

# Optical Manipulation of Matter Waves

Kamran Akbari

**Valerio Di Giulio and Javier García de Abajo**

ICFO-The Institute of Photonic Sciences, Barcelona, Spain



Institut  
de Ciències  
Fotòniques



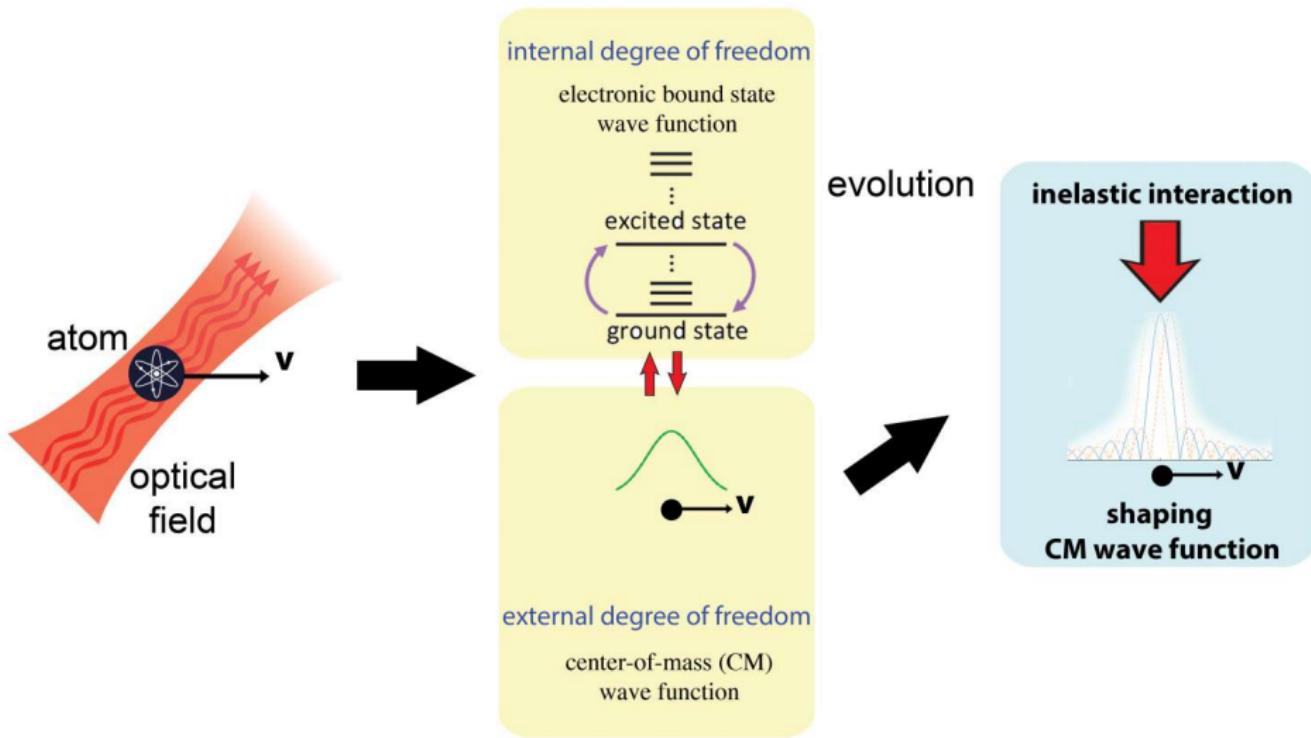
INSTITUCIÓ CATALANA DE  
RECERCA I ESTUDIS AVANÇATS



Benasque – Nanolight  
March 11, 2022

What is meant to say ...

## Optical Manipulation of Matter Waves



## Introduction

Electron world

Atom world

## What We Are Doing ...

A bit on the technical side

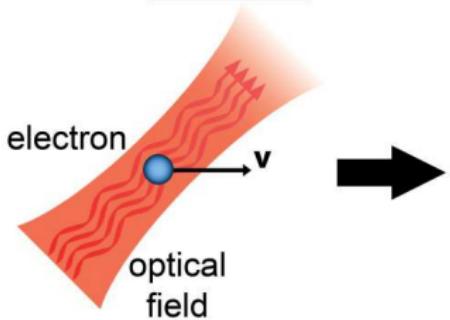
PINAM

Stimulated Compton scattering

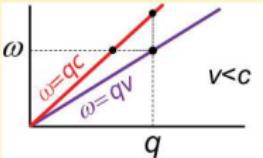
## Wrap-up

# Phase-matching

## free space



energy-momentum  
mismatch



## elastic interaction

ponderomotive interaction:  $H \sim A^2$

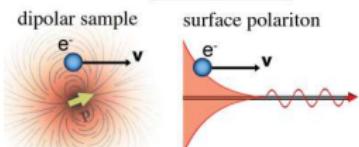
steering  
diffraction

## inelastic interaction

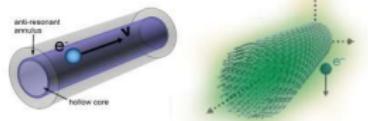
direct coupling:  $H \sim \mathbf{A} \cdot \mathbf{v}$

not possible!

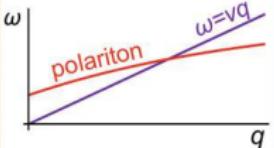
## near-field



optical hollow fiber    carbon nanotube



## phase matching



## elastic interaction

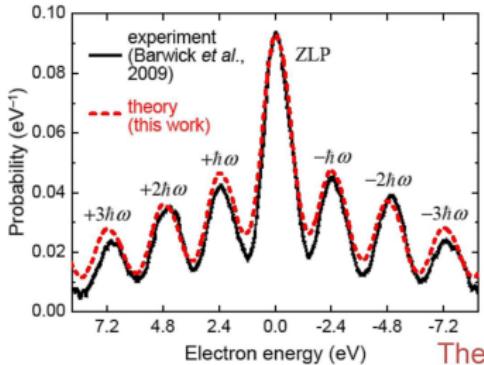
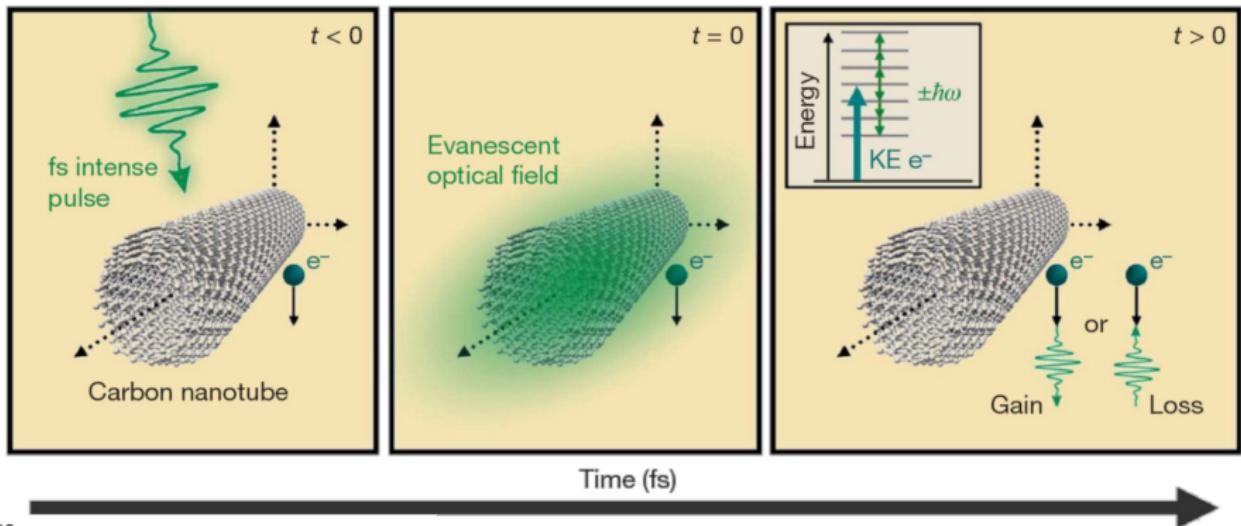
ponderomotive interaction:  $H \sim A^2$

steering  
diffraction

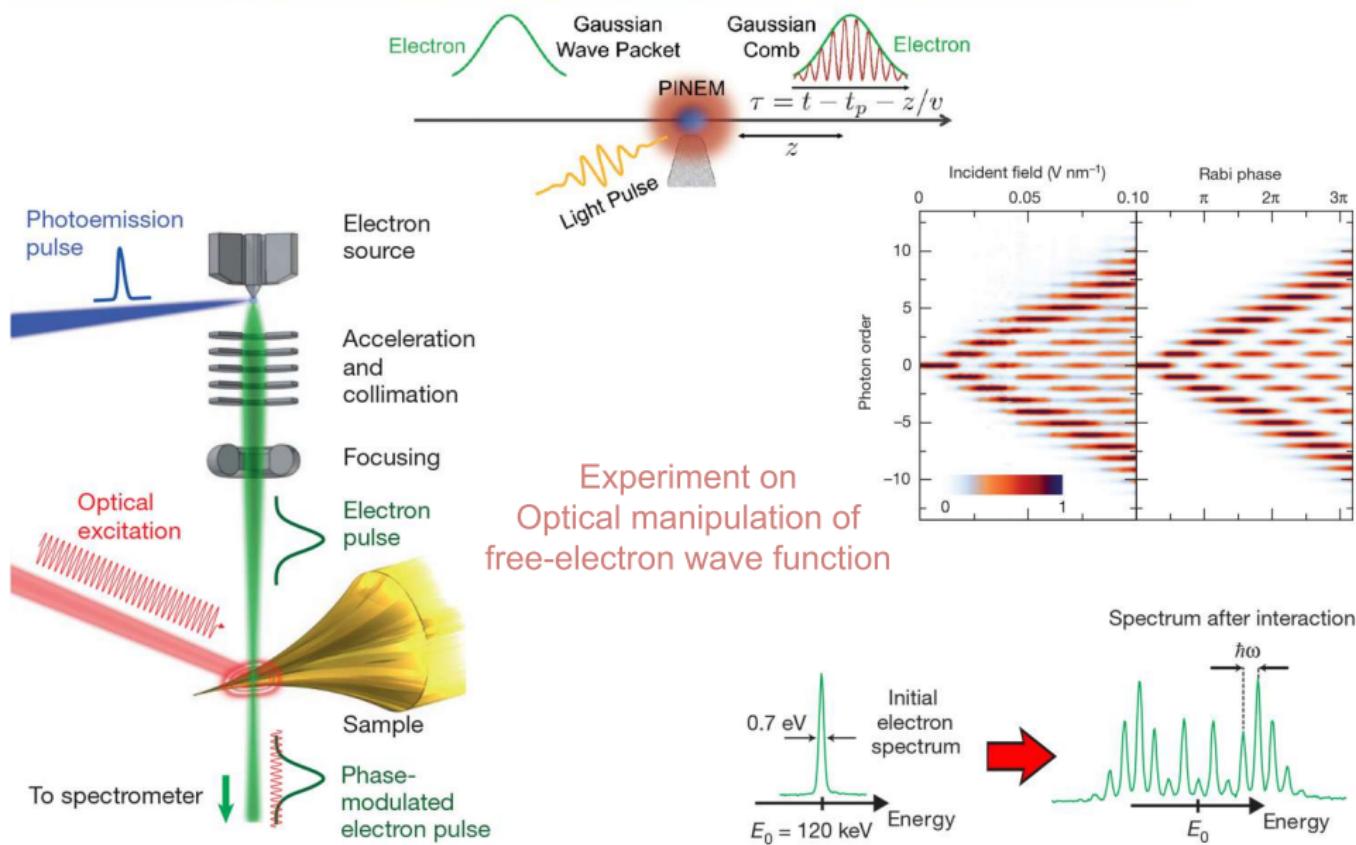
## inelastic interaction

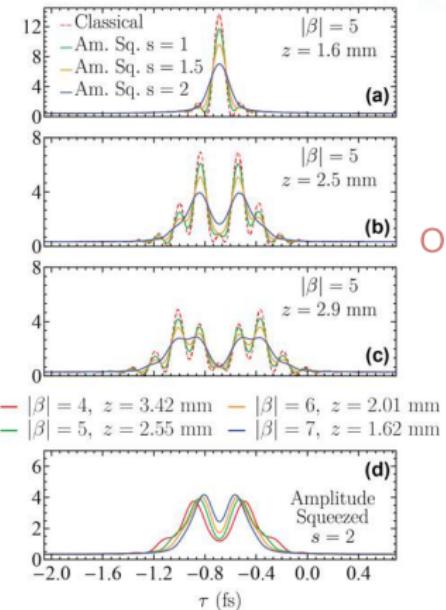
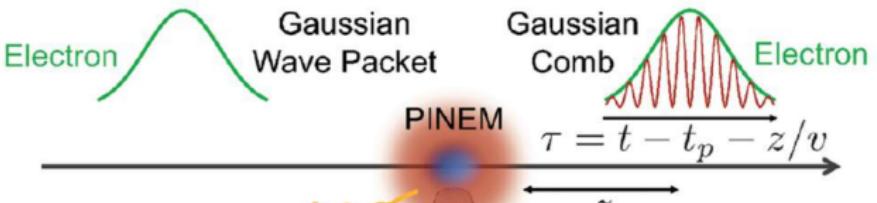
direct coupling:  $H \sim \mathbf{A} \cdot \mathbf{v}$

possible  
PINEM

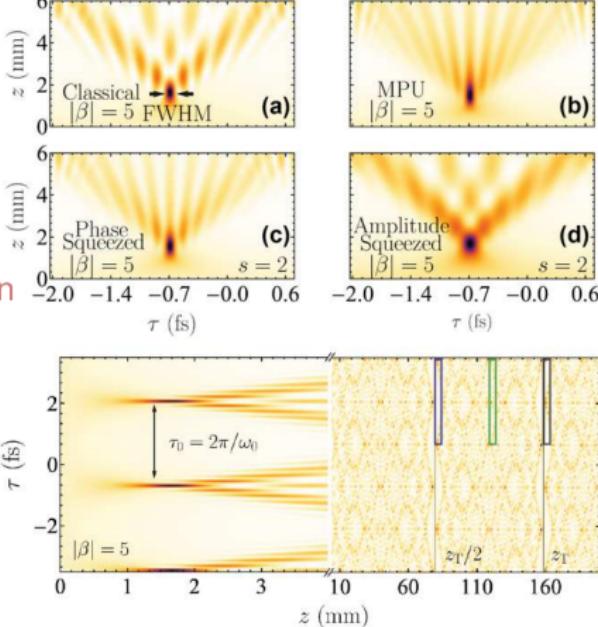


Experiment: Barwick, Flannigan, Zewail, Nature (2009)  
 Theory: García de Abajo, Asenjo-García, and Kociak, Nano Lett. (2010)

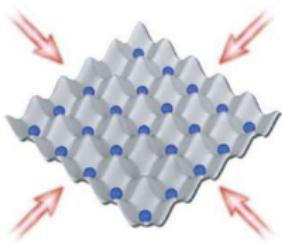
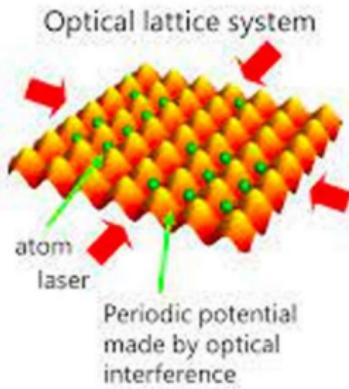
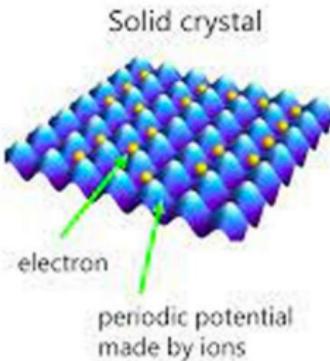
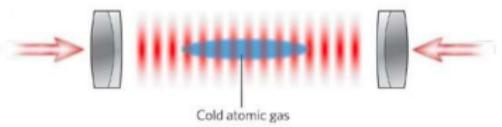
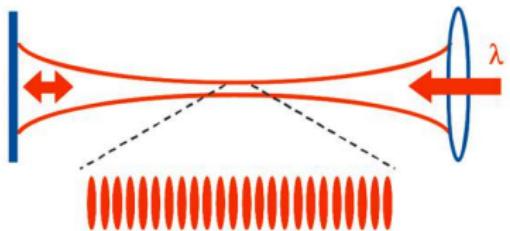




## Theory on Optical manipulation of free-electron wave function



# Atom-light interaction



# Theory

$$\hat{\mathcal{H}}(t) = \hat{\mathcal{H}}^{\text{at}} + \hat{\mathcal{H}}'(t) + \hat{\mathcal{H}}''(t)$$

$$\begin{aligned}\hat{\mathcal{H}}'(t) &= \frac{i\hbar eZ}{m_n c} \mathbf{A}(\mathbf{r}_n, t) \cdot \nabla_{\mathbf{r}_n} - \frac{i\hbar e}{m_e c} \sum_i \mathbf{A}(\mathbf{r}_i, t) \cdot \nabla_{\mathbf{r}_i} \\ \hat{\mathcal{H}}''(t) &= \frac{e^2 Z^2}{2m_n c^2} A^2(\mathbf{r}_n, t) + \frac{e^2}{2m_e c^2} \sum_i A^2(\mathbf{r}_i, t)\end{aligned}$$



$$i\hbar \dot{\psi}(\mathbf{r}, t) = \left[ E_0 - \hbar(i\nabla_{\mathbf{r}} + \mathbf{q}_0) \cdot \mathbf{v} + H^{\text{eff}}(\mathbf{r}, t) \right] \psi(\mathbf{r}, t)$$

$$H^{\text{eff}}(\mathbf{r}, t) = \frac{e^2}{\hbar c^2} \sum_{j \neq 0} \omega_{j0} |\hat{\mathbf{x}} \cdot \mathbf{d}_{j0}|^2 \mathbf{A}(\mathbf{r}, t) \cdot \tilde{\mathbf{A}}_j(\mathbf{r}, t)$$

$$\tilde{\mathbf{A}}_j(\mathbf{r}, t) = -i\omega_{j0} \int_{-\infty}^t e^{-i\omega_{j0}(t-t')} \mathbf{A}(\mathbf{r} - \mathbf{v}t + \mathbf{v}t', t') dt'$$

# Theory

$$i\hbar \dot{\psi}(\mathbf{r}, t) = \left[ E_0 - \hbar(i\nabla_{\mathbf{r}} + \mathbf{q}_0) \cdot \mathbf{v} + H^{\text{eff}}(\mathbf{r}, t) \right] \psi(\mathbf{r}, t)$$

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collimated beam  
 $(E_0, \mathbf{p}_0)$



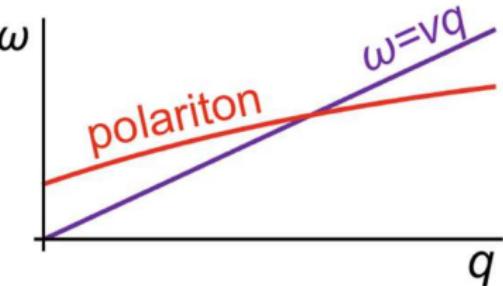
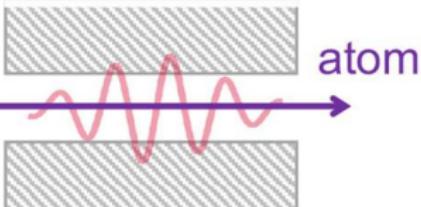
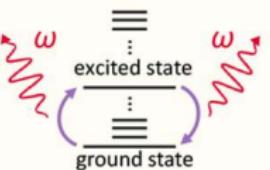
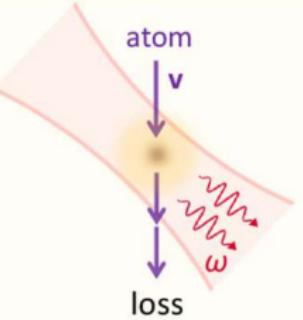
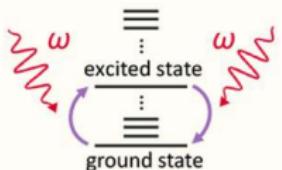
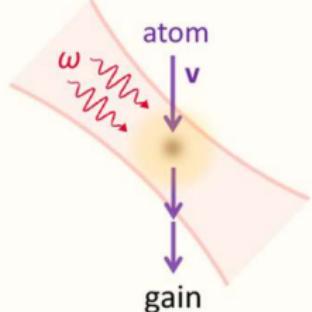
$$\psi(\mathbf{r}, t) = \psi^{\text{inc}}(\mathbf{r}, t) e^{-(i/\hbar) \int_{-\infty}^t dt' H^{\text{eff}}(\mathbf{r} - \mathbf{v}t + \mathbf{v}t', t')}$$

$\varphi$  static  
 elastic interaction

dynamical  
 inelastic interaction  $\beta$

## Inelastic interaction

PINAM

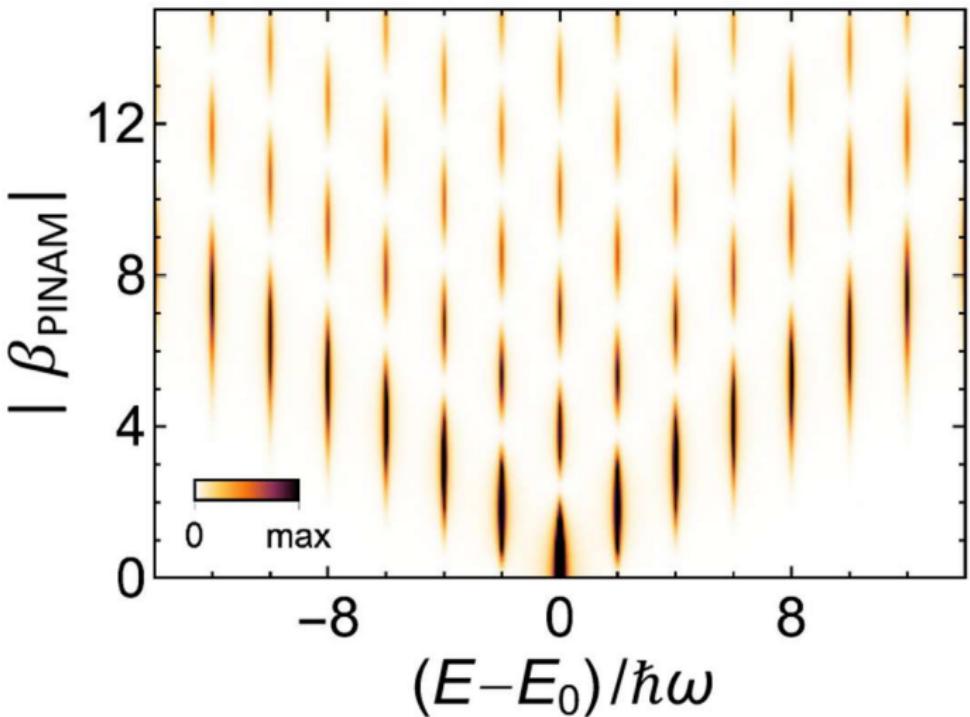


## Near-field interaction

$$\mathbf{q} \cdot \mathbf{v} = \omega$$

inelastic interaction:  $\psi(\mathbf{r}, t) = \psi^{\text{inc}}(\mathbf{r}, t) e^{i\varphi(\mathbf{R})} \exp \left\{ -\beta(\mathbf{R}) e^{2i\omega(z-vt)/v} + \beta^*(\mathbf{R}) e^{-2i\omega(z-vt)/v} \right\}$

$$|\beta_{\text{PINAM}}| \propto L \alpha_0 |\mathcal{E}_0|^2 / v$$



atom

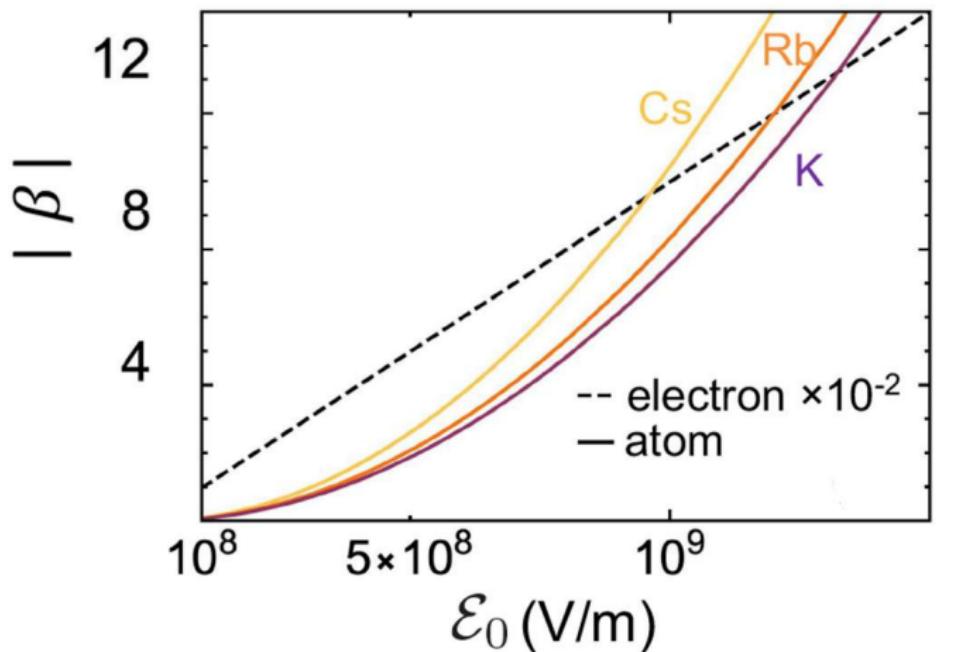
$$\exp \left\{ -\beta(\mathbf{R}) e^{i\omega(z-vt)/v} + \beta^*(\mathbf{R}) e^{-2i\omega(z-vt)/v} \right\}$$

$$|\beta_{\text{PINAM}}| \propto L \alpha_0 |\mathcal{E}_0|^2 / v$$

electron

$$\exp \left\{ -\beta(\mathbf{R}) e^{i\omega(z-vt)/v} + \beta^*(\mathbf{R}) e^{-i\omega(z-vt)/v} \right\}$$

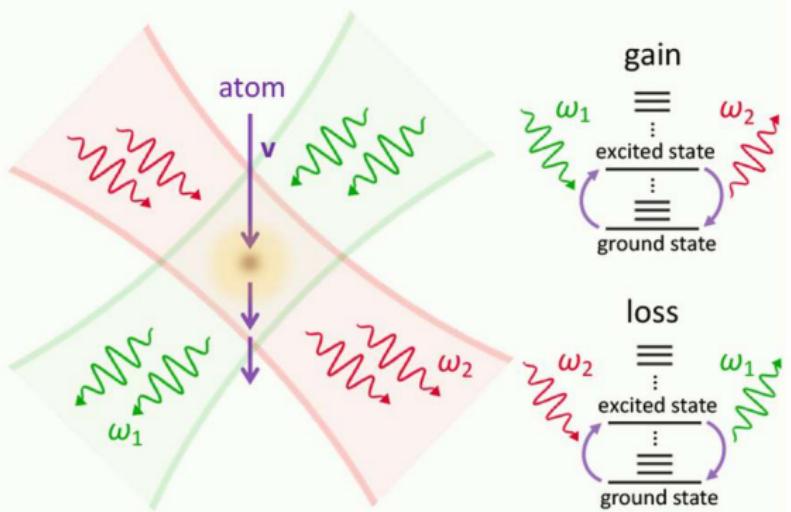
$$|\beta_{\text{PINEM}}| \propto L |\mathcal{E}_0| / \omega$$



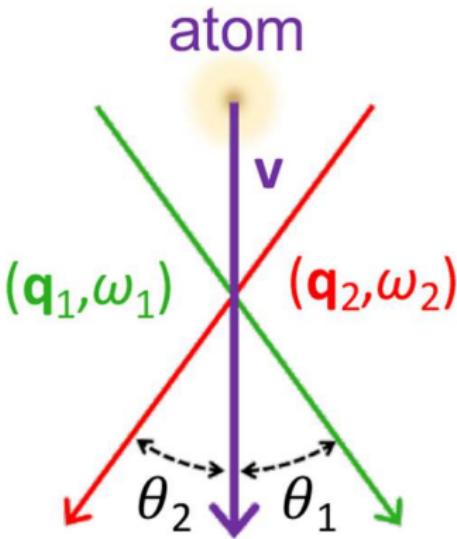
# Stimulated Compton Scattering

Inelastic interaction

Stimulated Compton scattering



Free-space interaction



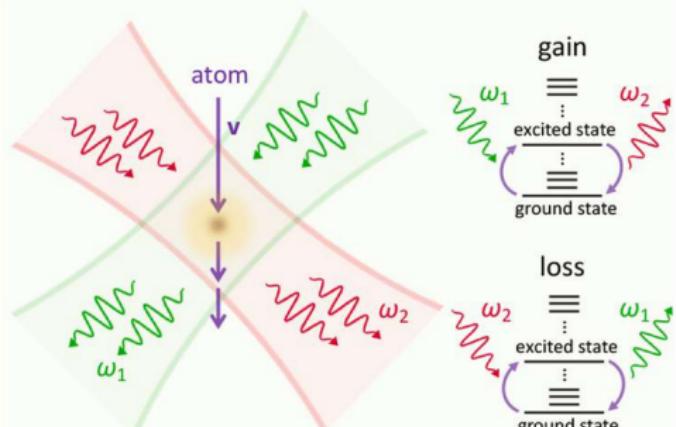
$$(\mathbf{q}_1 - \mathbf{q}_2) \cdot \mathbf{v} = \omega_1 - \omega_2$$

# Stimulated Compton Scattering

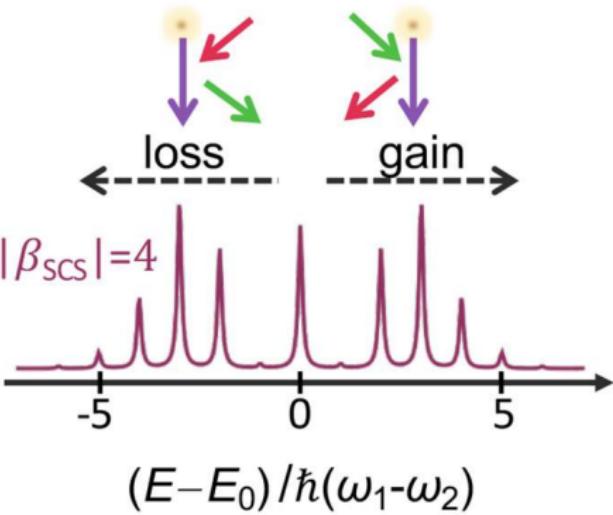
$$\psi(\mathbf{r}, t) = \psi^{\text{inc}}(\mathbf{r}, t) e^{i\varphi} \exp \left\{ -\beta e^{i(\mathbf{q}_1 - \mathbf{q}_2) \cdot (\mathbf{r} - \mathbf{v}t)} + \beta^* e^{-i(\mathbf{q}_1 - \mathbf{q}_2) \cdot (\mathbf{r} - \mathbf{v}t)} \right\}$$

Inelastic interaction

Stimulated Compton scattering



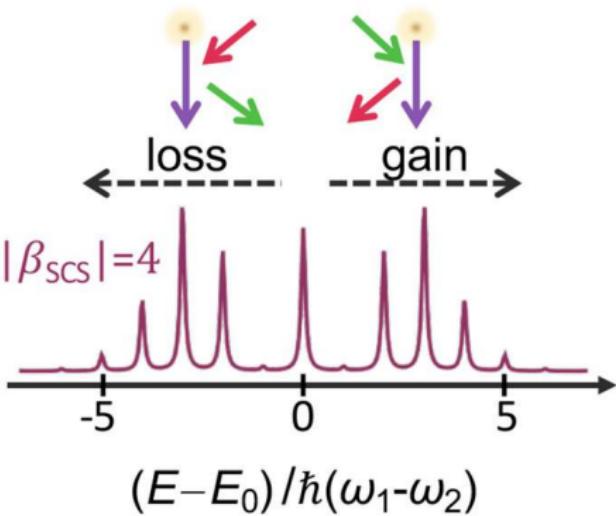
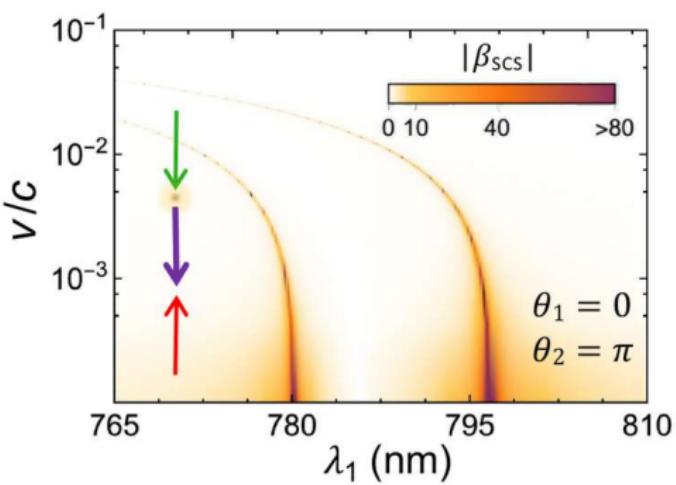
Free-space interaction



# Stimulated Compton Scattering

$$\psi(\mathbf{r}, t) = \psi^{\text{inc}}(\mathbf{r}, t) e^{i\varphi} \exp \left\{ -\beta e^{i(\mathbf{q}_1 - \mathbf{q}_2) \cdot (\mathbf{r} - \mathbf{v}t)} + \beta^* e^{-i(\mathbf{q}_1 - \mathbf{q}_2) \cdot (\mathbf{r} - \mathbf{v}t)} \right\}$$

$$\beta = \beta_{\text{SCS}} \equiv -\frac{2ie^2\omega_1 L}{\hbar^2 v \omega_2} \mathbf{E}_1 \cdot \mathbf{E}_2^* \sum_{j \neq 0} \frac{\omega_{j0} |\hat{\mathbf{x}} \cdot \mathbf{d}_{0j}|^2}{\omega_{j0}^2 - (\omega_1 - \mathbf{q}_1 \cdot \mathbf{v})^2}$$



# Wrap-up

- ▶ Light & atoms before
  - steer the motion of atoms in free space
    - ▶ cooling and trapping of matter waves
    - ▶ ponderomotive interaction & Doppler-mediated photon scattering
- ▶ Light & free electrons
  - modulation of the electron wave function
- ▶ Combination of these two worlds
  - manipulation of matter waves by inelastic interactions with optical fields
- ▶ Realization of the modulation
  - stimulated photon absorption and emission by an atomic beam
    - ▶ interaction with phase-matching evanescent optical fields
    - ▶ stimulated Compton scattering in free space
- ▶ Optical manipulation of matter waves
  - powerful tool for application in atom-based microscopy & spectroscopy

# Optical Manipulation of Matter Waves

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