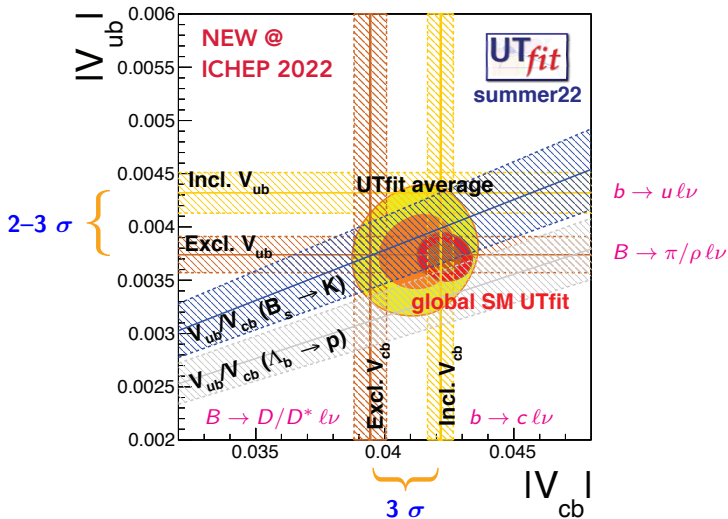


V_{cb} & V_{ub} : Inclusive–Exclusive Tension



Cabibbo Anomaly $\sim 3\sigma$

CKM Unitarity \rightarrow

$$1 = |V_{ud}|^2 + |V_{us}|^2 + |V_{ub}|^2 \approx |V_{ud}|^2 + |V_{us}|^2$$

$$K \rightarrow \pi \ell \nu \rightarrow V_{us}$$

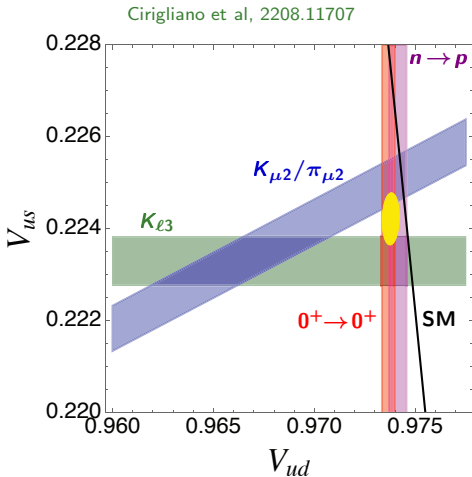
$$K \rightarrow \mu \nu / \pi \rightarrow \mu \nu \rightarrow V_{us}/V_{ud}$$

$$0^+ \rightarrow 0^+ \text{ nuclear } \beta \text{ decays} \rightarrow V_{ud}$$

$$n \rightarrow p e \nu \rightarrow V_{ud}$$

Recalculation of radiative corrections

C.-Y. Seng, 2112.10942



Cabibbo Anomaly $\sim 3\sigma$

CKM Unitarity \rightarrow

$$1 = |V_{ud}|^2 + |V_{us}|^2 + |V_{ub}|^2 \approx |V_{ud}|^2 + |V_{us}|^2$$

$$K \rightarrow \pi \ell \nu \rightarrow V_{us}$$

$$K \rightarrow \mu \nu / \pi \rightarrow \mu \nu \rightarrow V_{us}/V_{ud}$$

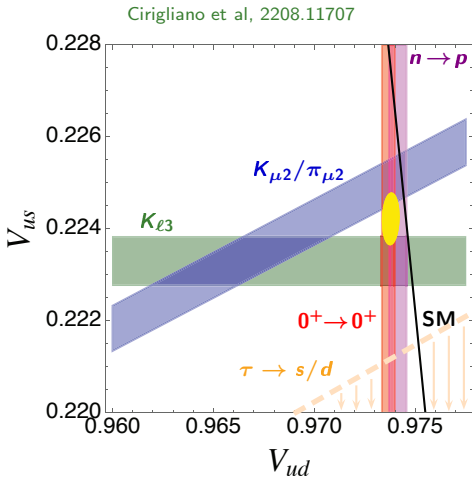
$$0^+ \rightarrow 0^+ \text{ nuclear } \beta \text{ decays} \rightarrow V_{ud}$$

$$n \rightarrow p e \nu \rightarrow V_{ud}$$

$$\tau \rightarrow \nu_\tau s \bar{u} / \tau \rightarrow \nu_\tau d \bar{u} \rightarrow V_{us}/V_{ud}$$

Recalculation of radiative corrections

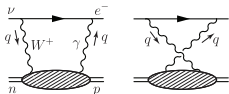
C.-Y. Seng, 2112.10942



V_{ud} : Superaligned ($0^+ \rightarrow 0^+$) nuclear β transitions

$$f_+(0) = 1 + \mathcal{O}[(m_u - m_d)^2] \quad \Rightarrow \quad |V_{ud}|^2 = \frac{\pi^3 \log 2}{ft G_F^2 m_e^5 (1 + \delta_{RC})} = \frac{(2984.48 \pm 0.05) \text{ s}}{ft (1 + \delta_{RC})}$$

$$\delta_{RC} = \Delta_R^V + \Delta_{\text{Nucl}} \quad , \quad \mathcal{F}t = ft (1 + \Delta_{\text{Nucl}})$$



Nucleus-independent radiative corrections

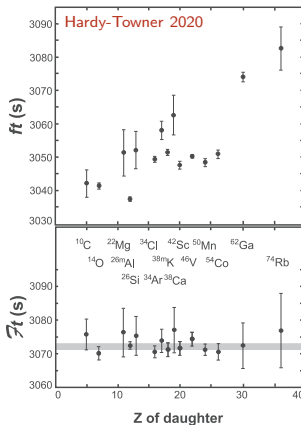
$$\Delta_R^V = \begin{cases} 0.02361 \text{ (38)} \\ 0.02467 \text{ (22)} \\ 0.02426 \text{ (32)} \end{cases}$$

Marciano-Sirlin 2006

Seng et al, 1807.10197

Czarnecki et al, 1907.06737

$$\Rightarrow |V_{ud}| = \begin{cases} 0.97420 \text{ (21)} & \text{PDG 2018} \\ 0.97373 \text{ (31)} & \text{Hardy-Towner 2020} \end{cases}$$



$$|V_{us}| = \begin{cases} 0.2231 \text{ (6)} & K \rightarrow \pi \ell \nu \\ 0.2252 \text{ (5)} & K/\pi \rightarrow \mu \nu \end{cases}$$

PDG 2022



$$1 - \sum_i |V_{ui}|^2 = \begin{cases} 0.00206 \text{ (66)} & 3.1 \sigma \\ 0.00112 \text{ (64)} & 1.7 \sigma \end{cases}$$

V_{ud} : Superaligned ($0^+ \rightarrow 0^+$) nuclear β transitions

$$f_+(0) = 1 + \mathcal{O}[(m_u - m_d)^2] \quad \Rightarrow \quad |V_{ud}|^2 = \frac{\pi^3 \log 2}{ft G_F^2 m_e^5 (1 + \delta_{RC})} = \frac{(2984.48 \pm 0.05) \text{ s}}{ft (1 + \delta_{RC})}$$

$$\delta_{RC} = \Delta_R^V + \Delta_{\text{Nucl}} \quad , \quad \mathcal{F}t = ft (1 + \Delta_{\text{Nucl}}) \quad , \quad \Delta_{\text{Nucl}} = \delta'_R + \delta_{\text{NS}} - \delta_C$$

Hardy-Towner 2020:

$$\Delta_R^V = 0.02454 (19)$$

$$\begin{aligned} \mathcal{F}t &= (3072.24 \pm 0.57_{\text{stat}} \pm 0.36_{\delta'_R} \pm 1.73_{\delta_{\text{NS}}}) \text{ s} \\ &= (3072.24 \pm 1.85) \text{ s} \end{aligned}$$

$\mathcal{F}t$ error 2.6 larger than in 2015 (δ_{NS})

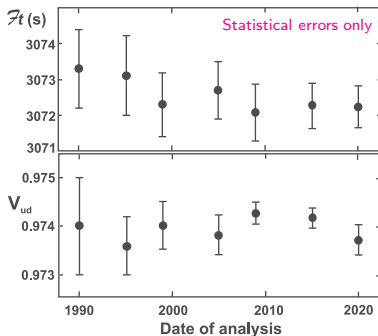
Seng et al, Gorchtein



$$|V_{ud}| = 0.97373 (31)$$



$$1 - \sum_i |V_{ui}|^2 = \begin{cases} 0.00206 (66) & K \rightarrow \pi \ell \nu & 3.1 \sigma \\ 0.00112 (64) & K/\pi \rightarrow \mu \nu & 1.7 \sigma \end{cases}$$



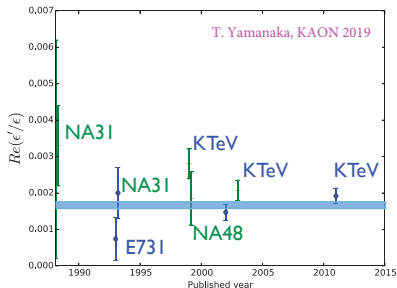
CP Violation in $K \rightarrow \pi\pi$

$$\eta_{00} \equiv \frac{\mathcal{M}(K_L^0 \rightarrow \pi^0\pi^0)}{\mathcal{M}(K_S^0 \rightarrow \pi^0\pi^0)} \equiv \varepsilon - 2\varepsilon' \quad , \quad \eta_{+-} \equiv \frac{\mathcal{M}(K_L^0 \rightarrow \pi^+\pi^-)}{\mathcal{M}(K_S^0 \rightarrow \pi^+\pi^-)} \equiv \varepsilon + \varepsilon'$$

- **Indirect CP:** $|\varepsilon| = \frac{1}{3} |\eta_{00} + 2\eta_{+-}| = (2.228 \pm 0.011) \cdot 10^{-3}$
- **Direct CP:** $\text{Re}(\varepsilon'/\varepsilon) = \frac{1}{3} \left(1 - \left| \frac{\eta_{00}}{\eta_{+-}} \right| \right) = (16.6 \pm 2.3) \cdot 10^{-4}$

First evidence in 1988 by NA31

**Time evolution of
 ε'/ε measurements**



Time evolution of ε'/ε predictions:

10^{-3} units

- 1983	SD (Q_6), LO	~ 2	Gilman-Hagelin
- 1990-2000	SD, large m_t (Q_8), NLO + models of LD contributions	$\sim \text{few} \cdot 10^{-1}$ $\sim \mathcal{O}(1)$	Munich, Rome Dortmund, Trieste
- 1999-2001	SD + LD (χ PT) at NLO	1.7 ± 0.9	Scimemi-Pallante-Pich
- 2000-2003	models of LD contributions	$\sim \mathcal{O}(1)$	Lund, Marseille
- 2003	NLO isospin breaking in χ PT	1.9 ± 1.0	Cirigliano-Ecker-Neufeld-Pich
- 2015	Lattice	0.14 ± 0.70	RBC-UKQCD
- 2015-2017	Dual QCD, Lattice input	0.19 ± 0.45	Munich
- 2017	NLO χ PT re-analysis	1.5 ± 0.7	Gisbert-Pich
- 2019	χ PT re-analysis of NLO IB	1.4 ± 0.5	Cirigliano-Gisbert-Pich-Rodríguez
- 2020 (April)	Lattice re-analysis (no IB)	2.17 ± 0.84	RBC-UKQCD
- 2020 (May)	Lattice input + χ PT IB Lattice input + naive IB	1.74 ± 0.61 1.39 ± 0.52	Munich

Empirical Evidence

$$A[K^0 \rightarrow \pi^+ \pi^-] = A_0 e^{i\delta_0} + \frac{1}{\sqrt{2}} A_2 e^{i\delta_2} \equiv \mathcal{A}_{1/2} + \frac{1}{\sqrt{2}} \mathcal{A}_{3/2}$$

$$A[K^0 \rightarrow \pi^0 \pi^0] = A_0 e^{i\delta_0} - \sqrt{2} A_2 e^{i\delta_2} \equiv \mathcal{A}_{1/2} - \sqrt{2} \mathcal{A}_{3/2}$$

$$A[K^+ \rightarrow \pi^+ \pi^0] = \frac{3}{2} A_2 e^{i\delta_2} \equiv \frac{3}{2} \mathcal{A}_{3/2}$$

① $\Delta I = 1/2$ Rule:

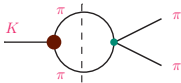
$$\omega \equiv \text{Re}(A_2)/\text{Re}(A_0) \approx 1/22$$

② Strong Final-State Interactions:

$$\delta_0 - \delta_2 \approx 45^\circ$$

• **Unitarity:**

$$\delta_0 = (39.2 \pm 1.5)^\circ \quad \Rightarrow \quad A_0 \approx 1.3 \times \text{Dis}(\mathcal{A}_0)$$



$$A_I = \text{Dis}(\mathcal{A}_I) \sqrt{1 + \tan^2 \delta_I}$$

$$\tan \delta_I = \frac{\text{Abs}(\mathcal{A}_I)}{\text{Dis}(\mathcal{A}_I)}$$

• **Analyticity:**

$$\Delta \text{Dis}(\mathcal{A}_I)[s] = \frac{1}{\pi} \int dt \frac{\text{Abs}(\mathcal{A}_I)[t]}{t - s - i\epsilon} + \text{subtractions}$$

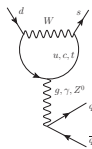
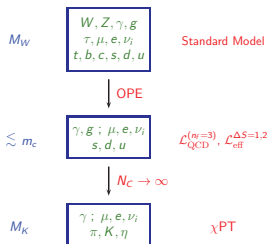
Large δ_0 \Rightarrow Large $\text{Abs}(\mathcal{A}_0)$ \Rightarrow Large correction to $\text{Dis}(\mathcal{A}_0)$

Claims of an ϵ'/ϵ anomaly originate in incorrect treatments of the $\pi\pi$ cut

SM Prediction of ϵ'/ϵ

Cirigliano, Gisbert, Pich, Rodríguez-Sánchez, 1911.01359

Effective
Field
Theory

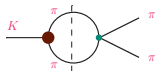


$$\mathcal{L}_{\text{eff}}^{\Delta S=1} \sim \sum_i C_i(\mu) Q_i(\mu)$$

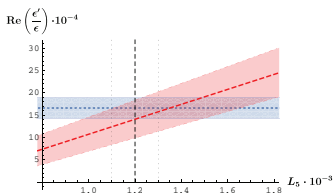
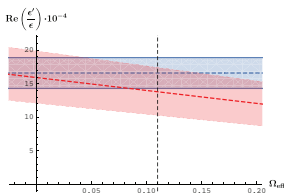
Large logarithms:

OPE: $\alpha_s^k(\mu) \log^n(M_W/\mu)$

χPT : $\log(\mu/m_\pi)$



$$\text{Re}(\epsilon'/\epsilon)_{\text{SM}} = (14 \pm 5) \cdot 10^{-4}$$

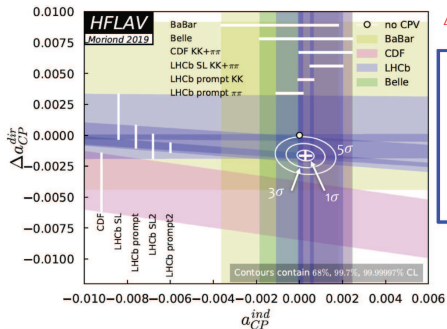


$$\text{Re}(\epsilon'/\epsilon)_{\text{SM}} = \left(13.8_{-0.4}^{+0.5} m_s + 1.7_{-1.3} \mu + 3.1_{-3.2} \nu_\chi \pm 1.3 \gamma_5 \pm 2.1 L_{5,8} \pm 1.3 L_7 \pm 0.2 K_i \pm 0.3 X_j \right) \cdot 10^{-4}$$

First evidence of C/P in charm decays (5.3σ)

LHCb 1903.08726

$$\Delta a_{CP} = (-15.4 \pm 2.9) \cdot 10^{-4} \quad , \quad \Delta a_{CP}^{\text{dir}} = (-15.7 \pm 2.9) \cdot 10^{-4}$$



$$\Delta a_{CP} = a_{CP}(K^+K^-) - a_{CP}(\pi^+\pi^-)$$

HFLAV combination
 $a_{CP}^{\text{ind}} = (0.028 \pm 0.026)\%$
 $\Delta a_{CP}^{\text{dir}} = (-0.164 \pm 0.028)\%$
 Consistency with NO CPV hypothesis: 5×10^{-8}

$$a_{CP} \equiv \frac{\Gamma(D^0 \rightarrow f) - \Gamma(\bar{D}^0 \rightarrow f)}{\Gamma(D^0 \rightarrow f) + \Gamma(\bar{D}^0 \rightarrow f)}$$

Large uncertainty in SM prediction:

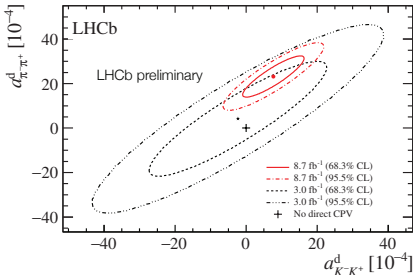
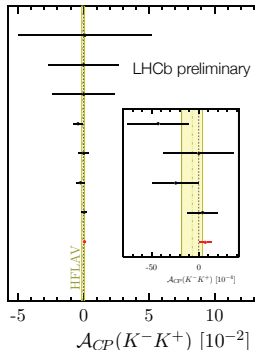
- Naive perturbative QCD (+ LCSR) $\Rightarrow |\Delta a_{CP}^{\text{dir}}| \leq 3 \cdot 10^{-4}$ Chala et al, 1903.10490
- Re-scattering: $\Delta a_{CP}^{\text{dir}} \Rightarrow \Delta U = 0$ rule in charm Grossman-Schacht, 1903.10952
- Dispersive work in progress Solomonidi, Vale-Silva, A.P.

Time-integrated CP asymmetry

$$\mathcal{A}_{CP}(f) \approx a_f^d + \frac{\langle t \rangle_f}{\tau_{D^0}} \Delta Y$$

$$a_f^d \equiv \frac{|\mathcal{M}(D^0 \rightarrow f)|^2 - |\mathcal{M}(\bar{D}^0 \rightarrow \bar{f})|^2}{|\mathcal{M}(D^0 \rightarrow f)|^2 + |\mathcal{M}(\bar{D}^0 \rightarrow \bar{f})|^2}$$

$$\mathcal{A}_{CP}(K^- K^+) = (6.8 \pm 5.4 \pm 1.6) \cdot 10^{-4}$$



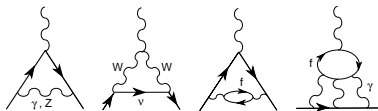
Evidence of direct C/P in $D^0 \rightarrow \pi^- \pi^+$ (3.8σ)

$$a_{\pi^- \pi^+}^d = (23.2 \pm 6.1) \cdot 10^{-4}$$

$$a_{K^- K^+}^d = (7.7 \pm 5.7) \cdot 10^{-4}$$

$$\rho(a_{KK}^d, a_{\pi\pi}^d) = 0.88$$

μ Anomalous Magnetic Moment



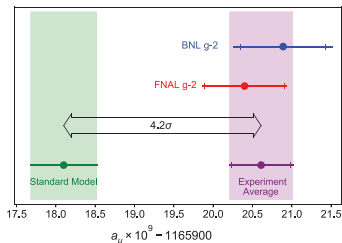
$$\mu_\ell = \frac{e}{2m_\ell} \frac{g_\ell}{2}$$

$$a_\ell \equiv \frac{1}{2} (g_\ell - 2)$$

White Paper (2020)

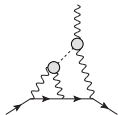
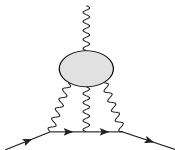
G. Colangelo, Moriond EW 2021

Contribution	Value $\times 10^{11}$
HVP LO (e^+e^-)	6931(40)
HVP NLO (e^+e^-)	-98.3(7)
HVP NNLO (e^+e^-)	12.4(1)
HVP LO (lattice, $udsc$)	7116(184)
HLbL (phenomenology)	92(19)
HLbL NLO (phenomenology)	2(1)
HLbL (lattice, uds)	79(35)
HLbL (phenomenology + lattice)	90(17)
QED	116 584 718.931(104)
Electroweak	153.6(1.0)
HVP (e^+e^- , LO + NLO + NNLO)	6845(40)
HLbL (phenomenology + lattice + NLO)	92(18)
Total SM Value	116 591 810(43)
Experiment (E821)	116 592 089(63)
Difference: $\Delta a_\mu := a_\mu^{\text{exp}} - a_\mu^{\text{SM}}$	279(76)



$$\Delta a_\mu \equiv a_\mu^{\text{exp}} - a_\mu^{\text{SM}} = (251 \pm 59) \cdot 10^{-11} \quad (4.2\sigma)$$

Light-by-Light Contributions



Colangelo, Moriond EW 2021

Contribution	PdRV(09) <i>Glasgow consensus</i>	N/JN(09)	J(17)	WP(20)
π^0, η, η' -poles	114(13)	99(16)	95.45(12.40)	93.8(4.0)
π, K -loops/boxes	-19(19)	-19(13)	-20(5)	-16.4(2)
S-wave $\pi\pi$ rescattering	-7(7)	-7(2)	-5.98(1.20)	-8(1)
subtotal	88(24)	73(21)	69.5(13.4)	69.4(4.1)
scalars	-	-	-	} - 1(3)
tensors	-	-	1.1(1)	
axial vectors	15(10)	22(5)	7.55(2.71)	
u, d, s -loops / short-distance	-	21(3)	20(4)	15(10)
c-loop	2.3	-	2.3(2)	3(1)
total	105(26)	116(39)	100.4(28.2)	92(19)

A lot of work since Glasgow consensus (Prades, de Rafael, Vainshtein, 2009):

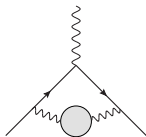
Masjuan, Sánchez-Puertas (17); Colangelo, Hagelstein, Hoferichter, Laub, Procura, Stoffer (17-20);

Hoferichter, Hoid, Kubis, Leupold, Schneider (18); Bijnens, Hermansson-Truedsson, Laub, Rodríguez-Sánchez (20, 21); ...

Errors reduced, size unchanged



Cannot account for the anomaly



LO Hadronic Vacuum Polarization

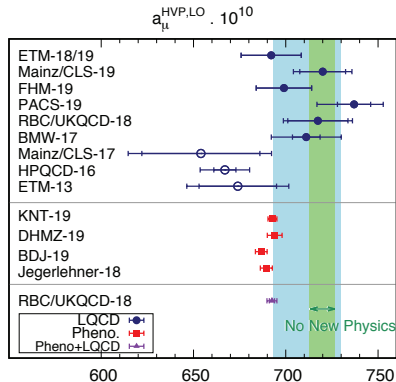
Aoyama et al, 2006.04822

$$a_{\mu}^{\text{HVP,LO}} = \frac{\alpha^2 m_{\mu}^2}{9\pi^2} \int_{s_{\text{th}}}^{\infty} \frac{ds}{s^2} \hat{K}(s) R(s)$$

Dominated (75%) by 2π contribution

$$R(s) = 12\pi \text{Im}\Pi_{\text{em}}(s)$$

$$= \frac{\sigma(e^+e^- \rightarrow \text{hadrons})}{\sigma(e^+e^- \rightarrow \mu^+\mu^-)}$$

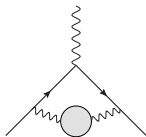


2020



$$\Delta a_{\mu} \equiv a_{\mu}^{\text{exp}} - a_{\mu}^{\text{SM}} = (279 \pm 76) \cdot 10^{-11} \quad (3.7\sigma)$$

LO Hadronic Vacuum Polarization



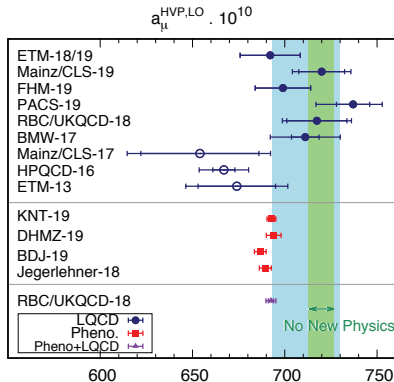
Aoyama et al, 2006.04822

$$a_{\mu}^{\text{HVP,LO}} = \frac{\alpha^2 m_{\mu}^2}{9\pi^2} \int_{s_{\text{th}}}^{\infty} \frac{ds}{s^2} \hat{K}(s) R(s)$$

Dominated (75%) by 2π contribution

$$R(s) = \frac{\sigma^0[e^+e^- \rightarrow \text{hadrons}(\gamma)]}{4\pi\alpha^2/(3s)}$$

Data need to be undressed \rightarrow MC

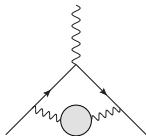


2020



$$\Delta a_{\mu} \equiv a_{\mu}^{\text{exp}} - a_{\mu}^{\text{SM}} = (279 \pm 76) \cdot 10^{-11} \quad (3.7\sigma)$$

LO Hadronic Vacuum Polarization

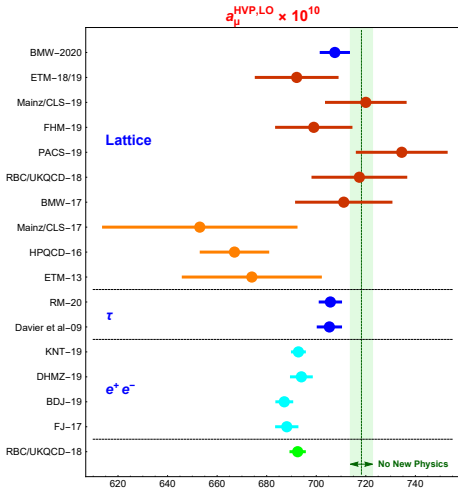


$$a_{\mu}^{\text{HVP,LO}} = \frac{\alpha^2 m_{\mu}^2}{9\pi^2} \int_{s_{\text{th}}}^{\infty} \frac{ds}{s^2} \hat{K}(s) R(s)$$

Dominated (75%) by 2π contribution

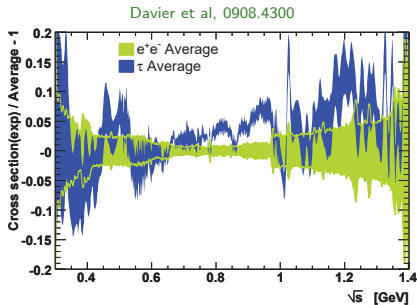
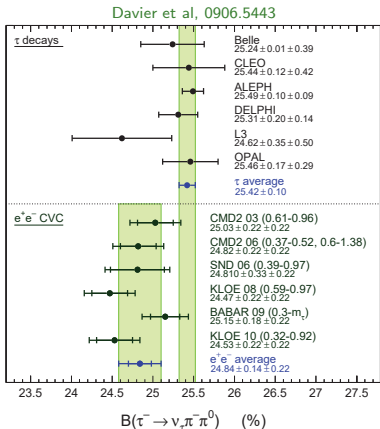
$$R(s) = \frac{\sigma^0[e^+e^- \rightarrow \text{hadrons}(\gamma)]}{4\pi\alpha^2/(3s)}$$

$$\frac{d\Gamma(\tau^- \rightarrow \nu_{\tau} V^-)}{ds} \propto \sigma^{l=1}(e^+e^- \rightarrow V^0)$$



The BMW-2020 and τ results were not included in the WP 2020 value

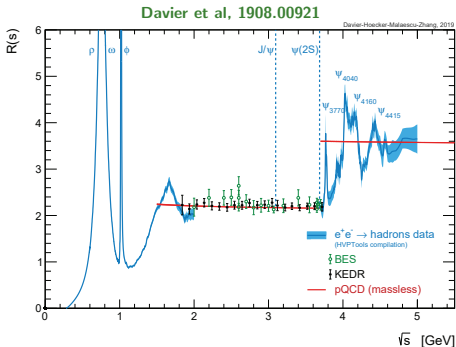
e^+e^- versus τ data



Isospin-breaking corrections: Cirigliano et al, hep-ph/0104267, hep-ph/0207310
 Flores-Baez et al, hep-ph/0608084

Updated in Miranda-Roig, 2007.11019

Major tensions in hadronic e^+e^- data

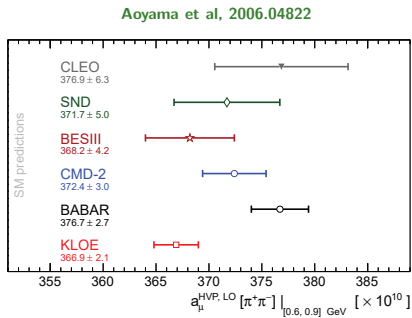
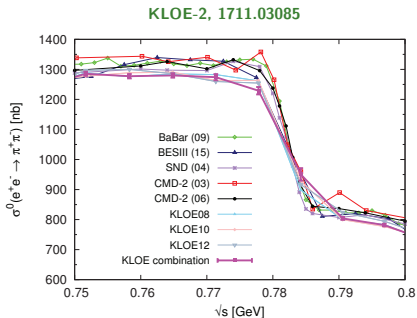


Experimental Discrepancies

- BaBar/KLOE disagreement at $\rho(\pi\pi)$
- Differences in $\phi(K^+K^-)$ largely exceed the quoted uncertainties
- Inclusive results larger than exclusive ones around 2 GeV

- Compilation of different data sets with quite different systematics
- Energy scanning versus Initial State Radiation method (BaBar, KLOE)
- Modelling of Final State Radiation needed (usually with scalar QED)
- The most relevant discrepancy for $a_\mu^{\text{HVP,LO}}$ is Babar vs KLOE at $\rho(\pi\pi)$

KLOE data vs other experiments



Discrepancies in the differential distribution are much larger than what gets reflected in the integral over the mass spectrum

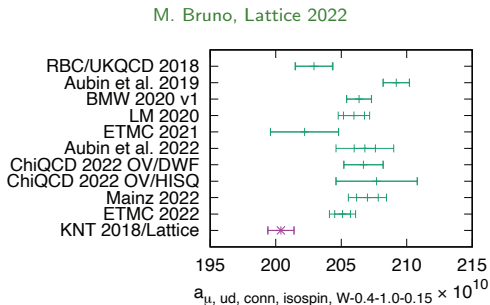
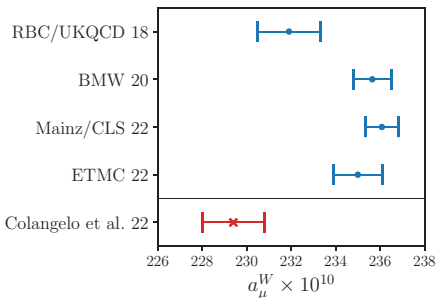
Compensating effects



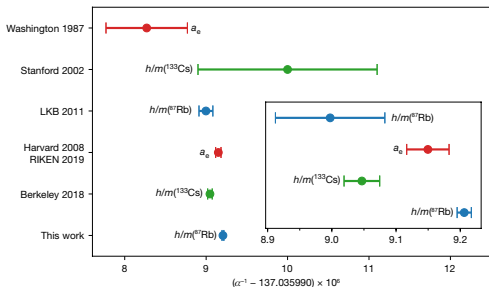
Underestimated systematics

Recent Lattice simulations agree with BMW & τ

Comparison performed with specific windows in Euclidean time to increase reliability



Electron Anomalous Magnetic Moment



Morel et al, Nature 588 (2020) 61

New measurement of α

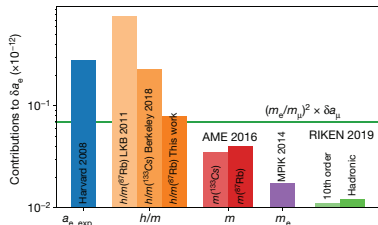
$$\alpha^{-1}(\text{Rb}) = 137.035\,999\,206 \quad (11)$$

8.1×10^{-11} accuracy

5.8 σ discrepancy with Cs experiment

$$\Delta a_e \equiv a_e^{\text{exp}} - a_e^{\text{SM}}$$

$$= \begin{cases} (-8.8 \pm 3.6) \cdot 10^{-13} & (\text{Cs}, -2.4\sigma) \\ (+4.8 \pm 3.0) \cdot 10^{-13} & (\text{Rb}, +1.6\sigma) \end{cases}$$



Summary

- Flavour structure and C/P are major pending questions
- Related to SSB \rightarrow Scalar Sector (Higgs)
- Important cosmological implications (Baryogenesis)
- Sensitive to New Physics: Flavour Anomalies!

Intriguing signals (Most anomalies related to 3rd family)

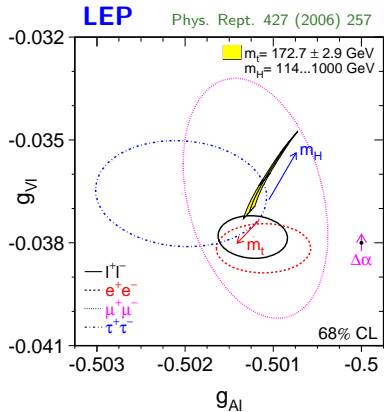
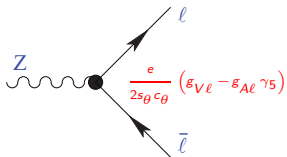
Many questions. Higher statistics & better systematics (QCD) needed

Eagerly awaiting new experimental results



Backup

Lepton Flavour Universality in Z Decays



V_{ij} Determinations

PDG 2022

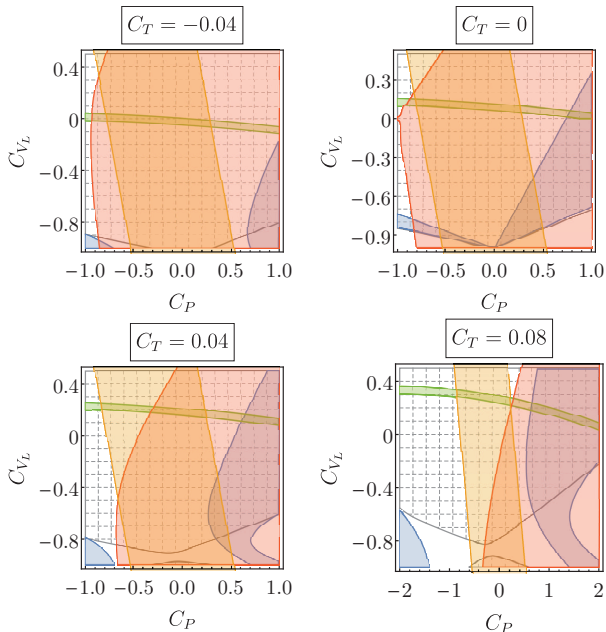
CKM	Value	Source
V_{ud}	0.97373 ± 0.00031	Nuclear β decay
V_{us}	0.2243 ± 0.0008	$K \rightarrow (\pi) l \nu$
V_{ub}	0.00382 ± 0.00020	$b \rightarrow ul \nu, B \rightarrow \pi l \nu$
V_{cd}	0.221 ± 0.004	$D \rightarrow (\pi) l \nu, \nu d \rightarrow c X$
V_{cs}	0.975 ± 0.006	$D \rightarrow K l \nu, D_s \rightarrow l \nu$
V_{cb}	0.0408 ± 0.0014	$b \rightarrow cl \nu, B \rightarrow D^{(*)} l \nu$
V_{td}	0.0086 ± 0.0002	$B_d^0 - \bar{B}_d^0$ mixing
V_{ts}	0.0415 ± 0.0009	$B_s^0 - \bar{B}_s^0$ mixing
V_{tb}	1.014 ± 0.029	$p\bar{p}, pp \rightarrow t\bar{b} + X$

} SM loop

$$\sum_j |V_{uj}|^2 = 0.9985 \quad (7) \quad , \quad \sum_j |V_{cj}|^2 = 1.001 \quad (12) \quad , \quad \sum_i |V_{ib}|^2 = 1.03 \quad (6)$$

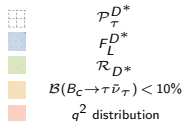
$$W \rightarrow l \bar{\nu}_e \quad \rightarrow \quad \sum_j (|V_{uj}|^2 + |V_{cj}|^2) = 2.002 \pm 0.027$$

D* Observables



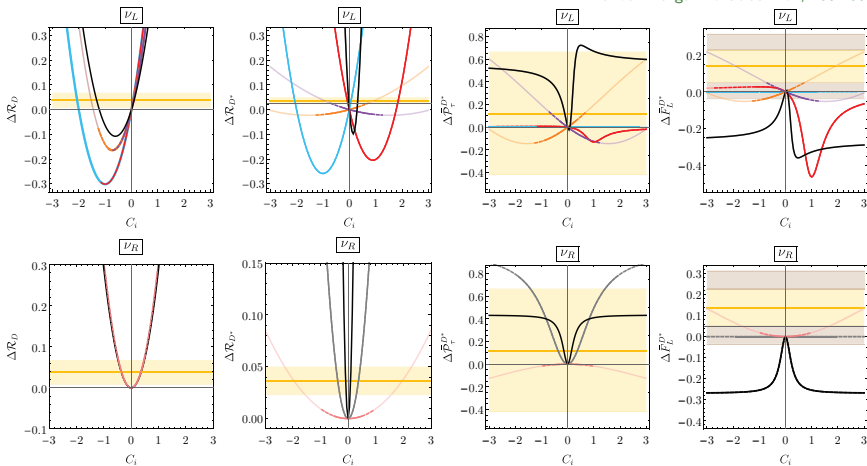
It is not possible to accommodate all D* data at 1σ

$$C_P \equiv C_{S_R} - C_{S_L}$$



Sensitivity to individual Wilson coefficients

Mandal-Murgui-Penüelas-Pich, 2004.06726



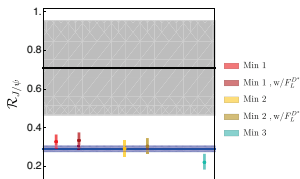
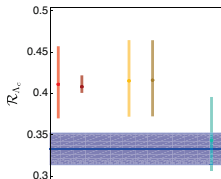
ν_L	C_{LL}^V	C_{RL}^V	C_{RL}^S	C_{LL}^S	C_{LL}^T
ν_R	$C_{LR}^V = C_{RR}^V$	$C_{RR}^S = C_{LR}^S$	C_{RR}^T		

F_L^{D*} always below
the exp. 1σ region

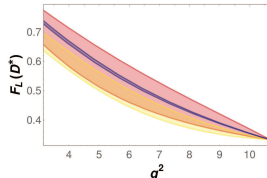
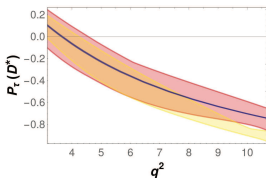
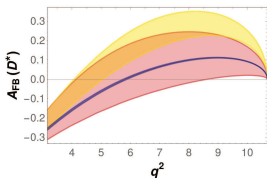
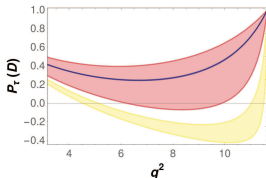
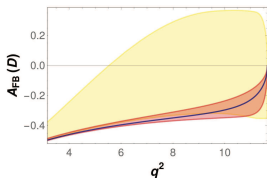
Solid (dashed) lines indicate ranges satisfying $\text{Br}(B_c \rightarrow \tau\nu) < 10\%$ (30%). Faint lines do not fulfil this constraint

Predictions from global fit:

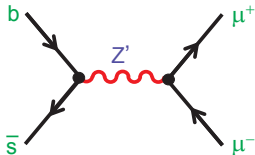
$$\frac{\mathcal{B}(\Lambda_b \rightarrow \Lambda_c \tau \bar{\nu}_\tau)}{\mathcal{B}(\Lambda_b \rightarrow \Lambda_c \ell \bar{\nu}_\ell)}$$



$$\frac{\mathcal{B}(B_c \rightarrow J\psi \tau \bar{\nu}_\tau)}{\mathcal{B}(B_c \rightarrow J\psi \ell \bar{\nu}_\ell)}$$



- Min 1
- Min 1, w/ $F_L^{D^*}$
- Min 2
- Min 2, w/ $F_L^{D^*}$
- Min 3

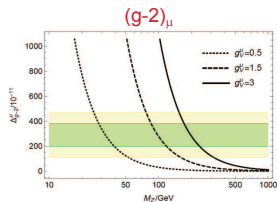
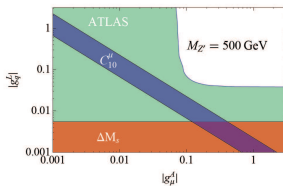
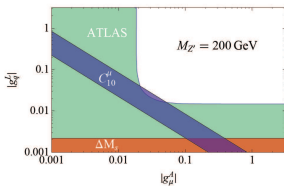
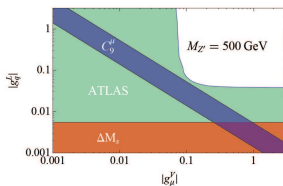
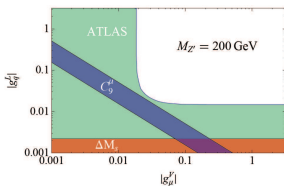


$$\mathcal{L} \supset \frac{g_2}{2c_W} Z'_\alpha \left\{ \left[\bar{s} \gamma^\alpha (g_L^Q P_L + g_R^Q P_R) b + h.c. \right] + \bar{\ell} \gamma^\alpha (g_V^\ell + \gamma_5 g_A^\ell) \ell \right\}$$



$$\frac{e^2}{16\pi^2} V_{tb} V_{ts}^* \cdot \{C_9^\ell, C_{10}^\ell\} = \frac{M_Z^2}{2m_{Z'}^2} \cdot \{g_L^Q g_V^\ell, g_L^Q g_A^\ell\}$$

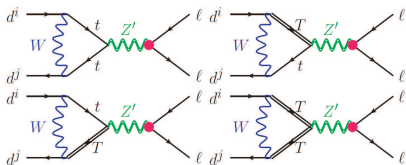
Di Chiara et al, 1704.06200



Many possibilities:

- $L_\mu - L_\tau$ Altmannshofer et al, ...
- $Z' + \text{VLQ}$ Kamenik et al
- Fermiophobic Falkowski et al
- Horizon. Sym. Guadagnoli et al
- ... Faisel-Tandean, ...

More possibilities...

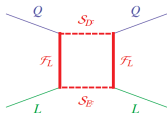
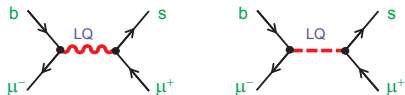


Flavour conserving Z'

Kamenik et al, 1704.06005

Leptoquarks

Hiller-Schmaltz, 1408.1627; Bauer et al, 1511.01900;
Hiller- Nisandzic, 1704.05444; D'Amico et al,
1704.05438; Becirevic-Sumensari, 1704.05835; ...



New Fermions and Scalars

D'Amico et al, 1704.05438; ...

LFUV \rightarrow LFV

Glashow-Guadagnoli-Lane, 1411.0565

$$\mathcal{H}_{NP} = G \bar{b}'_L \gamma^\lambda b'_L \bar{\tau}'_L \gamma_\lambda \tau'_L$$

$$b'_L = \sum_{i=1}^3 U_{L3i}^d d_{Li}, \quad \tau'_L = \sum_{i=1}^3 U_{L3i}^\ell \ell_{Li}$$

$$\mathcal{B}(B^+ \rightarrow K^+ \mu^\pm e^\mp) \cong 2\rho_{NP}^2 \left| \frac{U_{L31}^\ell}{U_{L32}^\ell} \right|^2 \mathcal{B}(B^+ \rightarrow K^+ \mu^+ \mu^-) = (2.16_{-1.50}^{+2.54}) \left| \frac{U_{L31}^\ell}{U_{L32}^\ell} \right|^2 \times 10^{-8}$$

Anatomy of ε'/ε calculation

$$\text{Re} \left(\frac{\varepsilon'}{\varepsilon} \right) = -\frac{\omega_+}{\sqrt{2}|\varepsilon|} \left\{ \frac{\text{Im} A_0^{(0)}}{\text{Re} A_0^{(0)}} (1 - \Omega_{\text{eff}}) - \frac{\text{Im} A_2^{\text{emp}}}{\text{Re} A_2^{(0)}} \right\}$$

$$\mathcal{A}_n^{(X)} = a_n^{(X)} \left[1 + \Delta_L \mathcal{A}_n^{(X)} + \Delta_C \mathcal{A}_n^{(X)} \right]$$

Cirigliano-Gisbert-Pich-Rodríguez 2019

- ① $O(p^4)$ χ PT Loops: Large correction (NLO in $1/N_C$) FSI

$$\Delta_L \mathcal{A}_{1/2}^{(8)} = 0.27 + 0.47i \quad ; \quad \Delta_L \mathcal{A}_{3/2}^{(g)} = -0.50 - 0.21i$$

- ② $O(p^4)$ LECs fixed at $N_C \rightarrow \infty$: Small correction

$$\Delta_C [A_{1/2}^{(8)}]^- = 0.10 \pm 0.05 \quad ; \quad \Delta_C [A_{3/2}^{(g)}]^- = -0.19 \pm 0.19$$

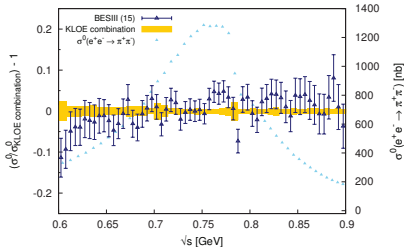
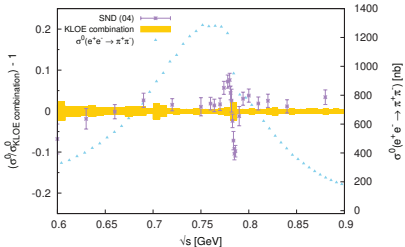
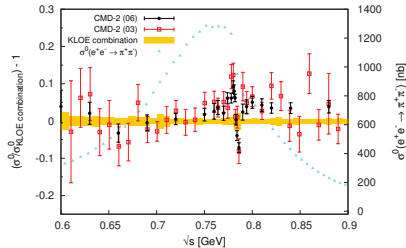
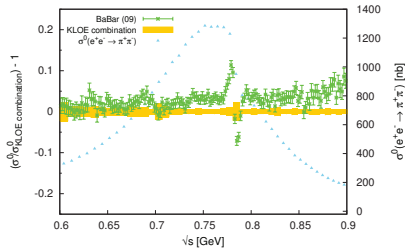
- ③ Isospin Breaking $O[(m_u - m_d)p^2, e^2 p^2]$: Sizeable correction

$$\Omega_{\text{eff}} = 0.11 \pm 0.09$$

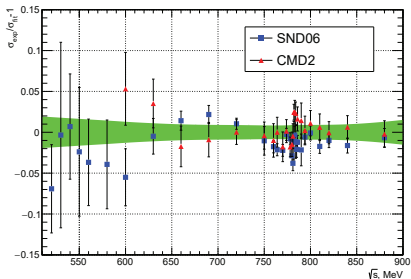
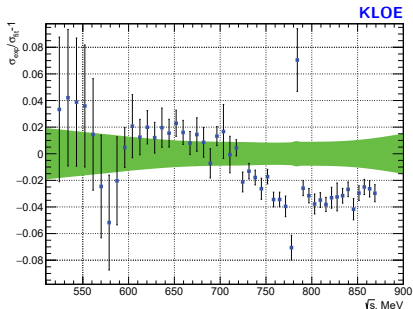
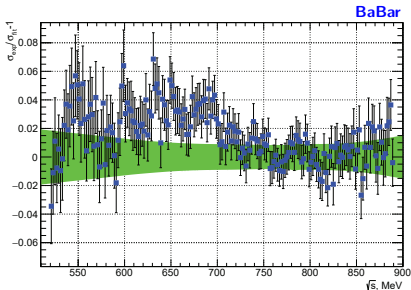
- ④ $\text{Re}(g_8)$, $\text{Re}(g_{27})$, $\chi_0 - \chi_2$ fitted to data

KLOE data vs other experiments

KLOE-2, 1711.03085



Internal tensions also among the three KLOE datasets: 2008, 2010, 2012

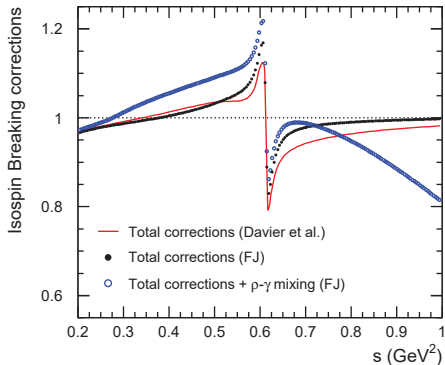


Measurement	$a_{\mu}(\pi\pi) \times 10^{10}$
This work	$409.79 \pm 1.44 \pm 3.87$
SND06	$406.47 \pm 1.74 \pm 5.28$
BaBar	$413.58 \pm 2.04 \pm 2.29$
KLOE	$403.39 \pm 0.72 \pm 2.50$

$$525 \text{ MeV} \leq \sqrt{s} \leq 883 \text{ MeV}$$

Isospin-breaking corrections applied to τ data

Z. Zhang, 1511.05405



In order to achieve compatibility with e^+e^- data, FJ introduces huge IB corrections (blue line), which are not supported by the explicit calculations available

My Personal Summary

- Unsatisfactory situation
- Large (underestimated) systematic errors
- Better data samples needed
Belle-II, Beijing, Novosibirsk
- Lattice will certainly help
- Forthcoming MUonE experiment at CERN: $\sigma(\mu e \rightarrow \mu e)$
Measure $\Pi_{\text{em}}(Q^2)$ with space-like data

The μ anomaly does not necessarily imply New Physics



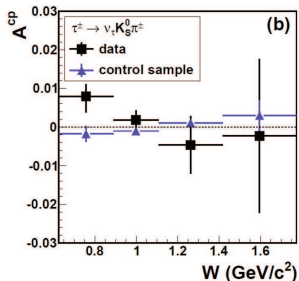
CP Asymmetry

$$A_\tau \equiv \frac{\Gamma(\tau^+ \rightarrow \pi^+ K_S \bar{\nu}_\tau) - \Gamma(\tau^- \rightarrow \pi^- K_S \nu_\tau)}{\Gamma(\tau^+ \rightarrow \pi^+ K_S \bar{\nu}_\tau) + \Gamma(\tau^- \rightarrow \pi^- K_S \nu_\tau)} = (-3.6 \pm 2.3 \pm 1.1) \cdot 10^{-3} \quad \text{BaBar'11} \\ (\geq 0 \pi^0)$$

$$A_\tau^{\text{SM}}(\tau^+ \rightarrow \pi^+ K_S \bar{\nu}_\tau) = (3.6 \pm 0.1) \cdot 10^{-3} \quad \text{Bigi-Sanda, Grossman-Nir} \quad \mathbf{2.8 \sigma \text{ discrepancy}}$$



Belle does not see any asymmetry at the 10^{-2} level



$$A_i^{\text{CP}} \simeq \langle \cos \beta \cos \psi \rangle_i^{\tau^-} - \langle \cos \beta \cos \psi \rangle_i^{\tau^+}$$

bins (i) of $W = \sqrt{Q^2}$

$\beta = K_S$ direction in hadronic rest frame

$\psi = \tau$ direction

BaBar signal incompatible (with EFT)
with other sets of flavour data

Cirigliano-Crivellin-Hoferichter, 1712.06595

Rendón-Roig-Toledo, 1902.08143