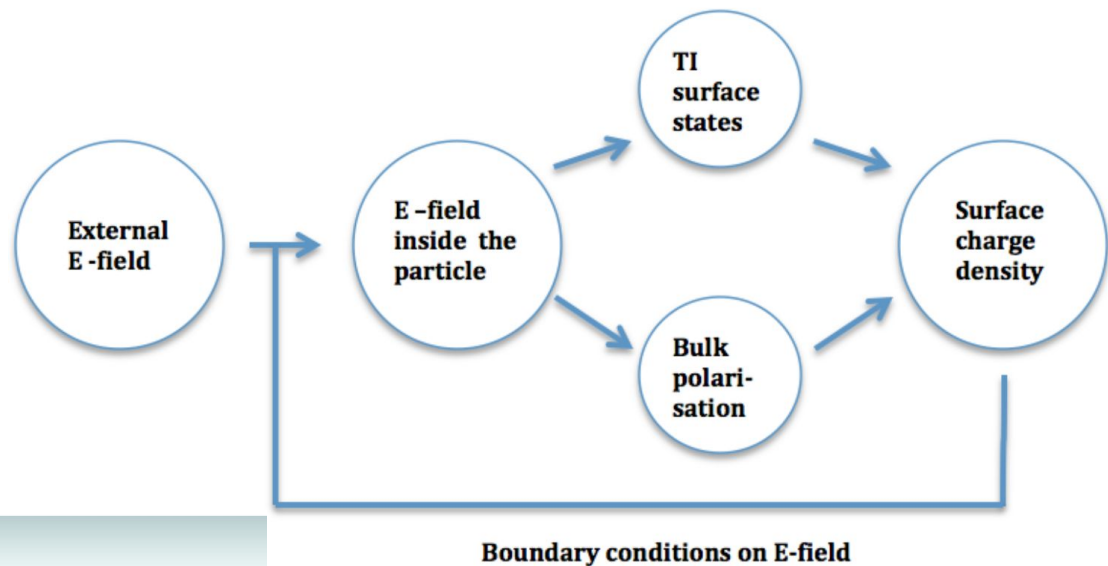
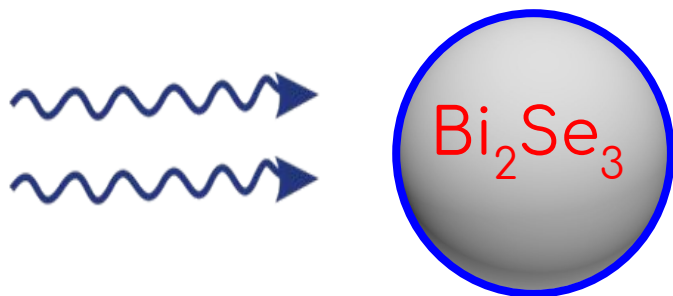
- Bulk insulator
- Topological protected conducting states on the surface

WHAT DO WE EXPECT...

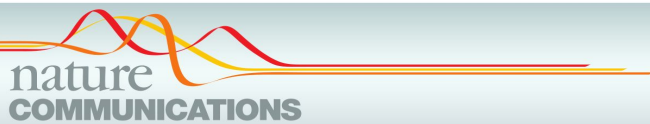
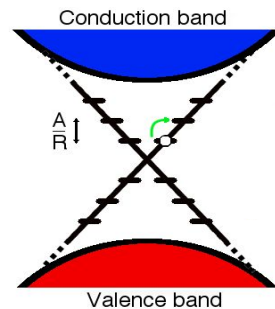


- Strong THz EM enhancements
- Protected particle plasmons
- Nano-sources for non-local and non-dipolar transitions
- Topological Quantum dot

LIGHT + TOPOLOGICAL INSULATOR NANOPARTICLE



Boundary conditions on E-field



ARTICLE

Received 10 Feb 2016 | Accepted 27 Jun 2016 | Published 5 Aug 2016

DOI: 10.1038/ncomms12375

OPEN

Single-electron induced surface plasmons on a topological nanoparticle

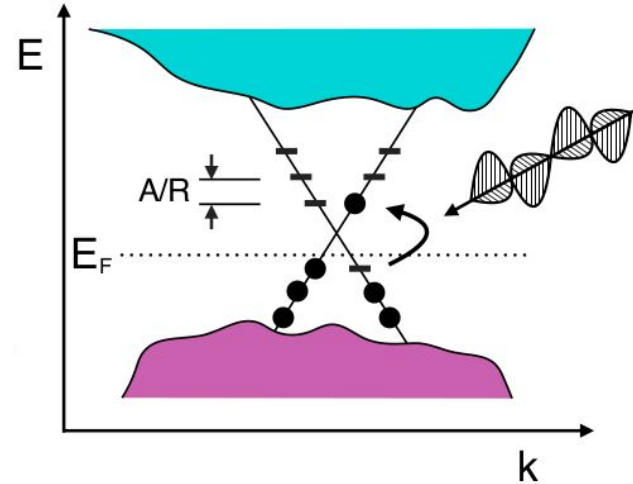
G. Siroki¹, D.K.K. Lee¹, P.D. Haynes^{1,2} & V. Giannini¹

LIGHT + TOPOLOGICAL INSULATOR NANOPARTICLE

...the perturbation (light) induces a time dependent surface charge density!

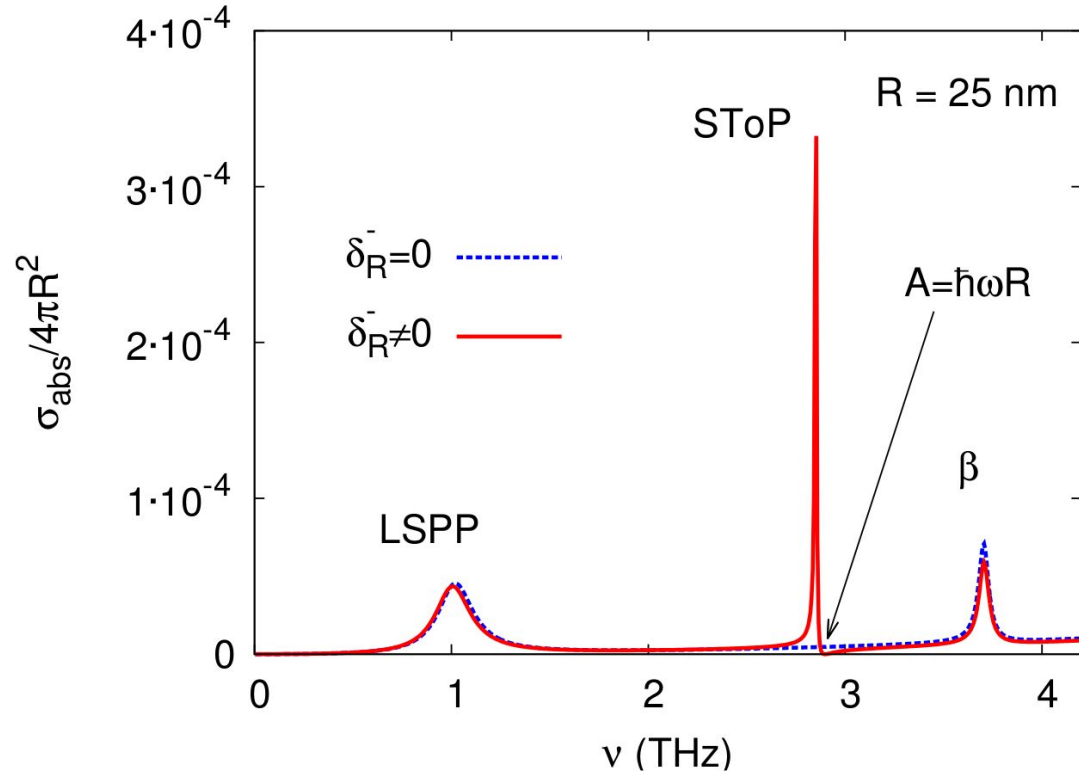
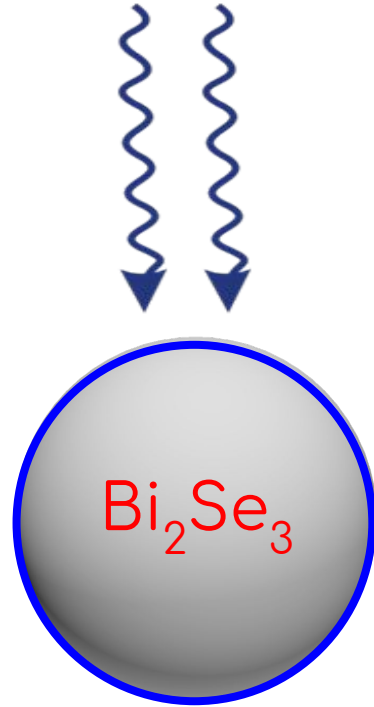
$$\sigma_{abs} = 4\pi R^3 \frac{2\pi}{\lambda} \text{Im} \left(\frac{\epsilon_{in} + \delta_R - 1}{\epsilon_{in} + \delta_R + 2} \right)$$

$$\delta_R = \frac{e^2}{6\pi\epsilon_0} \left(\frac{1}{A - \hbar\omega R} + \frac{1}{A + \hbar\omega R} \right)$$

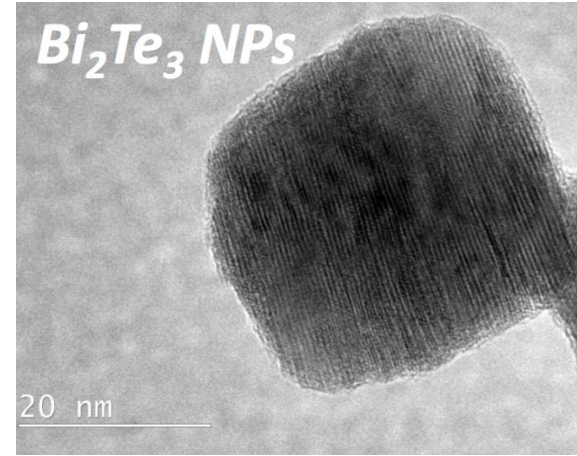
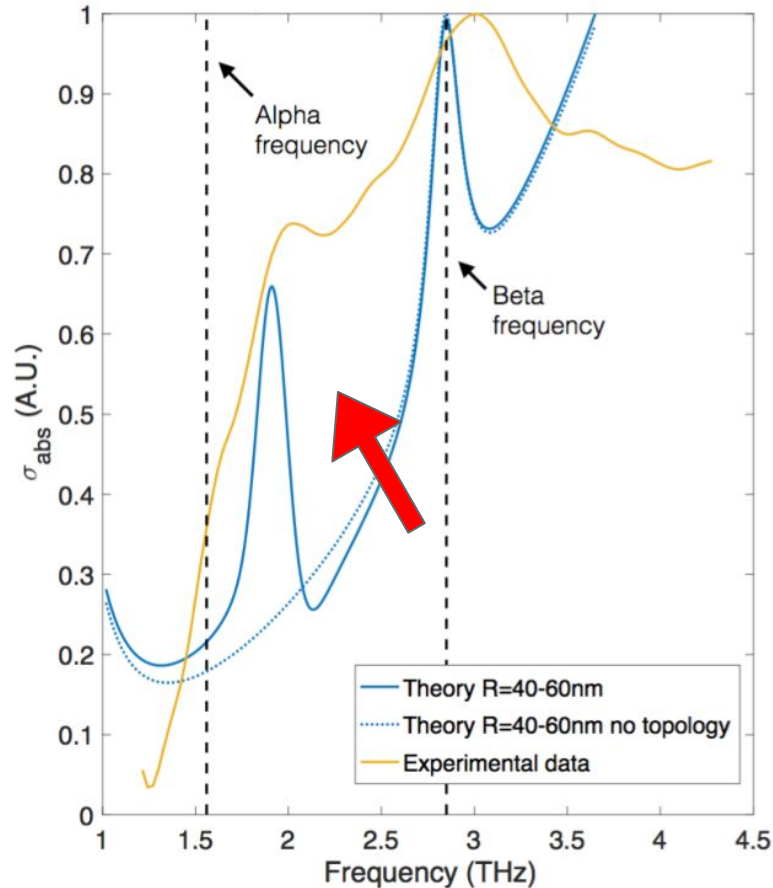


Fermi Energy and Radius dependence

SURFACE TOPOLOGICAL POLARITON



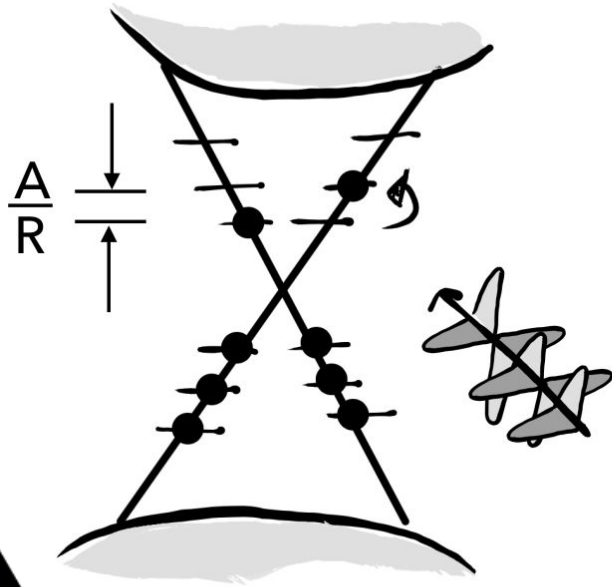
EXPERIMENTAL EVIDENCE OF SToP MODES



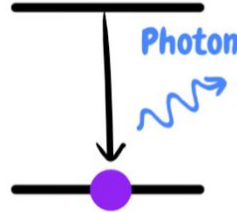
Stefano Lupi,
Sapienza University of Rome
Cecilia Mattevi,
Imperial College London

Under Review

TOPOLOGICAL NANOPARTICLE LESING

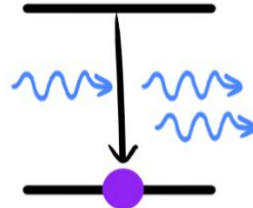


SPONTANEOUS EMISSION



$$\Gamma_{fi}^{spon} = \frac{4\alpha\omega_{fi}^3}{3c^2} |\langle f | \mathbf{x} | i \rangle|^2$$

STIMULATED EMISSION



$$\Gamma_{fi}^{stim} = \frac{4\pi^2\alpha I(\omega_{fi})}{\hbar} |\langle f | \boldsymbol{\varepsilon} \cdot \mathbf{x} | i \rangle|^2$$

RETARDATION INDUCED TRANSITIONS PHASE

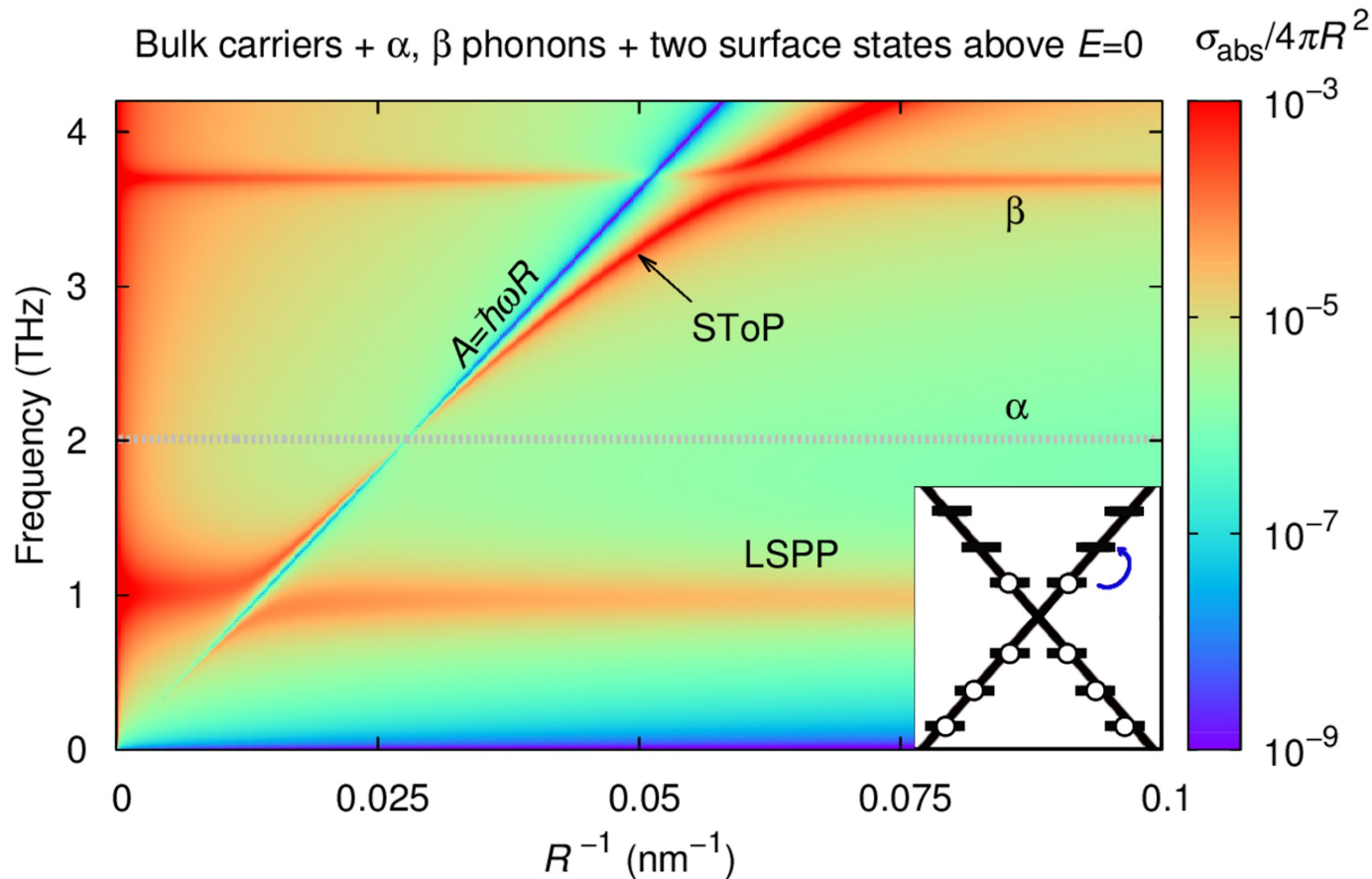
PLASMONIC CHAIN: PROTECTED HOTSPOTS

TOPOLOGICAL QUANTUM DOTS

TOPOLOGICAL PHOTONICS: RICH PHYSICS



TOPOLOGICAL QUANTUM DOTS (SToP MODE)



TOPOLOGICAL NANOPARTICLES

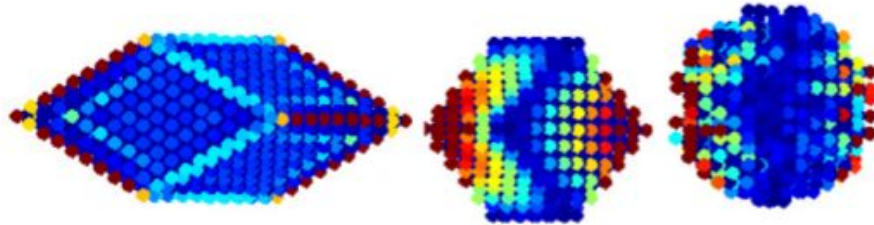
- Topological surface states are a bulk property!

Do we have enough bulk in a nanoparticle?

PHYSICAL REVIEW MATERIALS 1, 024201 (2017)

Protection of surface states in topological nanoparticles

Gleb Siroki,^{1,*} Peter D. Haynes,^{1,2} Derek K. K. Lee,¹ and Vincenzo Giannini^{1,3}



TOPOLOGICAL INSULATOR NANOPARTICLE

Quantized Bands

A is a constant entering surface Dirac equation that determines the energy spacing of surface states

PHYSICAL REVIEW B **86**, 081303(R) (2012)



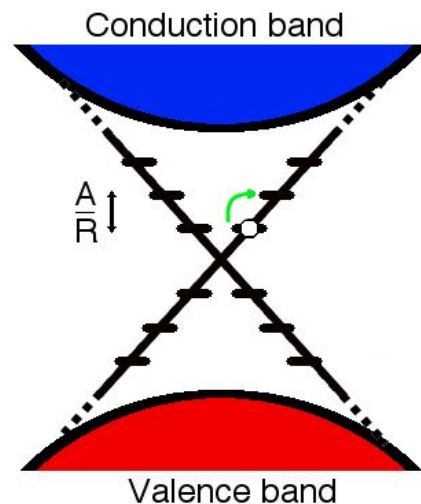
Surface states of topological insulators

Fan Zhang,^{*} C. L. Kane, and E. J. Mele

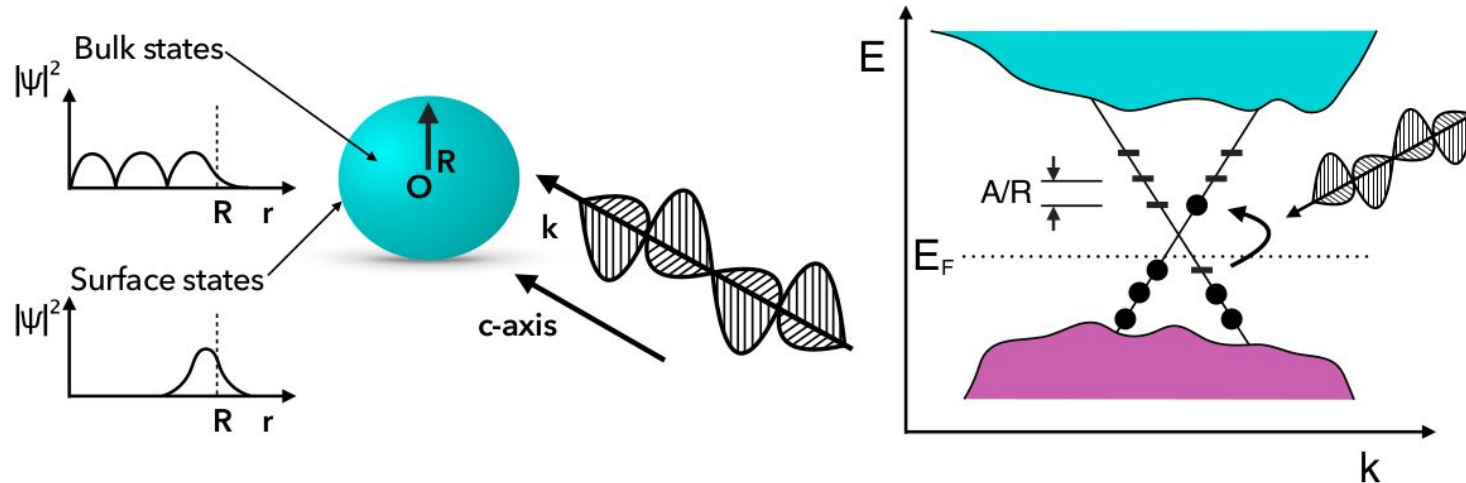
PHYSICAL REVIEW B **86**, 235119 (2012)

Spherical topological insulator

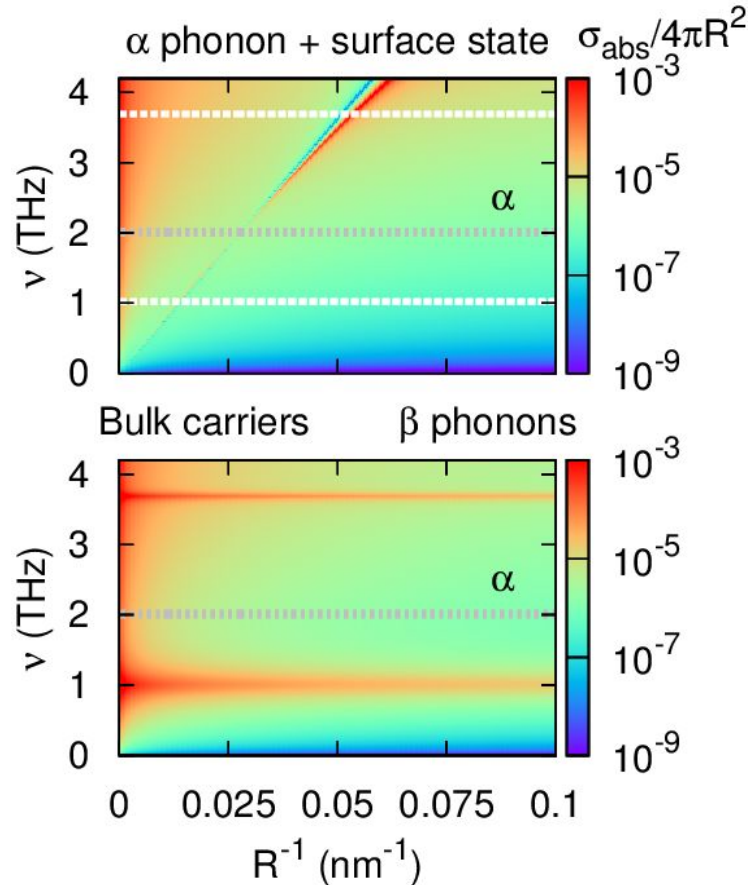
Ken-Ichiro Imura,¹ Yukinori Yoshimura,¹ Yositake Takane,¹ and Takahiro Fukui²



- A simple system (Sphere, Bi_2Se_3)
- A simple perturbation (circularly polarized light)
- Time dependent Perturbation Theory to the Imura simplified four-band Hamiltonian of Bi_2Se_3



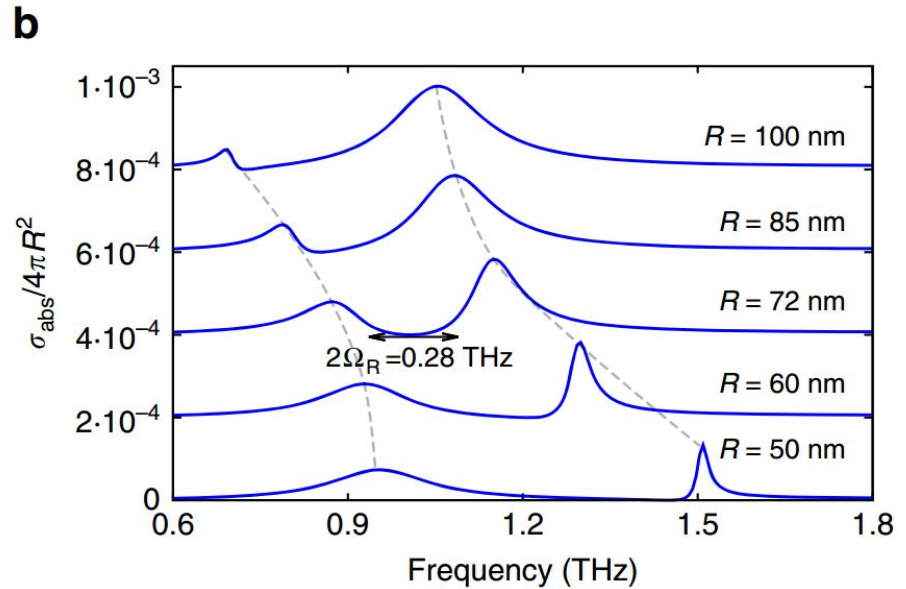
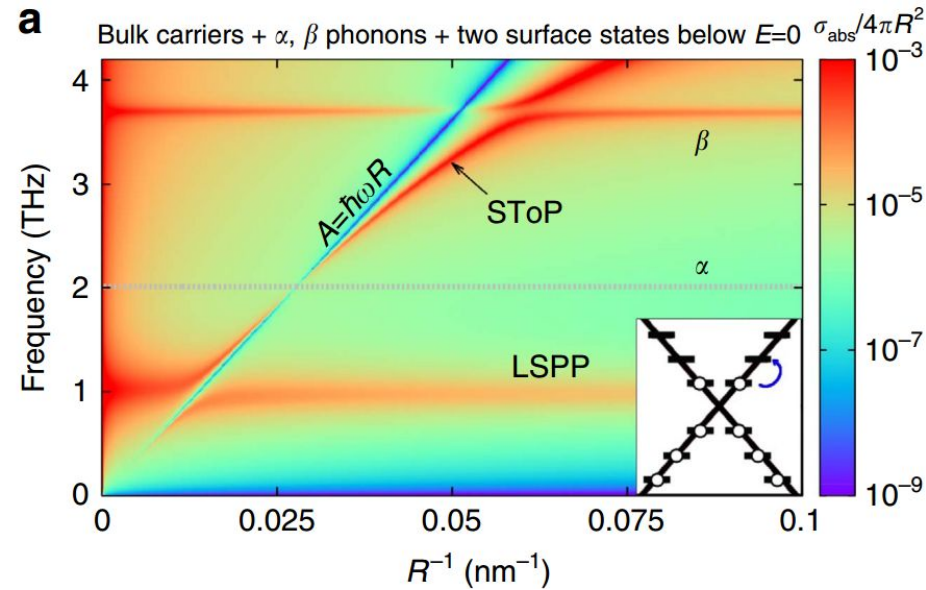
SURFACE TOPOLOGICAL POLARITON (SToP Mode)



SToP mode:

Interaction of α phonon
and surface states

SURFACE TOPOLOGICAL POLARITON (SToP MODE)



- Rabi Splitting ($g > 0.1$)
- Total Screening
- Quantum behaviour at room temperature... ???