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Ultra-high-Resolution, Label-Free Hyperlens Imaging in the Mid-IR

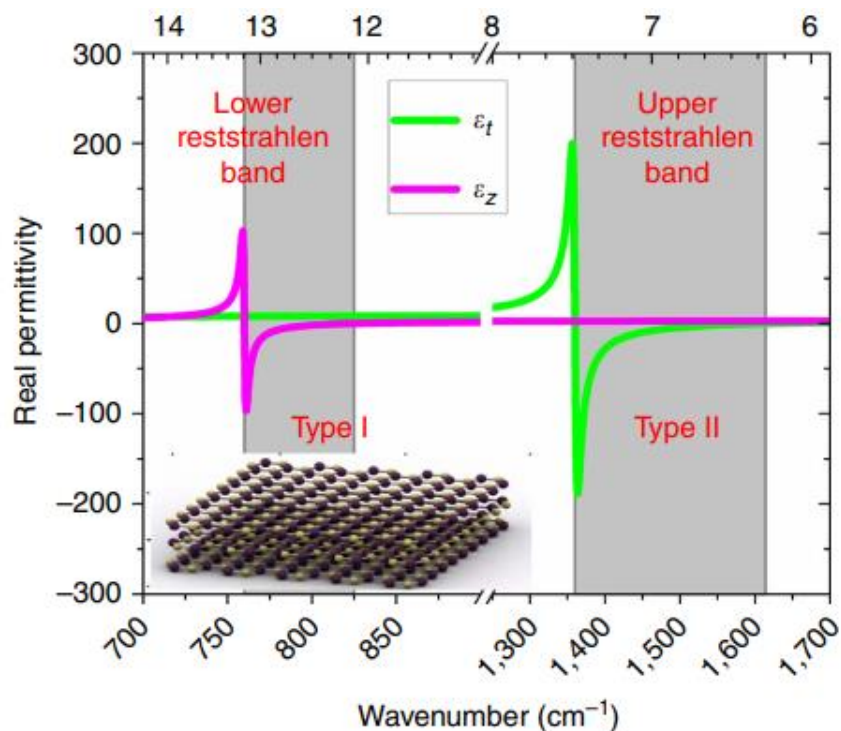
Mingze He: mingze.he@vanderbilt.edu, Ganjigunte R. S. Iyer, Shaurya Aarav

Prof. Joshua Caldwell's group, Vanderbilt University, USA

Josh.Caldwell@vanderbilt.edu



Hyperbolic phonon polaritons

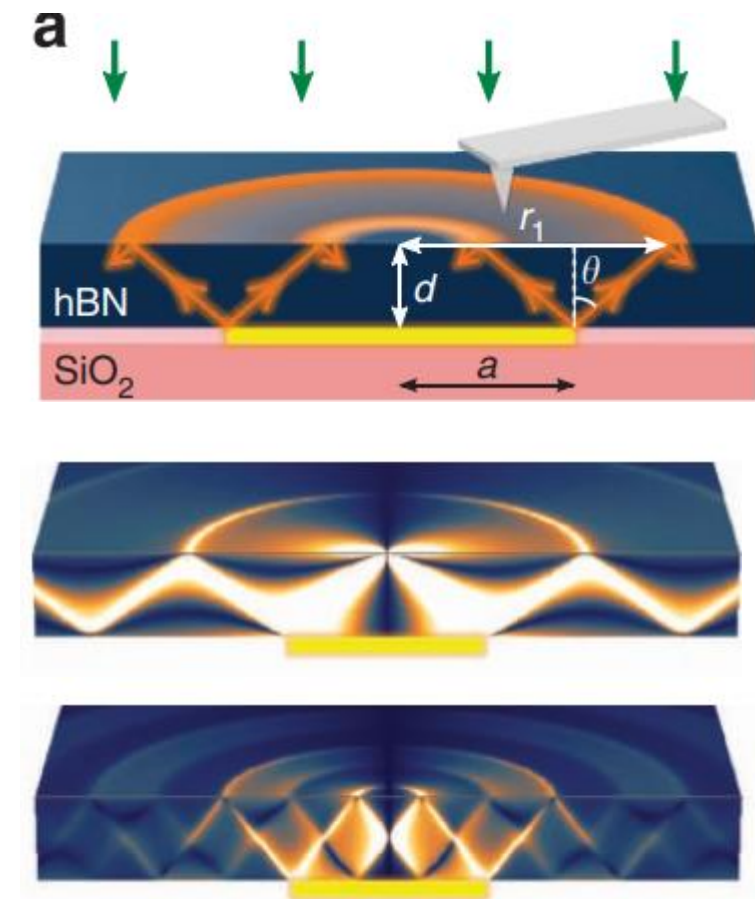


$$\frac{k_z^2}{\epsilon_t(\omega)} + \frac{k_t^2}{\epsilon_z(\omega)} = 0, \quad \frac{\omega}{c} \ll k_t, k_z \ll \frac{1}{a}. \quad (1)$$

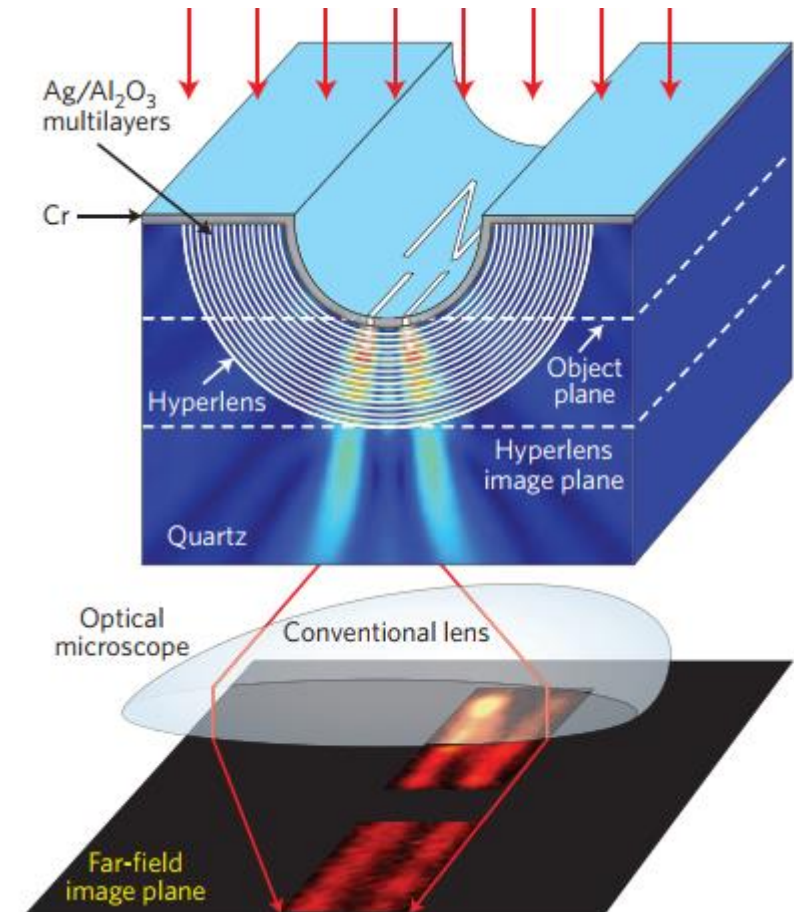
The angle of hyperbolic polaritons within the material is fixed



What does that profile mean?



Dai, S., et al. *Nature communications* 6.1 (2015): 1-7.

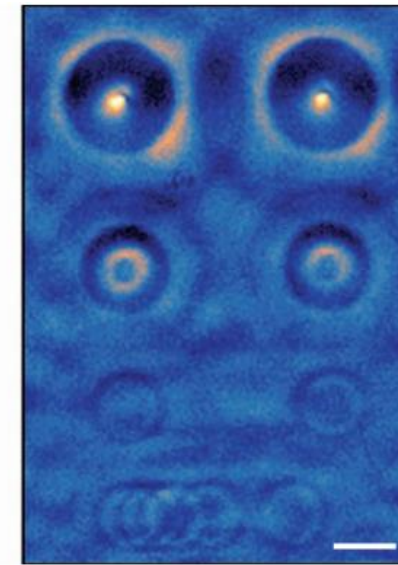
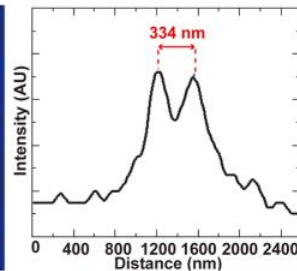
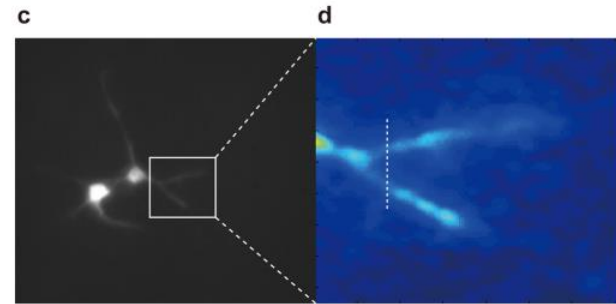
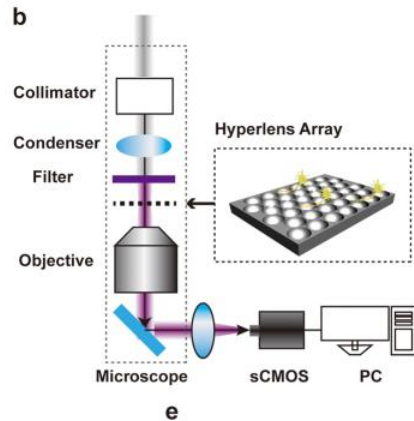
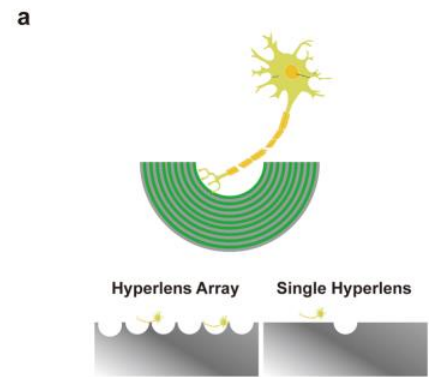
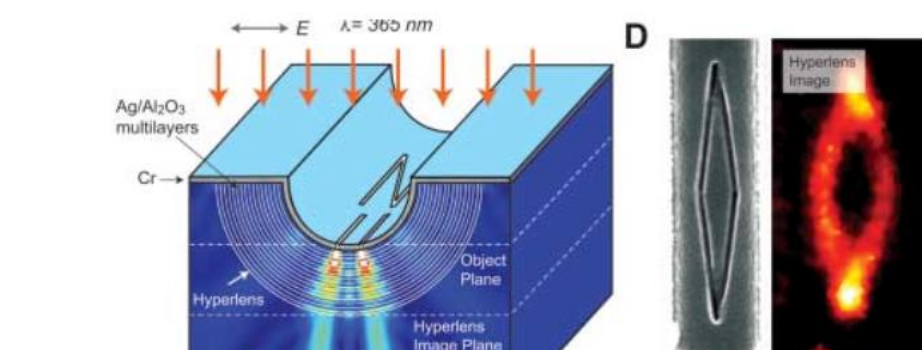


Liu, Z., et al, X. *Science* **315**, 1686 (2007).

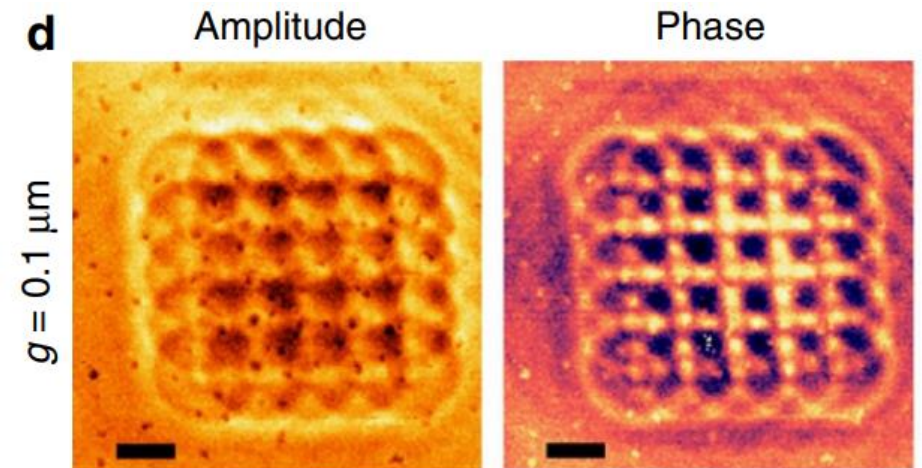
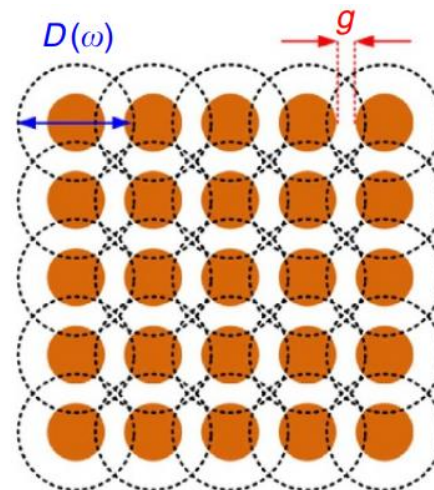
Objects under hyperbolic media can be magnified



Early demonstrations of super-resolution imaging



Dai, S., et al. *Nature communications* 6.1 (2015): 1-7.



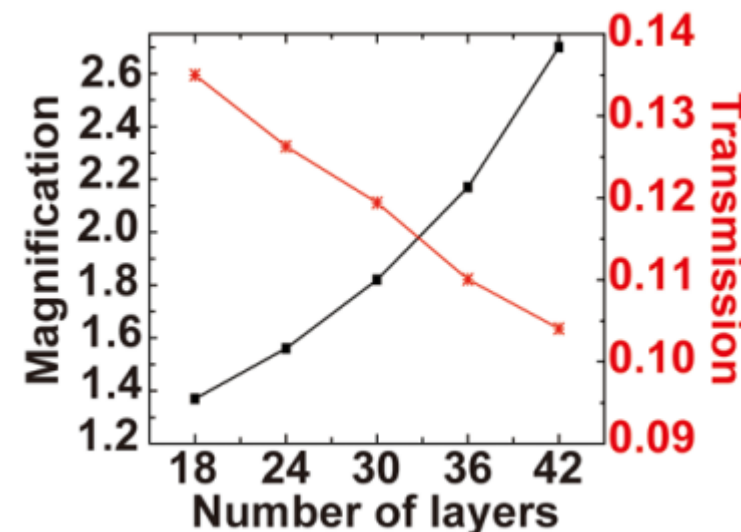
Liu, Z., et al. *X Science* 315, 1686 (2007).
Lee, D., et al. *ACS Photonics* 6, 2549-2554 (2019).

Li, Peining, et al. *Nature communications* 6.1 (2015): 1-9.



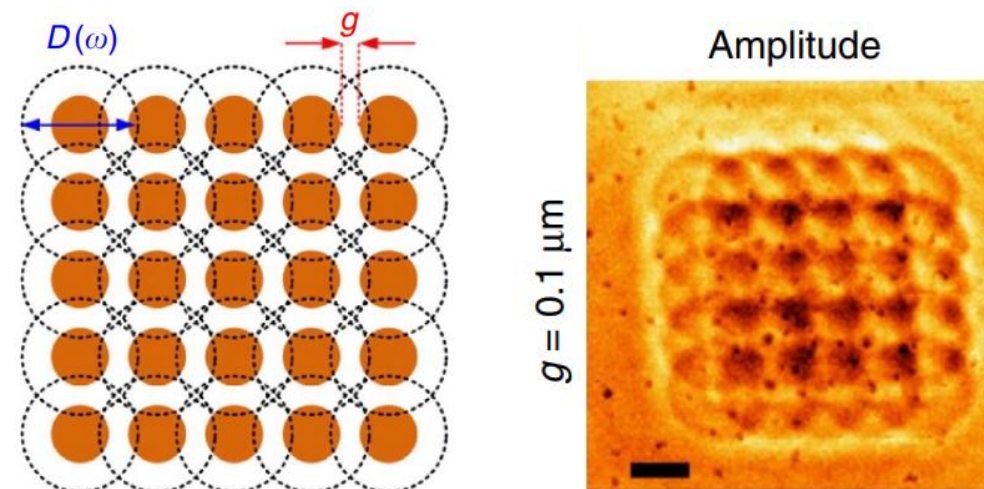
Challenges remaining

- Signal strength
 - (transmission rate, signal noise ratio, etc)
- Spatial resolution
- **Solution:**
- ***Decreased loss from hyperbolic material***



Lee, Dasol, et al. *ACS Photonics* 5.7 (2017): 2549-2554.

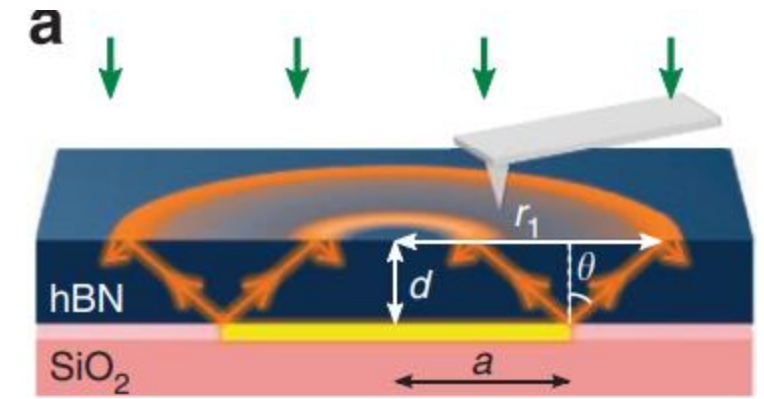
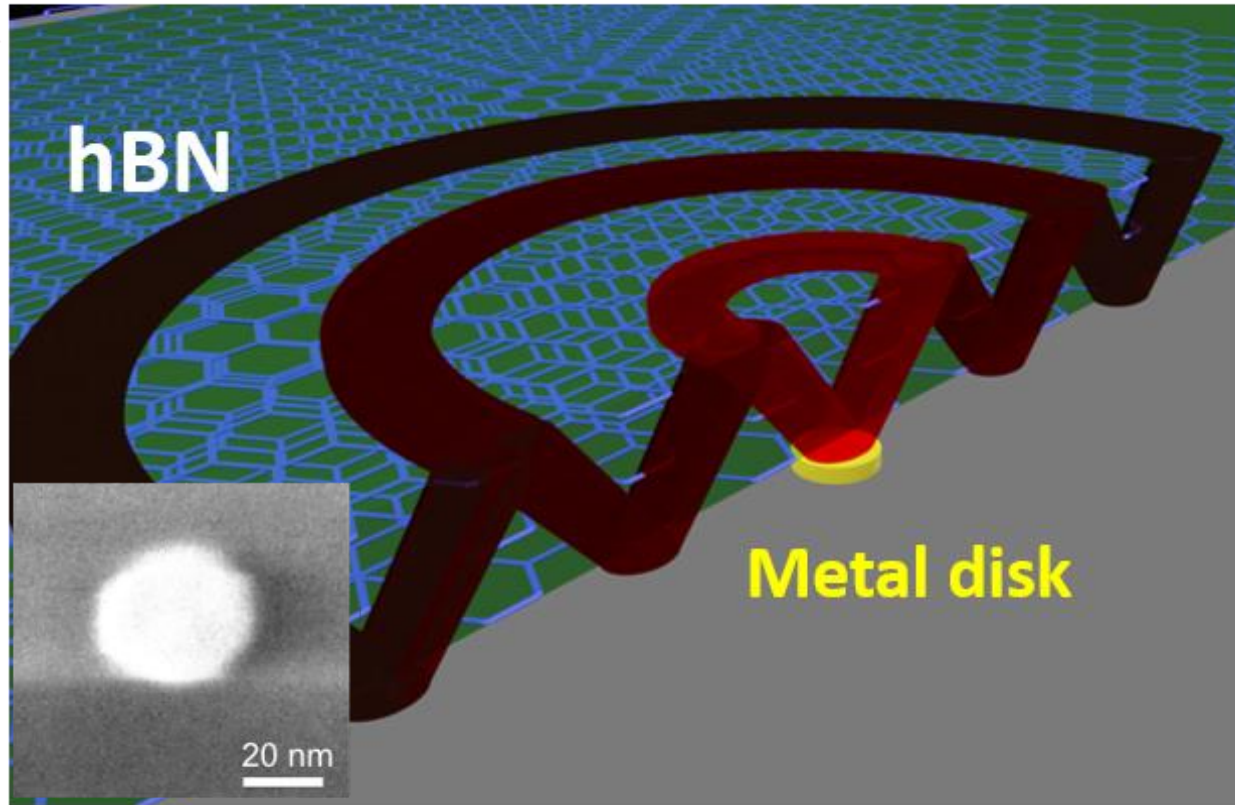
- Convoluted hyperlens field
- **Solution:**
- ***Algorithm reconstruction***



Li, Peining, et al. *Nature communications* 6.1 (2015): 1-9.



Schematics of our hyperlens

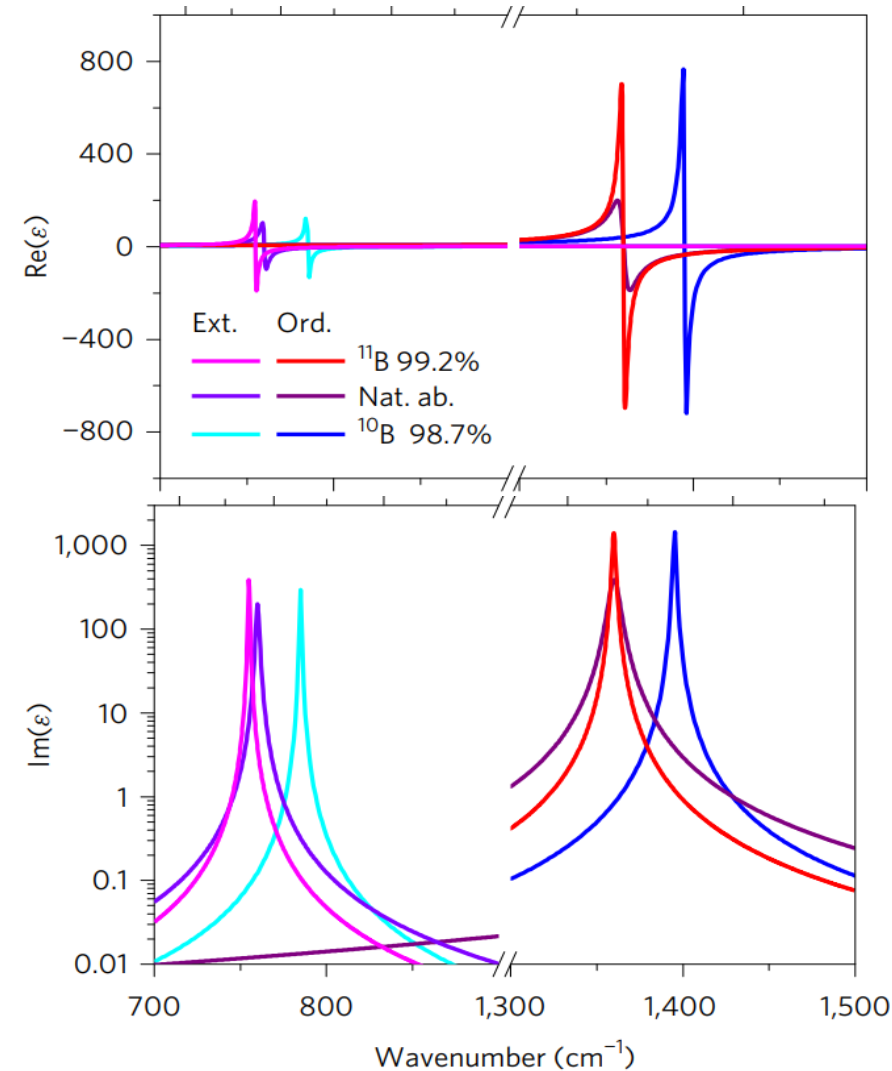
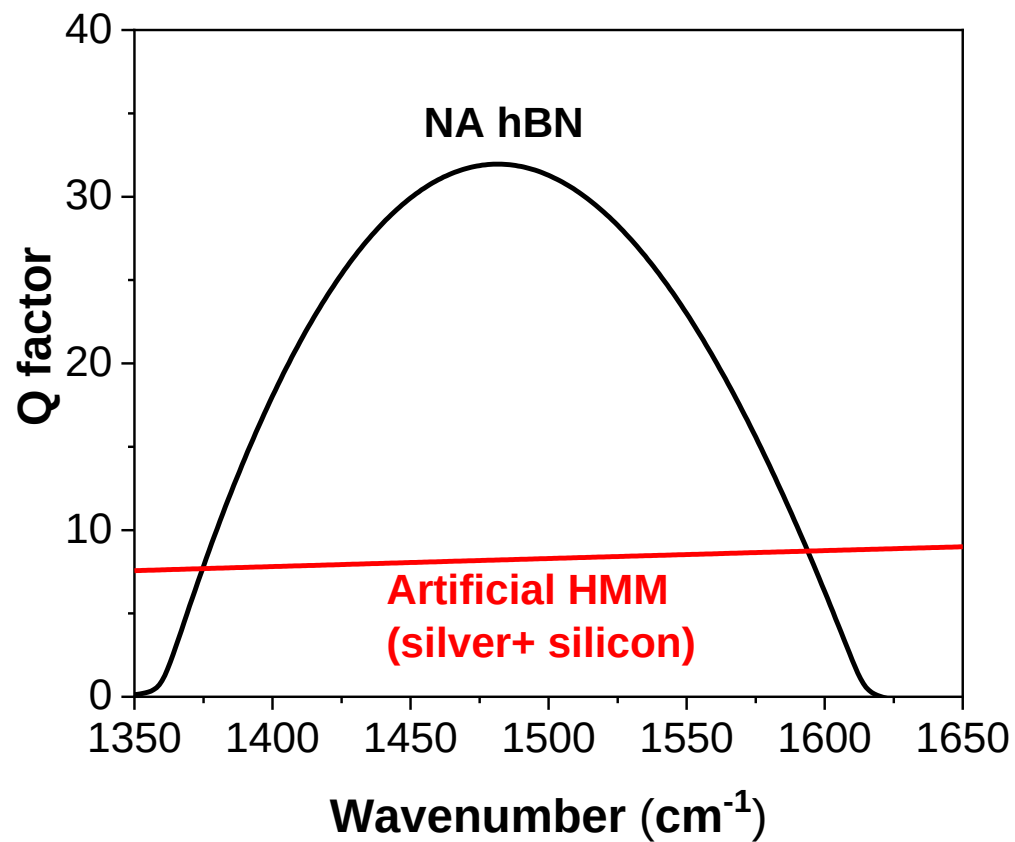


Dai, S., et al. *Nature communications* 6.1 (2015): 1-7.

1. High momentum polaritons launched by the objects
2. Propagating and magnified through the hyperbolic material
3. Probed in the near-field at the top surface



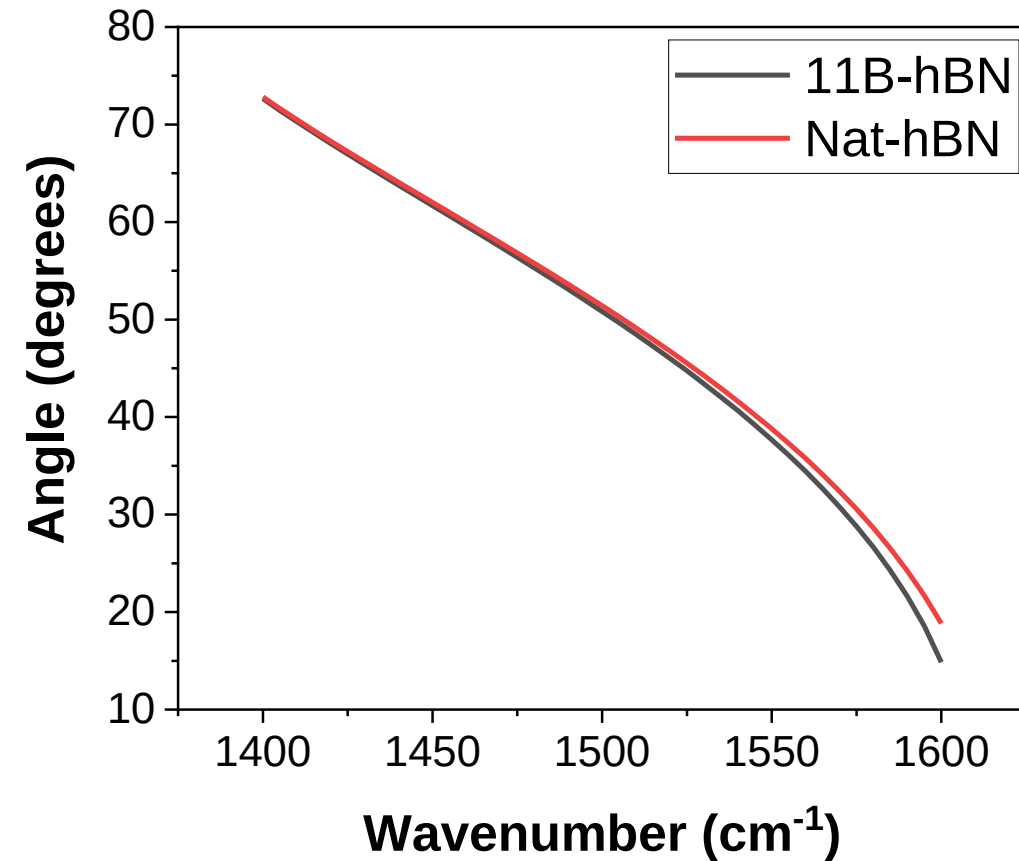
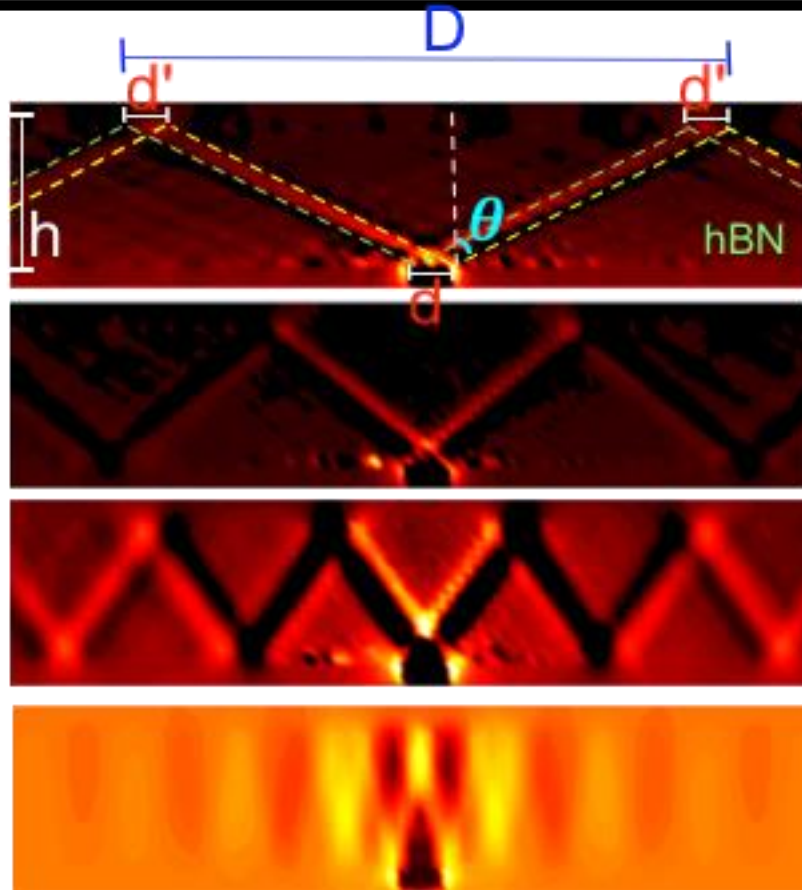
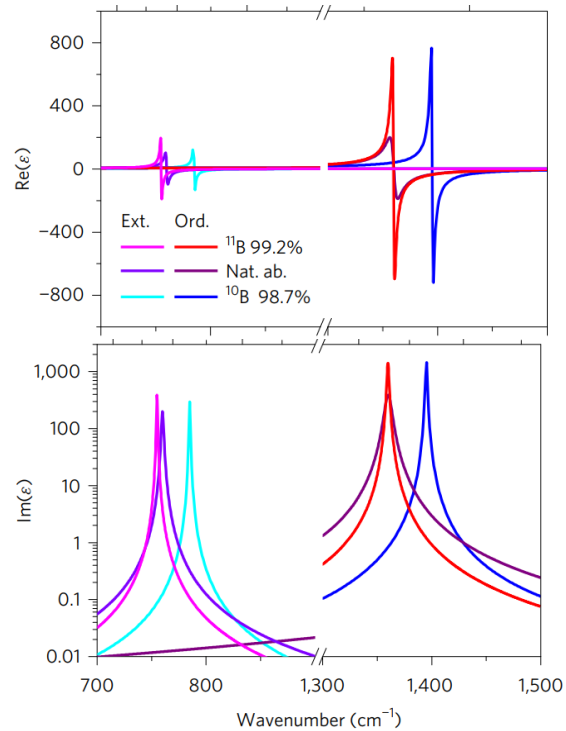
Material advancements via isotopic engineering



With isotopic enrichment, the loss can be further reduced

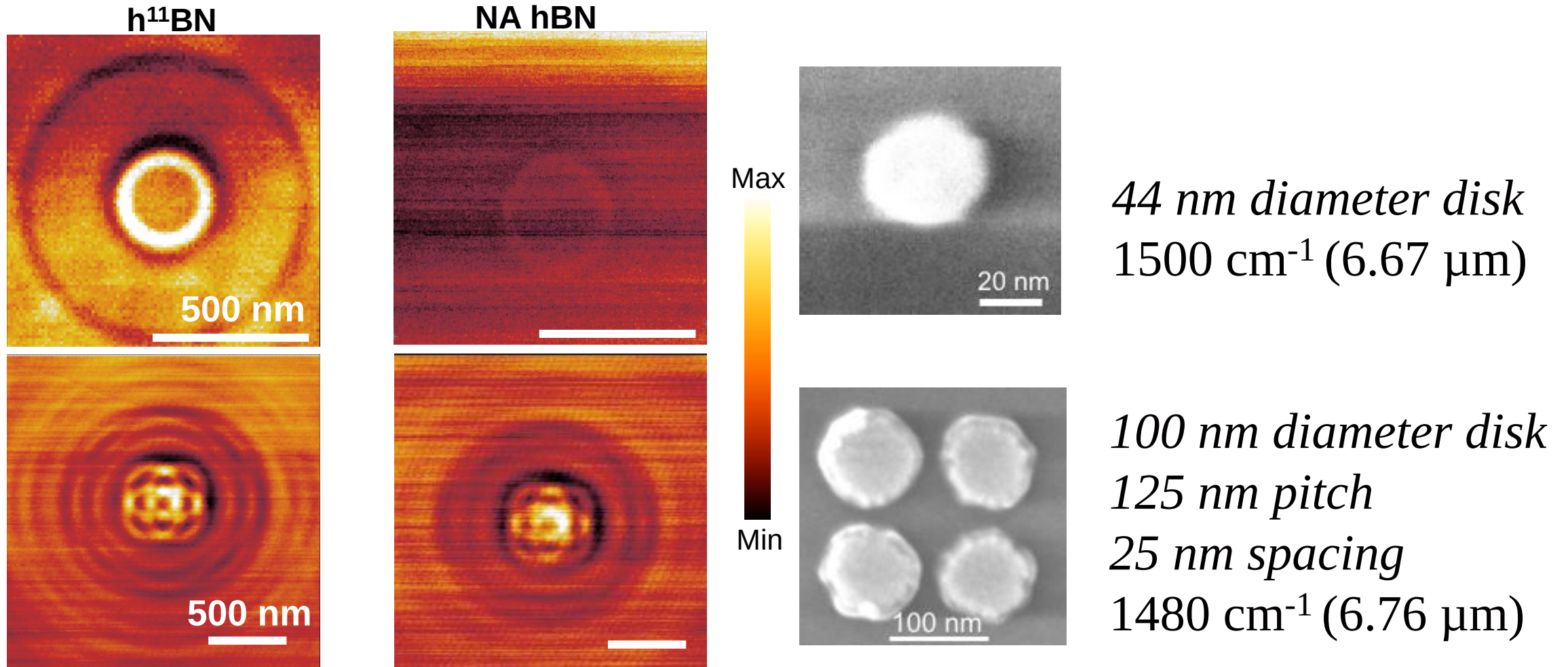


Material advancements via isotopic engineering



Same phonon frequency, reduced imaginary part of permittivity
Comparable real part (magnification times)

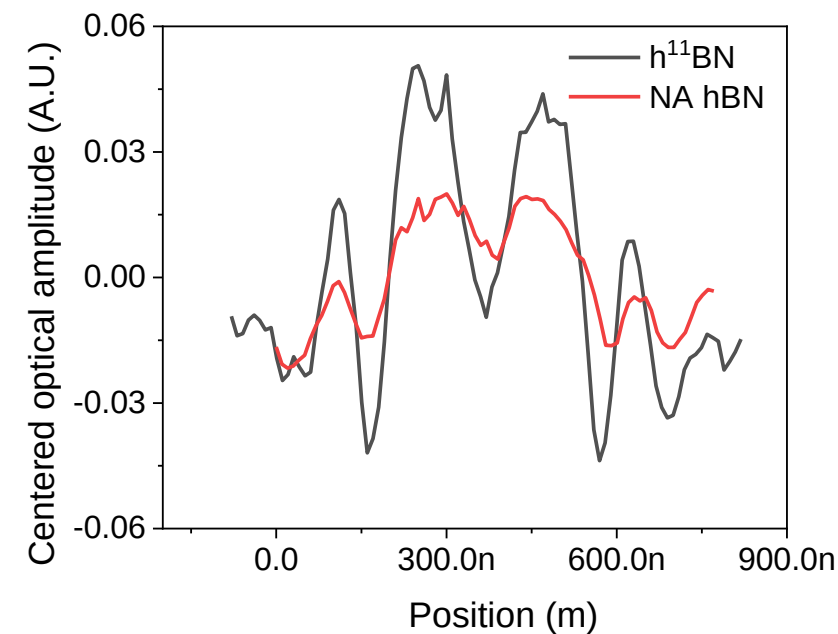
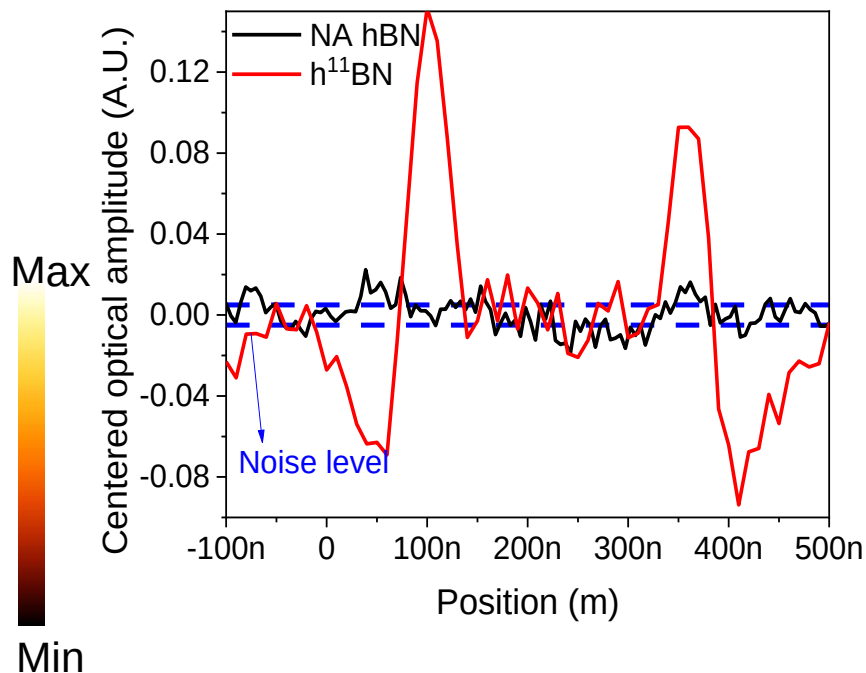
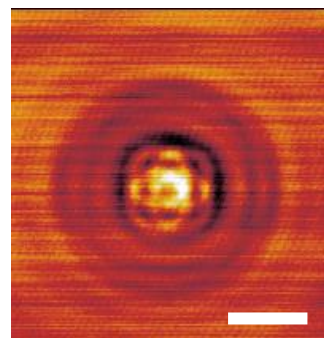
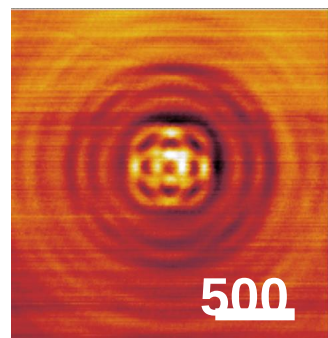
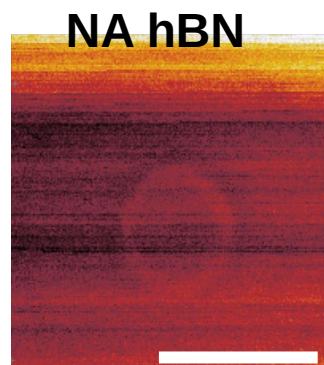
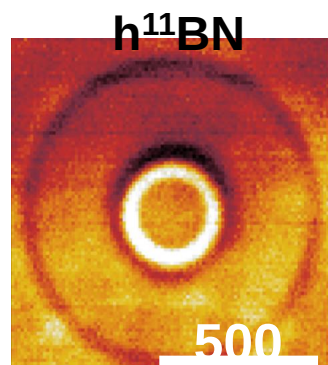
Experimental demonstration of reduced loss



Improved image quality from $h^{11}BN$



Quantifying the improvements

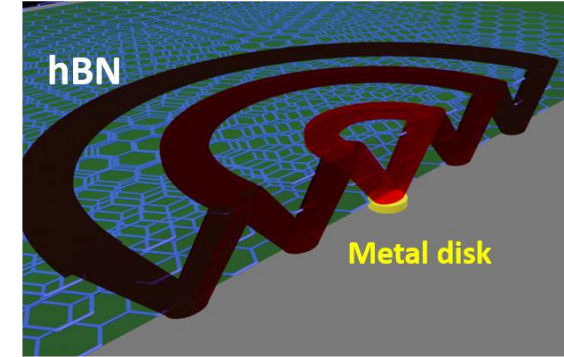
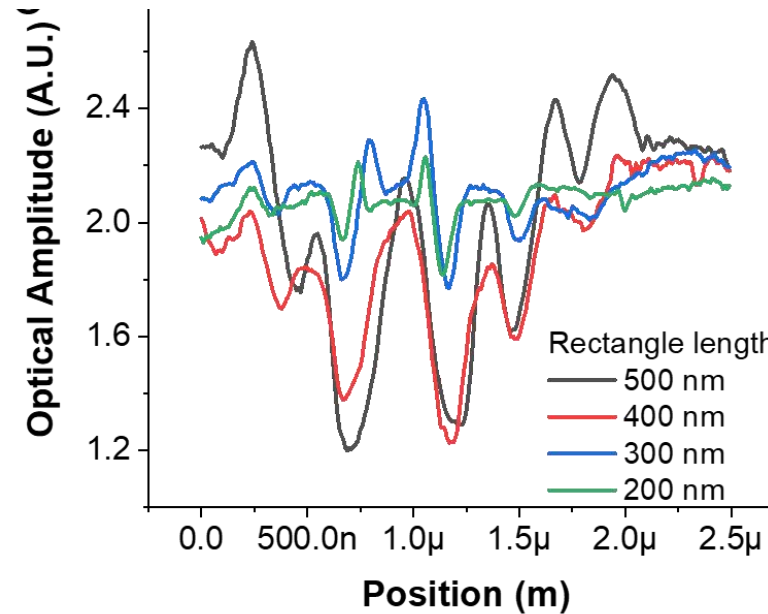
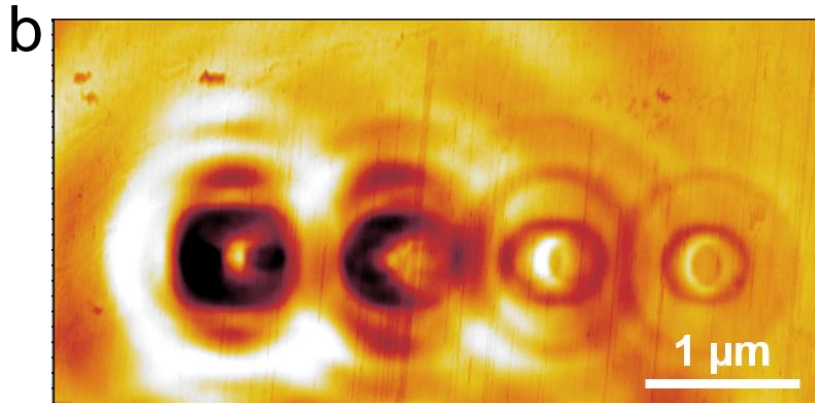
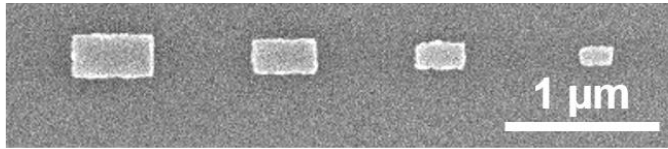


Comparable noise level
Enhanced signal strength
Improved signal noise ratio (SNR)



The relationship between loss and resolution

$$E_{top\ surface} = E_{bottom} \frac{circumference_{disk}}{circumference_{top\ ring}} \frac{1}{Loss}$$
$$= \frac{E_{bottom}}{Loss \cdot Magnification}$$



The measurable $E_{top\ surface}$ is defined as noise-equivalent power, which is a **constant** dictated by detector, s-SNOM...

With reduced loss, we can get higher *Magnification*.



Material advancements

$$k(w) = k' + ik'' = -\frac{\psi}{t} \left[a \tan\left(\frac{\varepsilon_o}{\varepsilon_t \psi}\right) + a \tan\left(\frac{\varepsilon_s}{\varepsilon_t \psi}\right) + \pi l \right]$$
$$\psi = -i \sqrt{\frac{\varepsilon_z}{\varepsilon_t}}$$

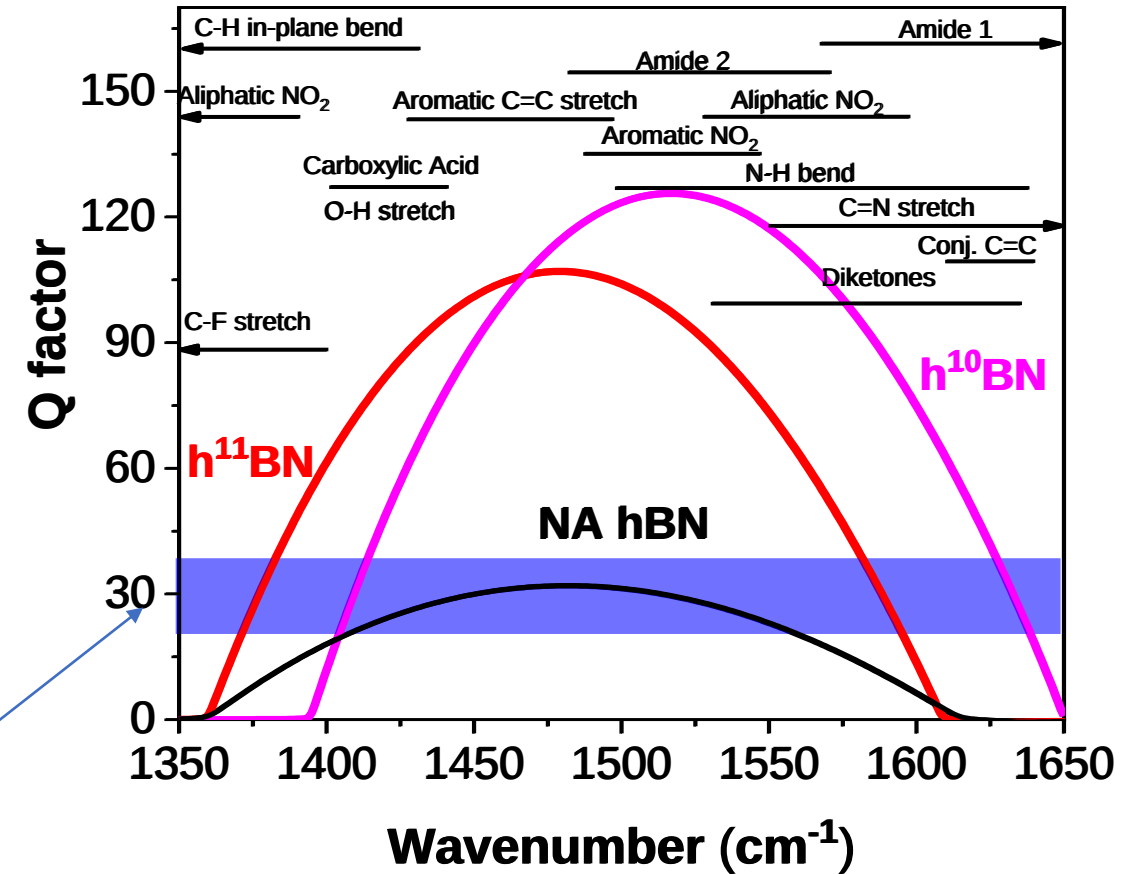
(3)

Dai, S. et al. *Nano letters* **19**, 1009-1014 (2018).

$$Q = \frac{k'}{k''} = 4\pi N$$

Assuming sodium/silicon HMM

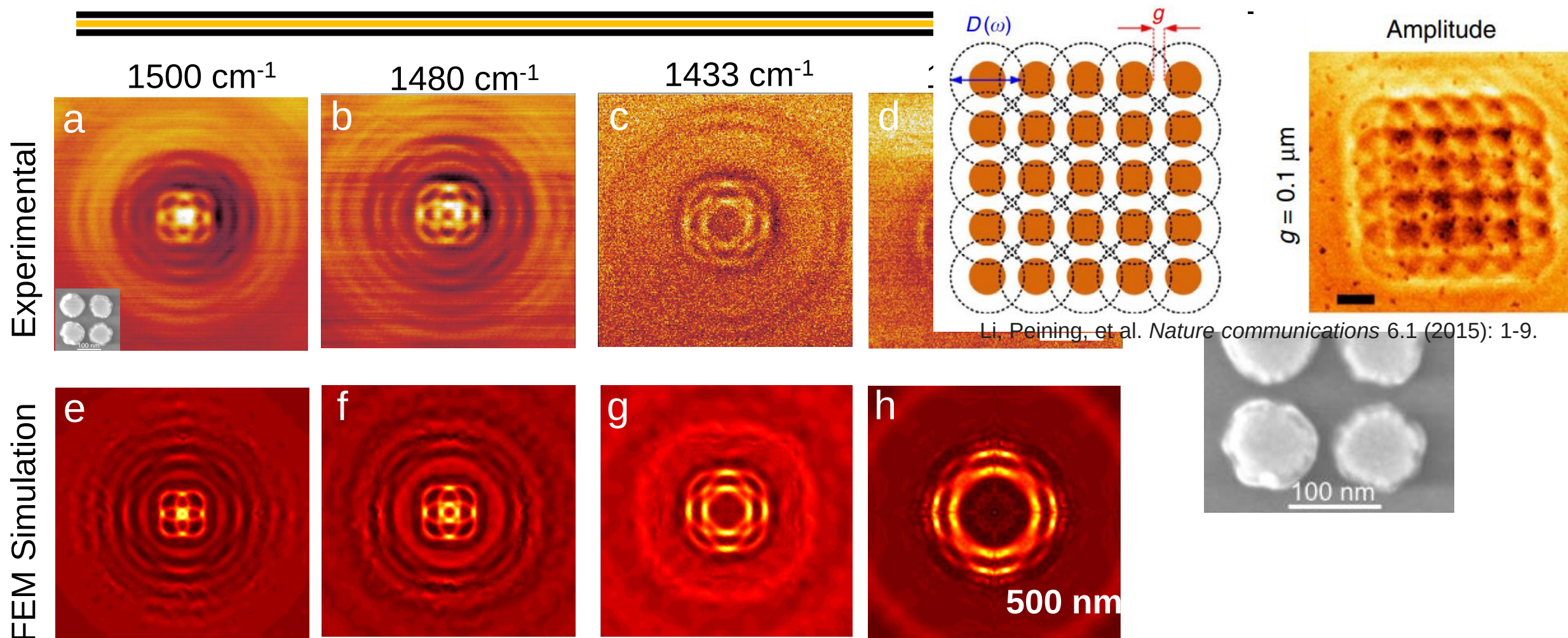
Wang, Yang, et al. *Nature* 581.7809 (2020): 401-405.



In the mid IR, isotopically enriched hBN outperforms natural hBN, as well as artificial hyperbolic materials (metal/dielectric stacks)



Complicated hyperlens field

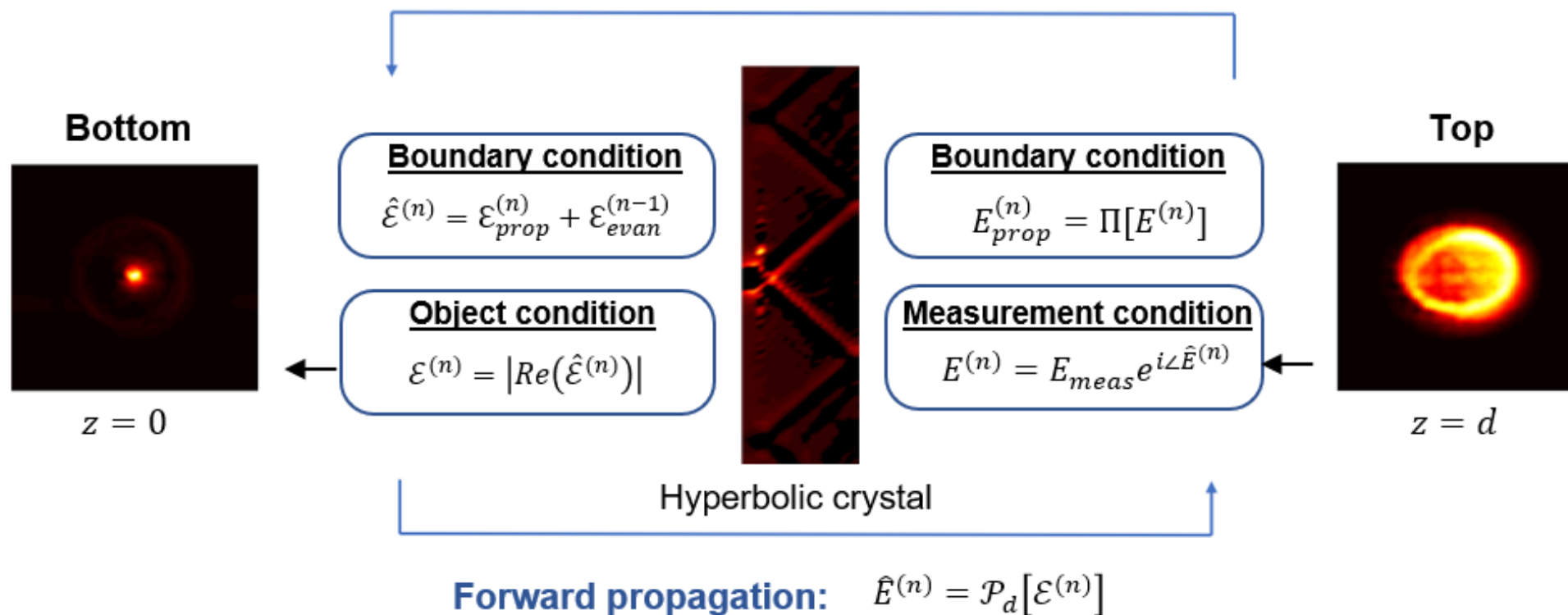


Hyperlens fields are convoluted



Algorithm to reconstruct hyperlens field

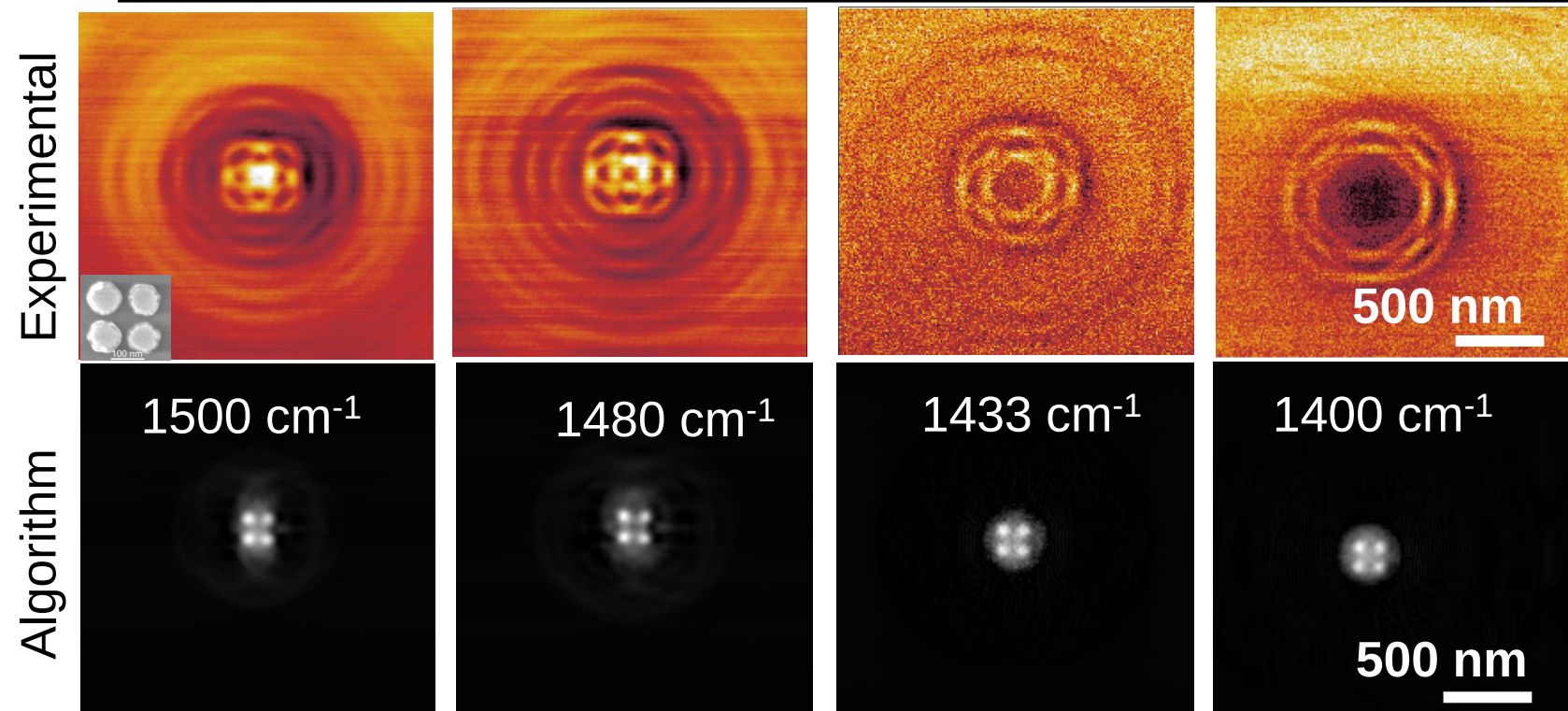
Back-propagation: $\varepsilon_{prop}^{(n)} = \mathcal{P}_{-d} [E_{prop}^{(n)}]$



Field under the hyperbolic material can be reconstructed from the E-field amplitude at the top surface

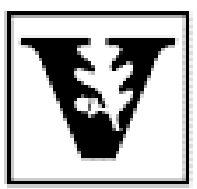


Reconstructed fields under hyperbolic media



Accurate reconstruction can be performed

Image frequency (cm ⁻¹)	Disk diameters (nm)	Pitch size (nm)	Interparticle gap (nm)
1400	86 (2)	113 (2)	27 (2)
1433	88 (5)	113 (8)	25 (8)
1482	83 (6)	117 (6)	34 (8)
1500	89 (5)	112 (12)	23 (13)
SEM	100	125	25

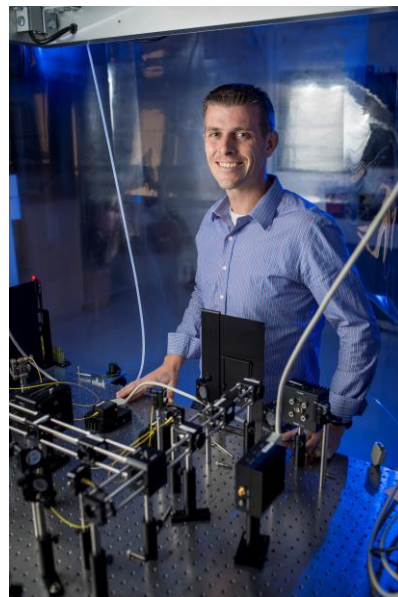


Summary

- Material advancements enable high-resolution hyperlens imaging
 - 44 nm diameter disk imaged
 - 100 nm diameter disks with 125 nm pitch resolved
 - Outperforms natural hBN and artificial HMM significantly
- Computational technique allows accurate reconstruction of E-field from convoluted hyperlens field with only amplitude information
 - Could be used in other measurement schemes, e.g., photothermal infrared (PTIR)



Prof. Joshua Caldwell



Prof. Tom Folland



Joseph
Matson



Mingze
He



Guanyu
Lu



Scott
Criswell



Ryan
Kowalski



Katja
Diaz-
Granados



Ryan
Nolen



Lauren
Potechin



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Song Liu