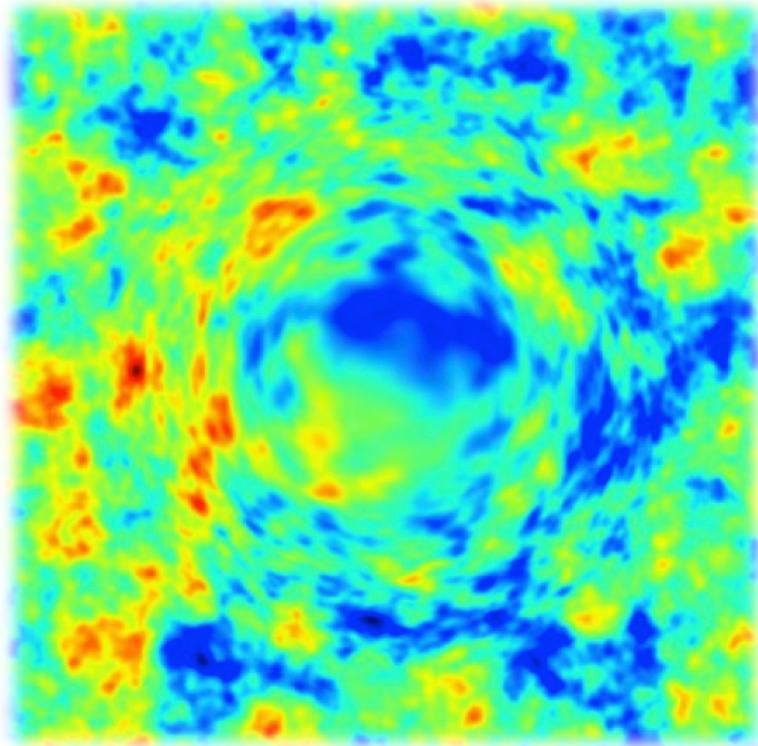


# CMB (De-)Lensing: New Data and New Approaches

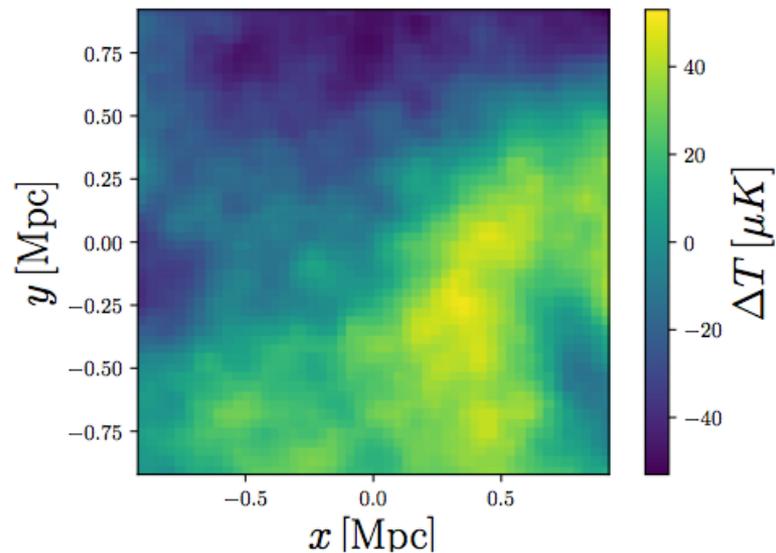


Blake D. Sherwin

Department of Applied Mathematics and Theoretical Physics / Kavli Institute for Cosmology  
University of Cambridge

# Other topics: find me for discussion!

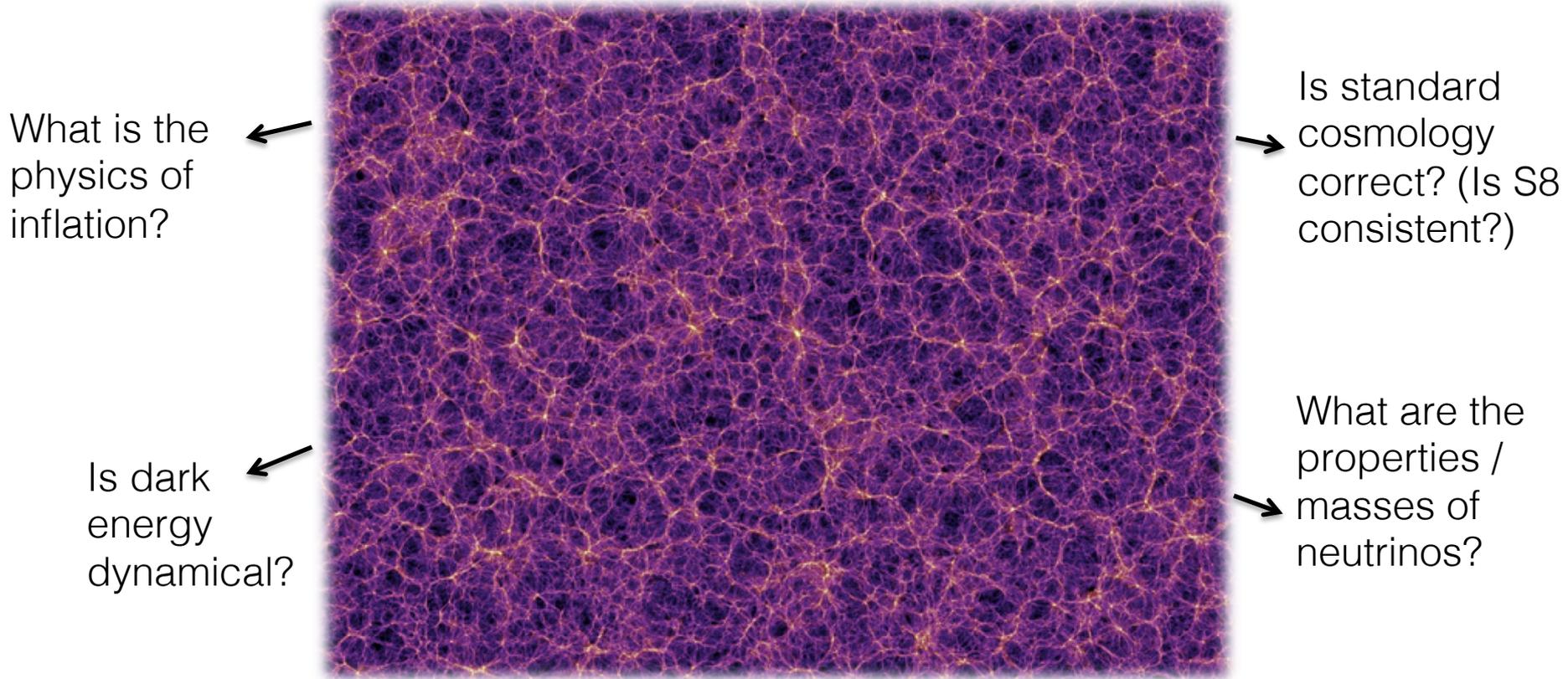
- First measurement (?) of kSZ from cluster rotation:  
Baxter, Sherwin, Raghunathan 2019



- What happens if I assume the wrong cosmology in BAO reconstruction? Sherwin & White 2019
- How well can I reconstruct low-k LSS modes with quadratic estimators? In prep. w. Darwish / Baldauf / Foreman / Meerburg

# Large Scale Dark Matter Structure

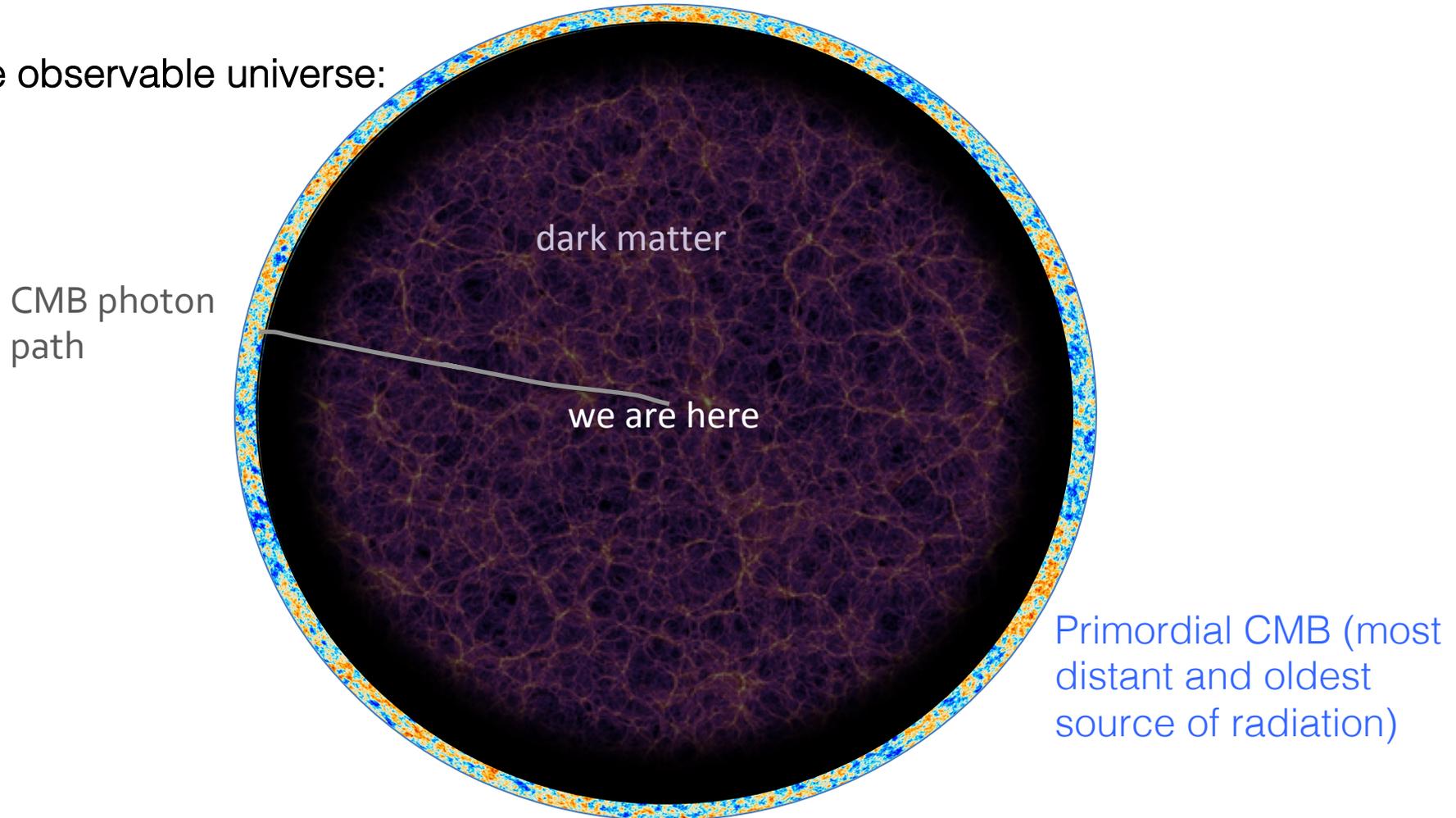
- Want to probe distribution in detail, as contains clean information (no gal. bias) on open questions in cosmology:



- Access directly with gravitational lensing.

# CMB: A Unique Source for Gravitational Lensing

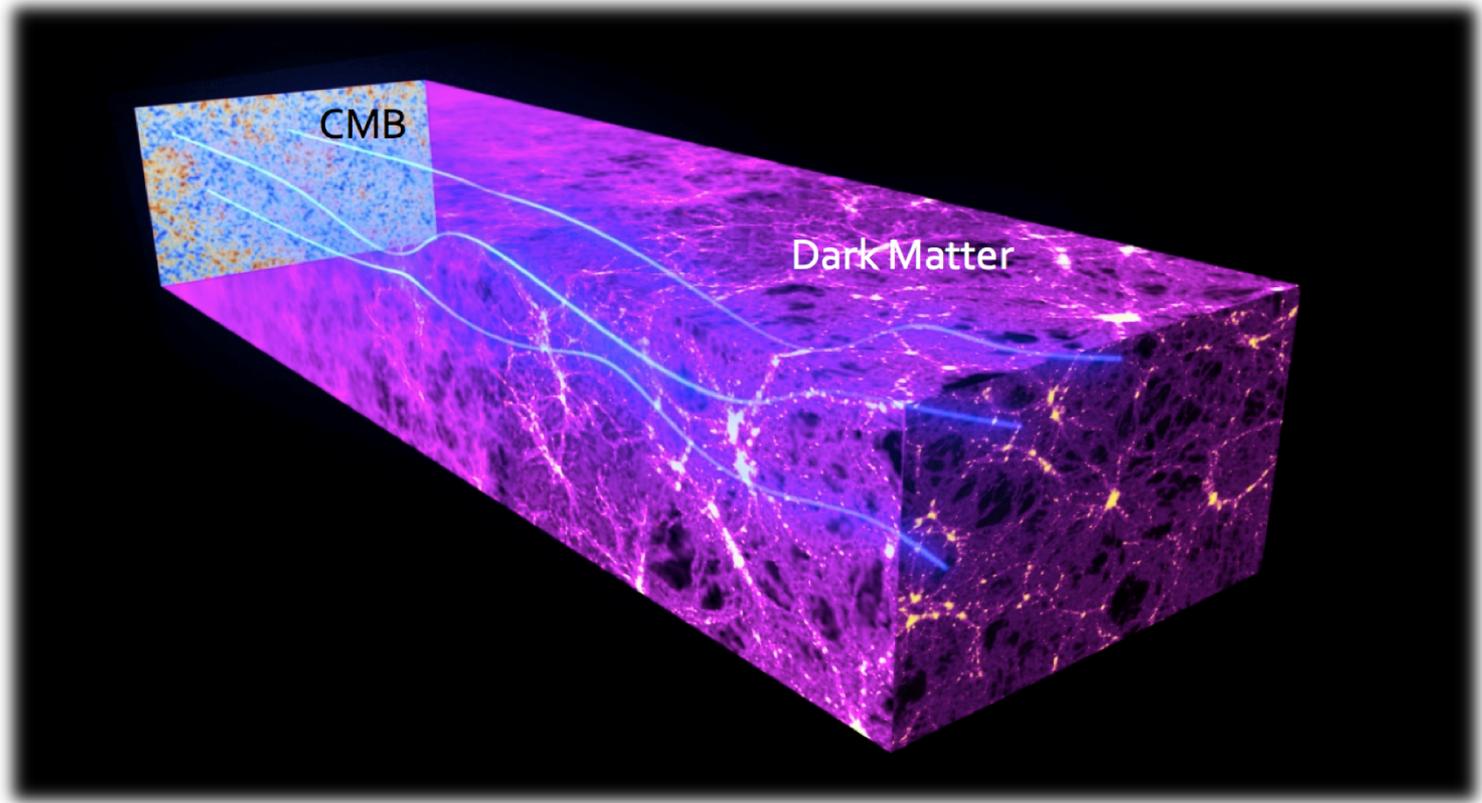
The observable universe:



- Advantages: CMB has perfectly known  $z$ , source physics linear/known, lens scales appear  $\sim$ immune to baryons for now (OWLS)

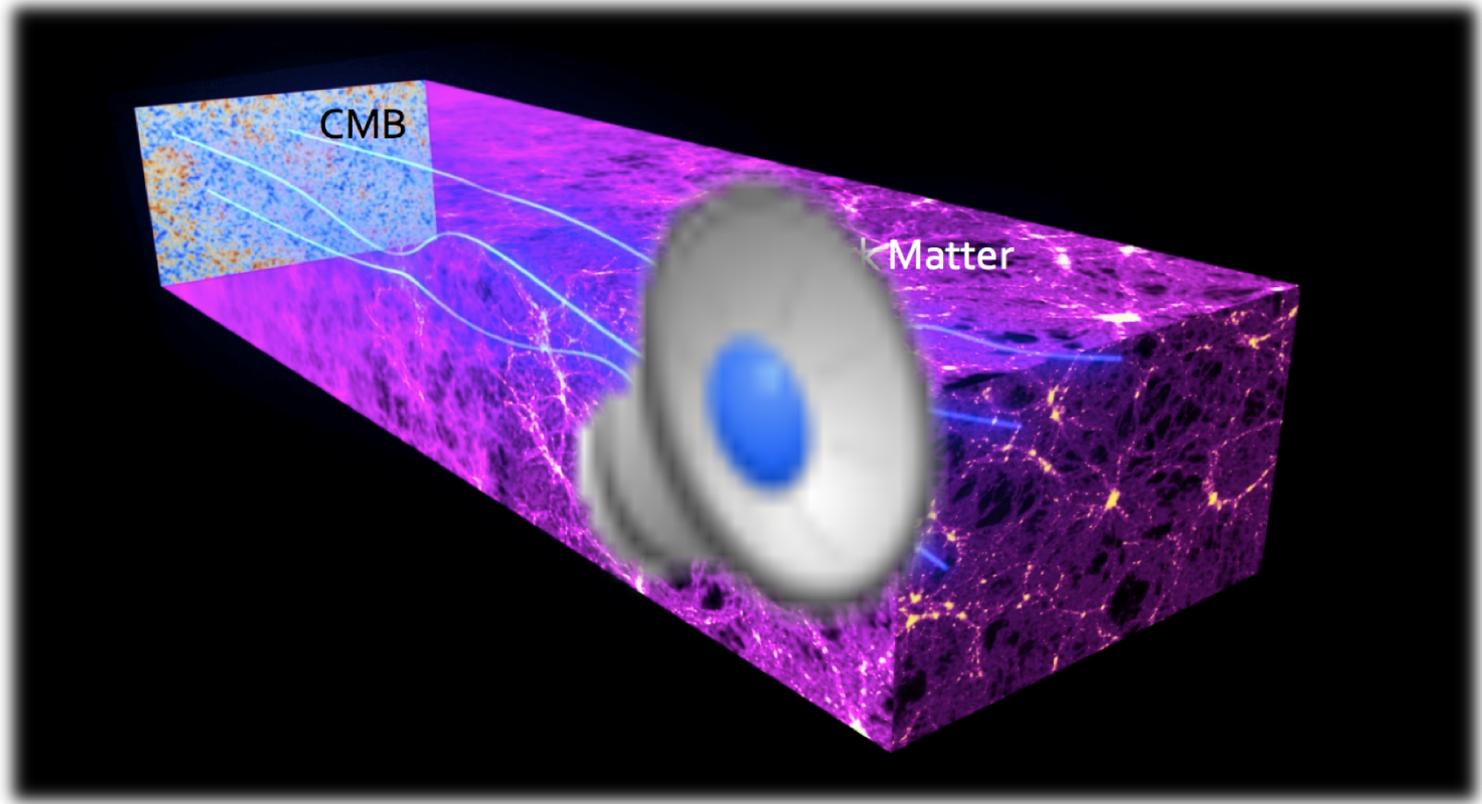
# CMB Gravitational Lensing

- Distribution of dark matter deflects CMB light that passes through

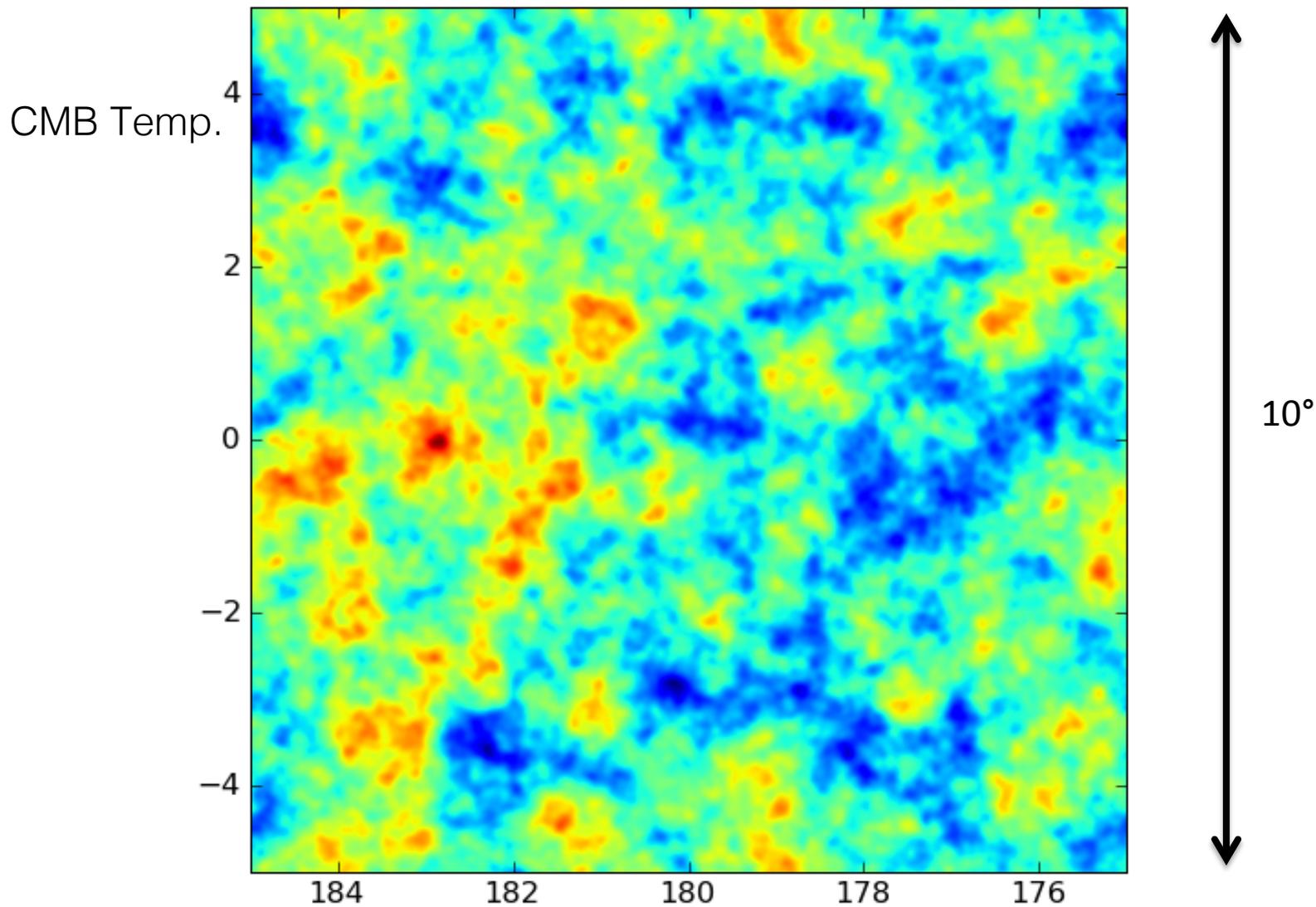


# “Light” Source for Lensing: The Cosmic Microwave Background (CMB)

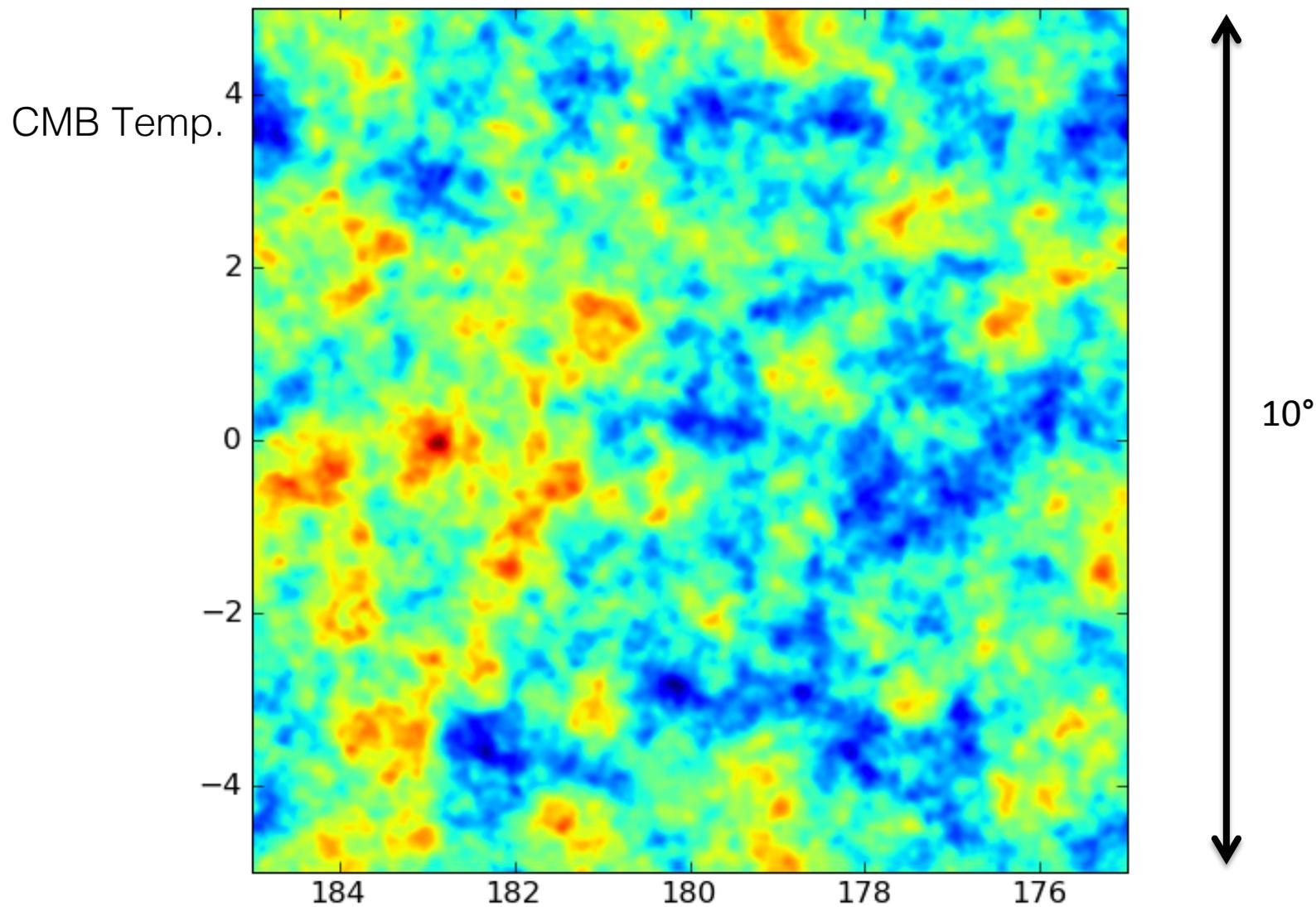
- CMB: leftover radiation from the hot primordial plasma – most distant observable source of light
- Distribution of dark matter deflects light that passes through



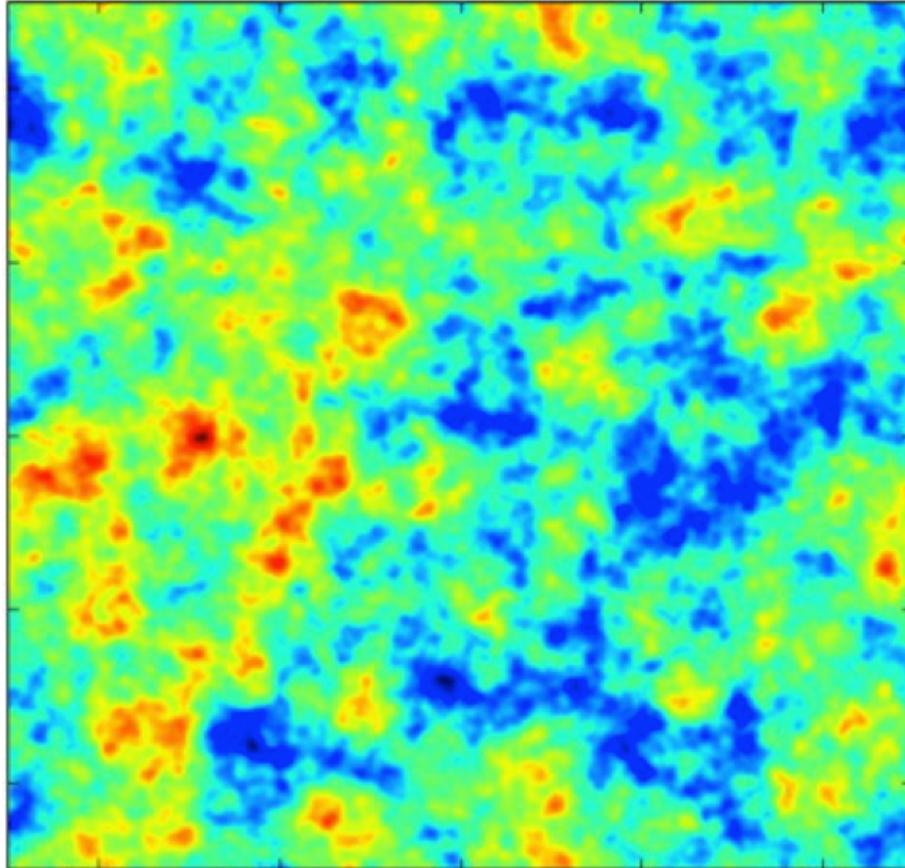
# Unlensed CMB



# Lensed CMB



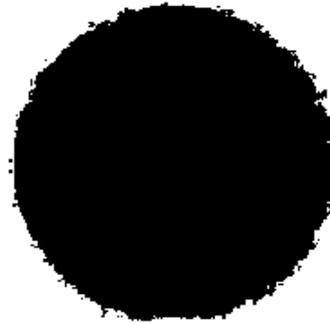
# CMB Lensing: An Approximate Picture



- Original, un-lensed, CMB fluctuations. Very well understood statistical properties, e.g., isotropy.

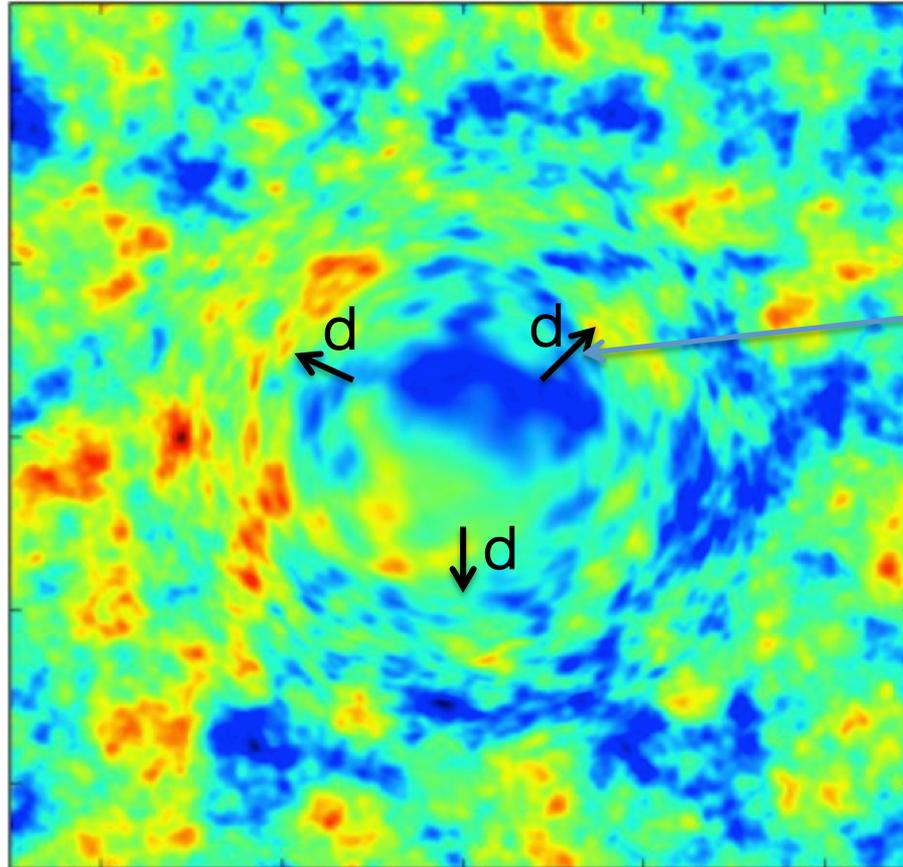
# CMB Lensing: An Approximate Picture

- Clump of dark matter in front...



# CMB Lensing: An Approximate Picture

$$T^{lensed}(\hat{\mathbf{n}}) = T^0(\hat{\mathbf{n}} + \mathbf{d})$$

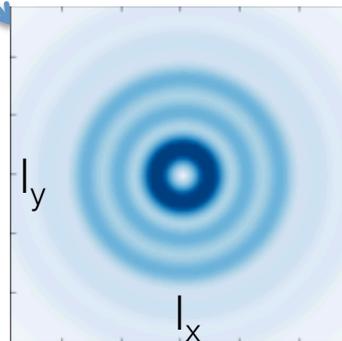
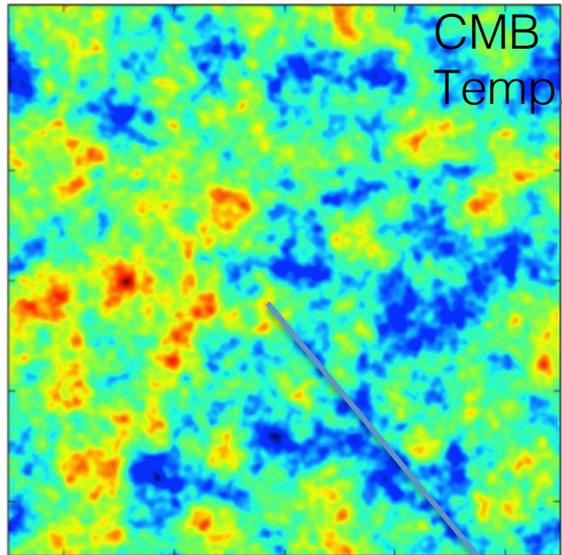


described by  
lensing  
deflection  
field:  $\mathbf{d} = \nabla\phi$

(very small:  
here  
exaggerated  
by  $x \sim 100$ ,  
actually a  
few arcmins)

- Dark matter causes lensing magnification feature in the CMB

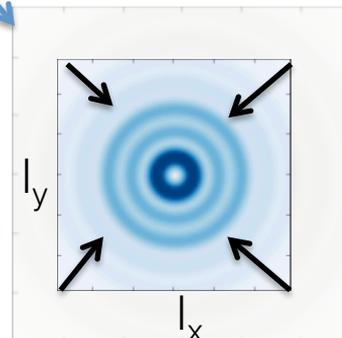
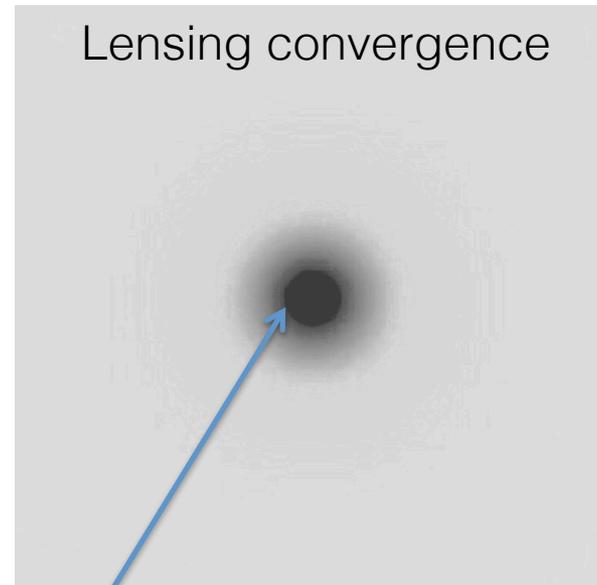
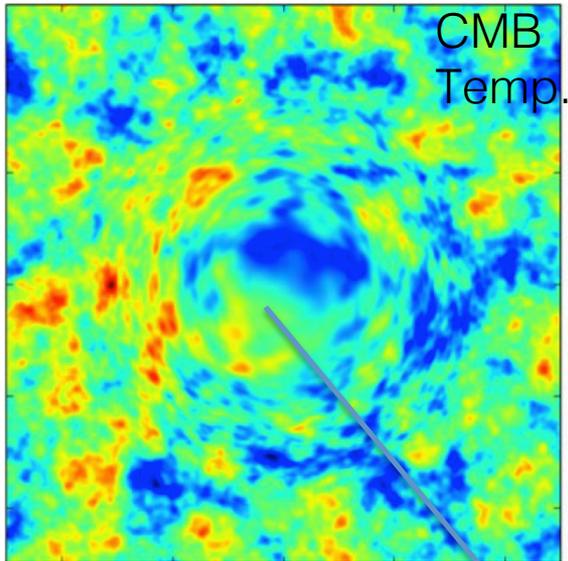
# CMB Lensing Measurement: An Approximate Picture



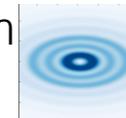
[Bucher++ 2012]

local 2D power spectrum

# CMB Lensing Measurement: An Approximate Picture



Infer lensing from “stretching”  
of the local CMB power  
spectrum (shearing)



N.B. better in polarization

[Bucher++ 2012]

local 2D power spectrum

# Lensing Reconstruction Details

- From translation invariance (of 2-point correlation function),

$$\langle T^0(\mathbf{l}) T^{0*}(\mathbf{l} - \mathbf{L}) \rangle = 0$$

T: temperature (Fourier mode)  
l: wavenumber

- **Lensing breaks translation invariance:** introduces new correlations  $T^{lensed}(\hat{\mathbf{n}}) = T^0(\hat{\mathbf{n}} + \mathbf{d}) \approx T^0 + \mathbf{d} \cdot \nabla T^0 + \dots$

$$\langle T(\mathbf{l}) T^*(\mathbf{l} - \mathbf{L}) \rangle \sim d(\mathbf{L})$$

- So: measure lensing by looking for these new, non-Gaussian correlations in the CMB two-point function

$$\hat{d}(\mathbf{L}) \sim \int d^2\mathbf{l} T(\mathbf{l}) T^*(\mathbf{l} - \mathbf{L})$$

Quadratic estimator

# What Does CMB Lensing Tell Us?

- Lensing probes the projected total mass density in each direction (of which most is dark matter) from  $z \sim 0.5-5$

$$\nabla \cdot \mathbf{d}(\hat{\mathbf{n}}) = \int_0^{r_{\text{CMB}}} dr W(r) \delta(\hat{\mathbf{n}}, r)$$

lensing deflection

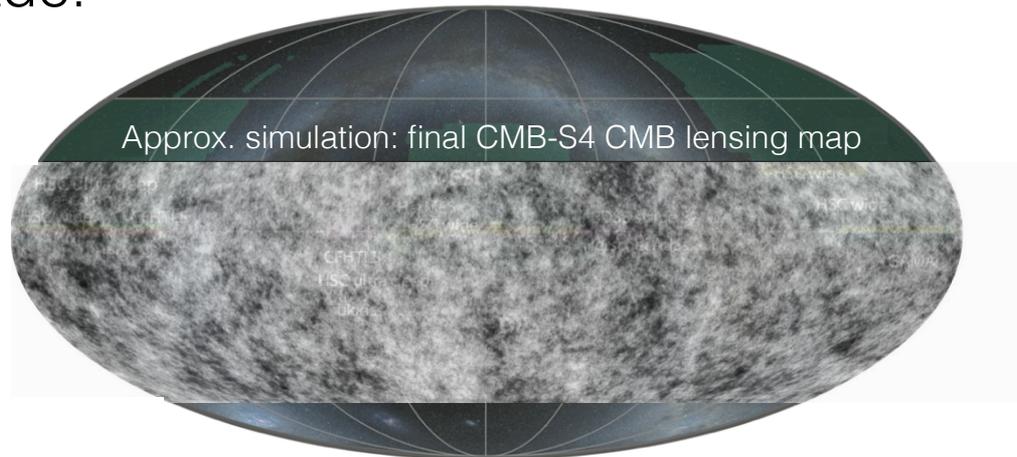
geometric projection kernel

radial distance

$\delta$  : fractional mass overdensity

$$\delta = (\rho - \bar{\rho}) / \bar{\rho}$$

- Next decade:



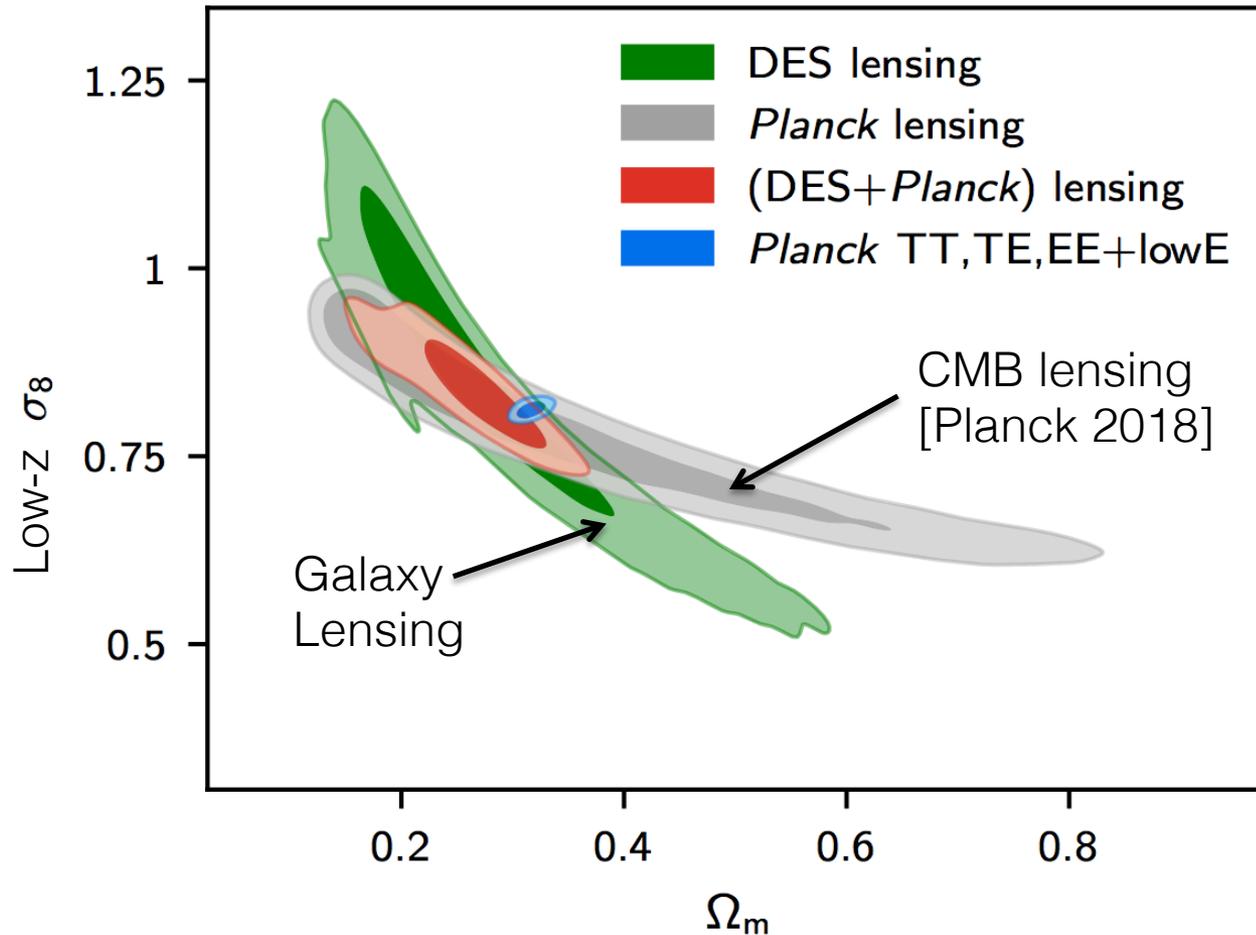
# Outline

- Part 1: Lensing science (neutrinos++) from new CMB data
- Part 2: New approaches to small-scale CMB lensing - are our current estimators good enough?
- Part 3: Delensing Simons Observatory: new methods for revealing inflationary signals



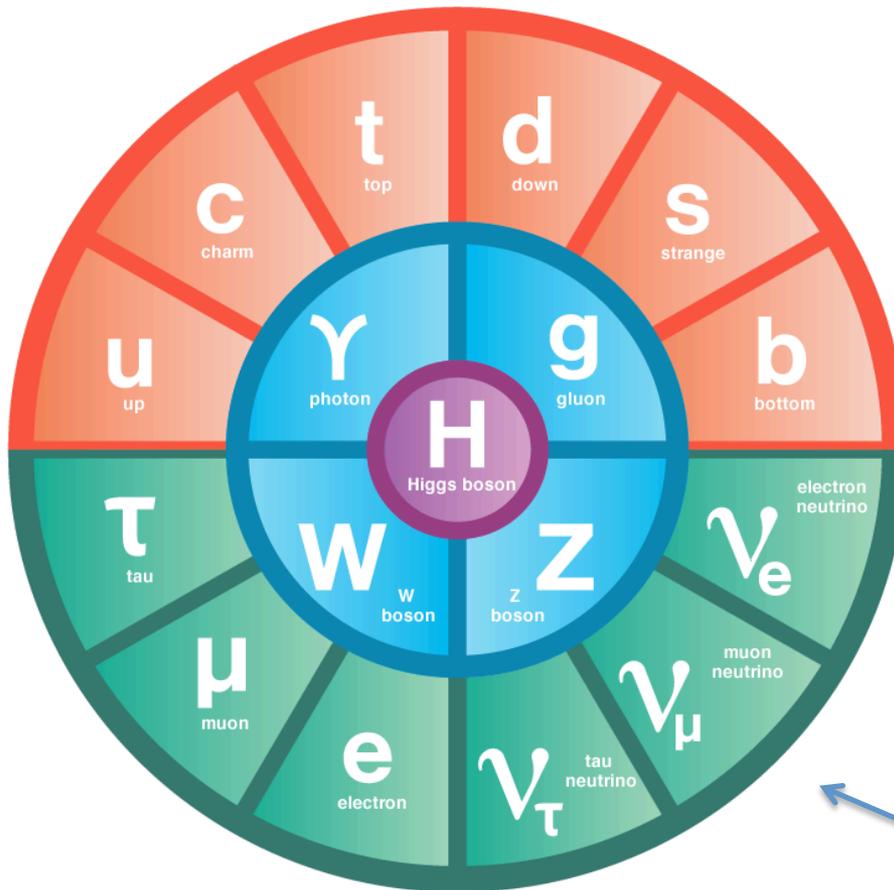
With Omar Darwish, Toshiya Namikawa et al.

# Example Physics Lensing Can Tell Us: General Test of Growth of Structure (Tensions?)



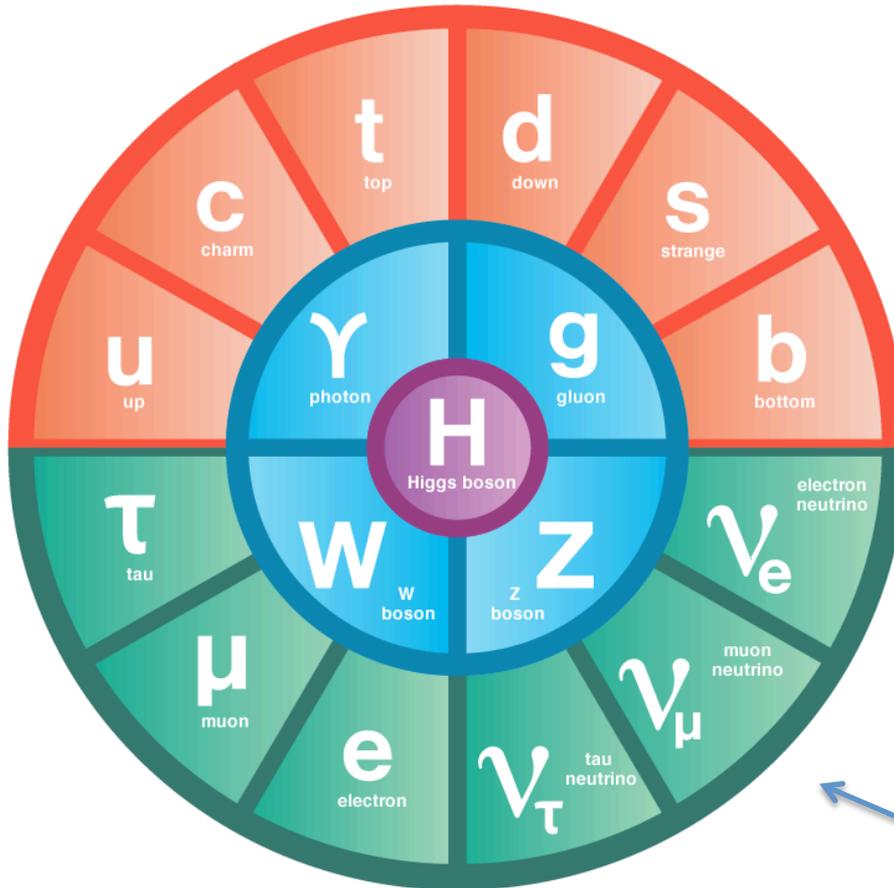
- Different degeneracy direction due to different z-dependence

# Example Physics Lensing Can Tell Us: Neutrino Mass



- Neutrinos have mass – associated physics not well understood
- we don't know:
  - absolute scale
  - mass ordering
  - their own antiparticle?
  - what gives neutrinos mass? +...
- Cosmology: measurement of mass sum  $\sum m_\nu > 60 \text{meV}$  will give insights

# Example Physics Lensing Can Tell Us: Neutrino Mass

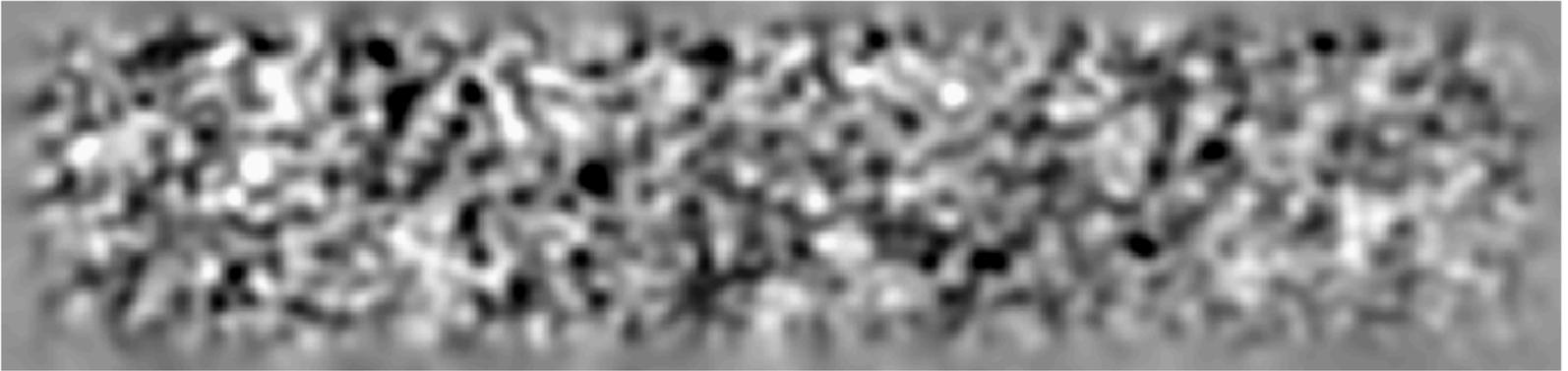


- Neutrinos have mass – associated physics not well understood
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  - absolute scale
  - mass ordering
  - their own antiparticle?
  - what gives neutrinos mass? +...
- Cosmology: measurement of mass sum  $\sum m_\nu > 60 \text{meV}$  will give insights

How to measure with lensing: neutrino mass suppresses small-scale structure growth and hence small-scales in a lensing map.

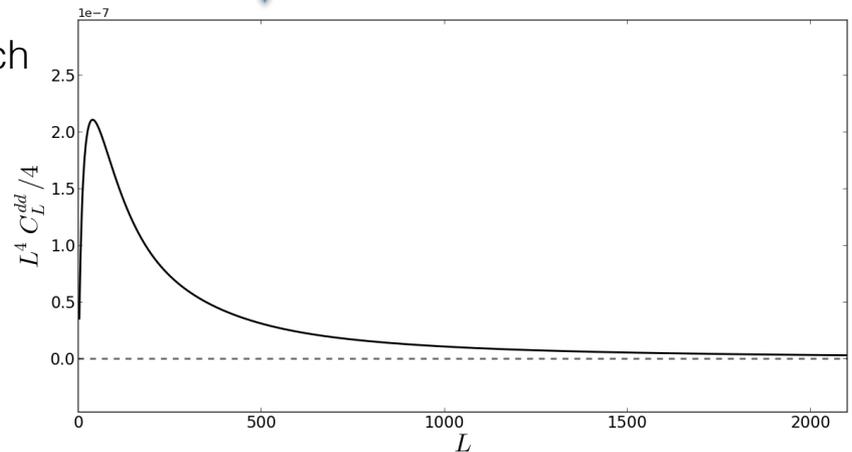
# Key Observable: CMB Lensing Power Spectrum $C_l^{dd}$

ACTPol CMB Lensing Dark Matter Map (small scales noise)



brightness = density

Y axis: “How much lensing ....”

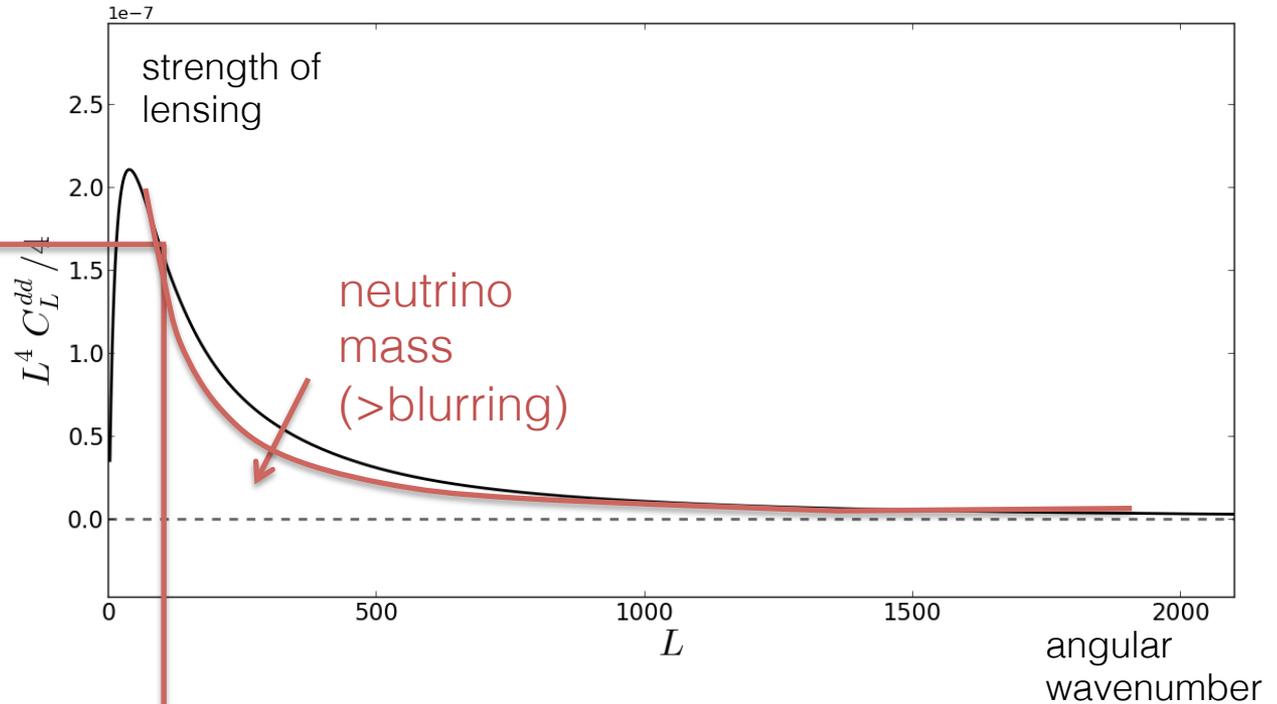


X axis: “for a lens of this angular scale?”

Describe lensing maps statistically with lensing power spectrum:

# Key Observable: CMB Lensing Power Spectrum $C_l^{dd}$

Y axis: “How much lensing<sup>2</sup> ....”

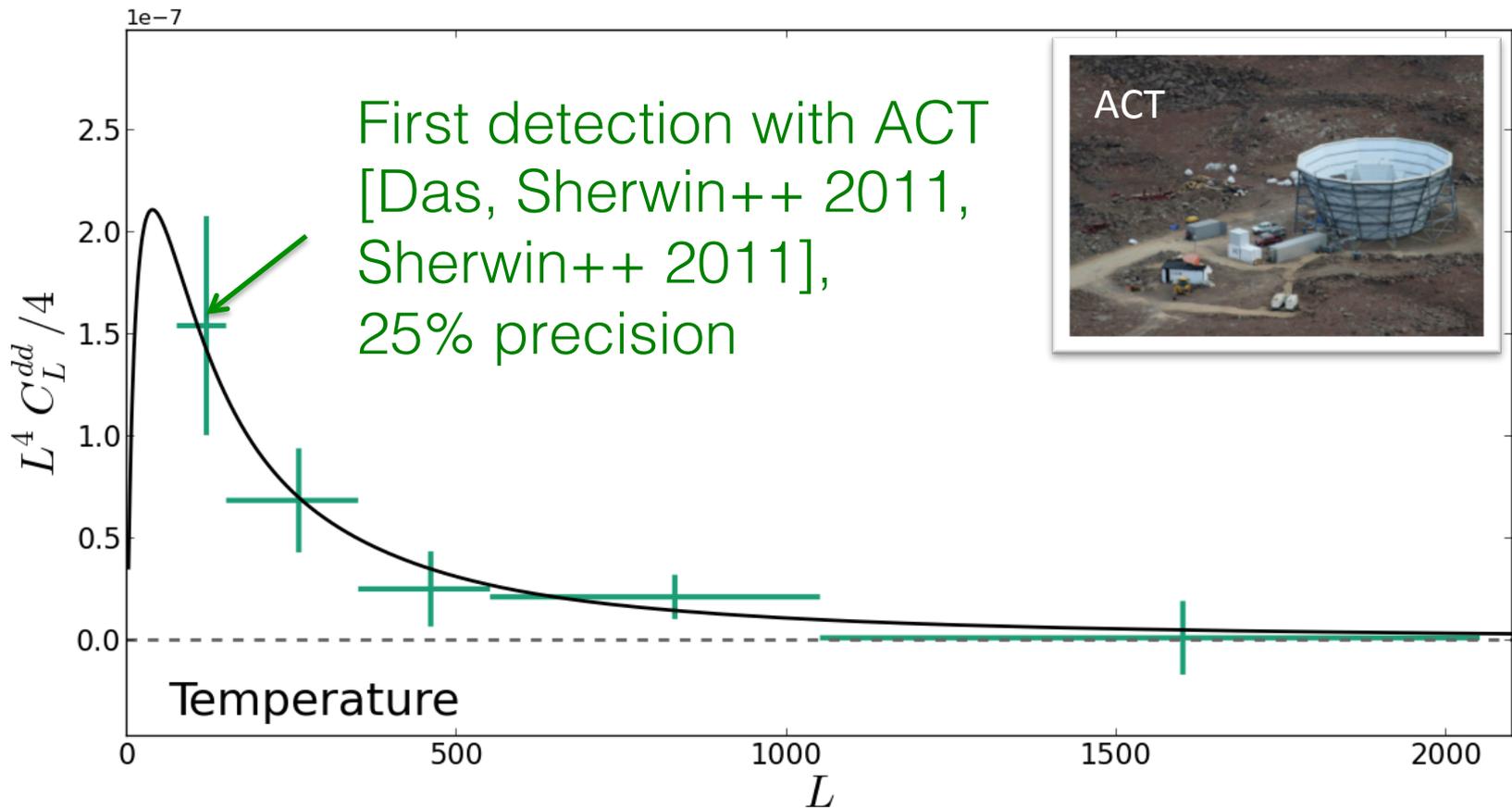


X axis: “for a lens of this angular scale?”

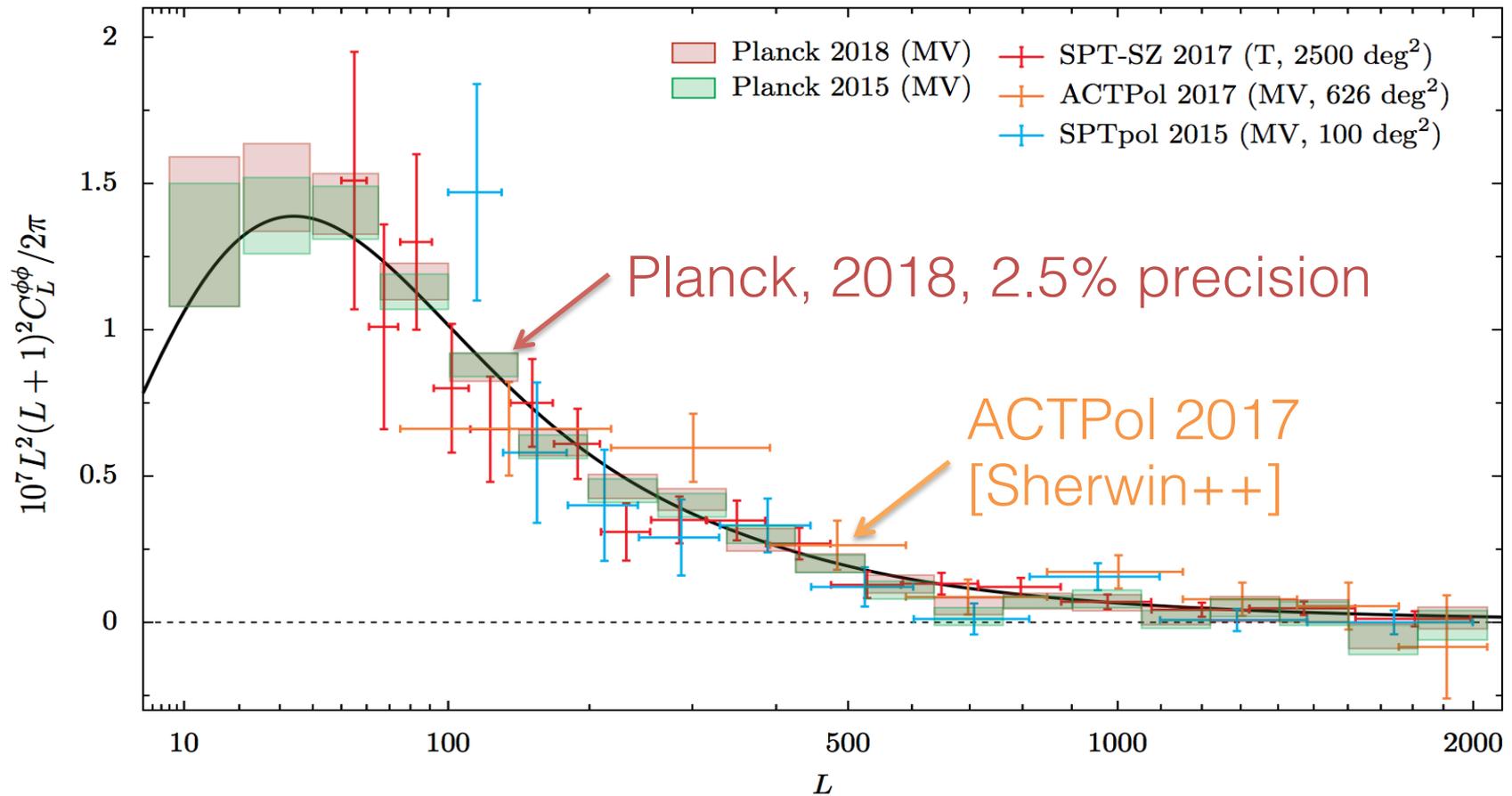
Measurement: non-Gaussianity in four-point function

$$C_L^{dd} \sim \langle d^2 \rangle_{\text{NG}} \sim \langle TTTT \rangle_{\text{NG}}$$

# CMB Lensing Power Spectra: From First Measurements...to a Precise Probe



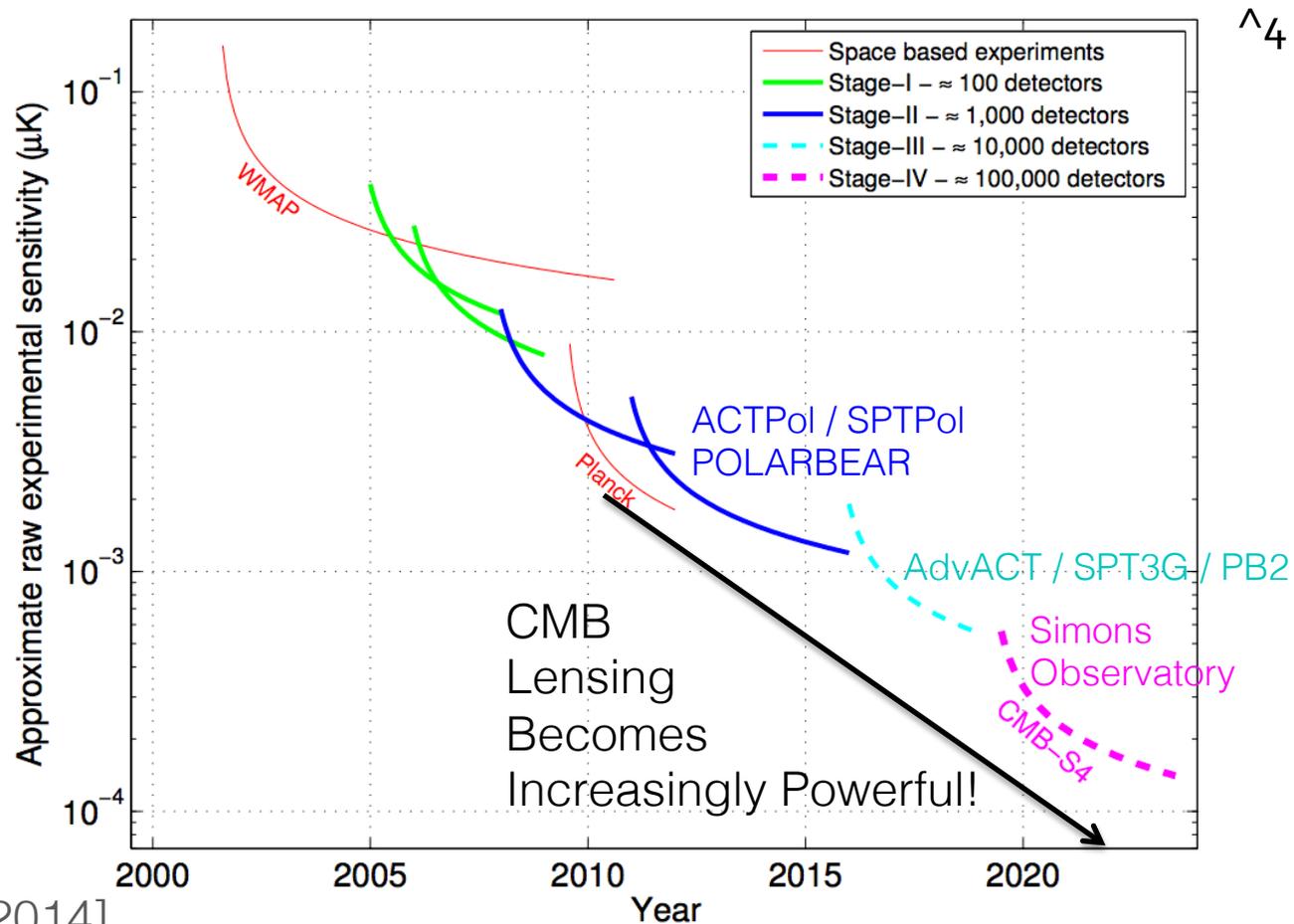
# CMB Lensing Power Spectra: From First Measurements...to a Precise Probe



- Rapid progress – but only just beginning!

# Rapid Progress: Upcoming Ground-Based CMB Experiments

CMB  
Experiment  
Noise  
Level



[Abazajian++ 2014]

# Atacama Cosmology Telescope (ACT)



- Arcminute resolution CMB telescope high in the Chilean Atacama desert, with arrays of sensitive (TES bolometer) detectors

# Now: ACTPol S13-S16

**S13**  
**PA1 @ 150 GHz**  
Patches: D1, D2, D5, D6

**S14**  
**PA1/PA2 @ 150 GHz**  
Patches: D56, BOSS-N

**S15**  
**PA1/PA2 @ 150 GHz**  
**PA3 @ 90/150 GHz**  
Patches: D56, D8, BOSS-N

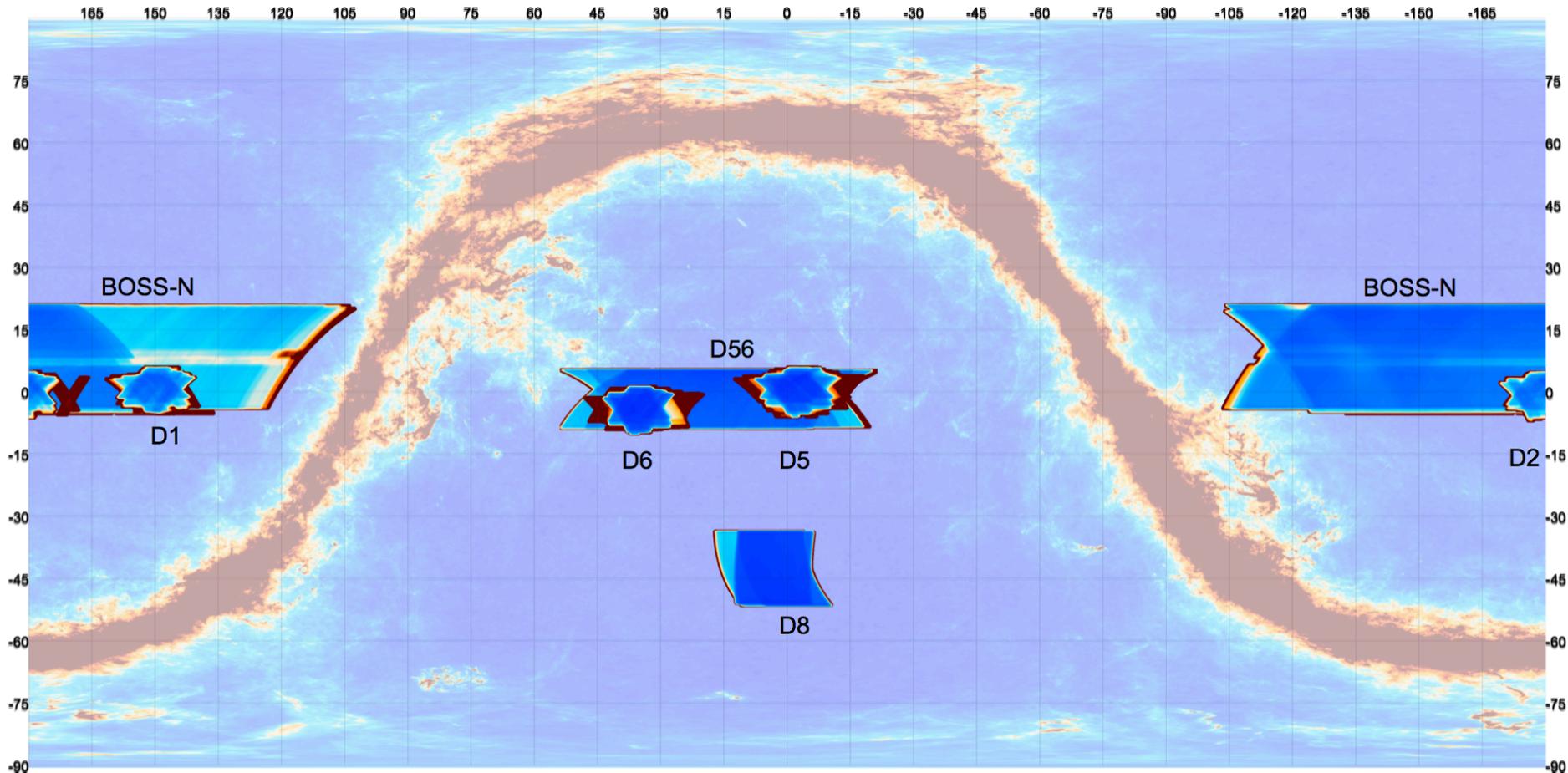
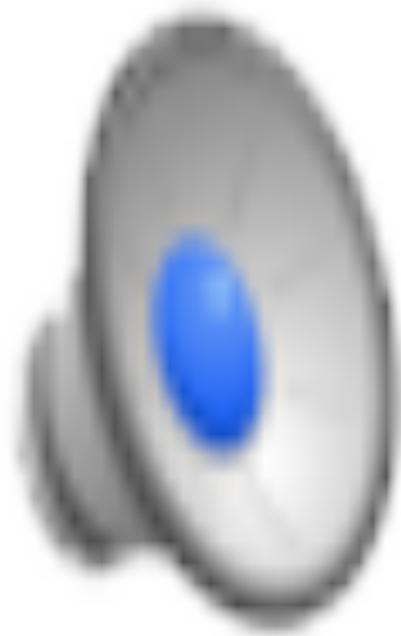


Figure: S. Aiola

- > 10x more data than used in Sherwin++ 2017 lensing

# Polarization Comparison

Q



U

ACT

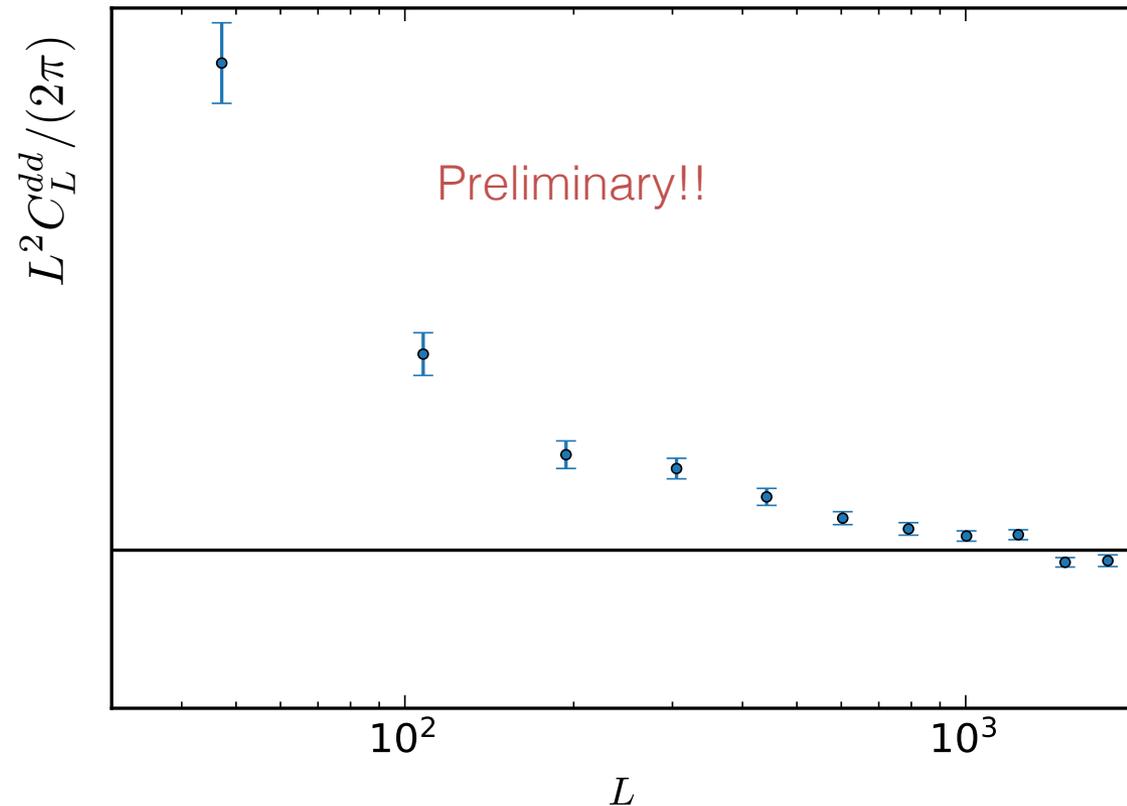
Planck

# ACTPol – next lensing paper (2019): Expect around 4% precision (preliminary results)

- Potential to independently test Planck – e.g.  $M_\nu$ , tensions (?) in high vs. low  $z$  structure,...

$$\sigma\left(\sum m_\nu\right) \sim 100 \text{ meV}$$

c.f. lower limit,  $>60\text{meV}$



[Van Engelen, Sherwin++ in prep.]  
[Namikawa++ in prep.]

# Much more to come: AdvancedACT, +...

**S16**  
**PA2 @ 150 GHz**  
**PA3 @ 90 / 150 GHz**  
**HF @ 150 / 220 GHz**

**S17**  
**MF @ 90 / 150 GHz**  
**MF @ 90 / 150 GHz**  
**HF @ 150 / 220 GHz**

**S18**  
**LF @ 28 / 41 GHz**  
**MF @ 90 / 150 GHz**  
**HF @ 150 / 220 GHz**

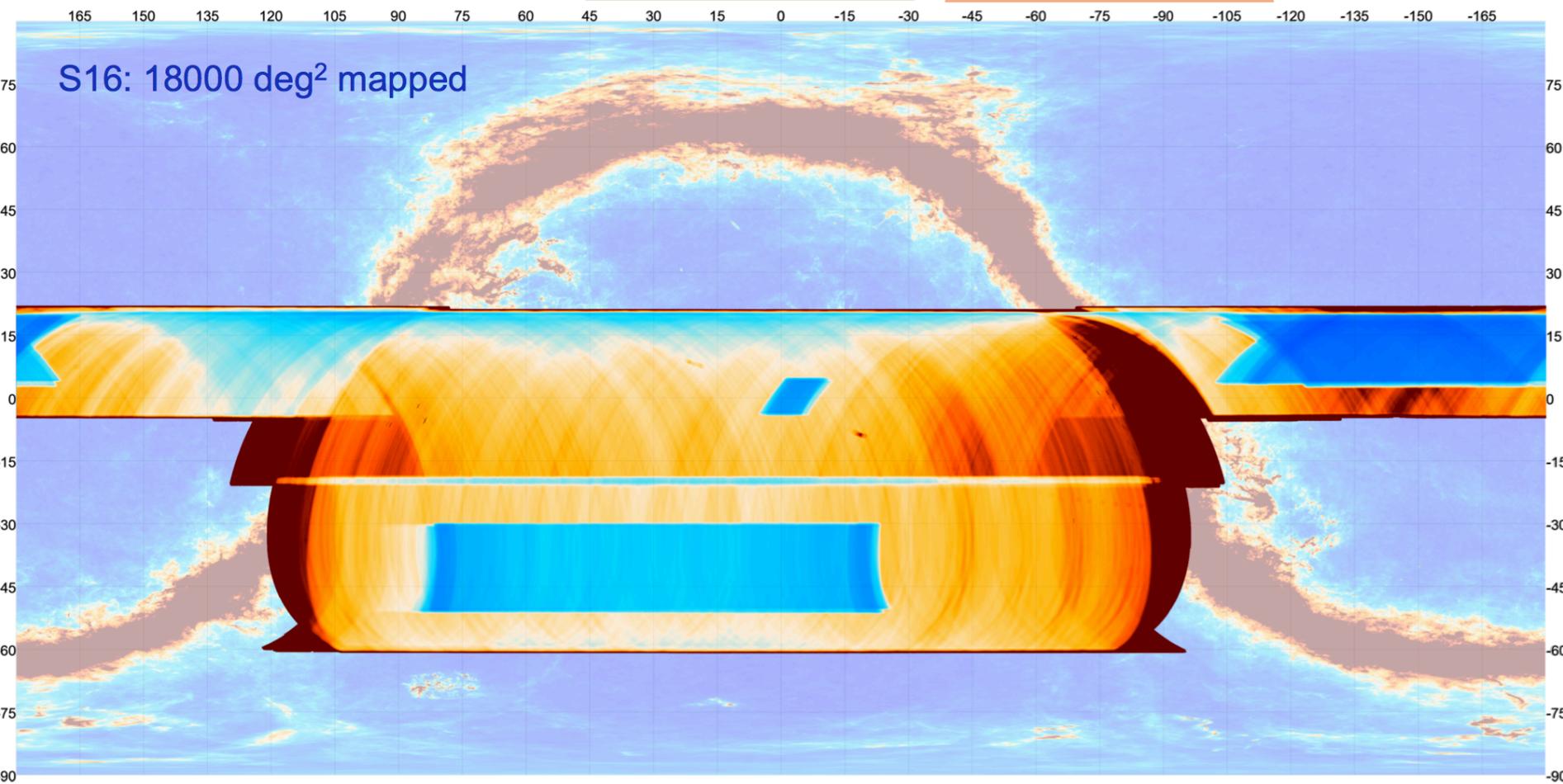
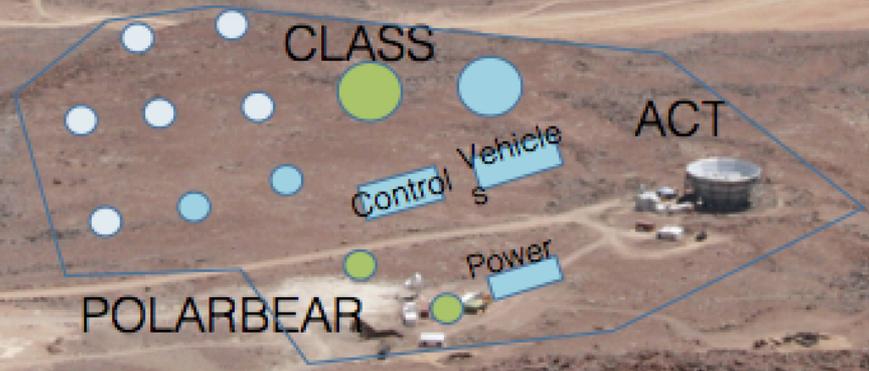
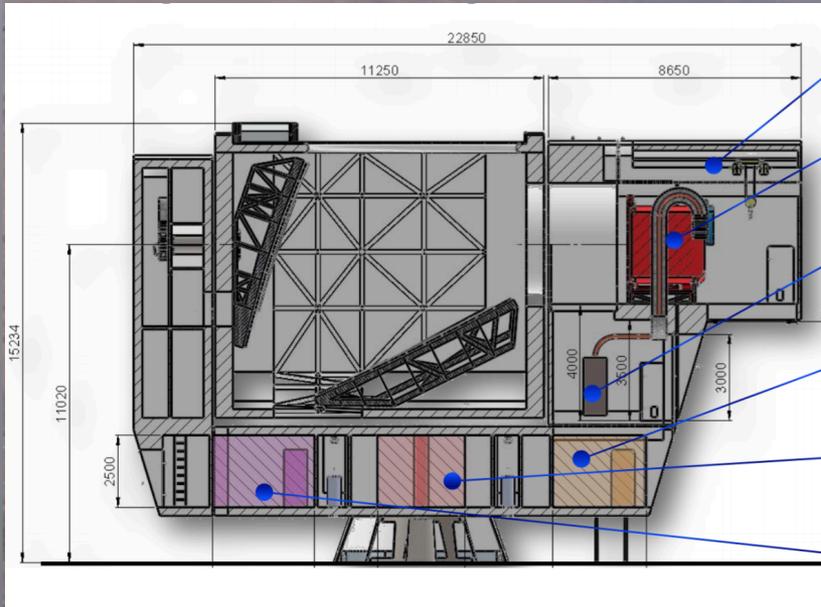


Figure: S. Aiola Map: S. Naess

# Simons Observatory

- Next generation, funded CMB experiment, 2020-
- Combines ACT, POLARBEAR collaborations

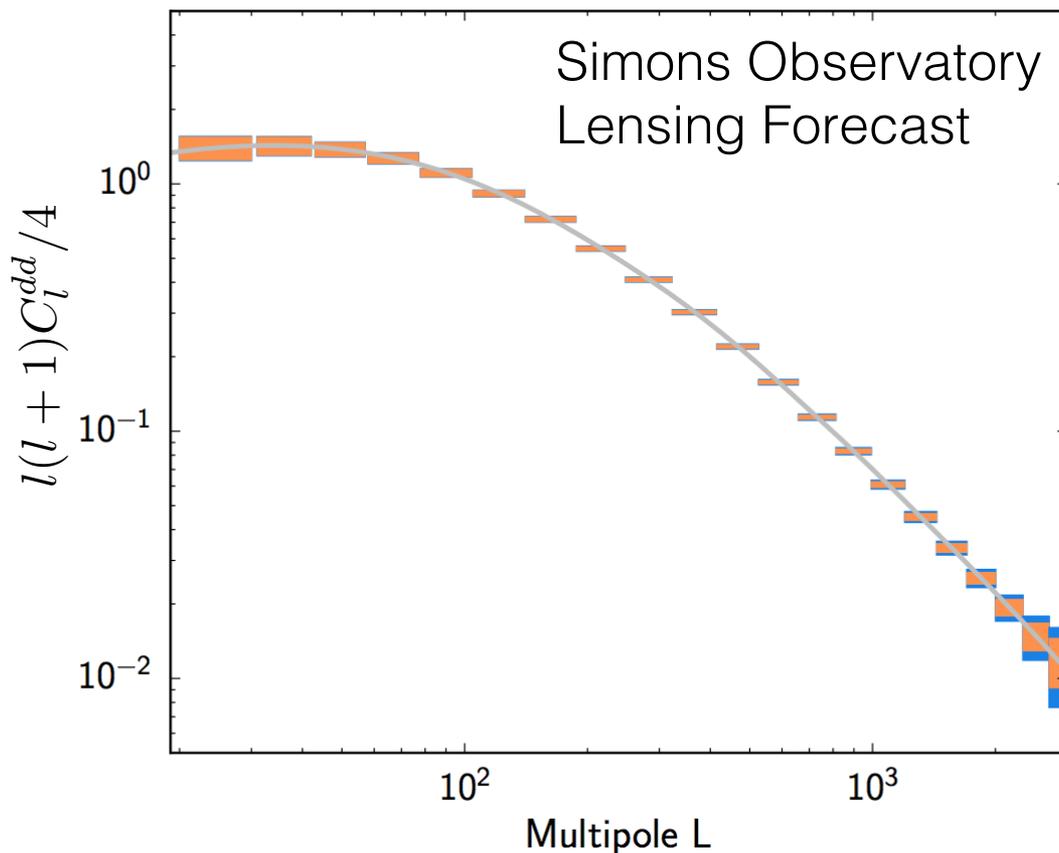


- Existing
- Notional Simons Observatory Phase 1
- Notional Pads for Simons Observatory Phase 2 and CMB S4

# The Future: Simons Observatory and CMB Stage-IV High-Precision Lensing Power Spectra

Simons Observatory:  
~0.6% precise lensing,  
half sky (2020-2025);  
CMB-S4: ~0.3%  
precise

- Will determine (to >few sigma) unknown neutrino mass in any scenario + generally test structure growth

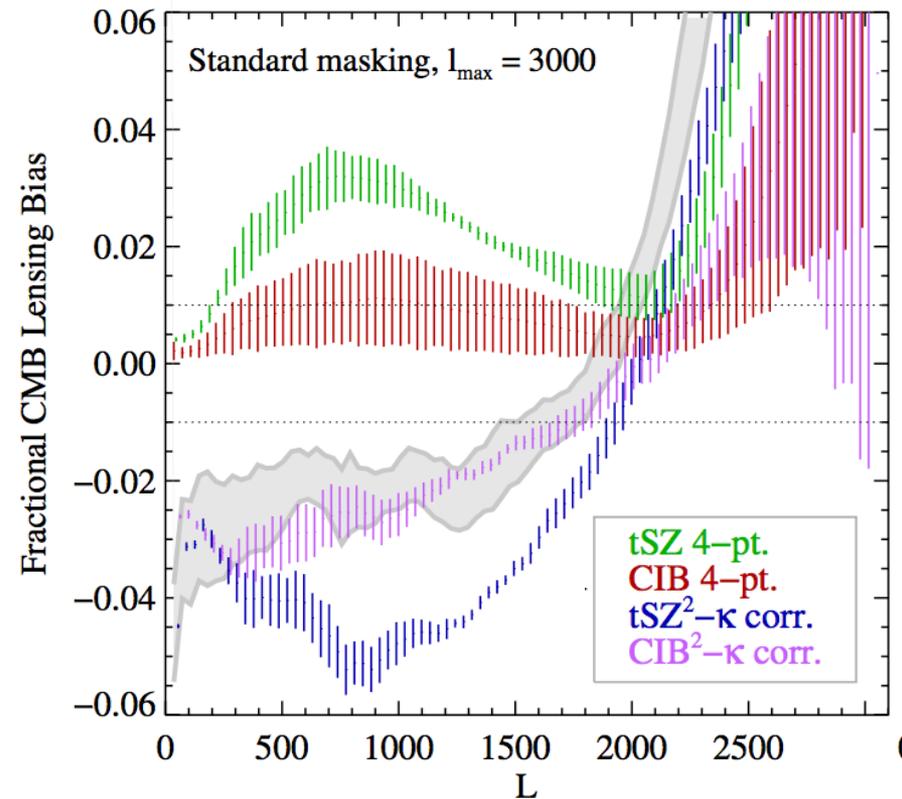


$$\sigma(\sum m_\nu) \approx 20 - 30 \text{meV} \quad (\text{Simons Obs.} / \text{CMB-S4})$$

c.f. limit, >60meV

# CMB Lensing Systematics: Main Concern

- **Foreground biases** from SZ, CIB, kSZ... contamination  
e.g.  $\langle \text{SZ SZ SZ SZ} \rangle$
- When nothing is done, ~few % effect. Multifrequency or geometric cleaning can reduce further – but work still required!
- Polarization: small (?)  
Unknown unknowns



[Sherwin++ in prep. 2016b]  
[Liu, Hill, Sherwin++ 2016]  
[van Engelen++ 2013,  
Osborne++2013]

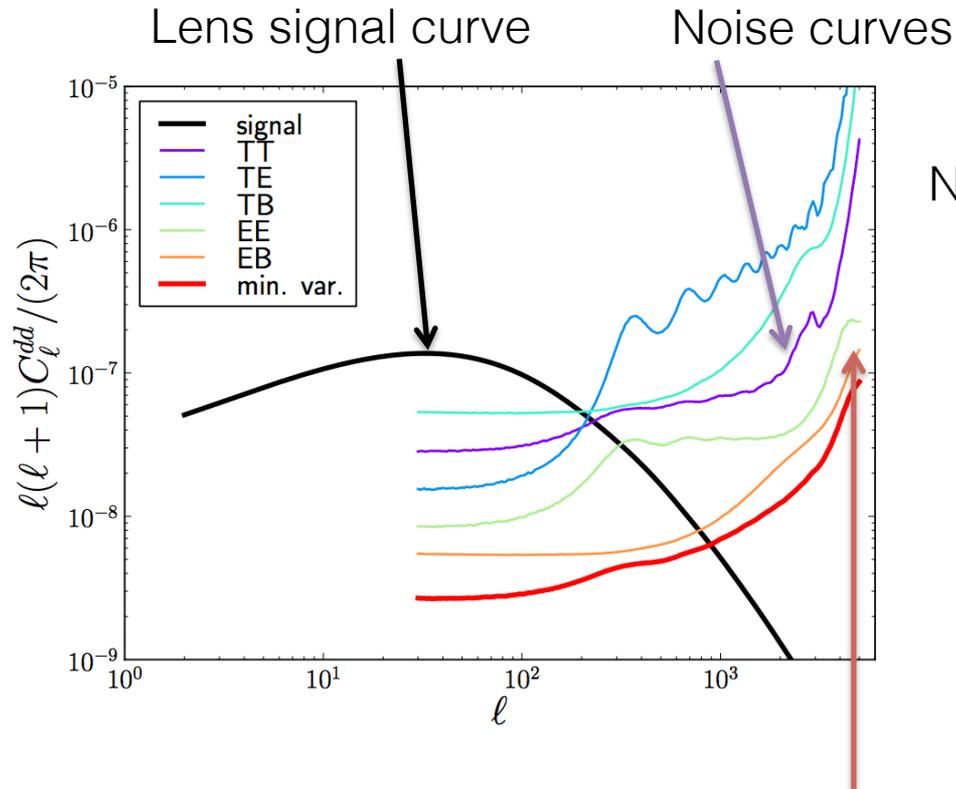
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- Part 1: Lensing science from new CMB data
- Part 2: New approaches to small-scale CMB lensing - are our current estimators good enough?
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with Boryana Hadzhiyska, Simone Ferraro,  
Mat Madhavacheril

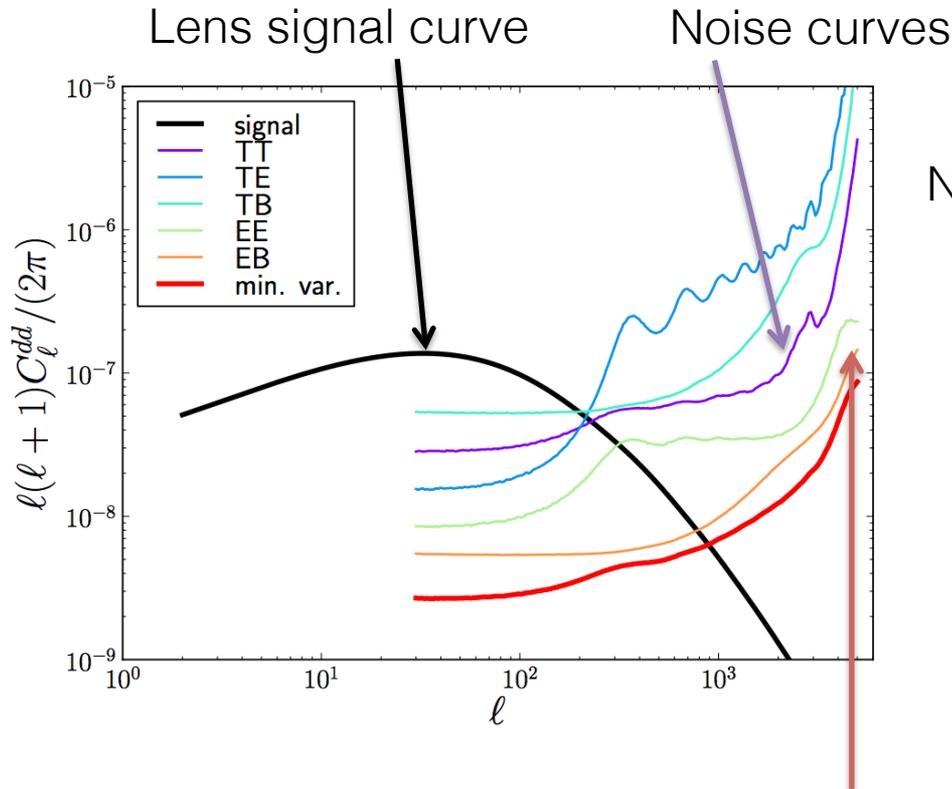
# Hints at possible improvements on small scales



Noise for CMB-S4 [from Schaan++]

- A puzzle: quadratic estimator noise gets large – **seemingly cannot probe tiny CMB lenses** / scales (interesting for e.g. axions, WDM, cross-corrs...)

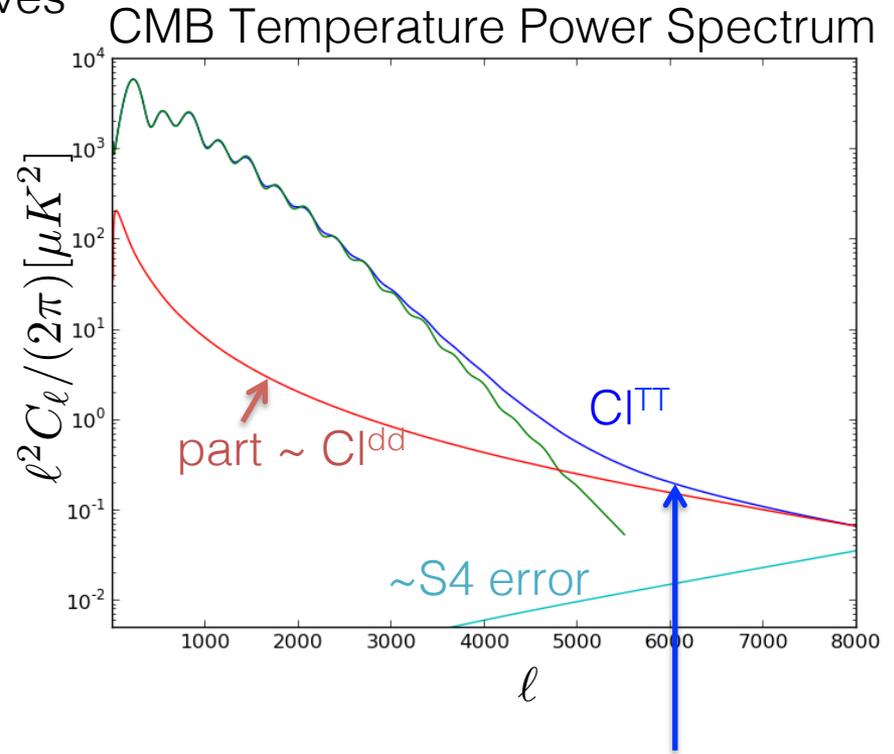
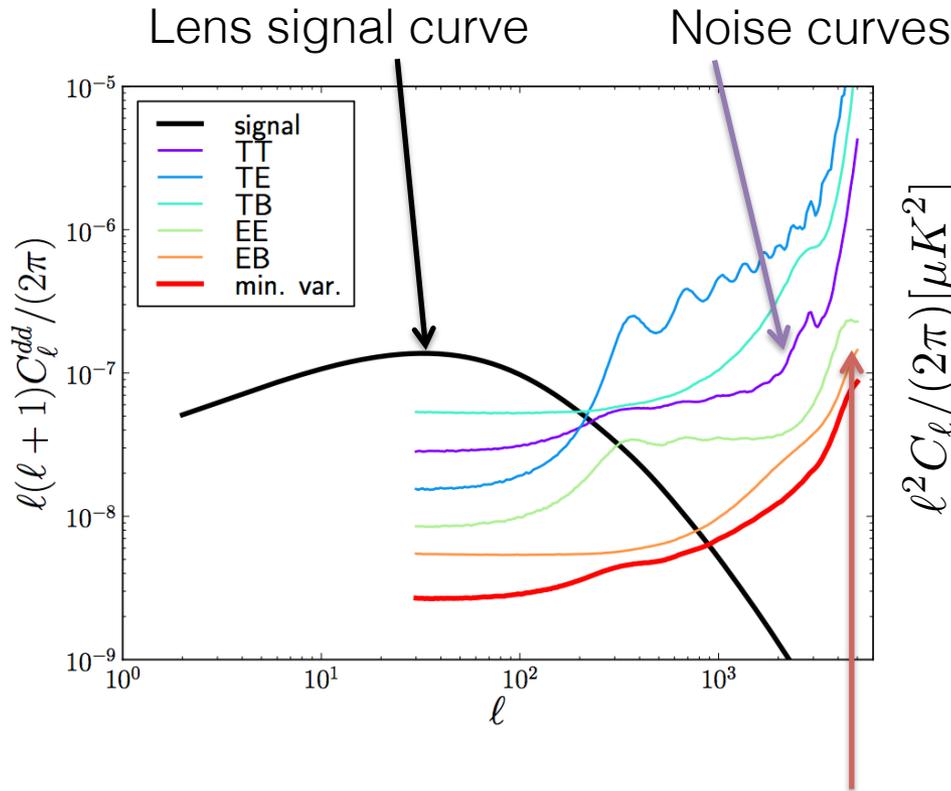
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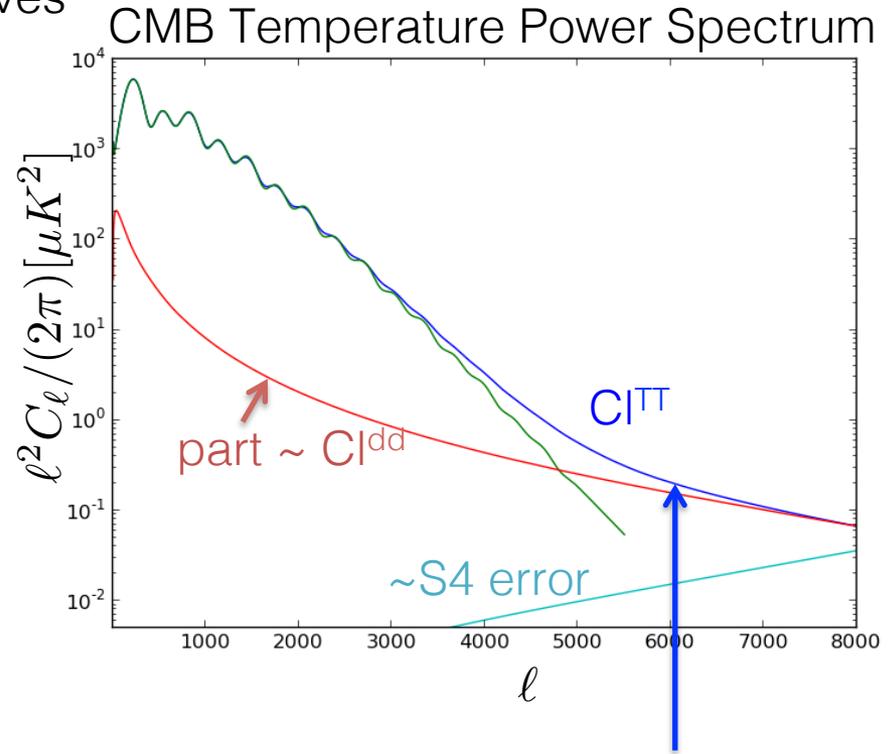
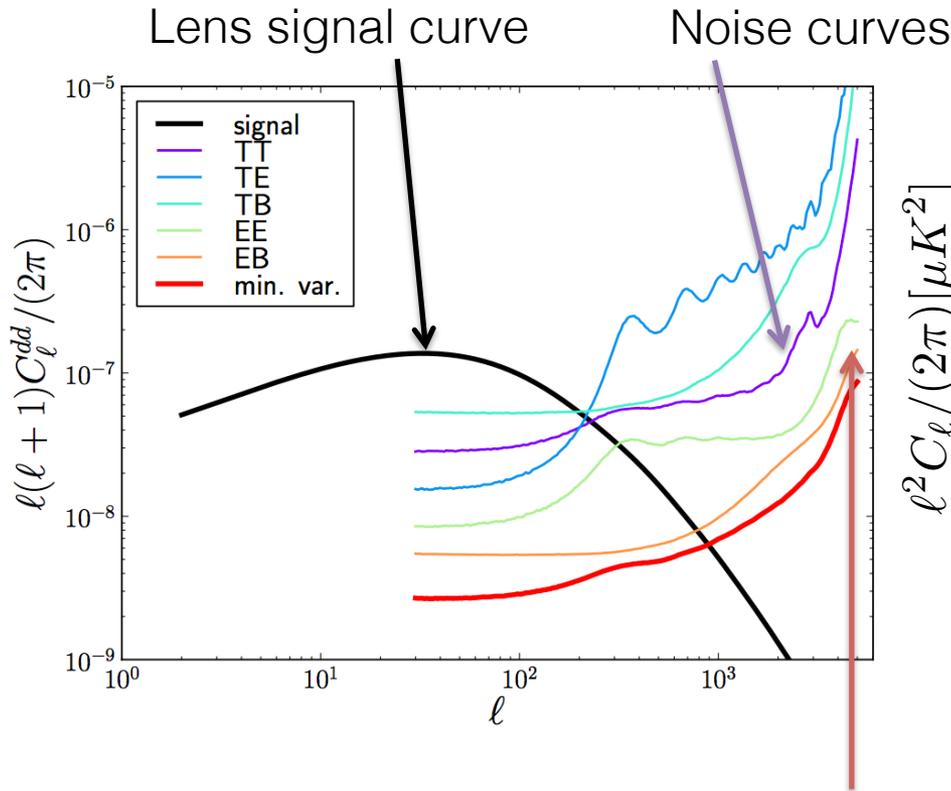
# Hints at possible improvements on small scales



- A puzzle: quadratic estimator noise gets large – seemingly cannot probe tiny CMB lenses / scales (interesting for e.g. axions, WDM, cross-corrs...)

- But with low enough noise, can read off tiny lenses from small-scale power spectrum.

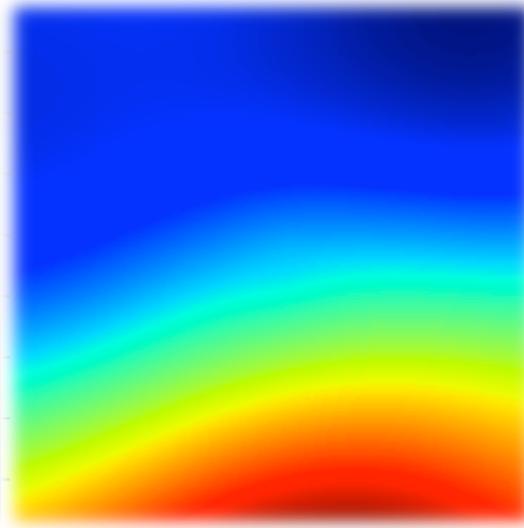
# Hints at possible improvements on small scales



- A puzzle: quadratic estimator noise gets large – seemingly cannot probe tiny CMB lenses / scales (interesting for e.g. axions, WDM, cross-corrs...)
- But with low enough noise, can read off tiny lenses from small-scale power spectrum. Is there a better estimator out there?

# The simplicity of small-scale CMB

Small-scale CMB / lens



~gradient

- On small scales, CMB gradient  $\nabla T$  is effectively constant. Lensing expansion:

$$T(\mathbf{x}) = T^u(\mathbf{x} + \mathbf{d}) \approx T^u(\mathbf{x}) + \mathbf{d}(\mathbf{x}) \cdot \nabla T^u + \dots$$

$\mathbf{d} = \nabla \phi$

Noise  
Foregrounds

- Fourier transform with constant gradient:

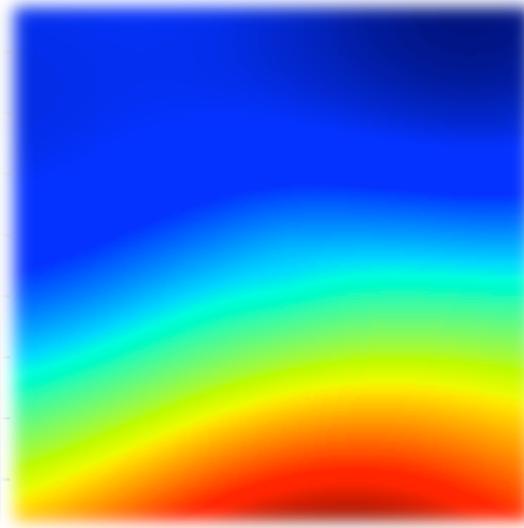
$$T(\mathbf{L}) = d(\mathbf{L}) \times \hat{\mathbf{n}}_{\mathbf{L}} \cdot \nabla T^u$$

measured  
CMB

can measure this gradient (projected  
on L direction) from data easily

# Gradient Inversion lensing estimation

Small-scale CMB / lens



~gradient

- Suggests simple “gradient inversion” estimator:

$$\hat{d}^{GI}(\mathbf{L}) = \frac{T(\mathbf{L})}{\hat{\mathbf{n}}_{\mathbf{L}} \cdot \nabla T^u}$$

- c.f. quadratic estimator: only divides out  $\langle \text{grad}^2 \rangle$  –  
extra error!

$$\hat{d}^{QE}(\mathbf{L}) = \hat{d}^{GI}(\mathbf{L}) \frac{(\hat{\mathbf{n}}_{\mathbf{L}} \cdot \nabla T^u)^2}{\langle (\hat{\mathbf{n}}_{\mathbf{L}} \cdot \nabla T^u)^2 \rangle}$$

# Continuous Small-scale Lensing Reconstruction

- Make continuous assuming slowly varying gradient, introduce anisotropic, gradient-dependent weighting:

$$\hat{d}^{GI}(\mathbf{L}) = \frac{T(\mathbf{L})}{\hat{\mathbf{n}}_{\mathbf{L}} \cdot \nabla T^u}$$

↓

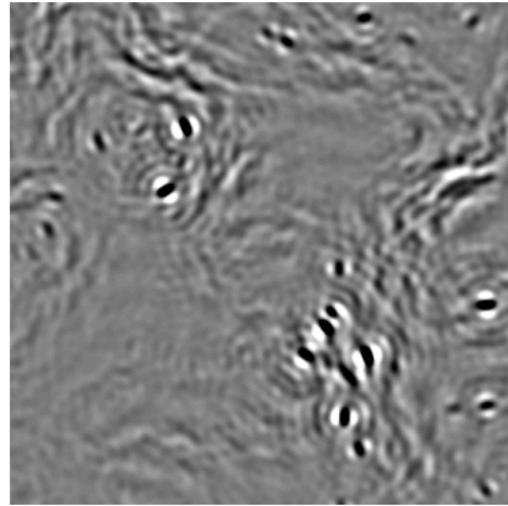
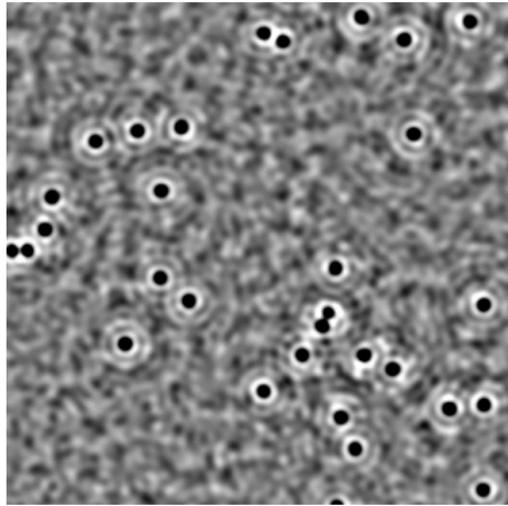
$$\hat{d}^{GI}(\mathbf{L}) \sim FT \left[ \frac{T(\mathbf{x}) - T^{<2000}(\mathbf{x})}{\hat{\mathbf{n}}_{\mathbf{L}} \cdot \nabla T^{<2000}(\mathbf{x})} \times W(\mathbf{x}, \mathbf{L}) \right]$$

“Gradient inversion” estimator

# Simulation: GI lensing maps and spectra

- Simulated lensing reconstruction with new method ( $L > 4000$ ):

Input  
small-  
scale lens  
map (with  
artificial  
“halos”)



Reconstructed  
lens map  
(weighted)

- GI reconstruction appears to do well, especially on large gradients

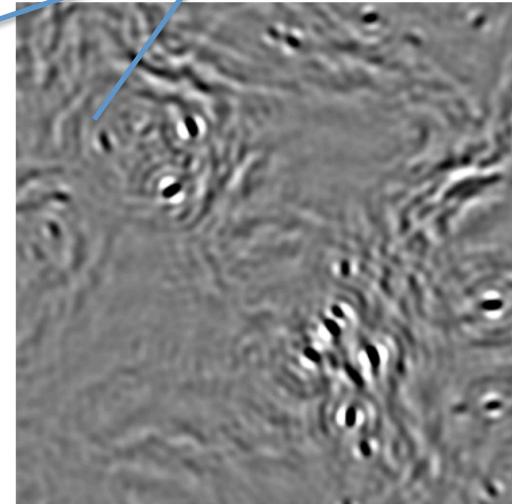
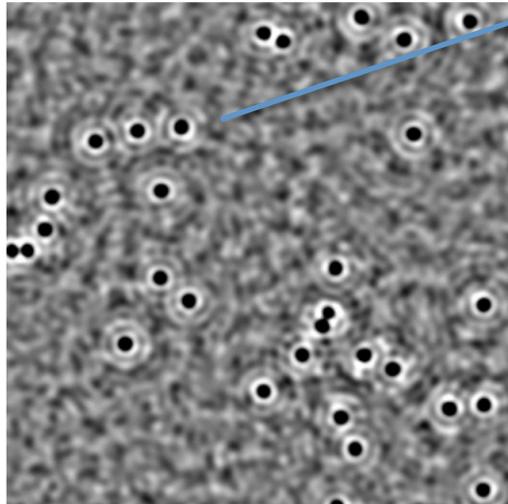
# Simulation: GI lensing maps and spectra

- Simulated lensing reconstruction

Validate: cross-correlate reconstruction with input lensing

>4000):

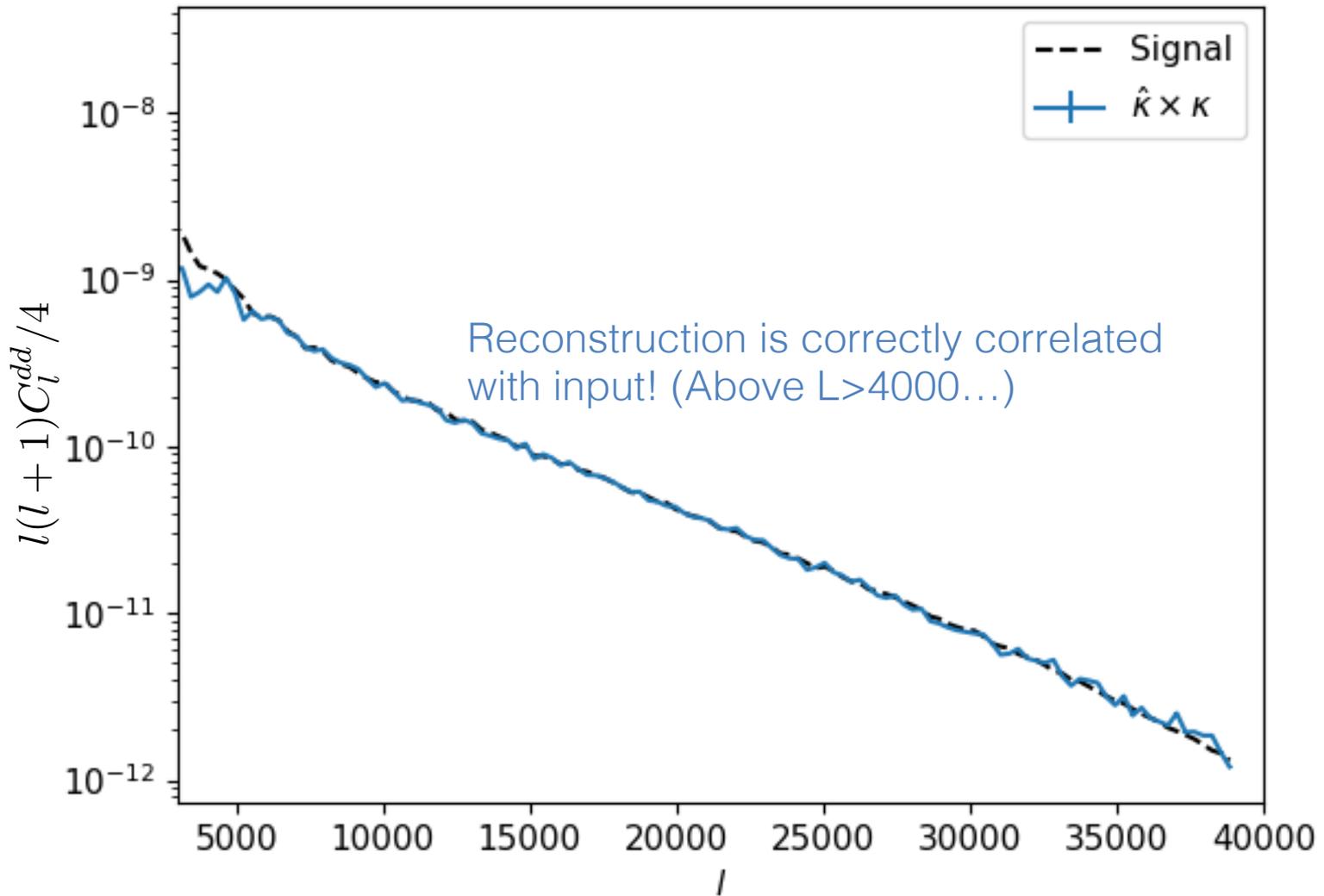
Input small-scale lens map (with artificial "halos")



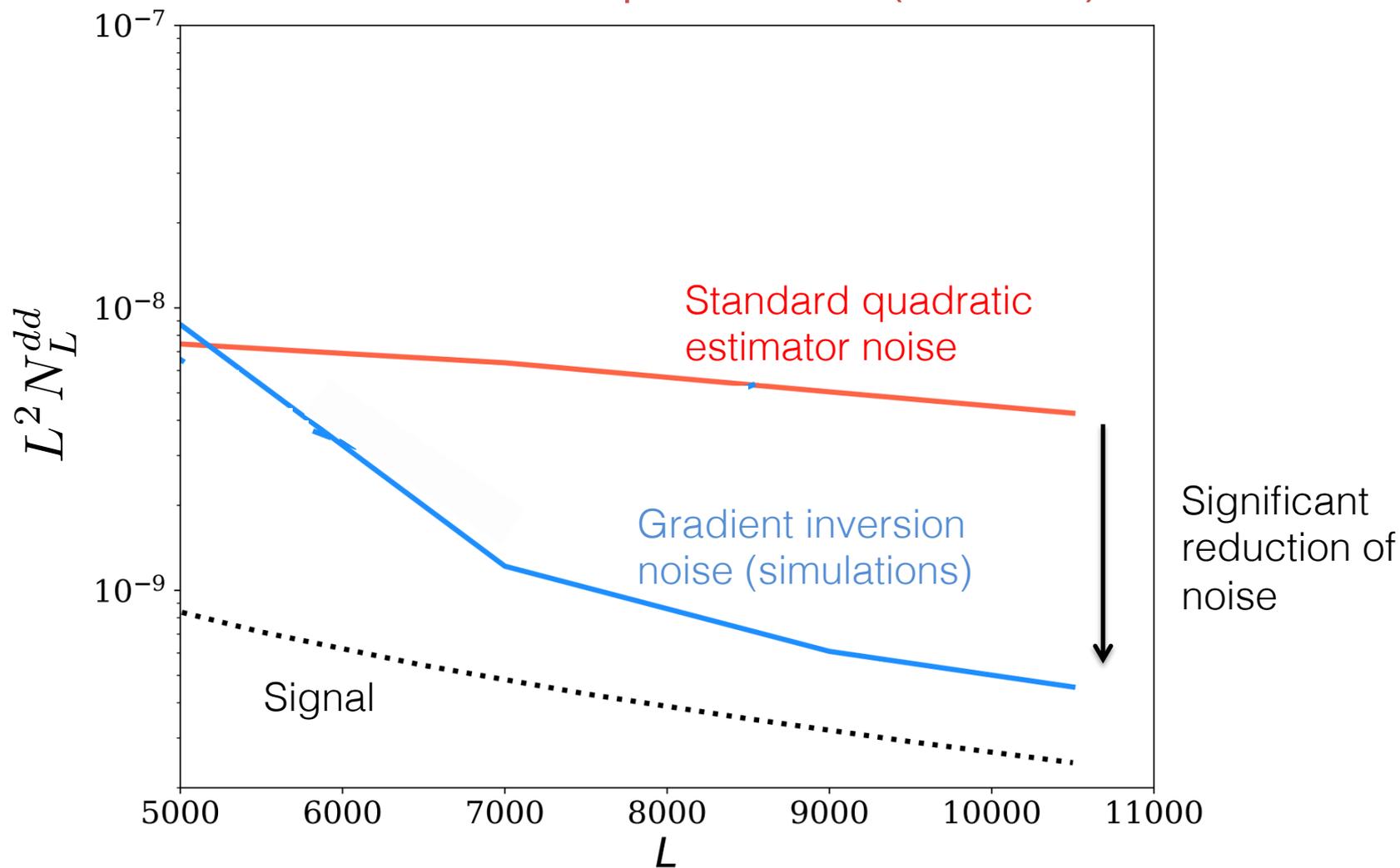
Reconstructed lens map (weighted)

- GI reconstruction appears to do well, especially on large gradients

# Validation: Reconstruction x input cross-correlation



# Lensing noise improvements possible? Future CMB experiment (0.1 $\mu$ K')



# Noise improvements possible? SO and CMB-S4

- Significant improvements possible on signal-noise ratio at  $L > 4000$

SNR	UL	S4-like	SO-like
Auto QE	205	100	7
Auto GI	1515	360	30

$C_L^{dd}$  →

Lensing power spectrum SNR ↗

↘ New method: factor ~four improvement in small scale SNR

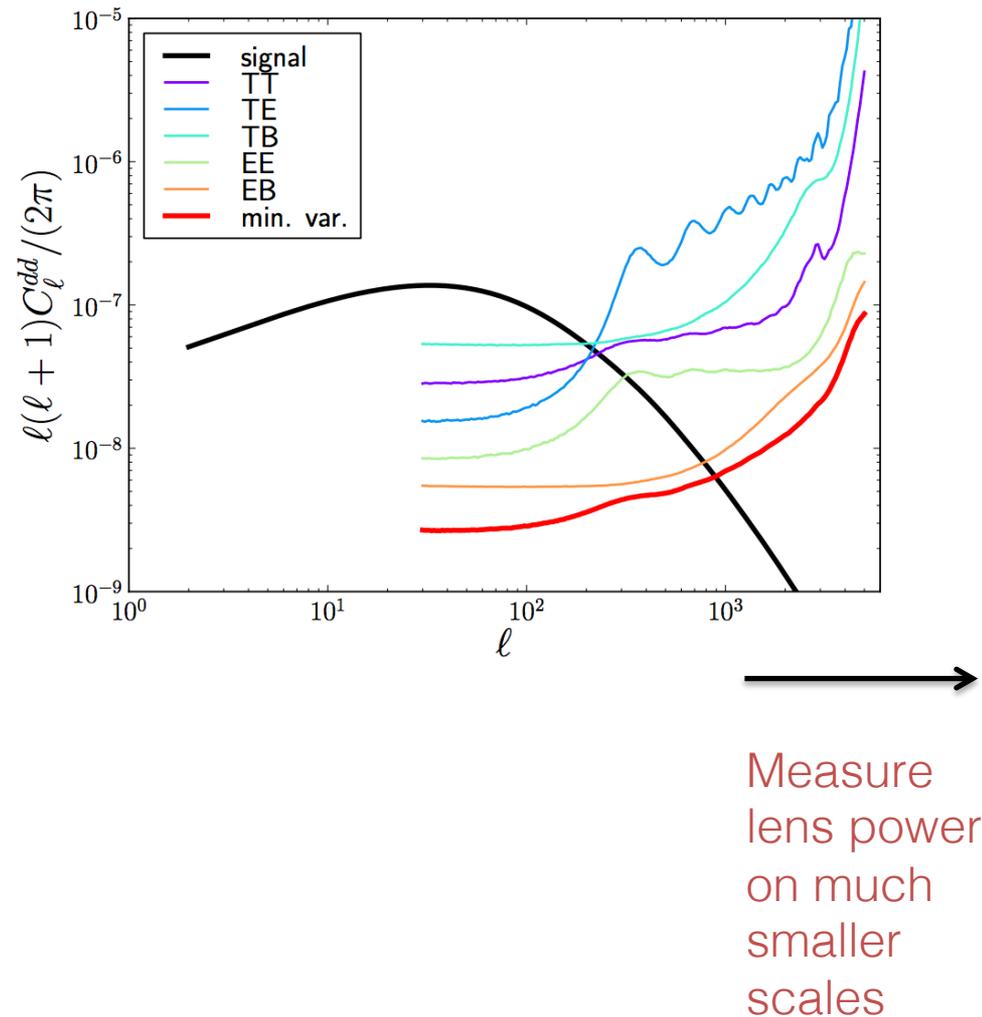
- Major caveat: scatter from foregrounds. But not bias; signal, unlike foregrounds, is correlated with gradients.

[Hadzhiyska, Sherwin, Madhavacheril, Ferraro 2019, Horowitz, Ferraro, Sherwin 2019]

# Next steps and future work

- Detailed foreground and polarization analysis
- Same physics in maximum likelihood derivations, but need to fix algorithms for convergence (?)
- Can this improve constraints on e.g., cross-correlations, WDM, axion physics?

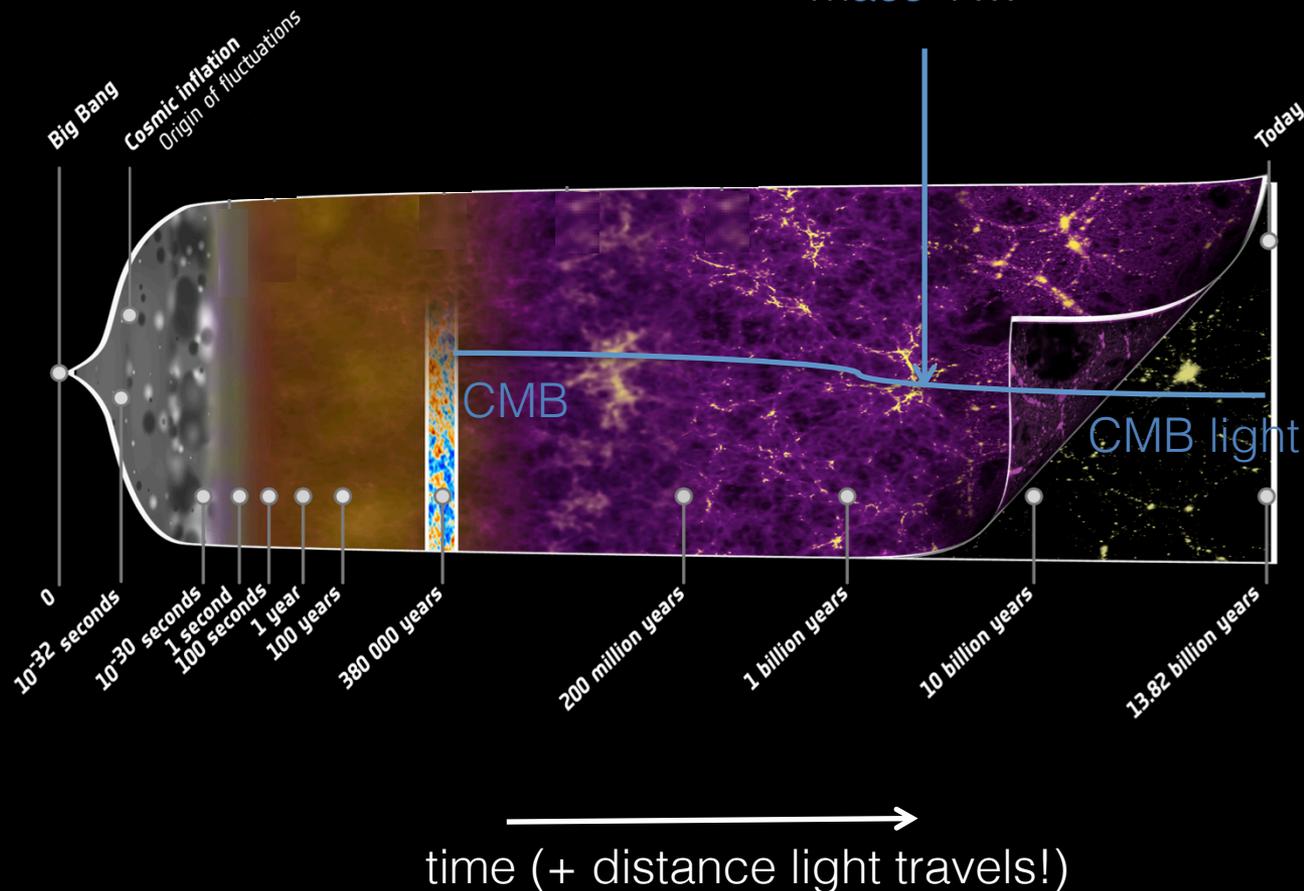
In progress!



# Recap

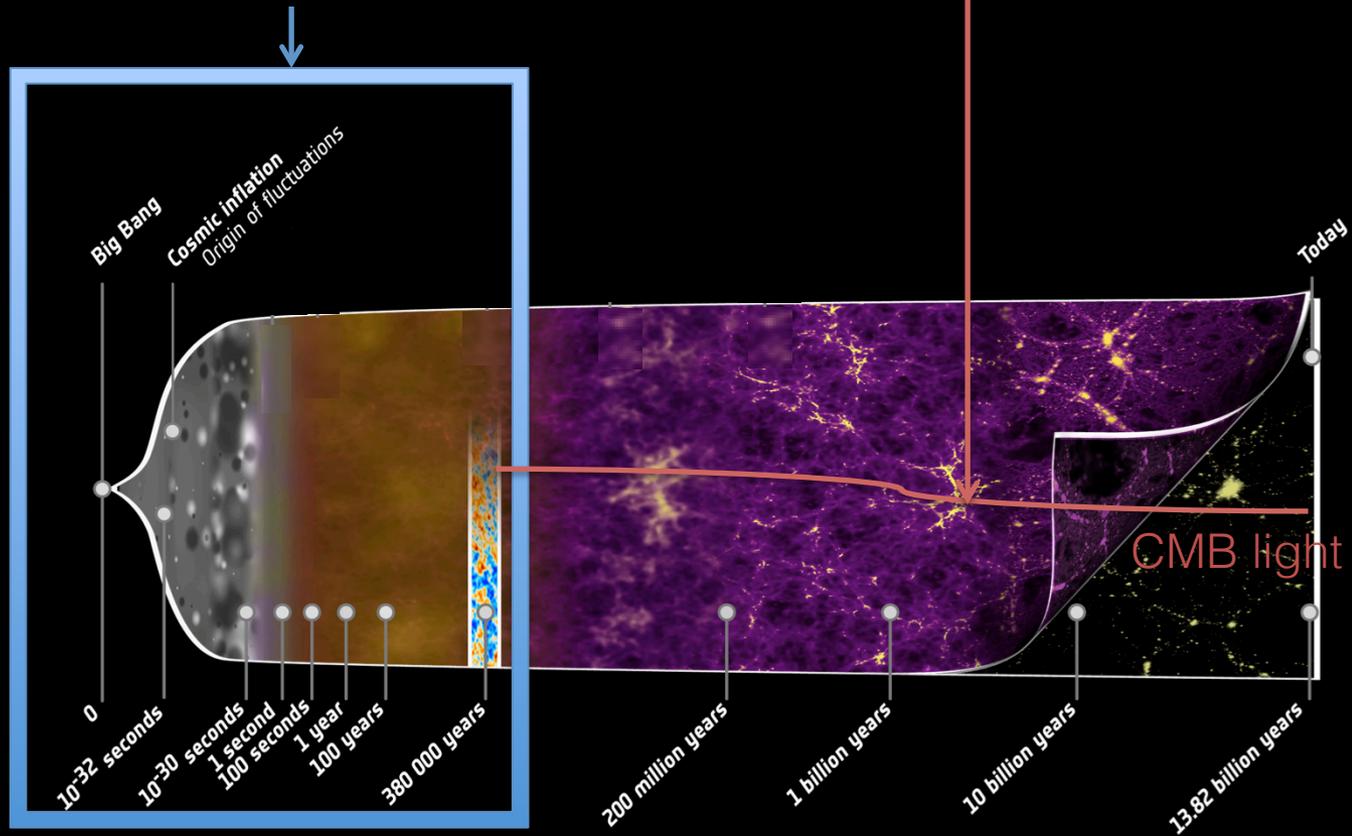
CMB Lensing dark matter map: a signal to study neutrinos,  
+ ...

Lensing of CMB lets us map  
dark matter to study neutrino  
mass + ...



# CMB Lensing as Noise for Early Universe Cosmology

But if we are interested in the early universe



time (+ distance light travels!)

# Outline

- Part 1: ACT and Simons Observatory: lensing and neutrino mass constraints
- Part 2: New approaches to small-scale CMB lensing - are our current estimators good enough?
- Part 3: Delensing Simons Observatory: new methods for revealing inflationary signals

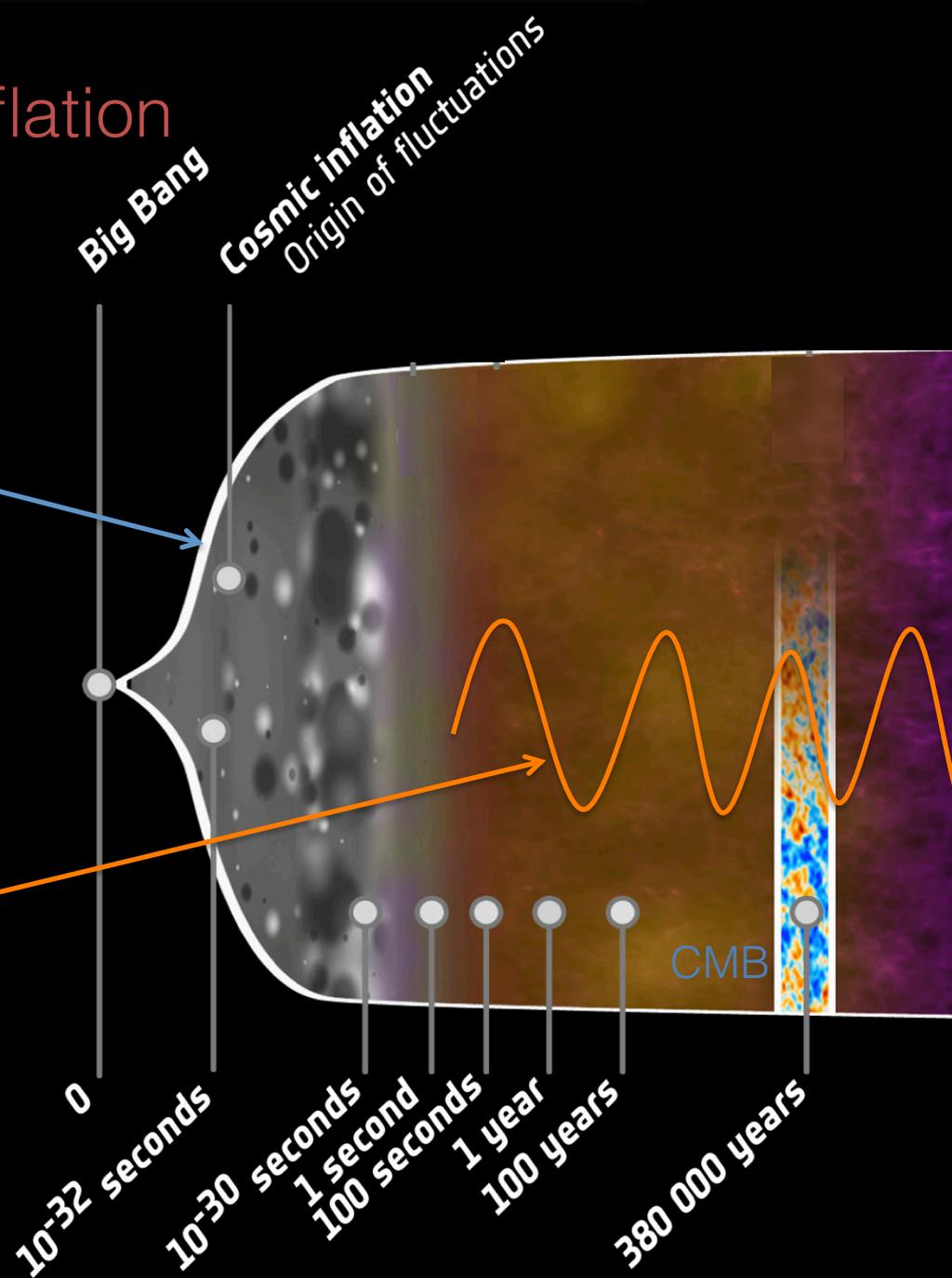


With Toshiya Namikawa, Anton Baleato, Byeonghee Yu, et al.

# Inflation

- Inflation: initial accelerated cosmic expansion.
- Good evidence for idea – but we don't know for sure
- Many (simple) models make **inflationary gravity waves\***

\*N.B. Some other models also produce GWs



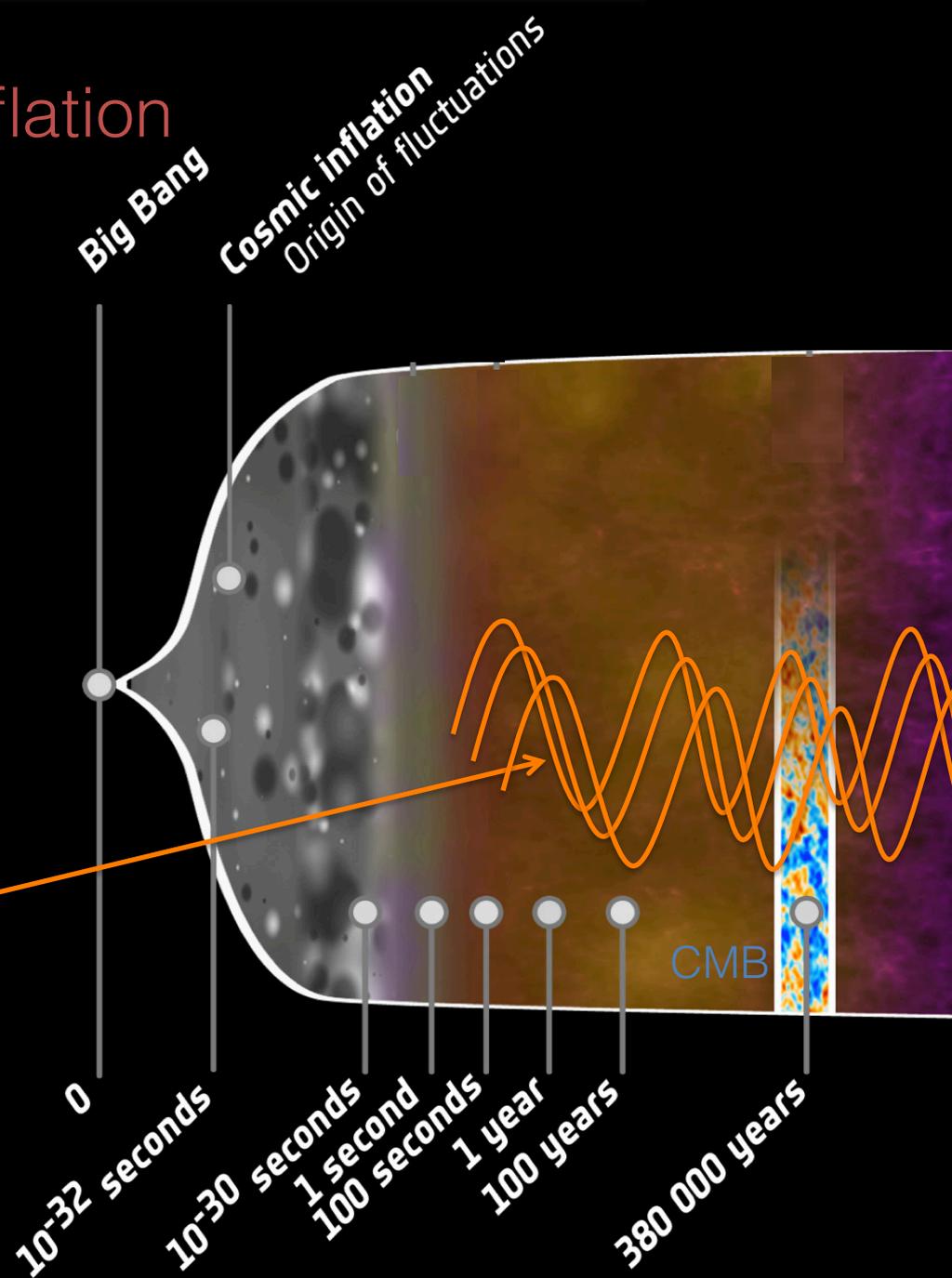
# Inflation

- Probe physics at ultra-high energy (at the doorstep of the Planck scale)

$$V^{1/4} = 1.04 \times 10^{16} \text{ GeV} \left( \frac{r_*}{0.01} \right)^{1/4}$$

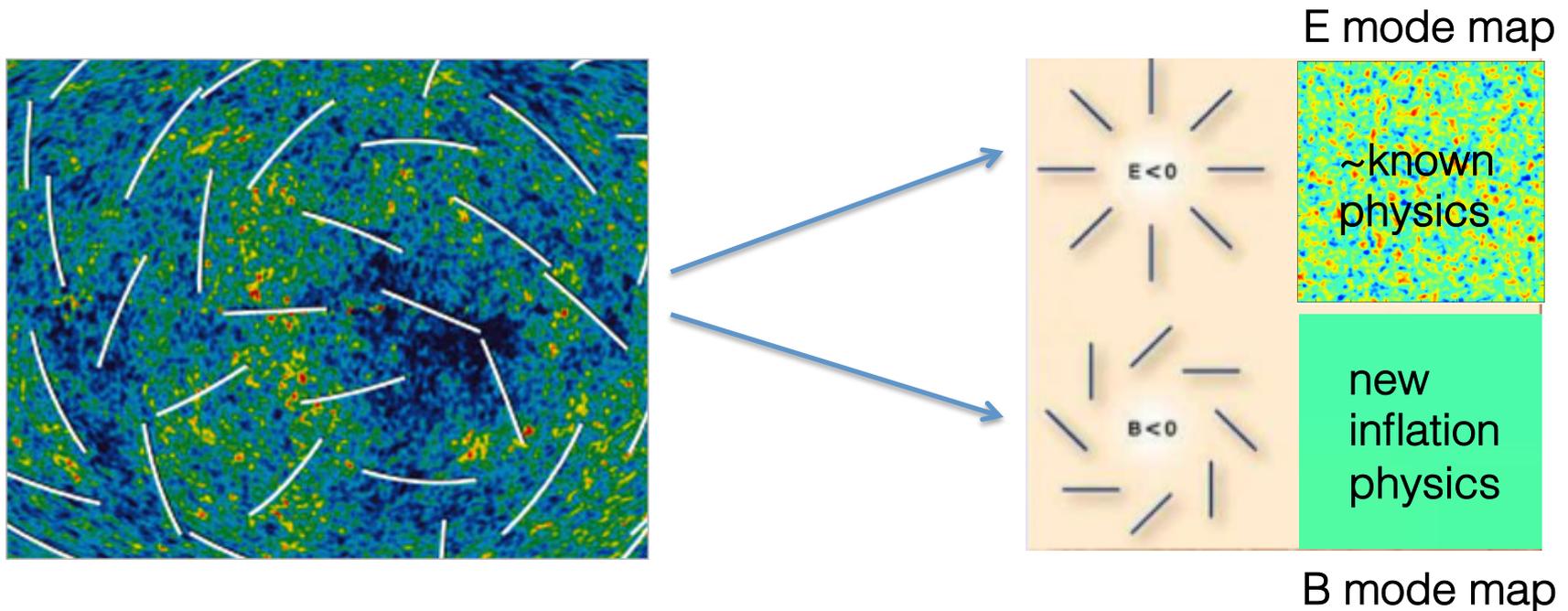
- The strength of the waves - tensor-to-scalar ratio  $r$  - tells us about the inflation energy scale, ...

- Leaves a characteristic polarization pattern in CMB polarization



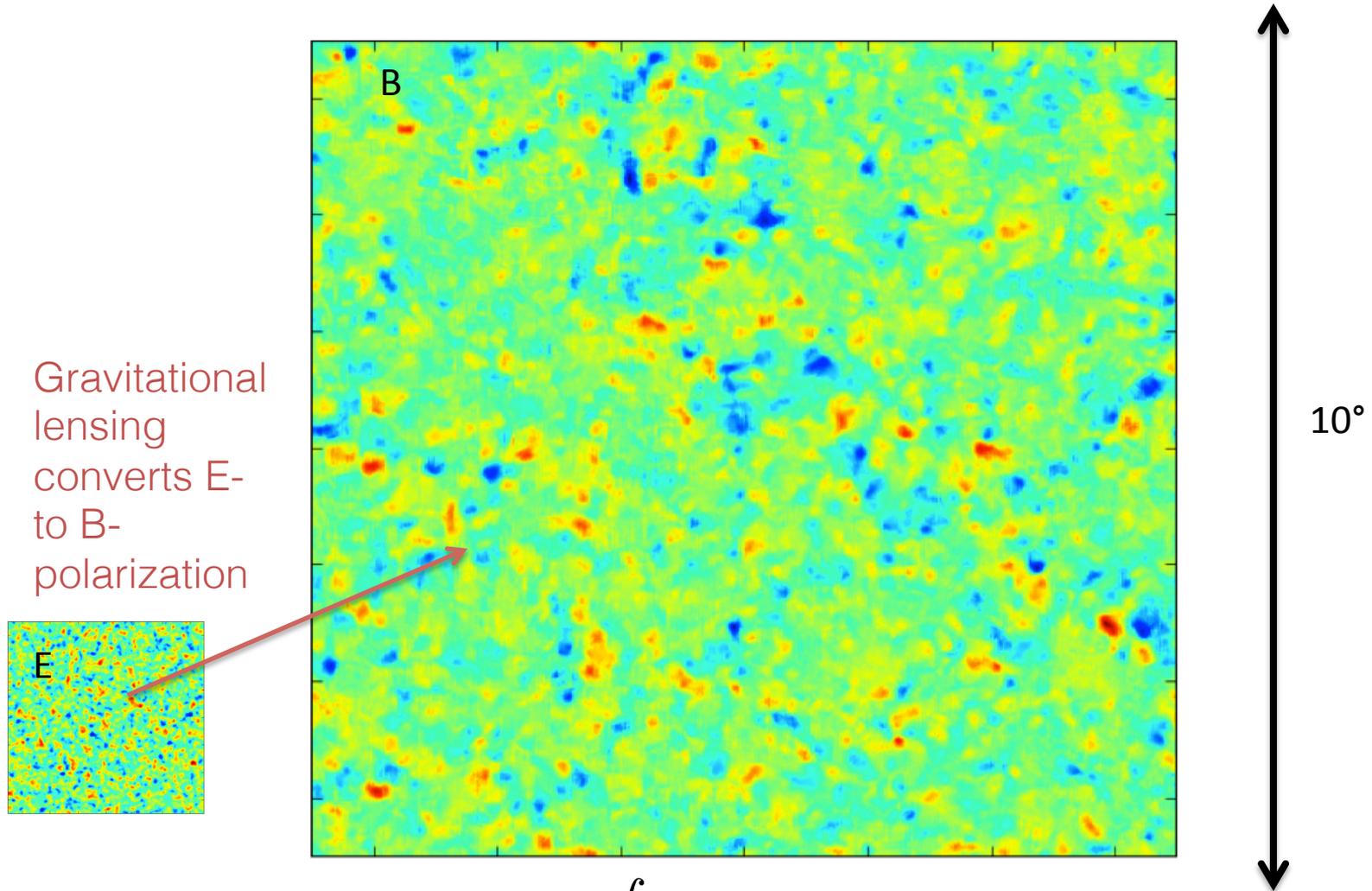
# CMB B-mode Polarization: Reminder

- Any polarization map can be decomposed into E and B mode fields
- B-mode: contains signals from inflation, if there



[Image credit: CMBPol]

# Problem for CMB B-mode Searches: Lensing B-Mode Polarization

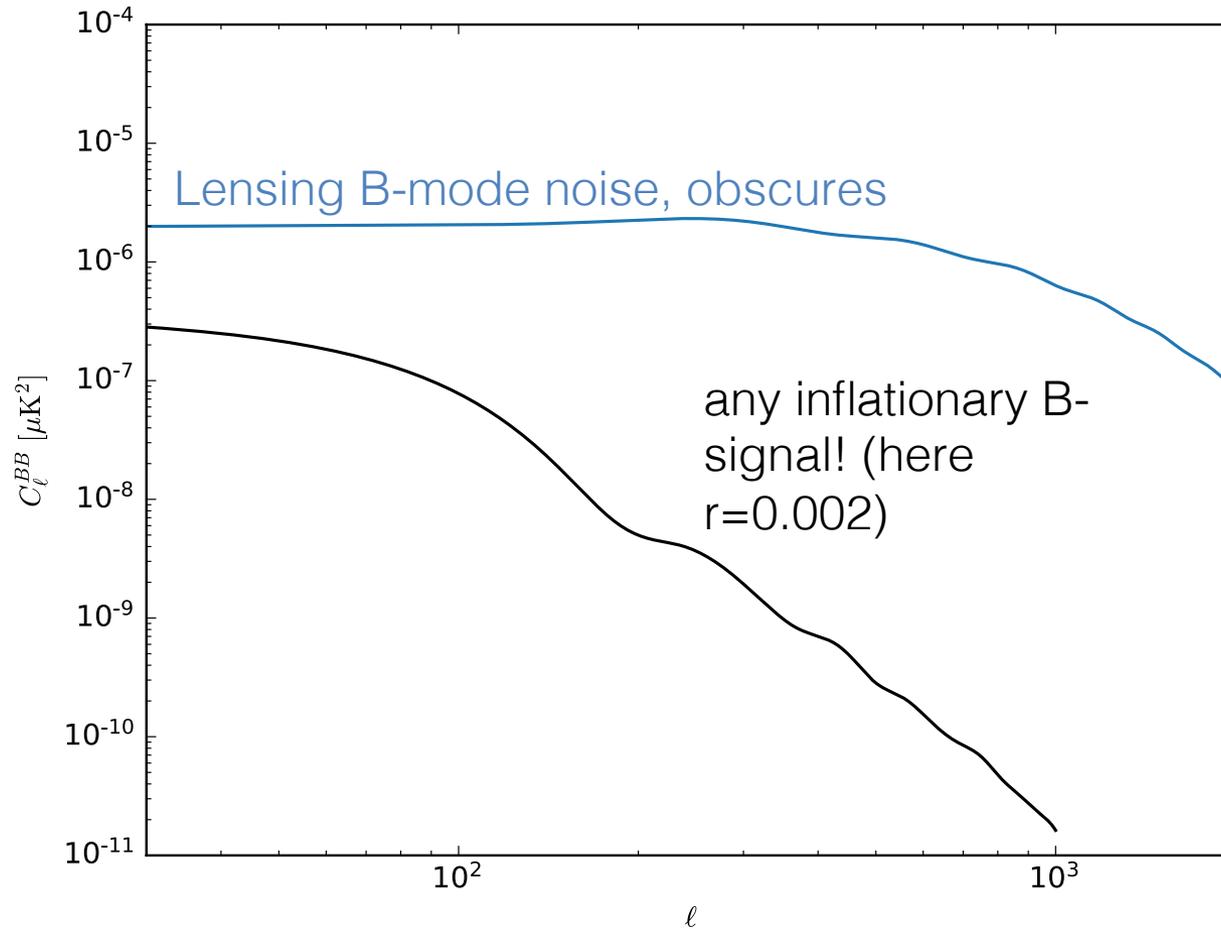


$$B^{lens}(\mathbf{L}) \sim \int d\mathbf{l} W(\mathbf{l}, \mathbf{L}) E(\mathbf{l}) d(\mathbf{L} - \mathbf{l})$$

W: geometric kernel

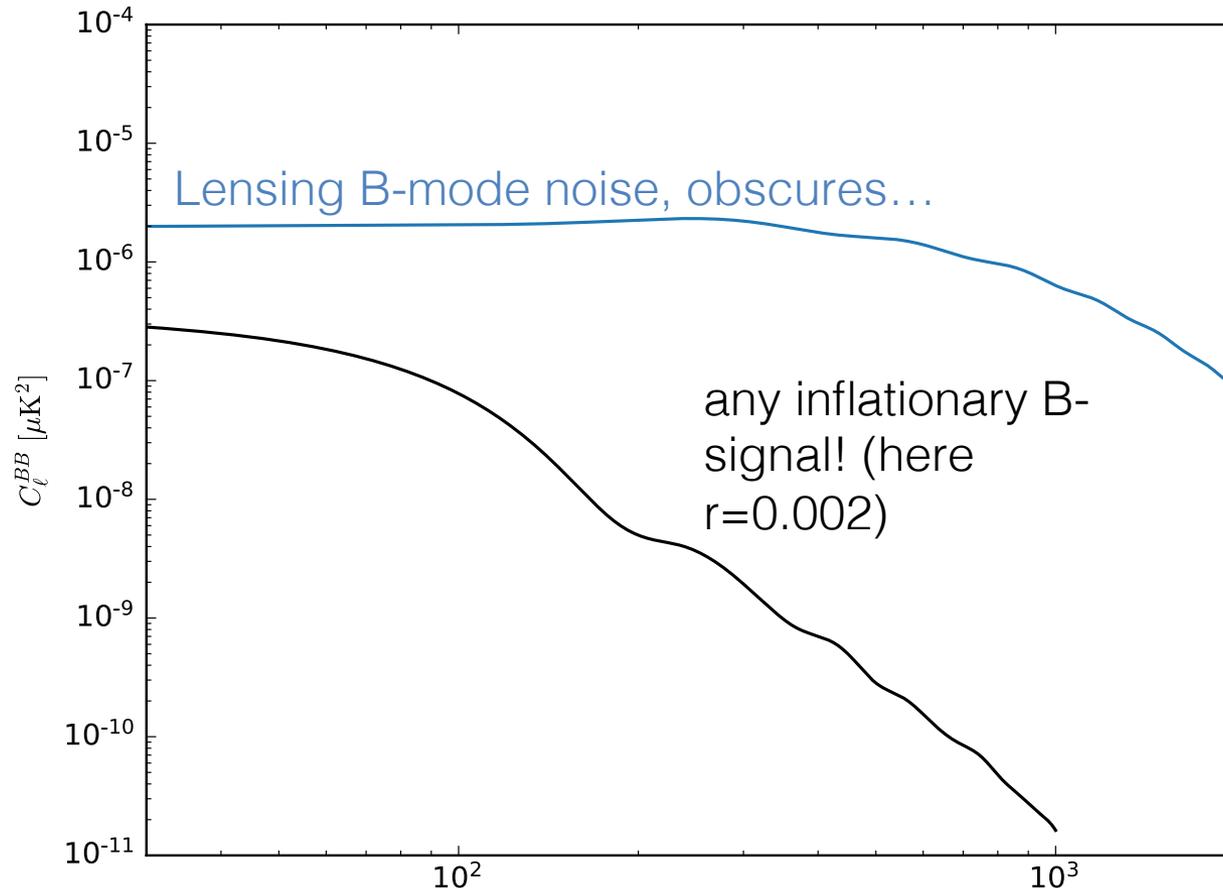
# Lensed CMB B-Polarization: Noise for Inflation-B

B-mode  
power



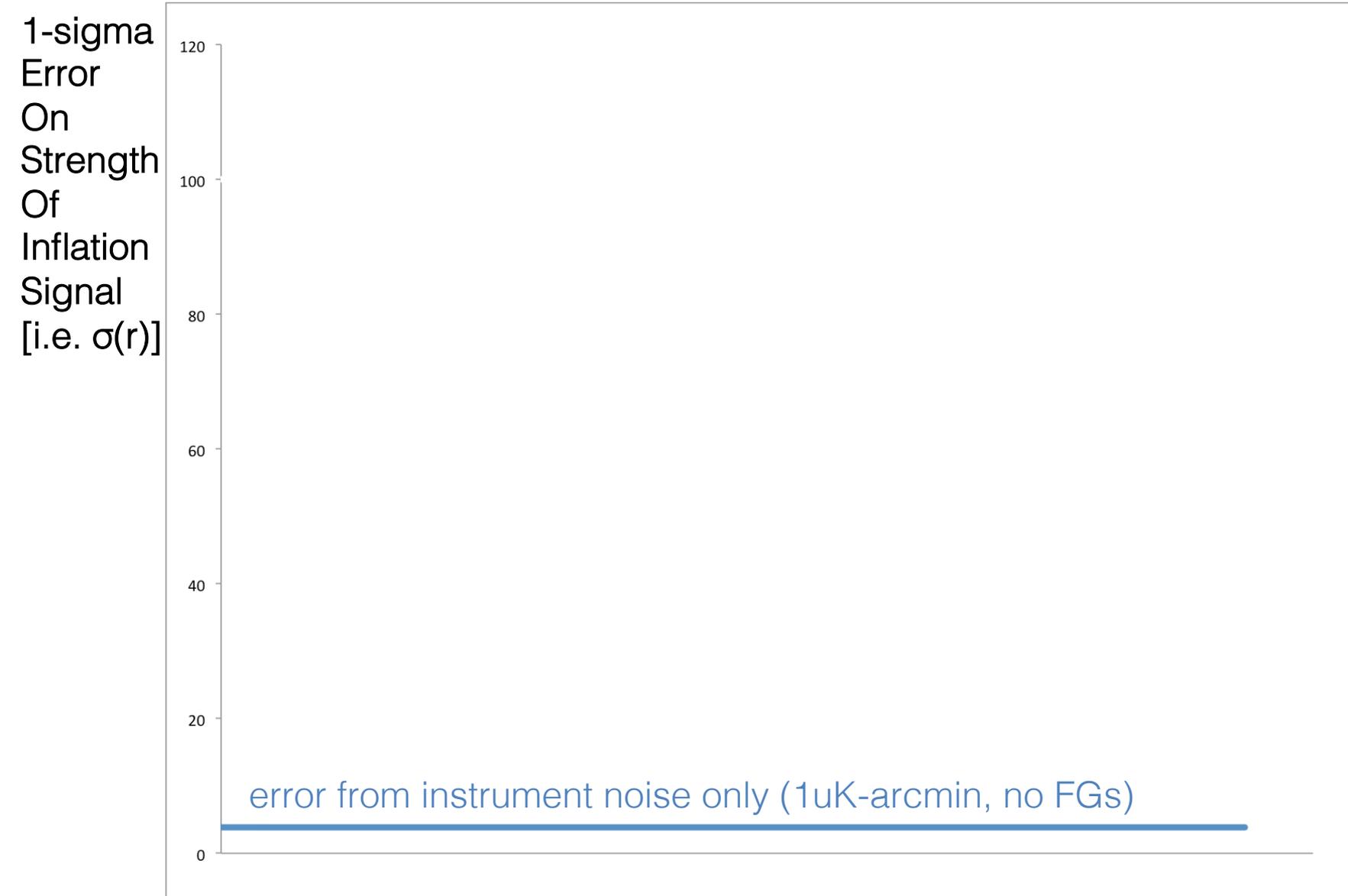
# Lensed CMB B-Polarization: Noise for Inflation-B

B-mode power



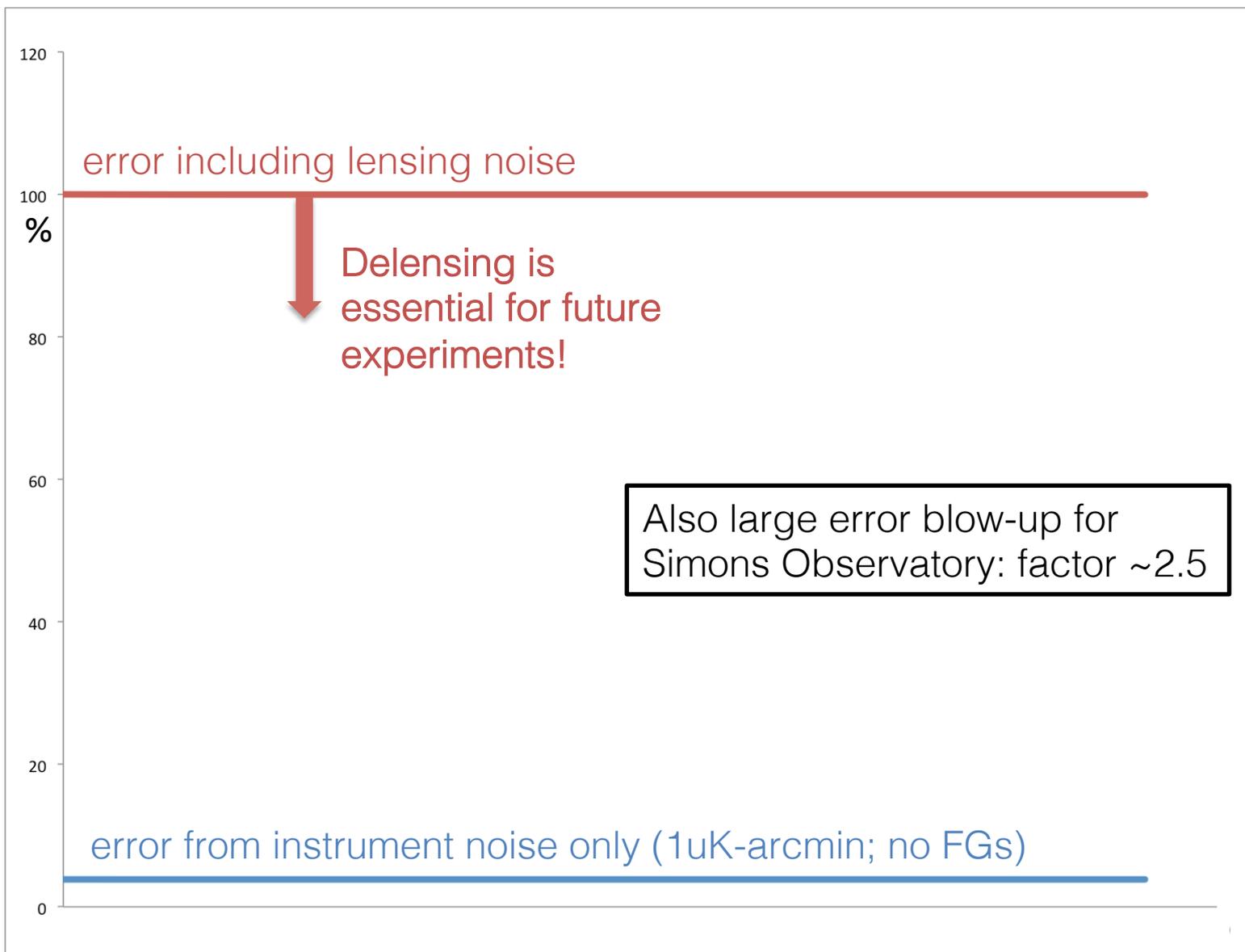
- Mean “problem”: must subtract  $\ell$  mean lensing power – unimportant!
- Error problem: lensing adds additional cosmic variance  
 $\sigma(r) \sim (N_l^{BB} + C_l^{BB, \text{lens}})$

# Error Inflation from Lensing Noise (Example: CMB-S4)

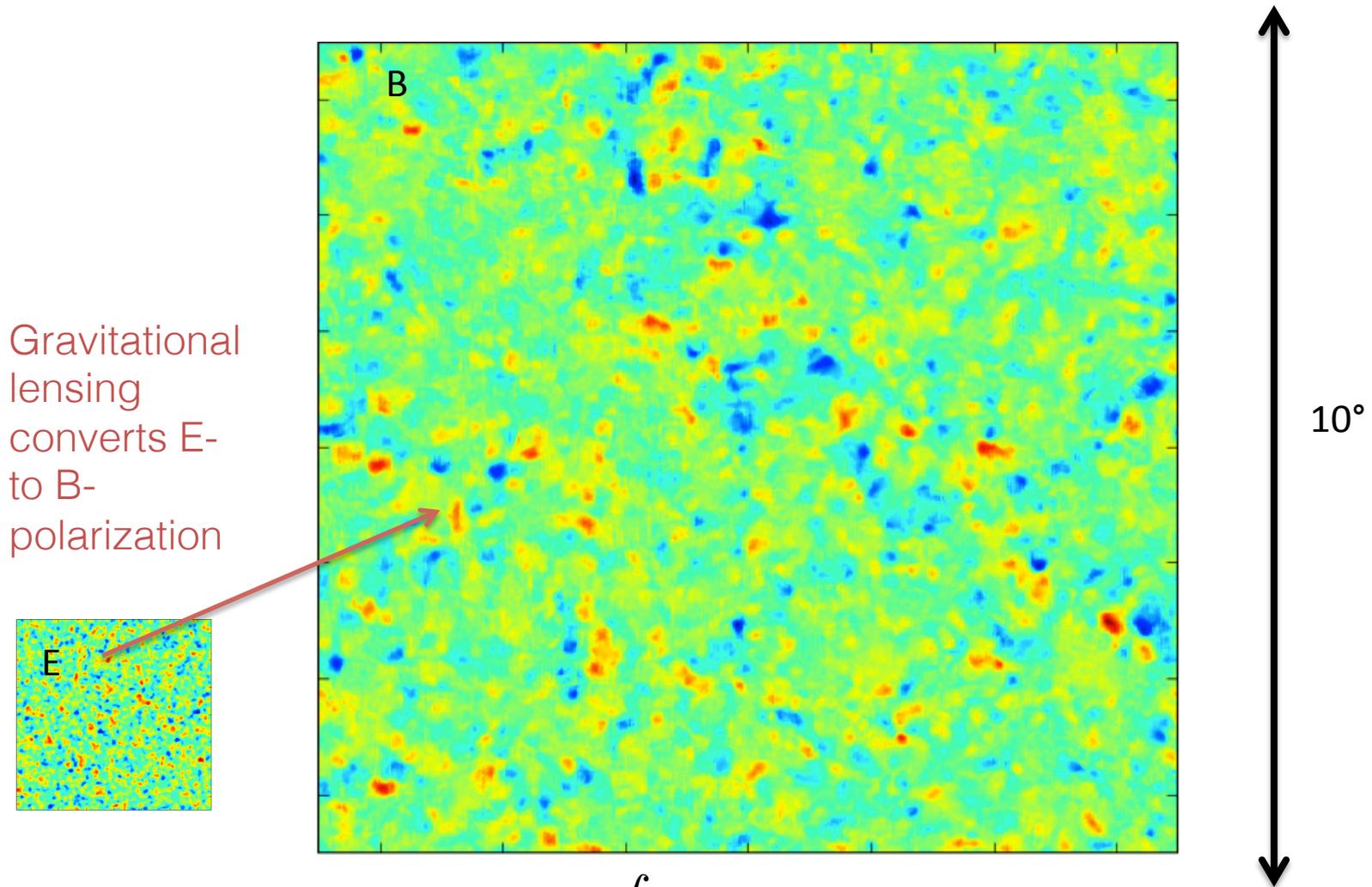


# Error Inflation from Lensing Noise (Example: CMB-S4)

1-sigma  
Error  
On  
Strength  
Of  
Inflation  
Signal  
[i.e.  $\sigma(r)$ ]

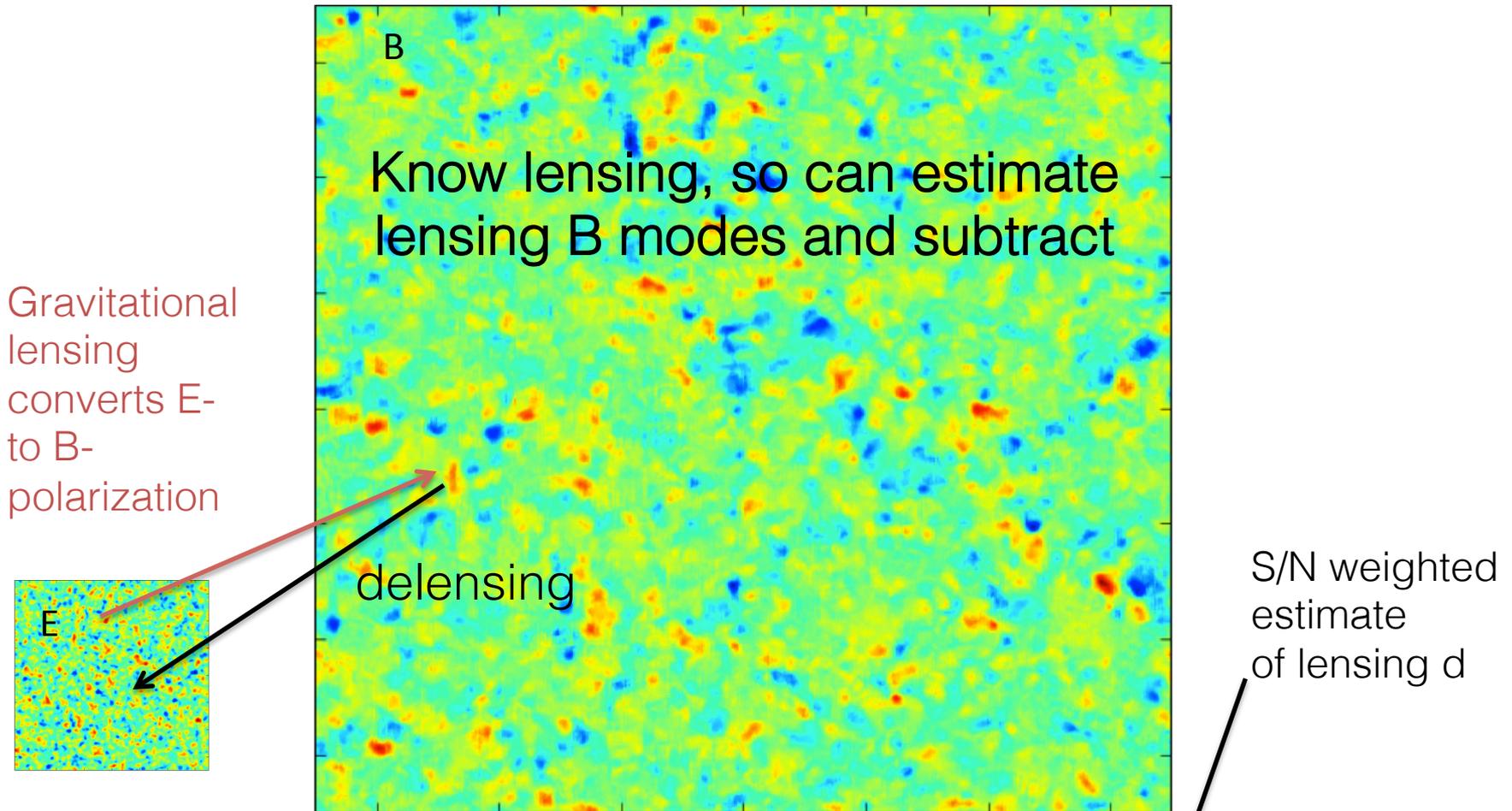


# Delensing the CMB: Lensing Removal



$$B^{lens}(\mathbf{L}) \sim \int d\mathbf{l} W(\mathbf{l}, \mathbf{L}) E(\mathbf{l}) d(\mathbf{L} - \mathbf{l})$$

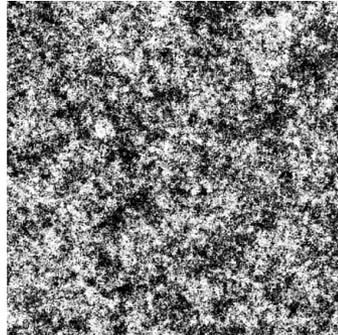
# Delensing the CMB: Lensing Removal



Linearized version:

$$B^{data} - \hat{B}^{lens} \sim B^{data} - \int d\mathbf{l} W(\mathbf{l}, \mathbf{L}) E(\mathbf{l}) \hat{d}^{filt}(\mathbf{L} - \mathbf{l})$$

# To Delens, Need To Measure Good Maps of CMB Lensing - How?



CMB lensing is a probe  
of the projected  
mass distribution

$$\nabla \cdot \mathbf{d} \sim \int dz W(z) \delta(z)$$

Standard “Internal” case:

1) Reconstruct lensing  $\hat{d}$  from  
changes in background CMB

# Delensing: Forecasting Performance

- Error reduction depends on residual lensing B-mode

$$\sigma(r) \sim \left\langle \frac{C_l^{BB,\text{lens}}}{C_l^{BB,\text{res}}} + N_l^{BB} \right\rangle_{l < 100}$$

- Find that delensing reduces B-mode power by a factor  $\sim (1 - \rho^2)$

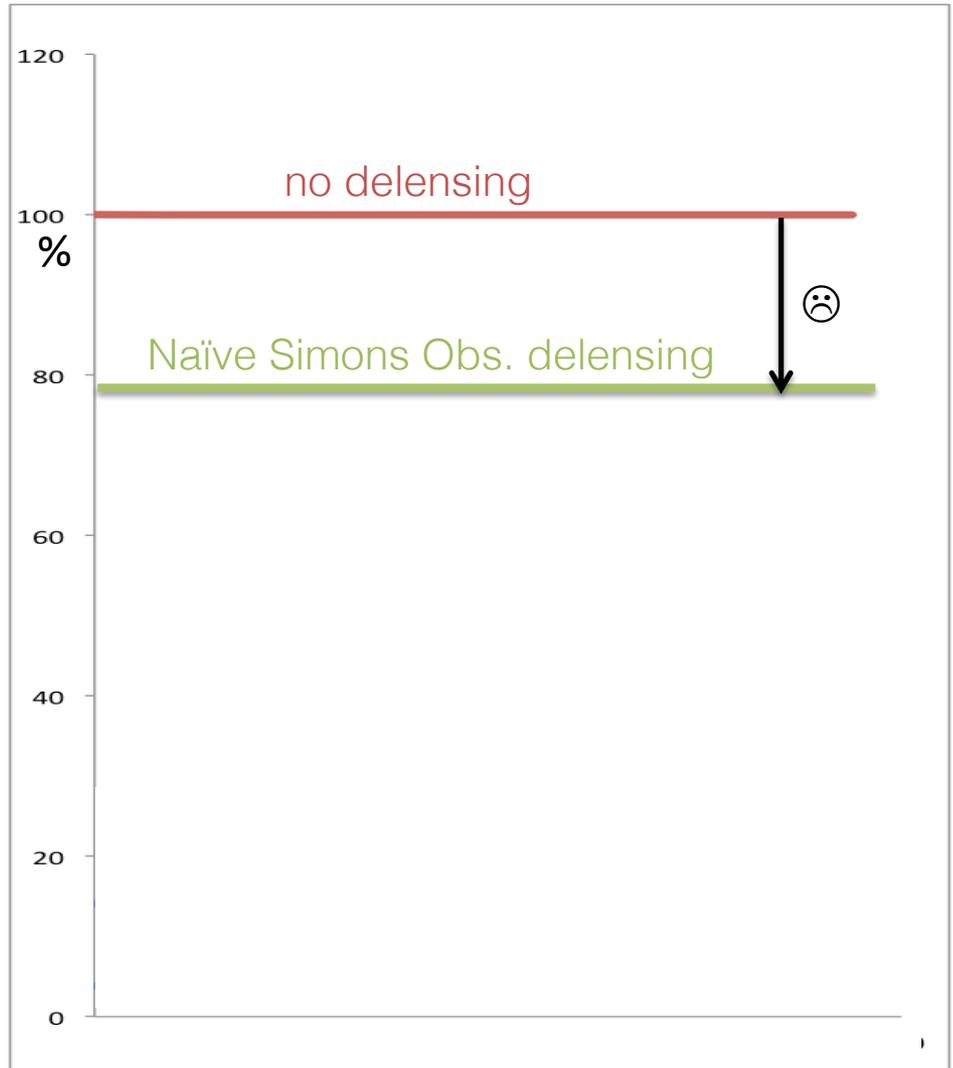
$$\rho_l^2 = \frac{(C_l^{\hat{d}d})^2}{C_l^{dd} C_l^{\hat{d}\hat{d}}}$$

[  $\rho$  : correlation coefficient of lensing estimate  $\hat{d}$  with true lensing  $d$  ]

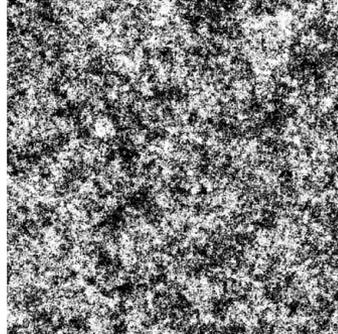
# Delensing for Simons Observatory (SO)

- SO is significantly limited by lensing B-modes
- Problem: SO lensing reconstruction, while powerful, is still too noisy to allow large improvements from internal delensing
- Only ~20 % improvement expected internally

1-sigma  
Error  
On  
Strength  
Of  
Inflation  
Signal  
[i.e.  $\sigma(r)$ ]



# To Delens Simons Observatory, Need To Measure Good Maps of CMB Lensing - How?



CMB lensing is a probe of the projected mass distribution

$$\nabla \cdot \mathbf{d} \sim \int dz W(z) \delta(z)$$

1) Reconstruct lensing from changes in background CMB

2) Estimate lensing from Large Scale Structure tracers of lensing, e.g. **CIB, galaxies**. Can show:

CIB-lensing cross

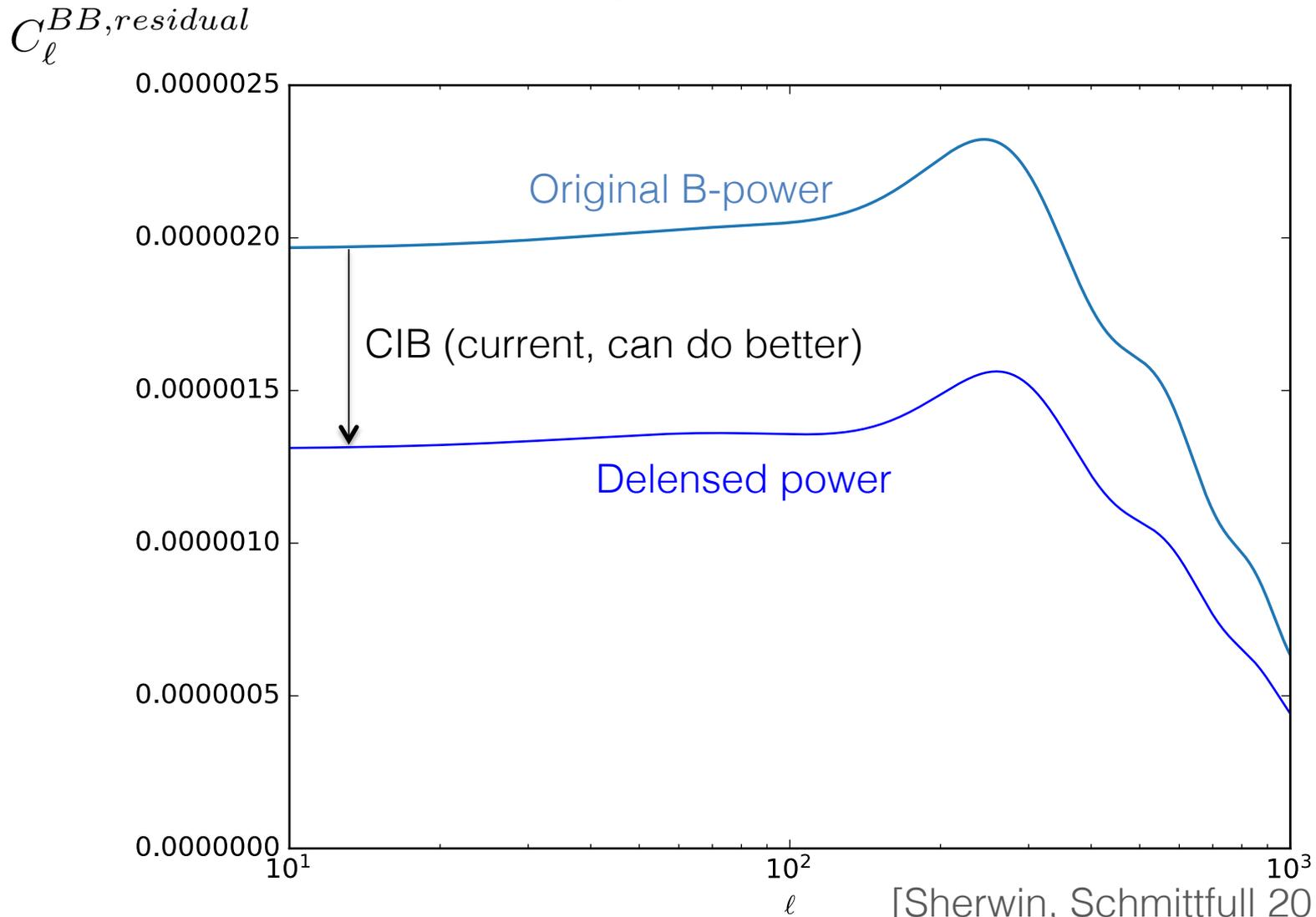
$$\hat{d}^I(\mathbf{l}) = \frac{C_l^{dI}}{C_l^{dd}} \times I(\mathbf{l})$$

CIB map

[Sherwin, Schmittfull 2015]

Lensing power

# CIB Delensing for Simons Observatory

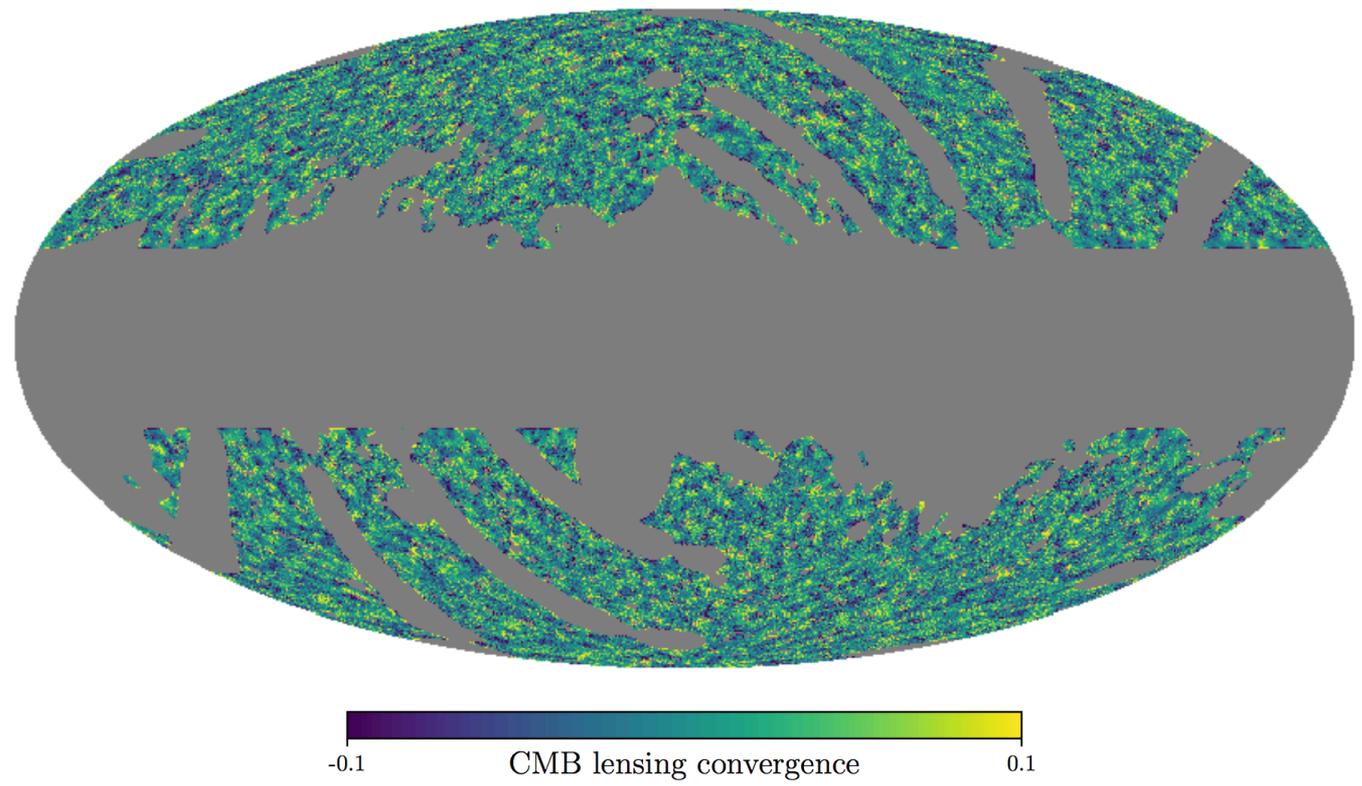


Use maps of cosmic infrared background (CIB), scaled by  $C_l^{dI} / C_l^{dd}$ , to infer and remove the lensing (used by SPT/BICEP now)

# Multi-tracer Delensing for Simons Observatory

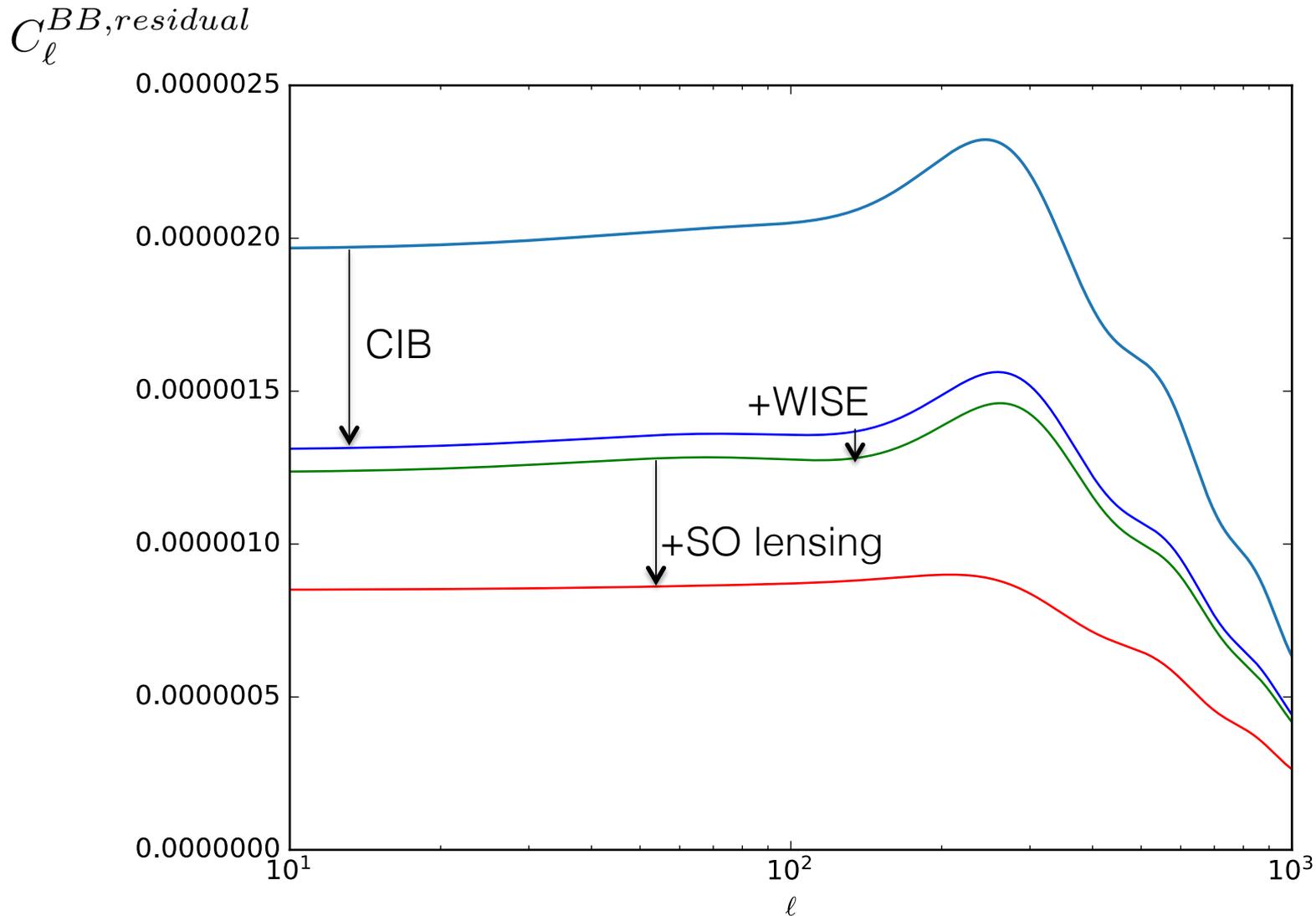
- Can co-add SO lensing map with different large scale structure tracers to delens [Yu, Hill, Sherwin 2017]

Example delensing map made from coadd of Planck lensing + CIB + WISE galaxies



- “Multitracer” delensing can greatly improve delensing performance: now coadd SO lensing + DES/LSST + CIB + ...

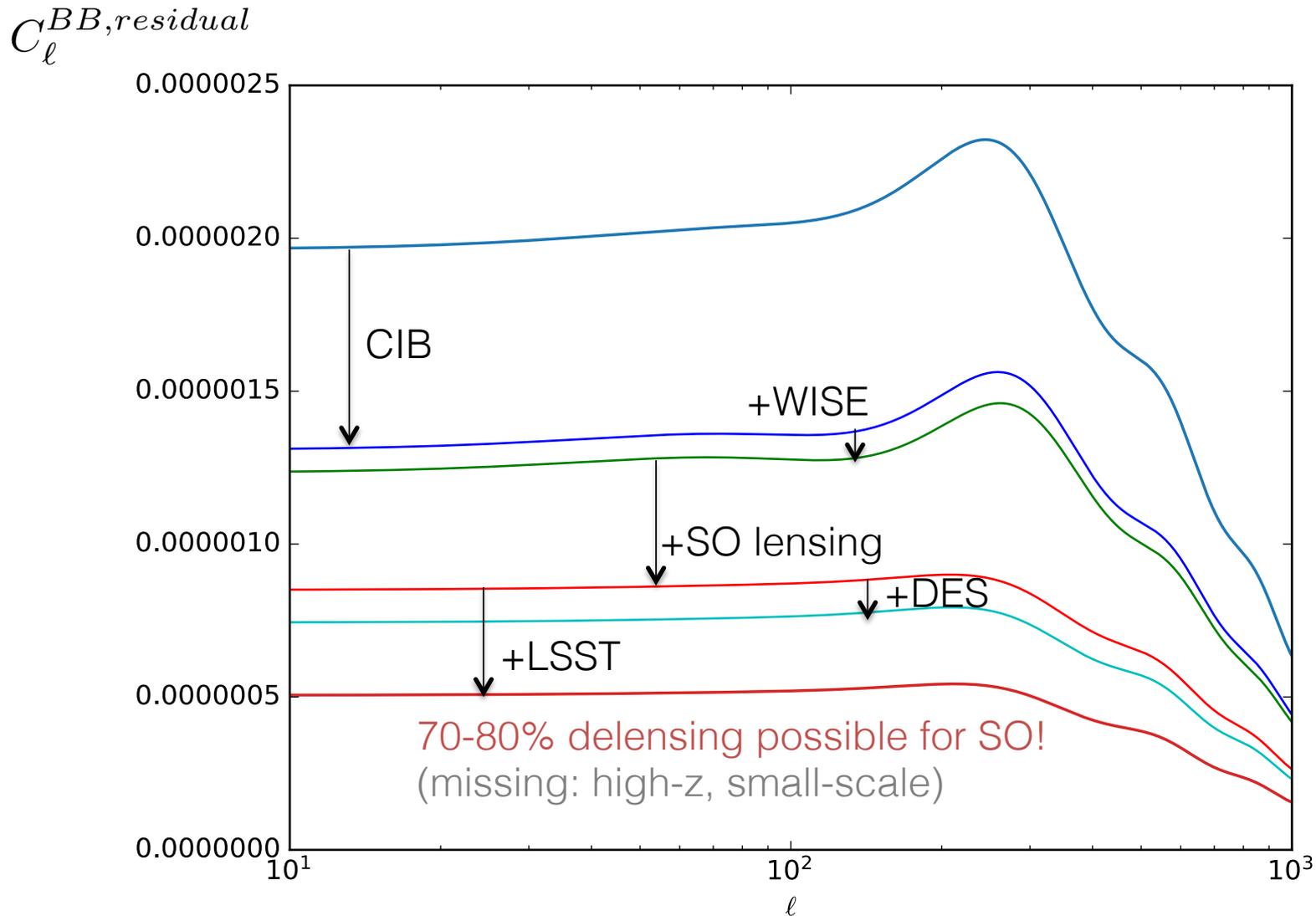
# Multi-tracer Delensing for Simons Observatory



$$I(\mathbf{l}) = \sum c_i(\mathbf{l}) I_i(\mathbf{l})$$

$$c_i = (C_l^{I_i I_j})^{-1} C_l^{d I_j}$$

# Multi-tracer Delensing for Simons Observatory



$$I(\mathbf{l}) = \sum c_i(\mathbf{l}) I_i(\mathbf{l})$$

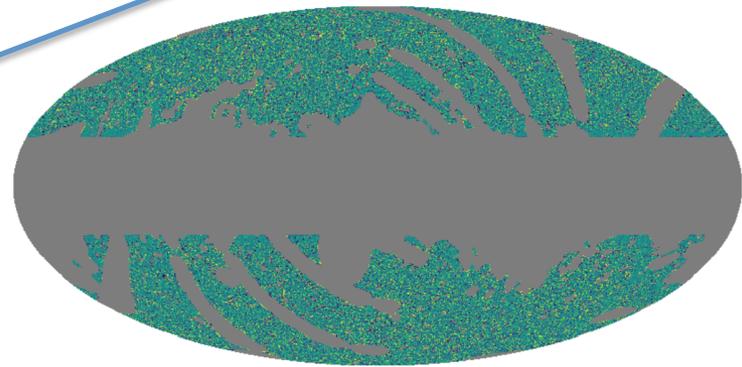
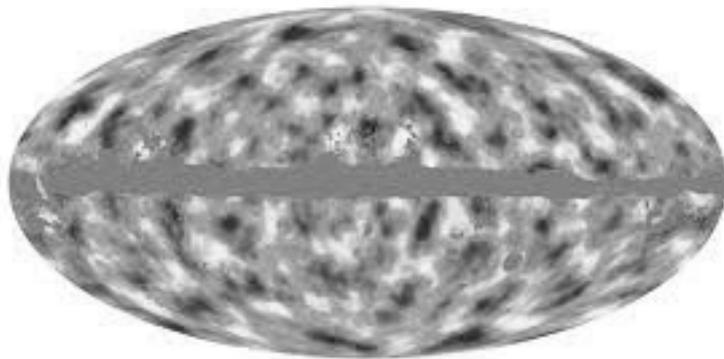
$$c_i = (C_l^{I_i I_j})^{-1} C_l^{d I_j}$$

# Why I think this will work I: LSS modeling required?

- Tracer calibration and delensing residual depend only on measurable spectra

$$I(\mathbf{l}) = \sum c_i(\mathbf{l}) I_i(\mathbf{l})$$

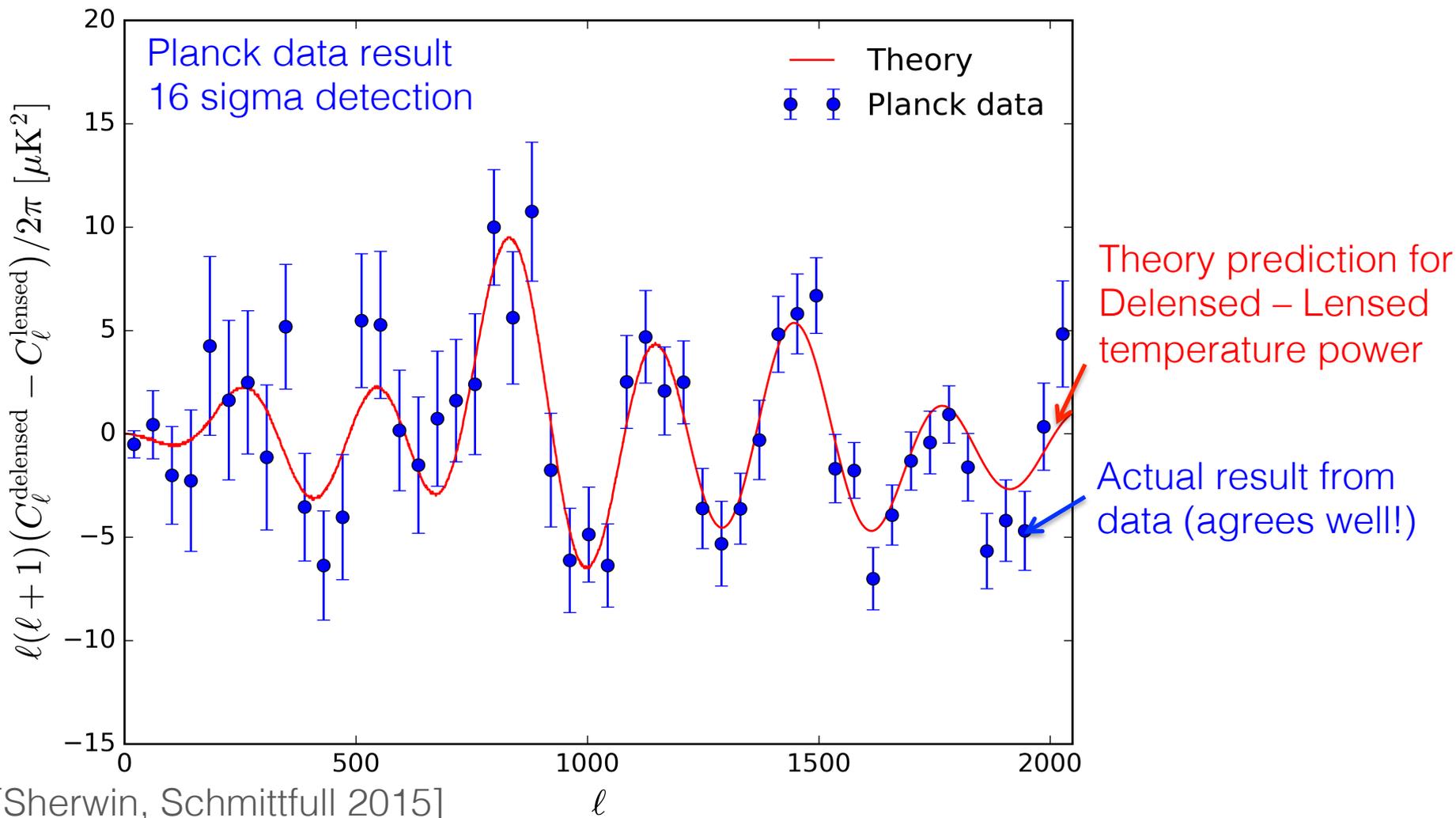
$$c_i = (C_l^{I_i I_j})^{-1} C_l^{d I_j}$$



Noisy-ish lensing map (low S/N per mode)    High S/N but mis-scaled LSS map

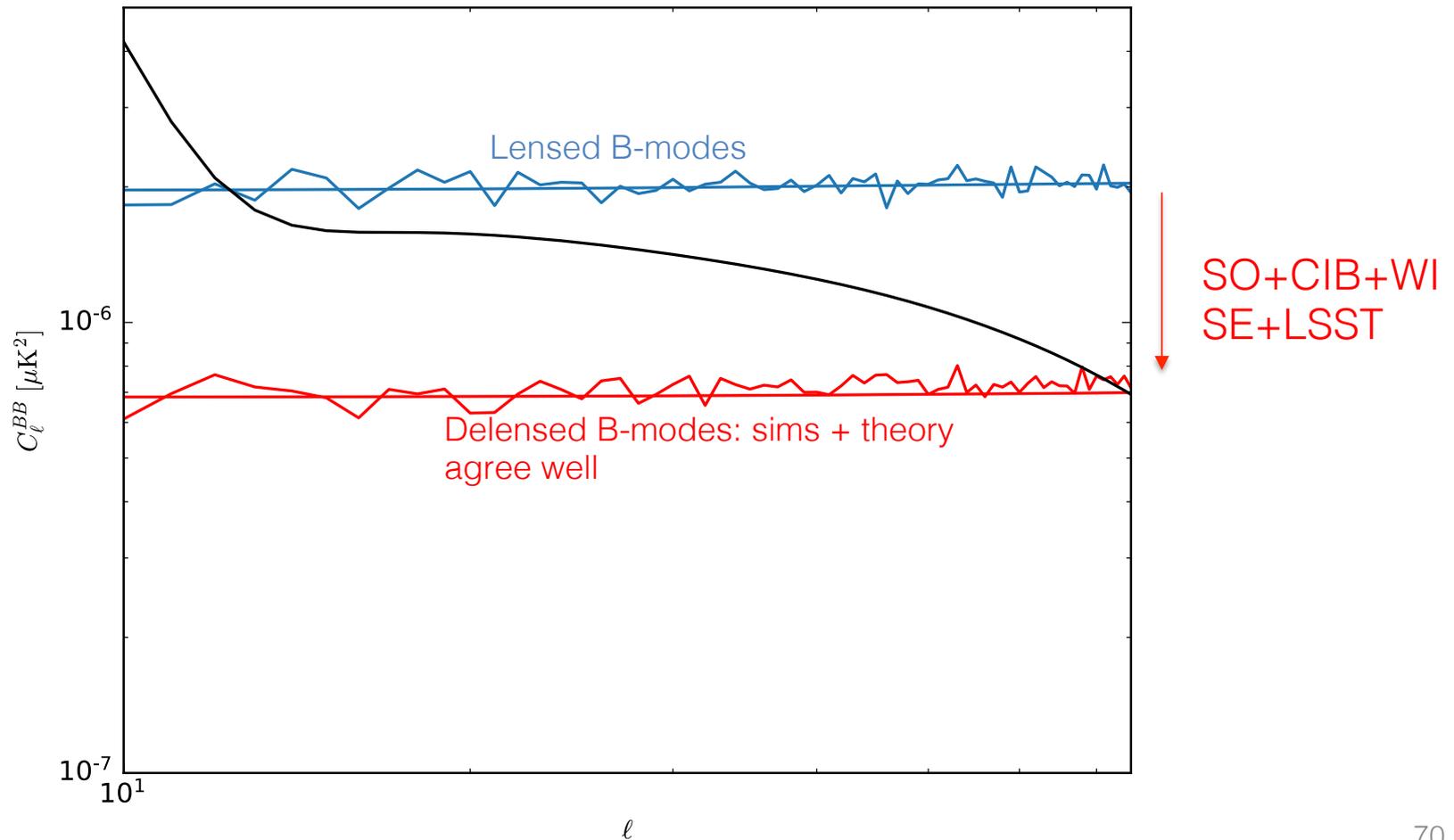
- Cross-spectra (assuming isotropy) can have high S/N -> can calibrate low noise LSS map, **modeling often not needed!**

# Why I think this will work II: Data demonstration of CIB delensing (of Temp.)

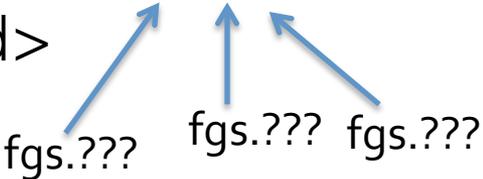


# Why I think this will work III: New SO delensing pipeline applied to simulations

- Polarization simulation: multitracer delensing demonstration with SO (preliminary)



## Why this might not work: Correlated foreground propagation,...

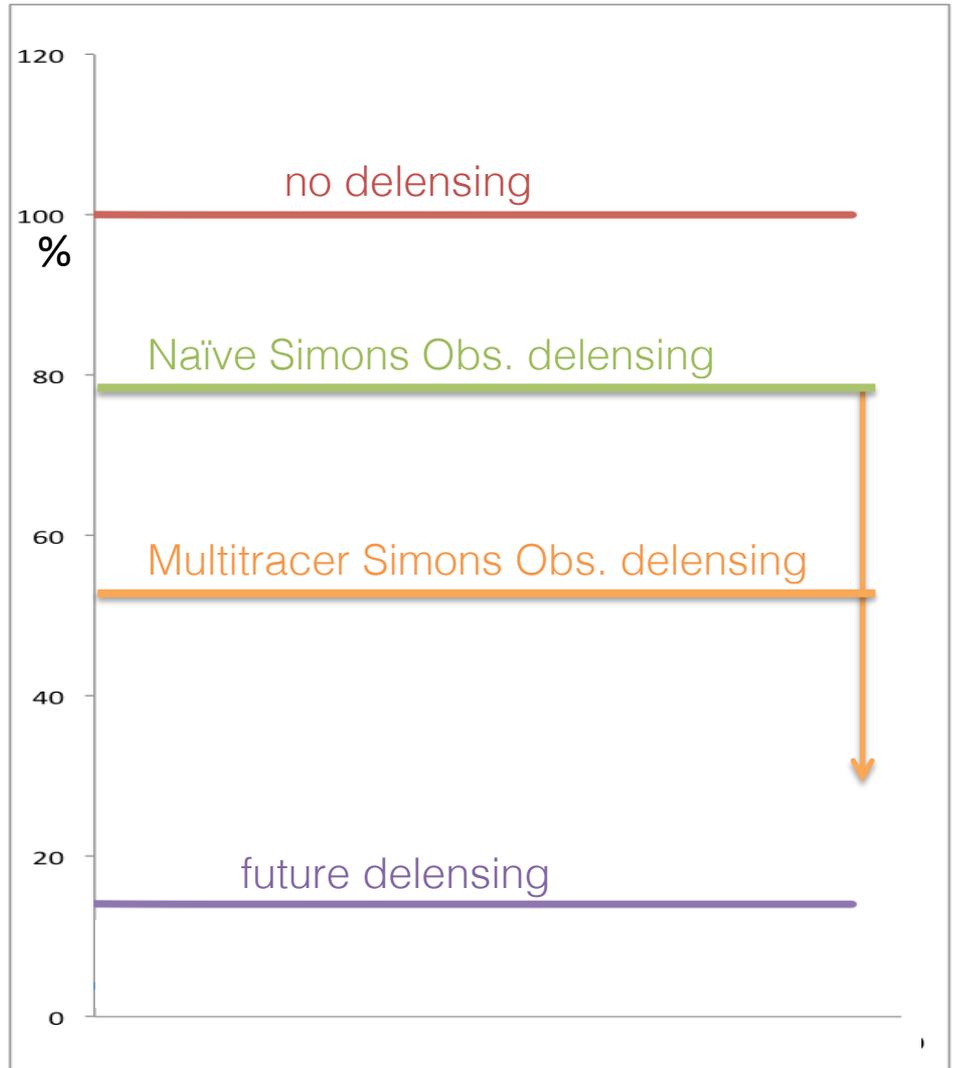
- Lensing foregrounds correlated with B foregrounds can give biases, e.g.,  $\langle (B-Ed) \times (B-Ed) \rangle$ , cross terms involving  $\langle BEd \rangle$   


fgs.???
- Foregrounds in B, E, and d all could matter. Investigation in progress (with A. Baleato, A. Challinor)
- Other challenges: likelihood, integration with foreground cleaning,...

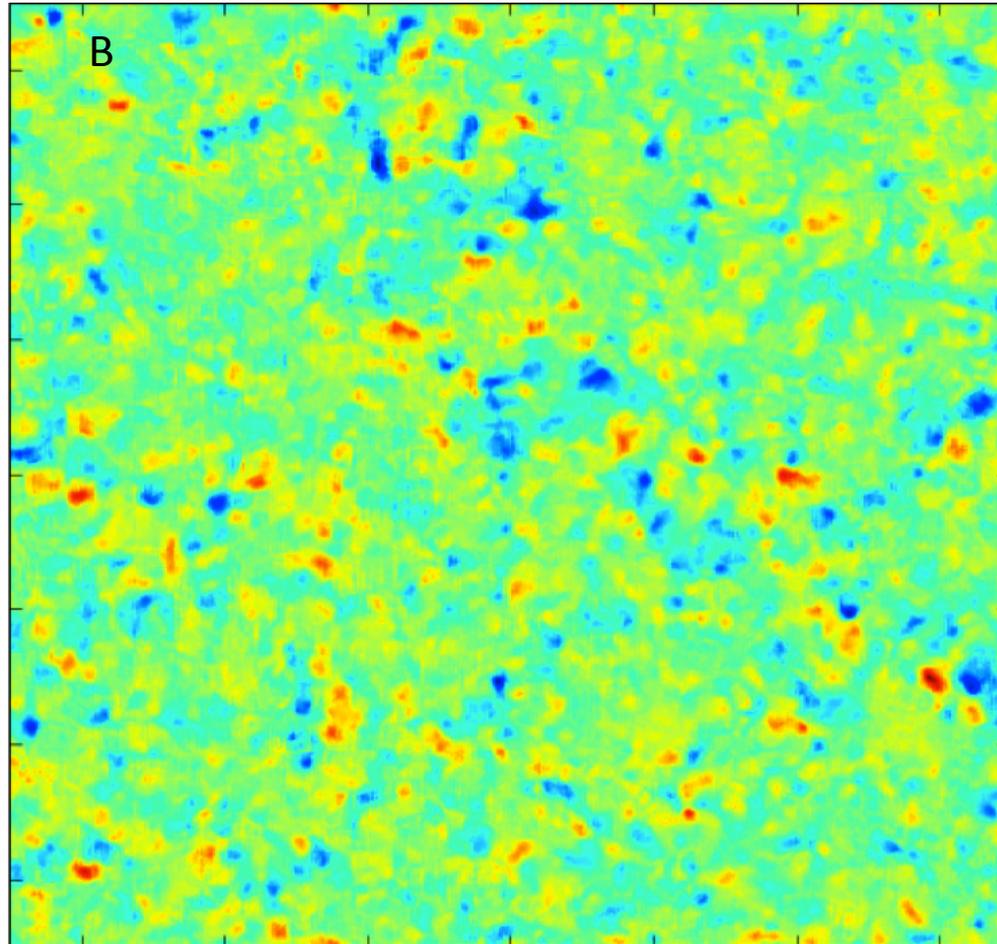
# Significant improvements possible for SO!

- Although lots to figure out:
- Significant improvements appear possible with multitracer delensing methods,  $\sim 2x$  improvement in SO  $r$  constraints [preliminary]
- Expected final results  $\sigma(r) \sim 0.002$  instead of 0.004 with delensing

1-sigma  
Error  
On  
Strength  
Of  
Inflation  
Signal  
[i.e.  $\sigma(r)$ ]

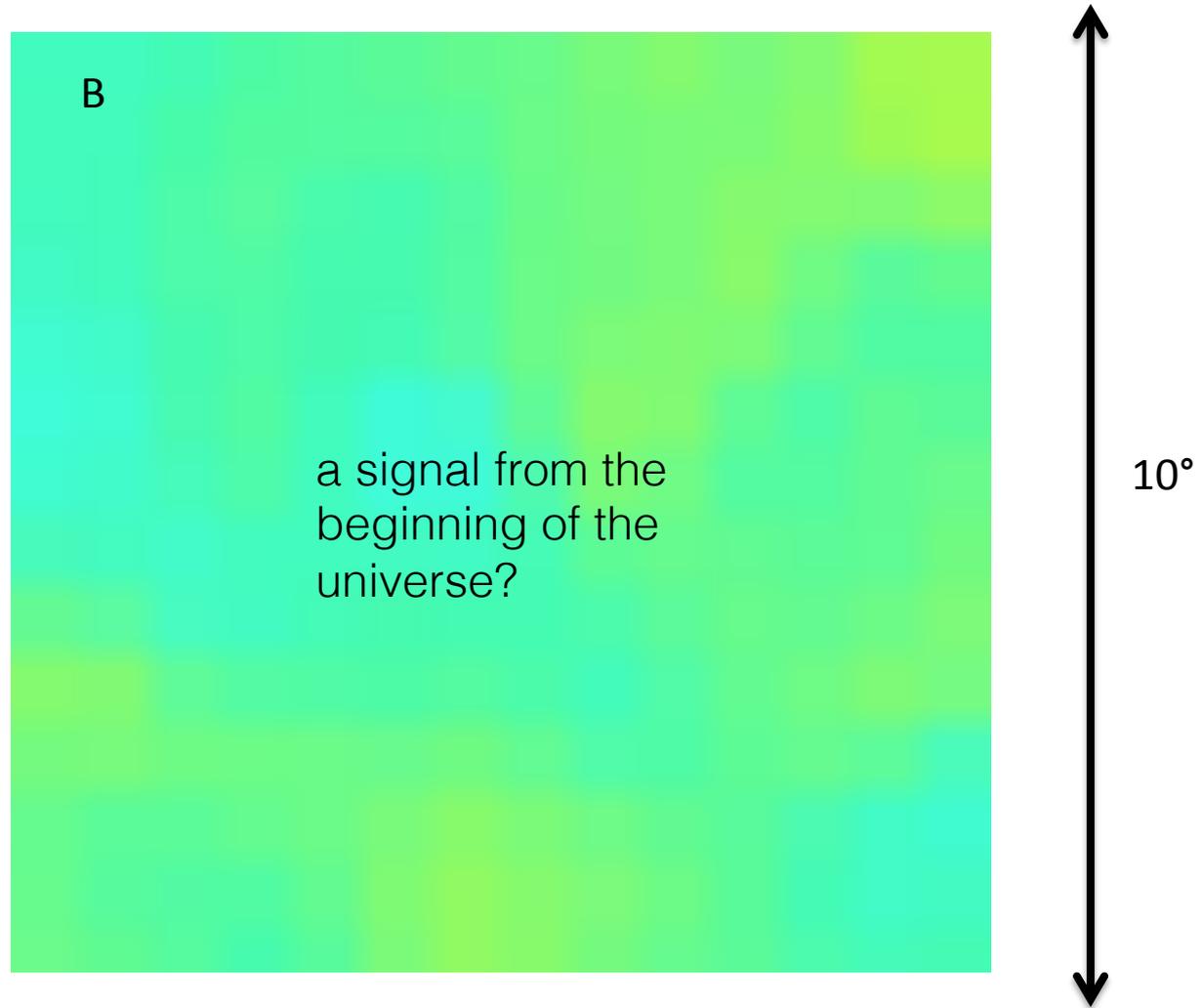


# Future B Mode Map – Lensing-Dominated



↑  
10°  
↓

# Delensed B Map – Inflation Signal?



# Summary

- CMB lensing has rapidly progressed. With AdvACT / Simons Observatory / CMB-S4 we will have lots more data and lensing science: neutrino masses, S8,...
- New opportunities with new data: novel small scale gradient inversion reconstruction
- +new multi-tracer delensing methods that could nearly double SO performance

