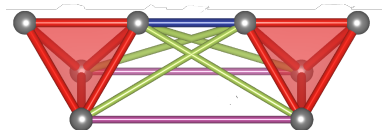


Chromium Breathing Pyrochlores

An exhibition of a variety of pyrochlore Hamiltonians

Pratyay Ghosh

Indian Institute of Technology Madras, Chennai, India



February 25, 2019

Collaborations

- ▶ Yasir Iqbal
- ▶ Tobias Müller
- ▶ Ronny Thomale
- ▶ Johannes Reuther
- ▶ Michel J. P. Gingras
- ▶ Harald O. Jeschke

Collaborations

- ▶ Yasir Iqbal
- ▶ Tobias Müller
- ▶ Ronny Thomale
- ▶ Johannes Reuther
- ▶ Michel J. P. Gingras
- ▶ Harald O. Jeschke

Acknowledgements

- ▶ Zenji Hiroi, Gøran Nilsen, Yoshihiko Okamoto, Owen Benton and Jason Gardner
- ▶ ICTS, Bengaluru, The 2nd Asia Pacific Workshop on Quantum Magnetism.
- ▶ SuperMUC

TABLE OF CONTENTS

INTRODUCTION

PYROCHLORE: CLASSICAL HEISENBERG MODEL

PYROCHLORE: QUANTUM HEISENBERG MODEL

BREATHING PYROCHLORES

METHODOLOGY

PFFRG

RESULTS

Model Hamiltonian

Oxides

Sulfides

Selenide

CONCLUSIONS

INTRODUCTION

Spin systems, Frustration, Exotic quantum disorders,
quantum-entangled **spin liquid ground states**, blah, blah, blah

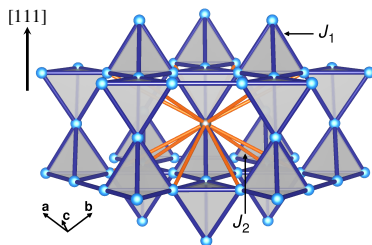
INTRODUCTION

Spin systems, Frustration, Exotic quantum disorders,
quantum-entangled **spin liquid ground states**, blah, blah, blah



PYROCHLORE: CLASSICAL HEISENBERG MODEL

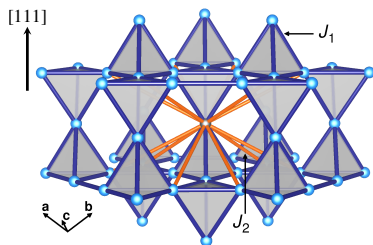
J_1 -only model



PYROCHLORE: CLASSICAL HEISENBERG MODEL

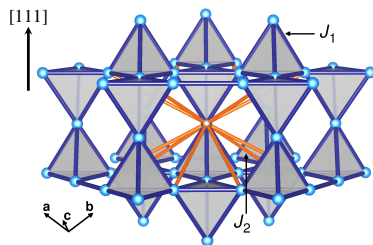
J_1 -only model

- extensive classical ground-state degeneracy



PYROCHLORE: CLASSICAL HEISENBERG MODEL

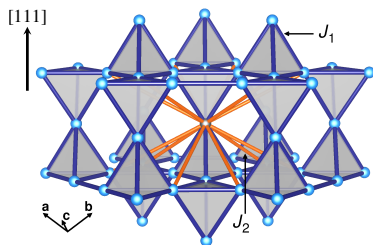
J_1 -only model



- ▶ extensive classical ground-state degeneracy
- ▶ **no** magnetic long-range **order** down to $T = 0$

PYROCHLORE: CLASSICAL HEISENBERG MODEL

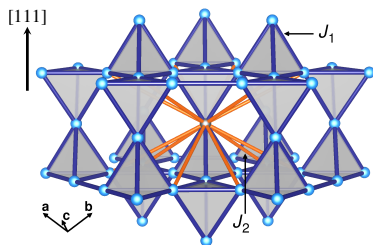
J_1 -only model



- ▶ extensive classical ground-state degeneracy
- ▶ **no** magnetic long-range **order** down to $T = 0$
- ▶ cooperative paramagnet $\Leftrightarrow$ “spin-ice”

PYROCHLORE: CLASSICAL HEISENBERG MODEL

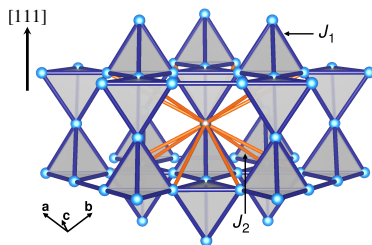
J_1 -only model



- ▶ extensive classical ground-state degeneracy
- ▶ **no** magnetic long-range **order** down to $T = 0$
- ▶ cooperative paramagnet $\Leftrightarrow$ “spin-ice”
 (“ice rule”: $\sum_{i=1}^4 \vec{S}_i = 0$)

PYROCHLORE: CLASSICAL HEISENBERG MODEL

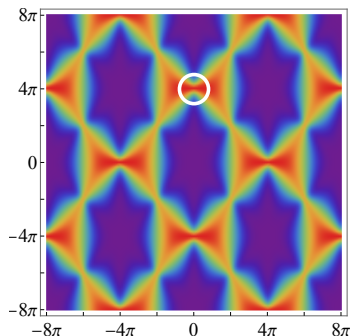
J_1 -only model



- ▶ extensive classical ground-state degeneracy
- ▶ **no** magnetic long-range **order** down to $T = 0$
- ▶ cooperative paramagnet $\Leftrightarrow$ “spin-ice”
 (“ice rule”: $\sum_{i=1}^4 \vec{S}_i = 0$)
- ▶ nonzero entropy

PYROCHLORE: CLASSICAL HEISENBERG MODEL

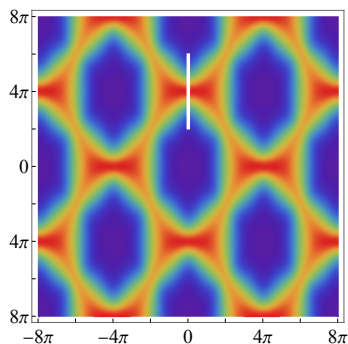
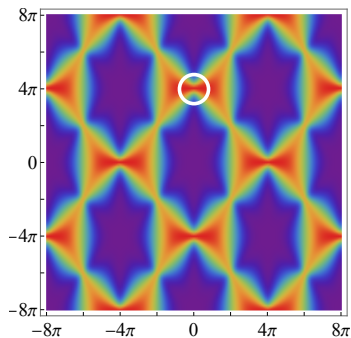
J_1 -only model



- ▶ extensive classical ground-state degeneracy
- ▶ **no** magnetic long-range **order** down to $T = 0$
- ▶ cooperative paramagnet $\Leftrightarrow$ “spin-ice”
 (“ice rule”: $\sum_{i=1}^4 \vec{S}_i = 0$)
- ▶ nonzero entropy

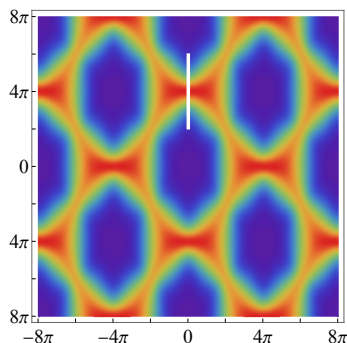
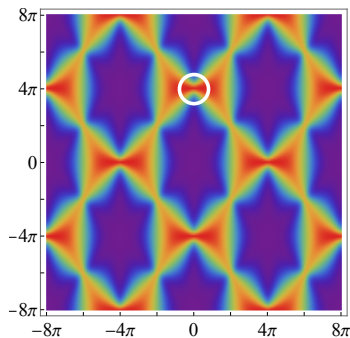
PYROCHLORE: QUANTUM HEISENBERG MODEL

J_1 -only model



PYROCHLORE: QUANTUM HEISENBERG MODEL

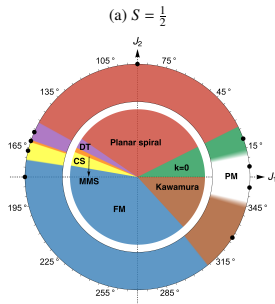
J_1 -only model



Coulomb spin-liquid

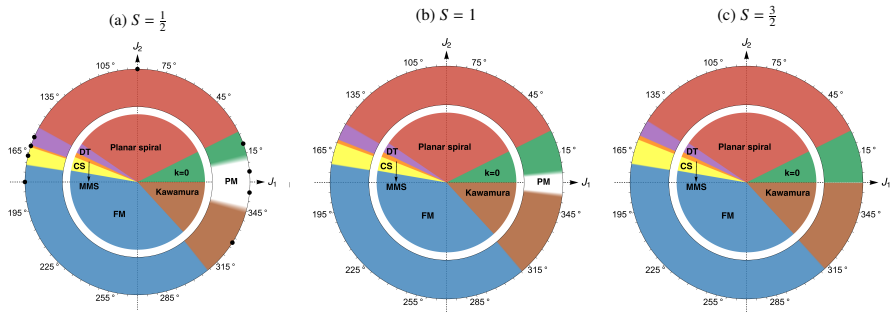
PYROCHLORE: QUANTUM PHASE DIAGRAM

J_1 - J_2 model



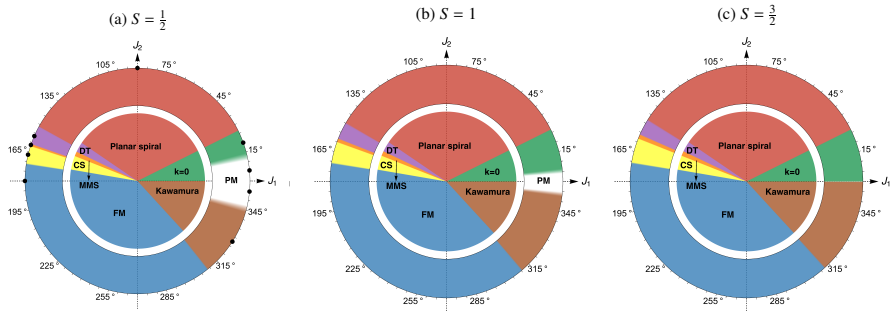
PYROCHLORE: QUANTUM PHASE DIAGRAM

J_1 - J_2 model



PYROCHLORE: QUANTUM PHASE DIAGRAM

J_1 - J_2 model



We study the Cr^{3+} systems which are $S = 3/2$

BREATHING PYROCHLORES

¹Phys. Rev. Lett. 110, 097203 (2013)

²Phys. Rev. B 91, 174435 (2015)

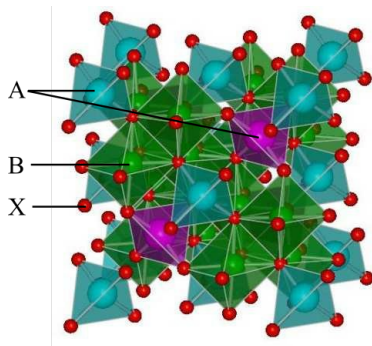
³Phys. Rev. B 97, 134117 (2018)

⁴J. Phys. Soc. Jpn. 87, 034709 (2018)

⁵Phys. Rev. B 77, 035207 (2008)

BREATHING PYROCHLORES

► Pyrochlore (AB_2X_4)



¹Phys. Rev. Lett. 110, 097203 (2013)

²Phys. Rev. B 91, 174435 (2015)

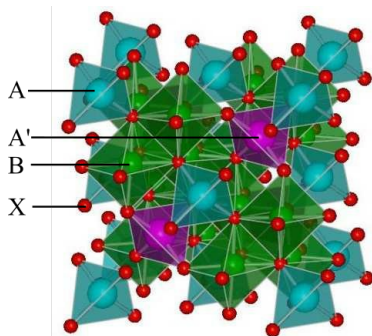
³Phys. Rev. B 97, 134117 (2018)

⁴J. Phys. Soc. Jpn. 87, 034709 (2018)

⁵Phys. Rev. B 77, 035207 (2008)

BREATHING PYROCHLORES

- Pyrochlore (AB_2X_4) $\Rightarrow$ Breathing Pyrochlore ($AA'B_4O_8$)



¹Phys. Rev. Lett. 110, 097203 (2013)

²Phys. Rev. B 91, 174435 (2015)

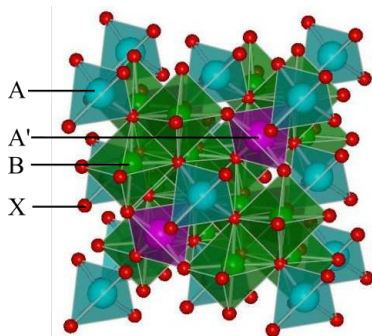
³Phys. Rev. B 97, 134117 (2018)

⁴J. Phys. Soc. Jpn. 87, 034709 (2018)

⁵Phys. Rev. B 77, 035207 (2008)

BREATHING PYROCHLORES

- ▶ Pyrochlore (AB_2X_4) $\Rightarrow$ Breathing Pyrochlore ($AA'B_4O_8$)
- ▶ **Size mismatch** between A and A'
 - ▶ $Fd\bar{3}m \rightarrow F\bar{4}3m$ (Symmetry reduction)



¹Phys. Rev. Lett. 110, 097203 (2013)

²Phys. Rev. B 91, 174435 (2015)

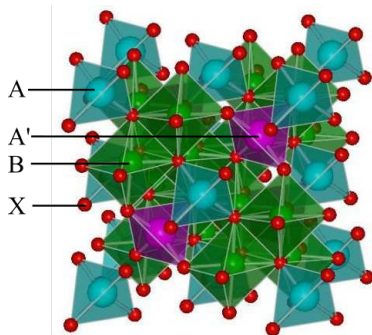
³Phys. Rev. B 97, 134117 (2018)

⁴J. Phys. Soc. Jpn. 87, 034709 (2018)

⁵Phys. Rev. B 77, 035207 (2008)

BREATHING PYROCHLORES

- ▶ Pyrochlore (AB_2X_4) $\Rightarrow$ Breathing Pyrochlore ($AA'B_4O_8$)
- ▶ **Size mismatch** between A and A'
 - ▶ $Fd\bar{3}m \rightarrow F\bar{4}3m$ (Symmetry reduction)
- ▶ **Spin-3/2** Cr^{3+} spinels



¹Phys. Rev. Lett. 110, 097203 (2013)

²Phys. Rev. B 91, 174435 (2015)

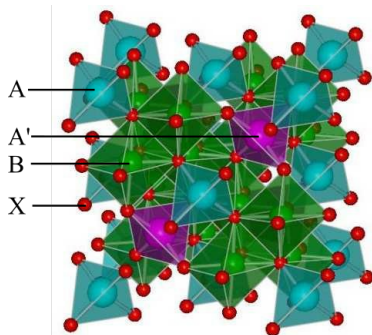
³Phys. Rev. B 97, 134117 (2018)

⁴J. Phys. Soc. Jpn. 87, 034709 (2018)

⁵Phys. Rev. B 77, 035207 (2008)

BREATHING PYROCHLORES

- ▶ Pyrochlore (AB_2X_4) $\Rightarrow$ Breathing Pyrochlore ($AA'B_4O_8$)
- ▶ **Size mismatch** between A and A'
 - ▶ $Fd\bar{3}m \rightarrow F\bar{4}3m$ (Symmetry reduction)
- ▶ **Spin-3/2** Cr^{3+} spinels
 - ▶ Oxides:^{1,2}
 - ▶ $LiInCr_4O_8$
 - ▶ $LiGaCr_4O_8$



¹Phys. Rev. Lett. 110, 097203 (2013)

²Phys. Rev. B 91, 174435 (2015)

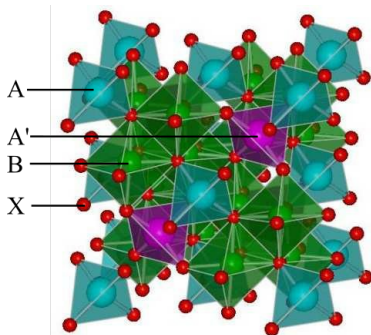
³Phys. Rev. B 97, 134117 (2018)

⁴J. Phys. Soc. Jpn. 87, 034709 (2018)

⁵Phys. Rev. B 77, 035207 (2008)

BREATHING PYROCHLORES

- ▶ Pyrochlore (AB_2X_4) $\Rightarrow$ Breathing Pyrochlore ($AA'B_4O_8$)
- ▶ **Size mismatch** between A and A'
 - ▶ $Fd\bar{3}m \rightarrow F\bar{4}3m$ (Symmetry reduction)
- ▶ **Spin-3/2** Cr^{3+} spinels
 - ▶ Oxides:^{1,2}
 - ▶ $LiInCr_4O_8$
 - ▶ $LiGaCr_4O_8$
 - ▶ Sulphides^{3,4}
 - ▶ $LiInCr_4S_8$
 - ▶ $LiGaCr_4S_8$
 - ▶ $CuInCr_4S_8$



¹Phys. Rev. Lett. 110, 097203 (2013)

²Phys. Rev. B 91, 174435 (2015)

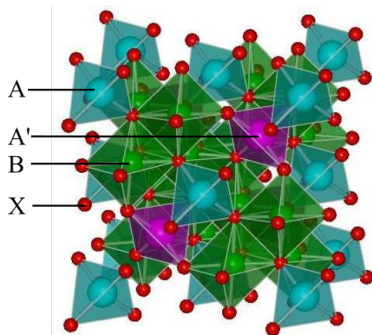
³Phys. Rev. B 97, 134117 (2018)

⁴J. Phys. Soc. Jpn. 87, 034709 (2018)

⁵Phys. Rev. B 77, 035207 (2008)

BREATHING PYROCHLORES

- ▶ Pyrochlore (AB_2X_4) $\Rightarrow$ Breathing Pyrochlore ($AA'B_4O_8$)
- ▶ **Size mismatch** between A and A'
 - ▶ $Fd\bar{3}m \rightarrow F\bar{4}3m$ (Symmetry reduction)
- ▶ **Spin-3/2** Cr^{3+} spinels
 - ▶ Oxides:^{1,2}
 - ▶ $LiInCr_4O_8$
 - ▶ $LiGaCr_4O_8$
 - ▶ Sulphides^{3,4}
 - ▶ $LiInCr_4S_8$
 - ▶ $LiGaCr_4S_8$
 - ▶ $CuInCr_4S_8$
 - ▶ Selenide⁵
 - ▶ $CuInCr_4Se_8$



¹Phys. Rev. Lett. 110, 097203 (2013)

²Phys. Rev. B 91, 174435 (2015)

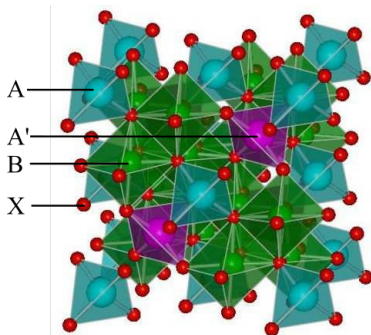
³Phys. Rev. B 97, 134117 (2018)

⁴J. Phys. Soc. Jpn. 87, 034709 (2018)

⁵Phys. Rev. B 77, 035207 (2008)

BREATHING PYROCHLORES

- ▶ Pyrochlore (AB_2X_4) $\Rightarrow$ Breathing Pyrochlore ($AA'B_4O_8$)
- ▶ **Size mismatch** between A and A'
 - ▶ $Fd\bar{3}m \rightarrow F\bar{4}3m$ (Symmetry reduction)
- ▶ **Spin-3/2** Cr^{3+} spinels
 - ▶ Oxides:^{1,2}
 - ▶ $LiInCr_4O_8$
 - ▶ $LiGaCr_4O_8$
 - ▶ Sulphides^{3,4}
 - ▶ $LiInCr_4S_8$
 - ▶ $LiGaCr_4S_8$
 - ▶ $CuInCr_4S_8$
 - ▶ Selenide⁵
 - ▶ $CuInCr_4Se_8$



¹Phys. Rev. Lett. 110, 097203 (2013)

²Phys. Rev. B 91, 174435 (2015)

³Phys. Rev. B 97, 134117 (2018)

⁴J. Phys. Soc. Jpn. 87, 034709 (2018)

⁵Phys. Rev. B 77, 035207 (2008)

TABLE OF CONTENTS

INTRODUCTION

PYROCHLORE: CLASSICAL HEISENBERG MODEL

PYROCHLORE: QUANTUM HEISENBERG MODEL

BREATHING PYROCHLORES

METHODOLOGY

PFFRG

RESULTS

Model Hamiltonian

Oxides

Sulfides

Selenide

CONCLUSIONS

METHODOLOGY

METHODOLOGY

- ▶ Energy mapping method $\Rightarrow$ model Hamiltonian

METHODOLOGY

- ▶ Energy mapping method $\Rightarrow$ model Hamiltonian
- ▶ Iterative minimization method $\Rightarrow$ classical ground state

METHODOLOGY

- ▶ Energy mapping method $\Rightarrow$ model Hamiltonian
- ▶ Iterative minimization method $\Rightarrow$ classical ground state
- ▶ Pseudofermion functional renormalization group method
 $\Rightarrow$ quantum ground state

PFFRG

Phys. Rev. B 83, 024402 (2011)

Phys. Rev. B 96, 045144 (2017)

PFFRG

Phys. Rev. B 83, 024402 (2011)

Phys. Rev. B 96, 045144 (2017)

Fermionic Hamiltonian:

$$H = \sum_{ij} J_{ij} \vec{S}_i \cdot \vec{S}_j$$

PFFRG

Phys. Rev. B 83, 024402 (2011)

Phys. Rev. B 96, 045144 (2017)

Fermionic Hamiltonian:

$$H = \sum_{ij} J_{ij} \vec{S}_i \cdot \vec{S}_j \rightarrow \frac{1}{4} \sum_{ij} J_{ij} \sum_{\mu} (f_i^{\dagger} \sigma^{\mu} f_i) (f_j^{\dagger} \sigma^{\mu} f_j)$$

PFFRG

Phys. Rev. B 83, 024402 (2011)

Phys. Rev. B 96, 045144 (2017)

Fermionic Hamiltonian:

$$H = \sum_{ij} J_{ij} \vec{S}_i \cdot \vec{S}_j \rightarrow \frac{1}{4} \sum_{ij} J_{ij} \sum_{\mu} (f_i^{\dagger} \sigma^{\mu} f_i) (f_j^{\dagger} \sigma^{\mu} f_j)$$

Diagrammatics in the fermion:

PFFRG

Phys. Rev. B 83, 024402 (2011)

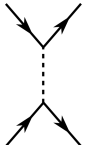
Phys. Rev. B 96, 045144 (2017)

Fermionic Hamiltonian:

$$H = \sum_{ij} J_{ij} \vec{S}_i \cdot \vec{S}_j \rightarrow \frac{1}{4} \sum_{ij} J_{ij} \sum_{\mu} (f_i^{\dagger} \sigma^{\mu} f_i) (f_j^{\dagger} \sigma^{\mu} f_j)$$

Diagrammatics in the fermion:

propagator: $G_0(i\omega) = \frac{1}{i\omega} =$ 

interaction vertex: $\Gamma_0 =$  $\sim J$

PFFRG

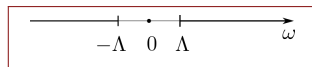
Functional Renormalization Group (FRG)

PFFRG

Functional Renormalization Group (FRG)

Infrared frequency cutoff

$$G_0(i\omega) = \frac{1}{i\omega} \rightarrow G_0^\Lambda(i\omega) = \frac{\Theta(|\omega| - \Lambda)}{i\omega}$$

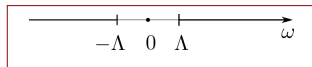


PFFRG

Functional Renormalization Group (FRG)

Infrared frequency cutoff

$$G_0(i\omega) = \frac{1}{i\omega} \rightarrow G_0^\Lambda(i\omega) = \frac{\Theta(|\omega| - \Lambda)}{i\omega}$$



Vertex functions become **Λ -dependent**

$$\Sigma = \text{[Diagram: a circle with a horizontal line through it and arrows at both ends]} \rightarrow \Sigma^\Lambda$$

$$\Gamma = \text{[Diagram: a square with rounded corners and arrows on all four sides]} \rightarrow \Gamma^\Lambda$$

PFFRG

Flow equations for self-energy and 2-particle vertex functions:

$$\frac{d}{d\Lambda} \text{ (self-energy bubble) } = - \text{ (diagram 1) } + \text{ (diagram 2) }$$

$$\frac{d}{d\Lambda} \text{ (2-particle vertex) } = \underbrace{\text{ (diagram 1) } + \text{ (diagram 2) }}_{\langle f_{i\uparrow}^\dagger f_{j\downarrow}^\dagger \rangle} + \underbrace{\text{ (diagram 3) } + \text{ (diagram 4) } + \text{ (diagram 5) }}_{\text{vertex corrections}}$$

$\langle f_{i\uparrow}^\dagger f_{j\downarrow}^\dagger \rangle$ $\langle f_{i\alpha}^\dagger f_{j\alpha} \rangle$ $\langle S_i^\mu \rangle = \frac{1}{2} \langle f_i^\dagger \sigma^\mu f_i \rangle$

PFFRG

Flow equations for self-energy and 2-particle vertex functions:

$$\frac{d}{d\Lambda} \text{ (self-energy bubble) } = - \text{ (self-energy diagram 1) } + \text{ (self-energy diagram 2) }$$

$$\frac{d}{d\Lambda} \text{ (2-particle vertex) } = \underbrace{\text{ (diagram 1) } + \text{ (diagram 2) }}_{\langle f_{i\uparrow}^\dagger f_{j\downarrow}^\dagger \rangle} + \underbrace{\text{ (diagram 3) } - \text{ (diagram 4) } + \text{ (diagram 5) } + \text{ (diagram 6) }}_{\text{vertex corrections}}$$

$\langle f_{i\uparrow}^\dagger f_{j\downarrow}^\dagger \rangle$ $\langle f_{i\alpha}^\dagger f_{j\alpha} \rangle$ $\langle S_i^\mu \rangle = \frac{1}{2} \langle f_i^\dagger \sigma^\mu f_i \rangle$

FRG flow starts with  $\xrightarrow{\Lambda \rightarrow \infty}$  $\sim J$ and ends at $\Lambda = 0$.

PFFRG

Flow equations for self-energy and 2-particle vertex functions:

$$\frac{d}{d\Lambda} \text{ (self-energy bubble) } = - \text{ (self-energy diagram 1) } + \text{ (self-energy diagram 2) }$$

$$\frac{d}{d\Lambda} \text{ (2-particle vertex) } = \underbrace{\text{ (diagram 1) } + \text{ (diagram 2) }}_{\langle f_{i\uparrow}^\dagger f_{j\downarrow}^\dagger \rangle} + \underbrace{\text{ (diagram 3) } - \text{ (diagram 4) } + \text{ (diagram 5) } + \text{ (diagram 6) }}_{\text{vertex corrections}}$$

$\langle f_{i\uparrow}^\dagger f_{j\downarrow}^\dagger \rangle$ $\langle f_{i\alpha}^\dagger f_{j\alpha} \rangle$ $\langle S_i^\mu \rangle = \frac{1}{2} \langle f_i^\dagger \sigma^\mu f_i \rangle$

FRG flow starts with  $\xrightarrow{\Lambda \rightarrow \infty}$  $\sim J$ and ends at $\Lambda = 0$.

Magnetic response (static susceptibility):

$$\text{ (Feynman diagram for magnetic susceptibility) } = \chi^\Lambda(\mathbf{k})$$

TABLE OF CONTENTS

INTRODUCTION

PYROCHLORE: CLASSICAL HEISENBERG MODEL

PYROCHLORE: QUANTUM HEISENBERG MODEL

BREATHING PYROCHLORES

METHODOLOGY

PFFRG

RESULTS

Model Hamiltonian

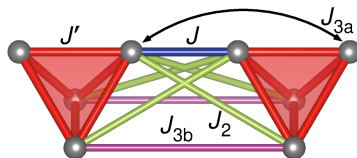
Oxides

Sulfides

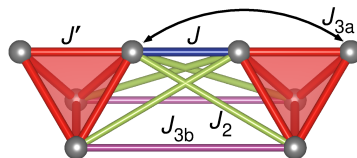
Selenide

CONCLUSIONS

MODEL HAMILTONIAN



MODEL HAMILTONIAN



Material	J (K)	J' (K)	J_2 (K)	J_{3a} (K)	J_{3b} (K)
LiInCr ₄ O ₈	59.8(2)	22.0(2)	0.3(1)	1.9(1)	0.9(1)
CuInCr ₄ S ₈	14.7(1)	-26.0(1)	1.1(1)	6.4(1)	4.5(1)
CuInCr ₄ Se ₈	-25.4(2)	-31.0(1)	0.3(1)	4.8(1)	3.9(1)

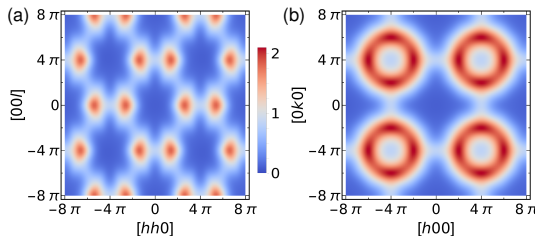
OXIDES



⁶Phys. Rev. B. 81, 224413 (2010)

⁷Phys. Rev. B, 78, 144418 (2008)

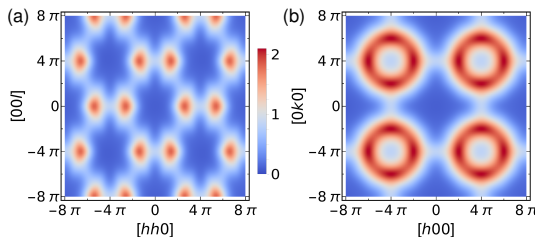
OXIDES



⁶Phys. Rev. B. 81, 224413 (2010)

⁷Phys. Rev. B, 78, 144418 (2008)

OXIDES

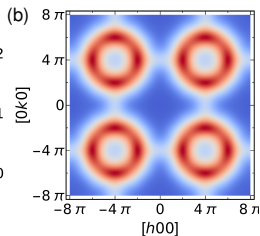
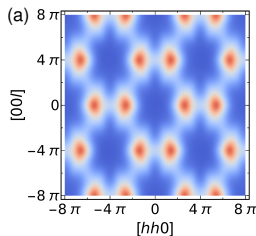


- ▶ $J'/J = 0.37$
- ▶ $J_2/J = 0.004$
- ▶ $J_{3a}/J = 0.03$
- ▶ $J_{3b}/J = 0.015$

⁶Phys. Rev. B. 81, 224413 (2010)

⁷Phys. Rev. B, 78, 144418 (2008)

OXIDES



- ▶ $J'/J = 0.37$
- ▶ $J_2/J = 0.004$
- ▶ $J_{3a}/J = 0.03$
- ▶ $J_{3b}/J = 0.015$

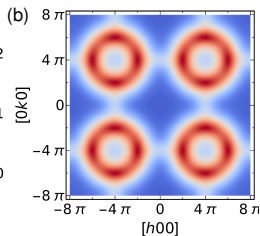
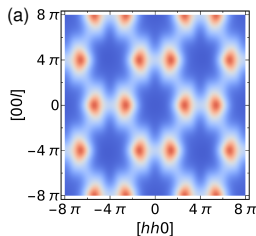
Ordering pitch vector

$$\mathbf{q} = \frac{2\pi}{a}(2, 1, 0) \Rightarrow$$

⁶Phys. Rev. B. 81, 224413 (2010)

⁷Phys. Rev. B, 78, 144418 (2008)

OXIDES



- ▶ $J'/J = 0.37$
- ▶ $J_2/J = 0.004$
- ▶ $J_{3a}/J = 0.03$
- ▶ $J_{3b}/J = 0.015$

Ordering pitch vector

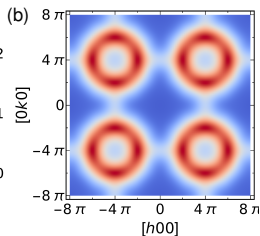
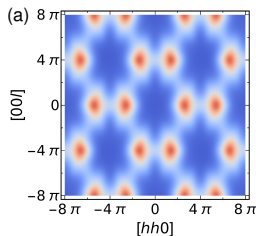
$$\mathbf{q} = \frac{2\pi}{a}(2, 1, 0) \Rightarrow$$

- ▶ FM J_2 ⁶
- ▶ AFM J_3

⁶Phys. Rev. B. 81, 224413 (2010)

⁷Phys. Rev. B, 78, 144418 (2008)

OXIDES



- ▶ $J'/J = 0.37$
- ▶ $J_2/J = 0.004$
- ▶ $J_{3a}/J = 0.03$
- ▶ $J_{3b}/J = 0.015$

Ordering pitch vector

$$\mathbf{q} = \frac{2\pi}{a}(2, 1, 0) \Rightarrow$$

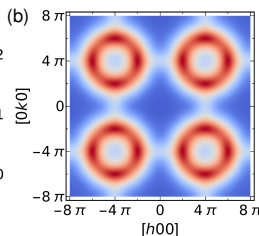
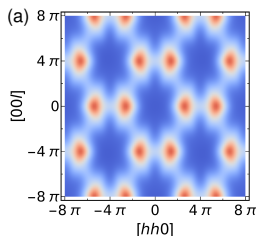
- ▶ FM J_2 ⁶
- ▶ AFM J_3

For strong AFM NN interactions, J_2 in an ideal pyrochlore lattice is **equivalent** to a J_{3a} with **opposite sign**⁷.

⁶Phys. Rev. B. 81, 224413 (2010)

⁷Phys. Rev. B, 78, 144418 (2008)

OXIDES



- ▶ $J'/J = 0.37$
- ▶ $J_2/J = 0.004$
- ▶ $J_{3a}/J = 0.03$
- ▶ $J_{3b}/J = 0.015$

Ordering pitch vector

$$\mathbf{q} = \frac{2\pi}{a}(2, 1, 0) \Rightarrow$$

- ▶ FM J_2 ⁶
- ▶ AFM J_3

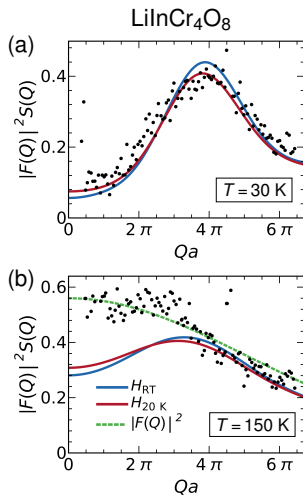
For strong AFM NN interactions, J_2 in an ideal pyrochlore lattice is **equivalent** to a J_{3a} with **opposite sign**⁷.

$$J_{3a}/J \rightarrow (J_{3a} - J_2)/J = 0.026$$

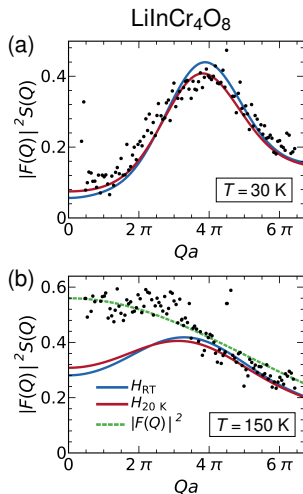
⁶Phys. Rev. B. 81, 224413 (2010)

⁷Phys. Rev. B, 78, 144418 (2008)

OXIDES



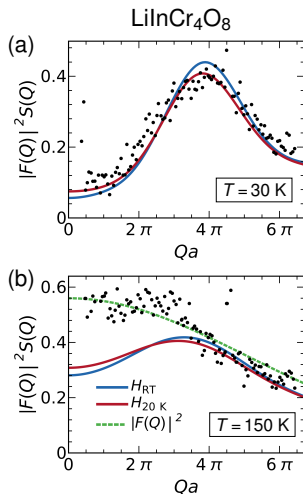
OXIDES



Experimental data from J. Phys. Soc. Jpn. 84, 043707 (2015)

- **Temperature** dependent Hamiltonian

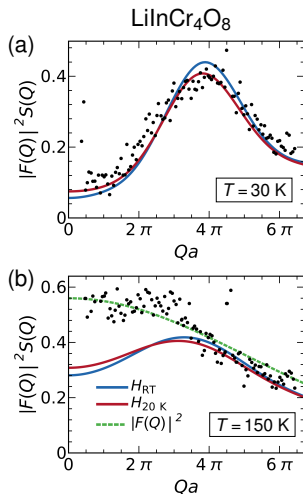
OXIDES



Experimental data from J. Phys. Soc. Jpn. 84, 043707 (2015)

- ▶ **Temperature** dependent Hamiltonian
- ▶ **absorption cross section** in barns of In: [193.8](#)
- ▶ absorption cross section in barns of Ga: [2.75](#)

OXIDES



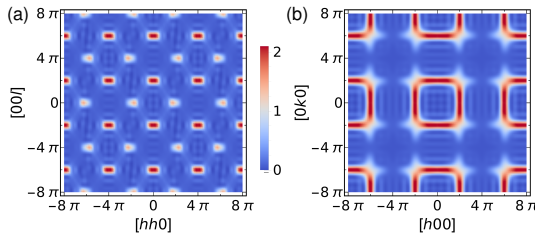
Experimental data from J. Phys. Soc. Jpn. 84, 043707 (2015)

- ▶ **Temperature** dependent Hamiltonian
- ▶ **absorption cross section** in barns of In: **193.8**
- ▶ absorption cross section in barns of Ga: **2.75**
- ▶ Experiments on **LiGaCr₄O₈**

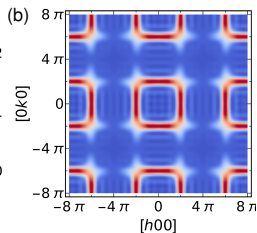
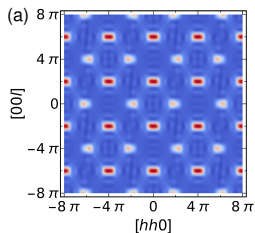
SULFIDES



SULFIDES

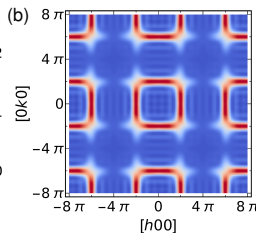
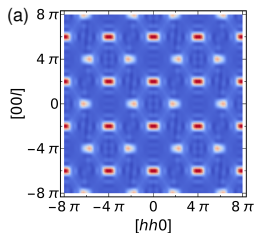


SULFIDES



- ▶ $J'/J = -1.49$
- ▶ $J_2/J = 0.07$
- ▶ $J_{3a}/J = 0.39$
- ▶ $J_{3b}/J = 0.27$

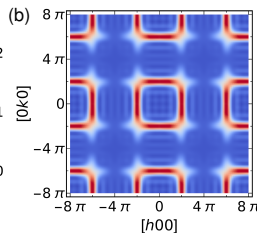
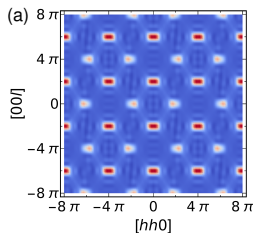
SULFIDES



- ▶ $J'/J = -1.49$
- ▶ $J_2/J = 0.07$
- ▶ $J_{3a}/J = 0.39$
- ▶ $J_{3b}/J = 0.27$

- ▶ Ordering pitch vector: $\frac{2\pi}{a}(1, 0, 0)$

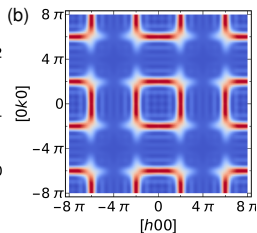
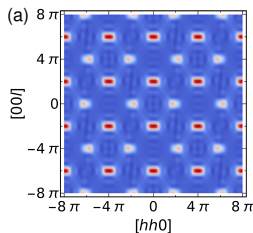
SULFIDES



- ▶ $J'/J = -1.49$
- ▶ $J_2/J = 0.07$
- ▶ $J_{3a}/J = 0.39$
- ▶ $J_{3b}/J = 0.27$

- ▶ Ordering pitch vector: $\frac{2\pi}{a}(1, 0, 0)$
- ▶ Pattern of almost degenerate line $\Leftarrow$ AFM NN FCC $\Rightarrow$ “spiral spin liquid”

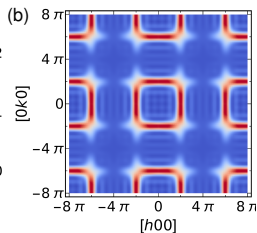
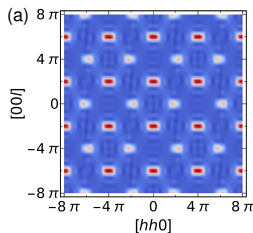
SULFIDES



- ▶ $J'/J = -1.49$
- ▶ $J_2/J = 0.07$
- ▶ $J_{3a}/J = 0.39$
- ▶ $J_{3b}/J = 0.27$

- ▶ Ordering pitch vector: $\frac{2\pi}{a}(1, 0, 0)$
- ▶ Pattern of almost degenerate line $\Leftarrow$ AFM NN FCC $\Rightarrow$ “spiral spin liquid”
- ▶ Strong FM $J' \Rightarrow S \approx 6$ FCC

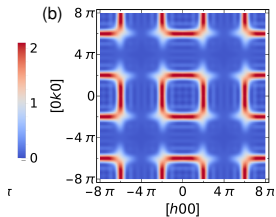
SULFIDES



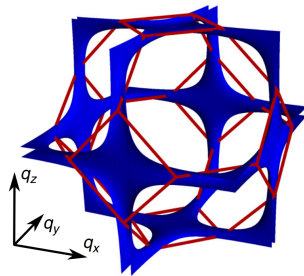
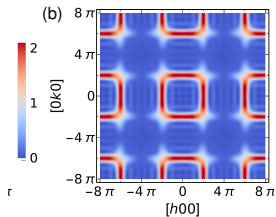
- ▶ $J'/J = -1.49$
- ▶ $J_2/J = 0.07$
- ▶ $J_{3a}/J = 0.39$
- ▶ $J_{3b}/J = 0.27$

- ▶ Ordering pitch vector: $\frac{2\pi}{a}(1, 0, 0)$
- ▶ Pattern of almost **degenerate line** $\Leftarrow$ **AFM NN FCC** $\Rightarrow$ **“spiral spin liquid”**
- ▶ Strong FM $J' \Rightarrow S \approx 6$ FCC
 - ▶ $J_1^{\text{fcc}} = (J + 4J_2 + 2J_{3a} + 2J_{3b})/16$

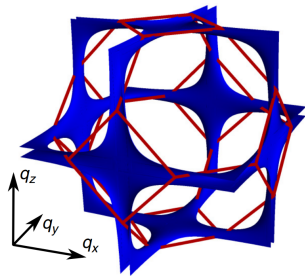
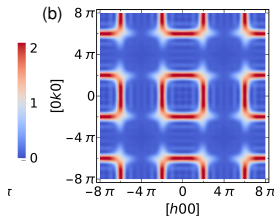
SULFIDES



SULFIDES

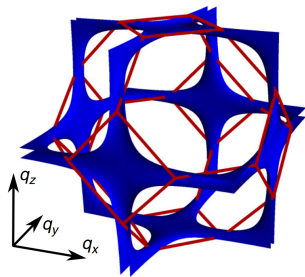
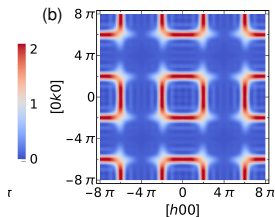


SULFIDES



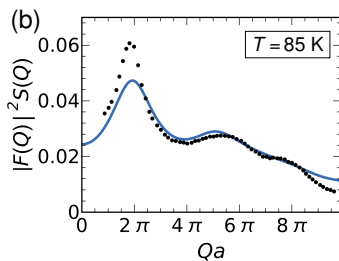
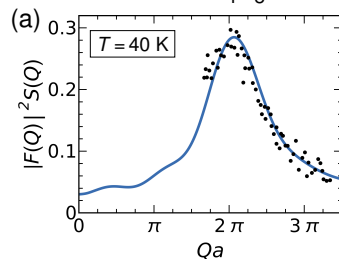
- Intersection of $\mathbf{q} = \frac{2\pi}{a}(1, \delta, 0)$ and $\mathbf{q} = \frac{2\pi}{a}(1, 0, \delta)$

SULFIDES

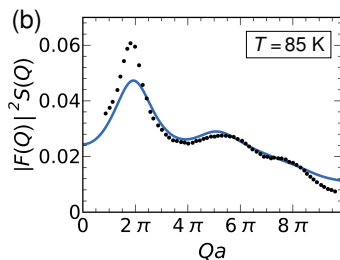
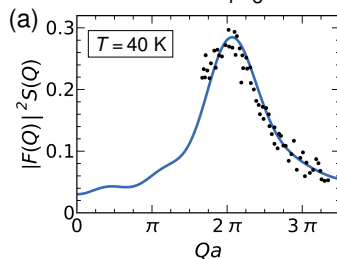


- Intersection of $\mathbf{q} = \frac{2\pi}{a}(1, \delta, 0)$ and $\mathbf{q} = \frac{2\pi}{a}(1, 0, \delta)$
- “Order by disorder” selects $\mathbf{q} = \frac{2\pi}{a}(1, 0, 0)$

SULFIDES

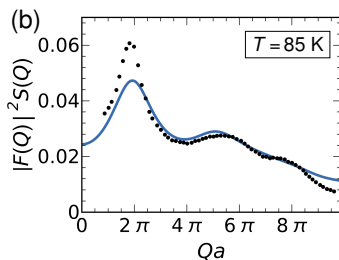
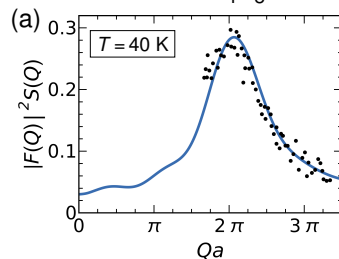


SULFIDES



Experimental data from J. Phys. Colloques 32, C1-324 (1971) and Phys. Lett. 60A, 431 (1977).

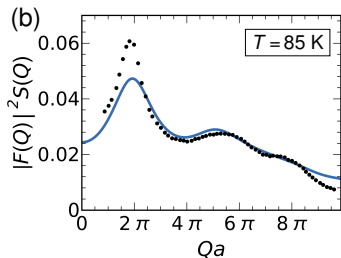
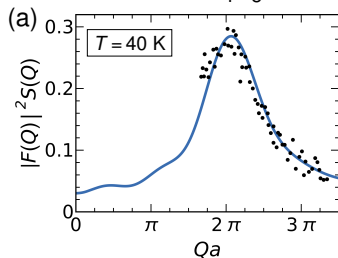
SULFIDES



Experimental data from J. Phys. Colloques 32, C1-324 (1971) and Phys. Lett. 60A, 431 (1977).

- **absorption cross section** in barns of In: 193.8(1.5)
- **absorption cross section** in barns of Ga: 2.75(1.5)

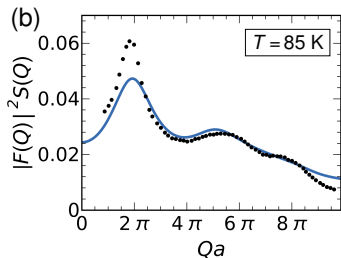
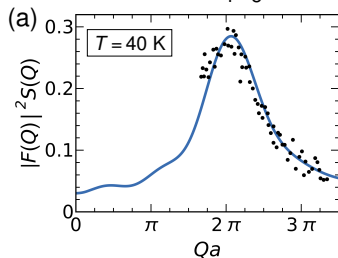
SULFIDES



Experimental data from J. Phys. Colloques 32, C1-324 (1971) and Phys. Lett. 60A, 431 (1977).

- **absorption cross section** in barns of In: 193.8(1.5)
- absorption cross section in barns of Ga: 2.75(1.5)
- Experiments on $\text{LiGaCr}_4\text{S}_8$

SULFIDES



Experimental data from J. Phys. Colloques 32, C1-324 (1971) and Phys. Lett. 60A, 431 (1977).

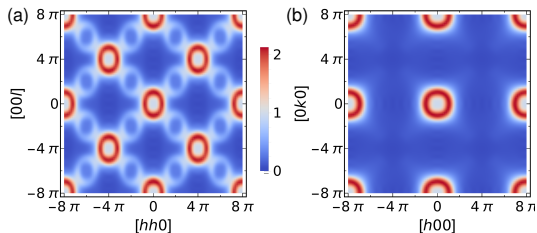
- ▶ **absorption cross section** in barns of In: 193.8(1.5)
- ▶ absorption cross section in barns of Ga: 2.75(1.5)
- ▶ Experiments on $\text{LiGaCr}_4\text{S}_8$
- ▶ Experiments on $\text{LiInCr}_4\text{S}_8$ and $\text{CuInCr}_4\text{S}_8$

SELENIDE

$\text{CuInCr}_4\text{Se}_8$

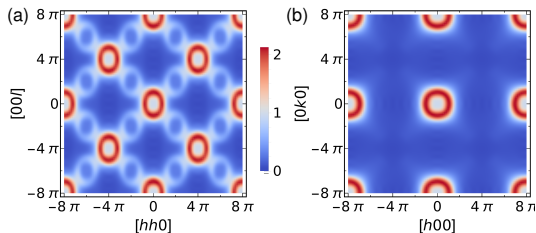
SELENIDE

$\text{CuInCr}_4\text{Se}_8$



SELENIDE

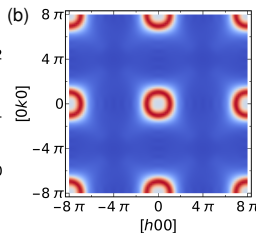
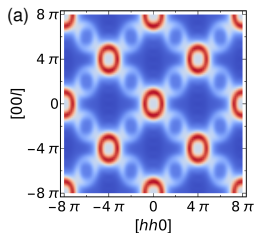
$\text{CuInCr}_4\text{Se}_8$



- ▶ $|J'|/|J| = 1.18$
- ▶ $J_2/|J| = 0.016$
- ▶ $J_{3a}/|J| = 0.2$
- ▶ $J_{3b}/|J| = 0.16$

SELENIDE

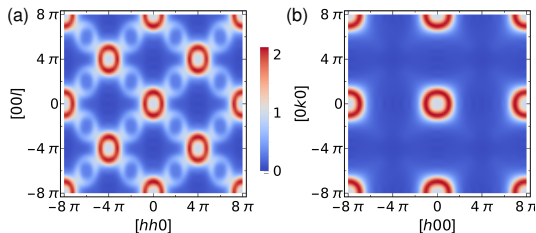
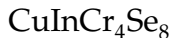
$\text{CuInCr}_4\text{Se}_8$



- ▶ $|J'|/|J| = 1.18$
- ▶ $J_2/|J| = 0.016$
- ▶ $J_{3a}/|J| = 0.2$
- ▶ $J_{3b}/|J| = 0.16$

- ▶ FM J and J'

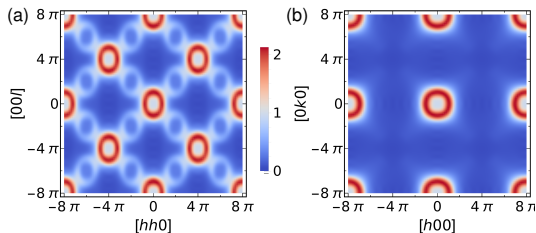
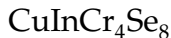
SELENIDE



- ▶ $|J'|/|J| = 1.18$
- ▶ $J_2/|J| = 0.016$
- ▶ $J_{3a}/|J| = 0.2$
- ▶ $J_{3b}/|J| = 0.16$

- ▶ FM J and J'
- ▶ Ordering pitch vector: $\mathbf{q} = (0.521278, 0, 0)$

SELENIDE

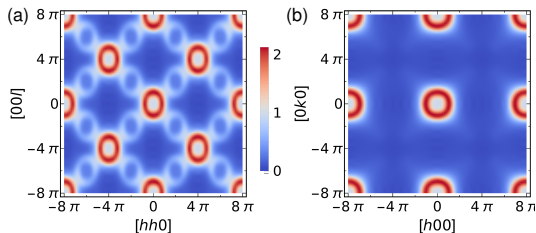
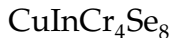


- ▶ $|J'|/|J| = 1.18$
- ▶ $J_2/|J| = 0.016$
- ▶ $J_{3a}/|J| = 0.2$
- ▶ $J_{3b}/|J| = 0.16$

- ▶ FM J and J'
- ▶ Ordering pitch vector: $\mathbf{q} = (0.521278, 0, 0)$
- ▶ Observed for the pyrochlore material ZnCr_2Se_4 ⁸

⁹Phys. Rev. B. 81, 224413 (2010)

SELENIDE



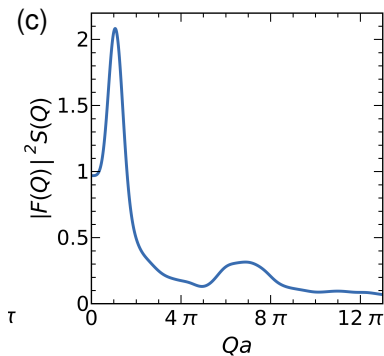
- ▶ $|J'|/|J| = 1.18$
- ▶ $J_2/|J| = 0.016$
- ▶ $J_{3a}/|J| = 0.2$
- ▶ $J_{3b}/|J| = 0.16$

- ▶ FM J and J'
- ▶ Ordering pitch vector: $\mathbf{q} = (0.521278, 0, 0)$
- ▶ Observed for the pyrochlore material ZnCr_2Se_4 ⁸
- ▶ “spiral spin liquid”?

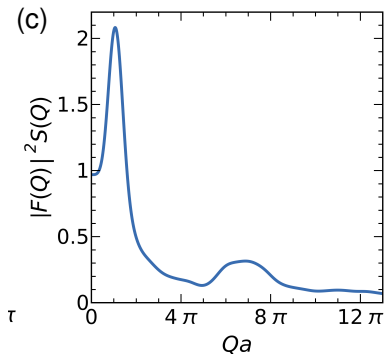
⁹Phys. Rev. B. 81, 224413 (2010)

SELENIDE

$\text{CuInCr}_4\text{Se}_8$

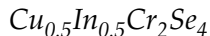


SELENIDE



“Inarticulated” matching with
the unpolarized neutron
scattering data

*MAGNETIC ORDERING IN
THE NORMAL SPINEL*



R. Plumier and M. Sougi

Solid State Communications,
Vol. 69, No. 4, pp.341-345, 1989.

TABLE OF CONTENTS

INTRODUCTION

PYROCHLORE: CLASSICAL HEISENBERG MODEL

PYROCHLORE: QUANTUM HEISENBERG MODEL

BREATHING PYROCHLORES

METHODOLOGY

PFFRG

RESULTS

Model Hamiltonian

Oxides

Sulfides

Selenide

CONCLUSIONS

CONCLUSIONS

CONCLUSIONS

- ▶ We have studied six Cr^{3+} breathing pyrochlore systems.

CONCLUSIONS

- ▶ We have studied six Cr^{3+} breathing pyrochlore systems.
- ▶ The physics of these systems can be grouped in to: Oxides, Sulfides, and Selenide.

CONCLUSIONS

- ▶ We have studied six Cr^{3+} breathing pyrochlore systems.
- ▶ The physics of these systems can be grouped in to: Oxides, Sulfides, and Selenide.
- ▶ We have presented the systems as a display of different types of model pyrochlore Hamiltonians to explain their completely different ground states.

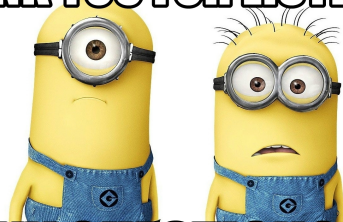
CONCLUSIONS

- ▶ We have studied six Cr^{3+} **breathing pyrochlore** systems.
- ▶ The physics of these systems can be grouped in to: **Oxides**, **Sulfides**, and **Selenide**.
- ▶ We have presented the systems as a display of different types of **model pyrochlore Hamiltonians** to explain their completely **different ground states**.
- ▶ We also present comparisons with **experimental data** and also proposing further studies of these systems.

CONCLUSIONS

- ▶ We have studied six Cr^{3+} **breathing pyrochlore** systems.
- ▶ The physics of these systems can be grouped in to: **Oxides**, **Sulfides**, and **Selenide**.
- ▶ We have presented the systems as a display of different types of **model pyrochlore Hamiltonians** to explain their completely **different ground states**.
- ▶ We also present comparisons with **experimental data** and also proposing further studies of these systems.
- ▶ The **temperature dependence** of these systems?

THANK YOU FOR LISTENING



ANY QUESTION???

memegenerator.net