

# Cold-atom regularizations of relativistic 4-Fermi QFTs:

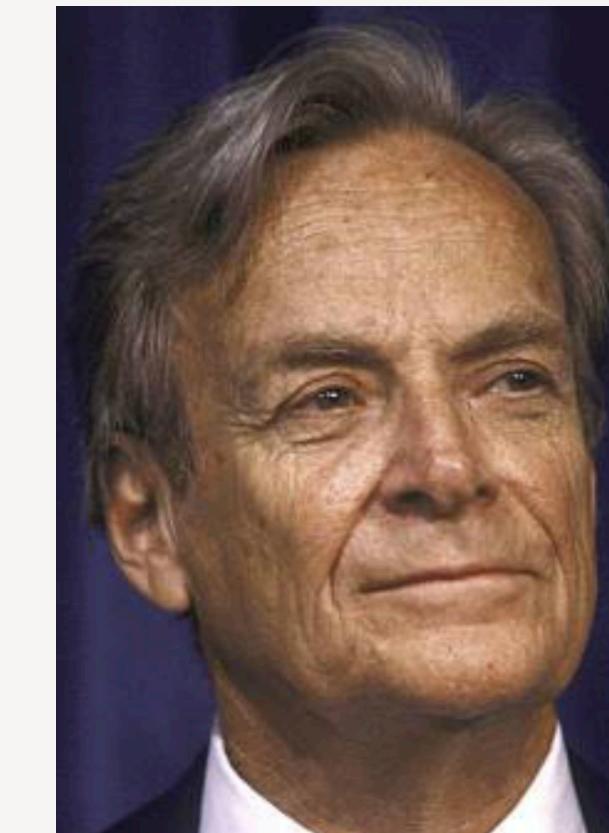
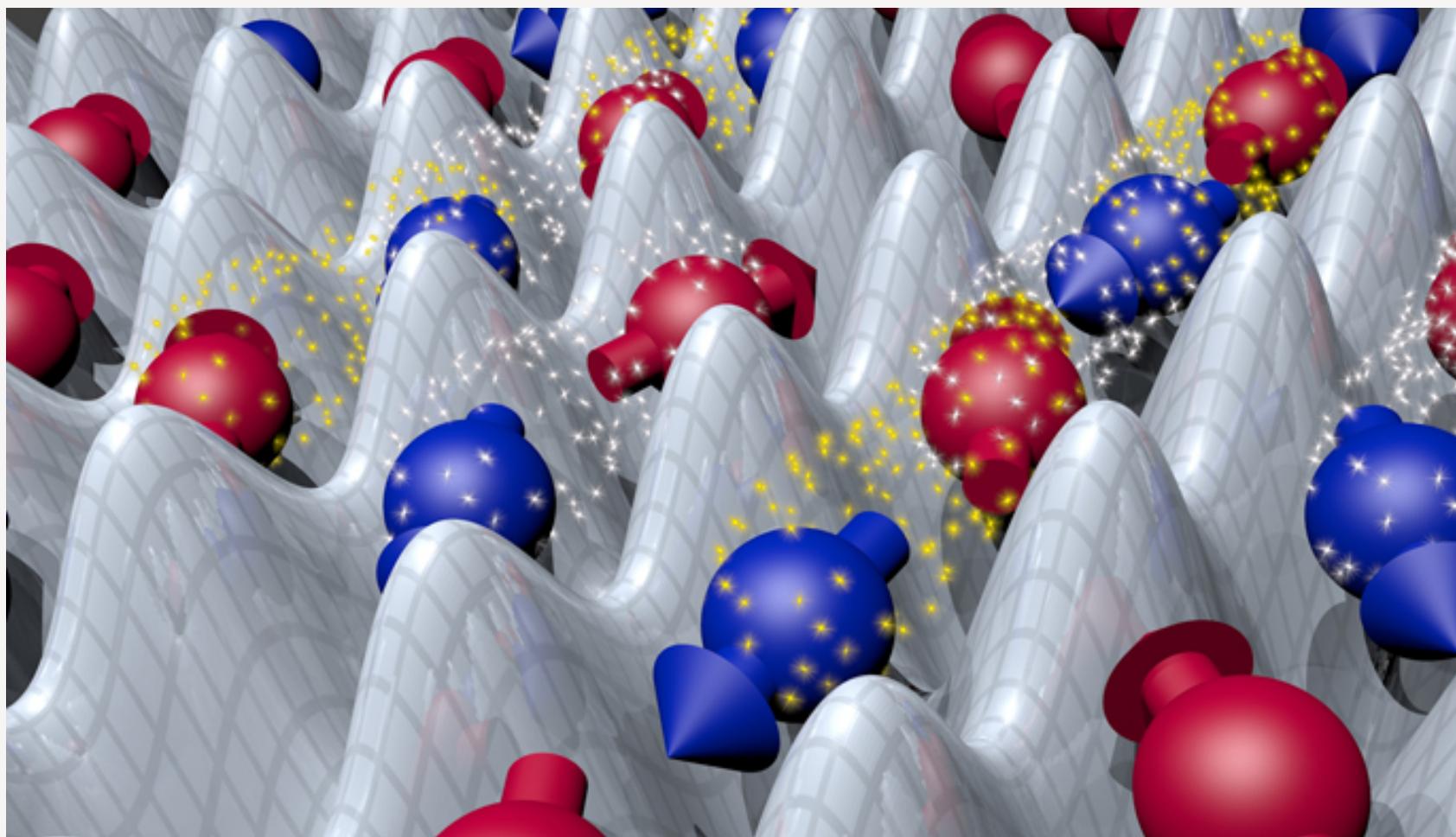
*Exploring correlated topological phases*



Alejandro Bermúdez,  
Atomtronics, Benasque 2022

# MOTIVATION

Can we exploit cold-atom quantum simulators for high-energy physics?



R. Feynman, *Int.J.Th.P.* **21**, 467 (1982).



S. P. Jordan, K. S. Lee,  
and J. Preskill, *Science* **336**, 1130 (2012)



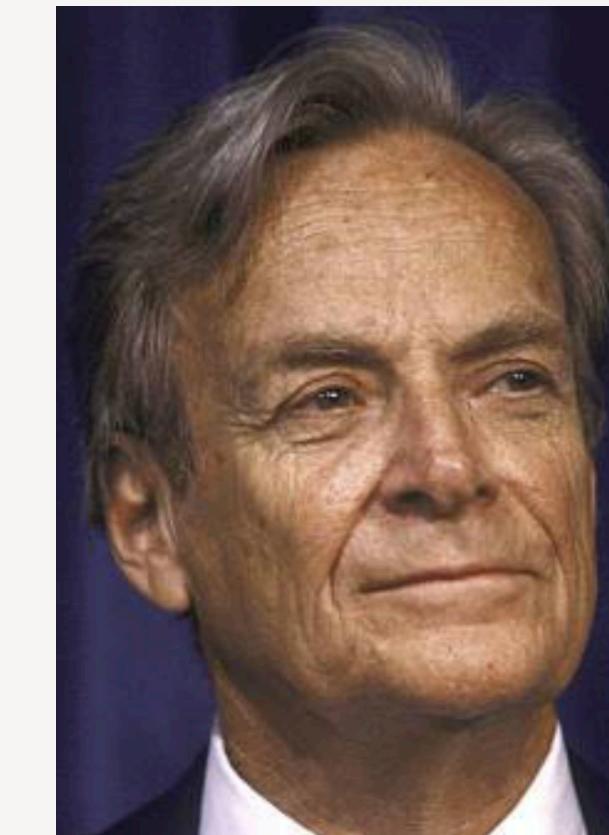
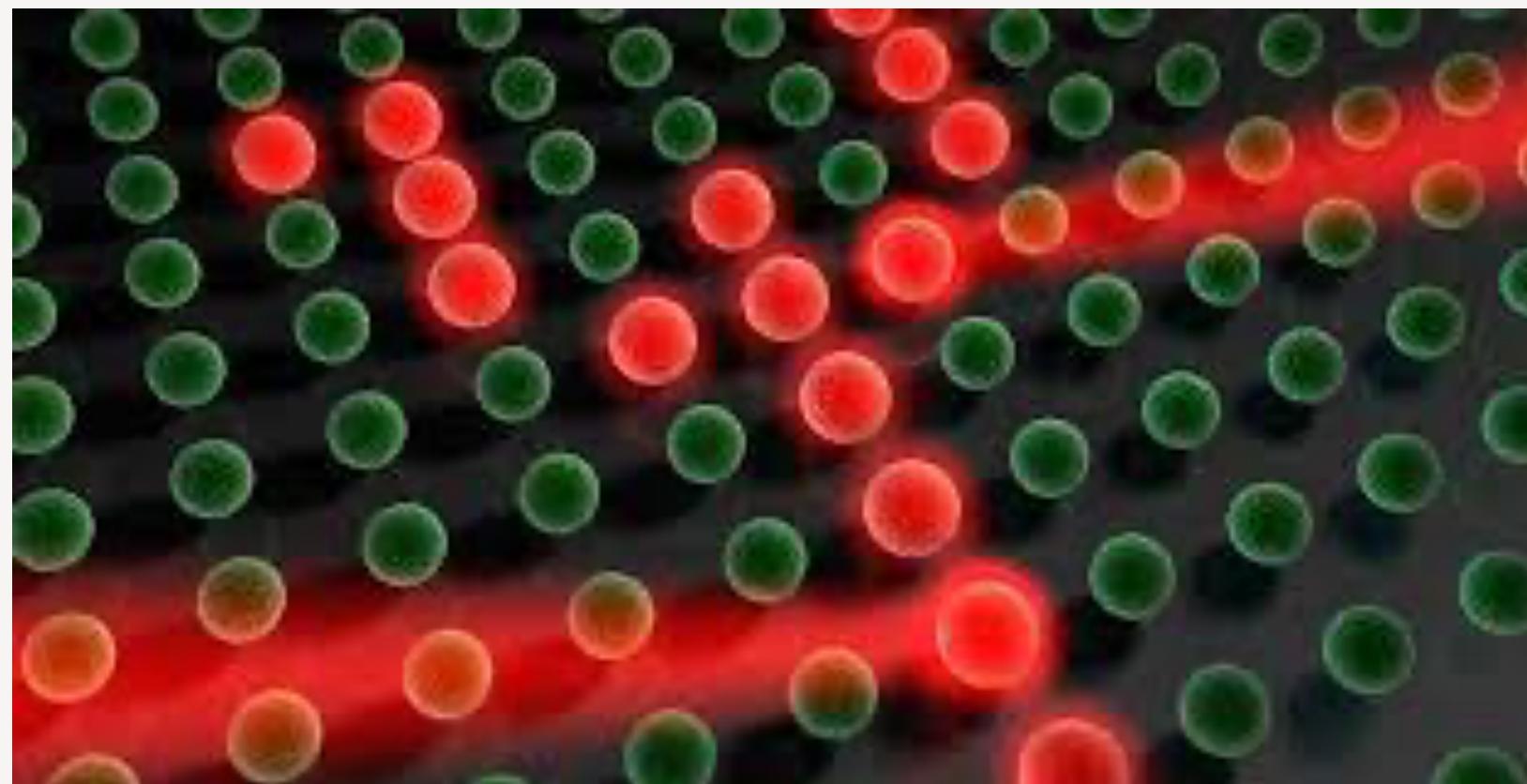
E. Zohar, et al., *PRL* **109**, 125302 (2012)  
D. Banerjee, et al., *PRL* **109**, 175302 (2012)



M. Bañuls et al., *Eur. Phys. J. D* **74**, 165 (2020).

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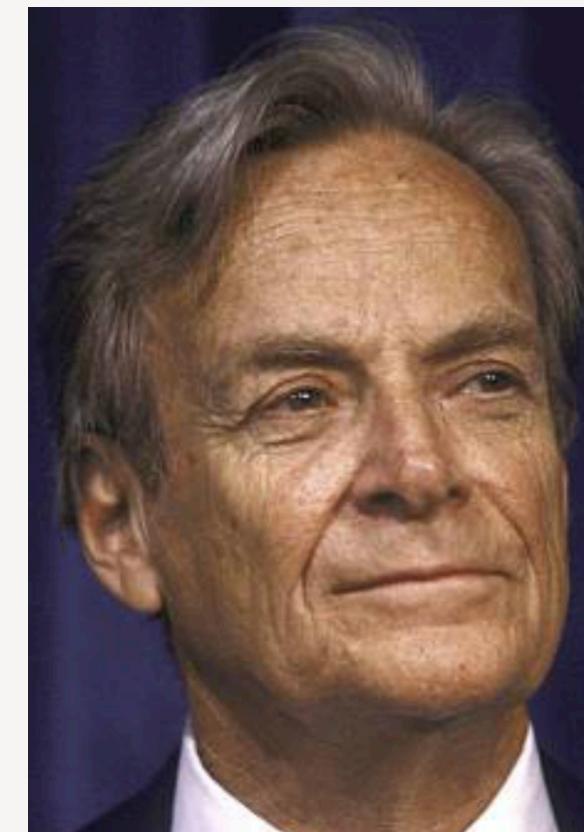
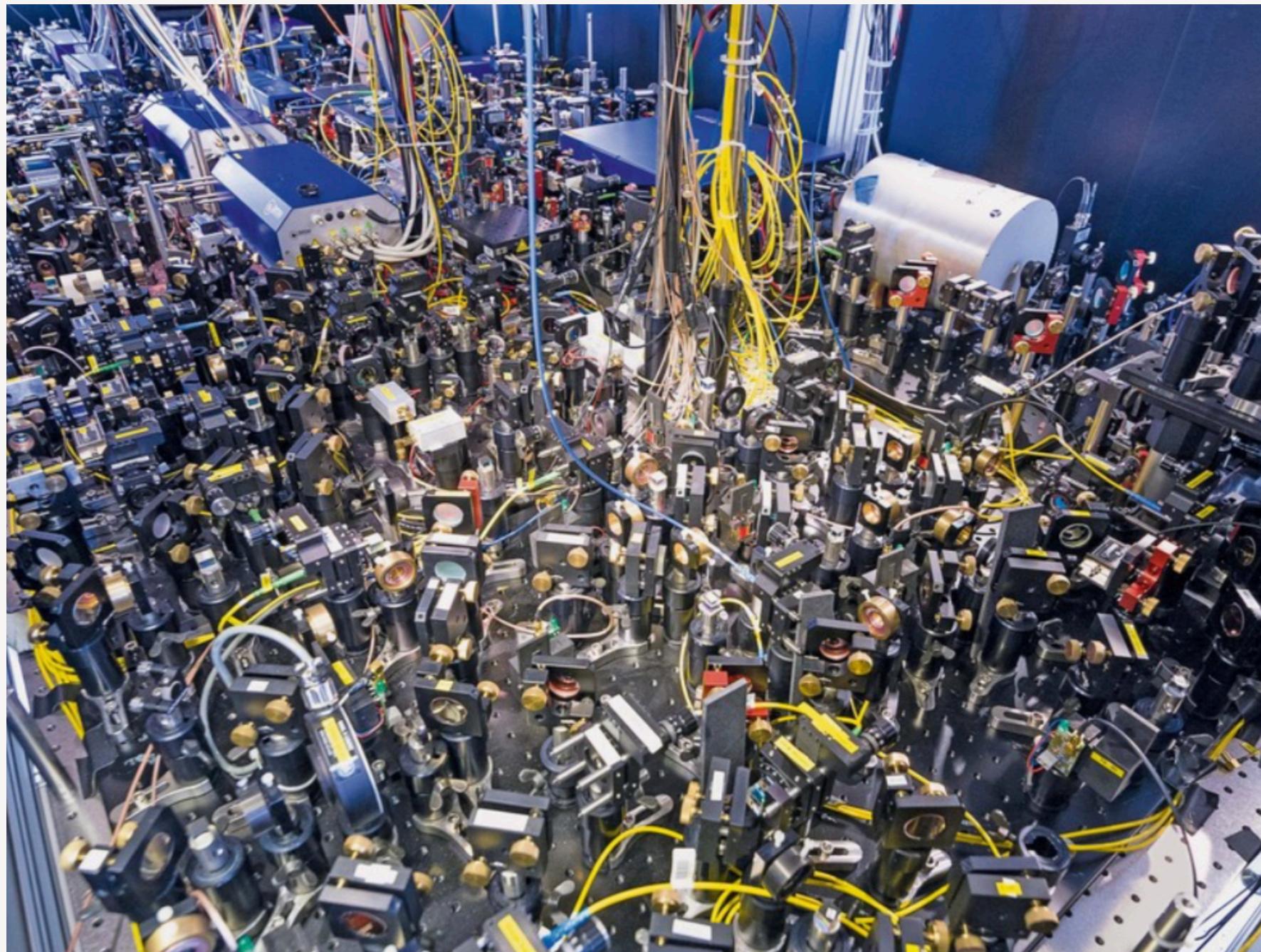
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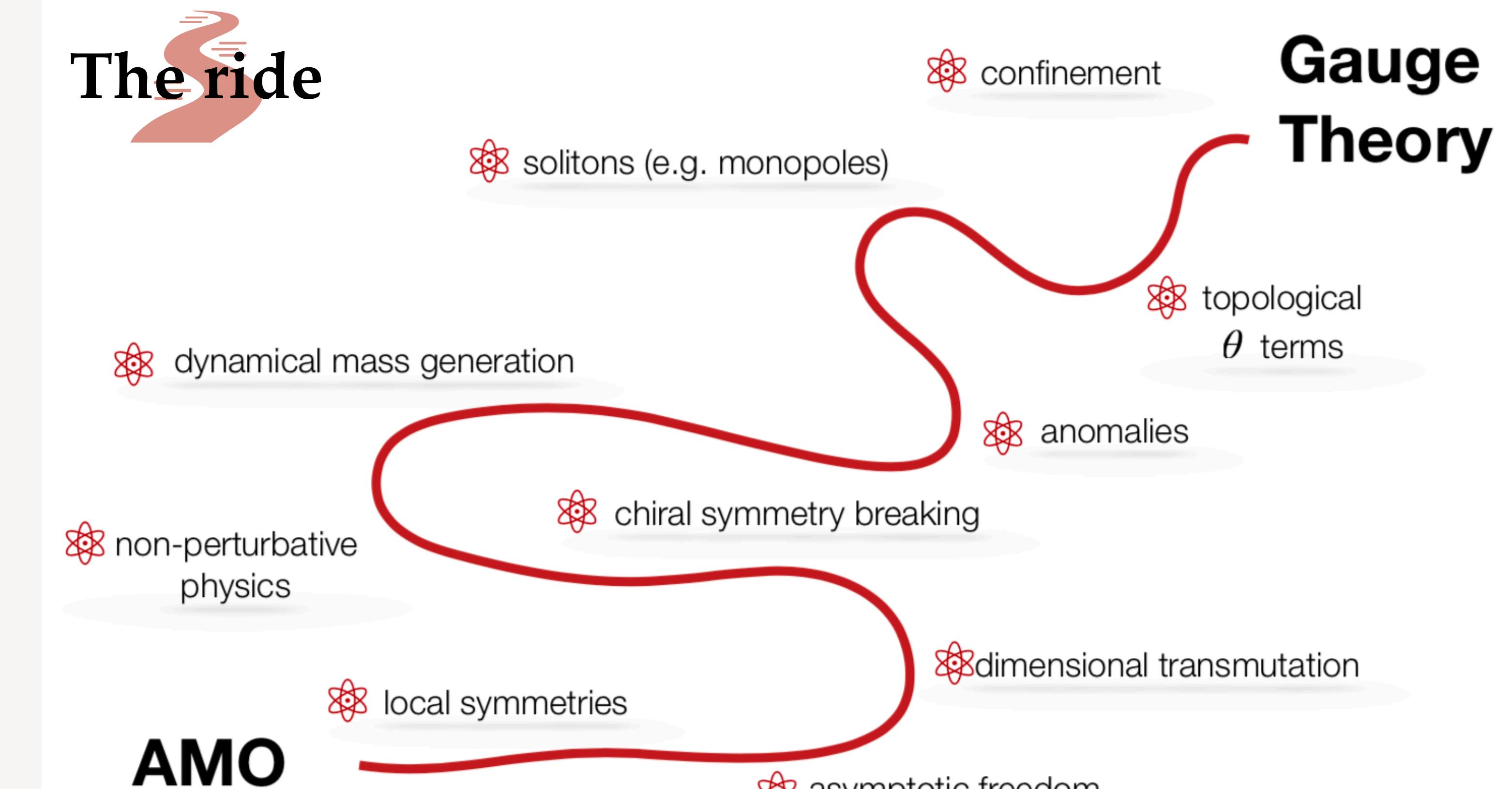


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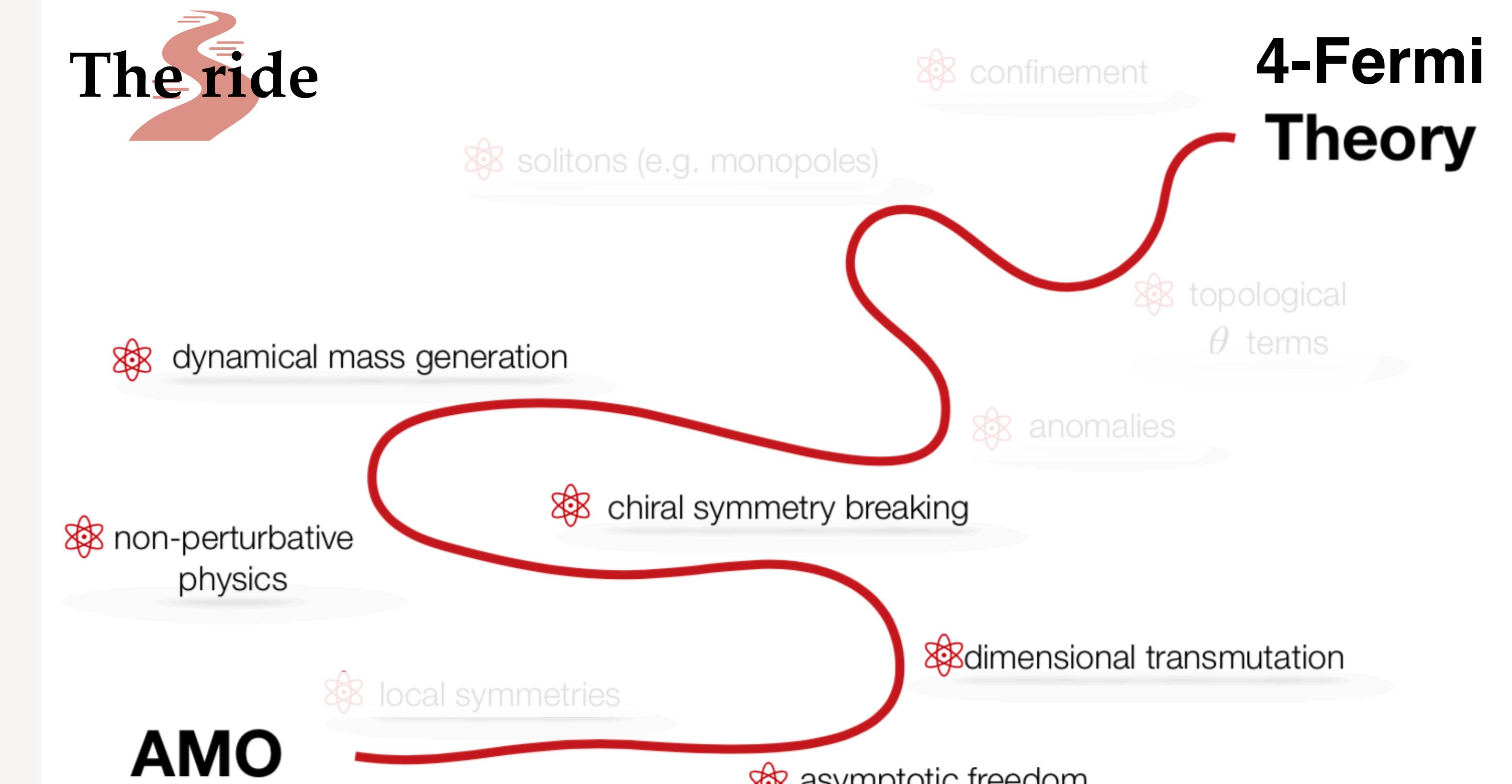


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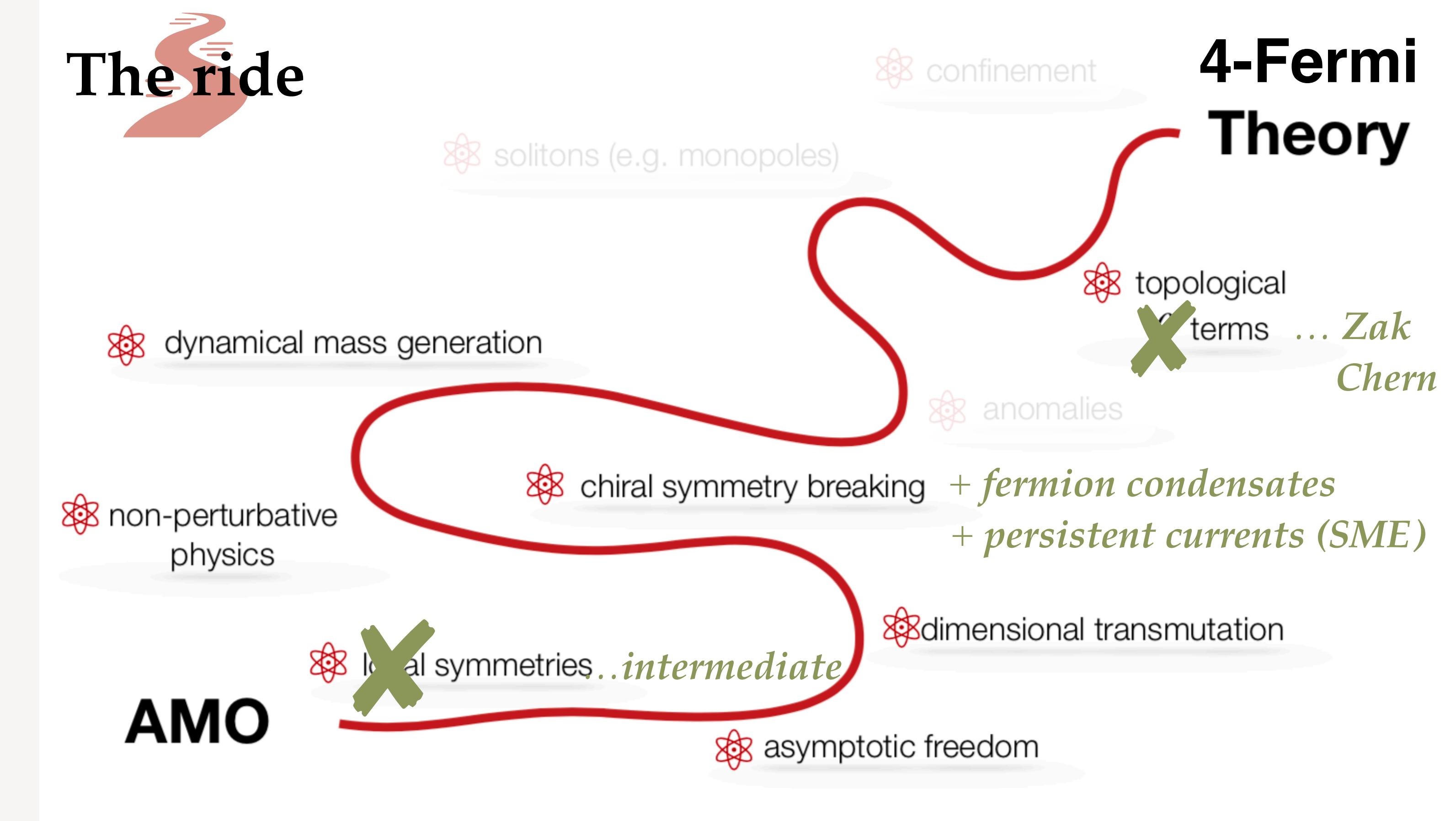
# MOTIVATION



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# 4-Fermi field theories in $d+1$ dimensions

We consider self-interacting Dirac fermions with  $N$  flavors in  $D = d + 1$  spacetime dimensions

$x = (x^0, \vec{x})$  Minkowski spacetime

$\eta = \text{diag}(1, -1, \dots, -1)$  metric

$\{\gamma^\mu, \gamma^\nu\} = 2\eta^{\mu\nu}$  Dirac matrices

$$\mathcal{L} = \sum_{f=1}^N \bar{\psi}_f(x) (i\gamma^\mu \partial_\mu) \psi_f(x) + \frac{g^2}{2N} \left( \sum_{f=1}^N \bar{\psi}_f(x) \psi_f(x) \right)^2,$$

free Dirac QFT      4-Fermi interactions

$$\psi_f(x) = (\psi_{f,\uparrow}(x), \psi_{f,\downarrow}(x))^t, \quad \bar{\psi}_f(x) = \psi_f^\dagger(x) \delta^0$$

$d=1, 2 \Rightarrow 2\text{-component spinors}$   $\rightarrow$   
 $\uparrow, \downarrow$

$$d=1, \text{ e.g. } \gamma^0 = \sigma^z, \gamma^1 = i\sigma^y, \gamma^5 = \gamma^0\gamma^1 = \sigma^x$$

$$d=2, \text{ e.g. } \gamma^0 = \sigma^z, \gamma^1 = i\sigma^y, \gamma^2 = -i\sigma^x, \gamma^5 = \gamma^0\gamma^1\gamma^2 = \sigma^x$$

4-Fermi term, e.g.  $N=1 \equiv$  Hubbard  $g^2/2 \left( \bar{\psi}_f(\vec{x}) \psi_f(\vec{x}) \right)^2 \propto -g^2 n_{f,\uparrow}(x) n_{f,\downarrow}(x)$

# 4-Fermi field theories in d+1 dimensions

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$D = 3 + 1$  non-renormalizable QFT,  $\chi\text{SB}$  by dynamical mass generation

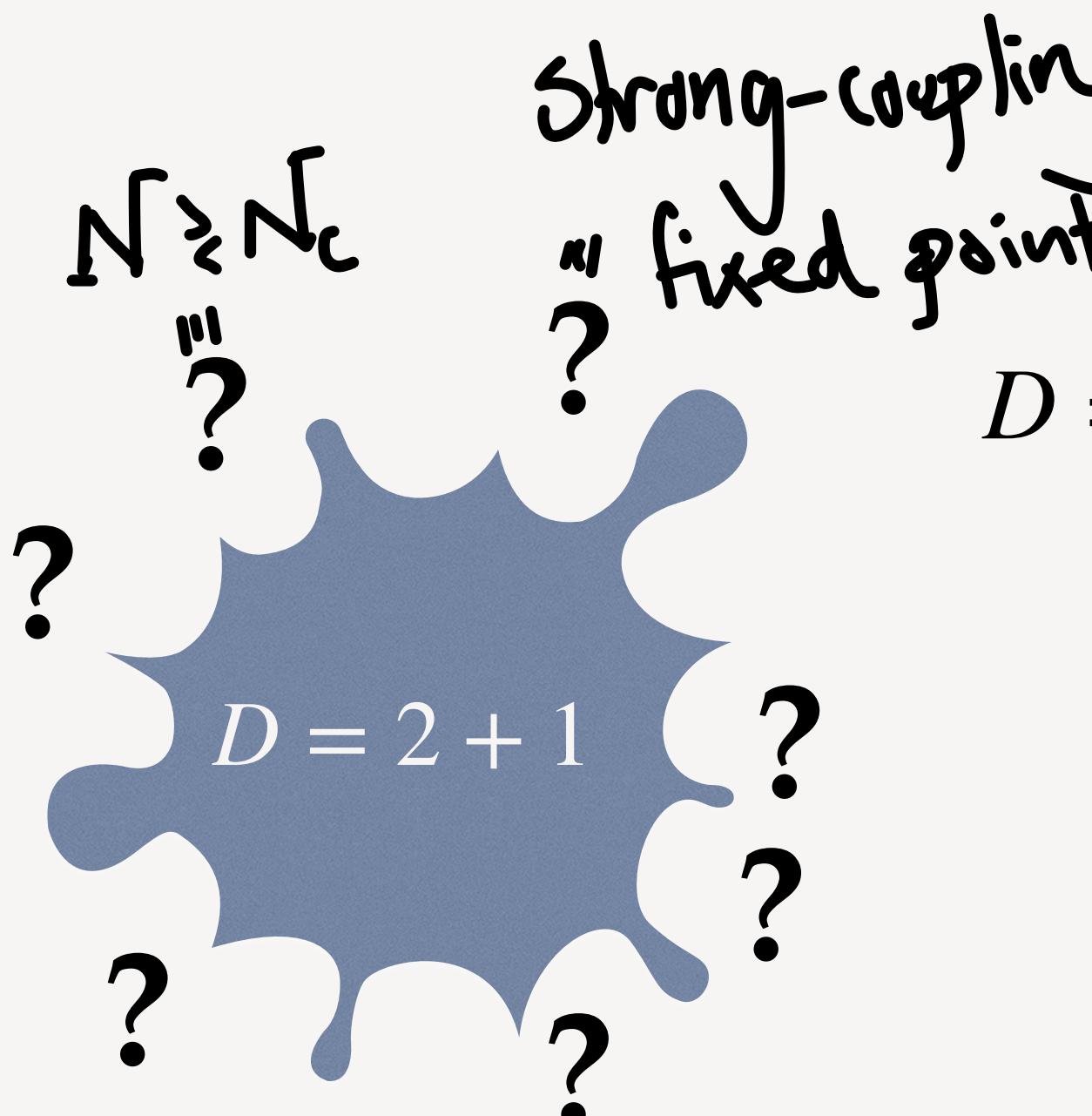
th Y. Nambu and G. Jona-Lasinio, **Phys. Rev.** **122**, 345 (1961).

$D = 1 + 1$  renormalizable QFTs,  $\chi\text{SB}$  by dynamical mass generation,  
asymptotic freedom, dimensional transmutation

th D. J. Gross and A. Neveu, **Phys. Rev. D** **10**, 3235 (1974).

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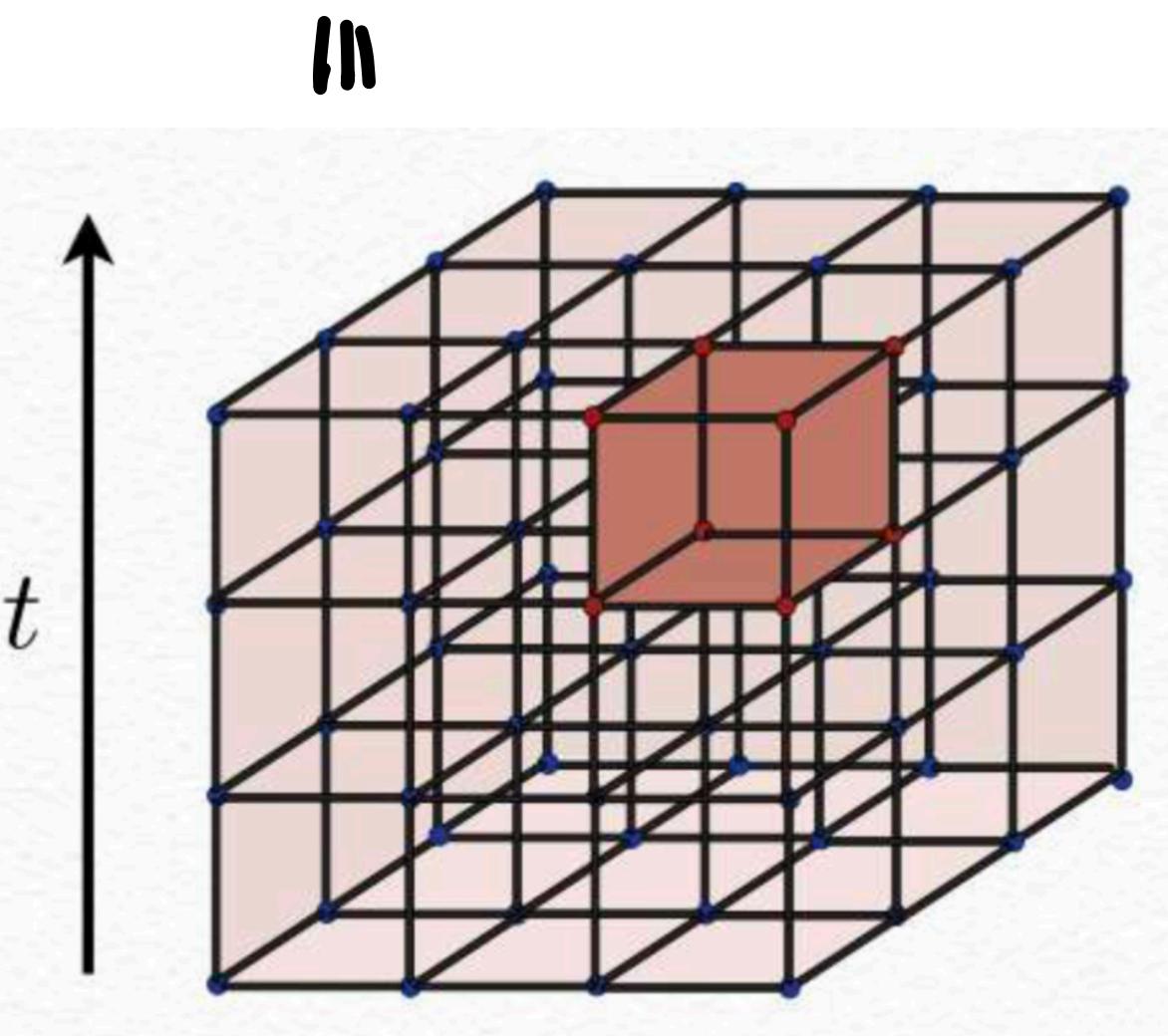
- S. Hands, [arXiv:hep-lat/9706018](https://arxiv.org/abs/hep-lat/9706018).

# 4-Fermi lattice field theories in d+1 dimensions

Exploring non-perturbative effects (e.g. strong-coupling fixed point) by an **artificial lattice**

Euclidean LFTs vs

Hamiltonian LFTs



$x^0 = t$   $\xrightarrow{\text{III}}$  continuous time th L. Susskind, PRD 16, 3031 (1977).

$\bar{x} = a n_i \hat{e}_j$ ,  $\bar{x}/a \in \mathbb{Z}^d$   $\xrightarrow{\text{discretized space}}$   $\Lambda_c = \frac{2\pi}{a}$   $=$   $V$  cutoff

$\partial_j \Psi(x) = \frac{\Psi(\bar{x} + a\hat{e}_j) - \Psi(\bar{x} - a\hat{e}_j)}{2a}$   $\xrightarrow{\text{naive discretization}}$

$$\sum_{\bar{n}_d} \bar{\Psi}_{\bar{n}_d}(x) (i \gamma_{\bar{n}_d}^\mu \partial_\mu - m) \Psi_{\bar{n}_d}(x) = \sum_{\bar{n}_d} S_{\bar{n}_d}$$

$$\bar{k}_{\bar{n}_d} = \frac{\pi}{a} \bar{n}_d, \bar{n}_d \in \mathbb{Z}^d, \bar{z}_2 = 40, 14 \rightarrow N_d = 2^d \quad \text{fermion doubles}$$

$\gamma_{\bar{n}_d}^5 \in \{-\gamma^5, +\gamma^5\}$   
opposite chiralities

$$N_+ = N_d/2$$
$$N_- = N_d/2$$

We recover Dirac QFT @ center of faces/corners BZ  $\equiv \Gamma, X, M$  points

# Wilson lattice regularization in d+1 dimensions

There are alternative discretizations that deal differently with the doublers

$$H = a_1 \cdots a_d \sum_{\mathbf{x} \in \Lambda_s} \left[ \sum_{j=1}^d \left( -\bar{\Psi}(\mathbf{x}) \left( \frac{i\gamma^j}{2a_j} + \frac{r_j}{2a_j} \right) \Psi(\mathbf{x} + a_j \mathbf{e}_j) + \bar{\Psi}(\mathbf{x}) \left( \frac{m}{4} + \frac{r_j}{2a_j} \right) \Psi(\mathbf{x}) + \text{H.c.} \right) - \frac{g^2}{2N} \left( \bar{\Psi}(\mathbf{x}) \Psi(\mathbf{x}) \right)^2 \right],$$

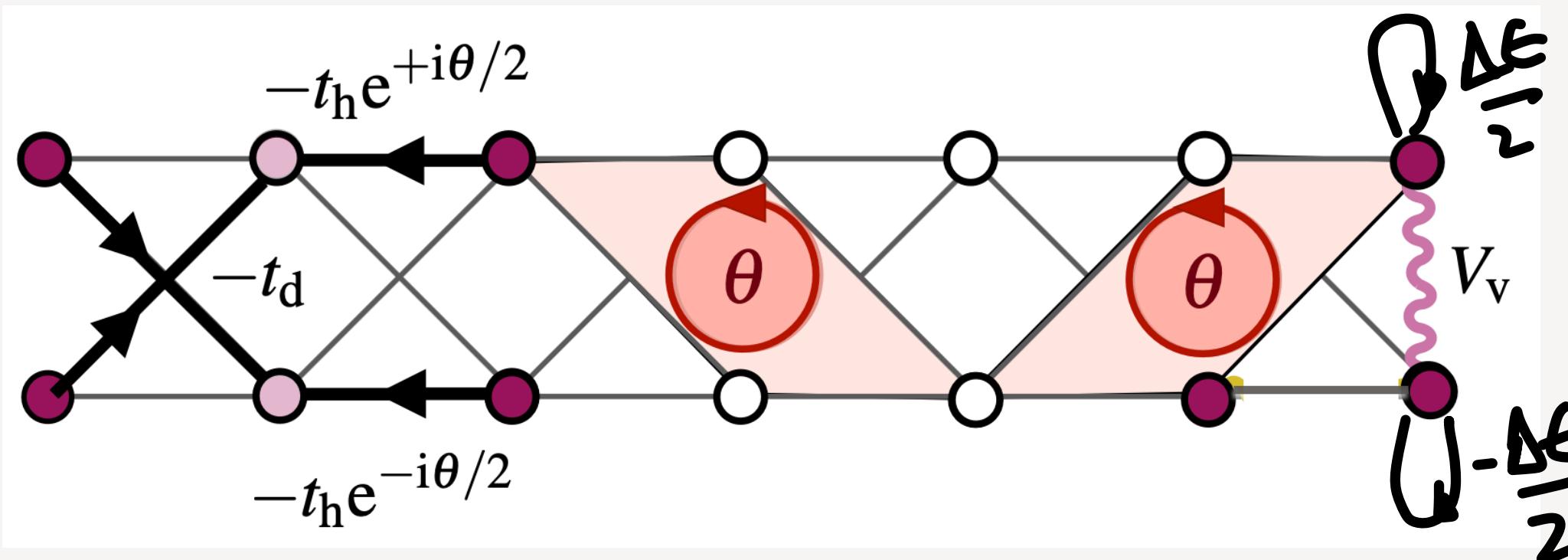
Wilson-type discretization

$$r_j \in \{0, 1\}$$



K. G. Wilson, in *New Phenomena in Subnuclear Physics* (1977)

d=1, N=1, Unitarily equivalent to an imbalanced cross-linked ladder pierced by a U(1) field



$$N=1, \theta=\pi$$

$\pi$ -flux ladder

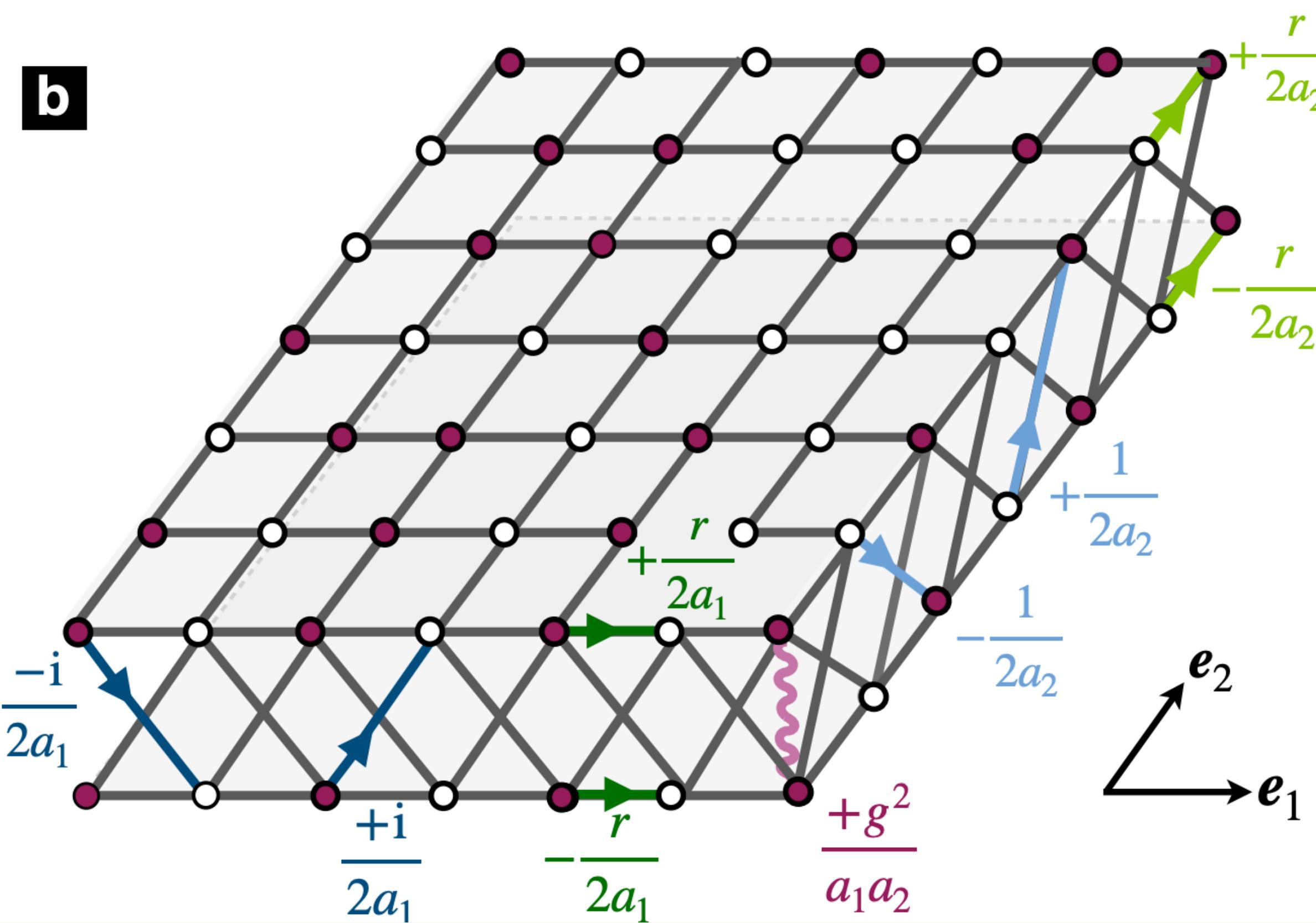
$$t_d = t_{\pm} = \frac{1}{2a},$$

$$ma = \frac{\Delta\epsilon}{4t_{\pm}} - r,$$

$$\frac{q^2}{2} = \frac{V_0}{4t_{\pm}}$$

# Wilson lattice regularization in d+1 dimensions

d=2, N=1, equivalent to an imbalanced cross-linked bilayer , again with Hubbard interactions



Intra-layer tunneling along  $\hat{e}_j$

$$t_j = \pm r/2a_j$$

+  $\rightarrow$   $\uparrow$  layer

-  $\rightarrow$   $\downarrow$  layer

Inter-layer tunneling along  $\hat{e}_j$

$$\tilde{t}_1 = \pm i/2a_1$$

$$\tilde{t}_2 = \pm 1/2a_2$$

Inter-layer

Hubbard interaction

$$g^2 = \frac{V_0}{4|\tilde{t}_1 \tilde{t}_2|}$$

$$ma = \frac{\Delta E}{4|\tilde{t}_1 \tilde{t}_2|} - (r_1 + r_2 \beta_2)$$

$$\beta_2 = a_1/a_2$$

# SPT phases in D=1+1 dimensions

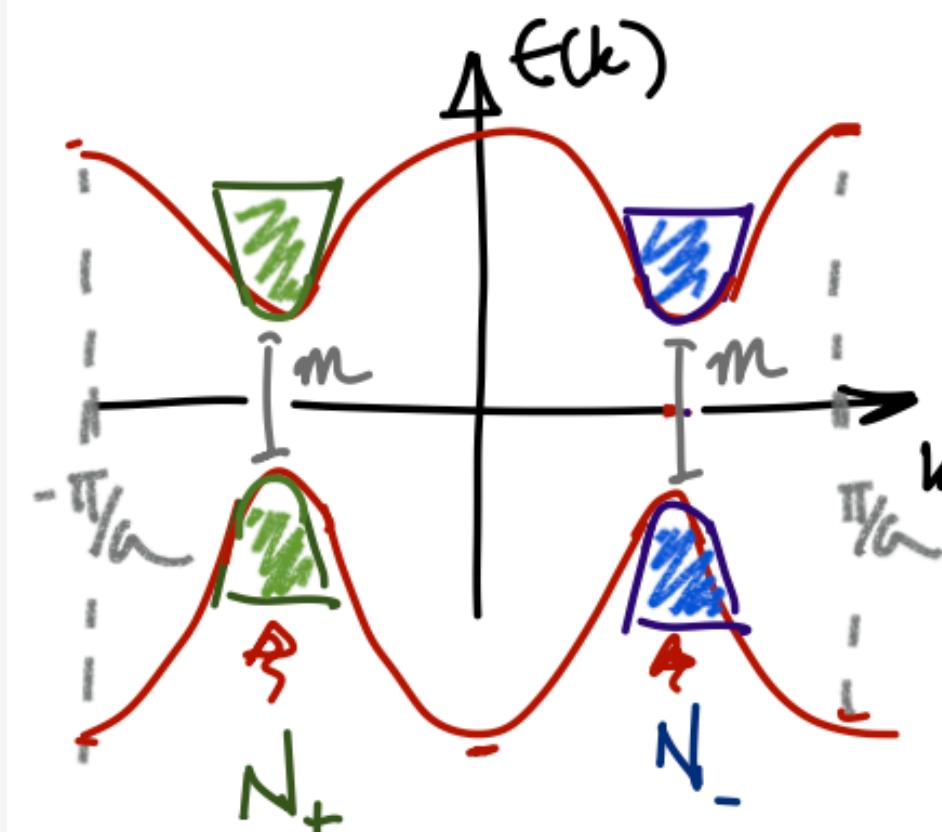
This discretization can host symmetry-protected topological groundstates

$$H_C = -\sum_{i,\ell} \left( t_h e^{-i \frac{s_\ell \theta}{2}} c_{i+1,\ell}^\dagger c_{i,\ell} + t_d c_{i+1,\ell}^\dagger c_{i,\bar{\ell}} - \frac{s_\ell \Delta \epsilon}{2} c_{i,\ell}^\dagger c_{i,\ell} + \text{H.c.} \right),$$

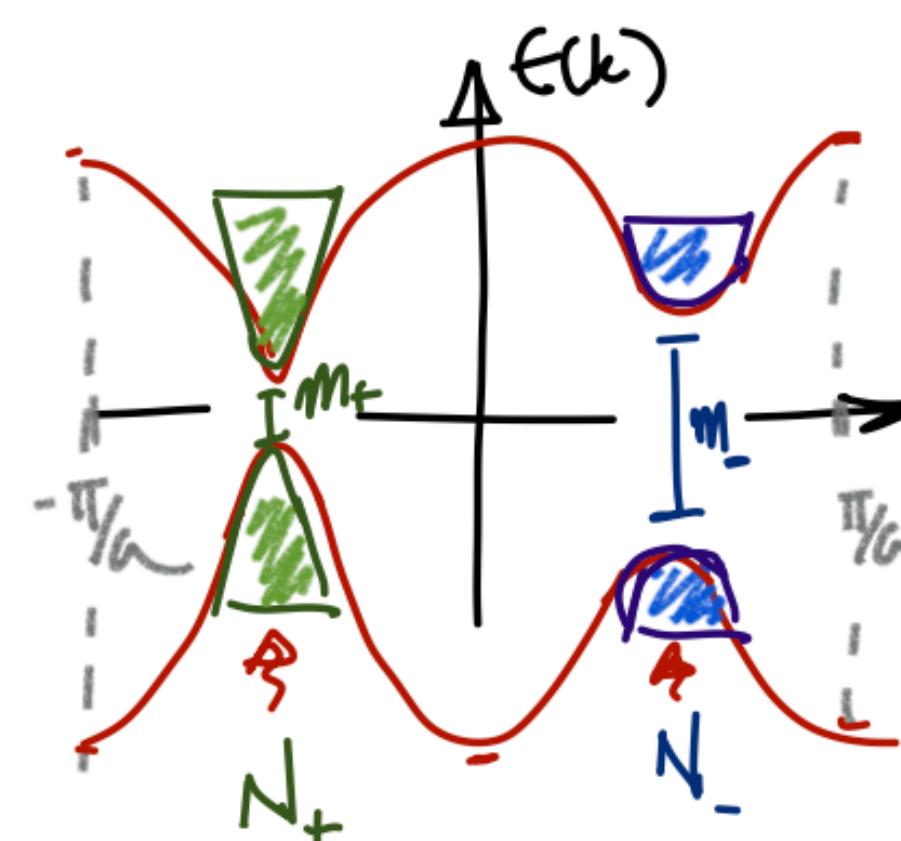
$$H_{CH} = H_C + \frac{V_v}{2} \sum_{i,\ell} c_{i,\bar{\ell}}^\dagger c_{i,\ell}^\dagger c_{i,\ell} c_{i,\bar{\ell}},$$

Imbalanced  $\nrightarrow$  interacting version of Creutz's ladder

Naïve



Wilson  $\theta=\pi$



th M. Creutz, Phys. Rev. Lett. 83, 2636 (1999).

$$\left. \begin{aligned} m_+ a &= \frac{\Delta \epsilon}{4t_h} - r \\ m_- a &= \frac{\Delta \epsilon}{4t_h} + r \end{aligned} \right\}$$

momentum-dependent masses

AIII/BDI phases for non-vanishing Berry phase

$$\gamma_B = \frac{\pi}{2} (\text{sgn}(m_-) - \text{sgn}(m_+))$$

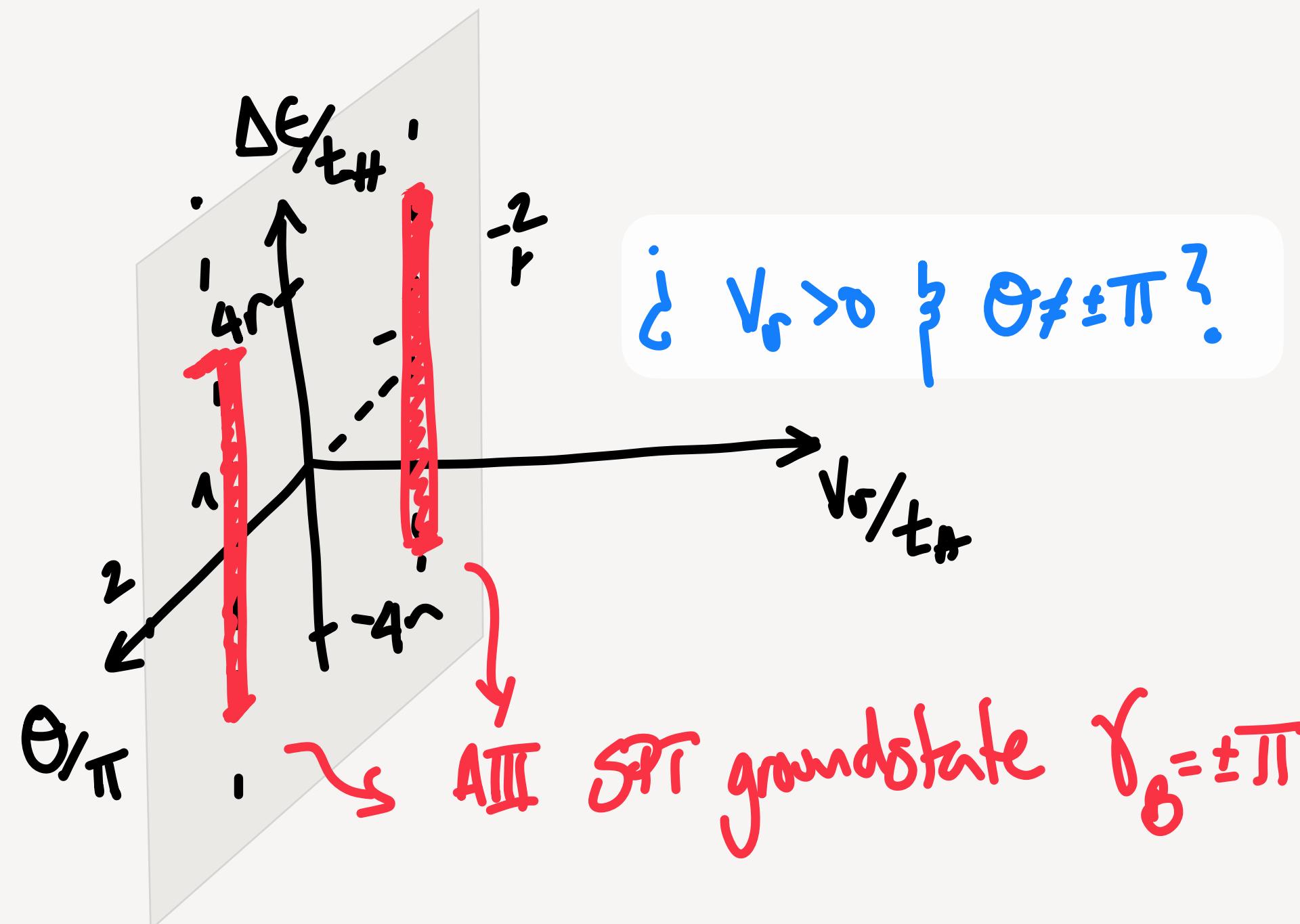
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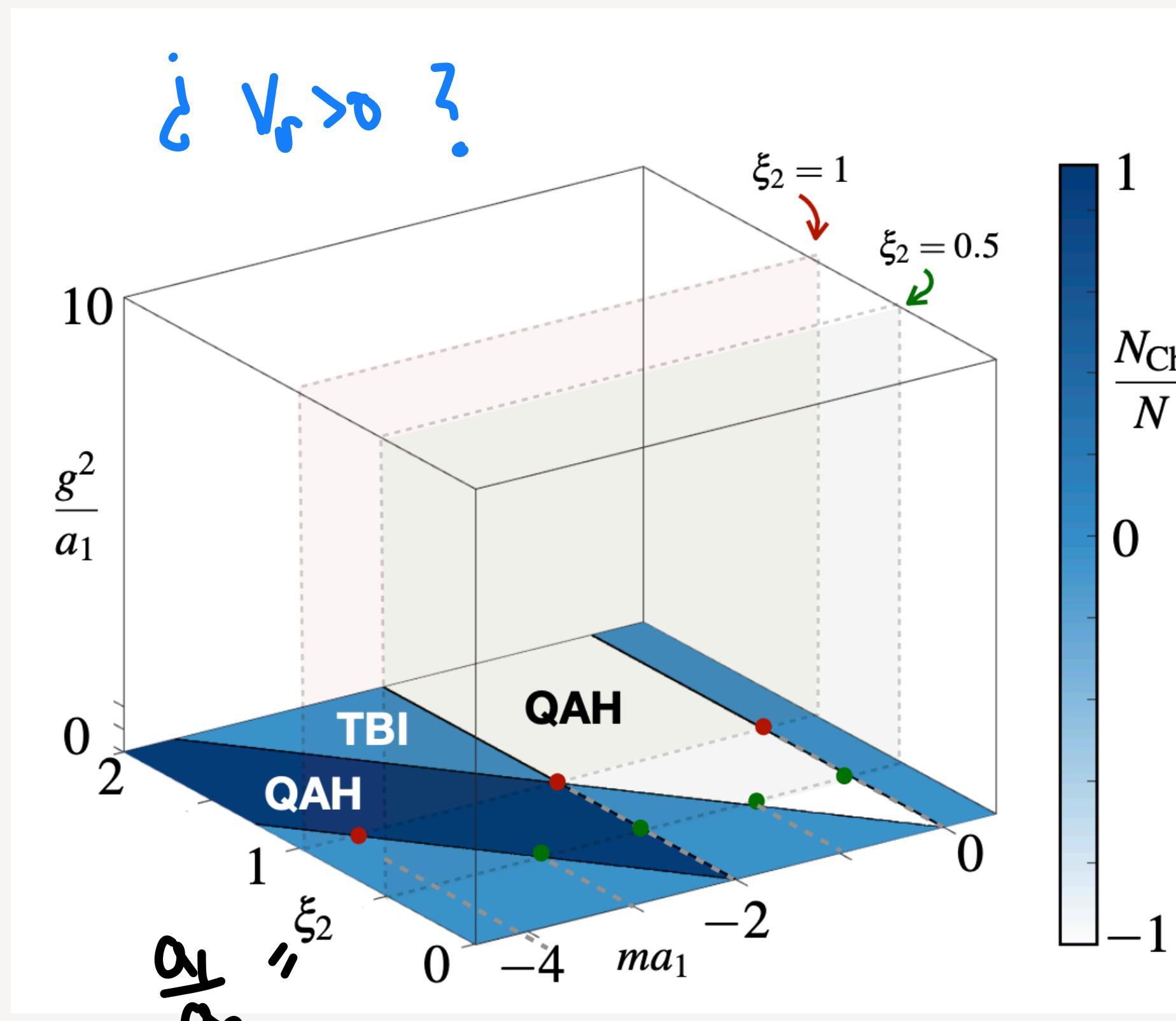
momentum-dependent masses

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# Chern insulators in D=2+1 dimensions

This discretization can host an quantum anomalous Hall (QAH) effect



momentum-dependent  
Wilson masses

$$\bar{n}_d \in \mathbb{Z}_2 \times \mathbb{Z}_2$$

th D. Haldane, Phys. Rev. Lett. 61, 2015 (1988).

M. Golterman, K. Jansen, and D. Kaplan, PLB 301, 219 (1993).

$$m_{\mathbf{n}_d} = m + \frac{2r_1}{a_1} n_{d,1} + \frac{2r_2}{a_2} n_{d,2}.$$

bilayer version of Haldane's

QAH

Non-vanishing Chern numbers

$$N_{\text{Ch}} = \frac{N}{2} \sum_{\mathbf{n}_d} (-1)^{(n_{d,1} + n_{d,2})} \text{sign}(m_{\mathbf{n}_d}).$$

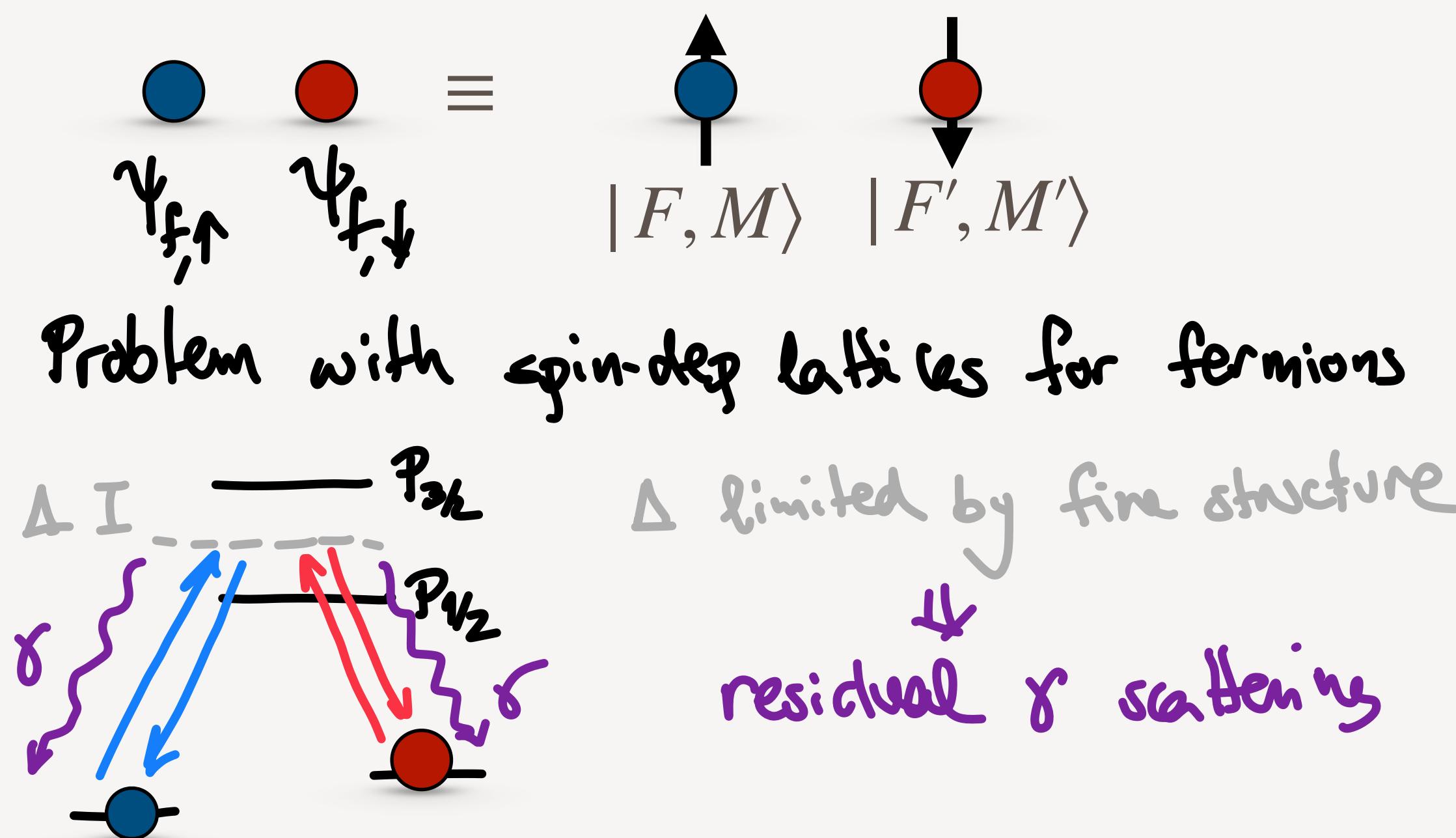
# Cold-atom regularization: photon-assisted tunneling

Dirac spinor as two hyperfine states  
of a neutral Fermi gas, e.g.  $^{87}\text{Sr}$

+

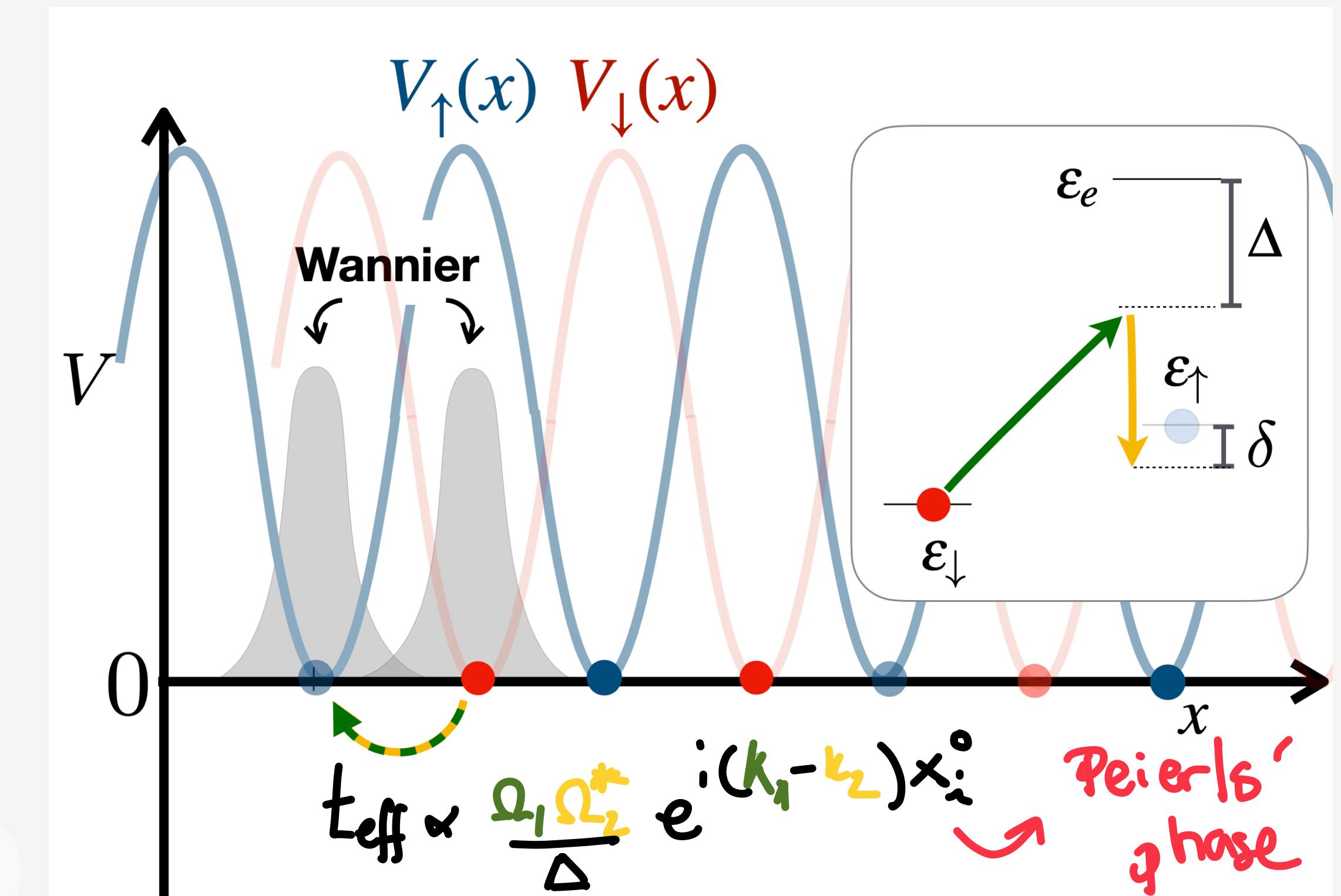
Raman-assisted tunneling in spin-dependent lattices

th D. Jaksch, P.Zoller, New J. Phys. 5, 56 (2003).



Alternatives based on e.g. Floquet instead of Raman

ex M. Aidelsburger, et al., PRL 111, 185301 (2013).



# Cold-atom regularization: Raman lattices

The advantage is that we need both spin-conserving and spin-flipping tunneling

# Avoid spin-dependent lattices

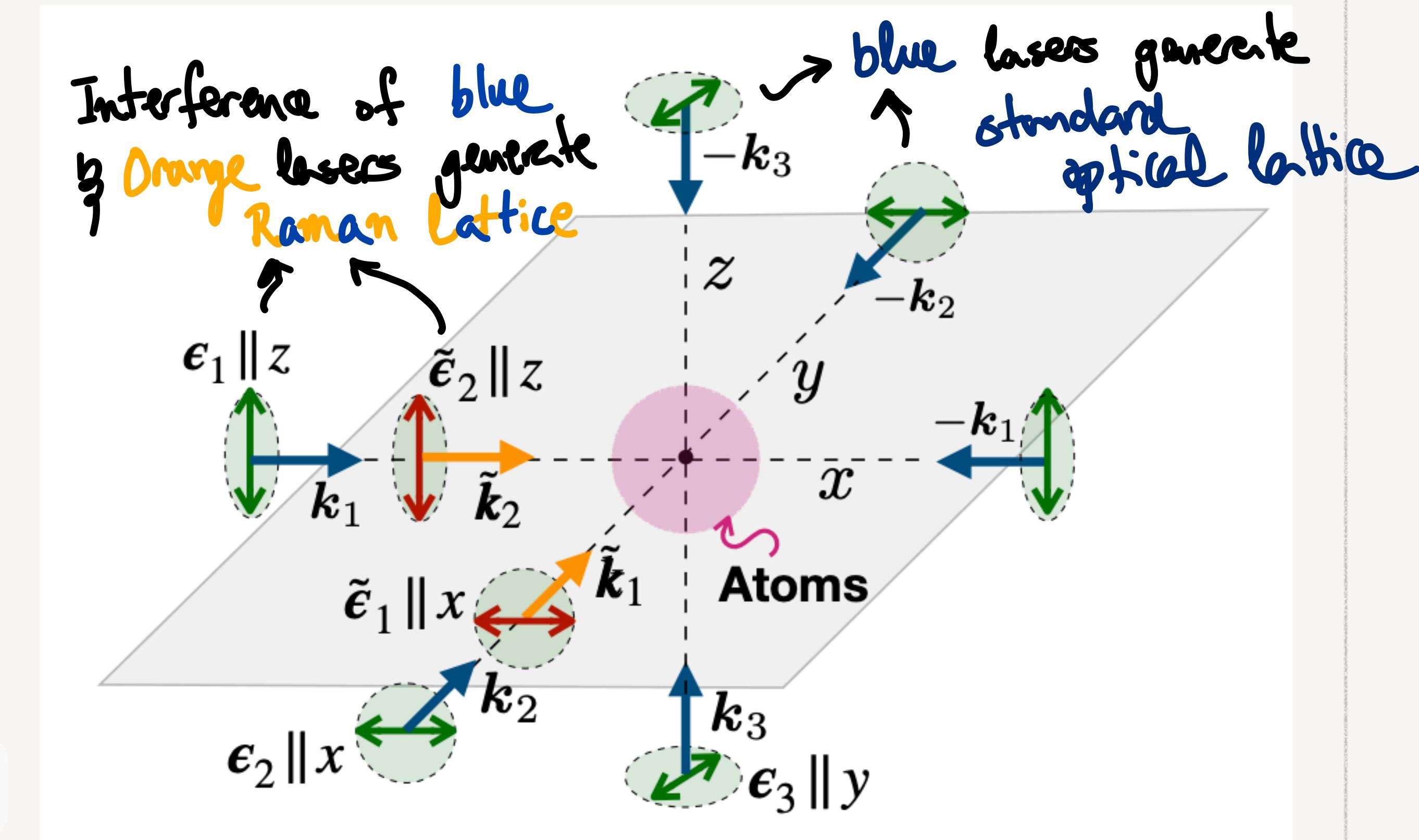
A red icon of a hand with fingers spread, pointing towards the right side of the page.

# The standard & cross-link tunnelings provided by a Raman optical lattice



# Recent experiment with fermions

 M.-C. Liang, et al., arXiv:2109.08885



L. Zhang and X.-J. Liu, *Synthetic Spin-Orbit Coupling in Cold Atoms*, pp. 1-87 (World Scientific 2018)

# Cold-atom regularization: Raman lattices

The spin-conserving tunnelings stem from the standard lattice  $t_j$

The spin-flipping terms benefit from the doubled period of the Raman potential

No local spin flips

$$\int d^3x w(x - x_i^0) \frac{\tilde{V}_{0,1}}{2} \cos(\tilde{k}_1 \cdot x) w(x - x_i^0) = 0.$$

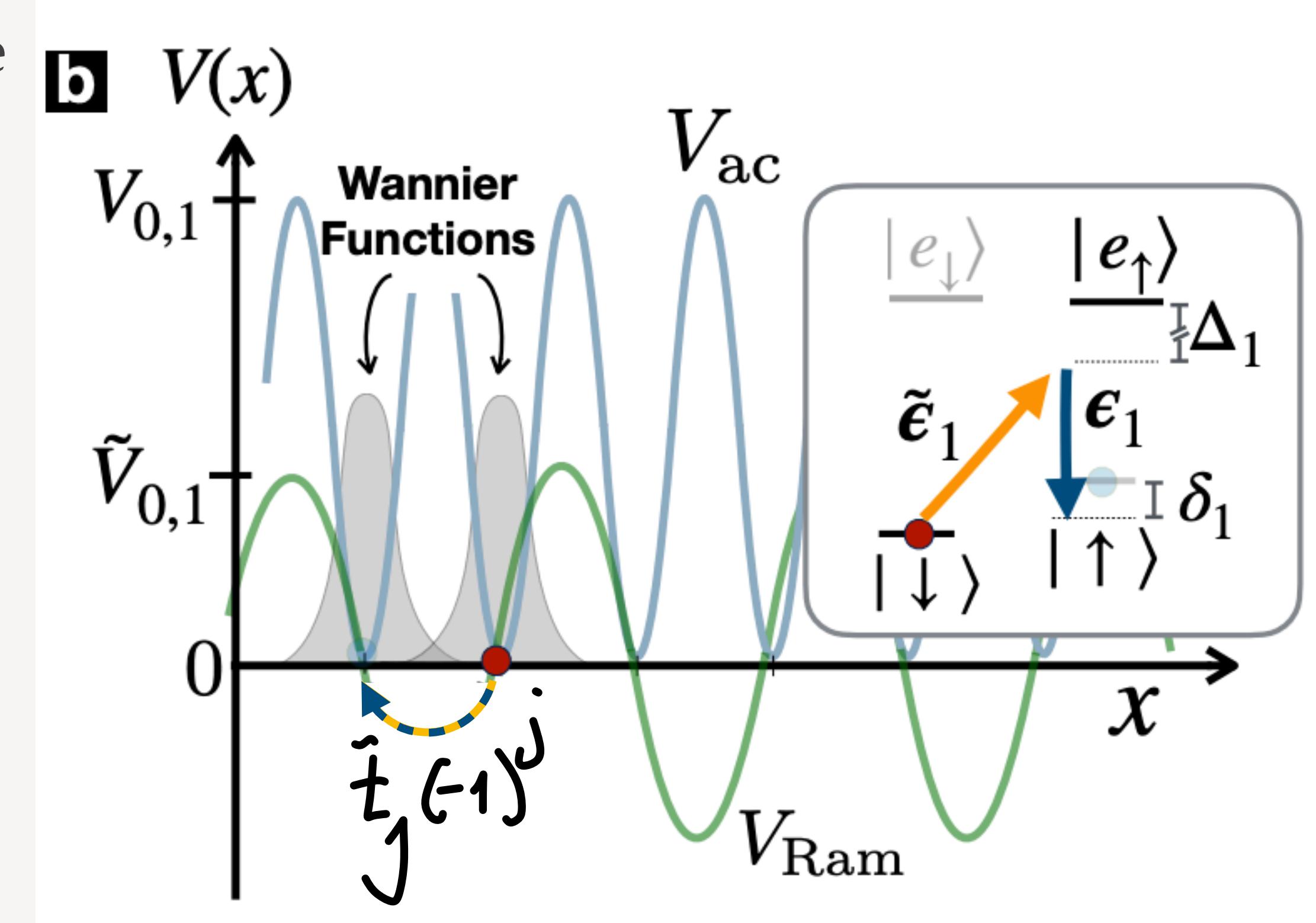
Alternating spin-flip tunneling

$$\tilde{t}_j = \left| \int d^3x w(x - x_i^0) \frac{\tilde{V}_{0,1}}{2} \cos(\tilde{k}_1 \cdot x) w(x - x_{i+e_j}^0) \right| \neq 0$$

Cold-atom mapping

$$a_j = \frac{1}{2\tilde{t}_j}, \quad f_j = \frac{\tilde{t}_j}{\tilde{t}_j}, \quad m = \frac{f}{2} - 2(t_1 + t_2),$$

$$g^2 = \frac{U_{11}}{4f_1 f_2}, \quad U_{11} \propto a_{S-wave}$$



# Cold-atom regularization: Raman lattices

The non-interacting limit has been explored in cold-atom experiments

$N_a \approx 10^4$   $^{87}\text{Sr}$  @  $0.2\mu\text{K}$

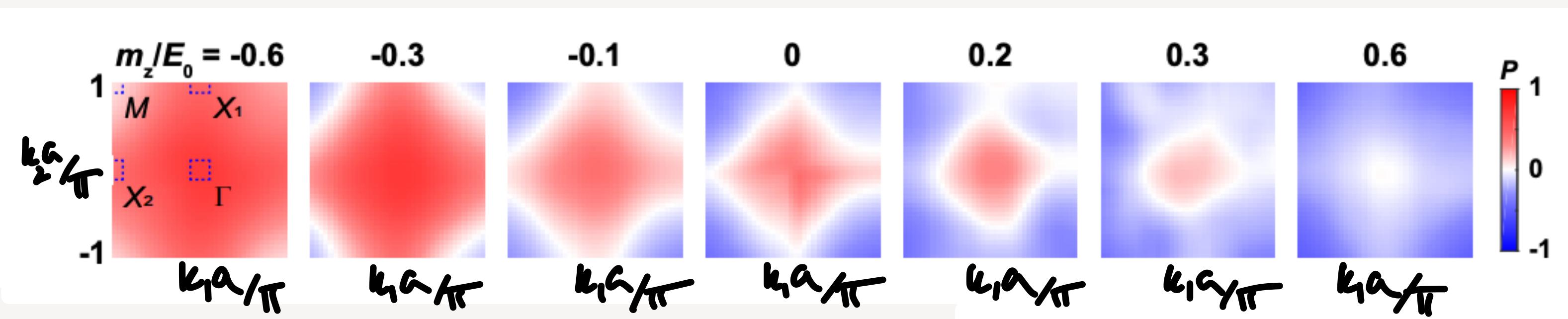
ex M.-C. Liang, et al., arXiv:2109.08885

Spin-resolved TOT

$$n_{\uparrow}(\vec{k}), n_{\downarrow}(\vec{k})$$

Polarization

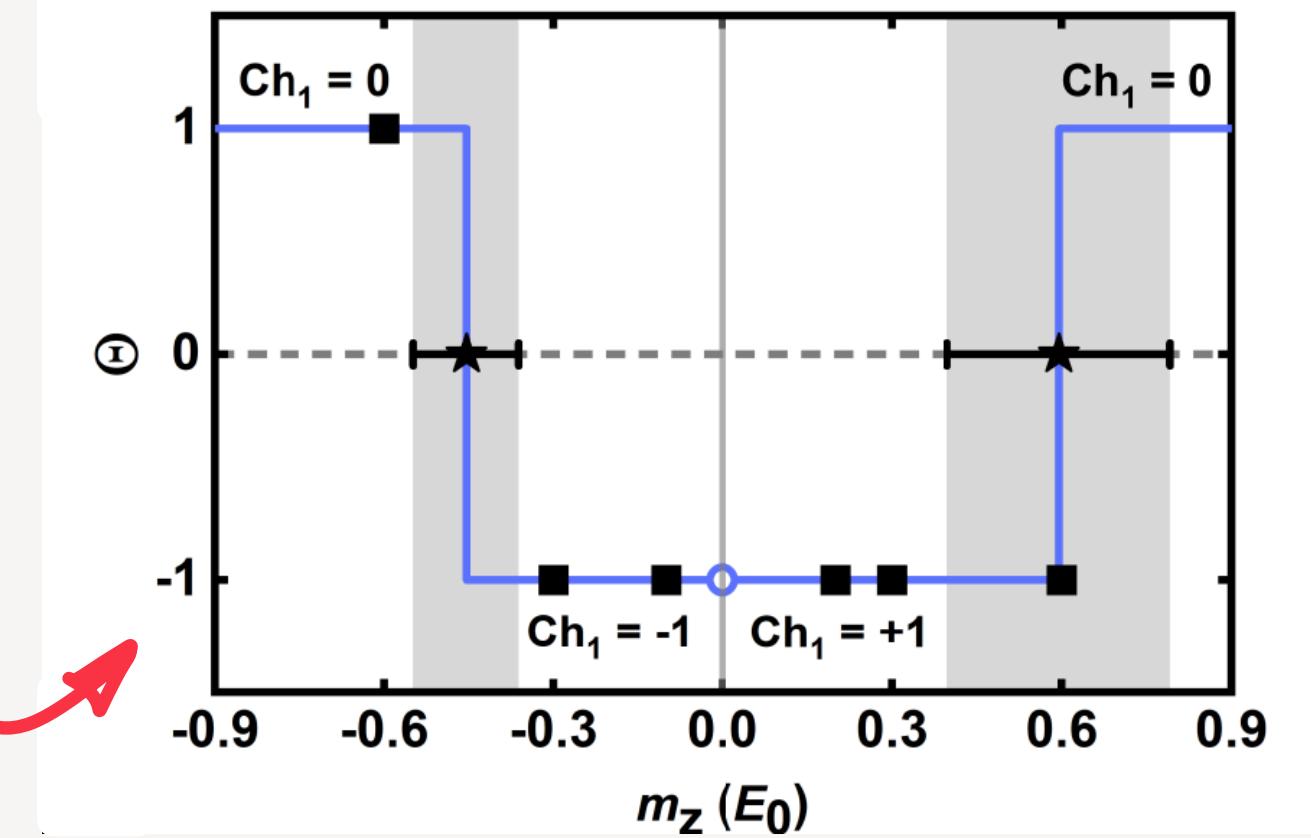
$$P_{\vec{k}} = \frac{n_{\uparrow}(\vec{k}) - n_{\downarrow}(\vec{k})}{n_{\uparrow}(\vec{k}) + n_{\downarrow}(\vec{k})}$$



$$\Theta = \text{sgn}(P(\Gamma) \cdot P(X_2) \cdot P(X_1) \cdot P(M))$$

center, corner, faces of BZ  
doublers

equivalent to  $\text{Ch}_1$  number



# Cold-atom regularization: Raman lattices

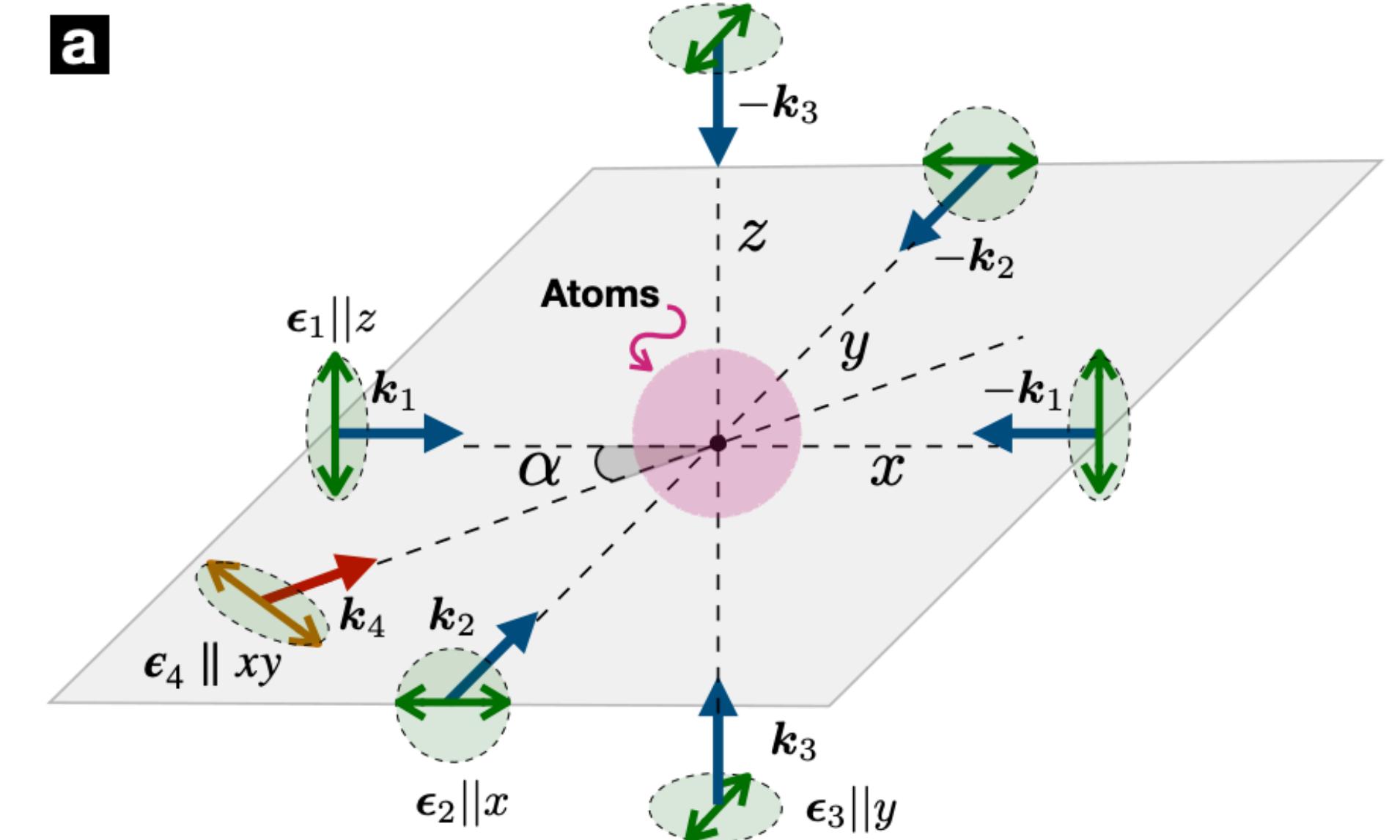
The interacting limit could be explored by tuning Feshbach resonances

*as-wave (Best)*

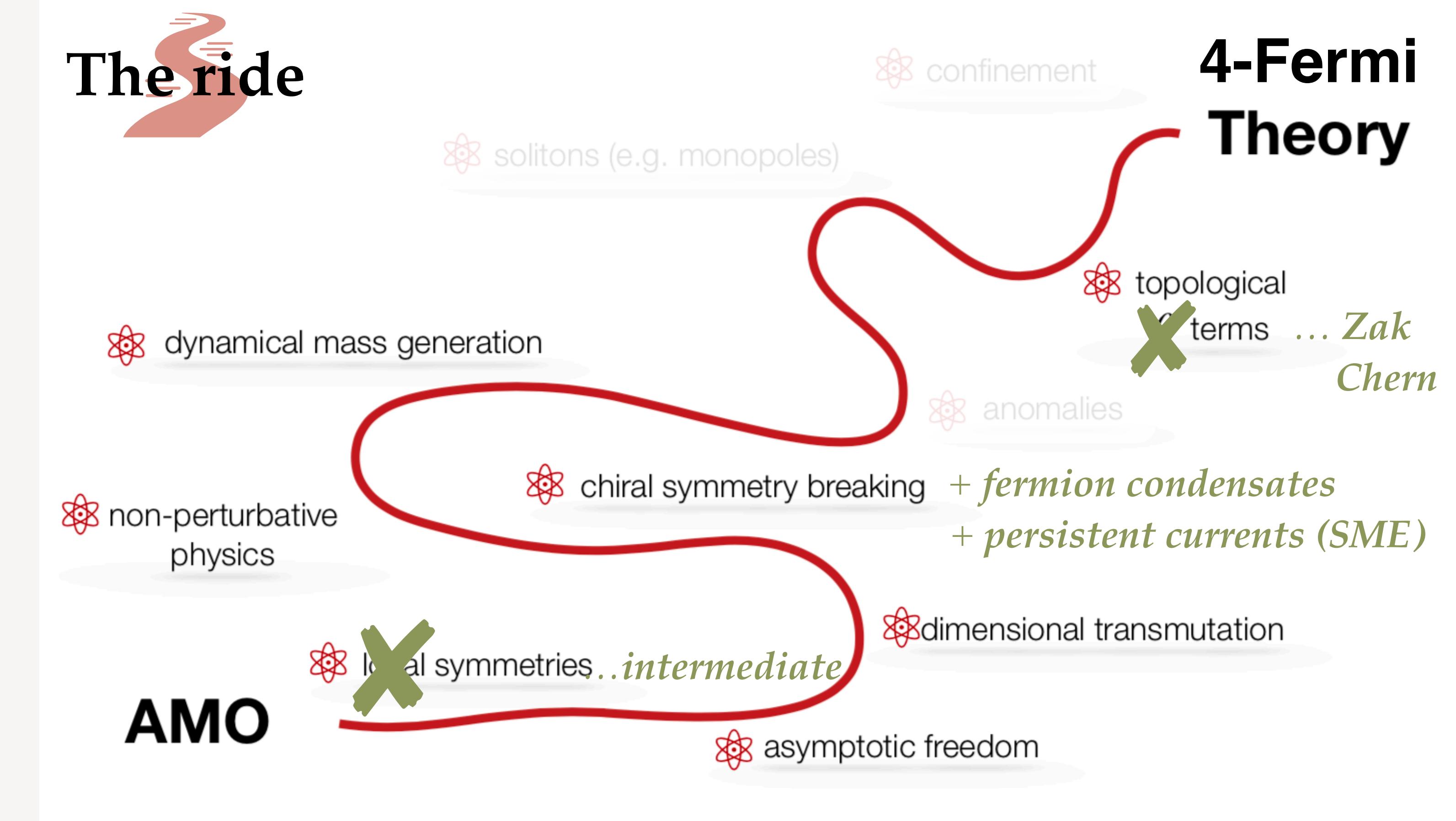
$$g^2 \alpha V_r \propto k_L a_{\text{S-wave}}(B_{\text{ext}}) \rightarrow V_r > 0 ?$$

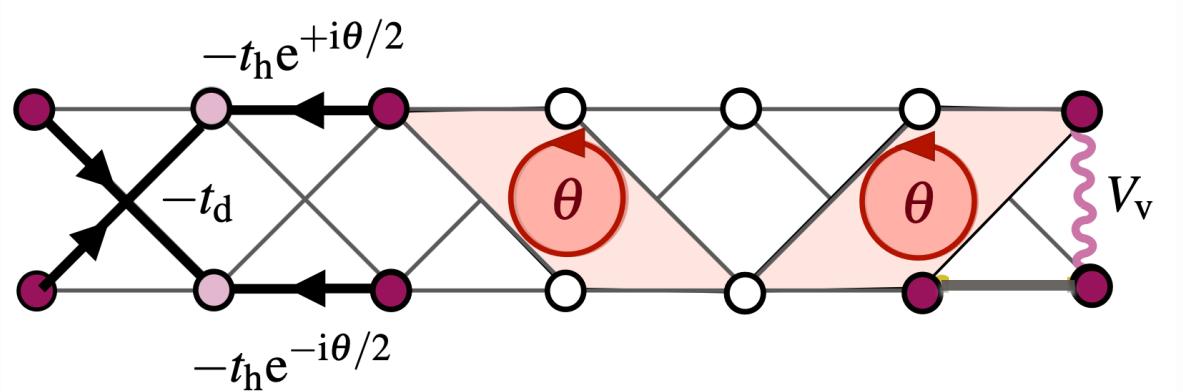
One could tilt the Raman beams  
to induce a  $U(1)$  gauge field (away from pi-flux)

$$\theta = \pi \left( 1 + \frac{k_3 \cos \alpha}{k_4} \right) \rightarrow \theta \neq \pm \pi ?$$



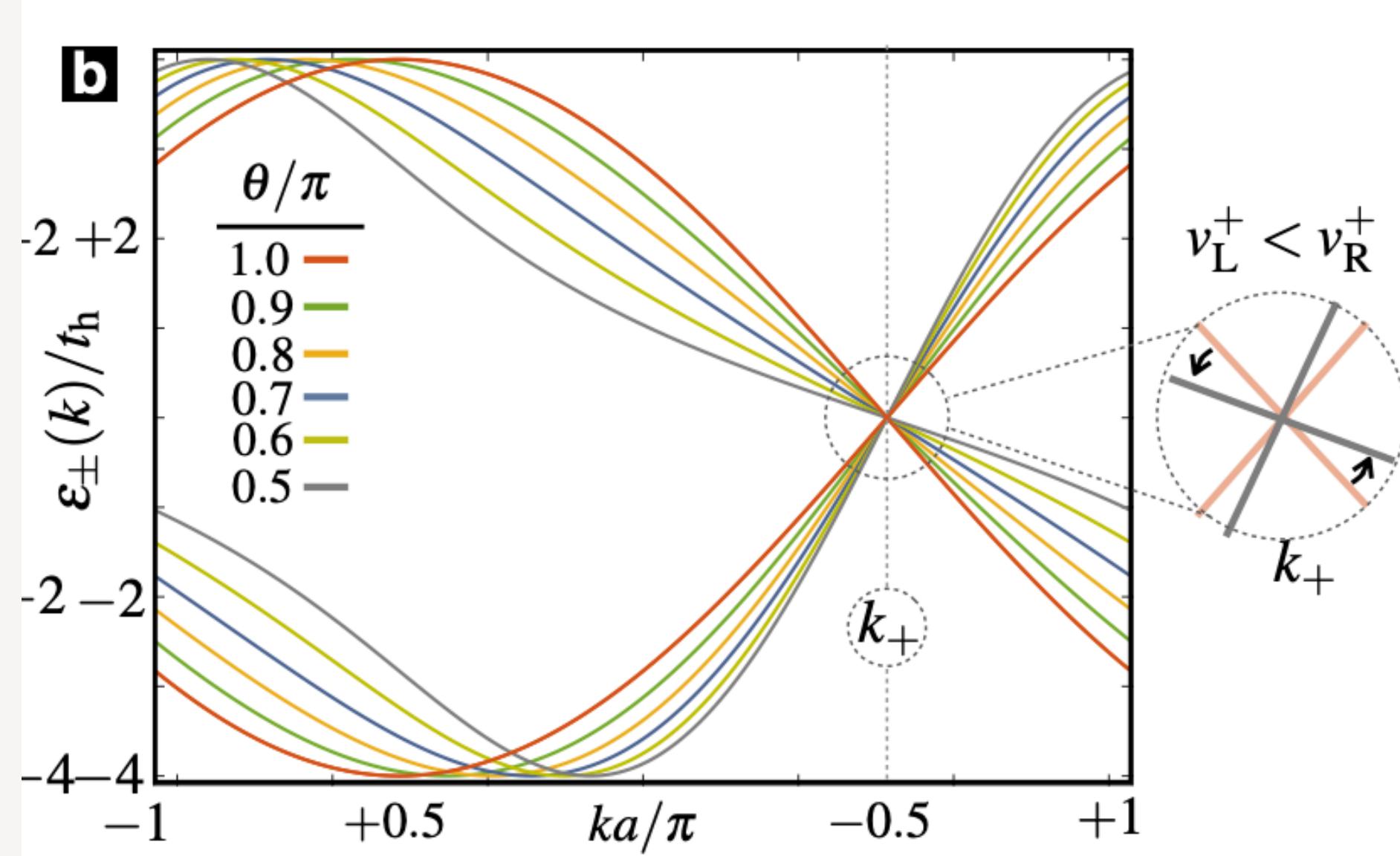
# MOTIVATION





The continuum limit now described by  
Dirac QFT with Lorentz violation

**th** Colladay, Kostelecky, PRD 58, 116002 (1998)



# Lorentz violations @ generic $\theta$

$$S_{\text{CH}} = \int d^2x \left( \sum_{\eta=+,-} \bar{\Psi}_\eta(x) (ic\Gamma_\eta^\mu \partial_\mu - m_\eta c^2) \Psi_\eta(x) \right)$$

SME: Lorentz violation  
modifies Dirac  $\gamma^\mu$

$$\Gamma_\eta^\mu = \gamma_\eta^\mu + c_\eta^{\mu\nu} g_{\mu\tau} \gamma_\eta^\tau.$$

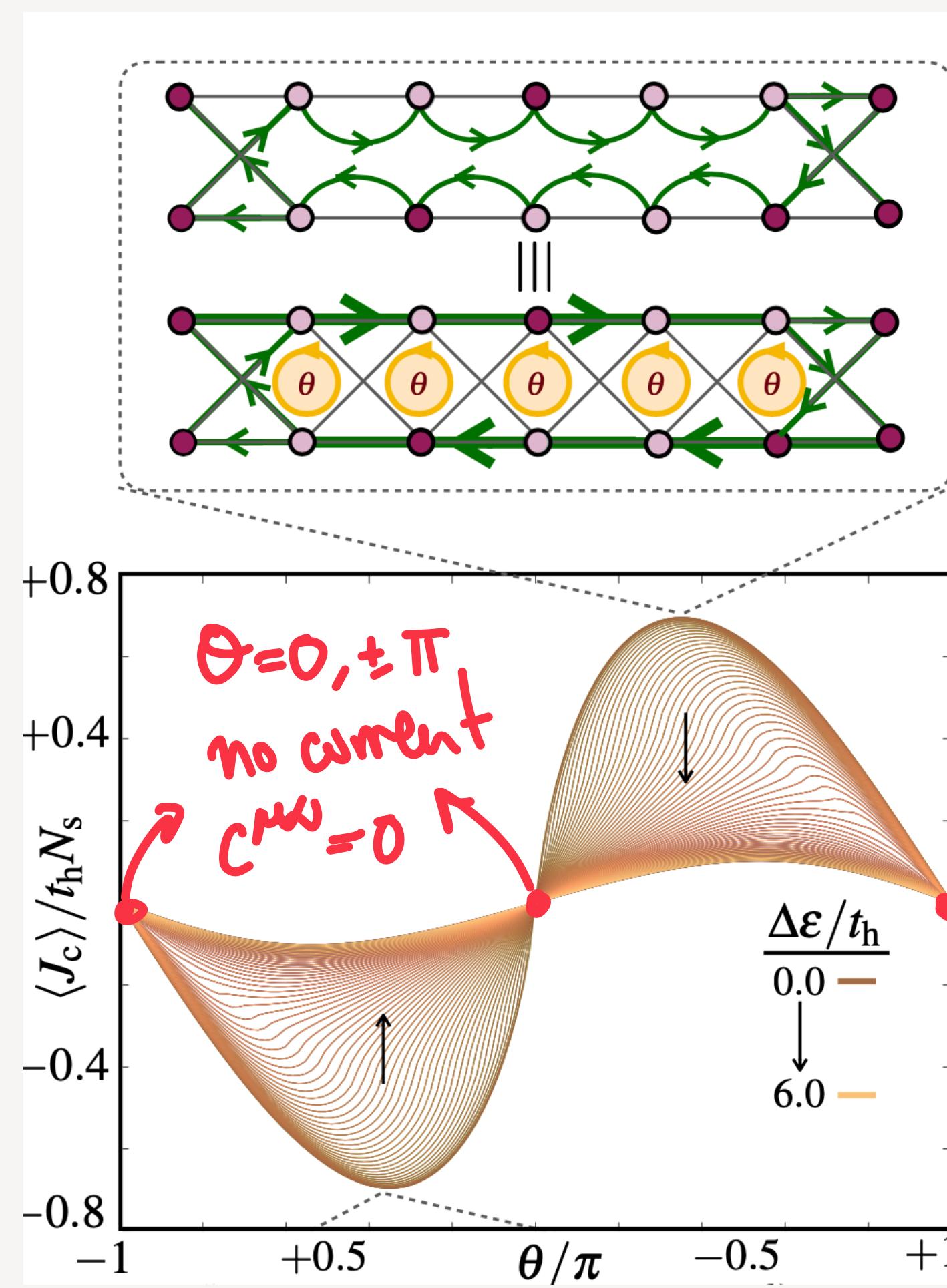
SME: tr-less  
tensor  $C^{\mu\nu}$

$$c_\pm^{\mu\nu} = \begin{cases} \pm \cos(\frac{\theta}{2}) & \text{if } \mu = 1, \nu = 0 \\ 0 & \text{else,} \end{cases}$$

This specific form amounts to diff.  $v_R/v_L$

$$v_R^\pm = 2t_h a \left( 1 \pm \cos \left( \frac{\theta}{2} \right) \right), \quad v_L^\pm = 2t_h a \left( 1 \mp \cos \left( \frac{\theta}{2} \right) \right)$$

# Persistent circulating 'chiral' currents @ generic $\theta$



Different R/L-moving velocities suggest possible net flow

"chiral" current

$$J_c = \sum_j \left( i t_h e^{i \frac{\theta}{2}} c_{j+1,\uparrow}^\dagger c_{j,\uparrow} - i t_h e^{-i \frac{\theta}{2}} c_{j+1,\downarrow}^\dagger c_{j,\downarrow} + \text{H.c.} \right).$$

skipping orbits in QHE / screening Meissner current bosonic SF

$\langle J_c \rangle$  has been measured in neutral-atom standard ladders

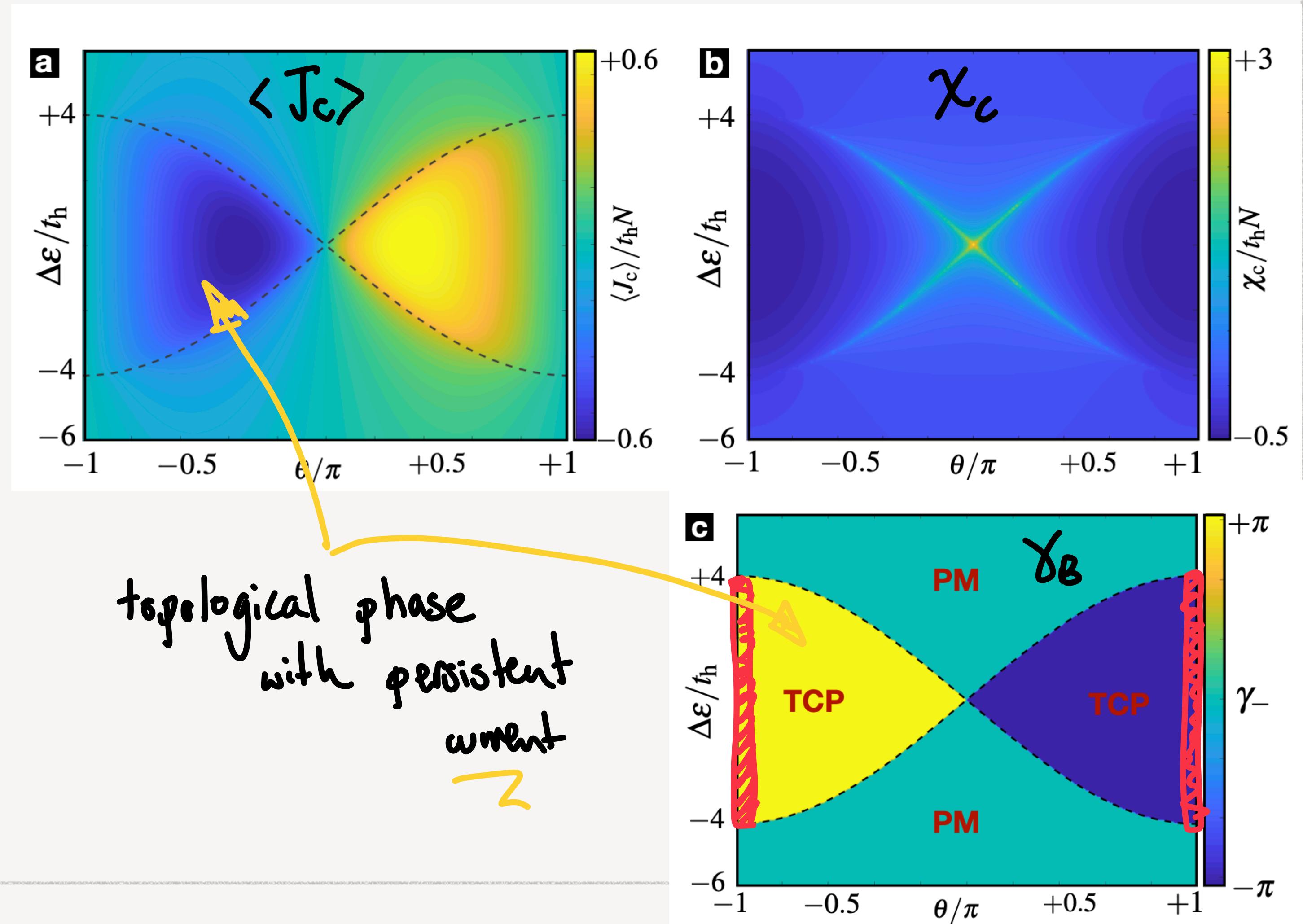
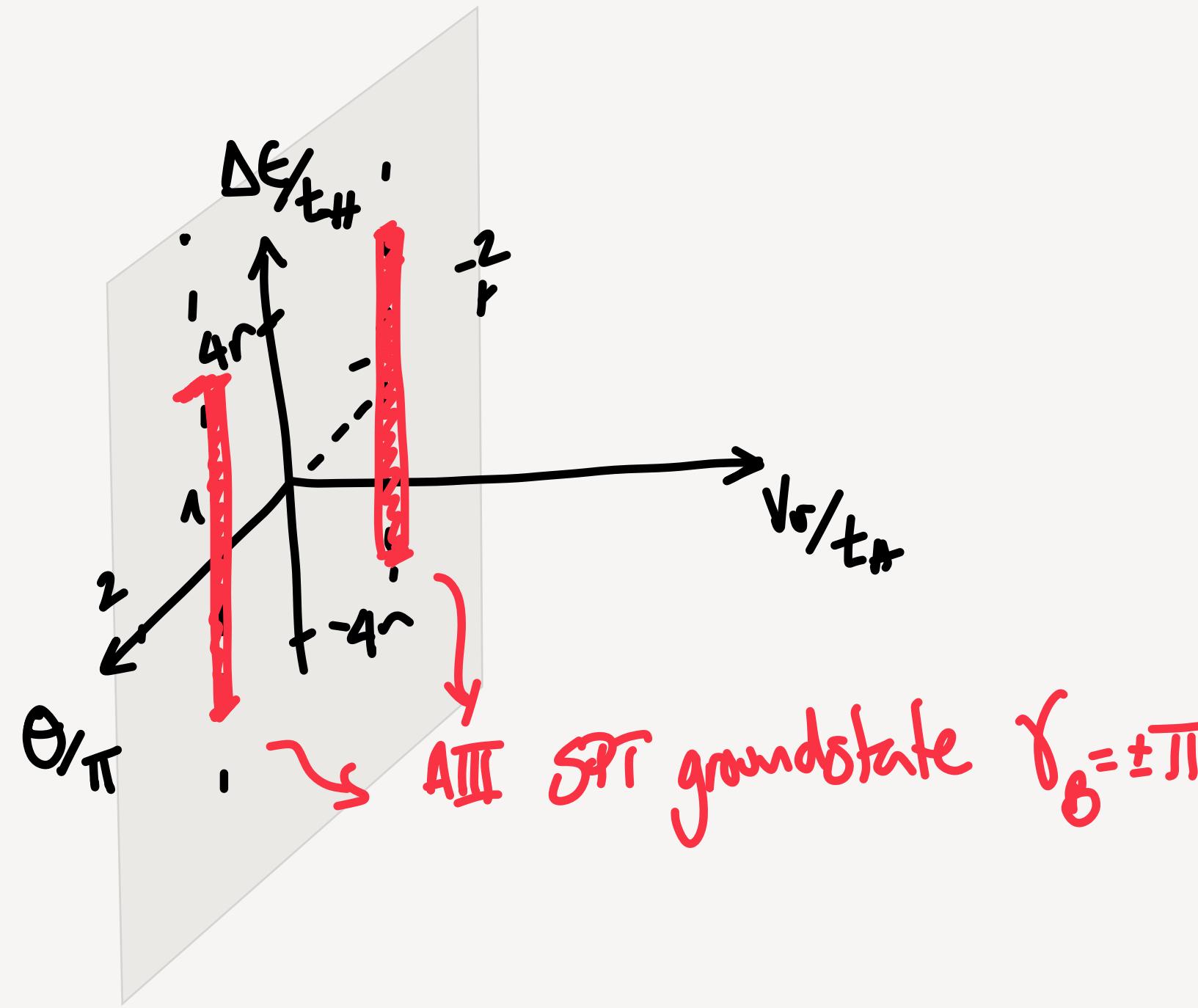
ex M. Atala, et al., Nat Phys 10, 588 (2014).

The "chiral" susceptibility  
can diverge @ critical points

$$\chi_c = \left\langle \frac{\partial J_c}{\partial \theta} \right\rangle$$

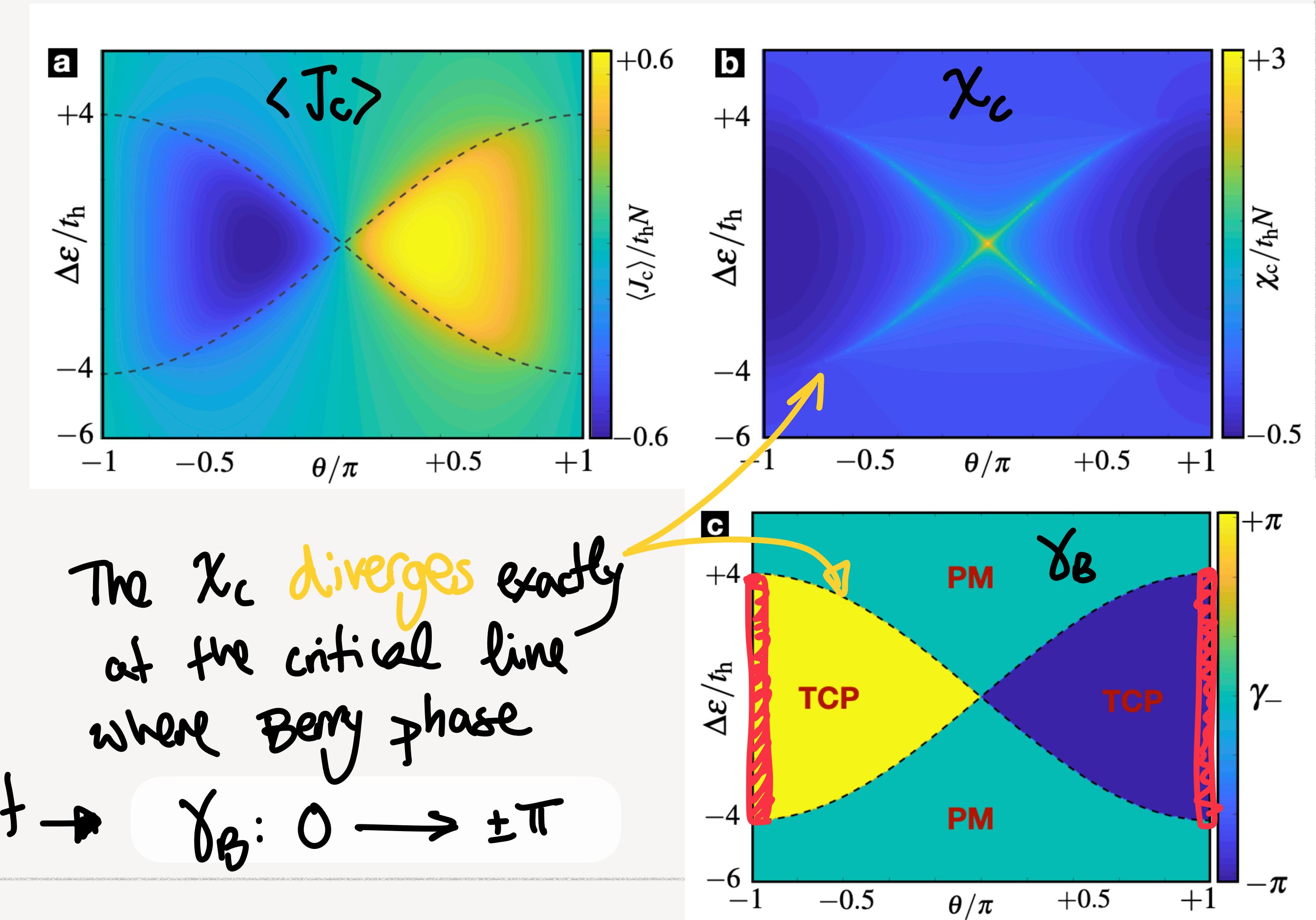
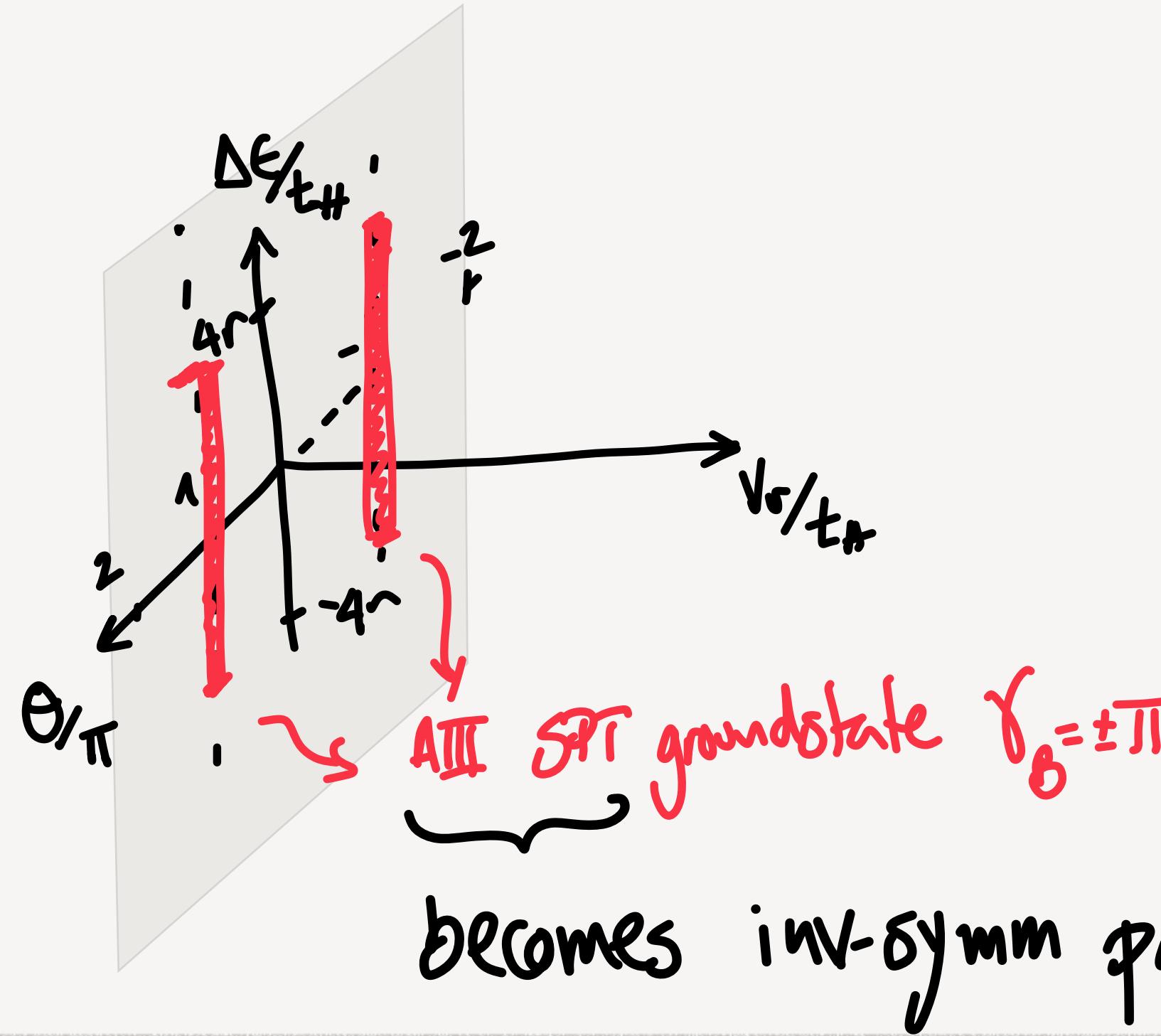
# Inversion-symmetry SPT @ generic $\theta$

Our goal was to understand  
the fate of SPT for  $\theta \neq \pm\pi$



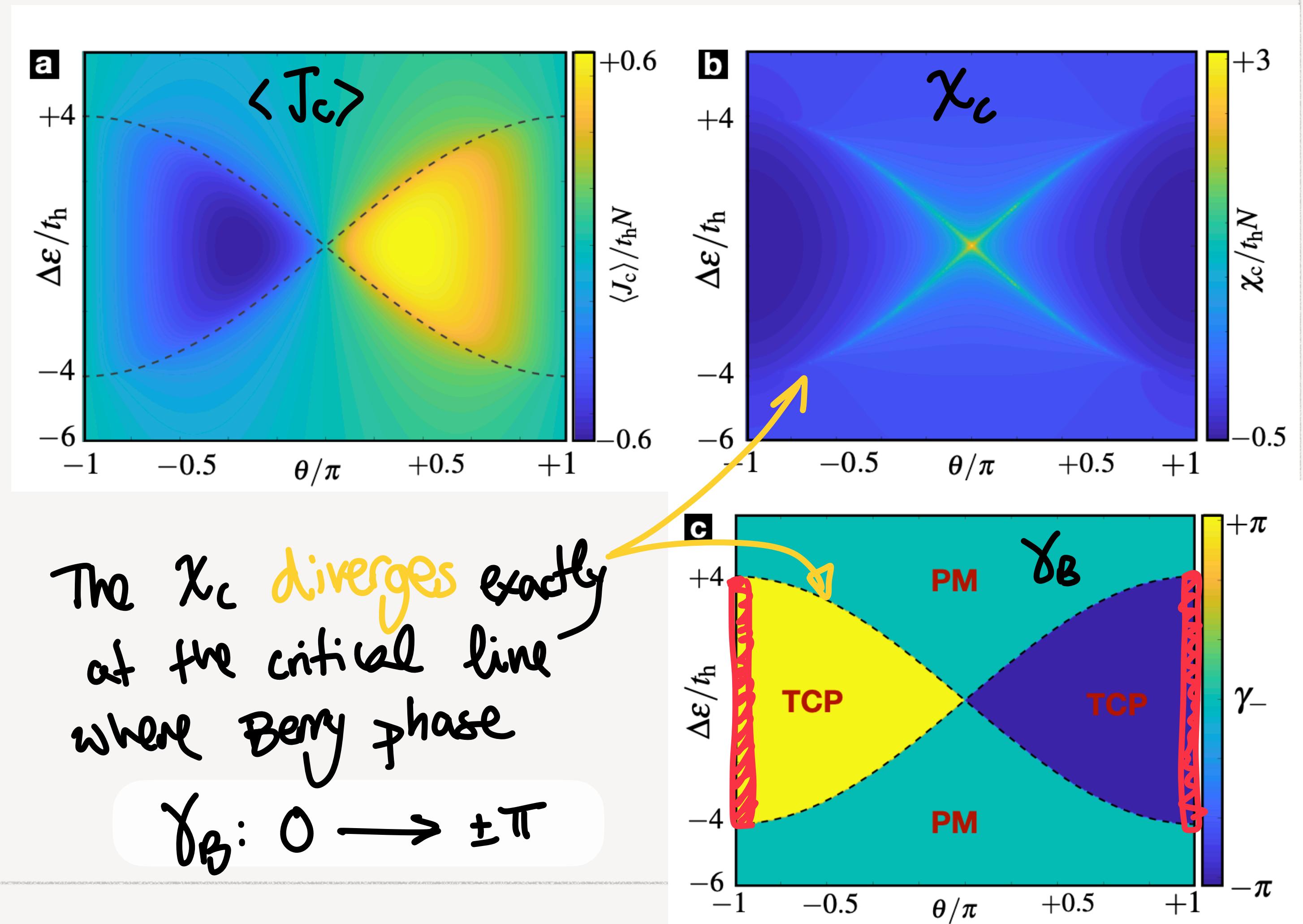
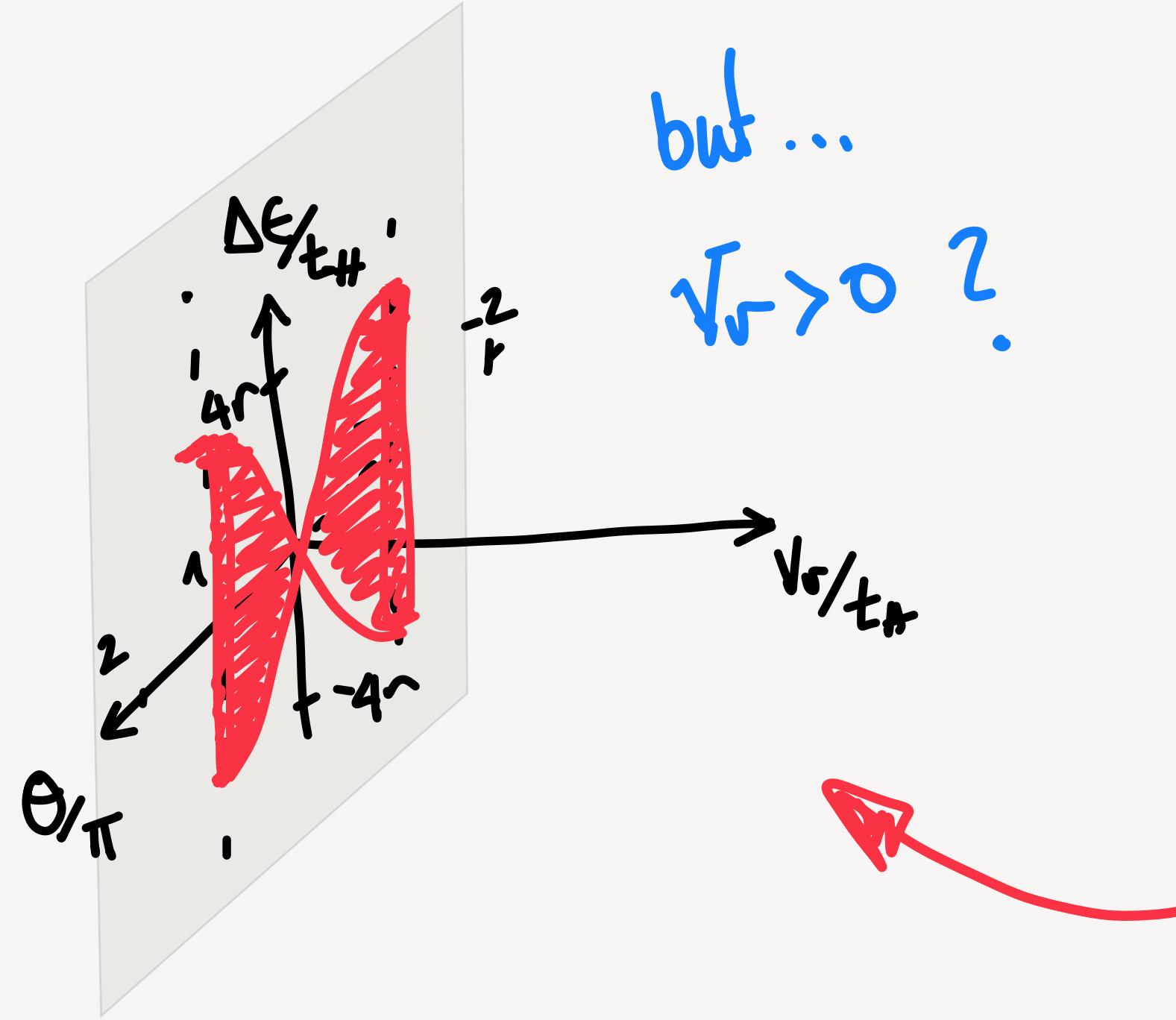
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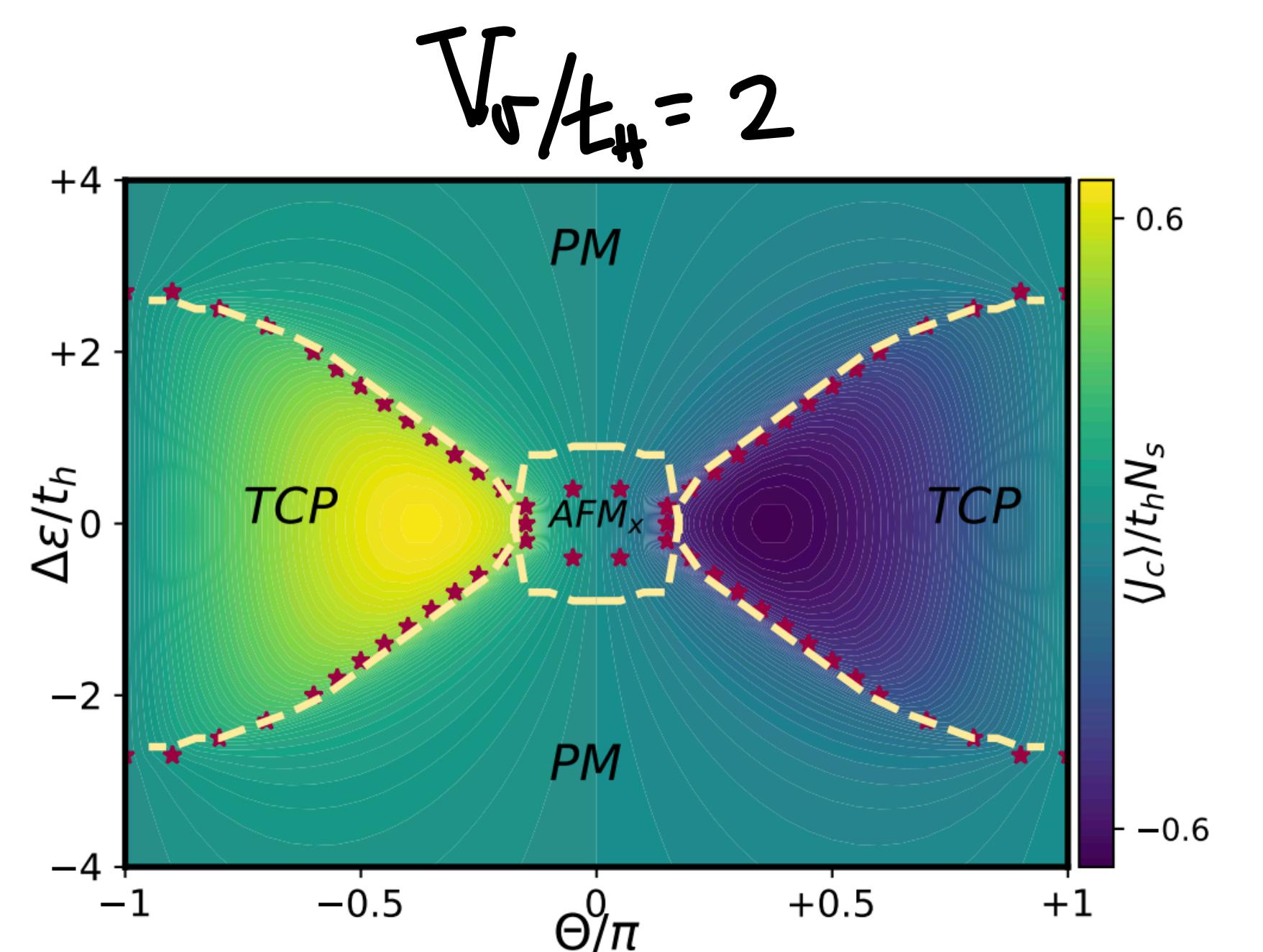
# Inversion-symmetry SPT @ generic $\theta$

Our goal was to understand  
the fate of SPT for  $\theta \neq \pm\pi$

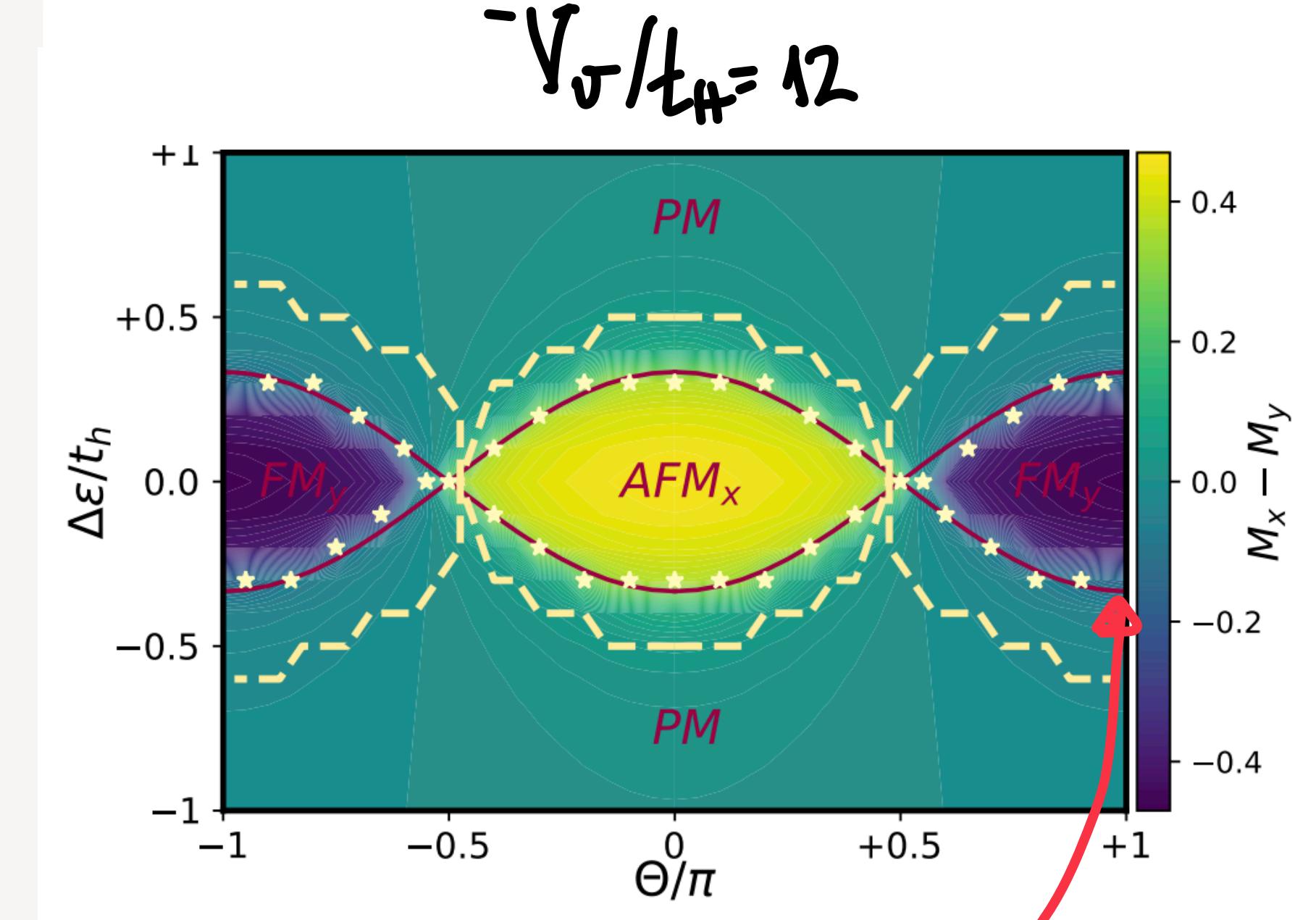


We use Hartree-Fock MFT ---  
 ↴ DMRG ★

# Orbital magnetism @ generic $\theta$



$V_0 \gg t_h$   
 Super-exchange  
 Dzyaloshinskii  
 Monya

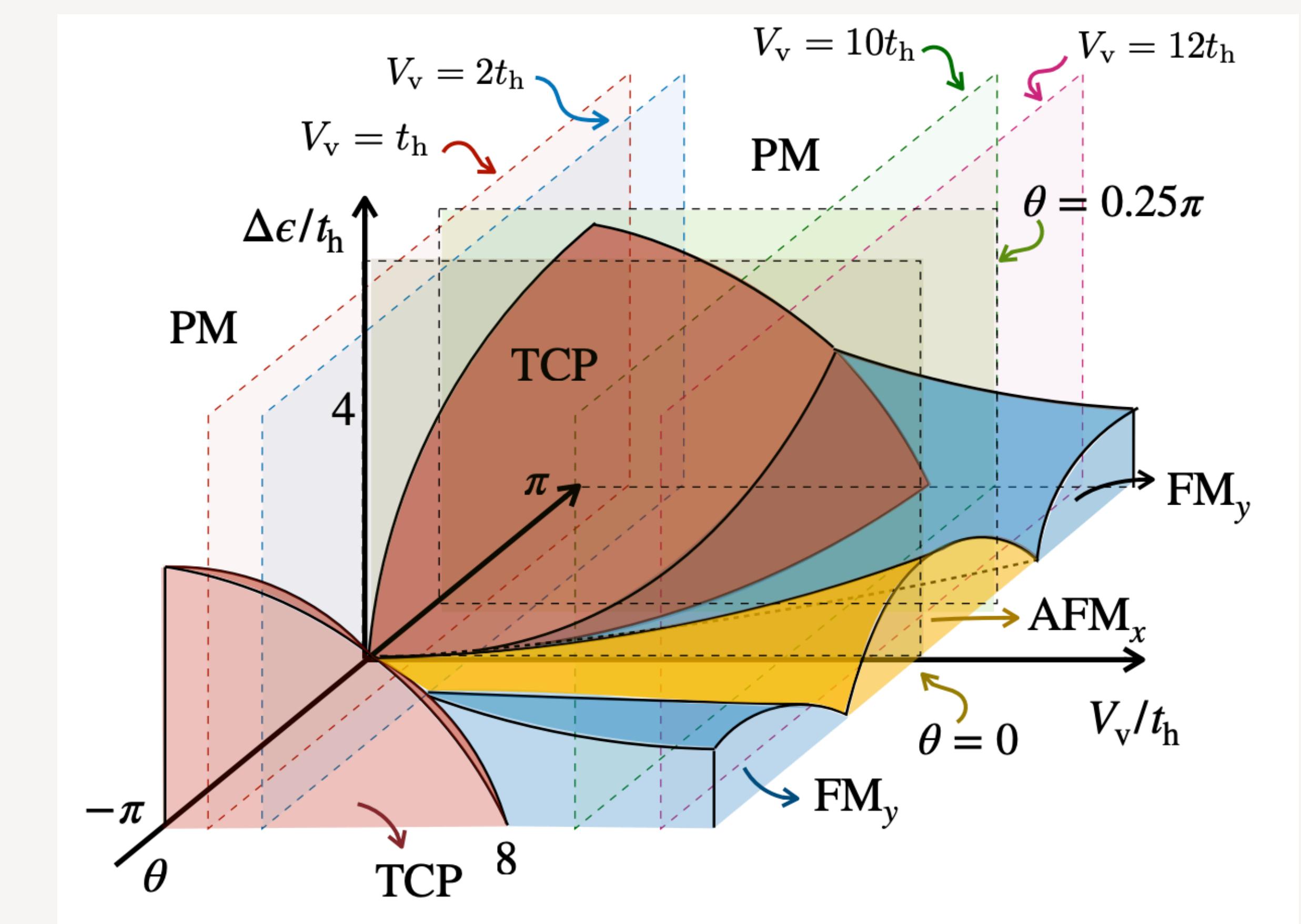
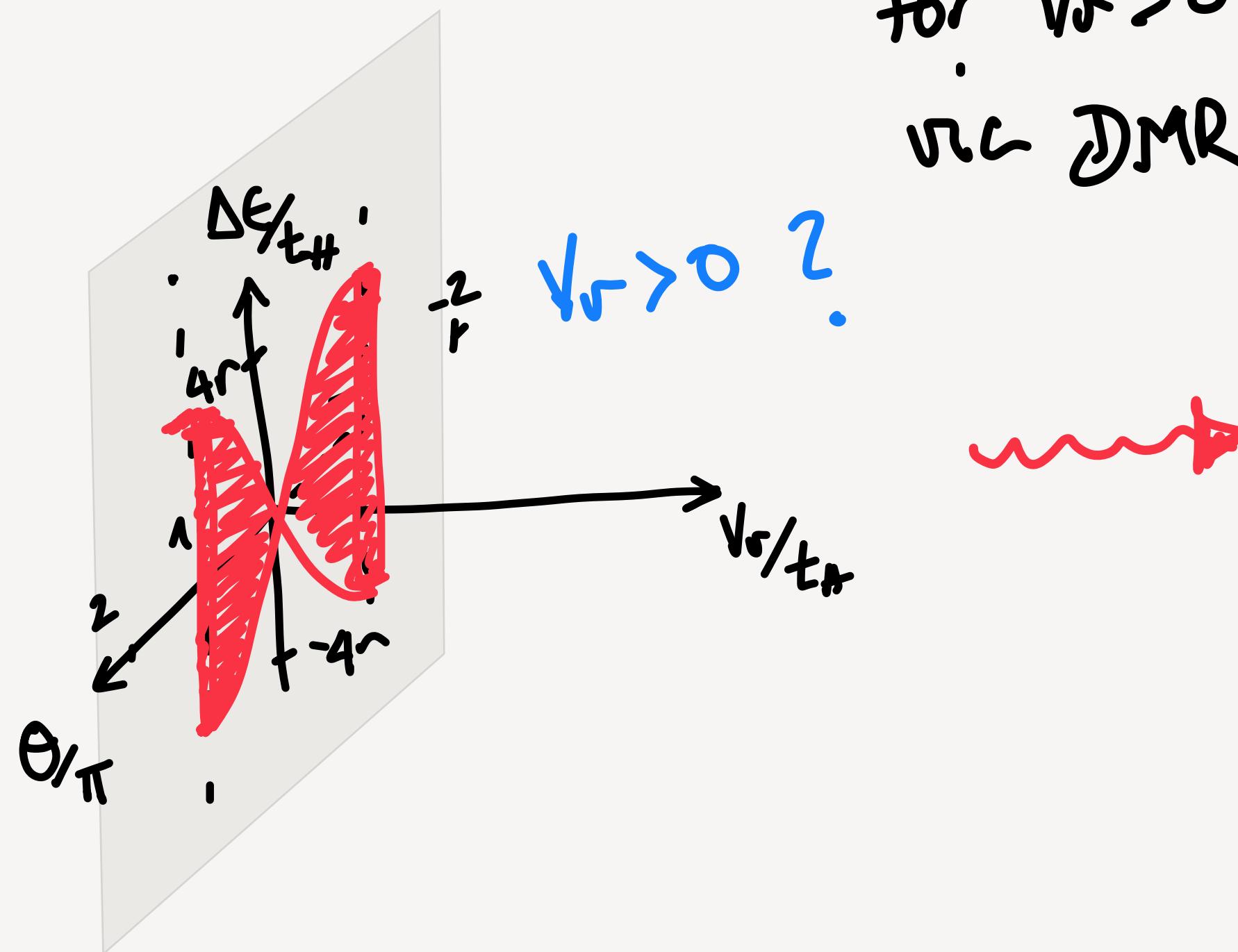


→ solid red links are exact solution

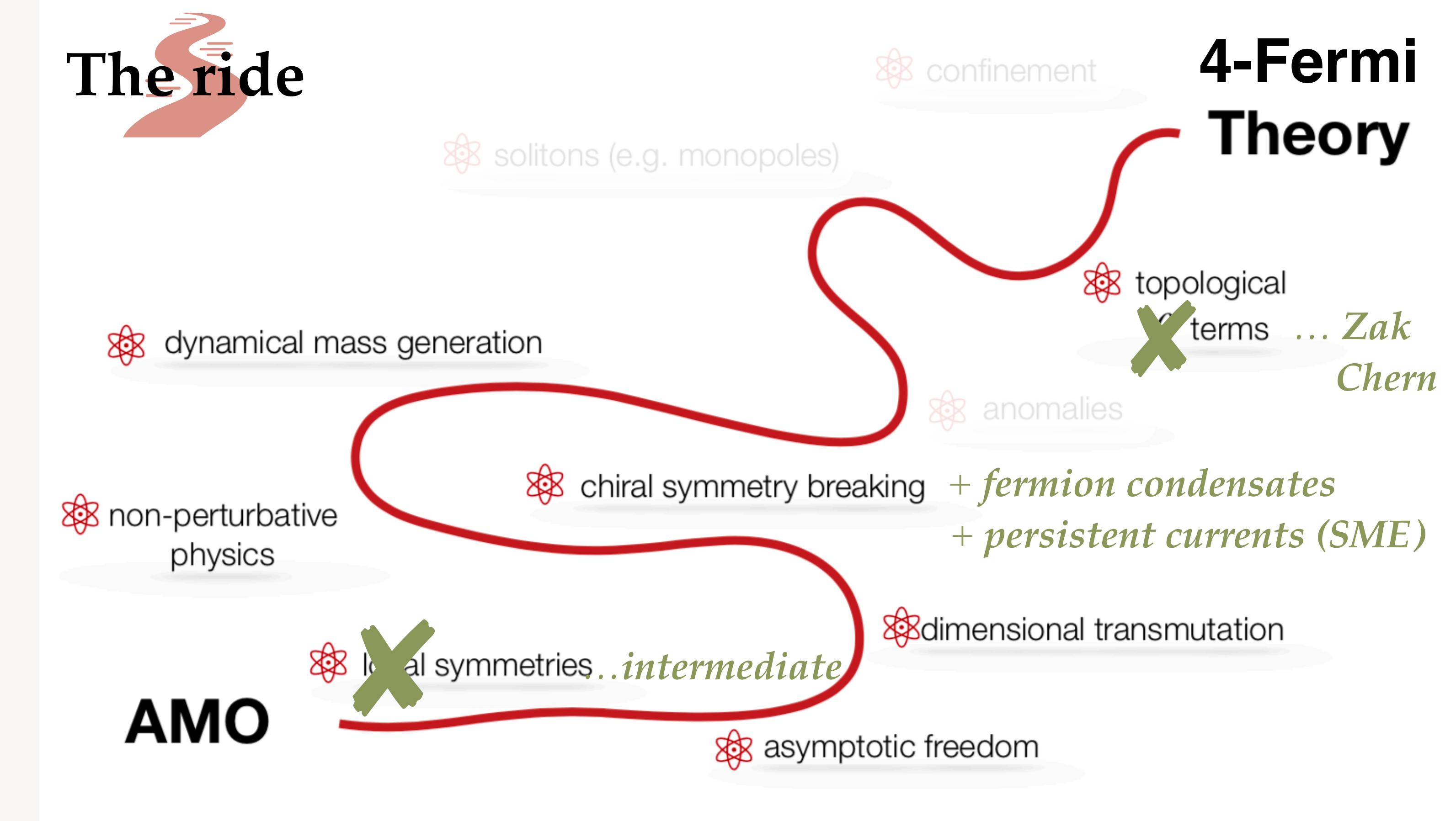
$$H_{DM} = \sum_i \left( J(1+\xi) T_i^x T_{i+1}^x + J(1-\xi) T_i^y T_{i+1}^y \right) + \sum_i \left( \mathbf{D} \cdot (\mathbf{T}_i \times \mathbf{T}_{i+1}) + h T_i^z \right),$$

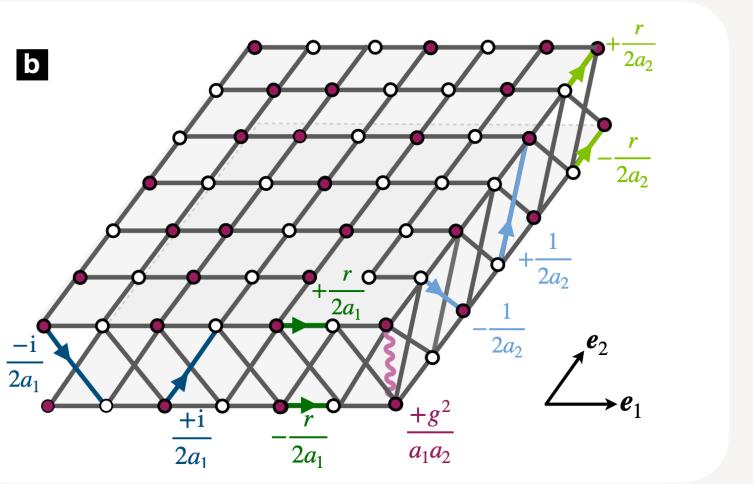
# Phase diagram for arbitrary $\theta$ and $V_v$

We have explored other planes  
for  $V_v > 0$   
via DMRG



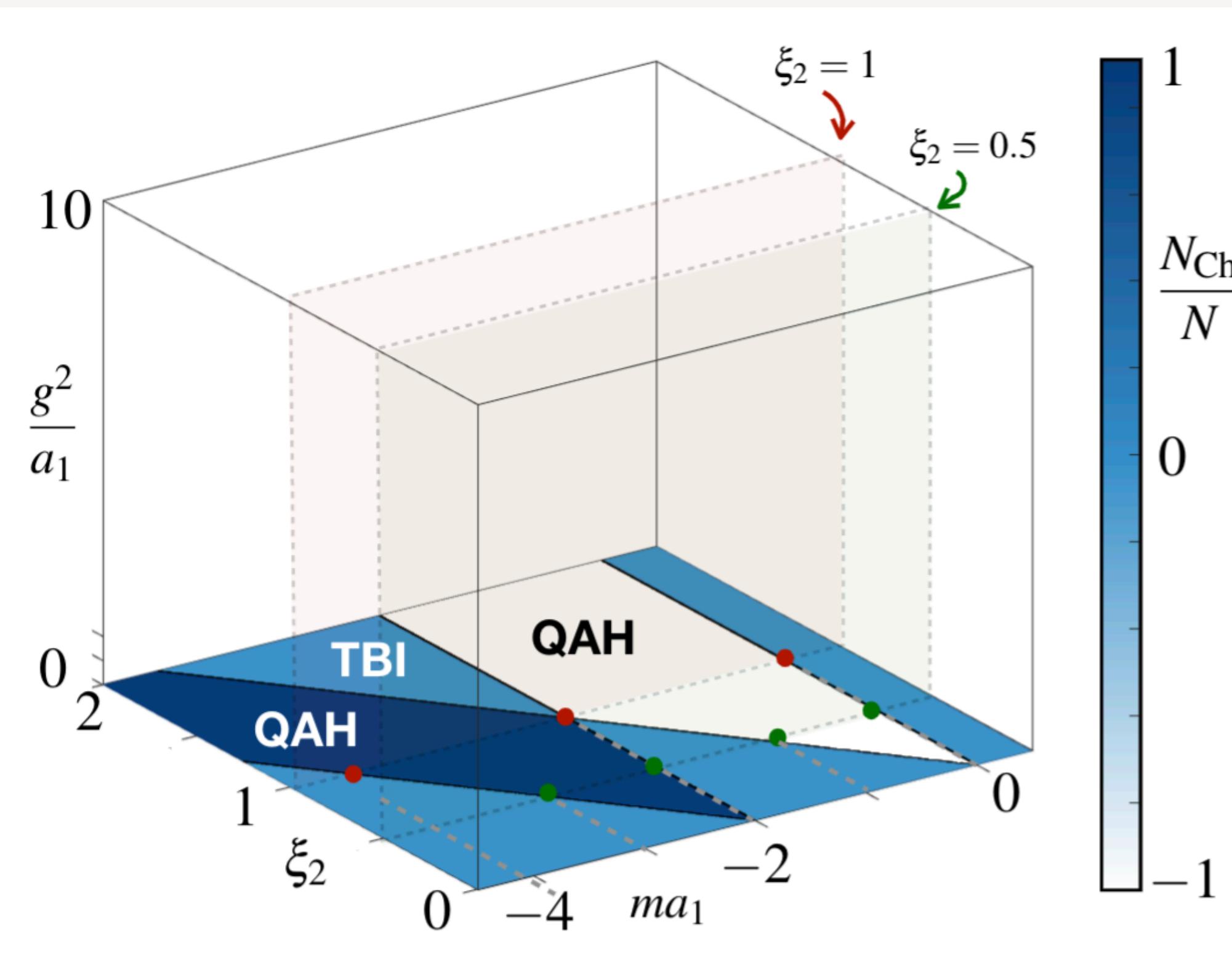
# MOTIVATION



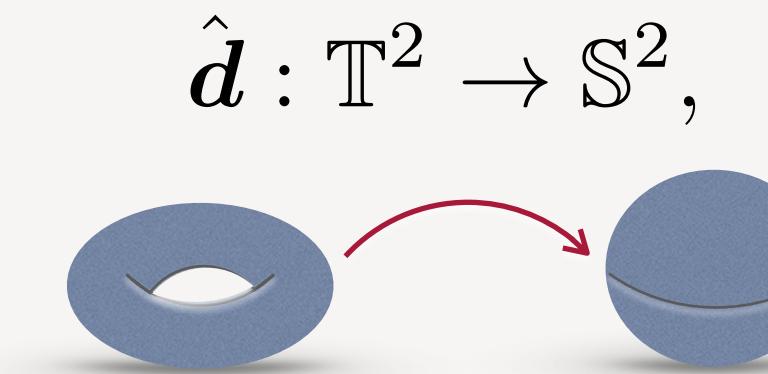


# Fate of Chern insulators @ strong couplings

At zero coupling  $g^2 = 0$ , the groundstate develops a **quantum anomalous Hall effect**



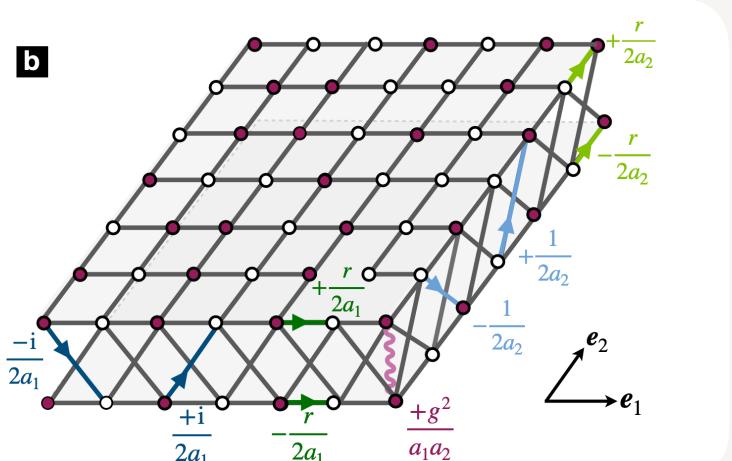
Topological ~~X~~ terms...Chern



$$N_{\text{Ch},b} = \frac{1}{4\pi} \int_{\text{BZ}} d^2k \hat{d}_k(m) \cdot (\partial_{k_1} \hat{d}_k(m) \wedge \partial_{k_2} \hat{d}_k(m)).$$

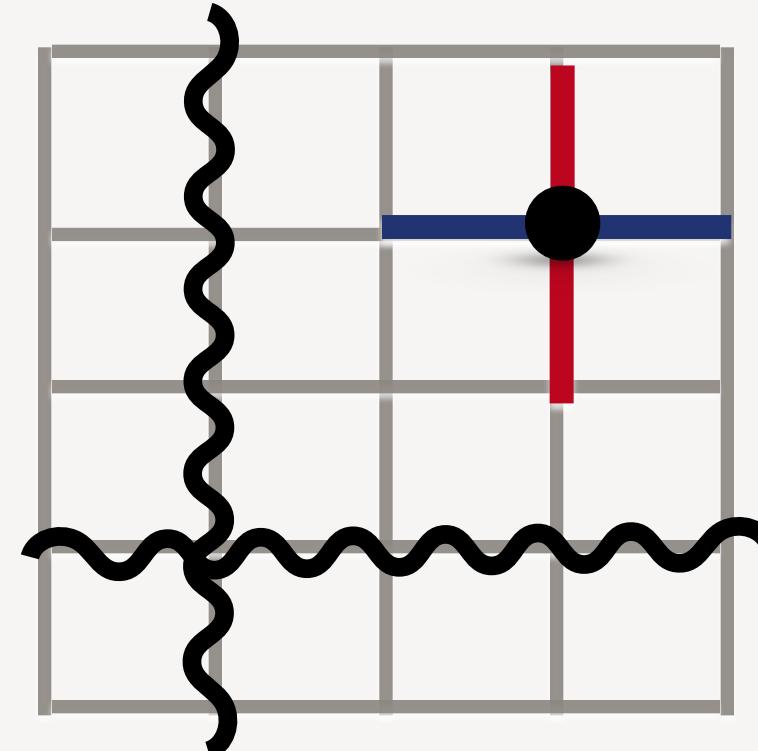


- F. D. M. Haldane, *Phys. Rev. Lett.* **61**, 2015 (1988)
- D. B. Kaplan, *Physics Letters B* **288**, 342 (1992).



# Fate of Chern insulators @ strong couplings

At strong couplings  $g^2/a_1 \gg 1$ , we obtain a **quantum compass model**



- $\tau^y\tau^y$  link
- |  $\tau^x\tau^x$  link
- ~~~~~  $S_{i_0}^x = \prod_j \tau_{i_0,j}^x$

$$H_{\text{eff}} = \sum_{\mathbf{n}} \left( J_x \tau_{\mathbf{n}}^x \tau_{\mathbf{n}+e_2}^x + J_y \tau_{\mathbf{n}}^y \tau_{\mathbf{n}+e_1}^y - h \tau_{\mathbf{n}}^z \right),$$

**X** local symmetry...**intermediate**  
similar to Dirac strings in  $\mathbb{Z}_2$ LGTs

th Z. Nussinov and E. Fradkin, *Phys. Rev. B* **71**, 195120 (2005)

We obtained the critical lines with **tensor-network variational methods (iPEPs)**

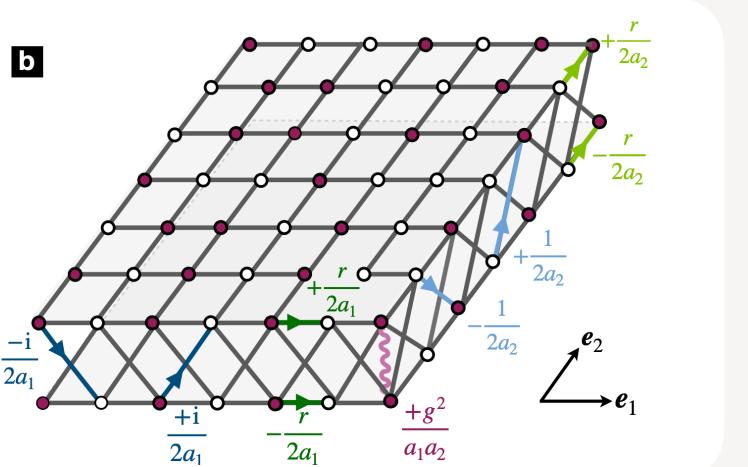
**X** chiral symmetry breaking...**inversion**

$$\Psi(\mathbf{x}) \mapsto \mathbb{I}_N \otimes \gamma^0 \Psi(-\mathbf{x})$$

**fermion condensates**

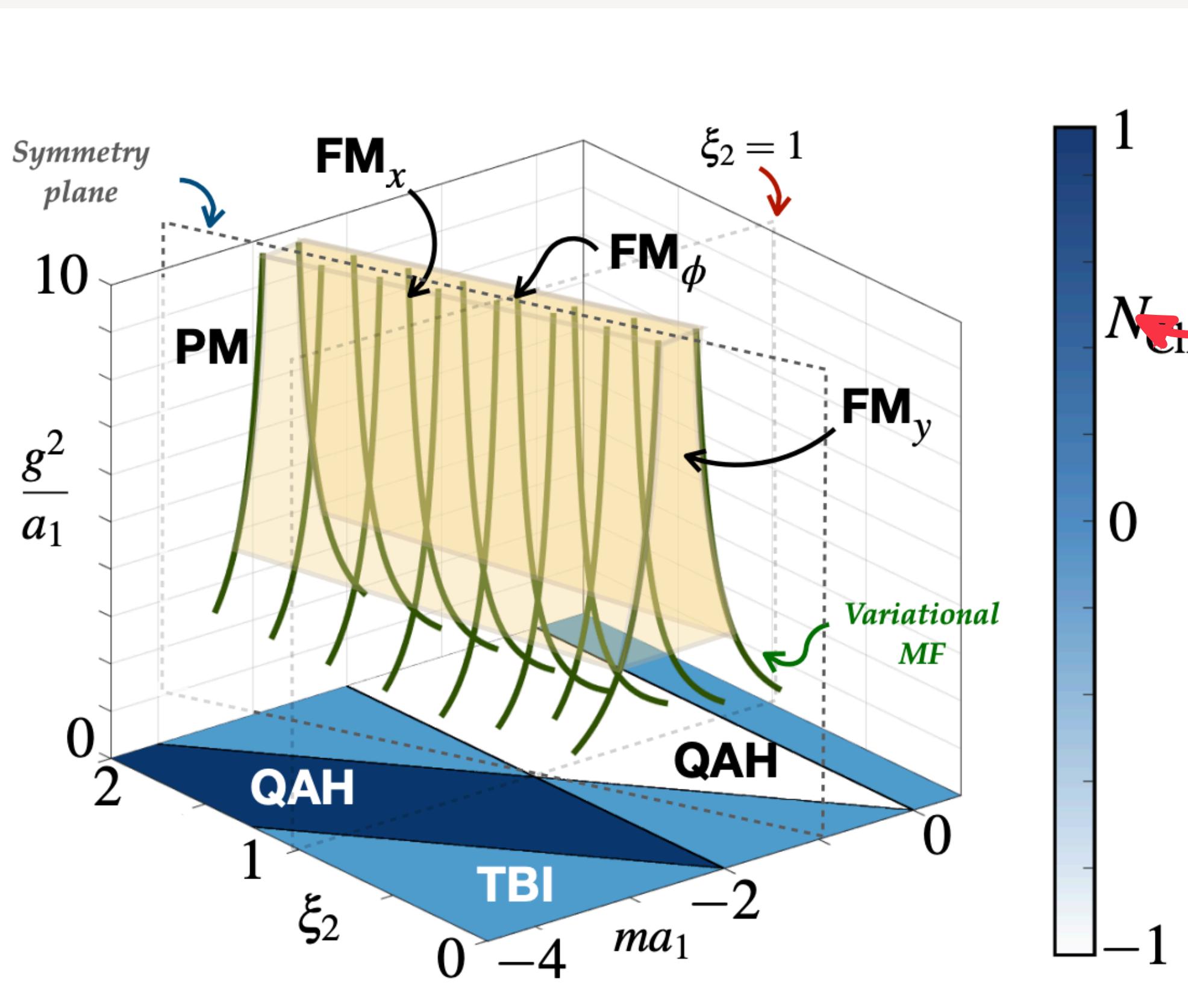
$$\Pi_1 = \langle \bar{\Psi} \gamma^1 \Psi \rangle \neq 0, \quad |J_x| \geq |h|, \quad |J_y| < |J_x|,$$

$$\Pi_2 = \langle \bar{\Psi} \gamma^2 \Psi \rangle \neq 0, \quad |J_y| \geq |h|, \quad |J_x| < |J_y|,$$



# Fate of Chern insulators @ strong couplings

At strong couplings  $g^2/a_1 \gg 1$ , we obtain a quantum compass model



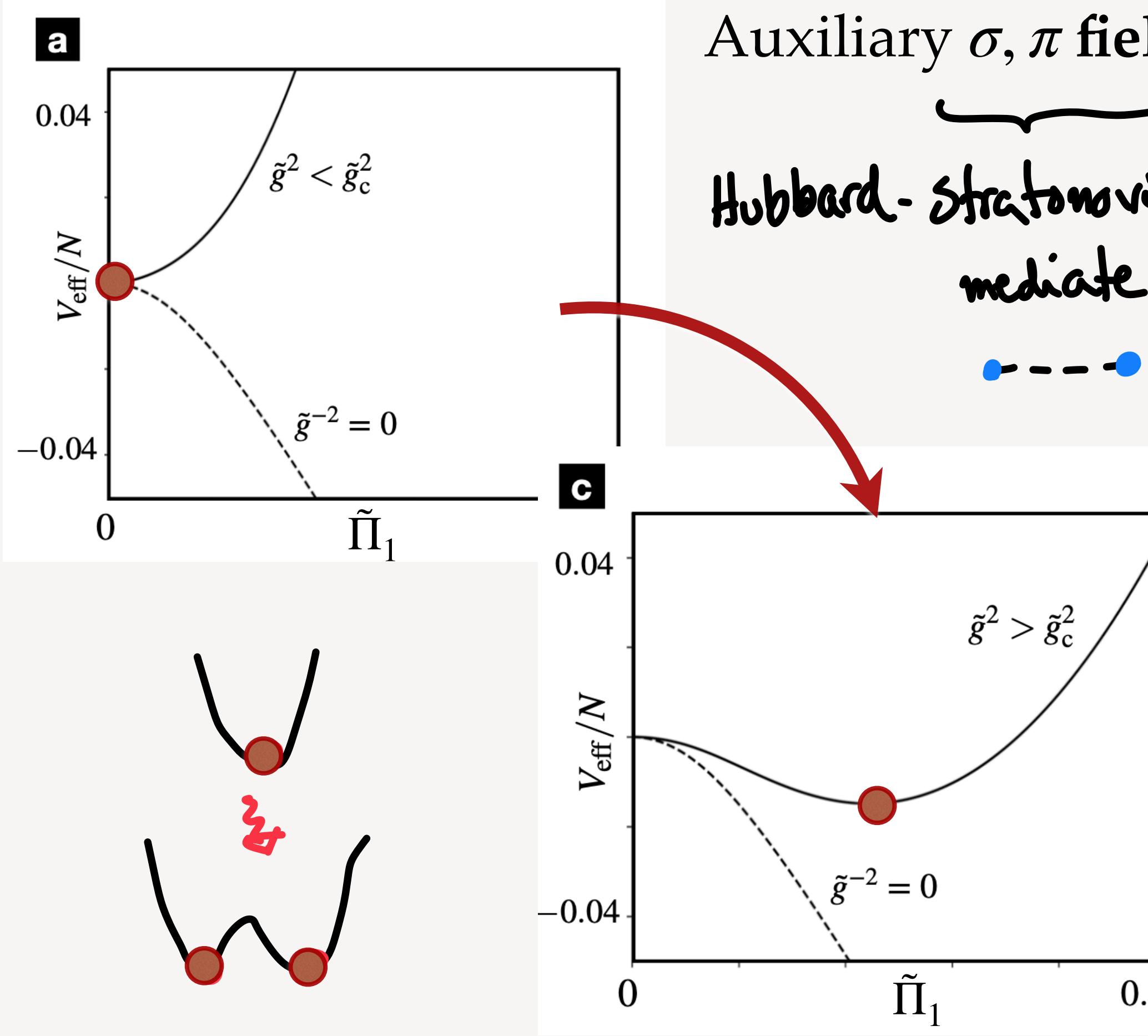
$$H_{\text{eff}} = \sum_n \left( J_x \tau_n^x \tau_{n+e_2}^x + J_y \tau_n^y \tau_{n+e_1}^y - h \tau_n^z \right),$$

We use a variational MF ansatz to obtain critical lines compass model in a transverse field  
(see next slide)

$$g^2 = \frac{a_1}{a_2 \left| m + \frac{1}{a_1} + \frac{1}{a_2} \right|}, \text{ if } a_1 > a_2,$$

$$g^2 = \frac{a_2}{a_1 \left| m + \frac{1}{a_1} + \frac{1}{a_2} \right|}, \text{ if } a_1 < a_2.$$

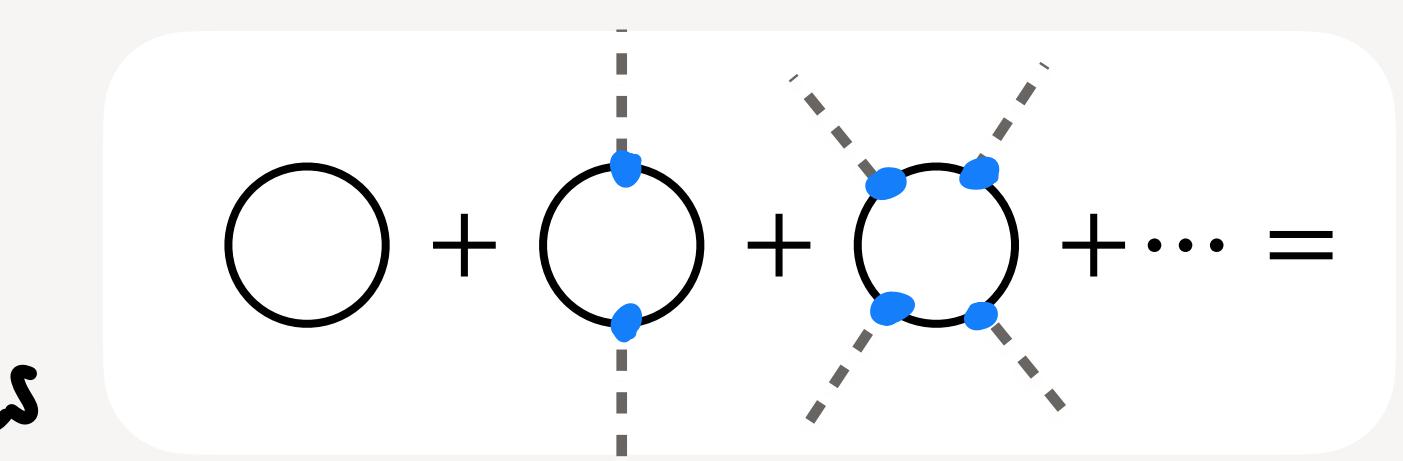
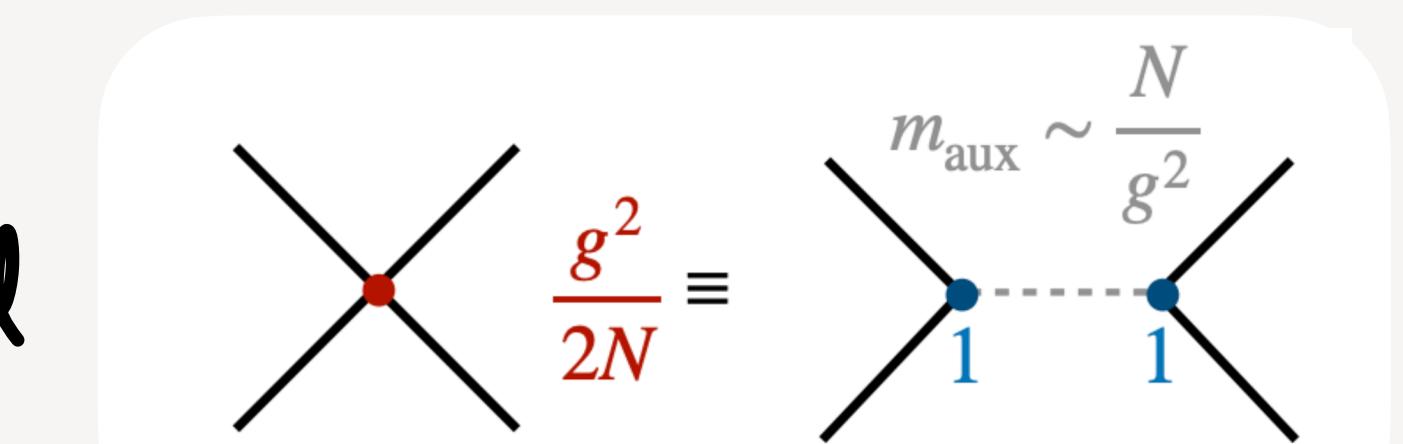
# Effective potential and large- $N$ Chern insulators



Auxiliary  $\sigma, \pi$  fields and resum the leading-order diagrams at large  $N$

Hubbard-Stratonovich fields  
mediate interactions via internal  
lines suppressed  $\frac{1}{m_{\text{aux}}} \sim \frac{1}{N}$

large- $N$   $V_{\text{eff}}$  by  
fermion loop by  $\text{NETZ}^+$   
external auxiliary lines

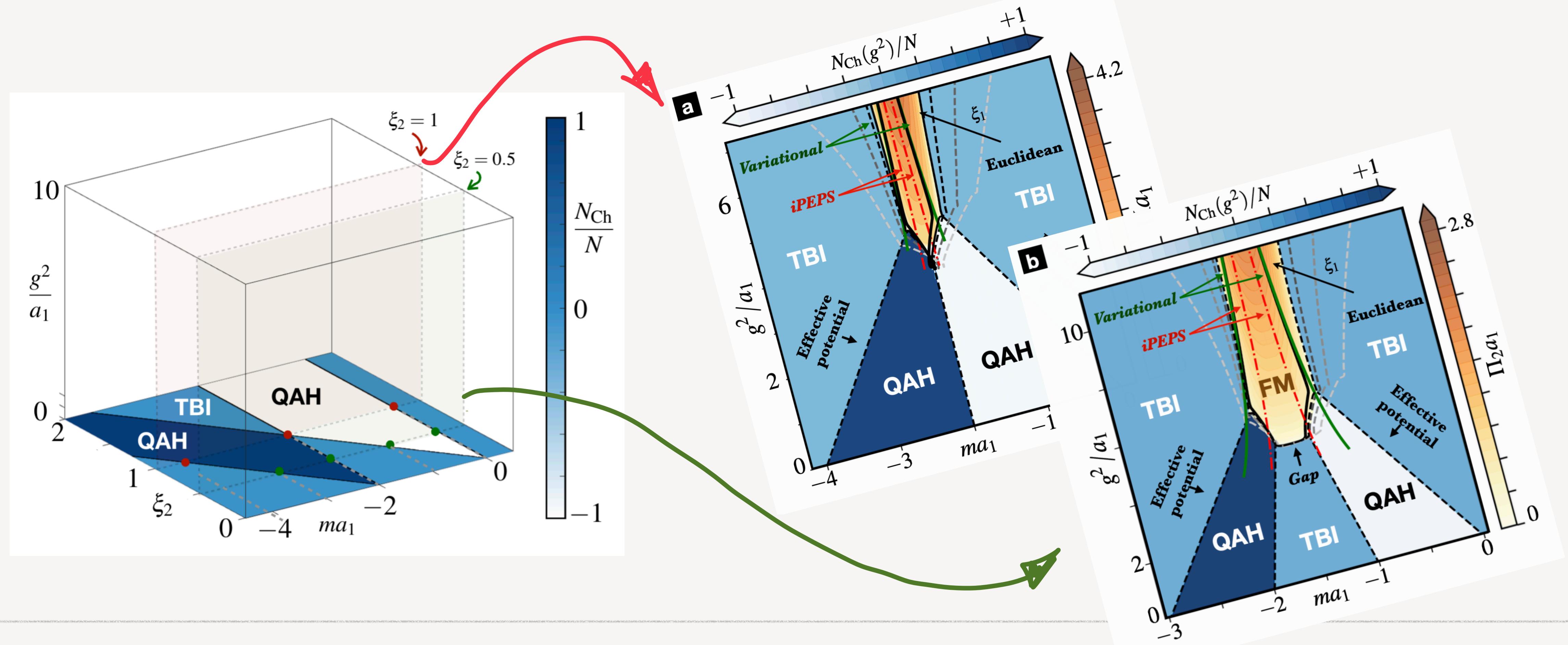


$$V_{\text{eff}}(\tilde{\Pi}_1) = \frac{N\tilde{\Pi}_1^2}{2\tilde{g}^2} + N \sum_{n=1}^{\infty} \frac{1}{n} \int_{\mathbf{p}} \text{Tr} \left( -i\tilde{\gamma}_1 \frac{\tilde{\Pi}_1}{i\mathbf{p} + \tilde{m}} \right)^n,$$

Non-standard resummation & novel radiative corrections

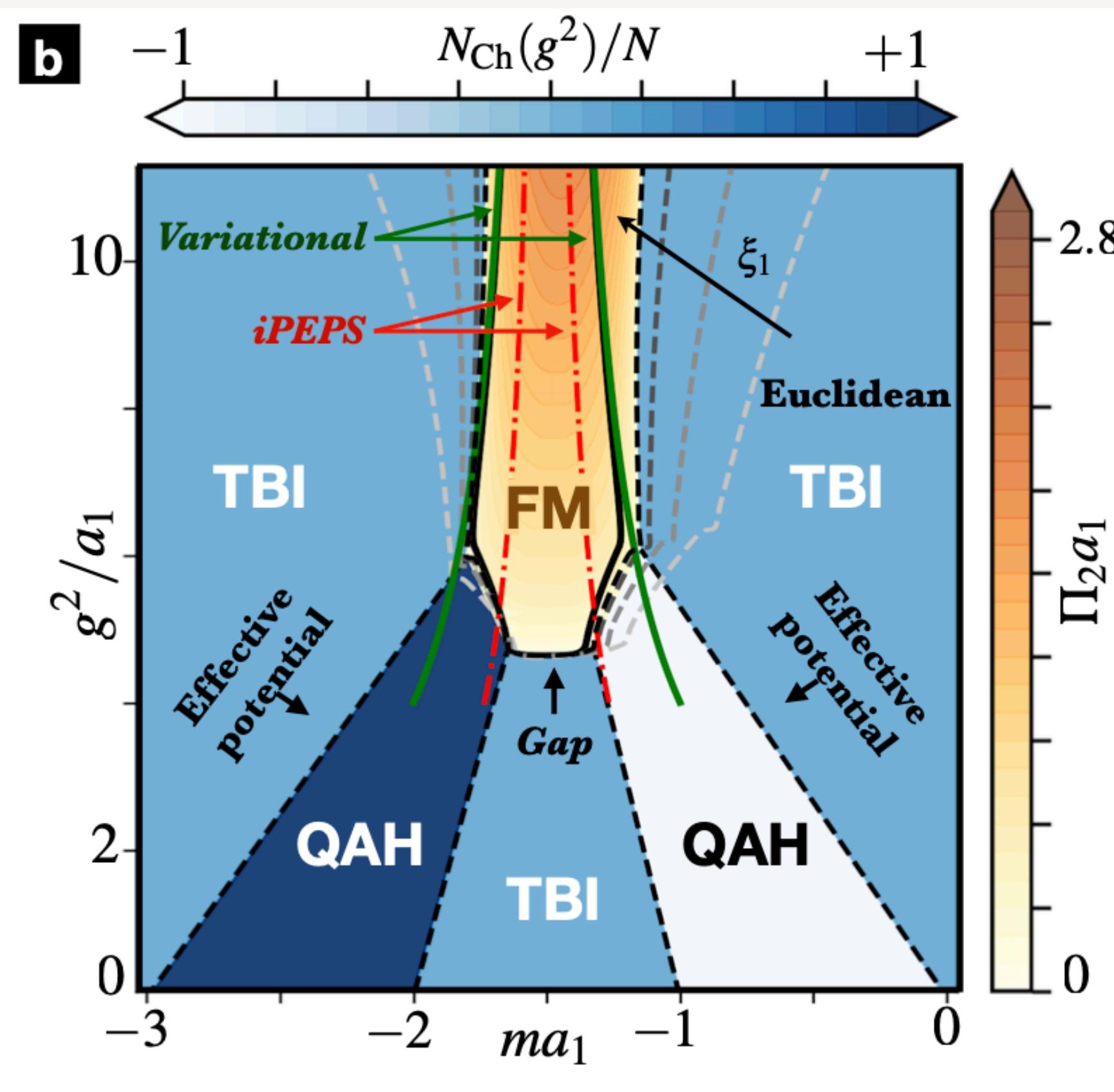
# Effective potential and large- $N$ Chern insulators

The phase diagram has regions hosting large- $N$  Chern insulators, TBIs, and FMs



# Effective potential and large- $N$ Chern insulators

Large- $N$  condensates give simple contributions to self-energy



$$\zeta_\delta(\omega, \vec{k}) = \mathbb{1}_N \otimes (\gamma^0 \Sigma + \gamma^0 \delta^\dagger \Pi_1) \delta(\omega - \delta) \delta(\vec{k} - \vec{\delta})$$

feed into topological Hamiltonian

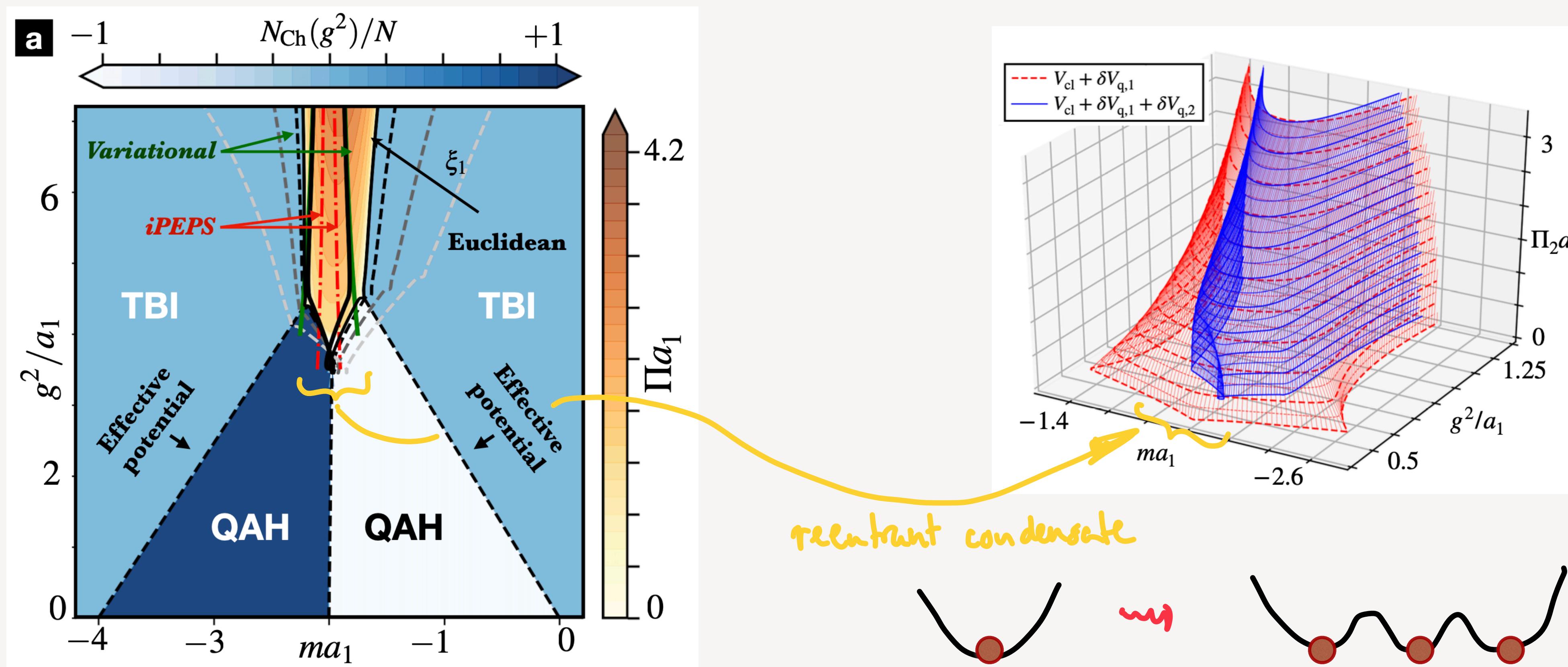
th Z. Wang and S.-C. Zhang, PRX 2, 031008 (2012)

The  $\delta$  condensate renormalizes bare  $m$   
 $\beta$  changes the value of  $N_{\text{Ch}}(g^2)$  via  $\Sigma_\delta(0, \vec{k})$

$$\hat{d}_k(m) \rightarrow \hat{d}_k(m + \Sigma, \Pi_1)$$

# Effective potential and large- $N$ Chern insulators

New large- $N$  quantum corrections lead to 1st-order phase transition



# Thanks for your attention

arXiv:2011.08744

arXiv:2111.04485

arXiv:2112.07654



E. Tirrito



L. Ziegler



M. Lewenstein



S. Hands

# Thanks for your attention

Instituto de Física Teórica IFT CSIC-UAM

<https://projects.ift.uam-csic.es/qift/>



arXiv:2011.08744

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*PhD & Postdoc openings  
QI group*



G. Sierra



E. López