

# Twisted Nanoresonators for Hyperbolic Light

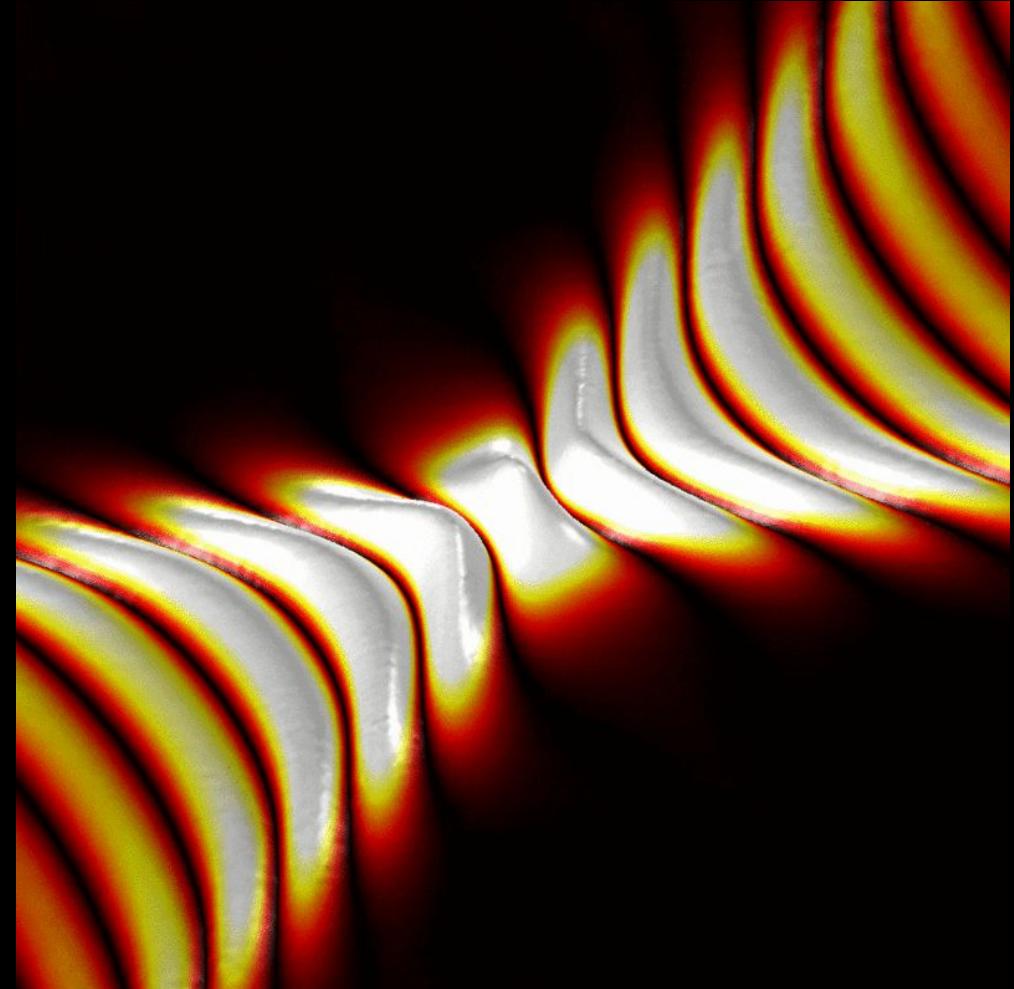
Kirill Voronin, Alexey Nikitin



Donostia International Physics Center



"la Caixa" Foundation



Science 359, 892 (2018)

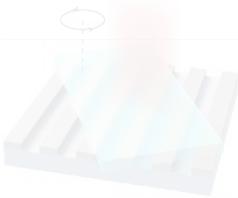
# Outline



**Introduction. Hyperbolic nanooptics with van der Waals crystals**



Elliptical and hyperbolic phonon-polaritons in  $\alpha\text{-MoO}_3$ . Twisted nanooptics

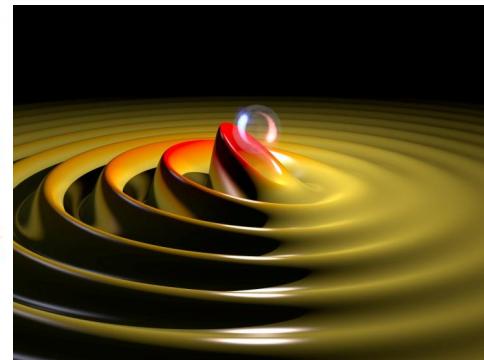
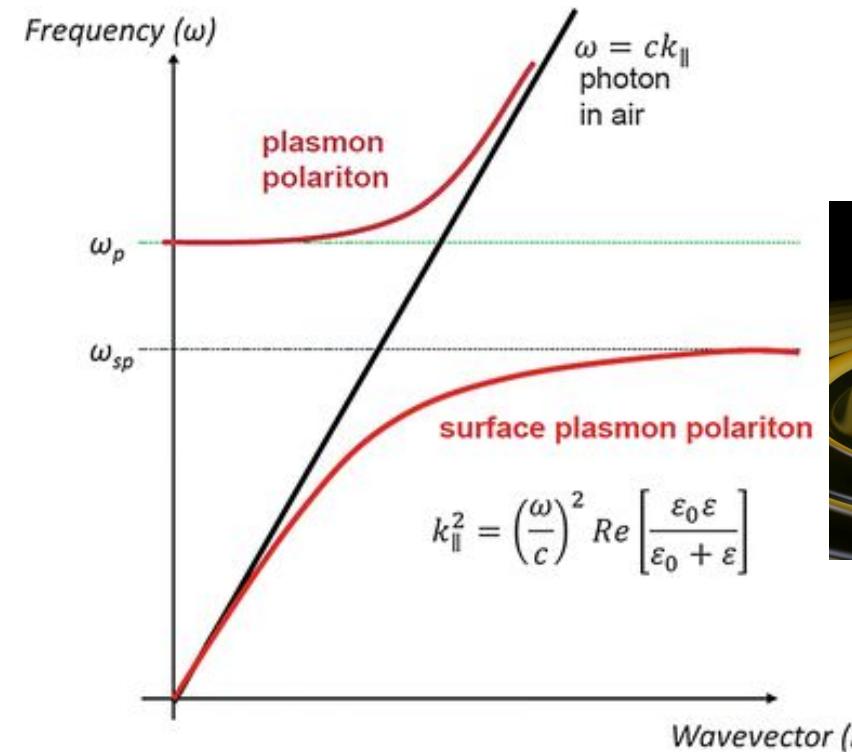
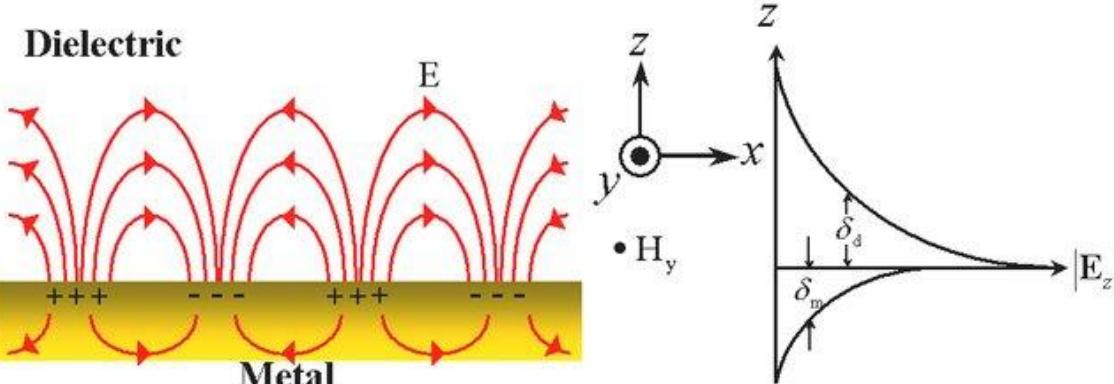


Far- and near-field measurements of resonances in rotated structures

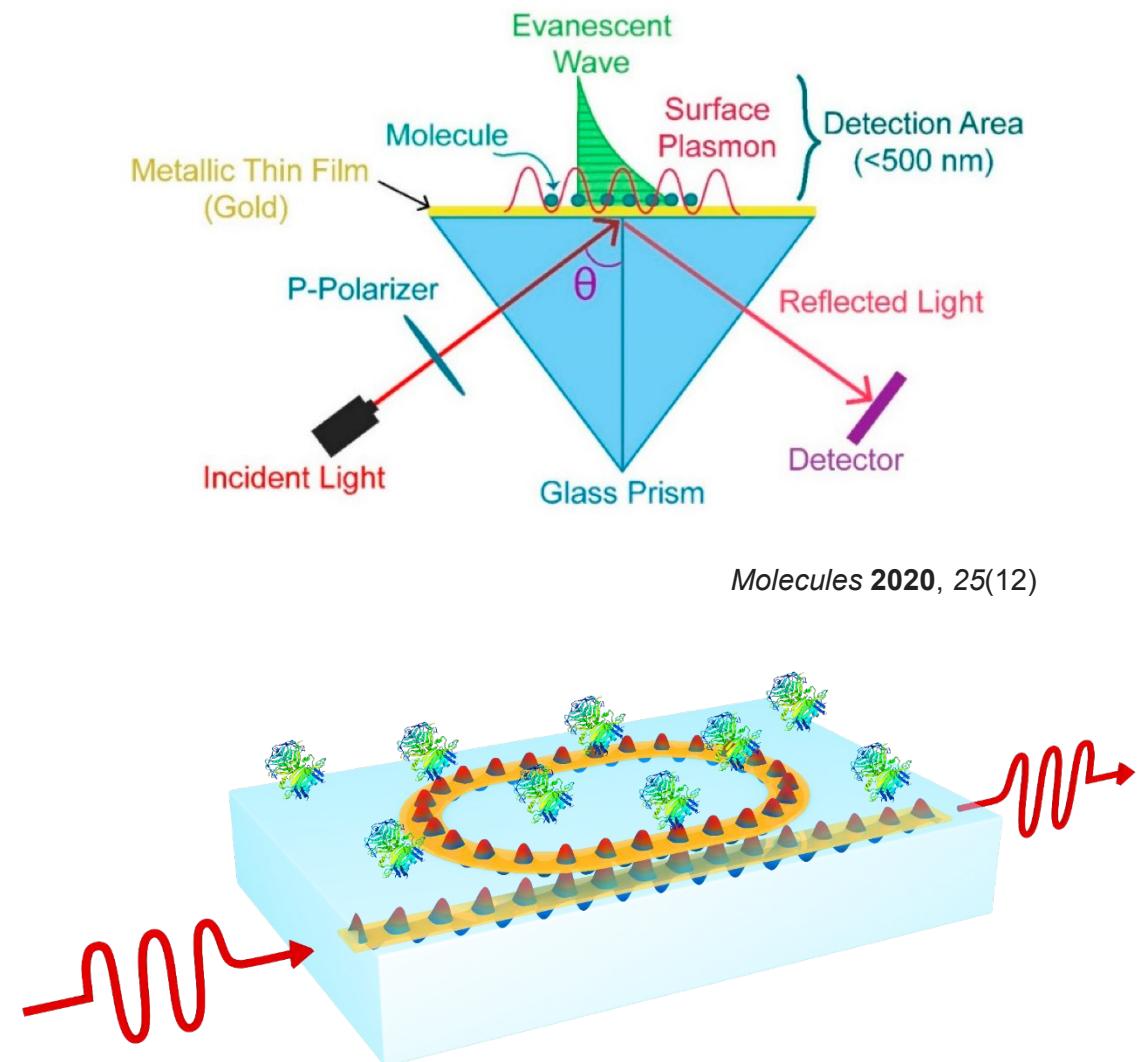


Mapping of dispersion surface

# Plasmon polaritons

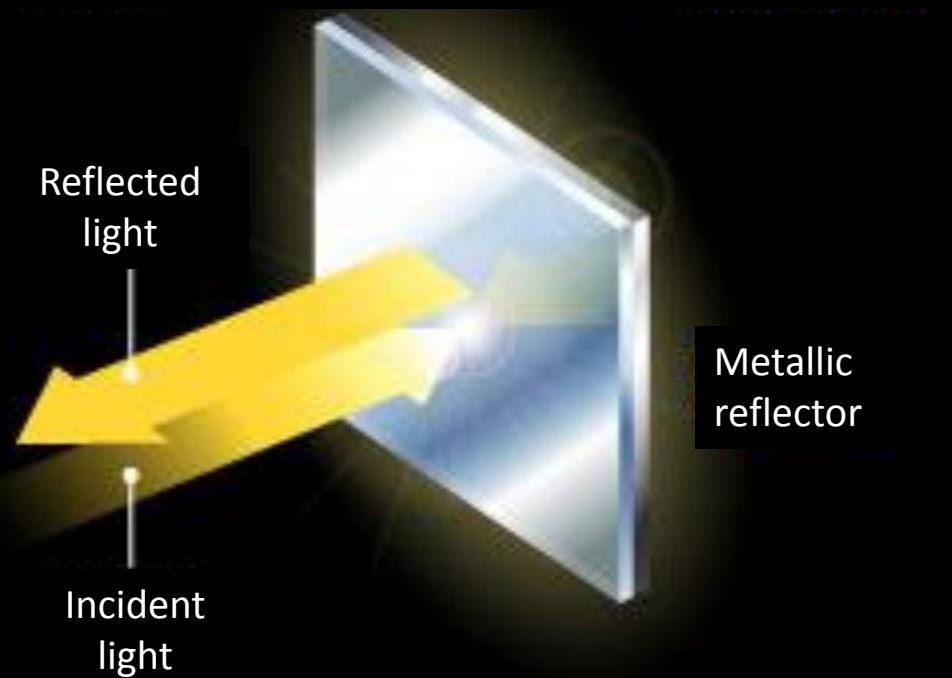


Science 340, 328 (2013)

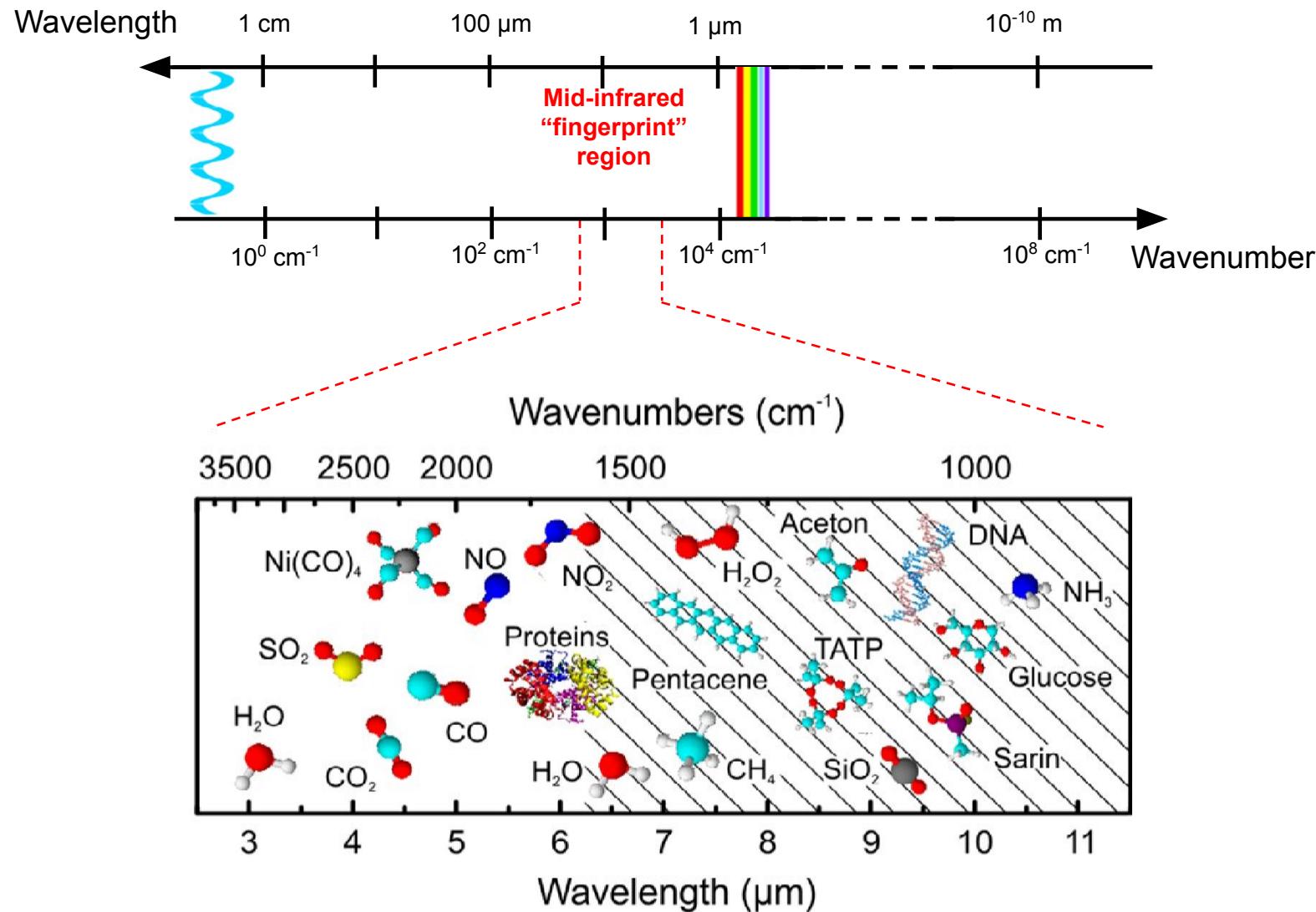


Sensors 2020, 20(1), 203

# Metals at mid-IR frequencies behave like mirrors

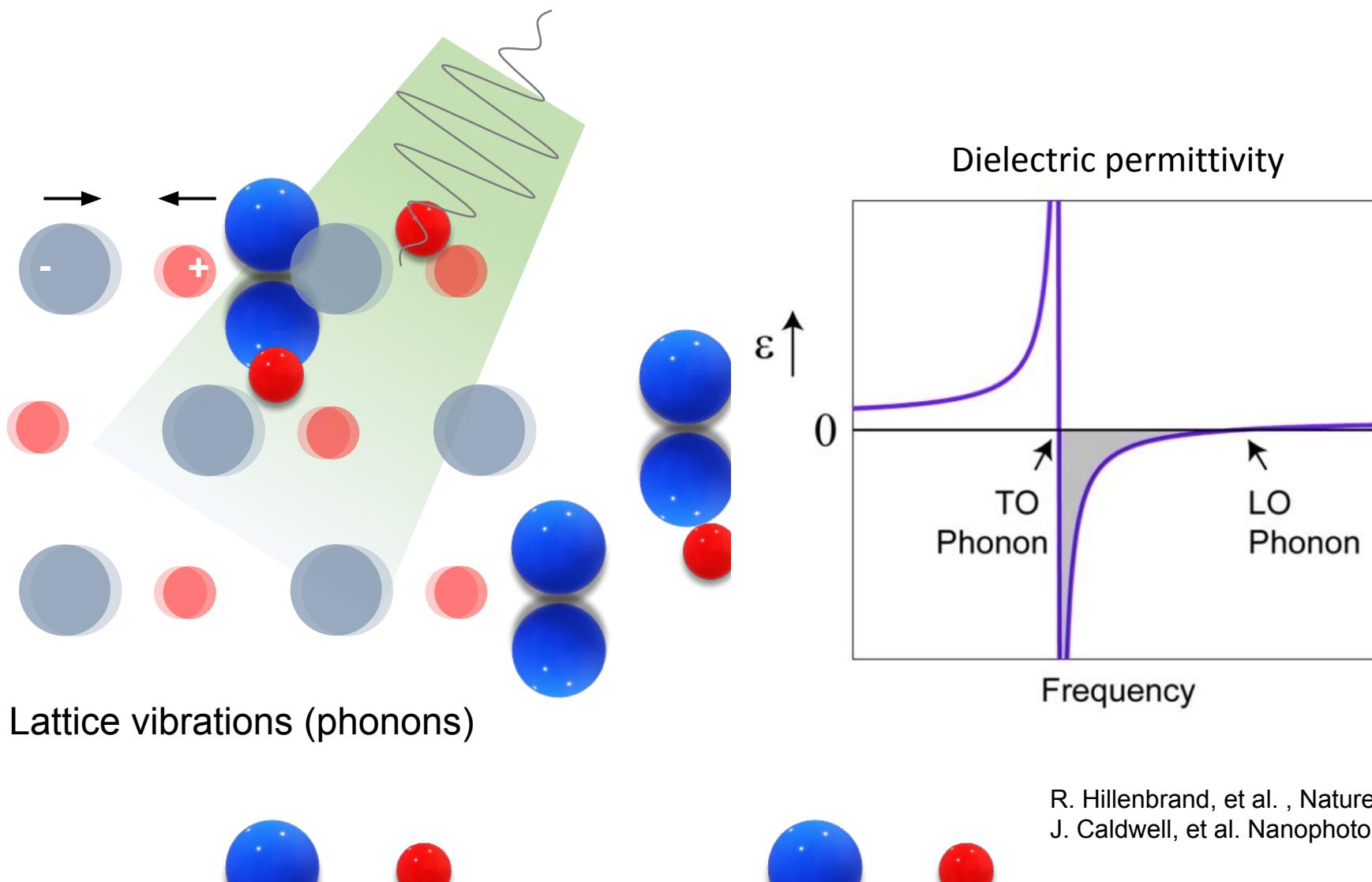


# Mid-IR molecular spectroscopy



F. Neubrech et al., Chem. Rev. 117, 5110 (2017)

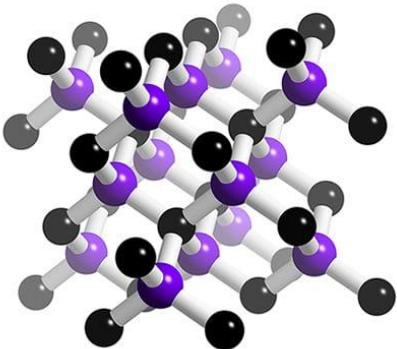
# Phonon polaritons



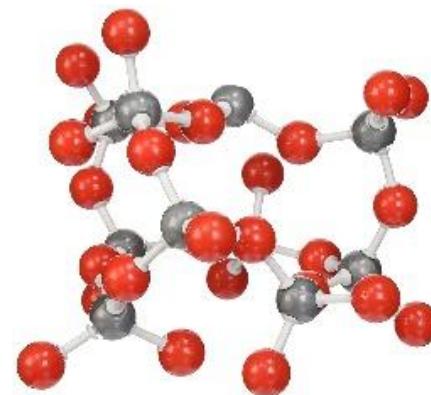
R. Hillenbrand, et al. , Nature **418**, 159, (2002)  
J. Caldwell, et al. Nanophotonics **4**, 44 (2015)

# Polar bulk crystals

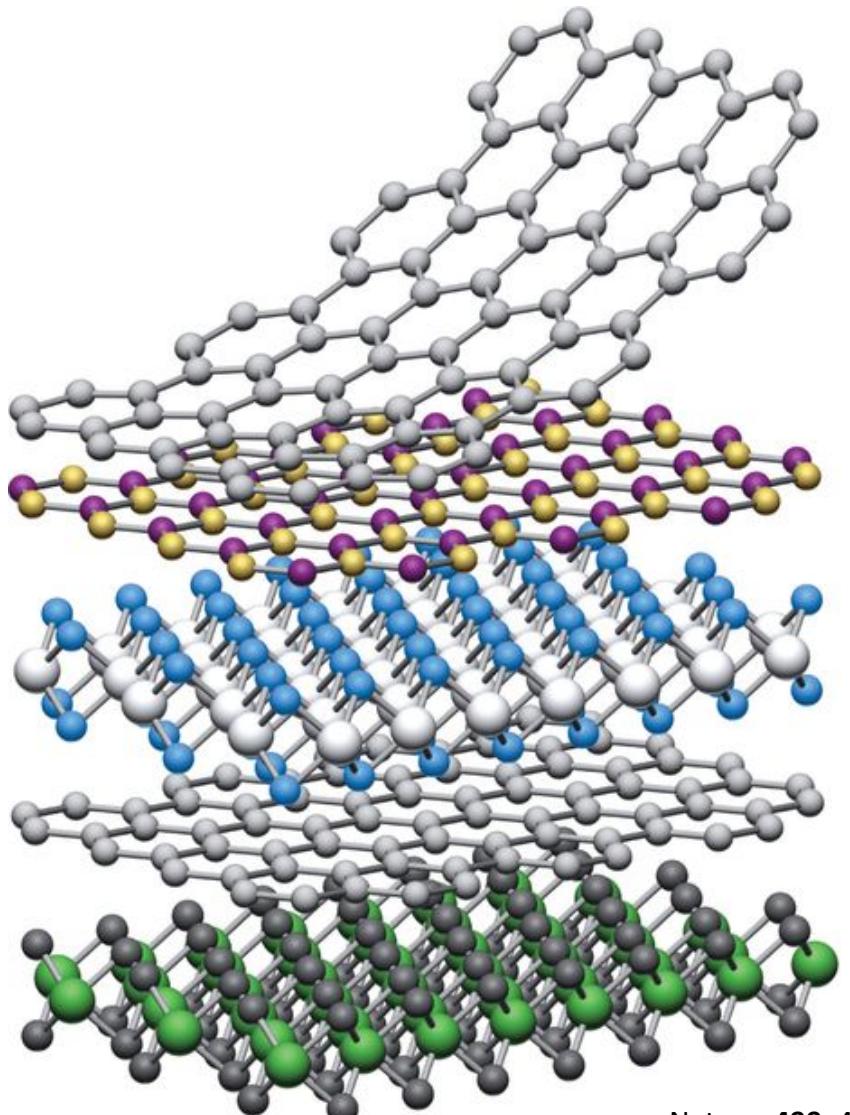
**SiC**



**SiO<sub>2</sub>**



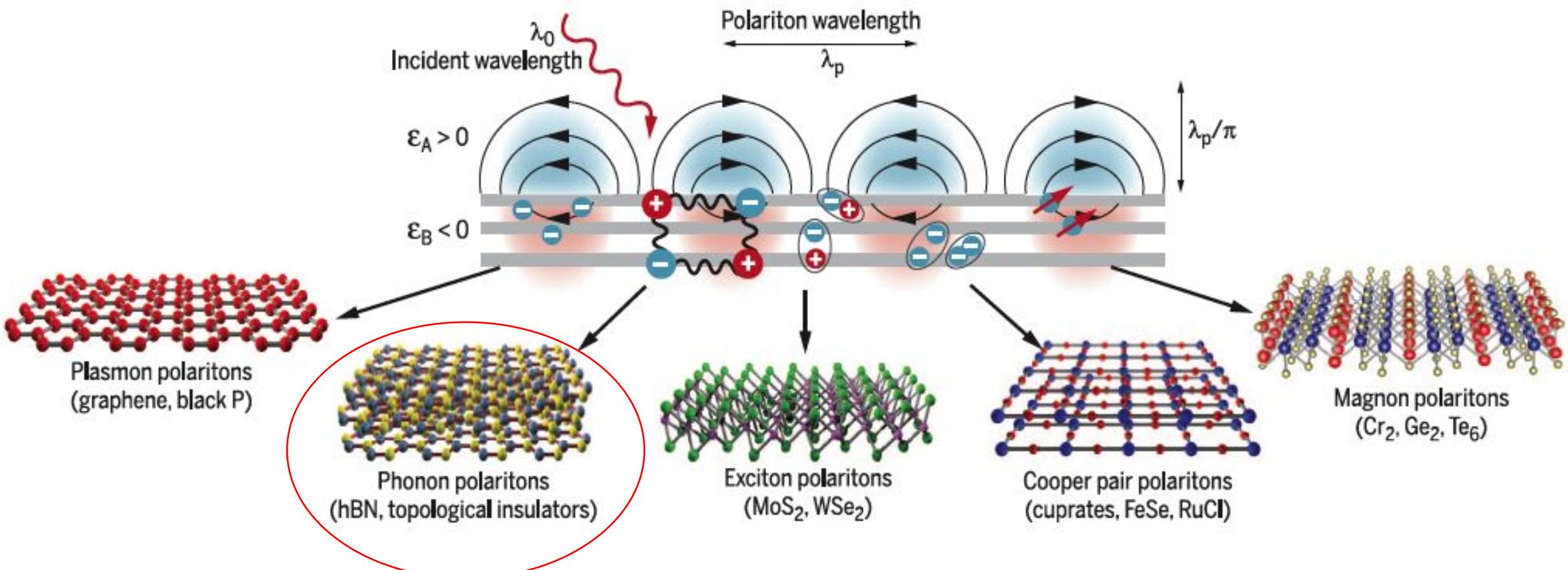
# Van der Waals materials



Nature 499, 419 (2013)

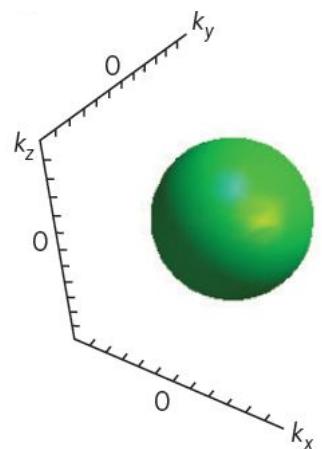
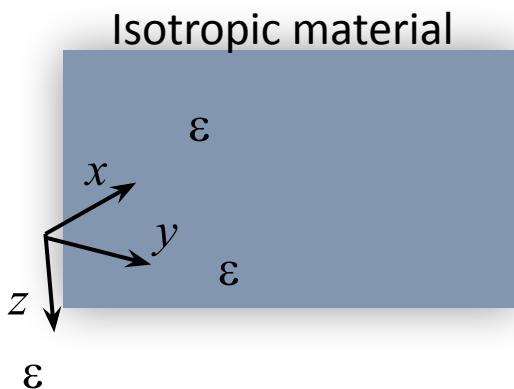


# Polaritons in van der Waals materials



Science 354, 1992 (2016)  
Nature Mat. 16, 182 (2017)

# Dispersion of polaritons in hyperbolic media



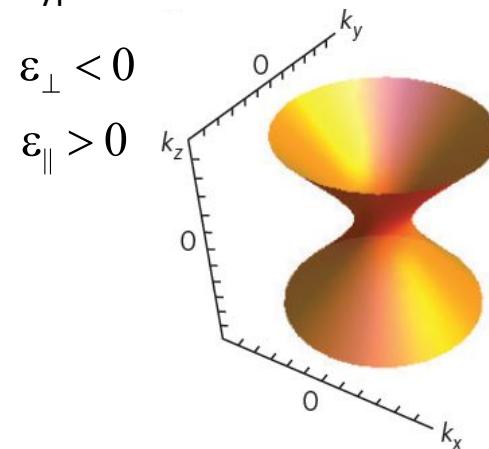
Isofrequency surface spheroid

$$\frac{k_x^2}{\epsilon} + \frac{k_y^2}{\epsilon} + \frac{k_z^2}{\epsilon} = \frac{\omega^2}{c^2}$$

Uniaxial hyperbolic crystal



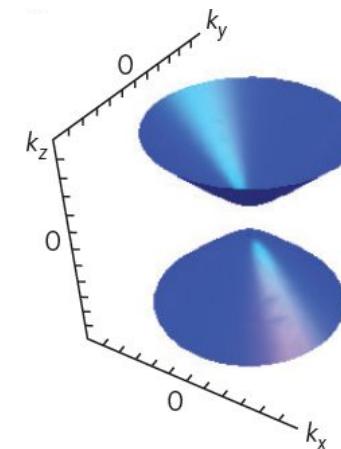
Type II



Isofrequency surface hyperboloid

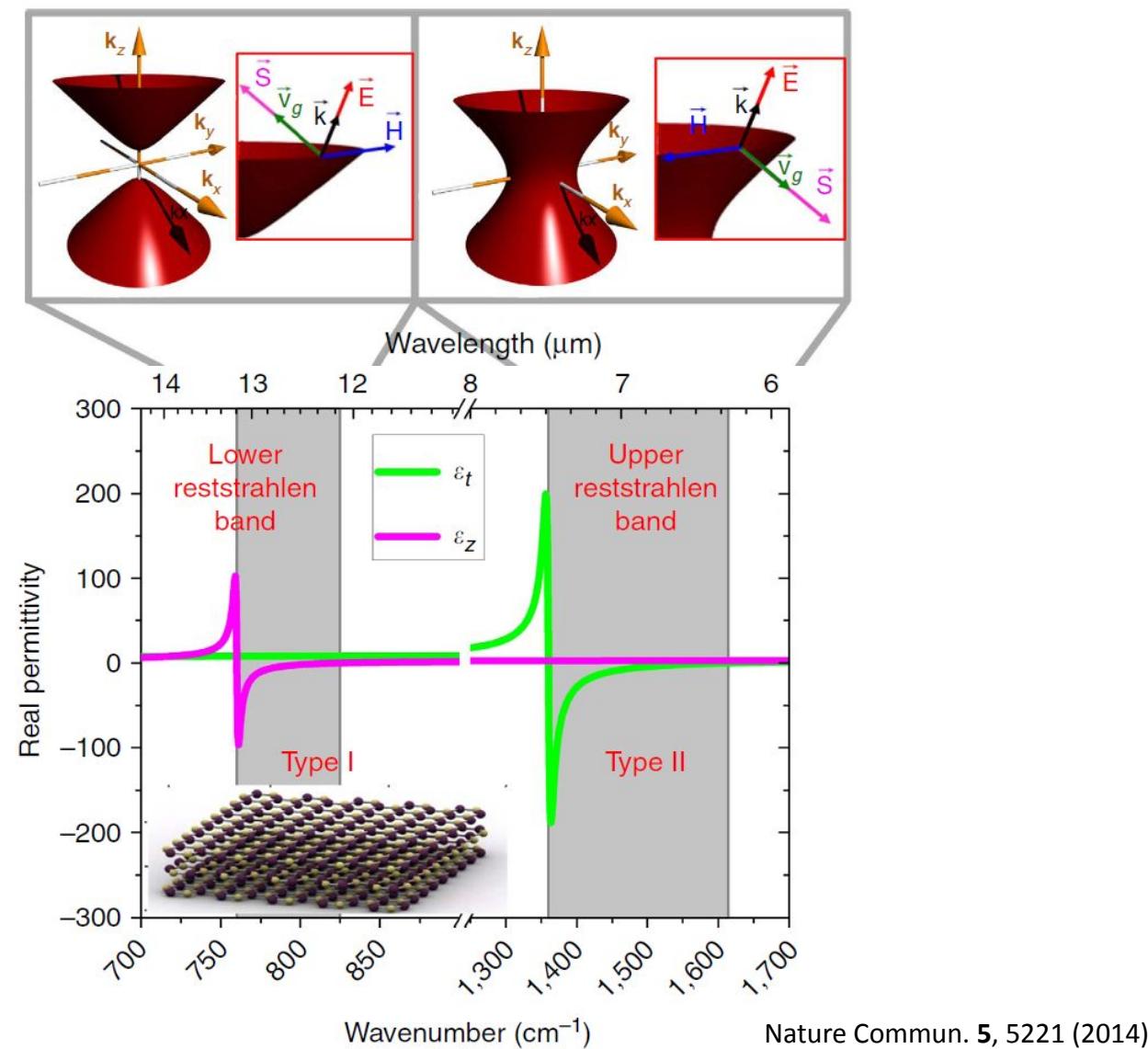
$$\frac{k_z^2}{\epsilon_{\perp}} + \frac{k_x^2 + k_y^2}{\epsilon_{\parallel}} = \frac{\omega^2}{c^2}$$

Type I  
 $\epsilon_{\perp} > 0$   
 $\epsilon_{\parallel} < 0$

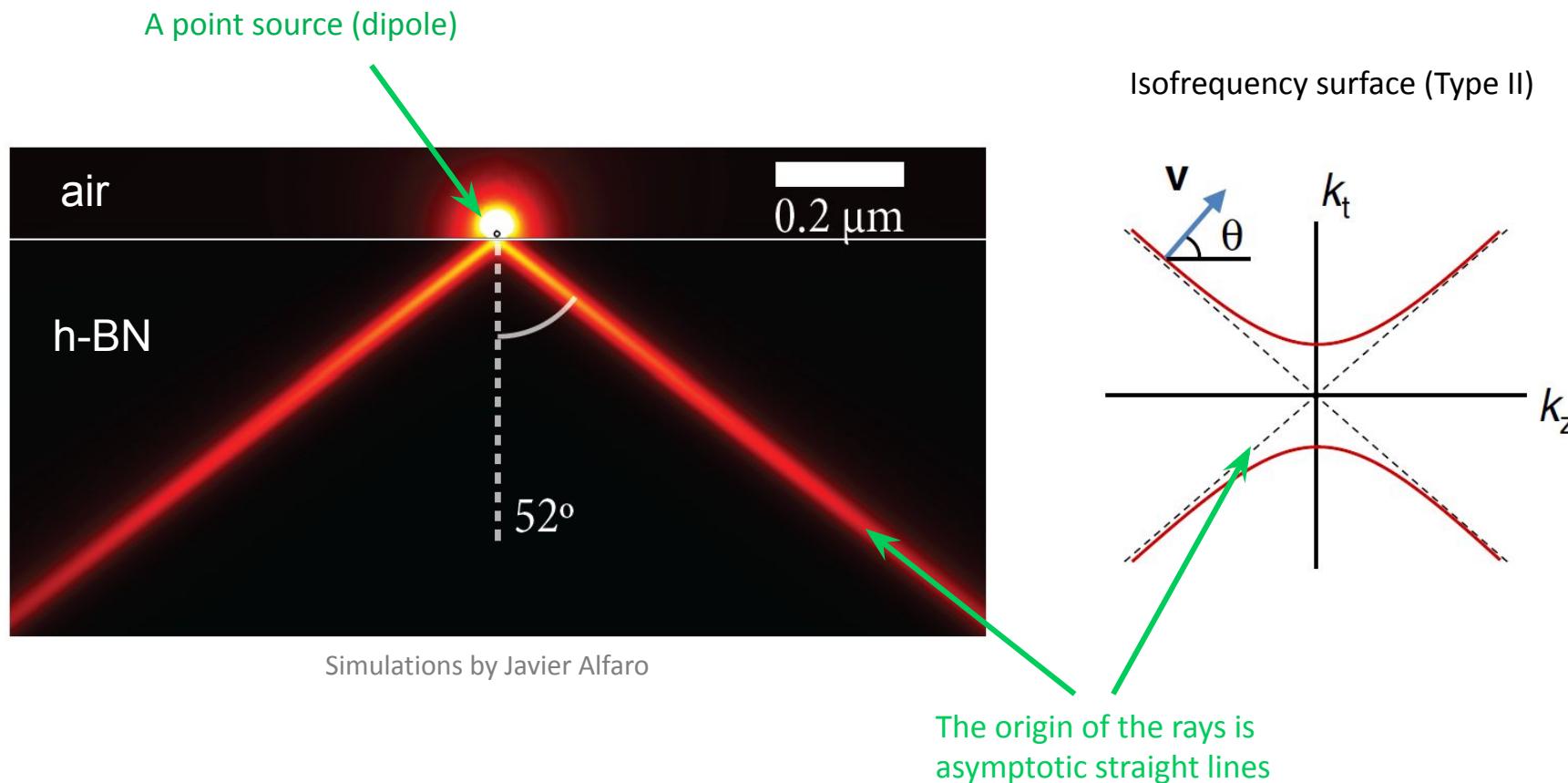


Nature Photon. 9, 214 (2015)

# h-BN: a natural hyperbolic material

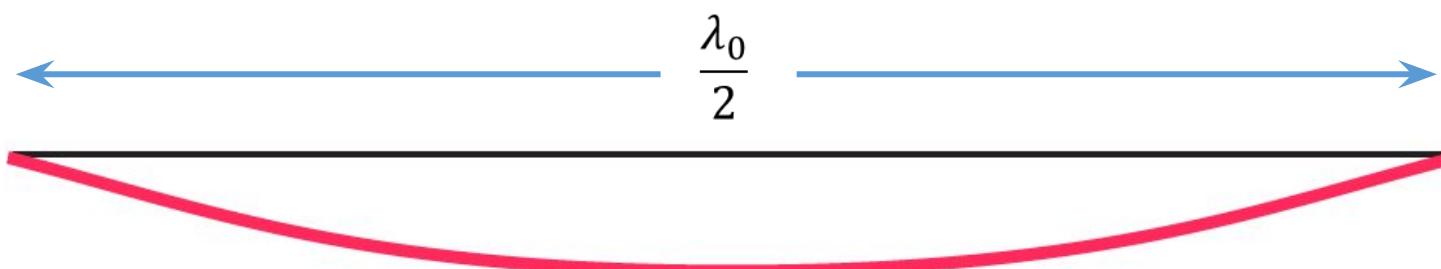
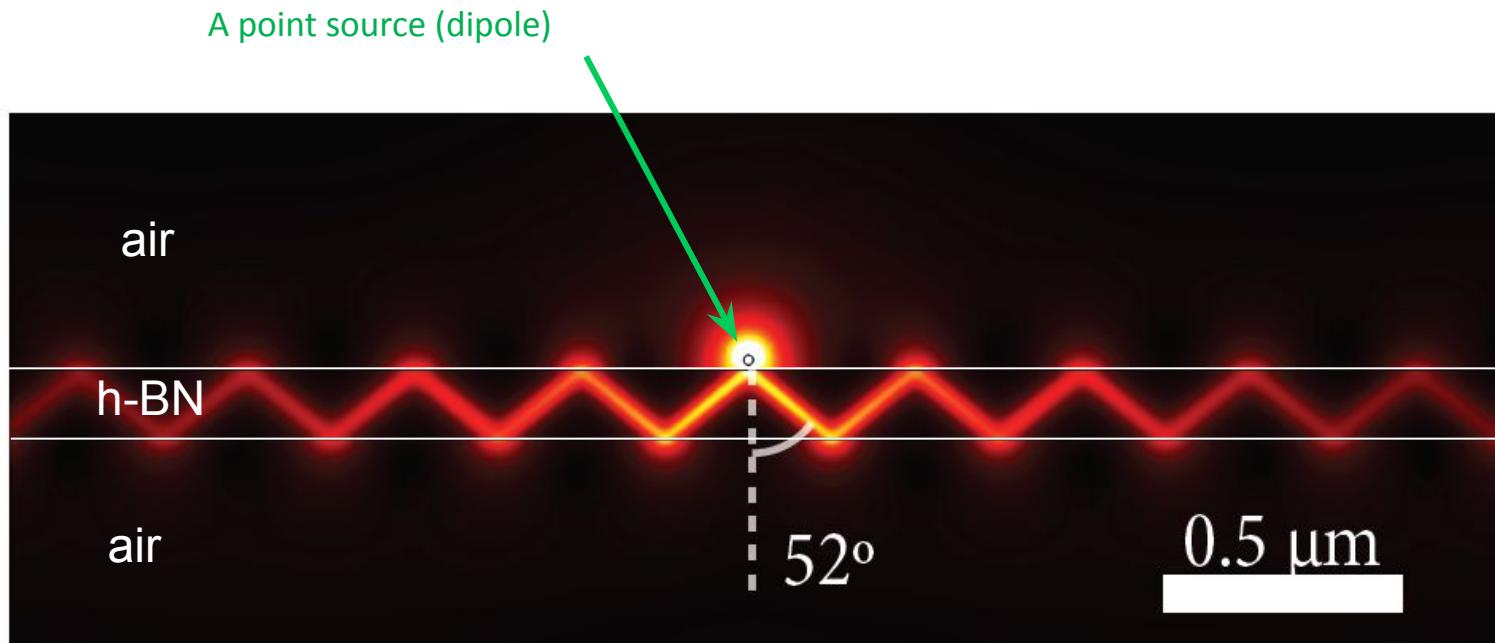


# Polaritons in hyperboilc media



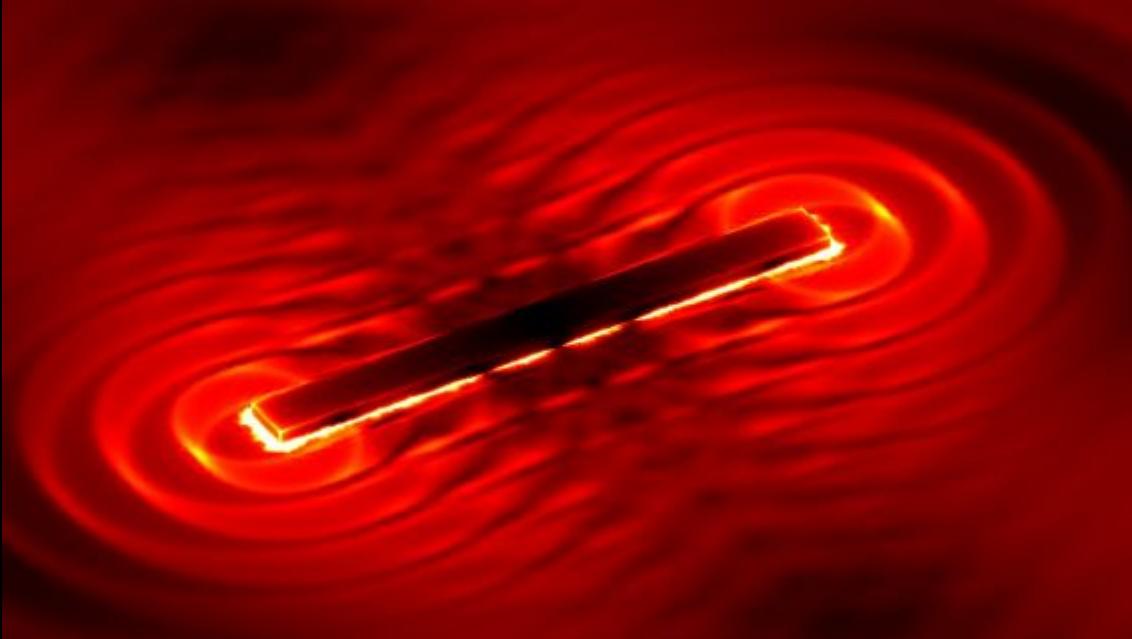
Due to the hyperbolic dispersion, the waves travelling inside h-BN crystals form rays

# Polaritons in thin hyperboilc slabs



When a h-BN crystal has a finite thickness (slab), the rays reflect from the faces of the slab forming the subwavelength zig-zag pattern

# Hyperbolic polaritons launched by an Au antenna



Simulations by Pablo Pons

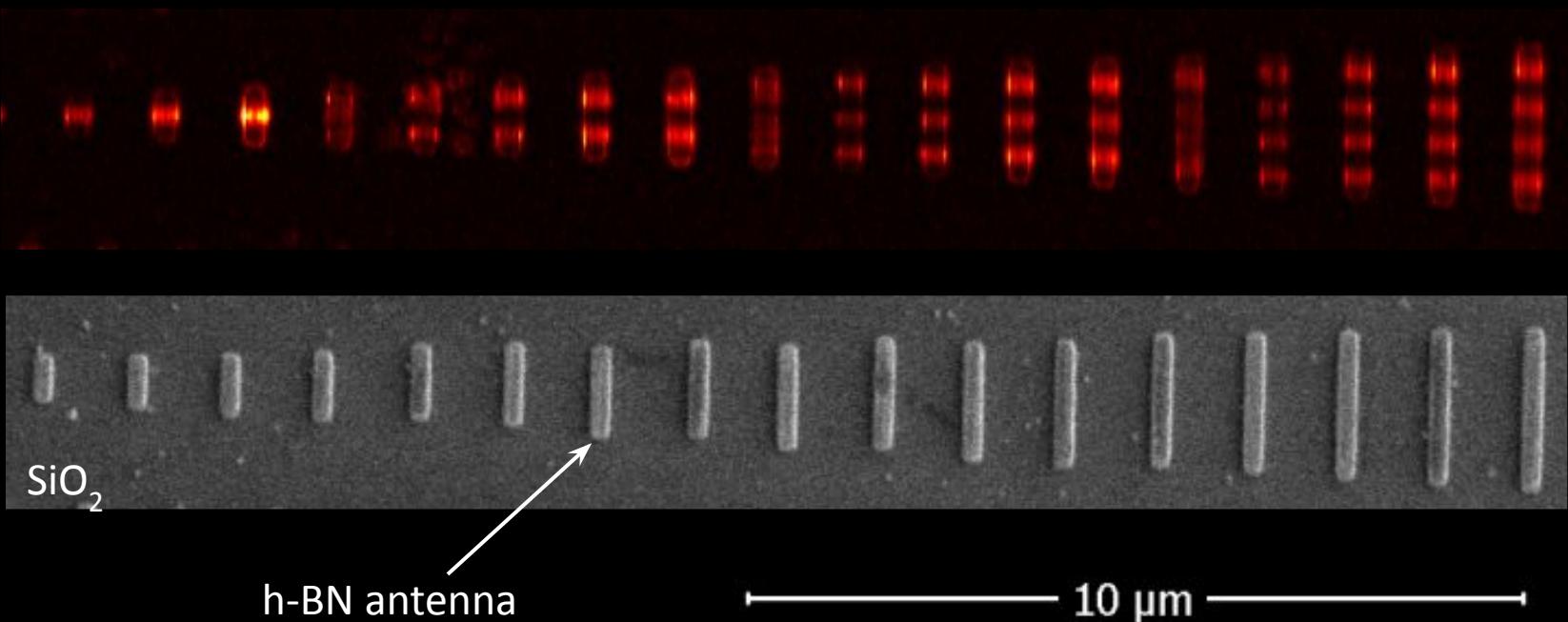
Au antenna



P. Pons et al, Nature Commun. 10, 3242 (2019)

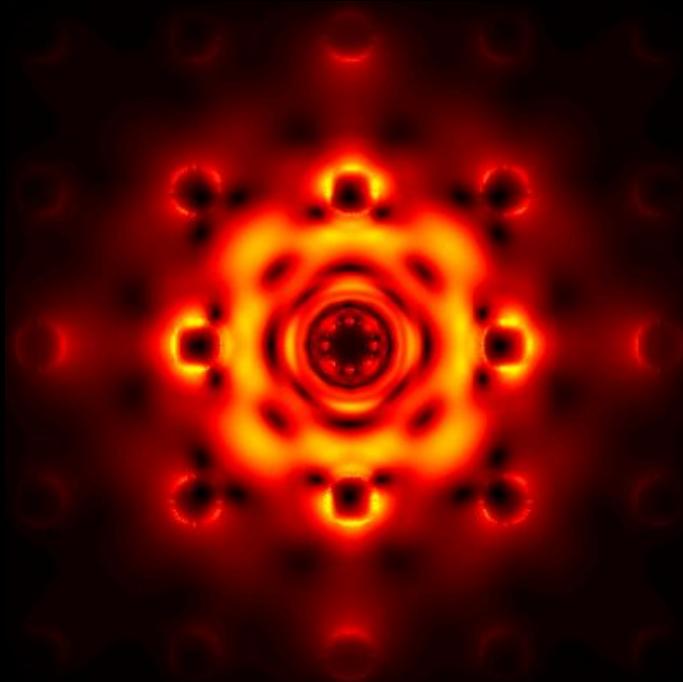
# Localized hyperbolic polaritons

Experiments by Javier Alfaro



J. Alfaro et al, Nature Commun. 8, 15624 (2017)

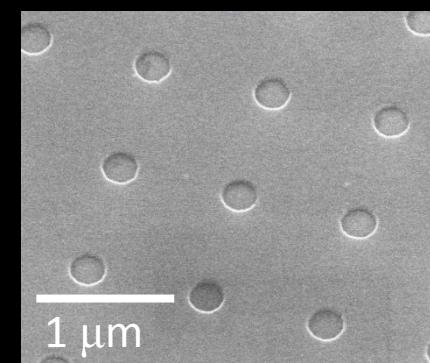
# Hyperbolic polaritons in h-BN photonic crystal



See poster by Nathaniel Capote

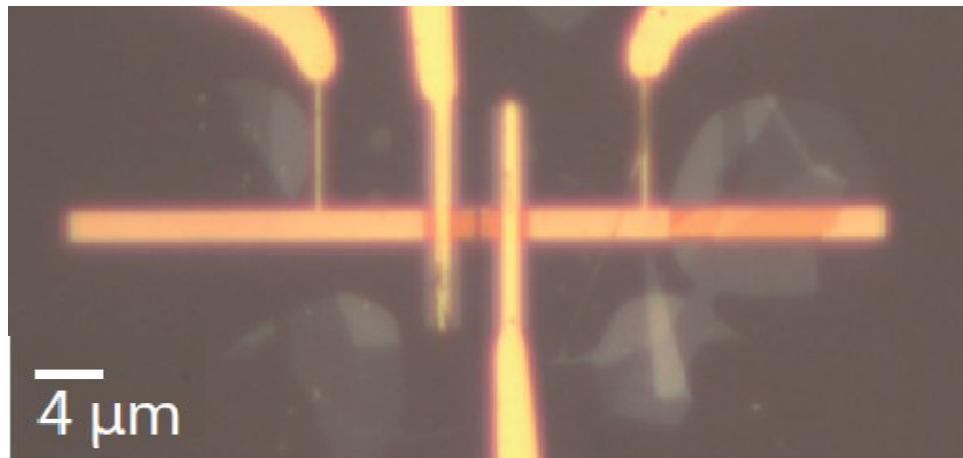
Simulations by Sergio Gutierrez

J. Alfaro et al, Nature Commun. 10, 42 (2019)

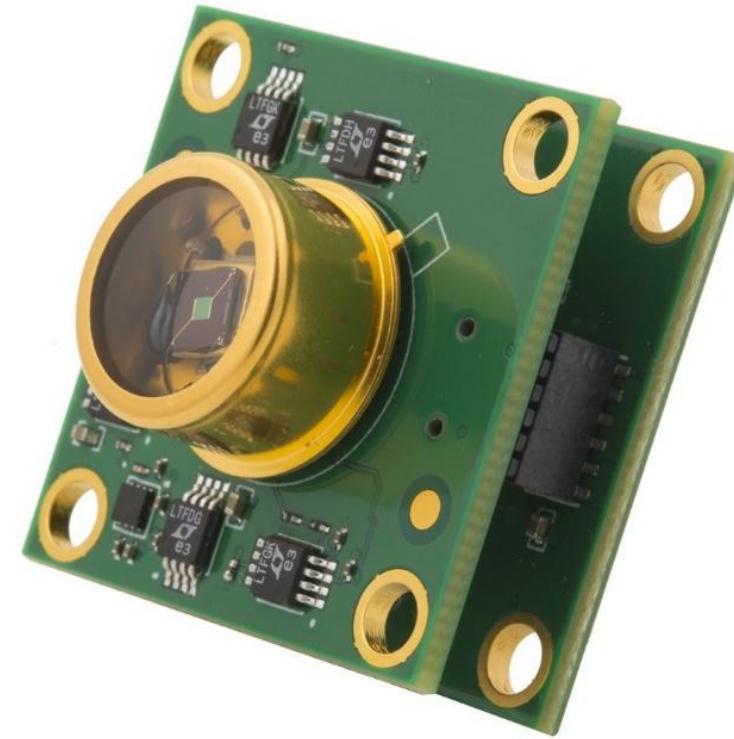
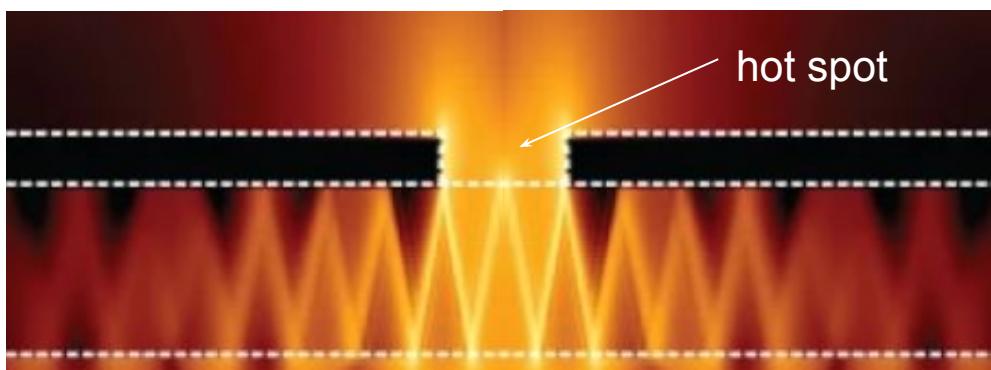


# Antenna-integrated graphene photodetector

Top view



Side view (zoom-in)



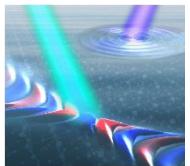
<http://www.emberion.com>

S. Castilla et. al, Nano Lett. **19**, 2765 (2019)

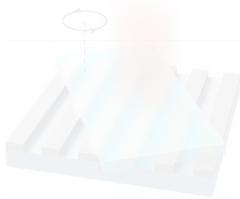
# Outline



Introduction. Hyperbolic nano optics with van der Waals crystals



**Elliptical and hyperbolic phonon-polaritons in  $\alpha\text{-MoO}_3$ . Twisted nano optics**

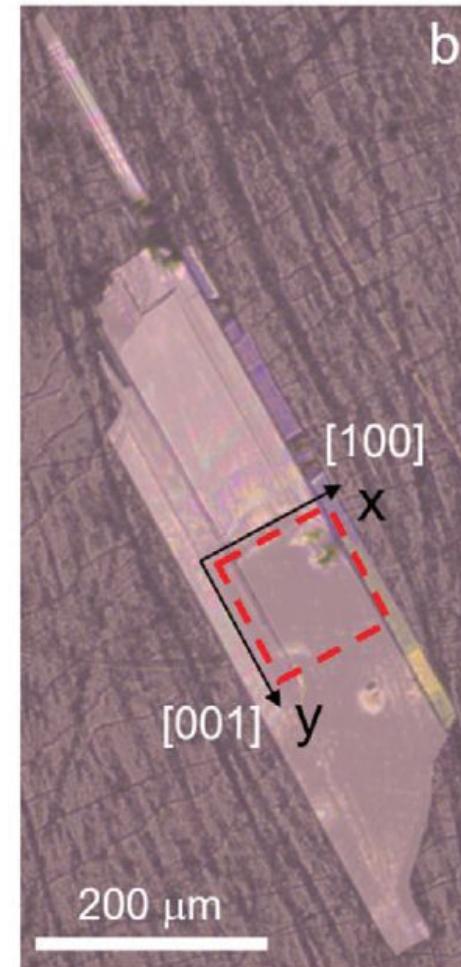
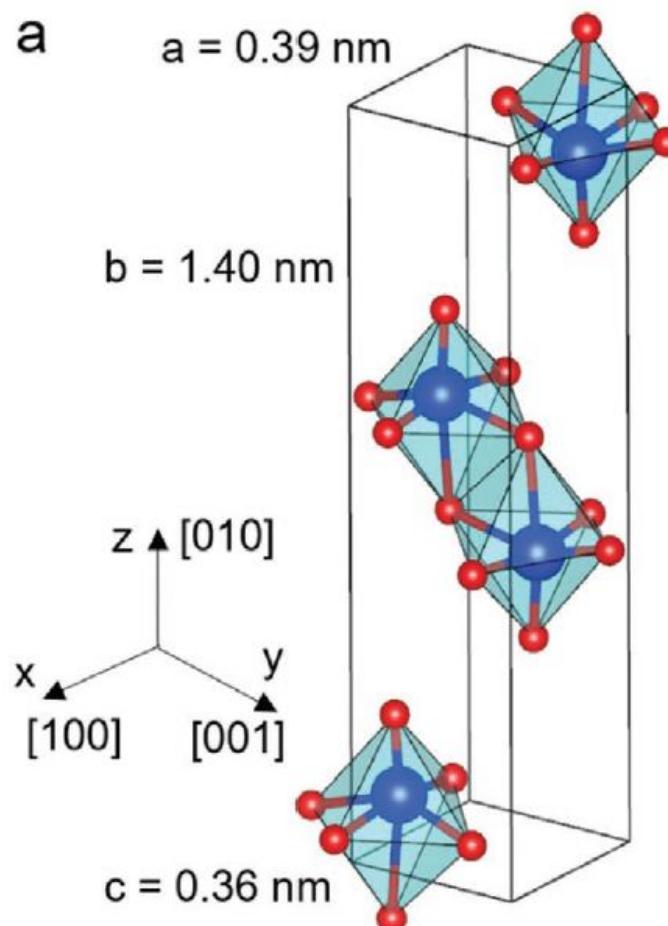
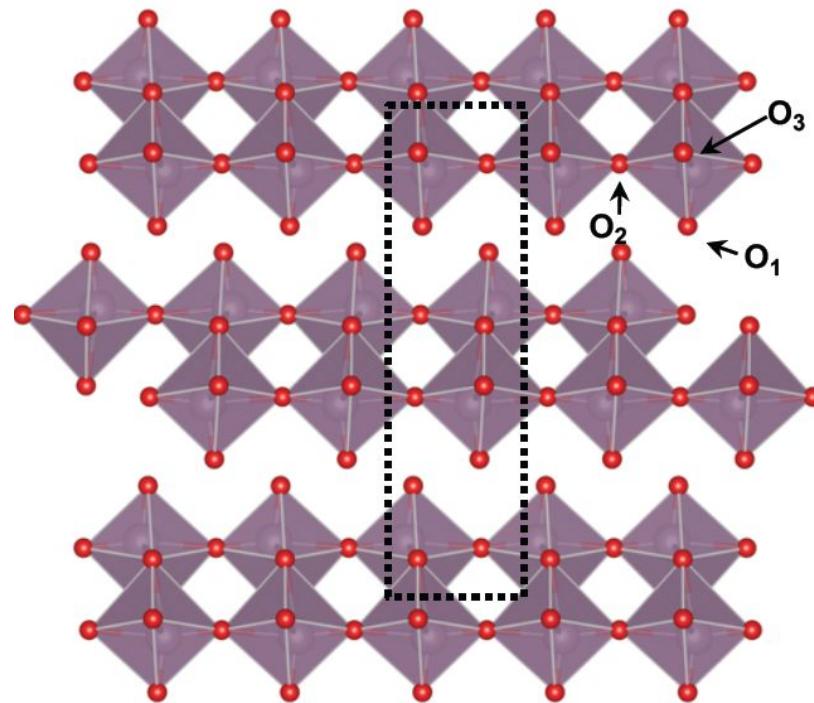


Far- and near-field measurements of resonances in rotated structures



Mapping of dispersion surface

# Biaxial van der Waals crystal, $\alpha\text{-MoO}_3$

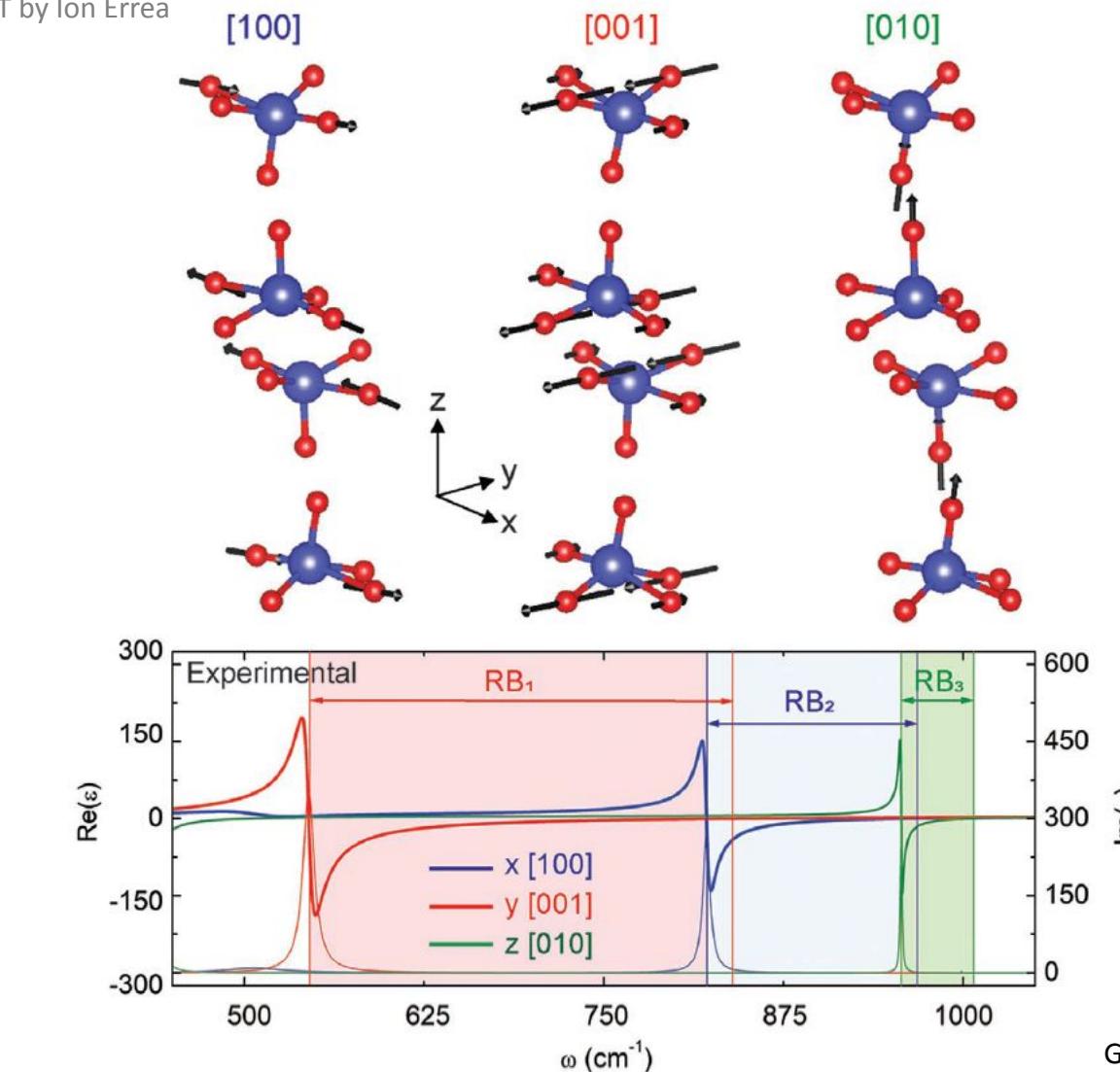


$\alpha\text{-MoO}_3$  crystals are anisotropic due to their molecular structure.  
They show a strong narrow-band phononic response

- W. Ma et al., Nature **562**, 557 (2018)  
Z. Zheng et al., Adv. Mat. **32**, 1705318 (2018)  
Z. Zheng et al., Science Adv. **5**, eaav8690 (2019)  
G. Álvarez-Pérez et al., Adv. Mat. **32**, 1908176 (2020)

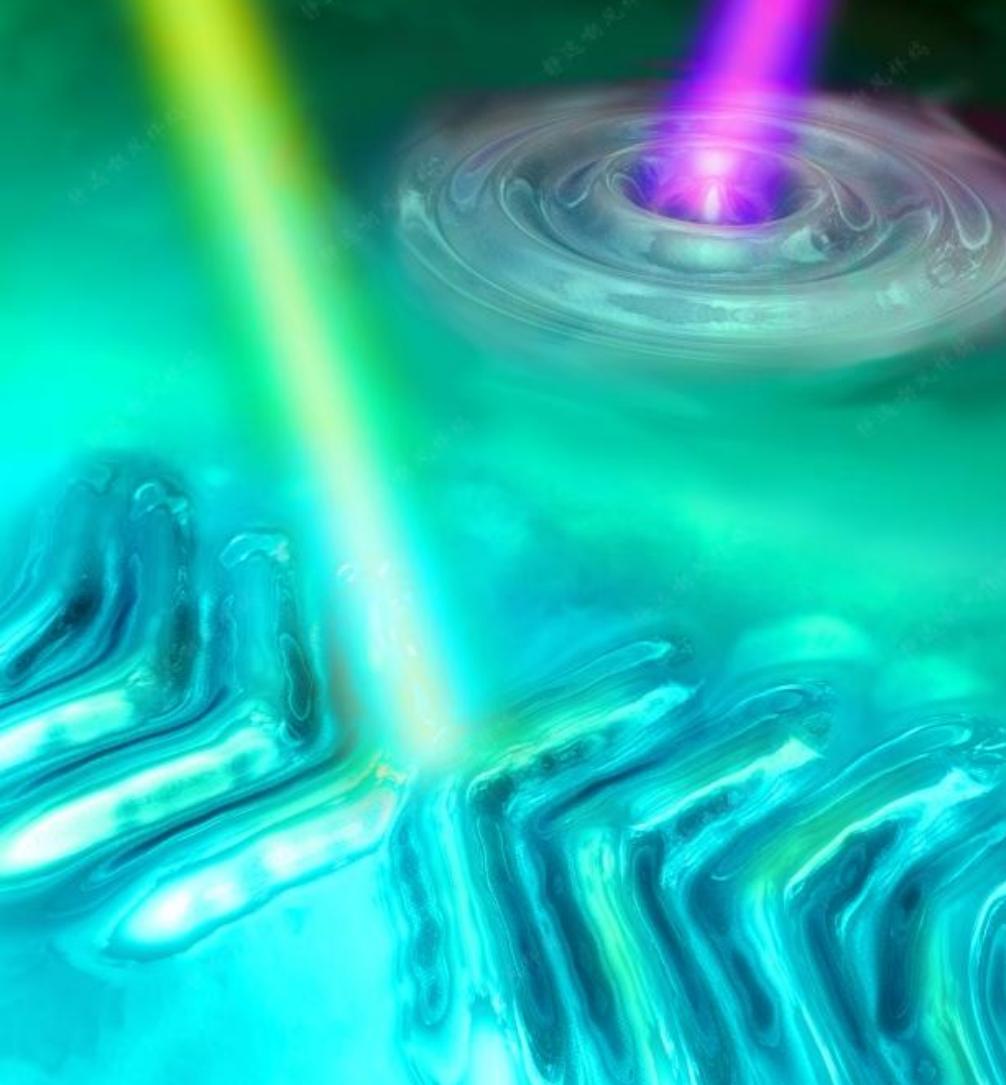
# Dielectric permittivity tensor of $\alpha$ -MoO<sub>3</sub>

DFT by Ion Errea

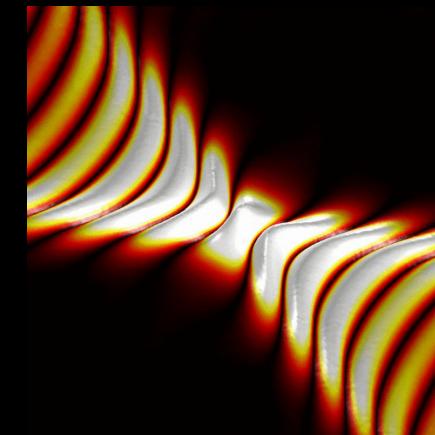
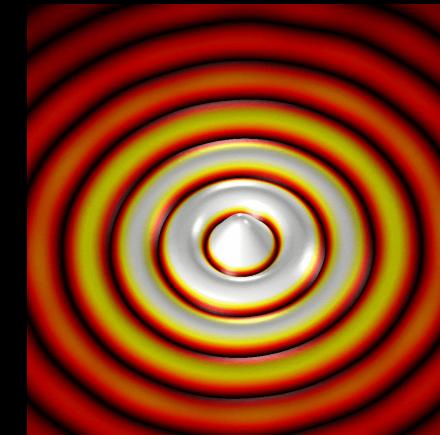


G. Álvarez-Pérez et al., Adv. Mat. **32**, 1908176 (2020)

# Hyperbolic and elliptic polaritons coexist



W. Ma et al., *Nature* **562**, 557 (2018)



Simulations by Peining Li

# Twisted bilayer graphene

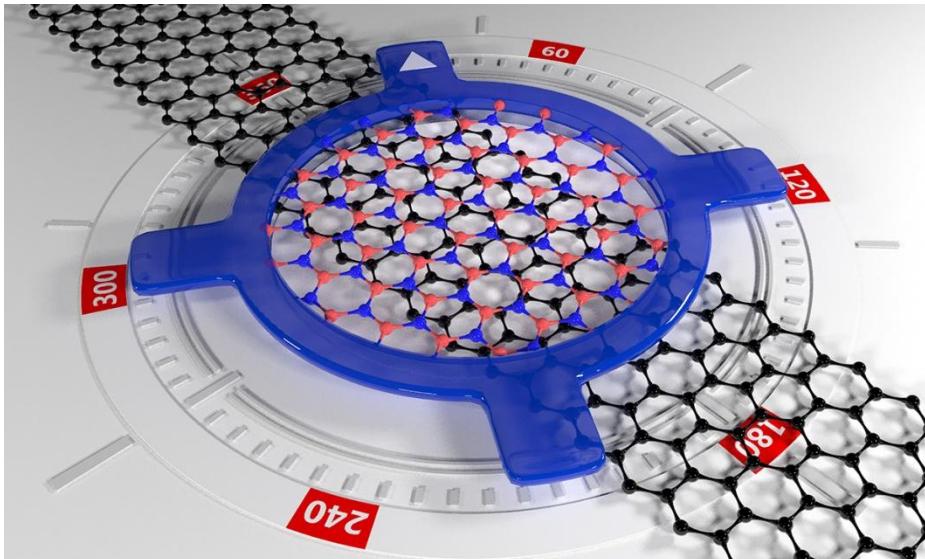
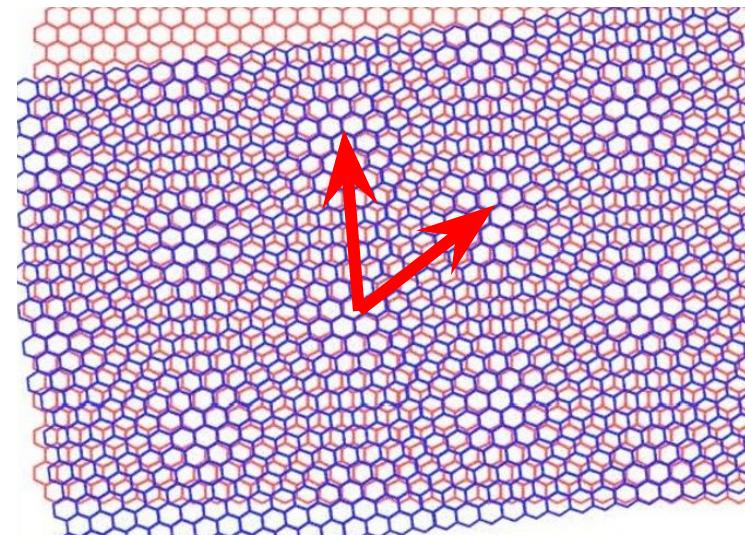


Illustration: Philip Krantz/Krantz NanoArt

Moiré patterns



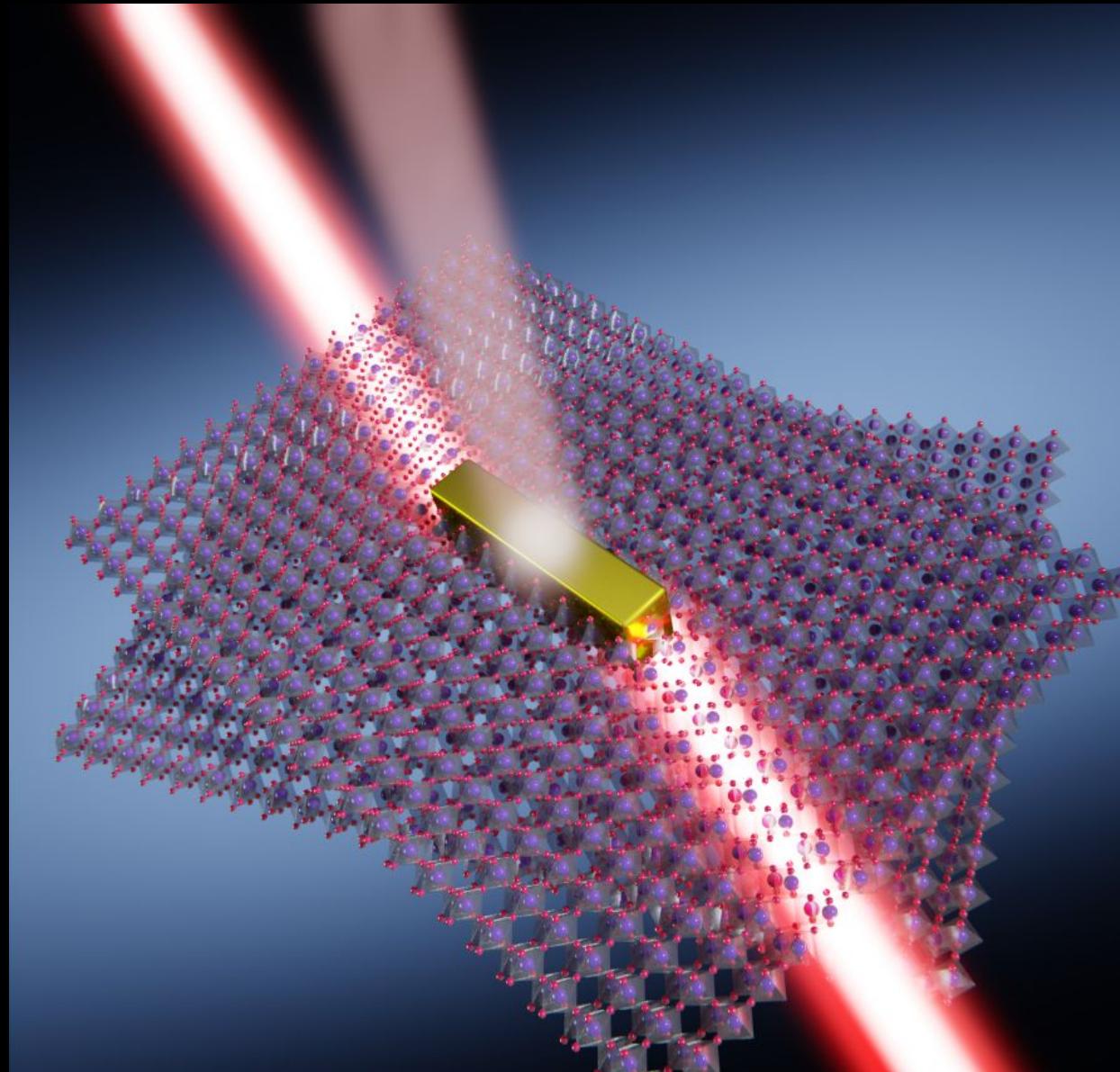
Superconductivity

Y. Cao et al., Nature **556**, 43, (2018)  
Y. Cao et al., Nature **556**, 80, (2018)

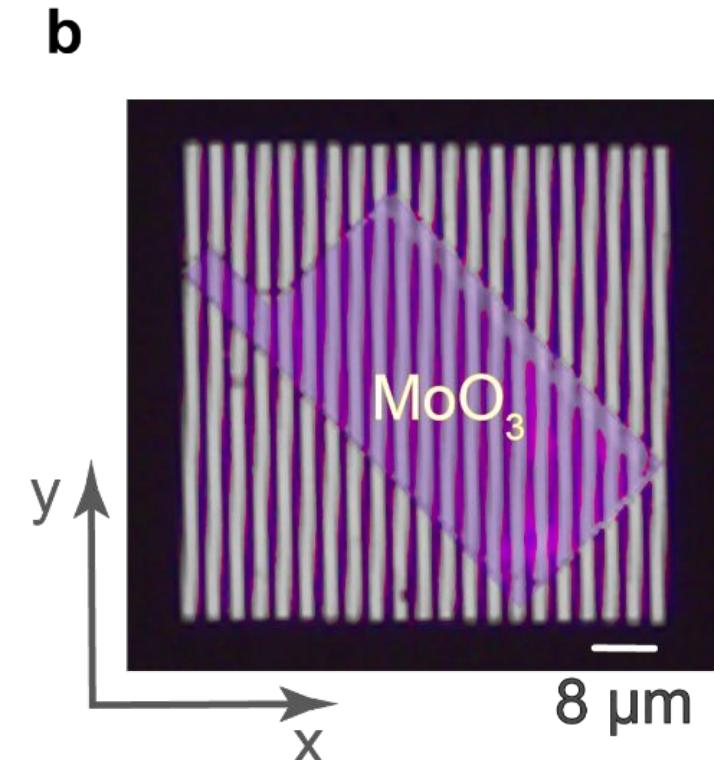
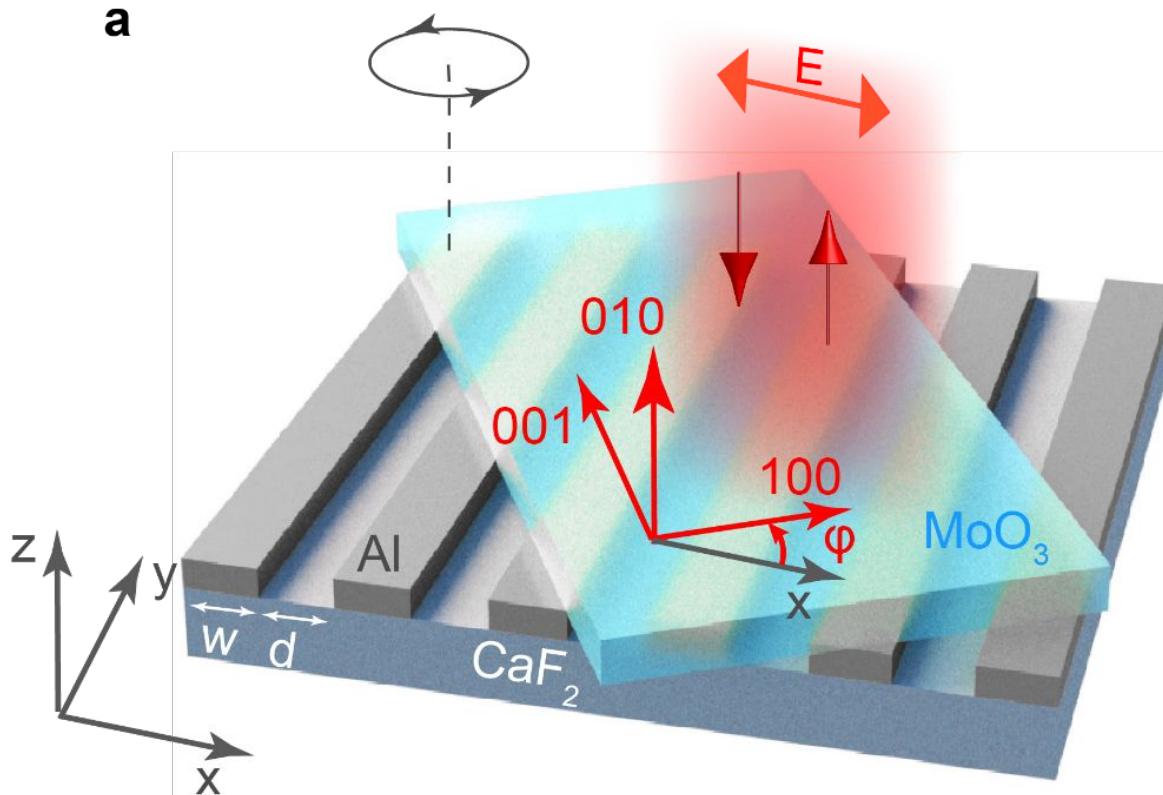
Photonic crystal

S.S. Sunkuet al., Science **362**, 1153, (2018)

# Twisted Nano-Optics



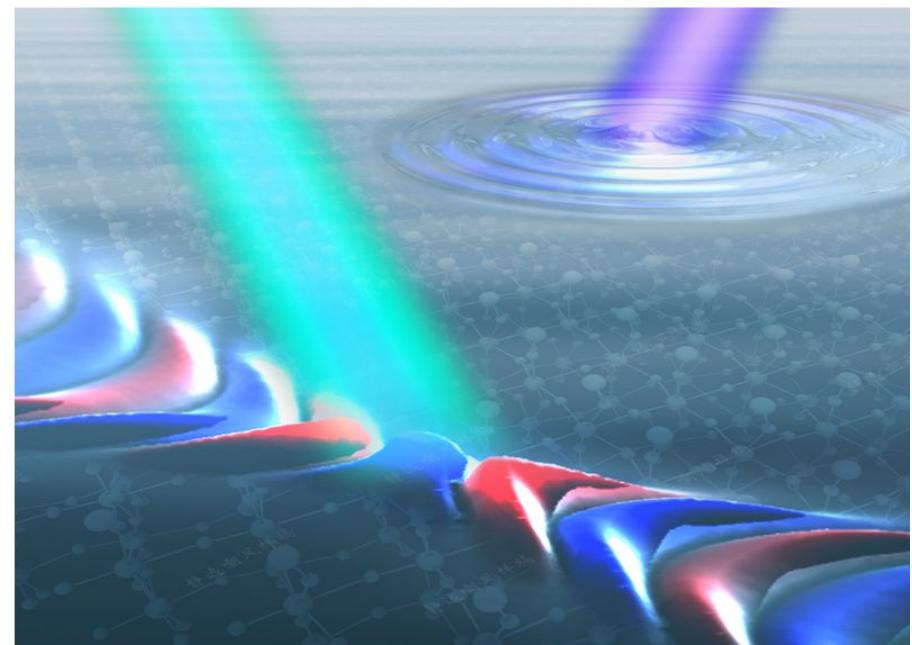
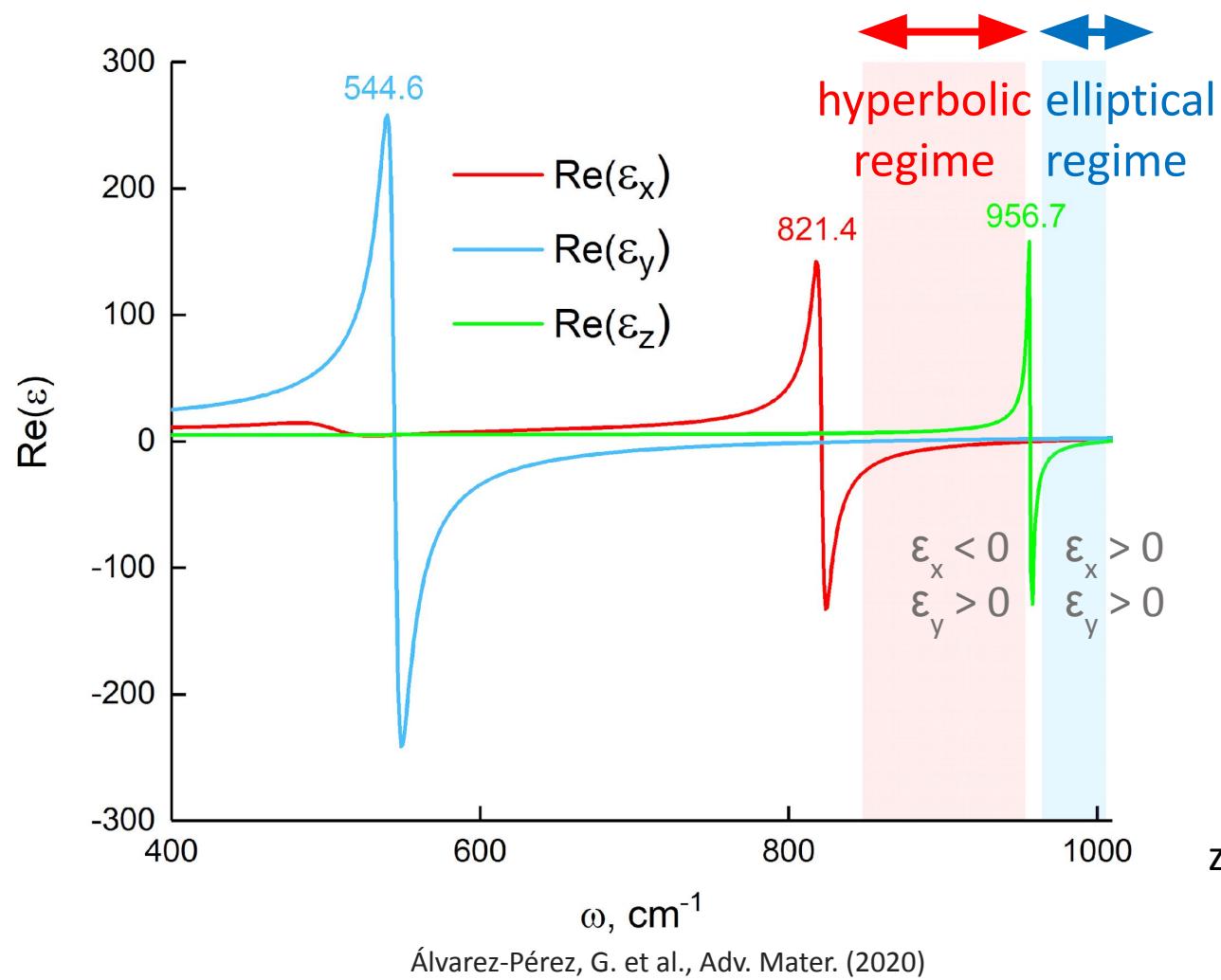
# Twisted nanoresonators for hyperbolic polaritons



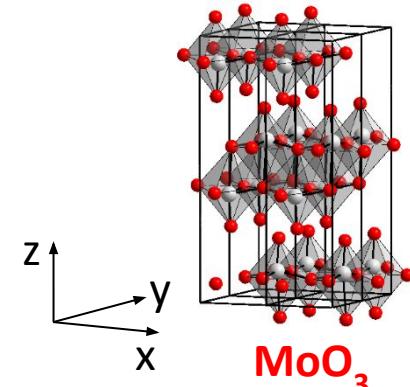
Nanoresonators are formed by  $\alpha\text{-MoO}_3$  placed above metallic ribbons

# Elliptic and hyperbolic regimes of phonon-polaritons in $\alpha\text{-MoO}_3$

We consider both elliptic and hyperbolic polaritons in  $\alpha\text{-MoO}_3$

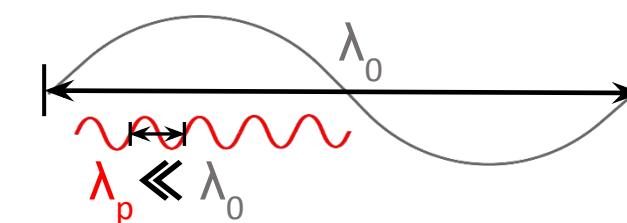
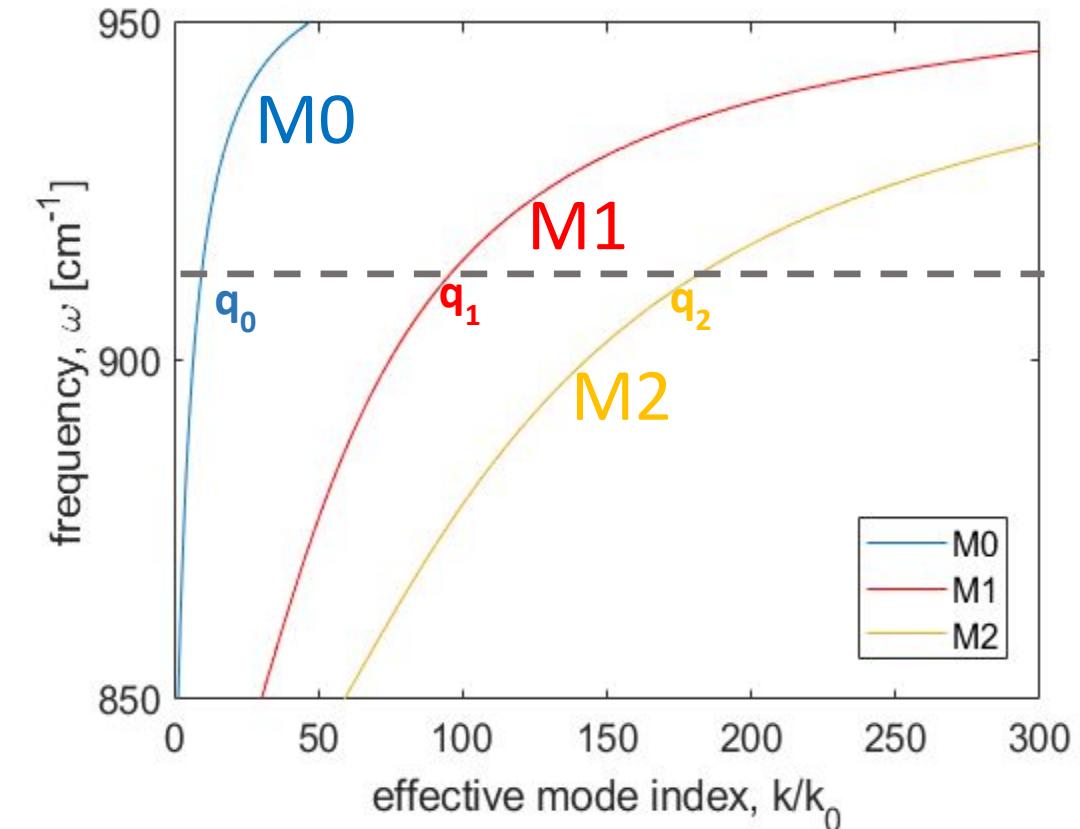
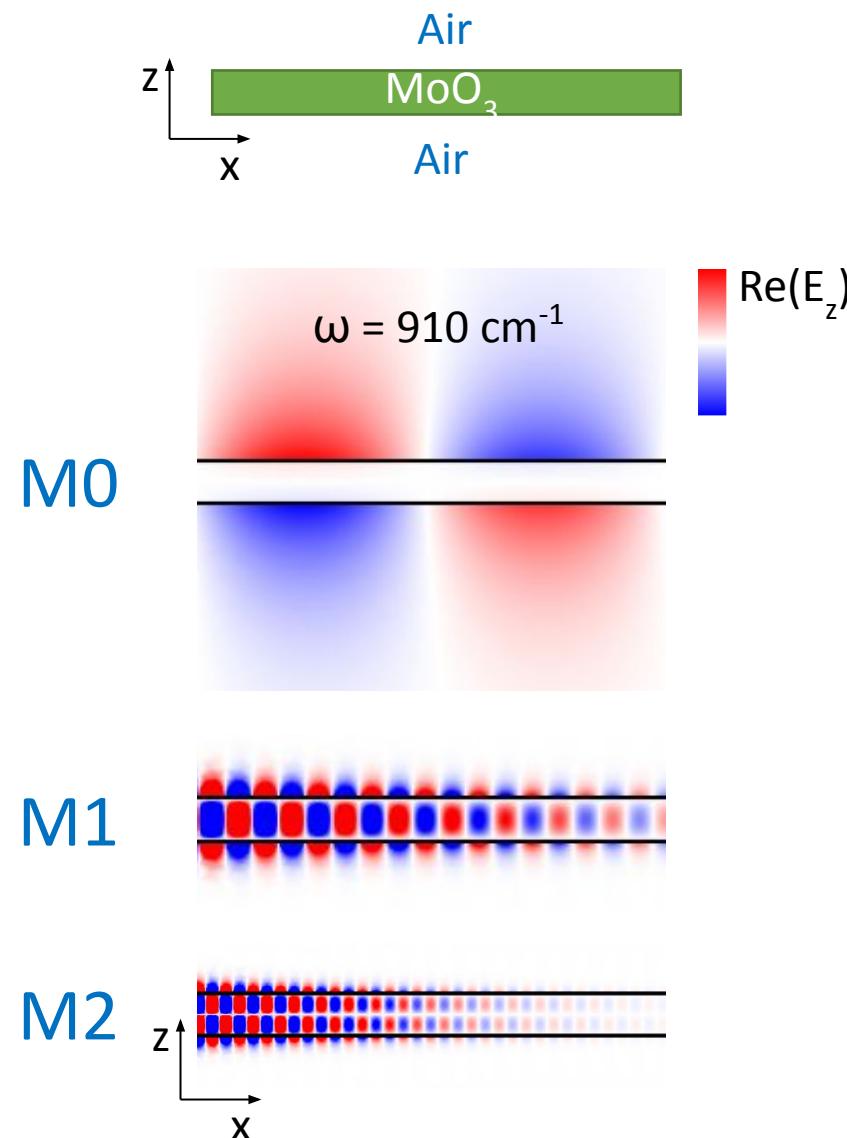


W. Ma et al., Nature 562, 557 (2018)

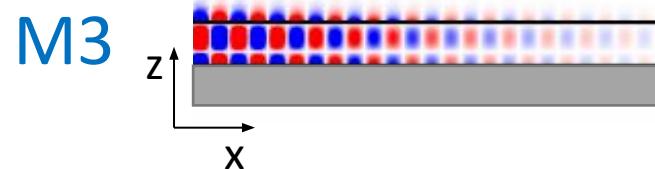
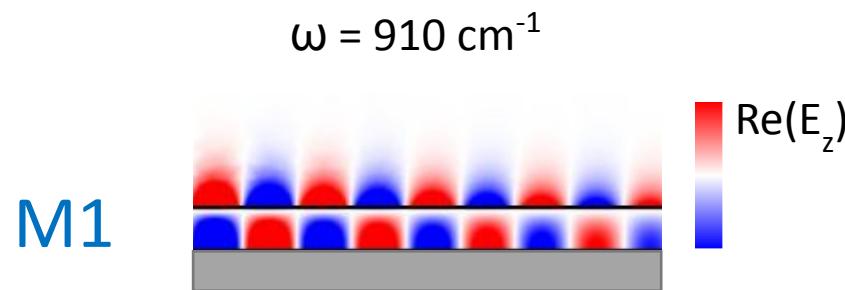
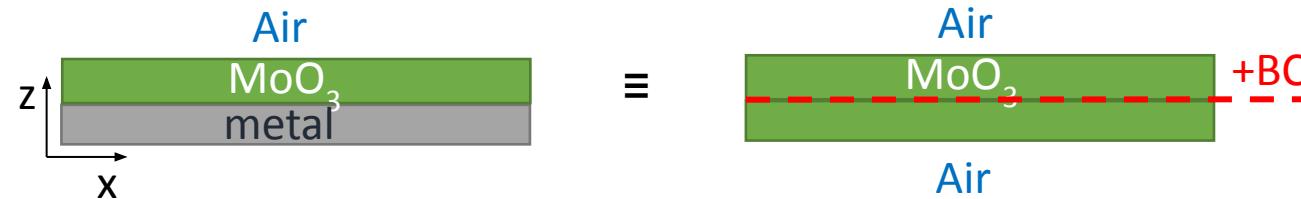


$$\hat{\epsilon}(\omega) = \begin{pmatrix} \epsilon_x(\omega) & 0 & 0 \\ 0 & \epsilon_y(\omega) & 0 \\ 0 & 0 & \epsilon_z(\omega) \end{pmatrix}$$

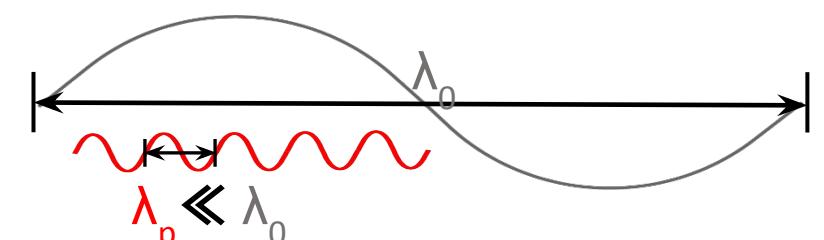
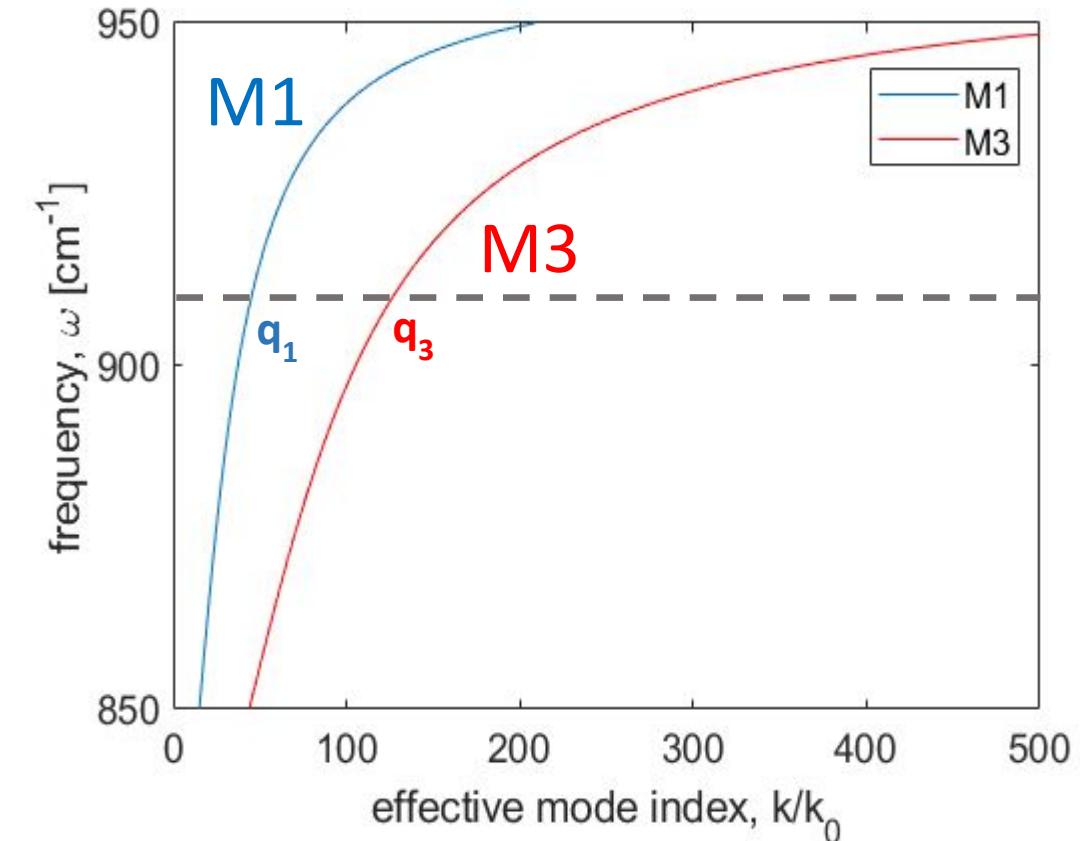
# Modes in thin slab of $\alpha$ -MoO<sub>3</sub>



# Modes in thin slab of $\alpha$ -MoO<sub>3</sub> above metal



odd modes only



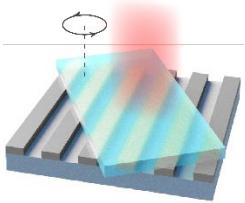
# Outline



Introduction. Hyperbolic nano optics with van der Waals crystals



Elliptical and hyperbolic phonon-polaritons in MoO<sub>3</sub>. Twisted nano optics



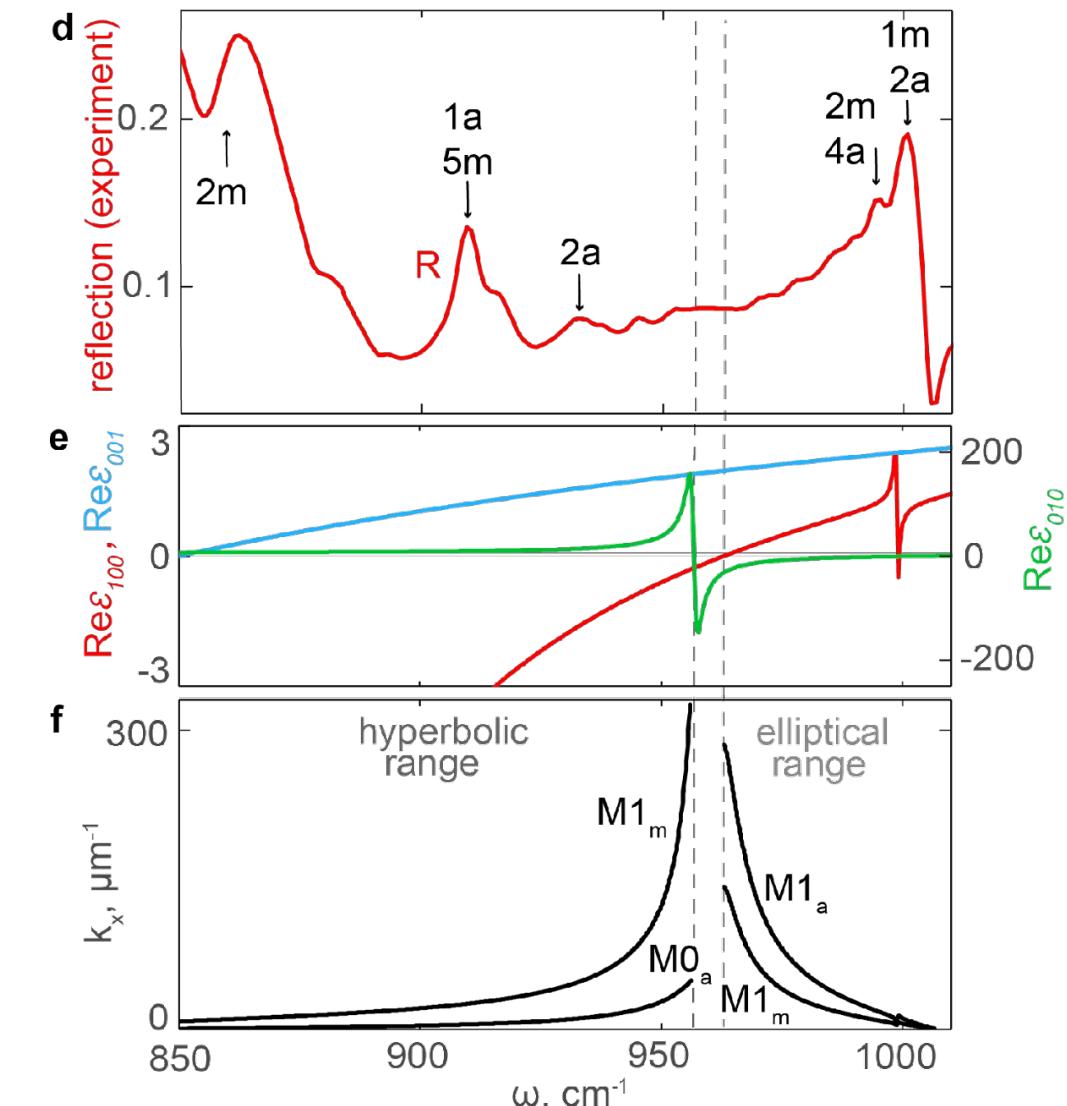
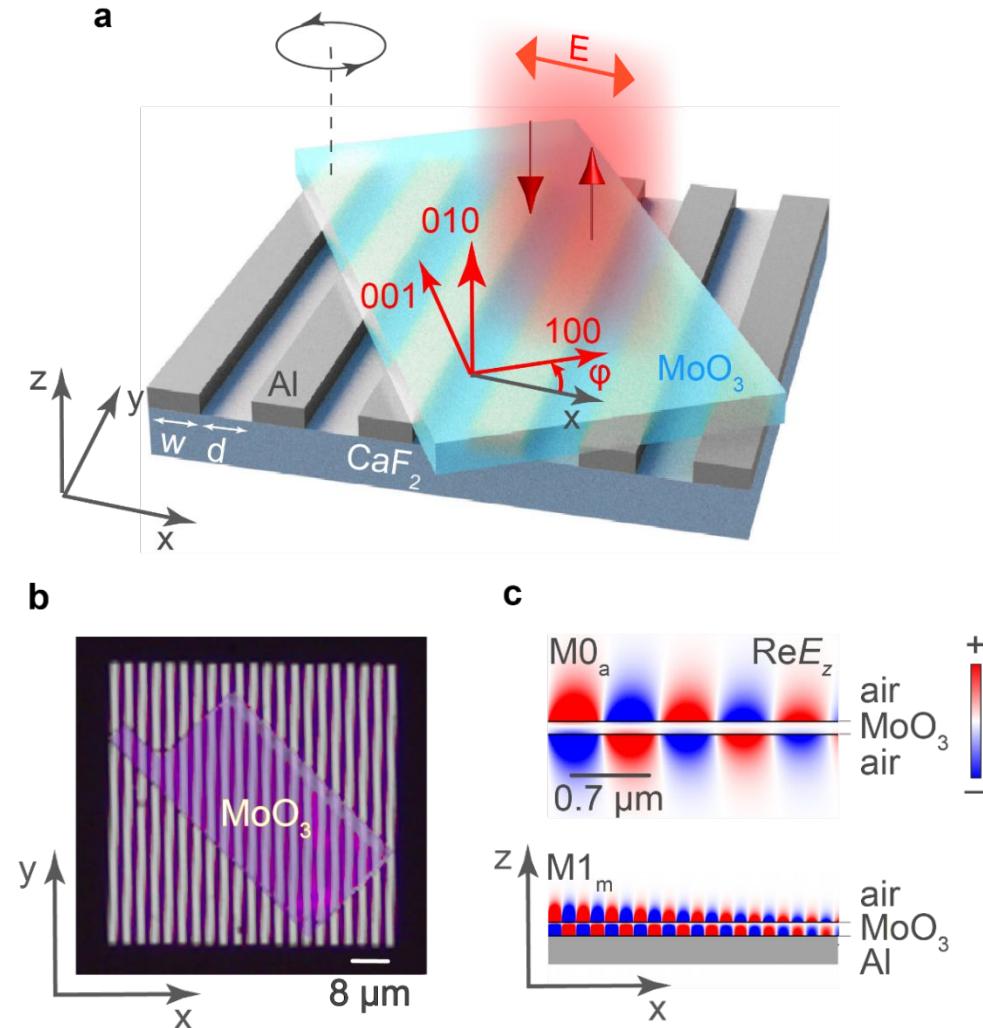
**Far- and near-field measurements of resonances in rotated structures**



Mapping of dispersion surface

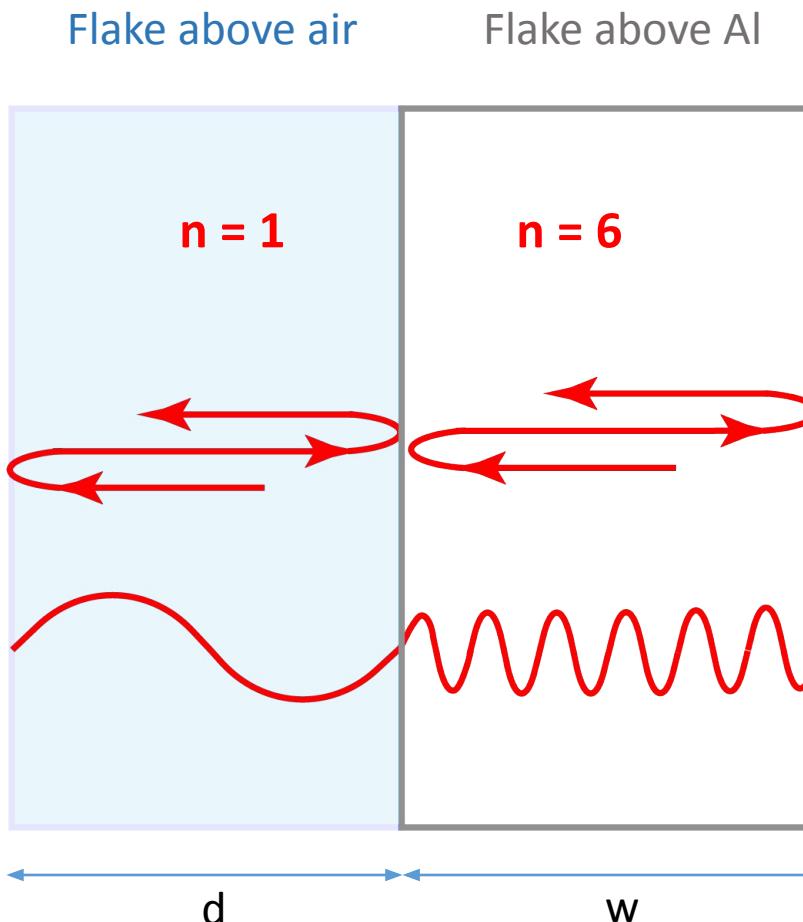
# Far-field measurements of resonances in twisted structures

$\alpha\text{-MoO}_3$  above air and  $\alpha\text{-MoO}_3$  above metal supports modes with significantly different wavevectors forming two types of Fabry-Perot resonators



# Model of resonances

We assume the structure to be equivalent to two independent Fabry-Perot resonators



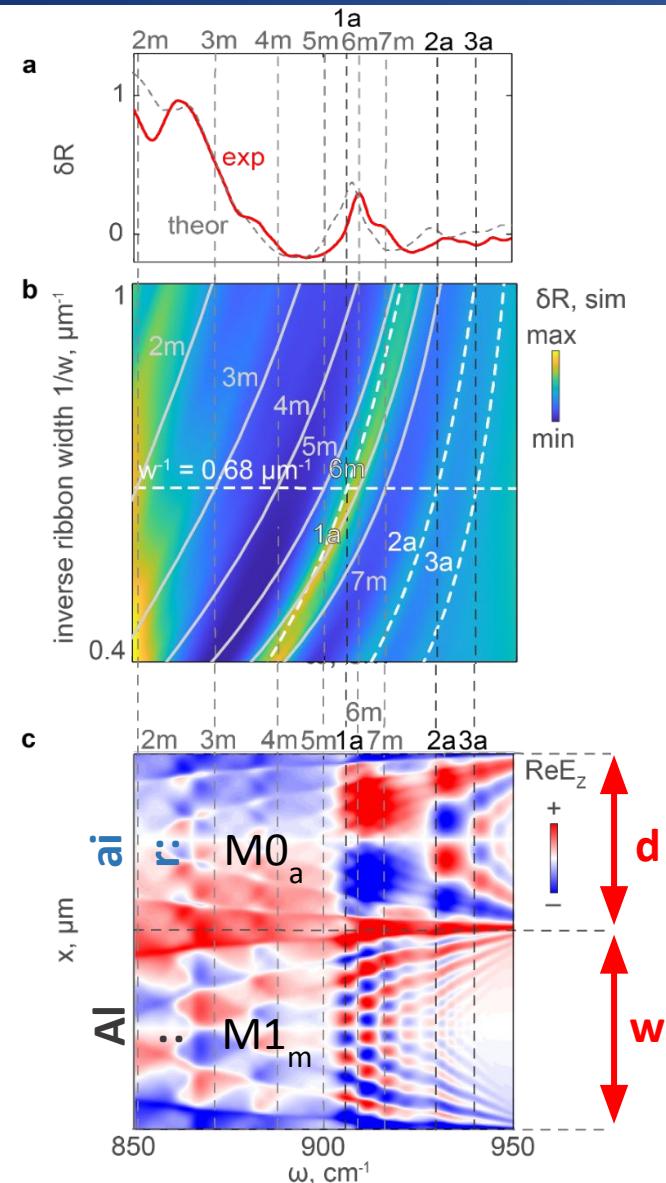
air:  
Al:

phase matching:

$$2kd + 2\Phi_a = 2\pi n$$
$$2kw + 2\Phi_m = 2\pi m$$

# Simulation of resonances in twisted structures

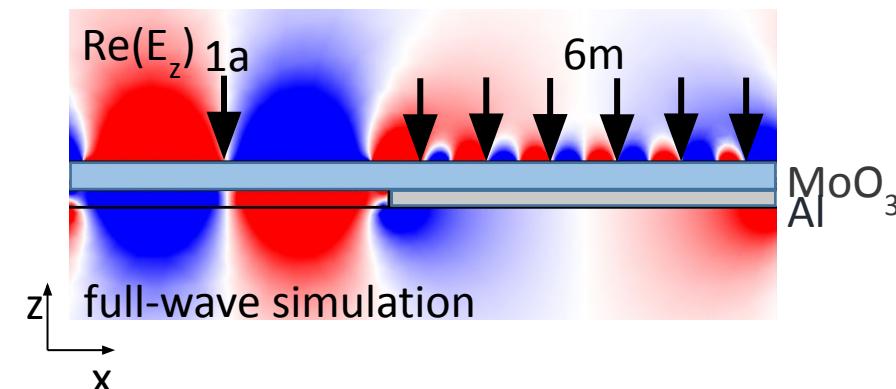
$\varphi = 0$ , period of lattice changes ( $d/w = \text{const}$ )



The dependance of the reflection coefficient on ribbon width and frequency. Comparison of the numerical simulation with the experimental results

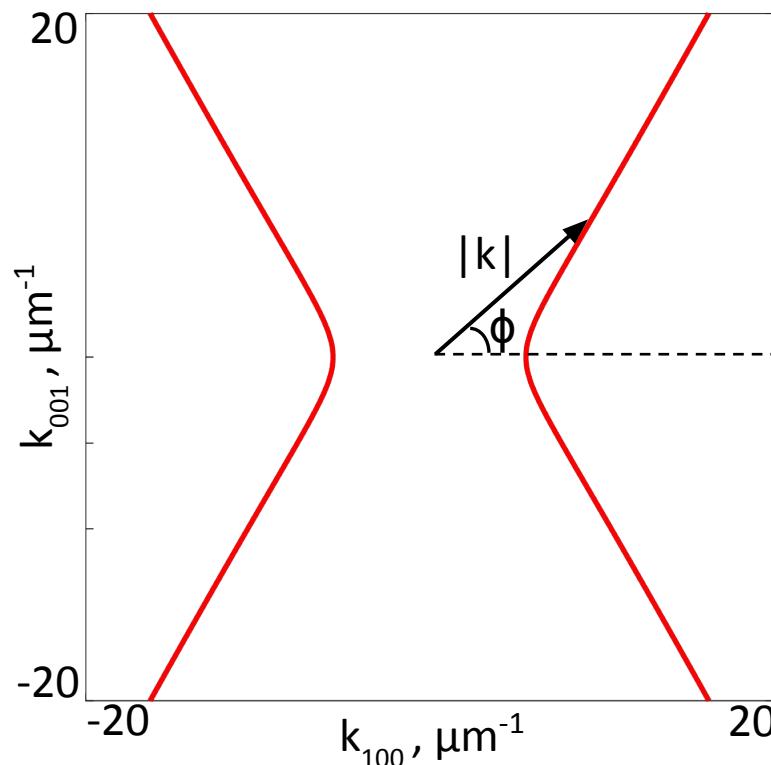
phase matching:

$$\begin{aligned}\text{air: } & 2kd + 2\Phi_a = 2\pi n \\ \text{Al: } & 2kw + 2\Phi_m = 2\pi m\end{aligned}$$

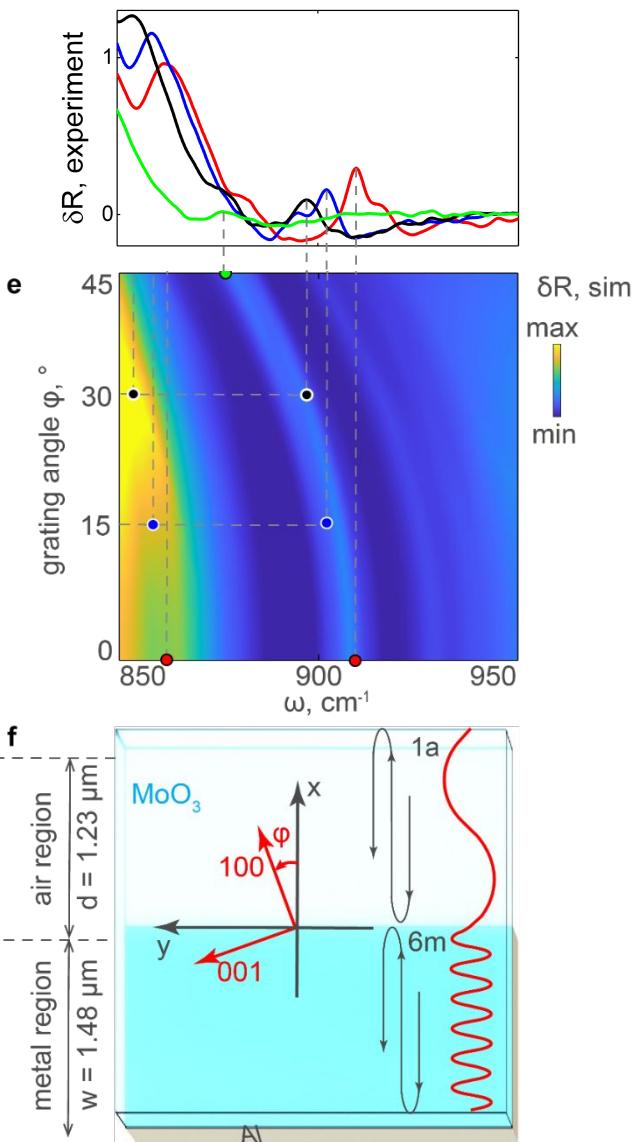
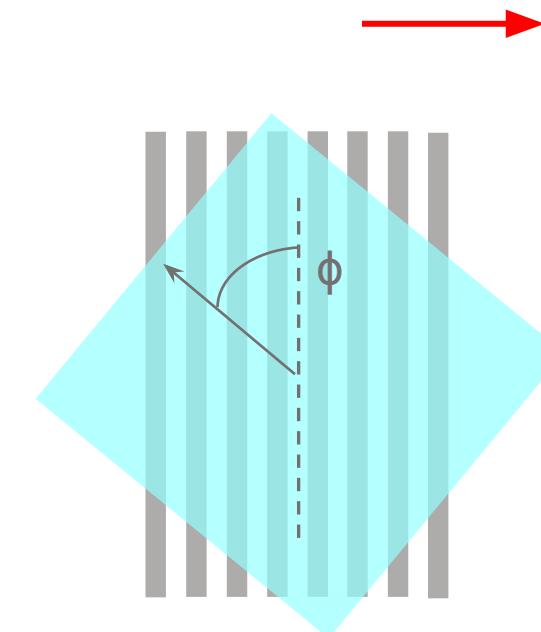


# Far-field measurements for different angles

The dependance of the reflection coefficient on frequency and the angle between main axes of the biaxial slab and ribbons direction. Comparison of the numerical simulation with the experimental results



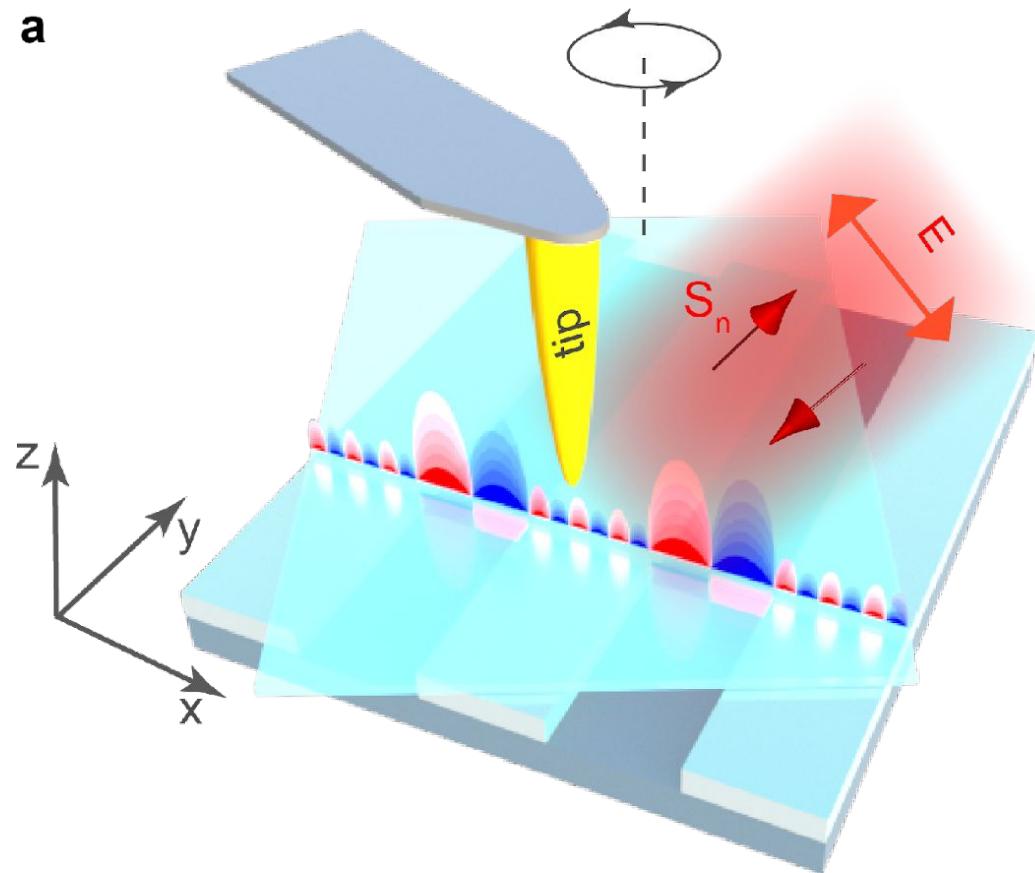
Period of lattice is fixed,  $\varphi$  changes



# s-SNOM measurements

s-SNOM measurements verify our assumption about resonances in  $\alpha\text{-MoO}_3$  film

a



# Outline



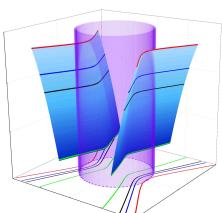
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Elliptical and hyperbolic phonon-polaritons in MoO<sub>3</sub>. Twisted nanooptics



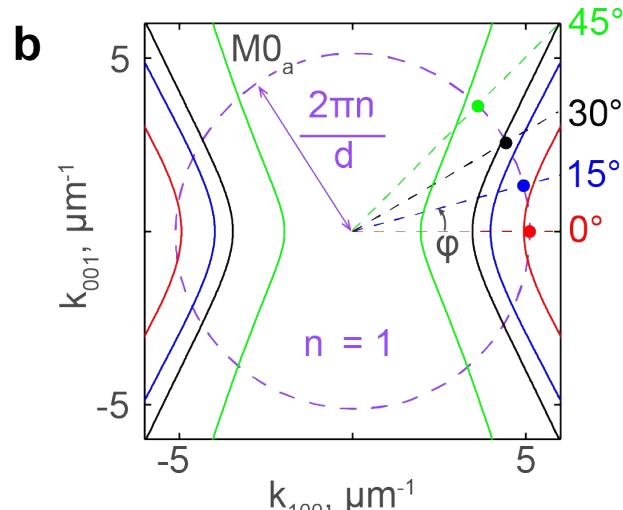
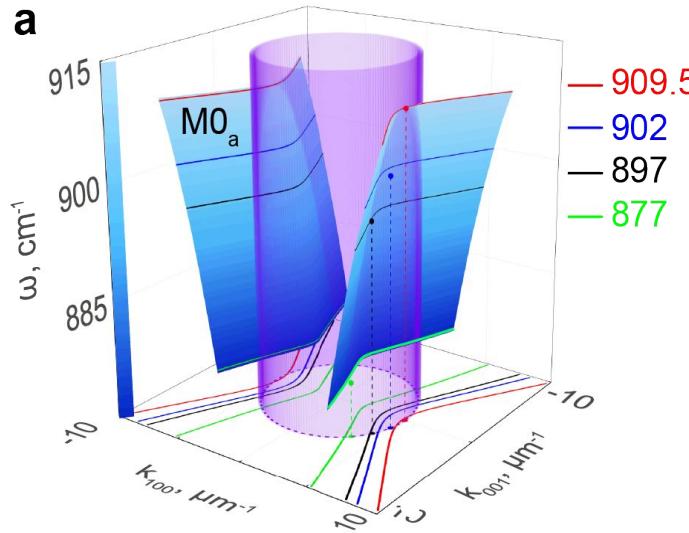
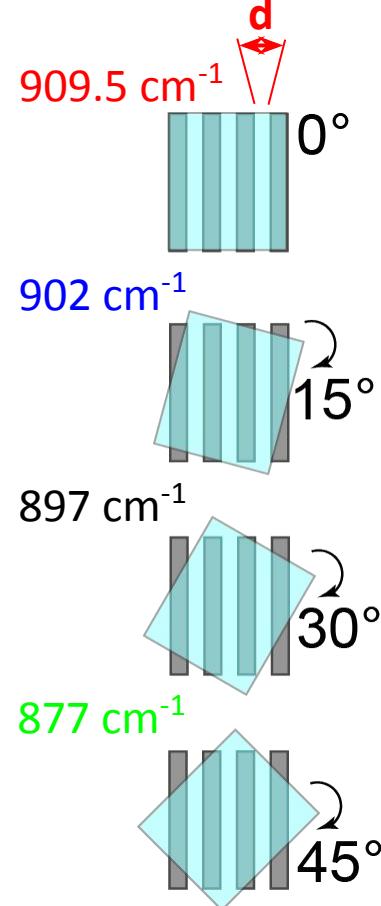
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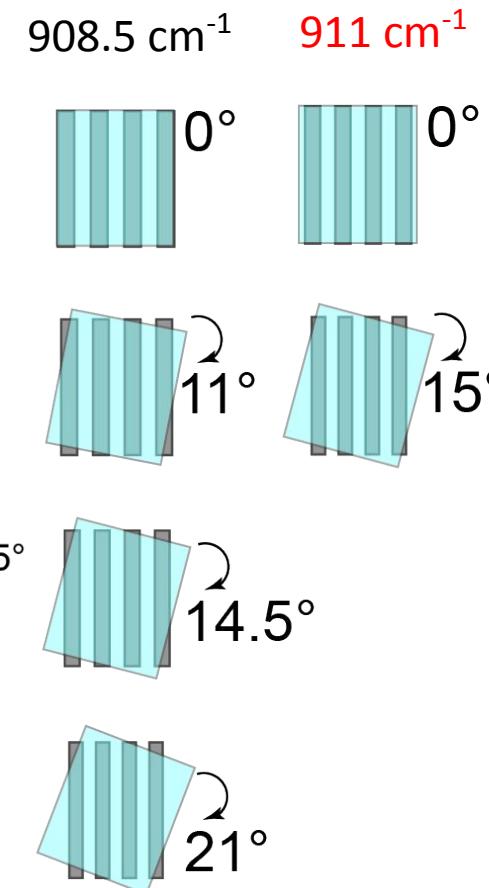
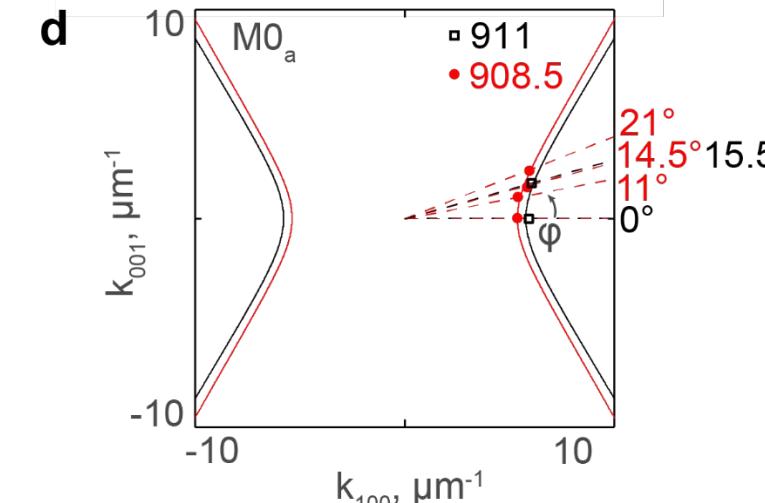
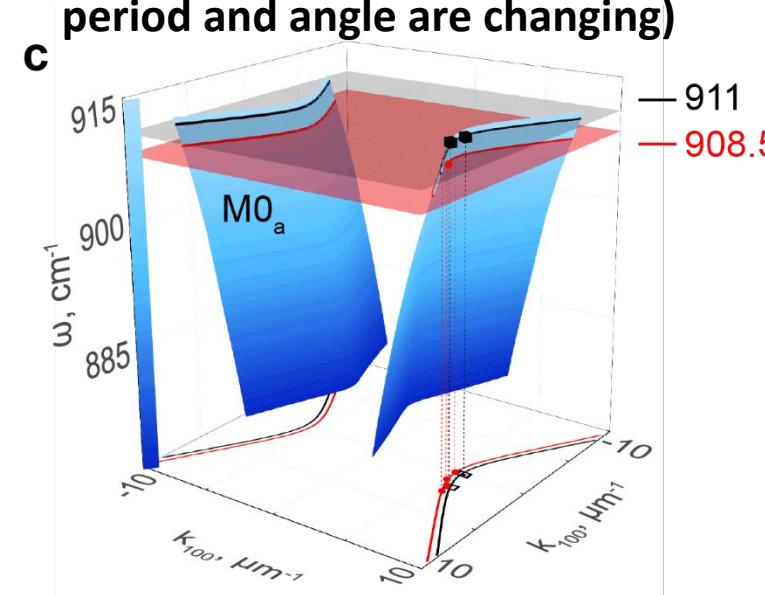
**Mapping of dispersion surface**

# Mapping of dispersion surface

**cut in momentum (period is constant, frequency and angle are changing)**



**cut in frequency (frequency is constant, period and angle are changing)**



# Take-home messages

- **High-quality ( $Q \approx 200$ ) resonances** of surface PhPs identified by far- and near-field measurements
- Unique **tunability** of resonators **by a rotation** of the crystal slab with respect to the grating
- Experimental **dispersion surface mapping**
- Applications to tunable strong coupling of PhP with organic molecules, **tunable infrared sensors** and photodetectors

# 2D Nanophotonics group

Kateryna Domina

Andrei Bylinkin

Alexey Nikitin

Gonzalo Alvarez

Olga Matveeva

Nathaniel Capote



*Nanolight 2022*

Kirill Voronin

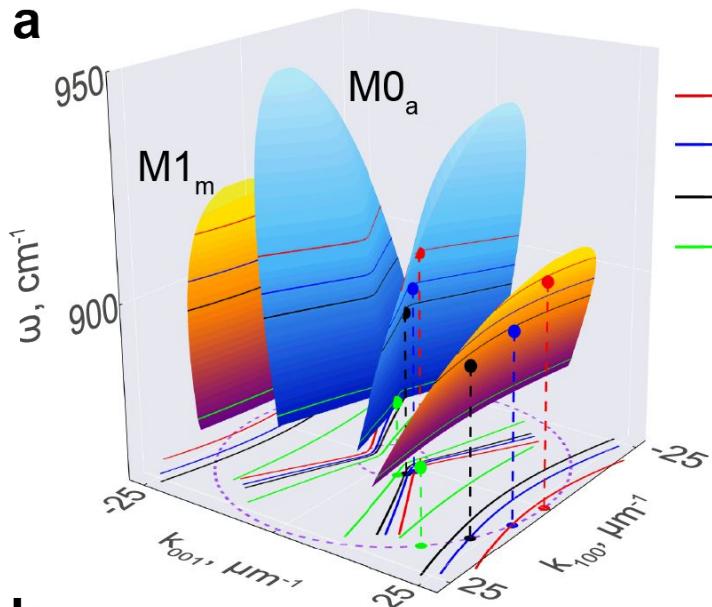


**Thank you for your attention!**

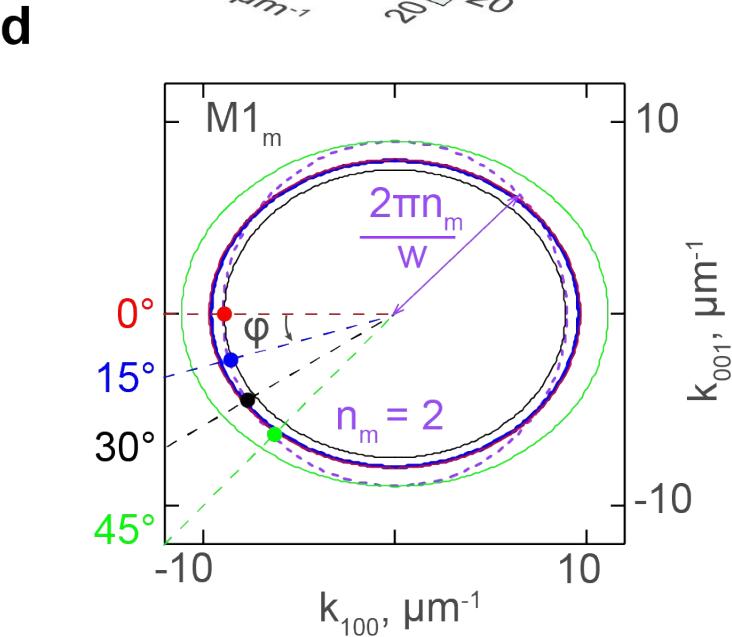
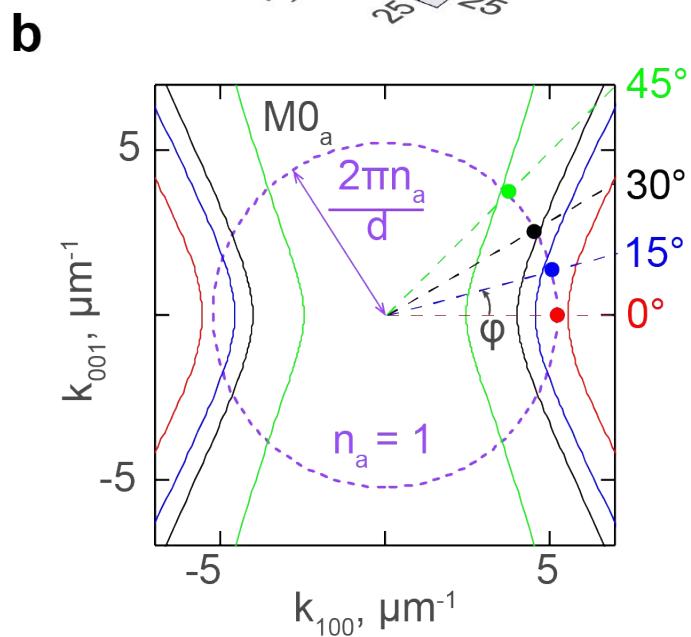
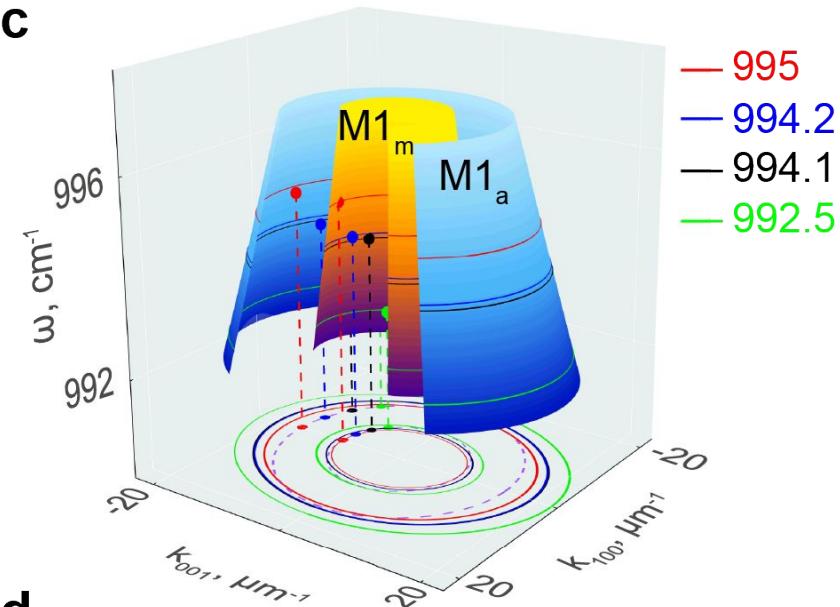
E-mail: [kirill.voronin@dipc.org](mailto:kirill.voronin@dipc.org)  
[voronin.kv@phystech.edu](mailto:voronin.kv@phystech.edu)

# **Supplementary slides**

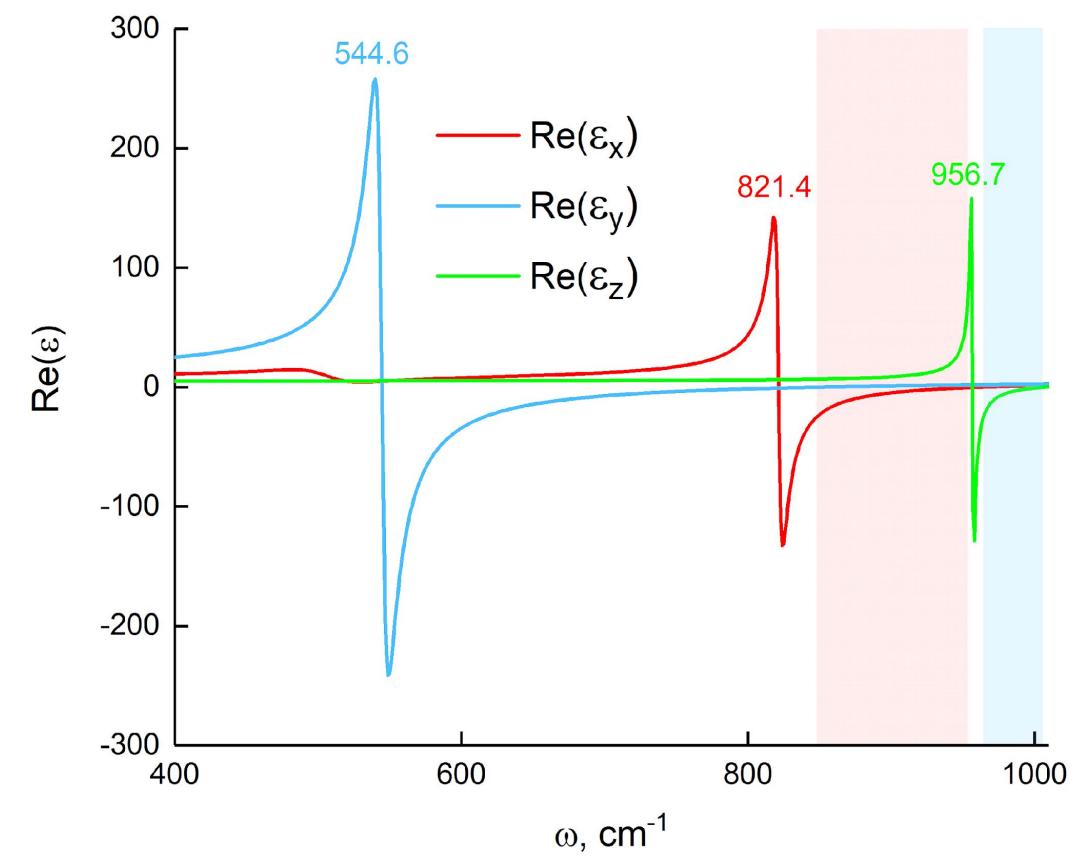
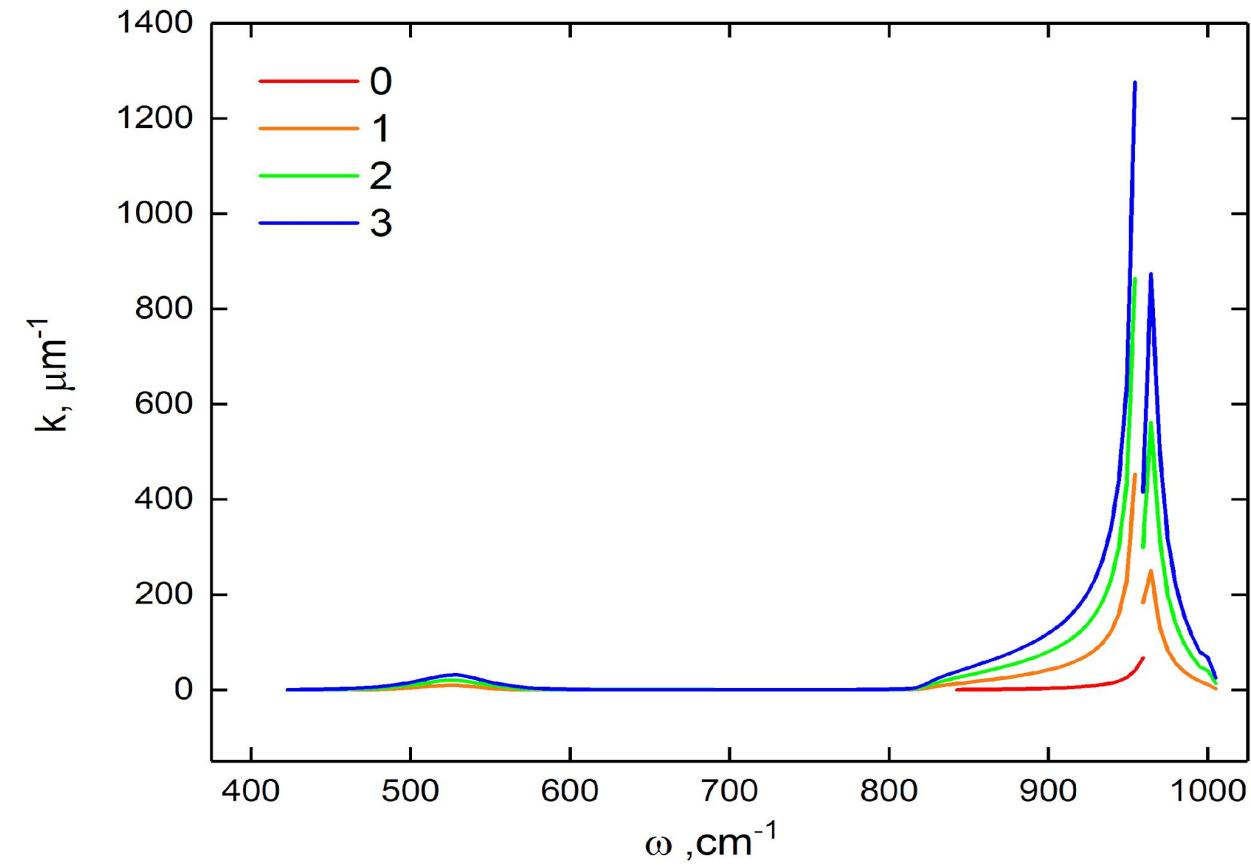
hyperbolic  
regime



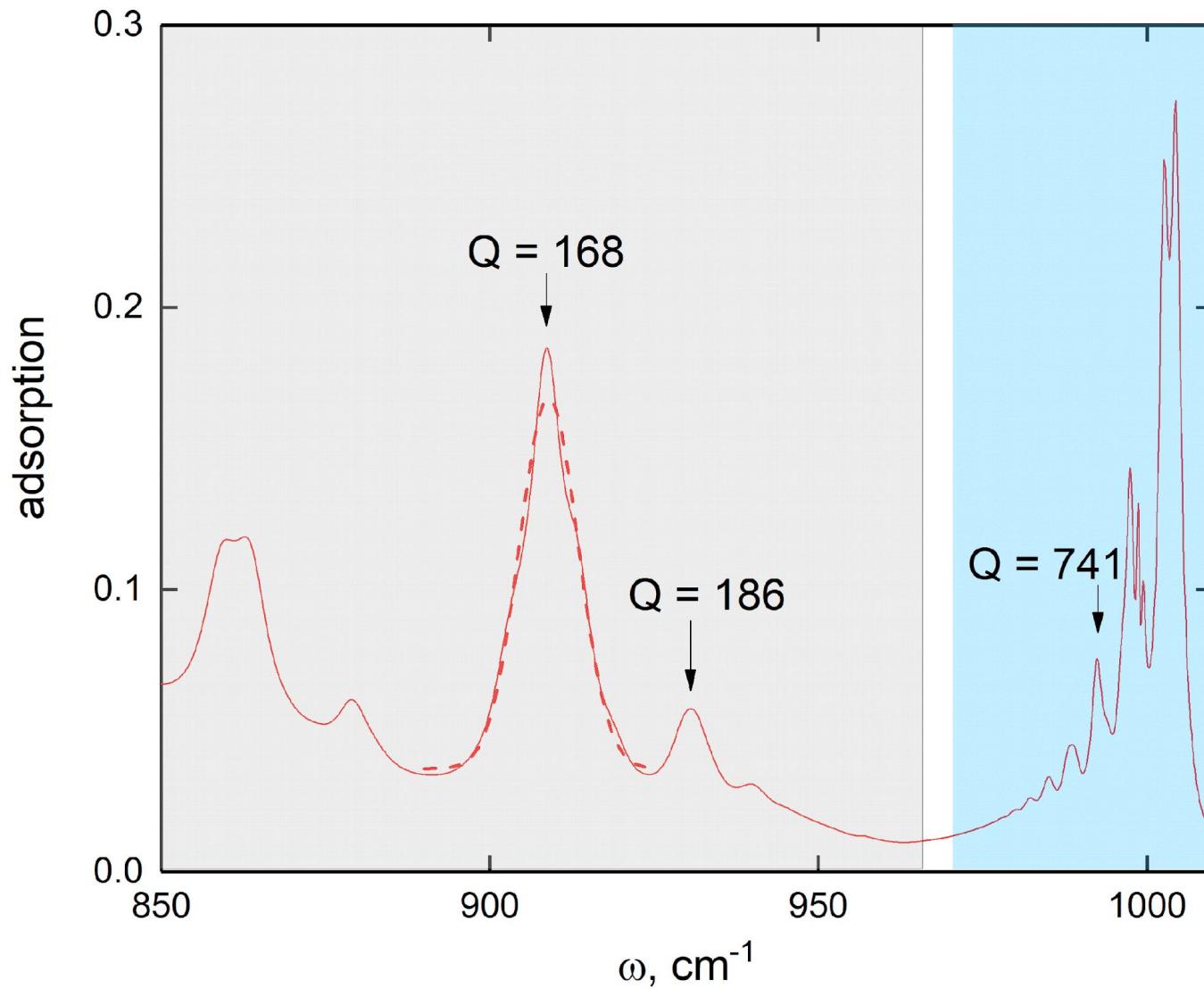
elliptic  
regime



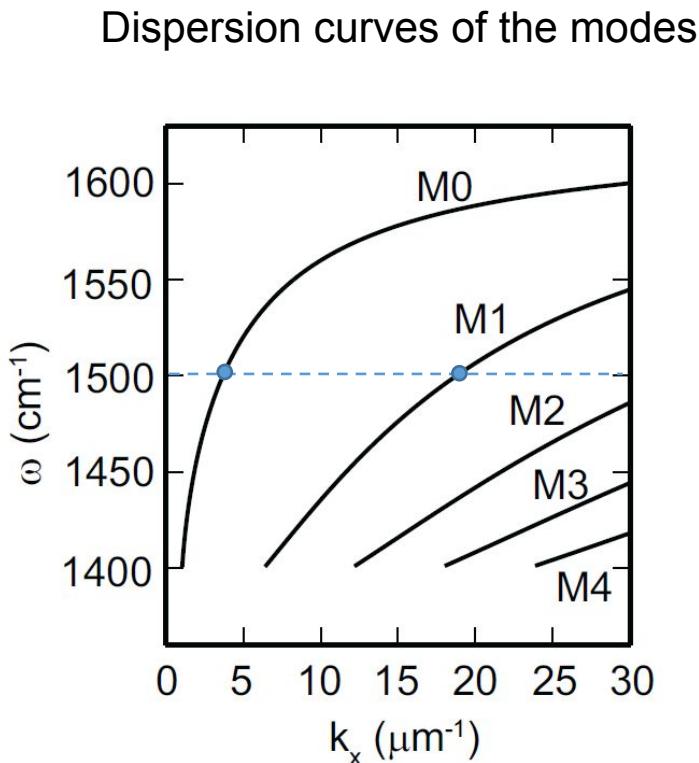
## Dispersion of modes



## resonance quality factor



# Hyperbolic volume modes in h-BN slabs



The zig-zag pattern can be seen as a superposition of the HPP waveguiding modes.

