

GW generation in dark energy EFTs

Marco Crisostomi



GWs meet EFTs
Benasque 23/08/23



European Research Council
Established by the European Commission

arXiv:2008.07546 (JCAP)

arXiv:2009.03354 (PRL)

Based on:

arXiv:2105.13992 (PRD)

arXiv:2107.05648 (PRL)

arXiv:2207.00443 (JCAP)

arXiv:2207.03437 (PRD)



Enrico Barausse



Lotte ter Haar



Carlos Palenzuela



Miguel Bezares

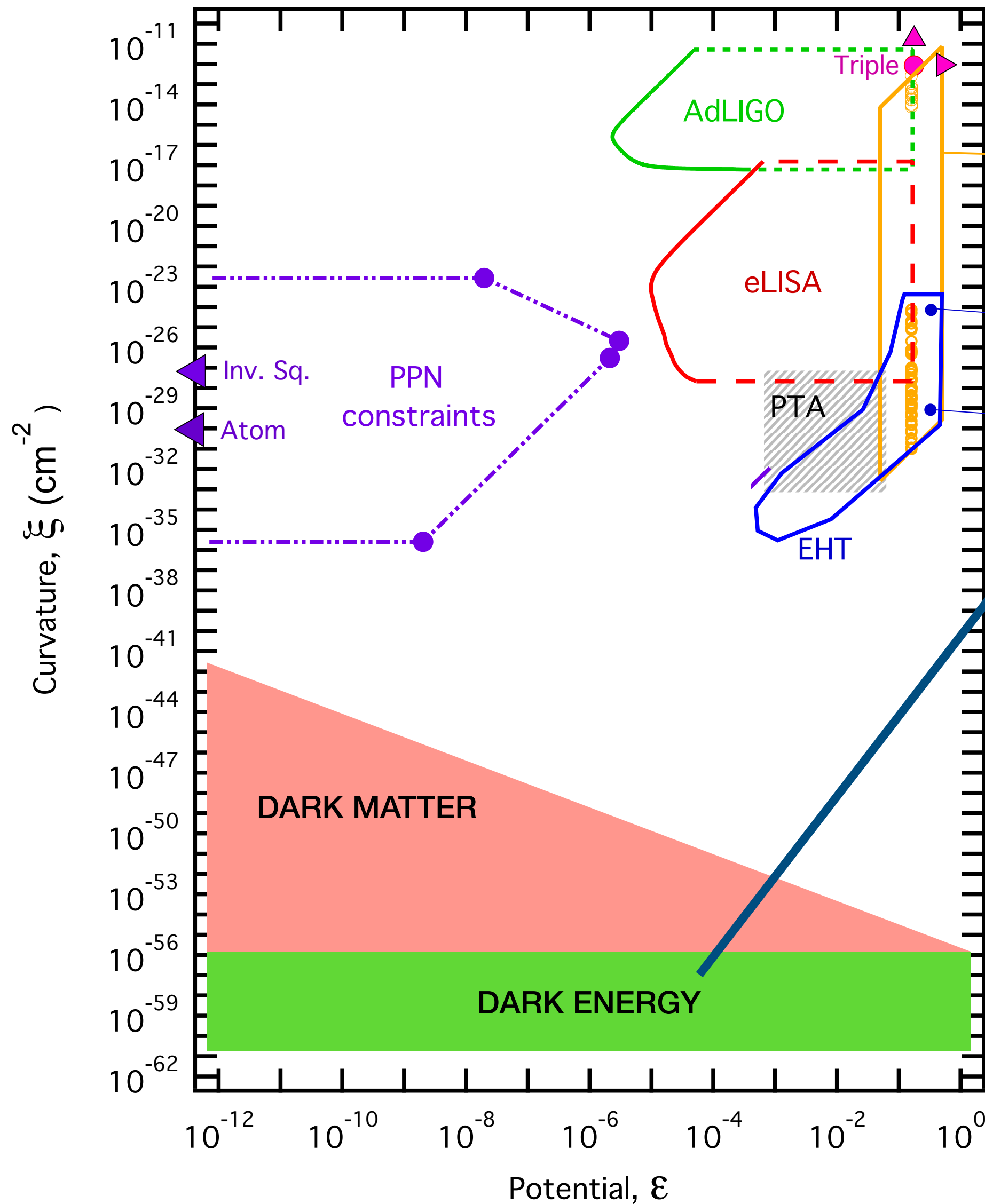


Guillermo Lara



Ricard Aguilera-Miret

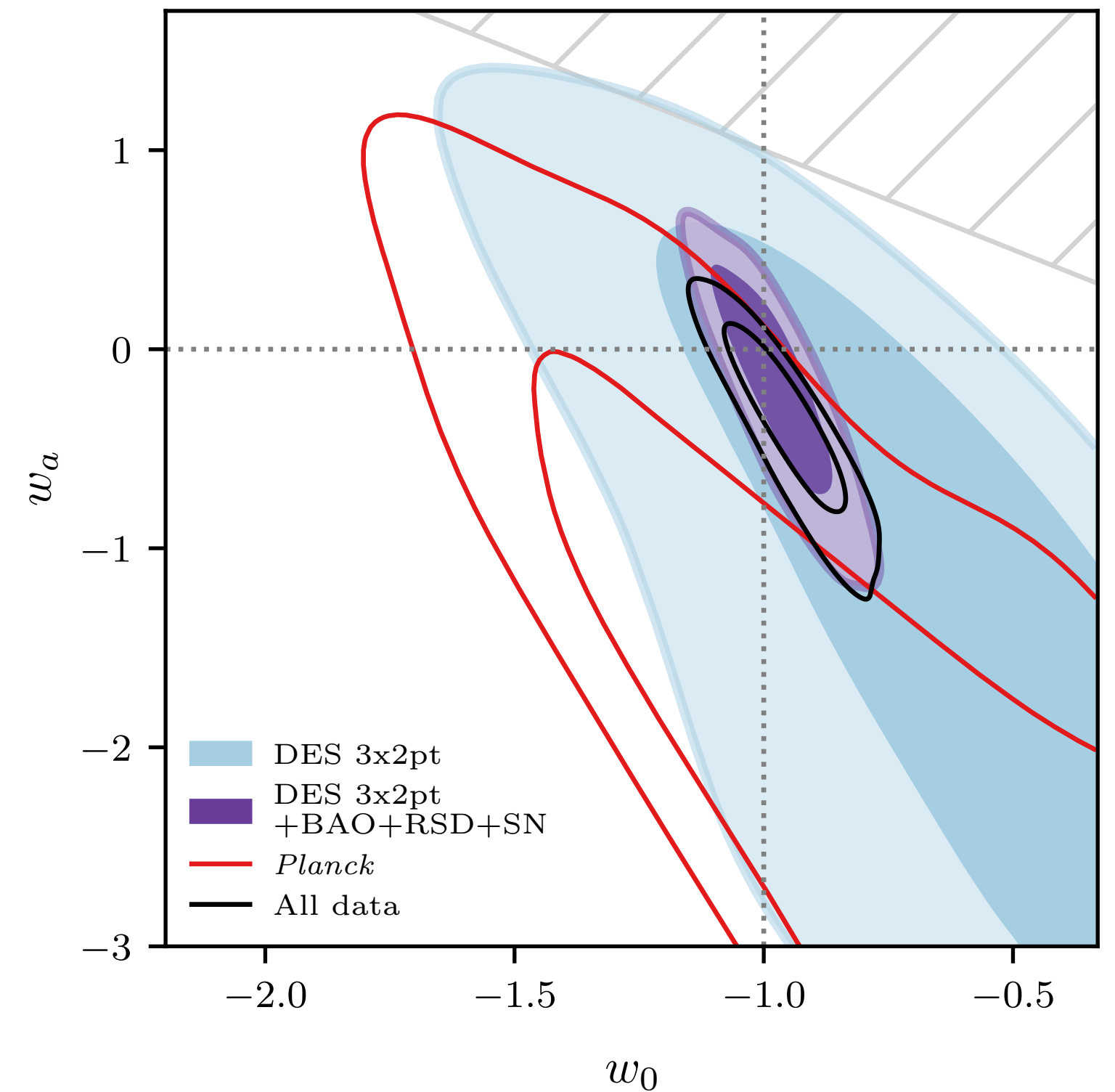
Tests of Gravity



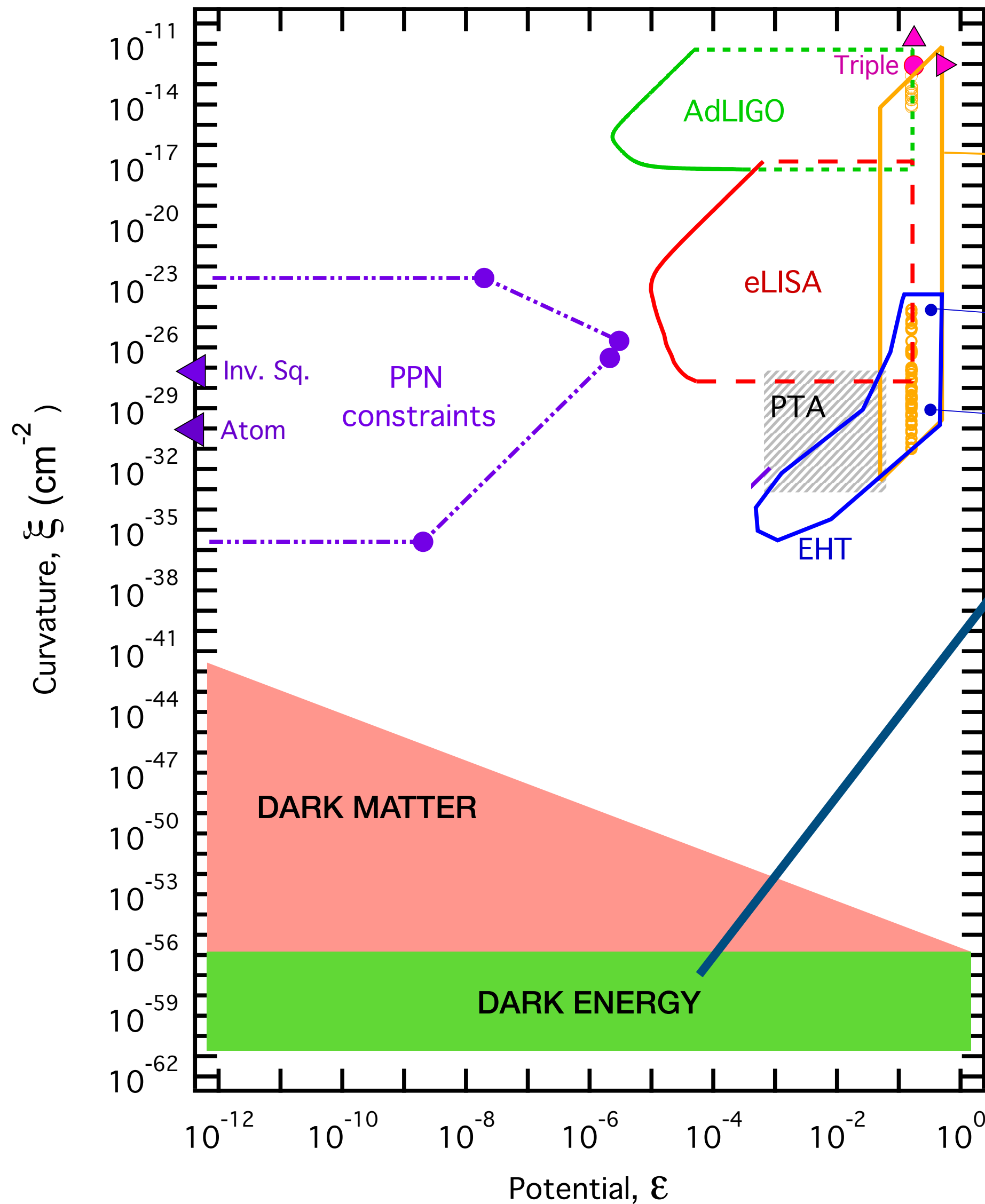
EUCLID
DESI
SKA
Vera Rubin Obs. (LSST)

Dark Energy Survey
 Year 3 Results

$$w_{DE}(a) = w_0 + w_a(1 - a)$$



Tests of Gravity

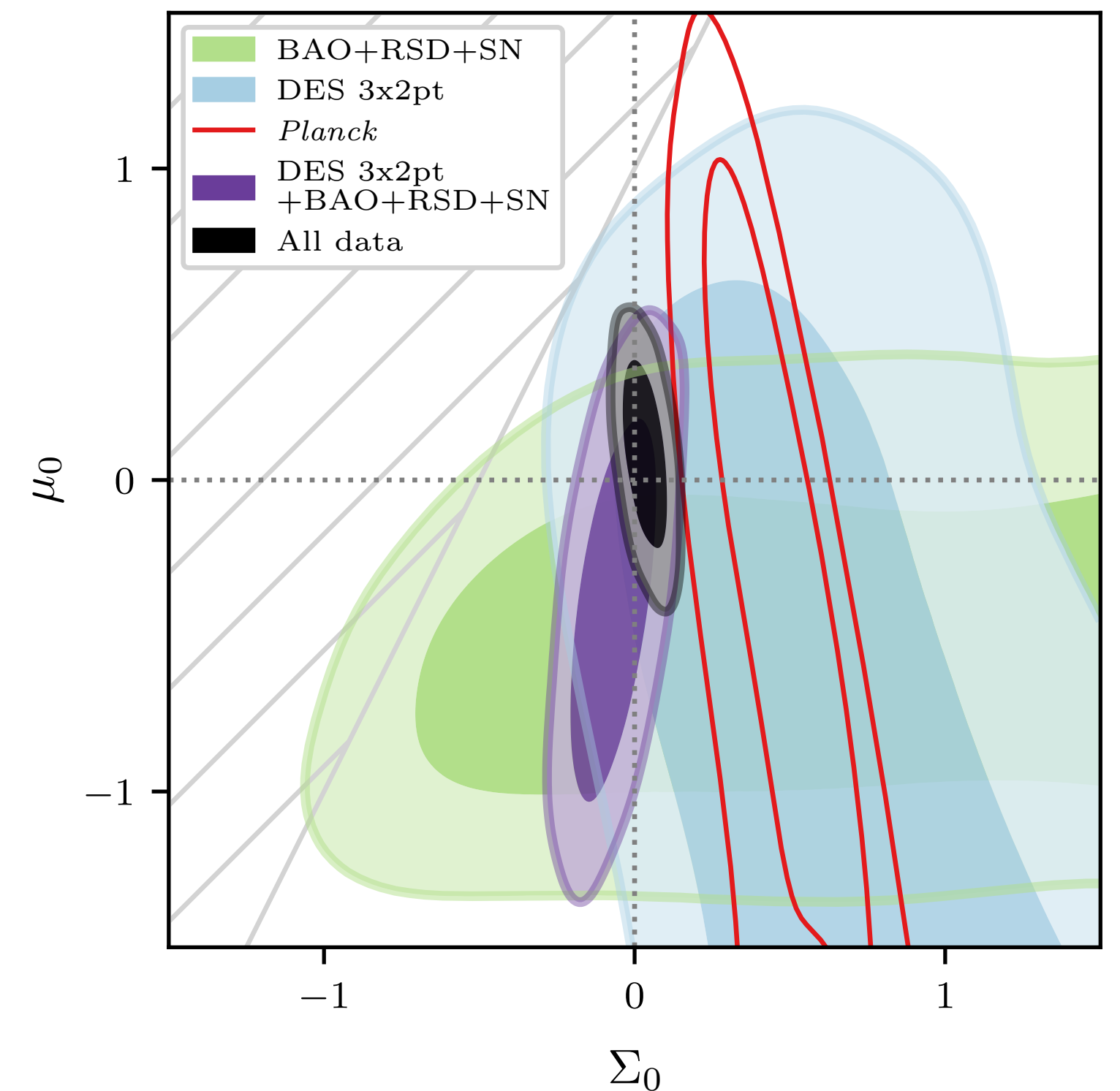


EUCLID
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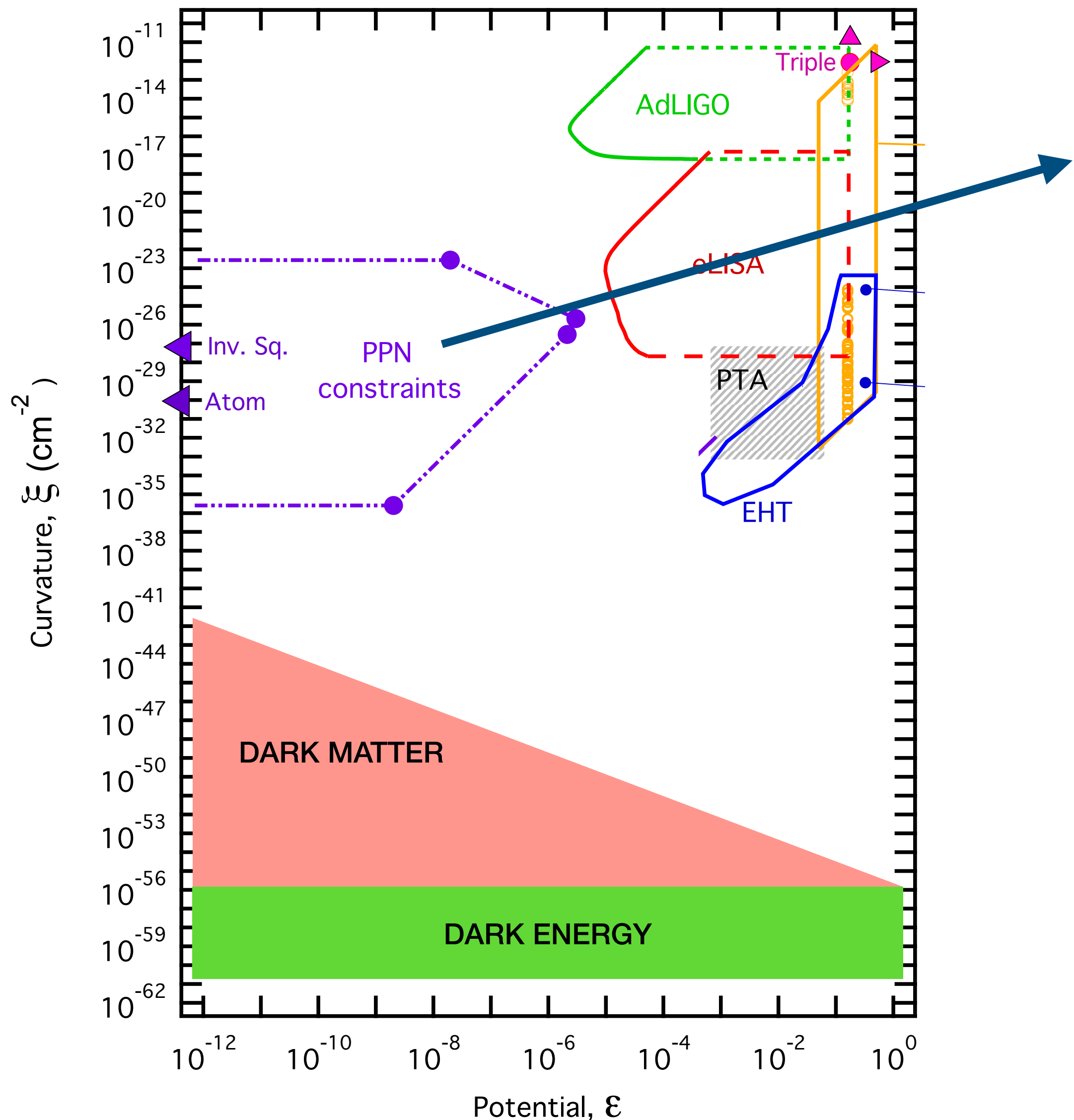
$$k^2 \Psi = -4\pi G a^2 (1 + \mu(a)) \rho \delta$$

$$k^2 (\Psi + \Phi) = -8\pi G a^2 (1 + \Sigma(a)) \rho \delta$$

Dark Energy Survey
 Year 3 Results



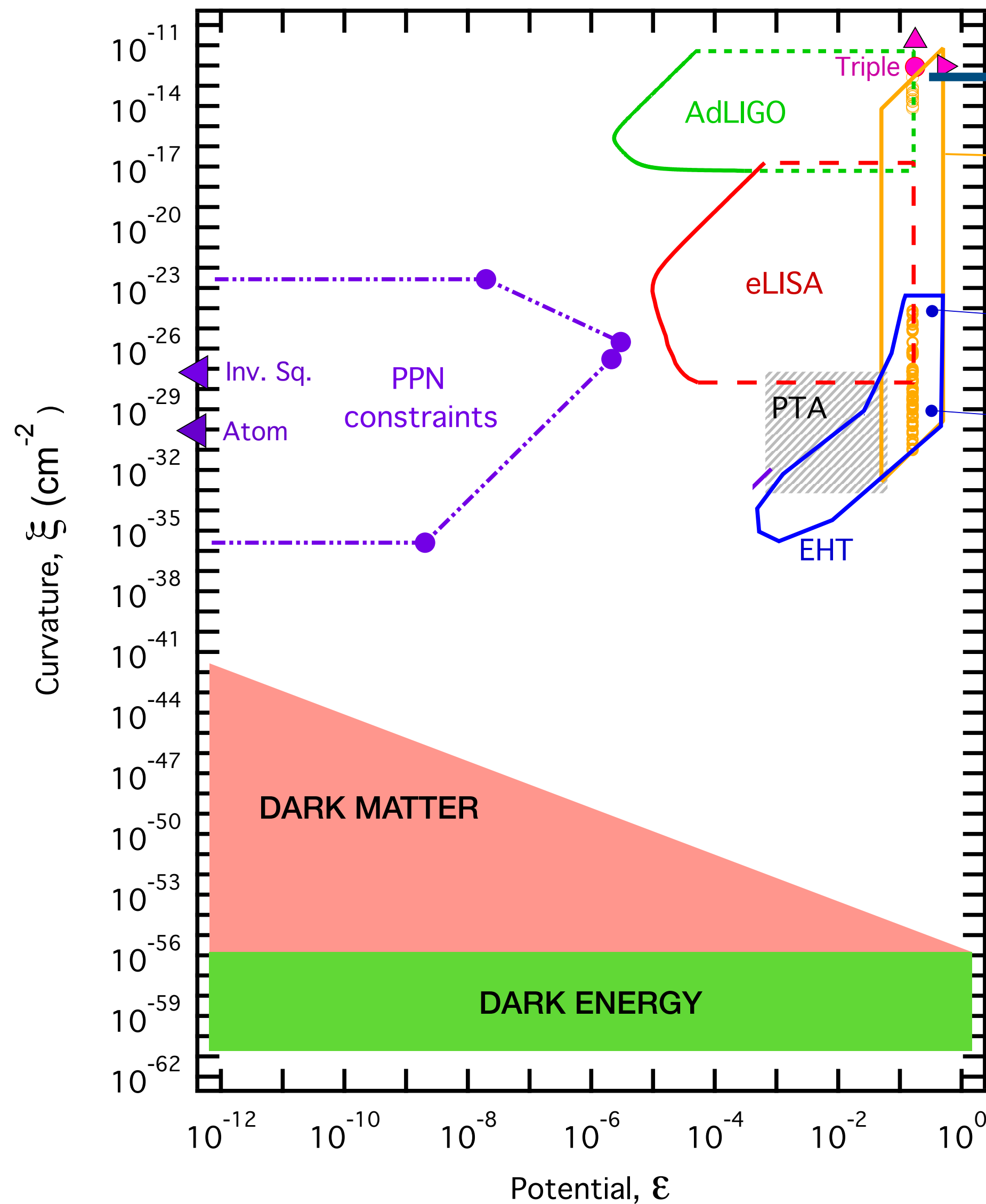
Tests of Gravity



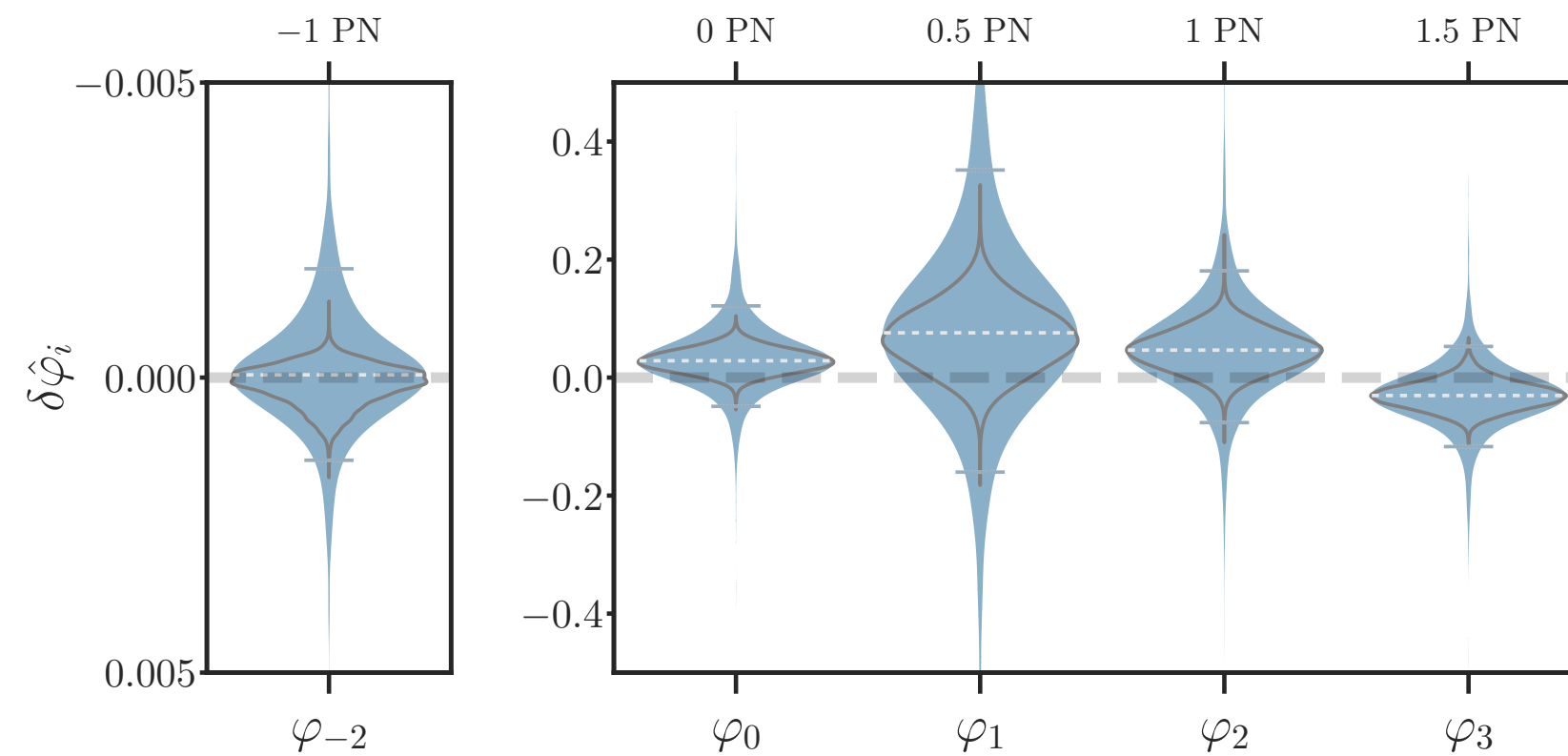
Parameter	Effect	Limit	Remarks
$\gamma - 1$	time delay	2.3×10^{-5}	Cassini tracking
	light deflection	2×10^{-4}	VLBI
$\beta - 1$	perihelion shift	8×10^{-5}	$J_{2\odot} = (2.2 \pm 0.1) \times 10^{-7}$
	Nordtvedt effect	2.3×10^{-4}	$\eta_N = 4\beta - \gamma - 3$ assumed
ξ	spin precession	4×10^{-9}	millisecond pulsars
α_1	orbital polarization	10^{-4}	Lunar laser ranging
		4×10^{-5}	PSR J1738+0333
α_2	spin precession	2×10^{-9}	millisecond pulsars
α_3	pulsar acceleration	4×10^{-20}	pulsar \dot{P} statistics
ζ_1	—	2×10^{-2}	combined PPN bounds
ζ_2	binary acceleration	4×10^{-5}	\ddot{P}_p for PSR 1913+16
ζ_3	Newton's 3rd law	10^{-8}	lunar acceleration
ζ_4	—	—	not independent [see Eq. (73)]

C. Will LLR '14

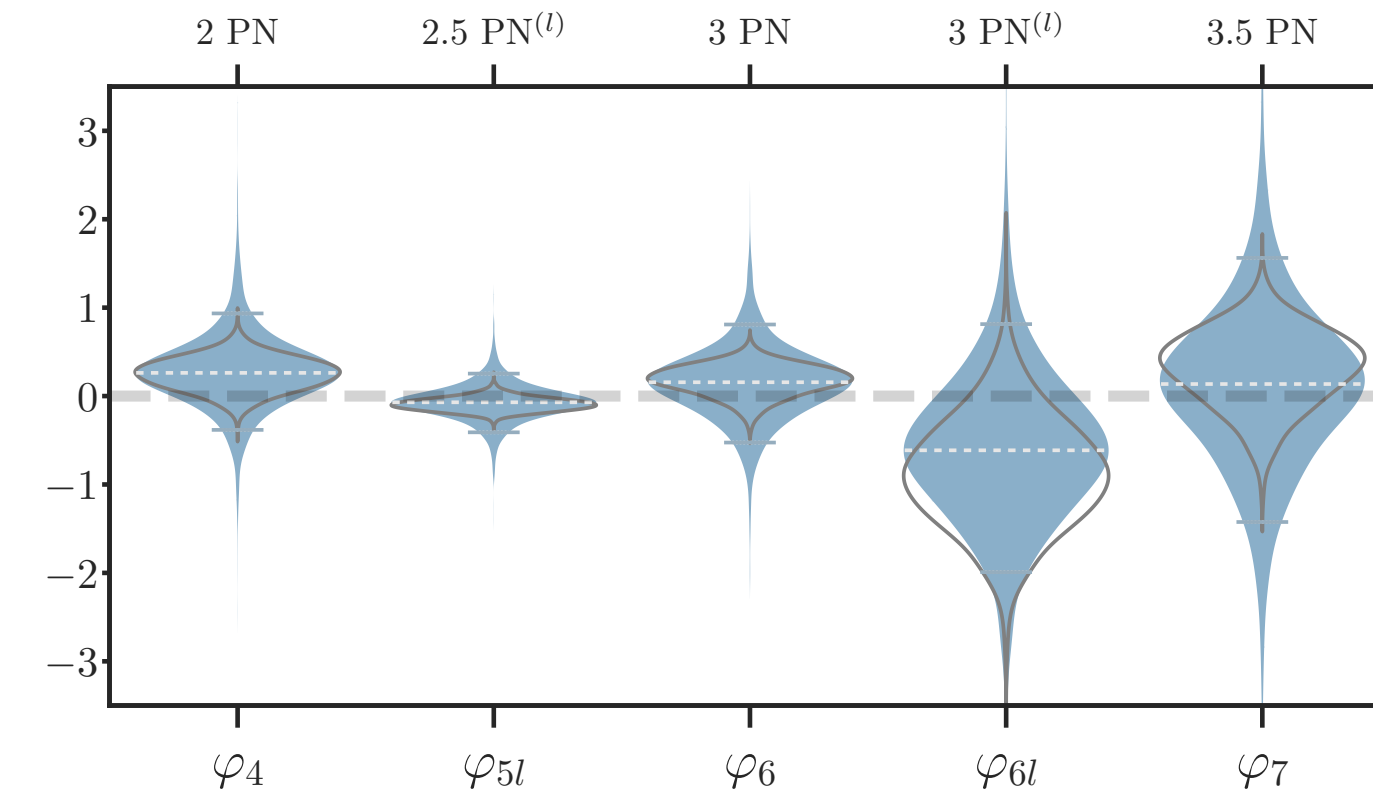
Tests of Gravity



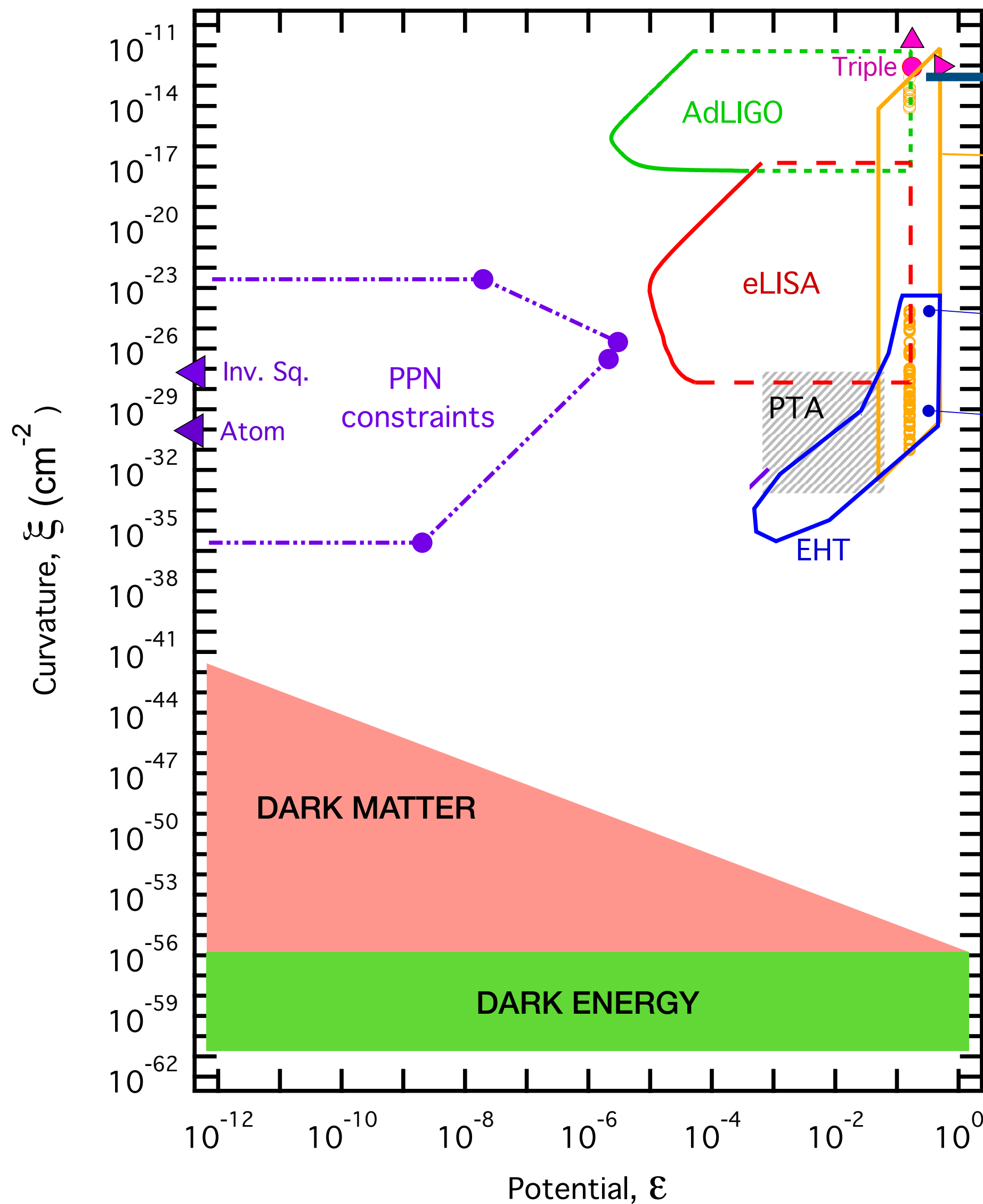
~ 65 BBH detected



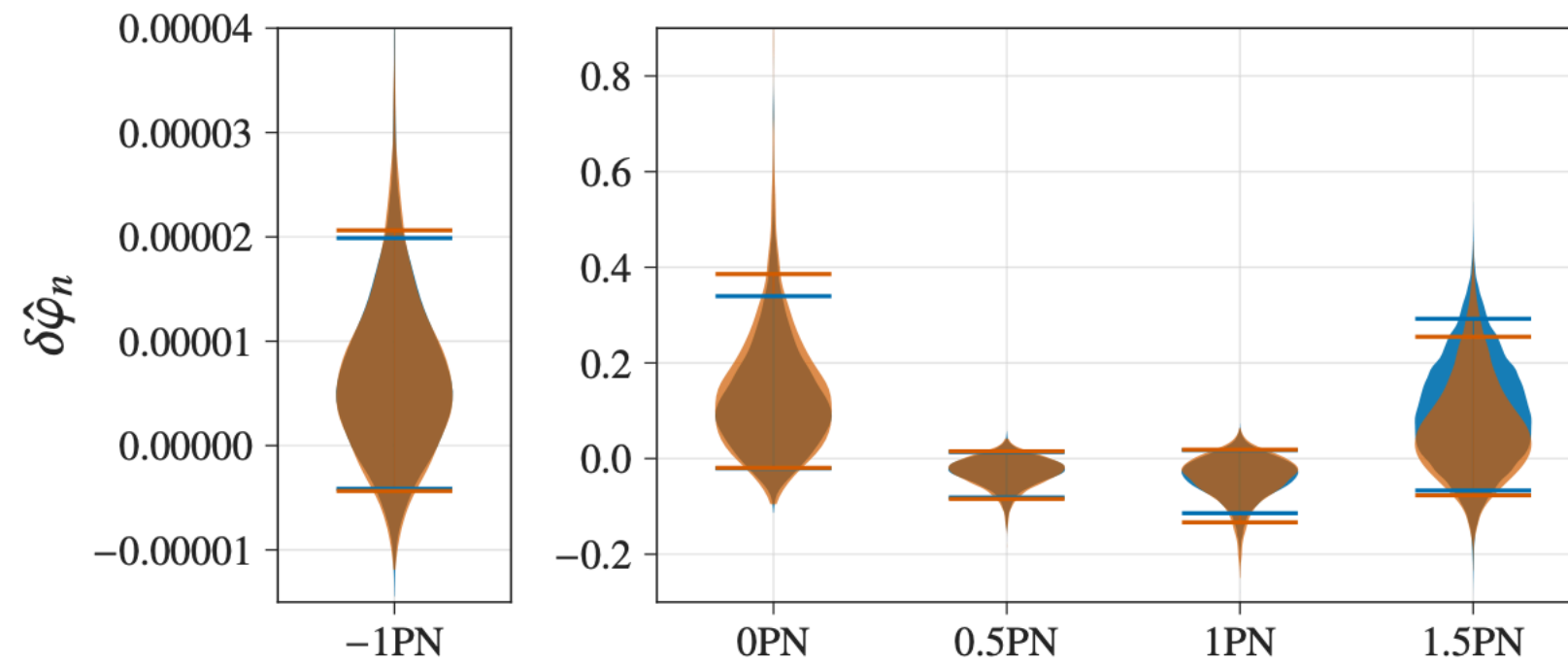
LIGO/Virgo Dec. '21



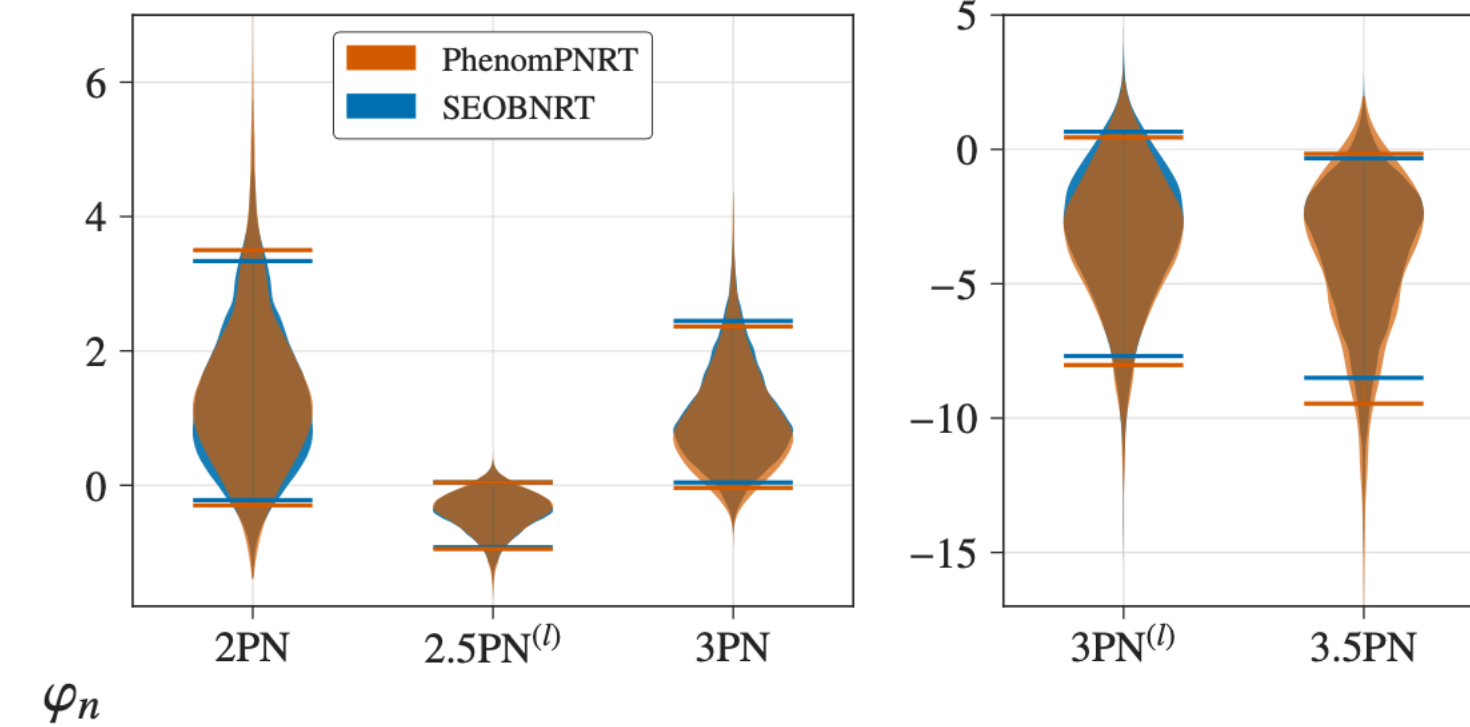
Tests of Gravity



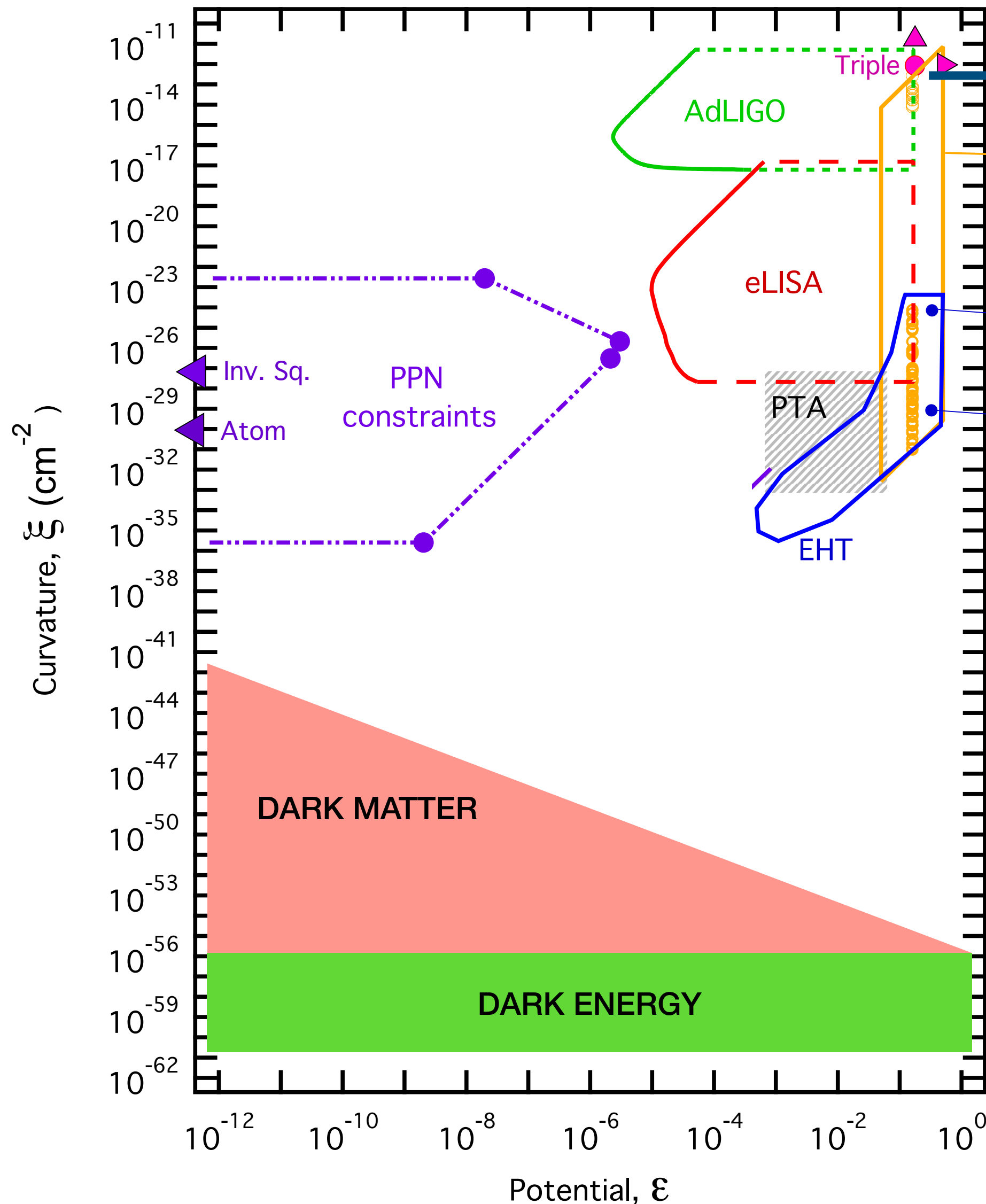
BNS GW170817



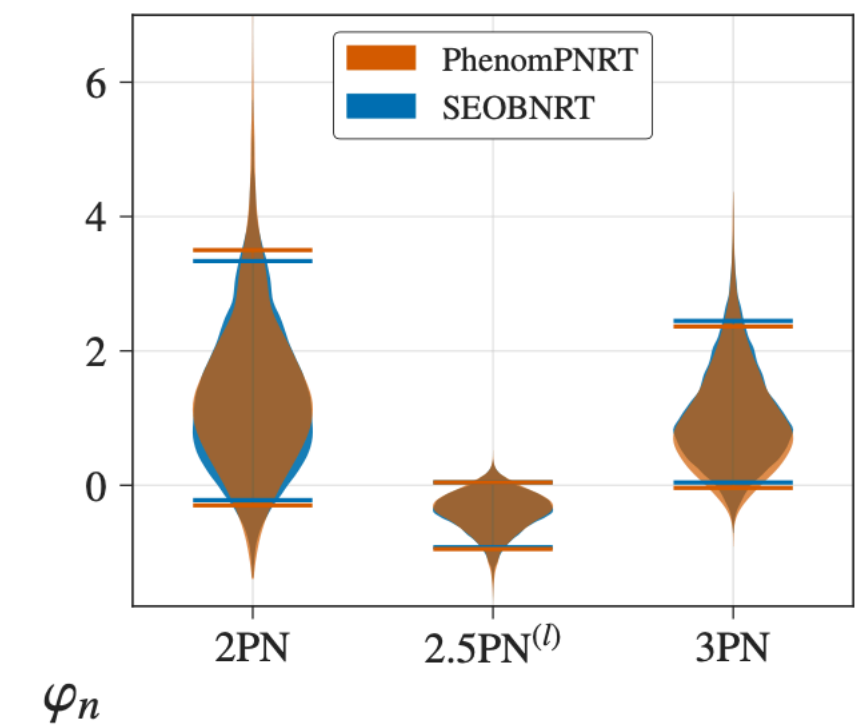
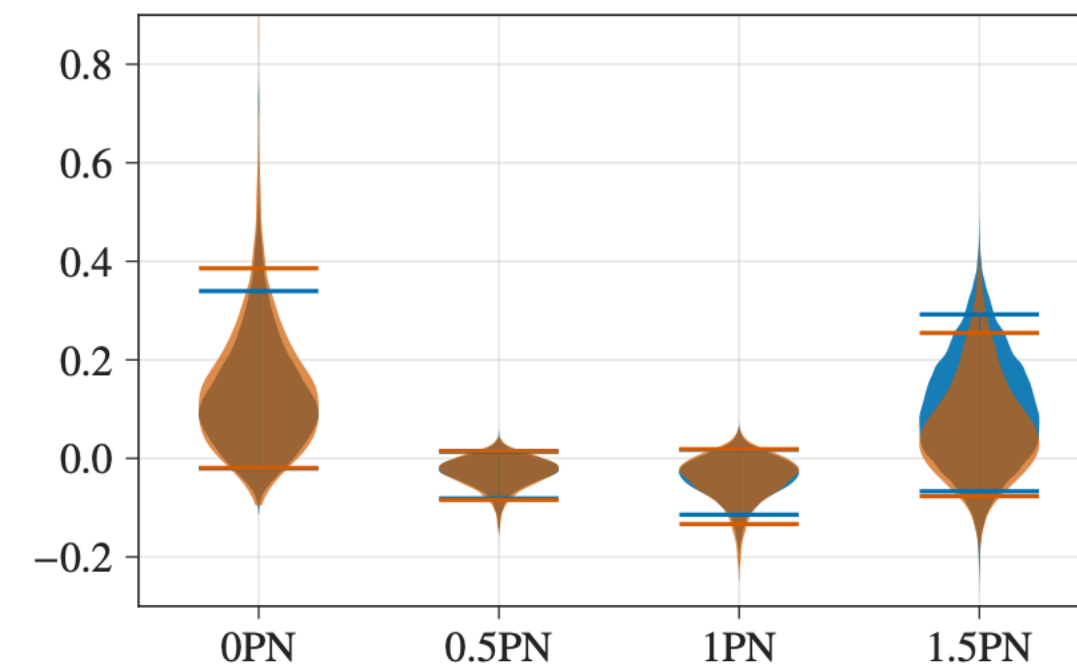
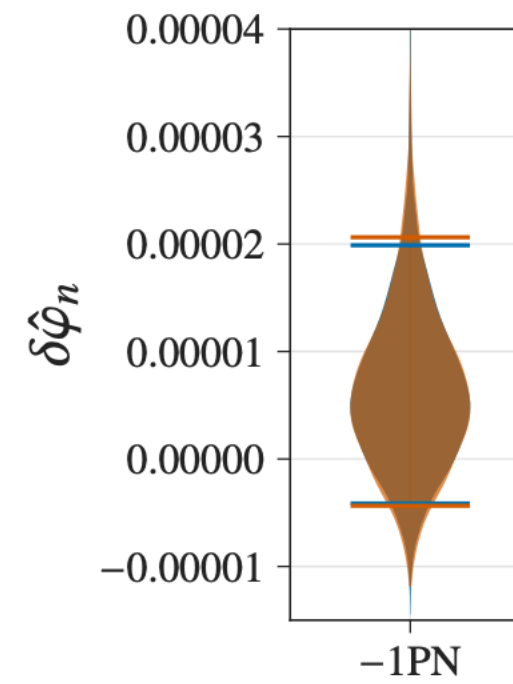
LIGO/Virgo '18



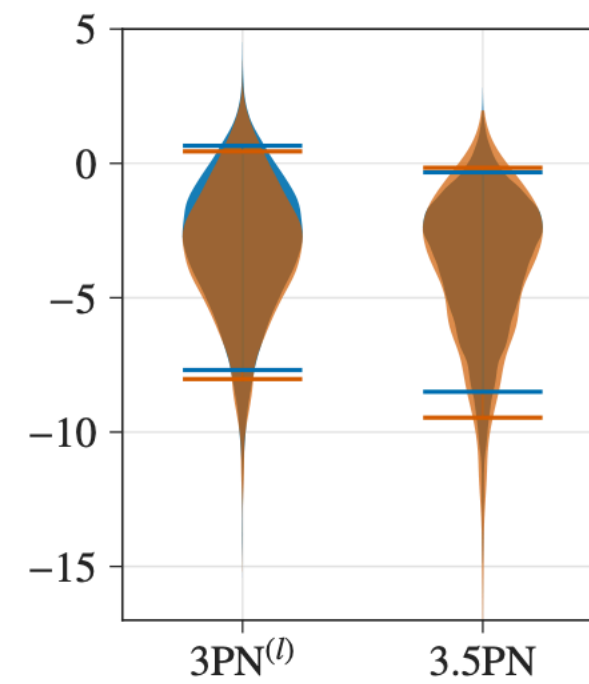
Tests of Gravity



BNS GW170817

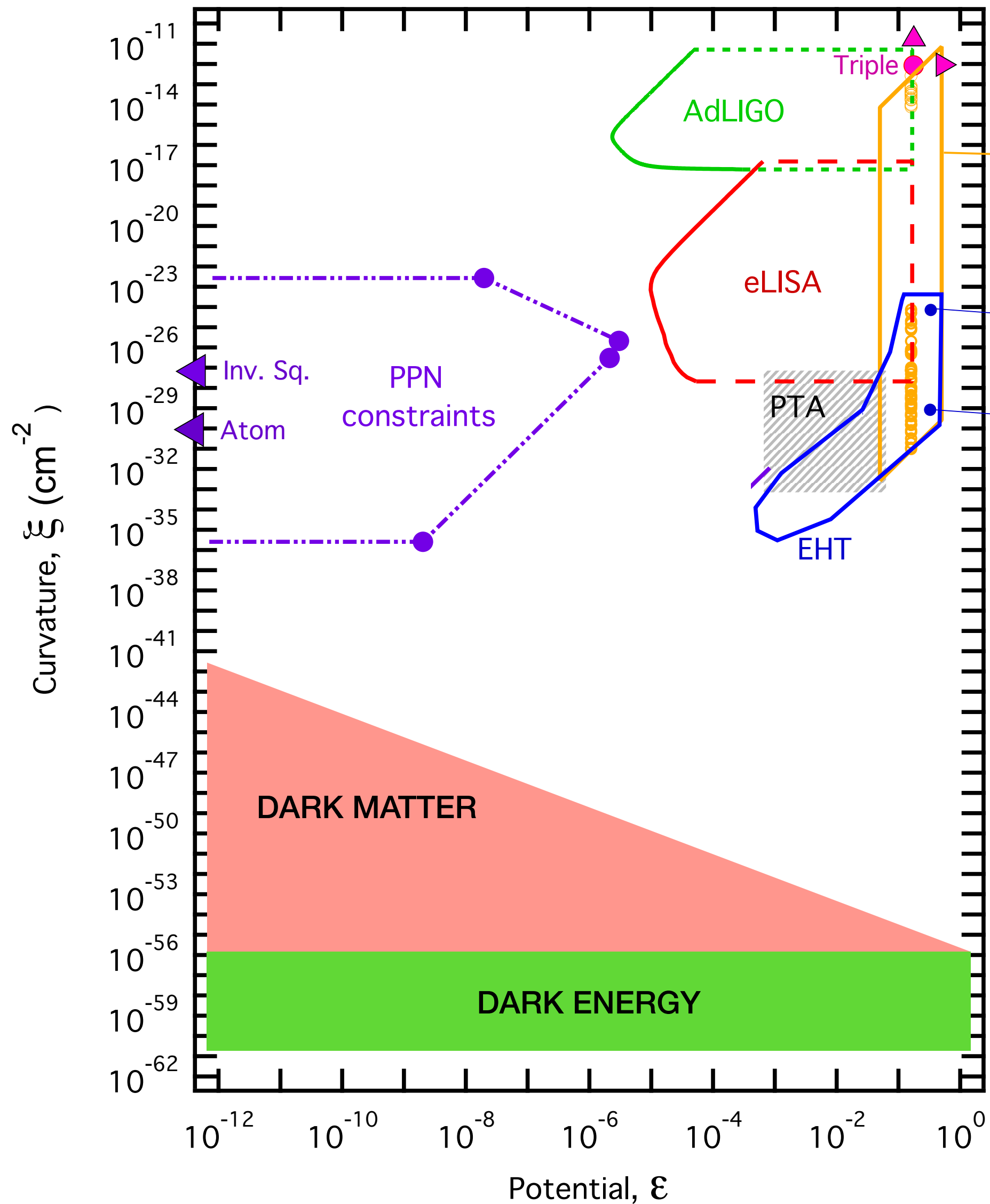


LIGO/Virgo '18



We find no evidence in support of physics beyond general relativity

Screening Mechanisms



Volume 39B, number 3

PHYSICS LETTERS

1 May 1972

TO THE PROBLEM OF NONVANISHING GRAVITATION MASS

A. I. VAINSHTEIN

Institute of Nuclear Physics, Novosibirsk, USSR

Revised manuscript received 17 February 1972

Large distances modification and screening

1) We do want a sizeable modification at cosmological scales

$$L = M_{Pl}^2 R - \frac{1}{2} (\partial\phi)^2 - \frac{1}{2} m^2 \phi^2$$

\Rightarrow Very light mode

$$H^2 \sim m^2$$

$$L = M_{Pl}^2 R - \frac{1}{2} (\partial\phi)^2 + \frac{\beta}{4\Lambda^4} (\partial\phi)^4$$

$$M_{Pl}^2 H^2 \sim \Lambda^4$$

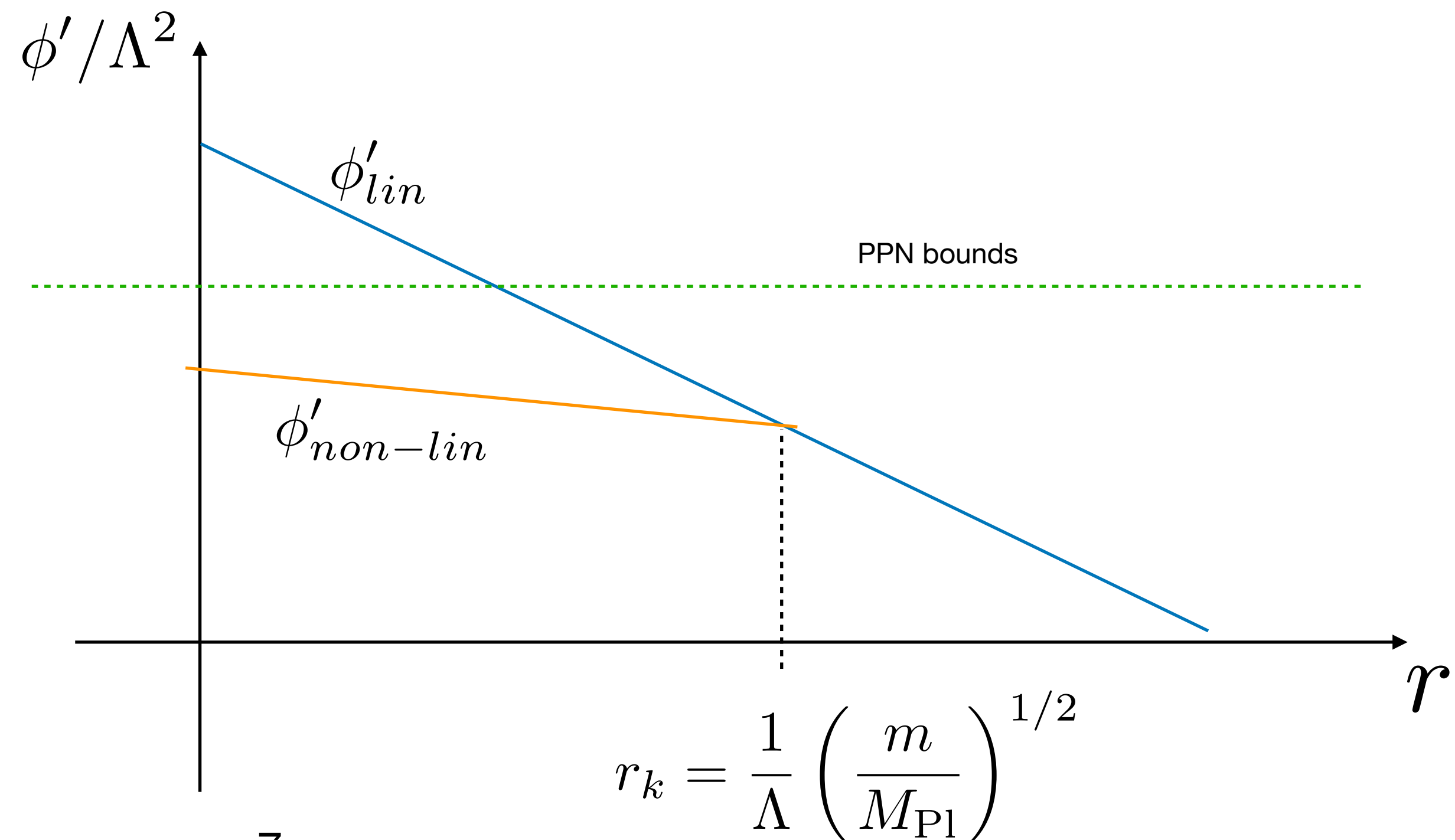
Large distances modification and screening

2) We do not want a modification at short scales

$$L = -\frac{1}{2}(\partial\phi)^2 + \frac{\beta}{4\Lambda^4}(\partial\phi)^4 + \frac{a}{M_{\text{Pl}}}\phi T$$

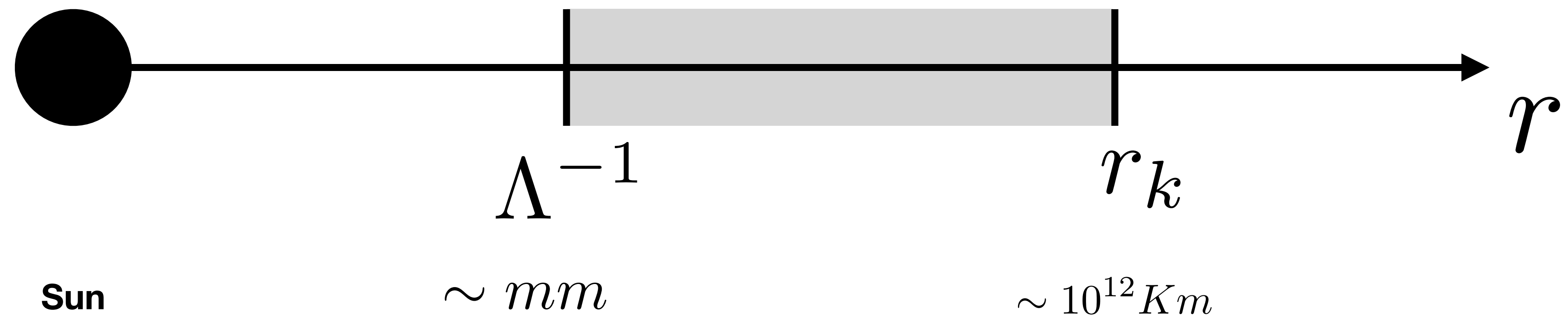
$$\phi'_{lin} \sim \frac{1}{r^2}$$

$$\phi'_{non-lin} \sim \frac{1}{r^{2/3}}$$



Large distances modification and screening

Summary

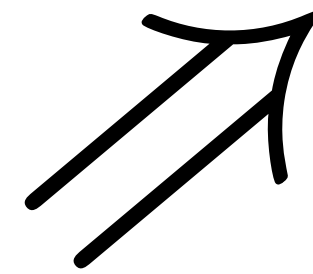


Nicolis & Rattazzi '04
De Rham & Ribeiro '14
Brax & Valageas '14

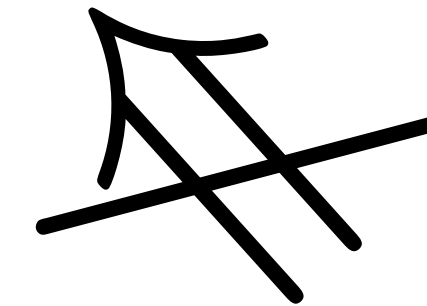
Well-posedness ?

Cauchy problem

Unique solution that depends continuously on the initial data



$$\partial_t \mathbf{u} + \mathbf{A}^k \partial_k \mathbf{u} = \mathbf{S}(\mathbf{u})$$



Strong hyperbolicity

Characteristic matrix

Weak hyperbolicity

Complete set of eigenvectors
and real eigenvalues

Real eigenvalues but
incomplete set of eigenvectors

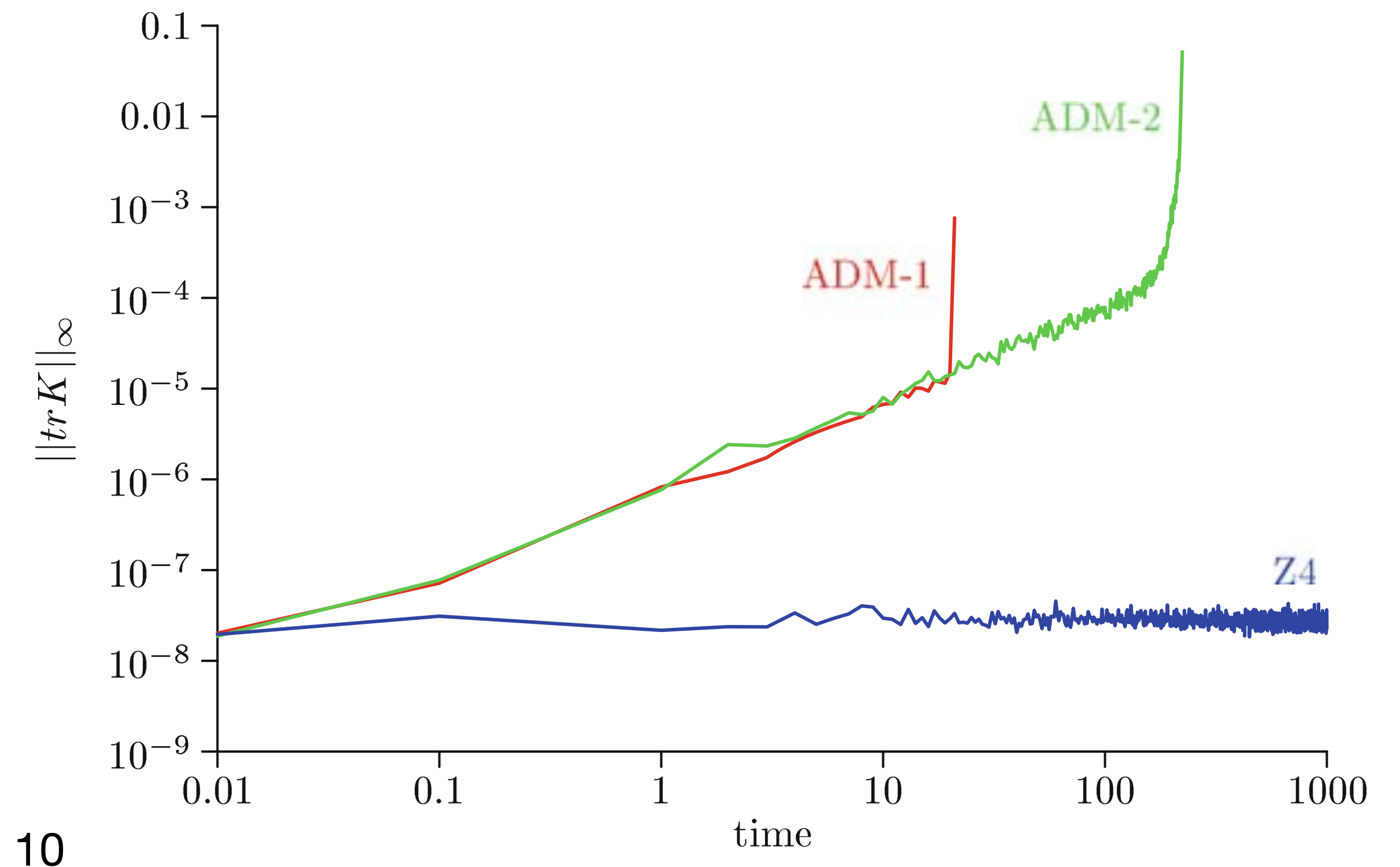
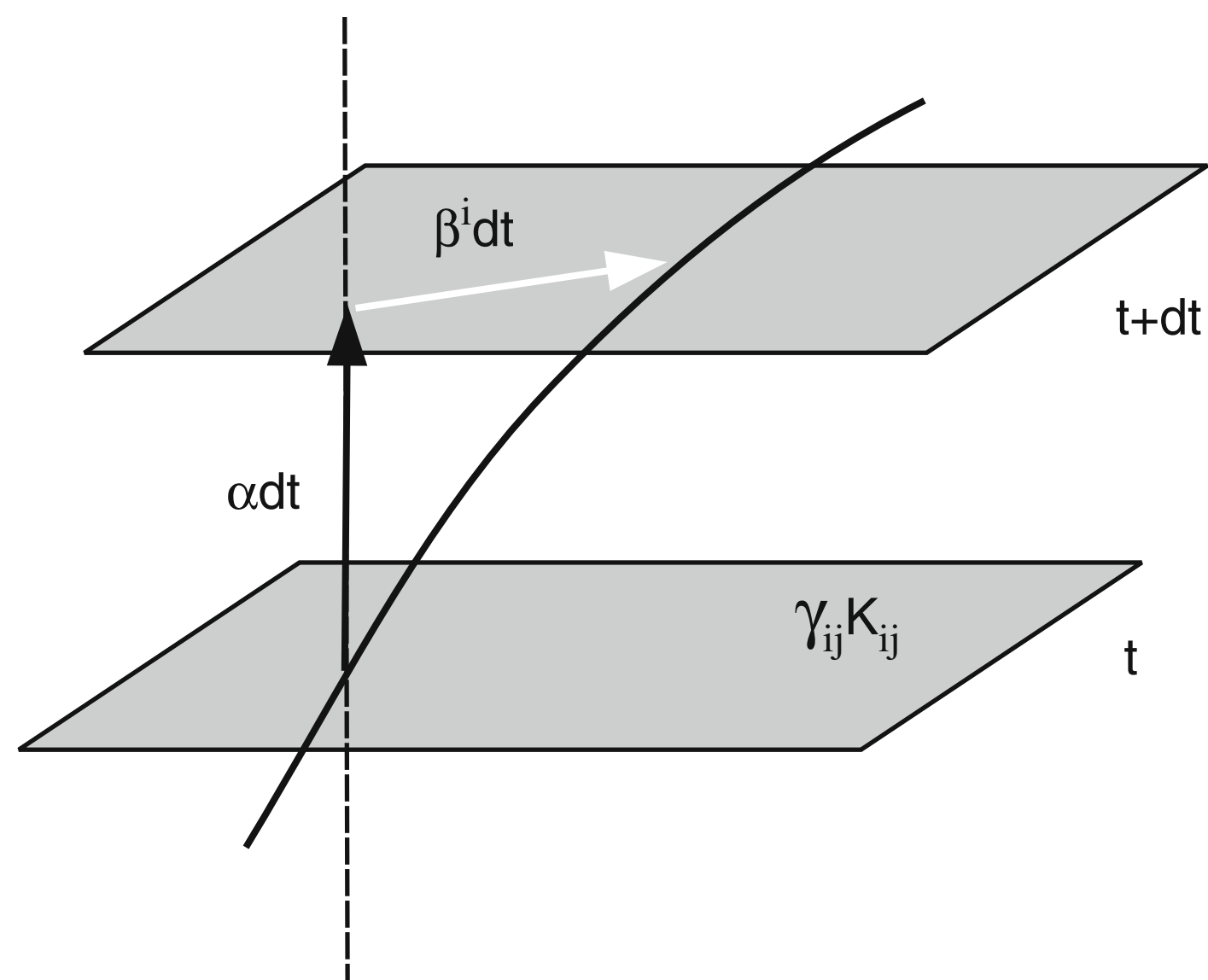
Well-posedness ?

Cauchy problem

Unique solution that depends continuously on the initial data

GR in ADM formulation is not well-posed!

$$ds^2 = -\alpha^2 dt^2 + \gamma_{ij} (dy^i + \beta^i dt) (dy^j + \beta^j dt)$$



Well-posedness ?

CCZ4 formalism

$$R_{ab} + \nabla_a Z_b + \nabla_a Z_b = 8\pi \left(T_{ab} - \frac{1}{2} g_{ab} \text{tr} T \right) + \kappa_z (n_a Z_b + n_b Z_a - g_{ab} n^c Z_c)$$

$$\begin{aligned} \partial_t \tilde{\gamma}_{ij} &= \beta^k \partial_k \tilde{\gamma}_{ij} + \tilde{\gamma}_{ik} \partial_j \beta^k + \tilde{\gamma}_{kj} \partial_i \beta^k - \frac{2}{3} \tilde{\gamma}_{ij} \partial_k \beta^k - 2\alpha \left(\tilde{A}_{ij} - \frac{\lambda_0}{3} \tilde{\gamma}_{ij} \text{tr} \tilde{A} \right) - \frac{\kappa_c}{3} \alpha \tilde{\gamma}_{ij} \ln \tilde{\gamma}, \\ \partial_t \tilde{A}_{ij} &= \beta^k \partial_k \tilde{A}_{ij} + \tilde{A}_{ik} \partial_j \beta^k + \tilde{A}_{kj} \partial_i \beta^k - \frac{2}{3} \tilde{A}_{ij} \partial_k \beta^k - \frac{\kappa_c}{3} \alpha \tilde{\gamma}_{ij} \text{tr} \tilde{A} \\ &\quad + \chi \left[\alpha \left({}^{(3)}R_{ij} + \nabla_i Z_j + \nabla_j Z_i - 8\pi S_{ij} \right) - \nabla_i \nabla_j \alpha \right]^{\text{TF}} + \alpha \left(\text{tr} \hat{K} \tilde{A}_{ij} - 2\tilde{A}_{ik} \tilde{A}^k_j \right), \\ \partial_t \chi &= \beta^k \partial_k \chi + \frac{2}{3} \chi \left[\alpha (\text{tr} \hat{K} + 2\Theta) - \partial_k \beta^k \right], \\ \partial_t \text{tr} \hat{K} &= \beta^k \partial_k \text{tr} \hat{K} - \nabla_i \nabla^i \alpha + \alpha \left[\frac{1}{3} (\text{tr} \hat{K} + 2\Theta)^2 + \tilde{A}_{ij} \tilde{A}^{ij} + 4\pi (\tau + \text{tr} S) + \kappa_z \Theta \right] \\ &\quad + 2 Z^i \nabla_i \alpha, \\ \partial_t \Theta &= \beta^k \partial_k \Theta + \frac{\alpha}{2} \left[{}^{(3)}R + 2\nabla_i Z^i + \frac{2}{3} \text{tr}^2 \hat{K} + \frac{2}{3} \Theta (\text{tr} \hat{K} - 2\Theta) - \tilde{A}_{ij} \tilde{A}^{ij} \right] - Z^i \nabla_i \alpha \\ &\quad - \alpha \left[8\pi \tau + 2\kappa_z \Theta \right], \\ \partial_t \hat{\Gamma}^i &= \beta^j \partial_j \hat{\Gamma}^i - \hat{\Gamma}^j \partial_j \beta^i + \frac{2}{3} \hat{\Gamma}^i \partial_j \beta^j + \tilde{\gamma}^{jk} \partial_j \partial_k \beta^i + \frac{1}{3} \tilde{\gamma}^{ij} \partial_j \partial_k \beta^k \\ &\quad - 2\tilde{A}^{ij} \partial_j \alpha + 2\alpha \left[\tilde{\Gamma}^i_{jk} \tilde{A}^{jk} - \frac{3}{2\chi} \tilde{A}^{ij} \partial_j \chi - \frac{2}{3} \tilde{\gamma}^{ij} \partial_j \text{tr} \hat{K} - 8\pi \tilde{\gamma}^{ij} S_i \right] \\ &\quad + 2\alpha \left[-\tilde{\gamma}^{ij} \left(\frac{1}{3} \partial_j \Theta + \frac{\Theta}{\alpha} \partial_j \alpha \right) - \frac{1}{\chi} Z^i \left(\kappa_z + \frac{2}{3} (\text{tr} \hat{K} + 2\Theta) \right) \right], \end{aligned}$$

$$\partial_t \alpha = \beta^i \partial_i \alpha - \alpha^2 f \text{tr} \hat{K},$$

$$\partial_t \beta^i = \beta^j \partial_j \beta^i + g B^i,$$

$$\partial_t B^i = \beta^j \partial_j B^i - \eta B^i + \partial_t \hat{\Gamma}^i - \beta^j \partial_j \hat{\Gamma}^i,$$

1+log slicing

Gamma-driver shift condition

**O(20) equations with
Thousands terms**

Well-posedness ?

$$S = \int d^4x \sqrt{-g} \left[\frac{R}{16\pi G} + K(X) \right]$$

$$K(X) = -\frac{1}{2}X + \frac{\beta}{4\Lambda^4}X^2 - \frac{\gamma}{8\Lambda^8}X^3$$

$$X \equiv \nabla_\mu \phi \nabla^\mu \phi$$

$$\gamma^{\mu\nu} \nabla_\mu \nabla_\nu \phi = 0$$

$$\gamma^{\mu\nu} \equiv g^{\mu\nu} + \frac{2K''(X)}{K'(X)} \nabla^\mu \phi \nabla^\nu \phi$$

$$\partial_t \mathbf{u} + \mathbf{A}^k \partial_k \mathbf{u} = \mathbf{S}(\mathbf{u})$$

$$V_\pm = -\frac{\gamma^{tr}}{\gamma^{tt}} \pm \sqrt{\frac{-\det(\gamma^{\mu\nu})}{(\gamma^{tt})^2}} < 0 \neq 0$$

$$\mathbf{u} \equiv (\partial_t \phi, \partial_r \phi)$$

$$\det(\gamma^{\mu\nu}) = -\frac{1}{\alpha^2 g_{rr}} \left(1 + \frac{2K''}{K'} X \right)$$

Well-posedness ?

Caustics / shocks

$$\partial_t \mathbf{u} + \mathbf{A}^k \partial_k \mathbf{u} = \mathbf{S}(\mathbf{u}) \quad \longrightarrow \quad \partial_t \mathbf{u} + \partial_k \mathbf{F}^k(\mathbf{u}) = \mathbf{S}(\mathbf{u})$$

Burgers equation

$$\partial_t u + u \partial_x u = 0$$

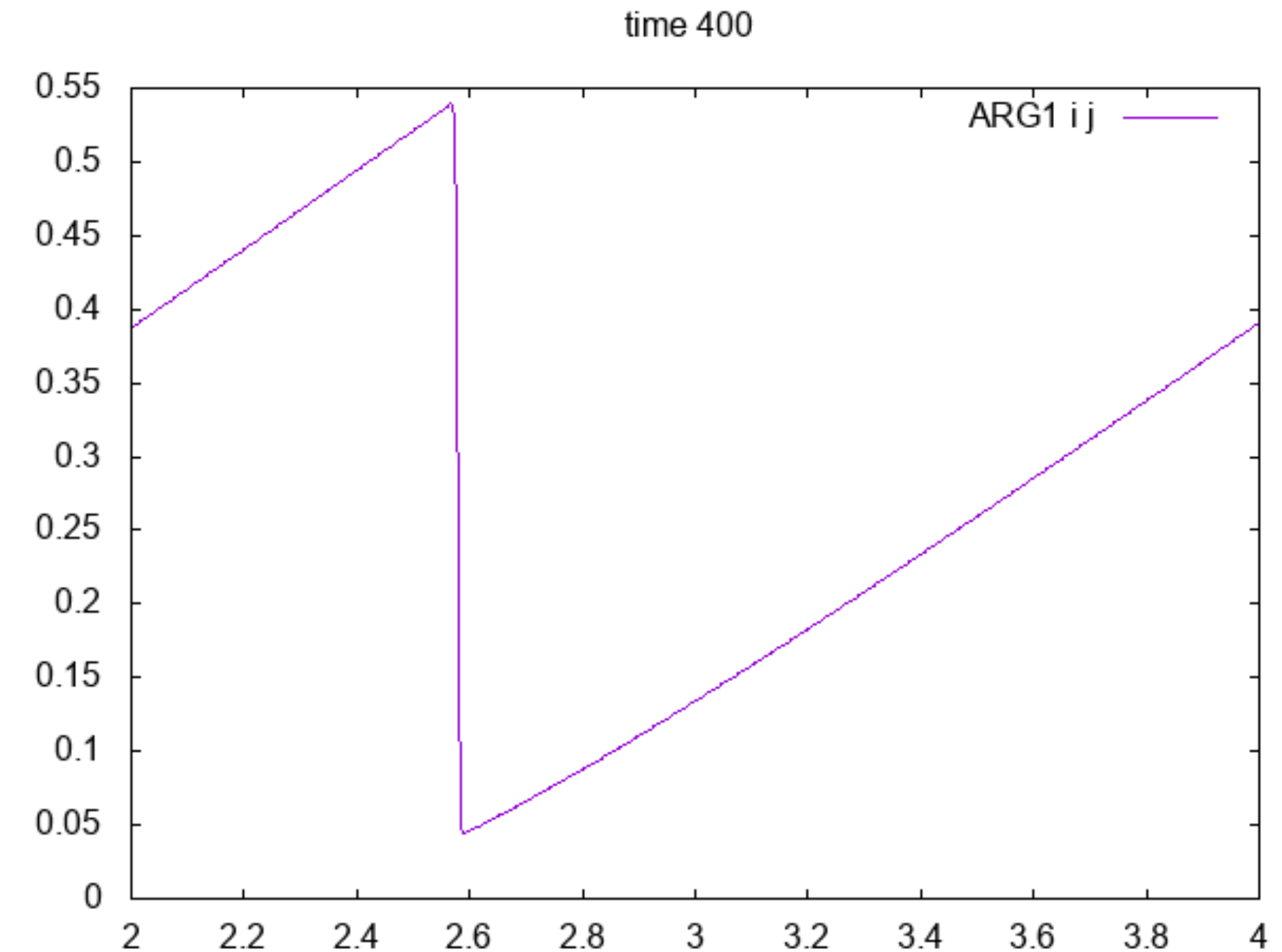
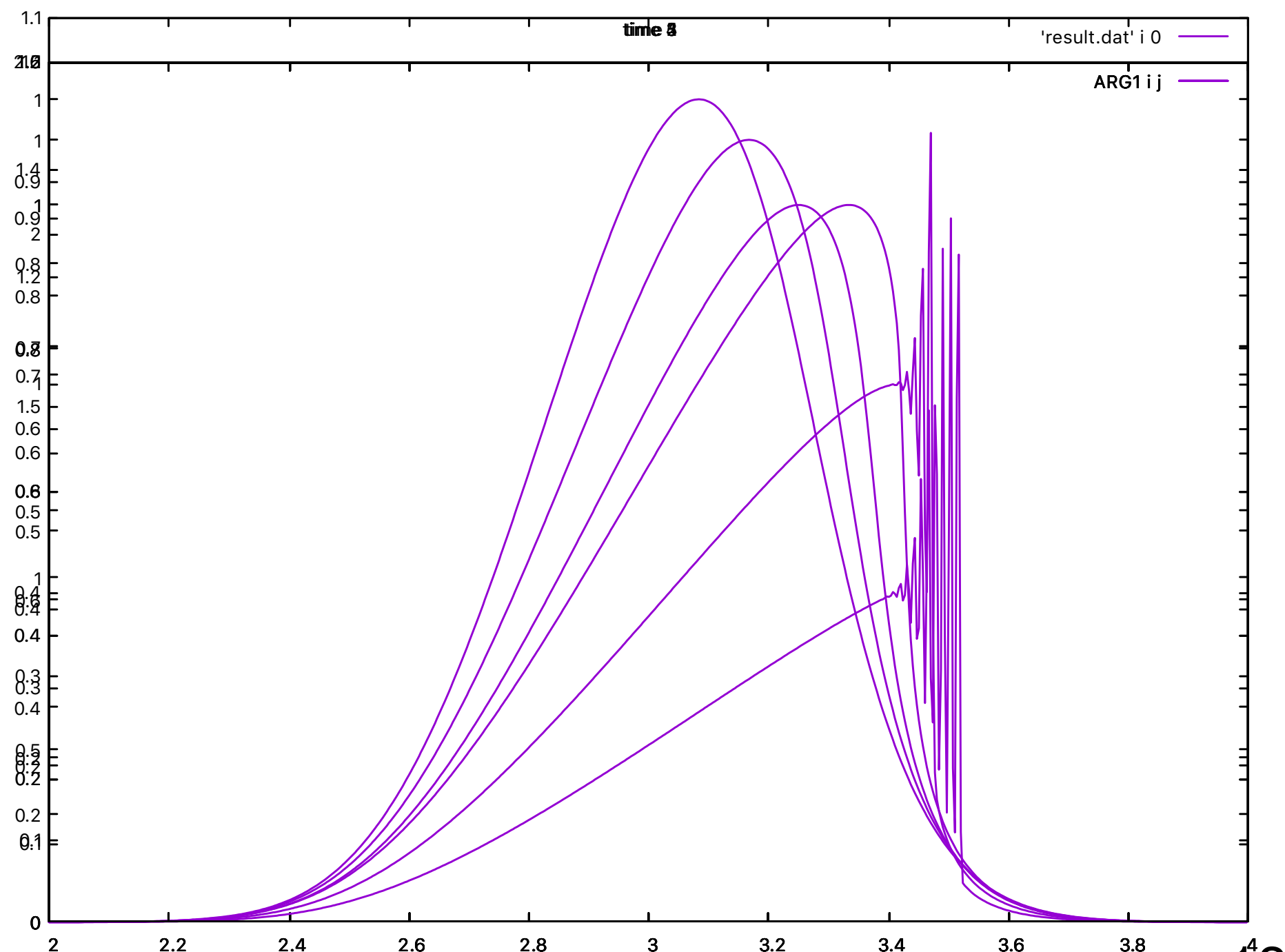
$$u = h(p)$$

$$p = x - ut$$

$$\partial_t u + \frac{1}{2} \partial_x u^2 = 0$$

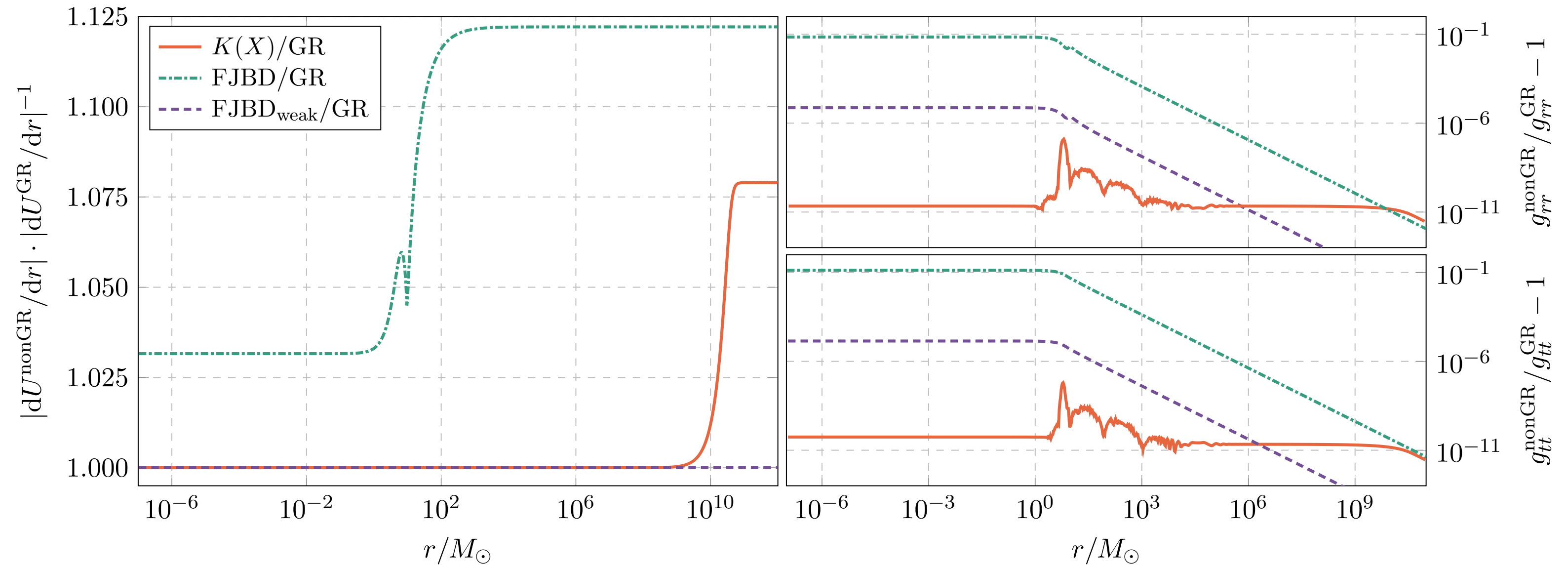
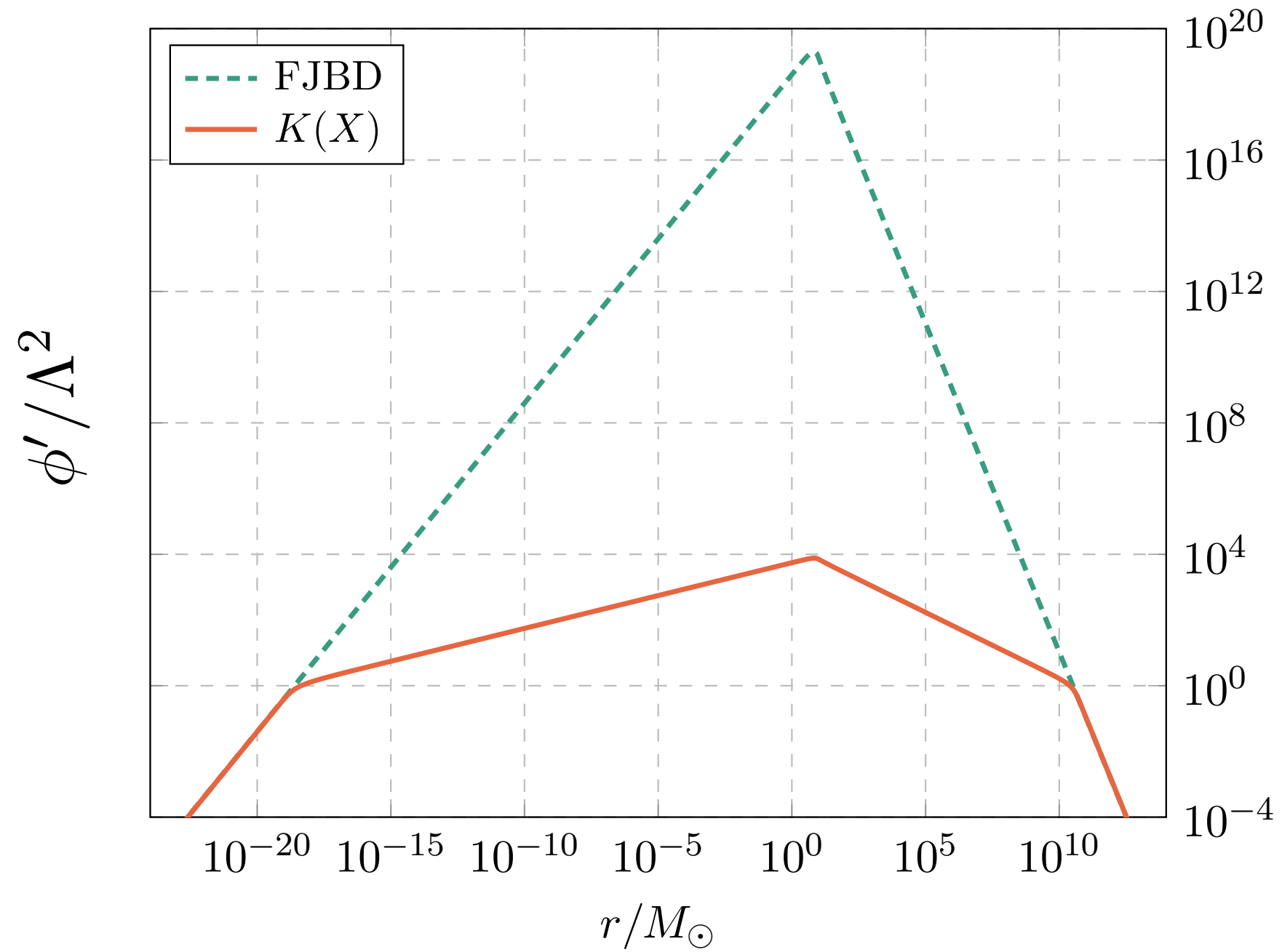
Finite difference

HRSC



Screened NS

Initial data: TOV solution

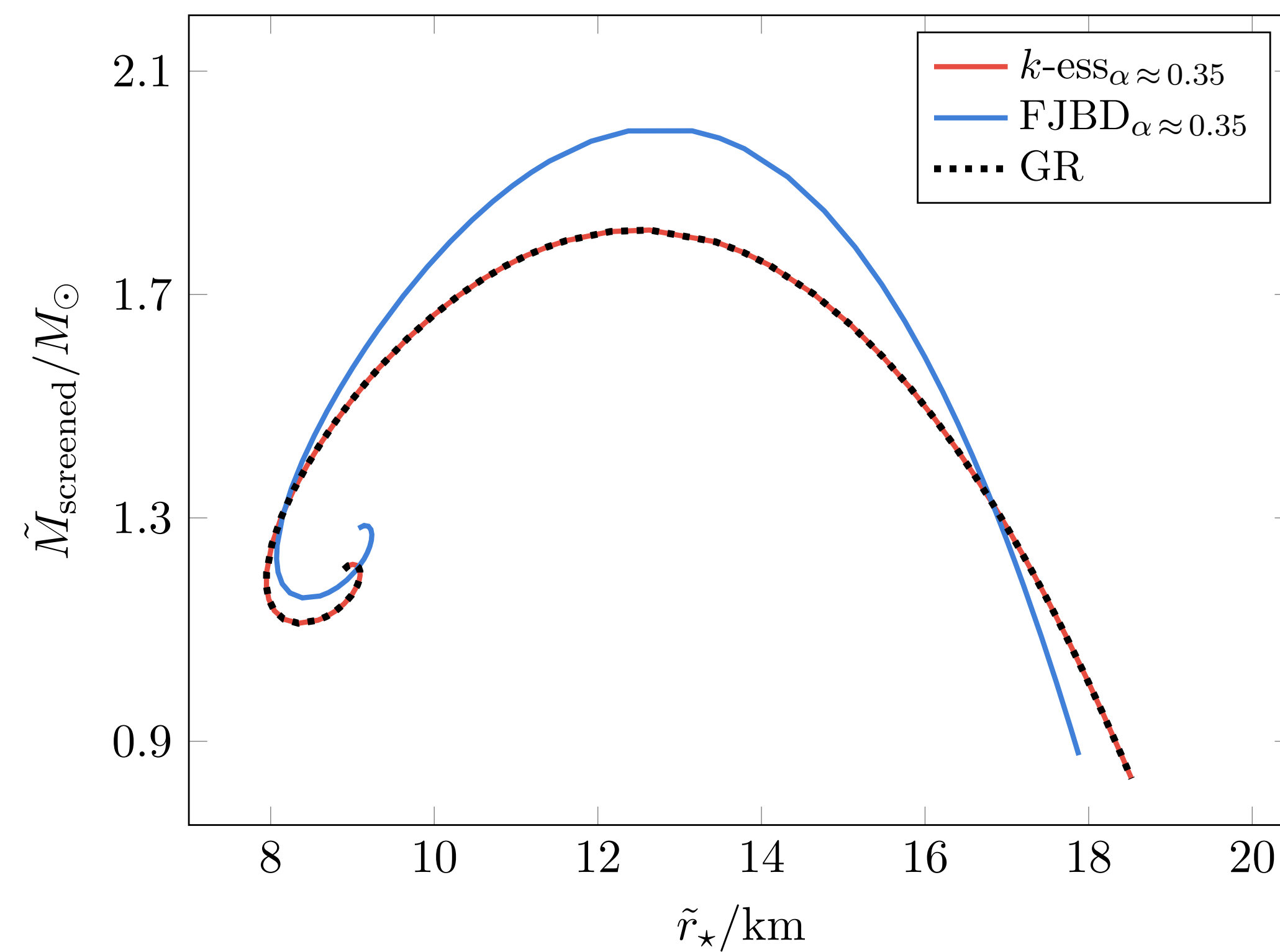
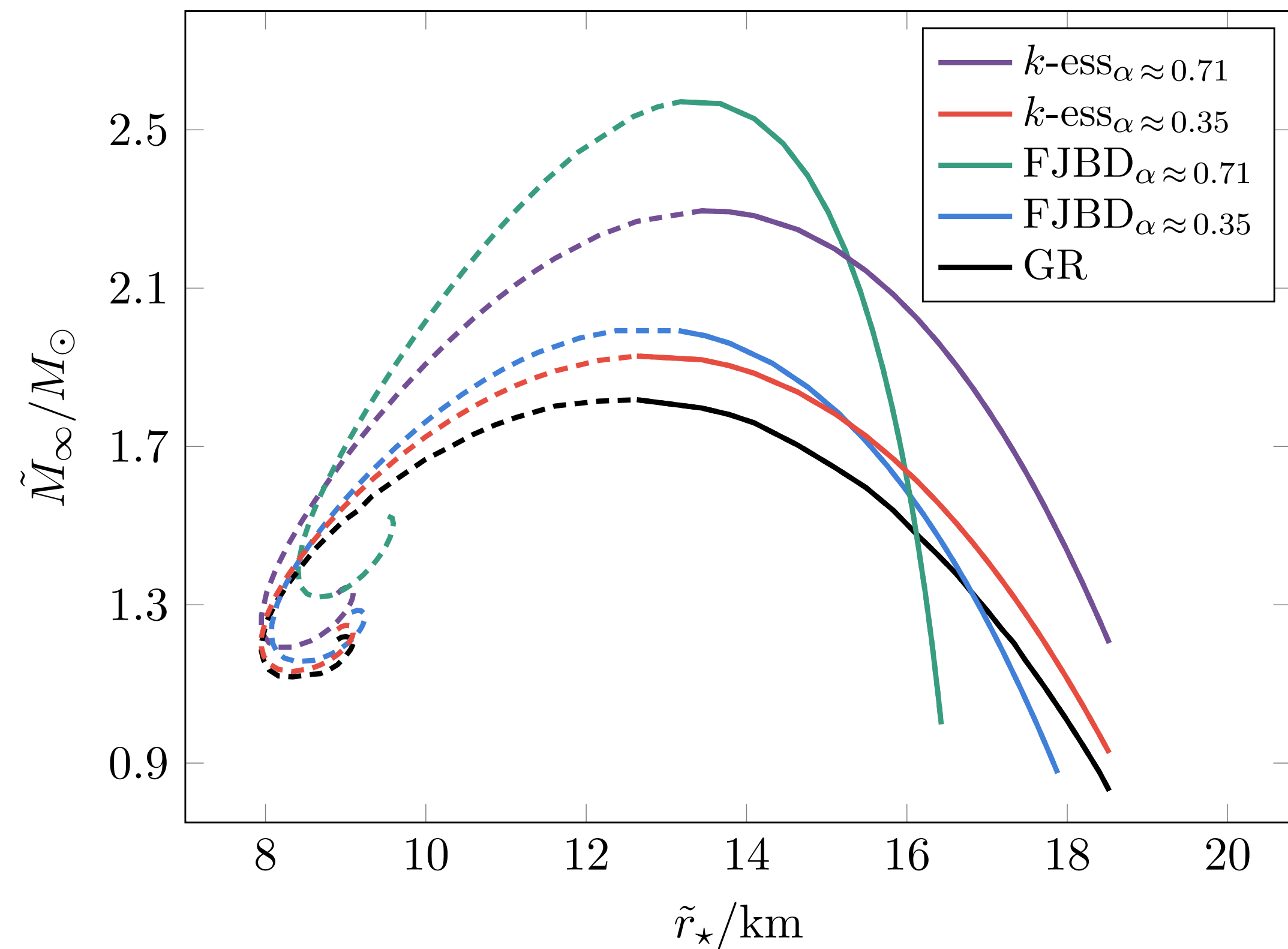


$$\gamma^{\text{PPN}} - 1 = (-2.98 \pm 1.38) \times 10^{-12},$$

$$\beta^{\text{PPN}} - 1 = (1.10 \pm 0.764) \times 10^{-10},$$

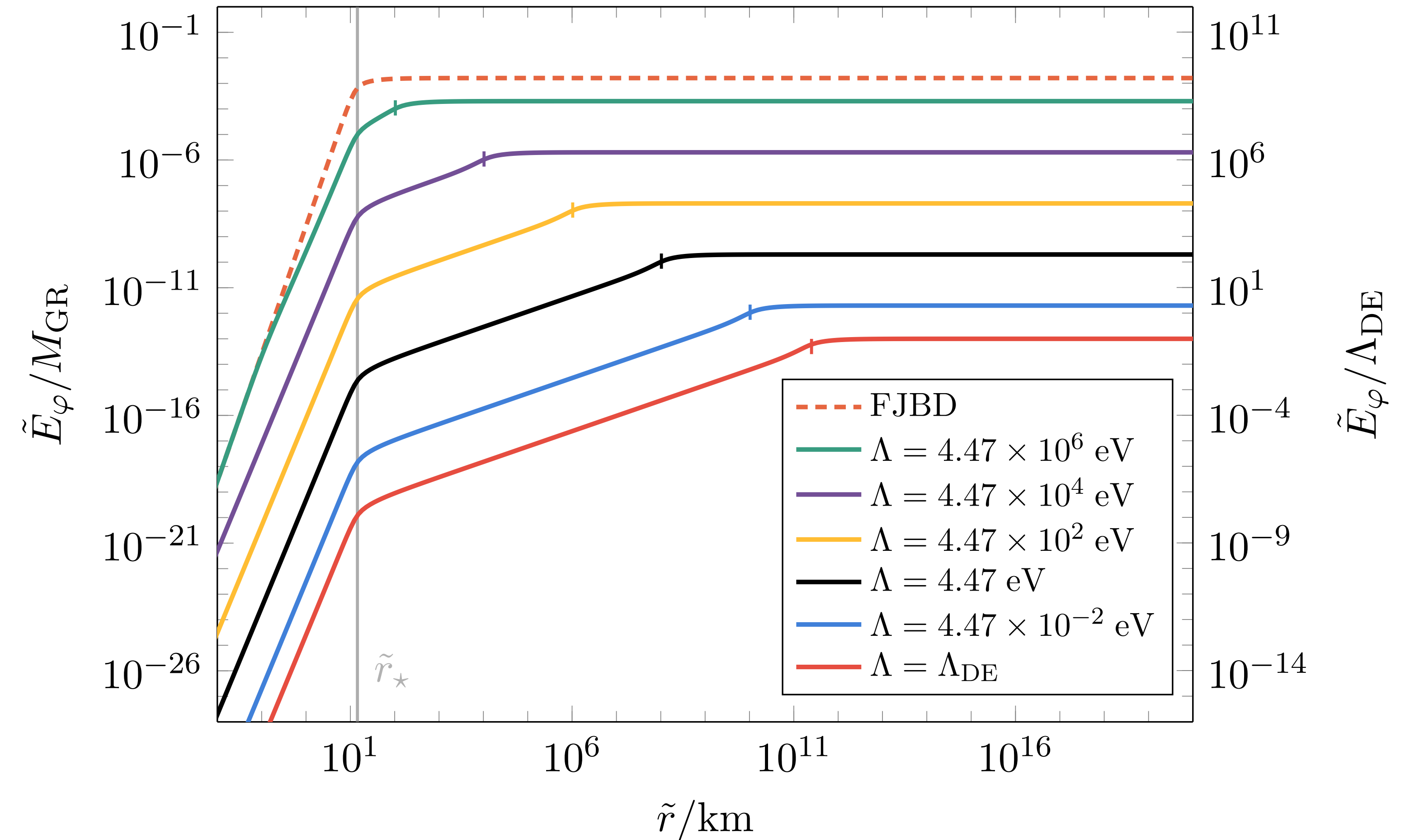
Screened NS

Mass-Radius curves



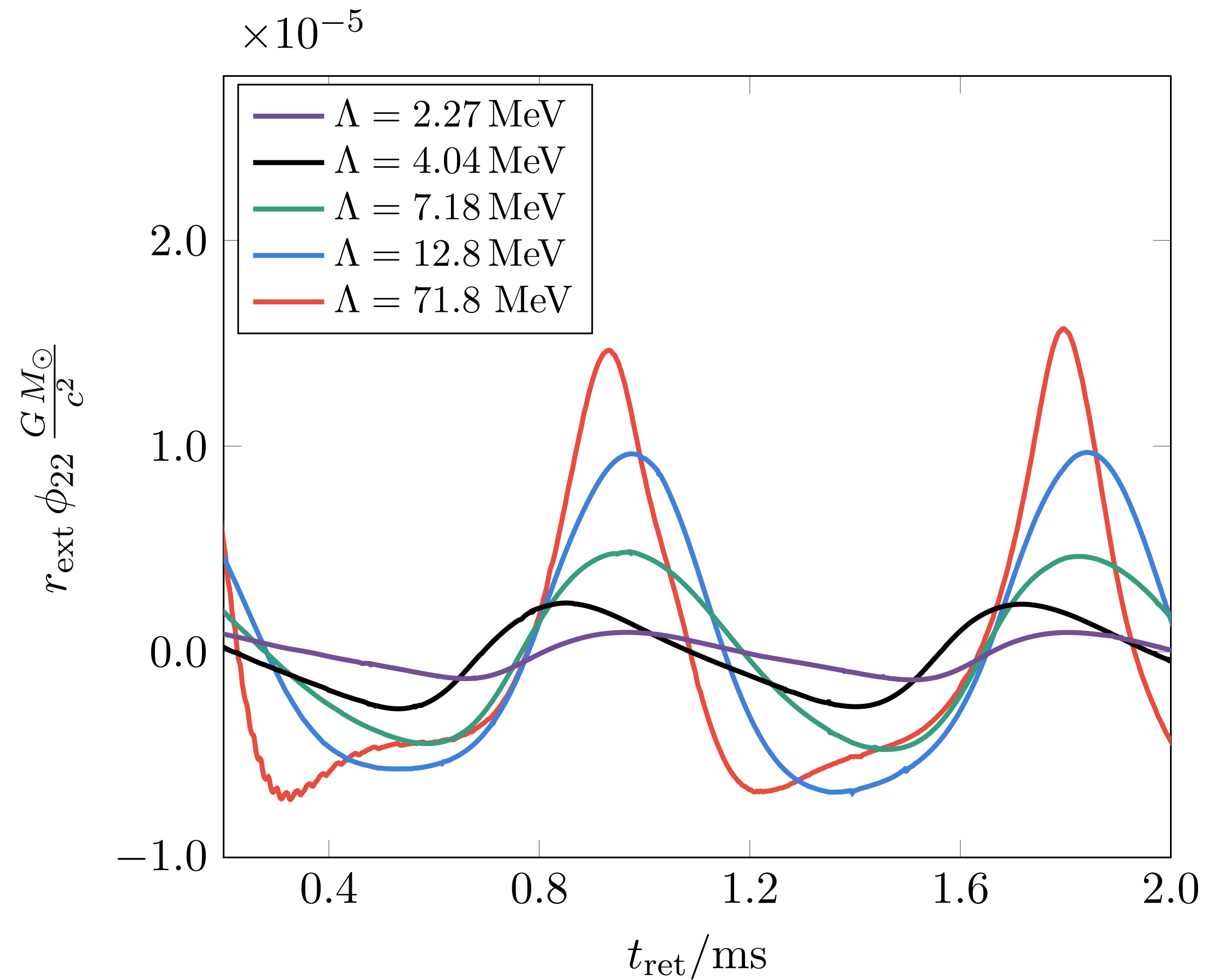
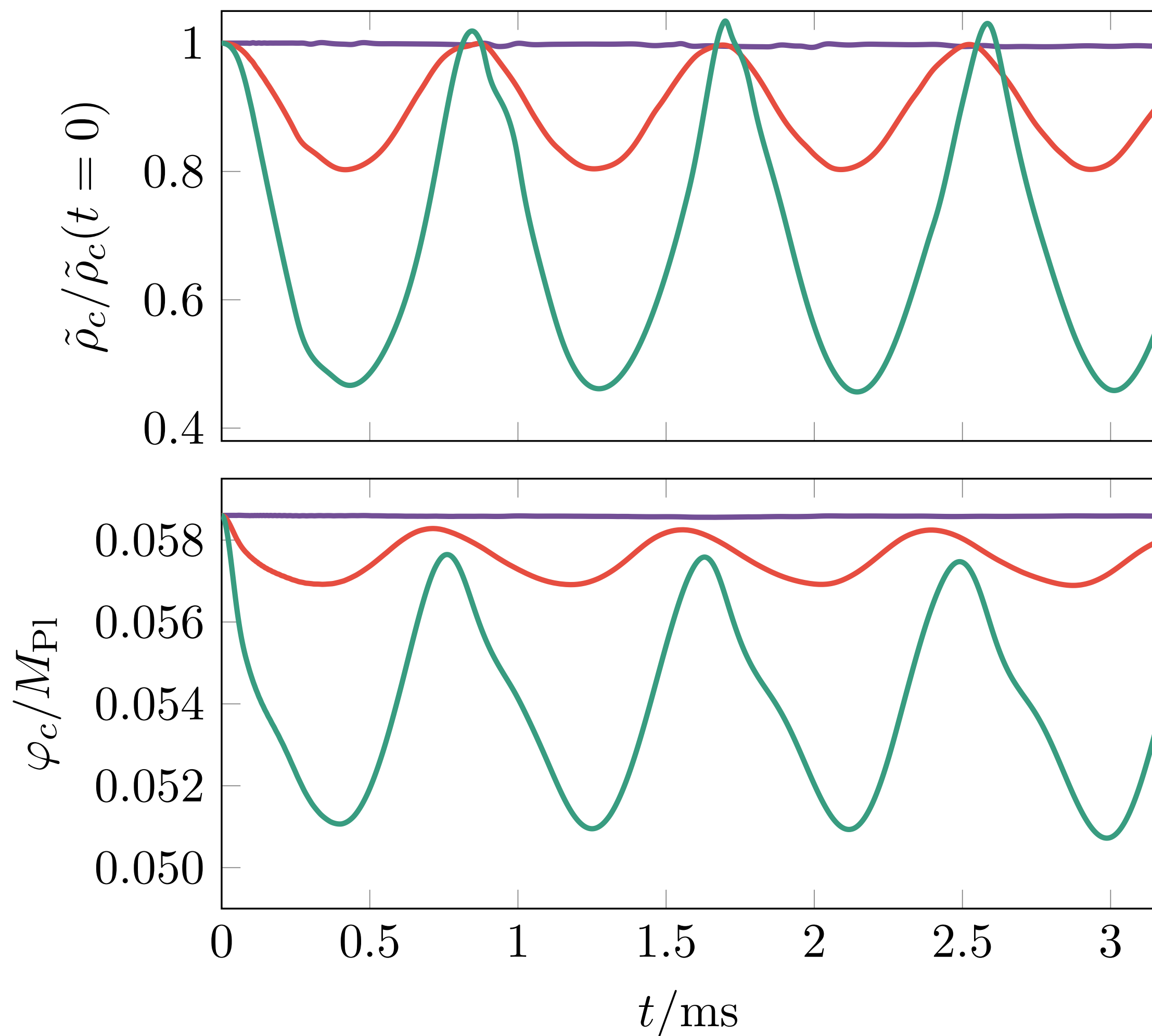
Screened NS

Scalar field energy



Dynamics of Screened NS

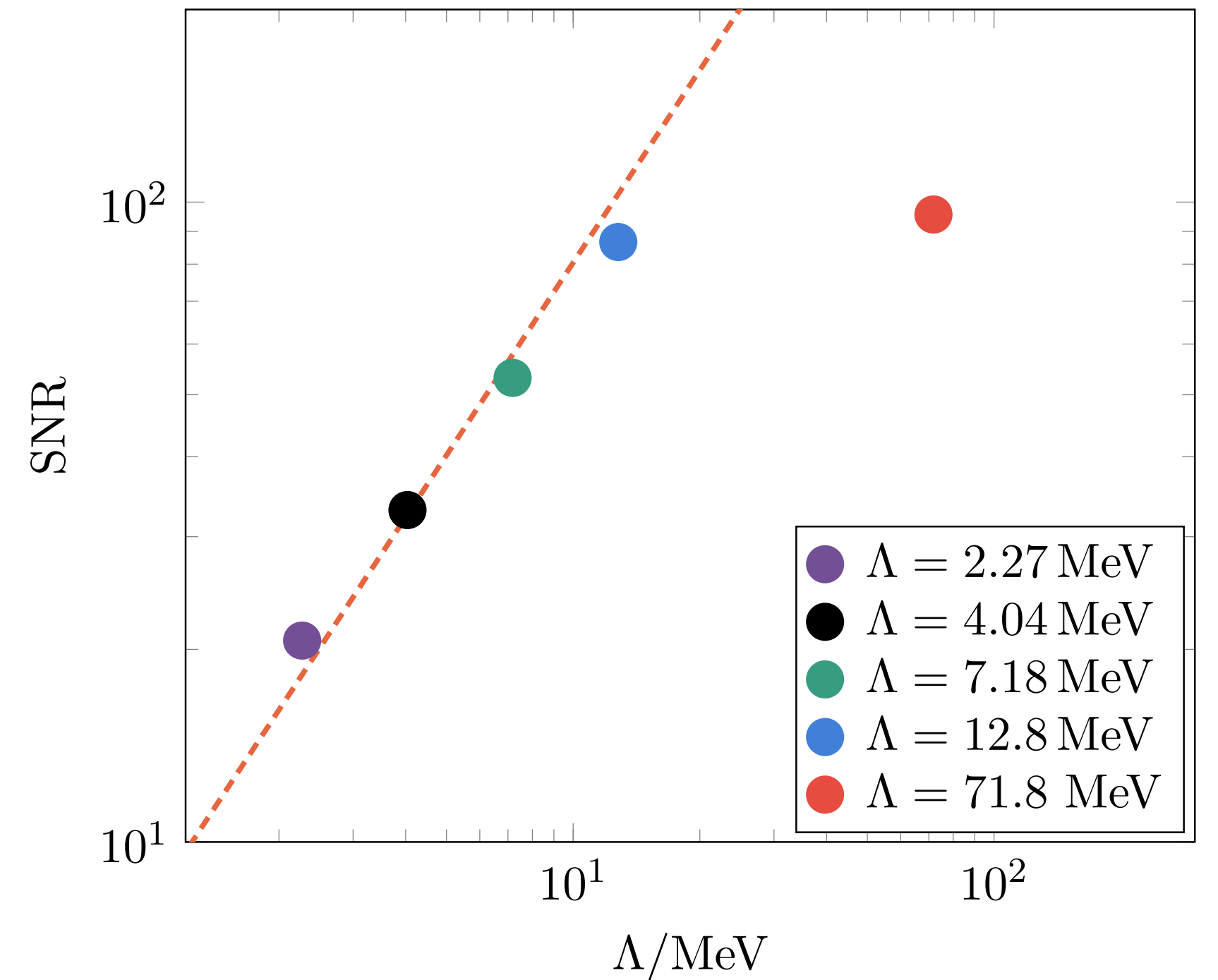
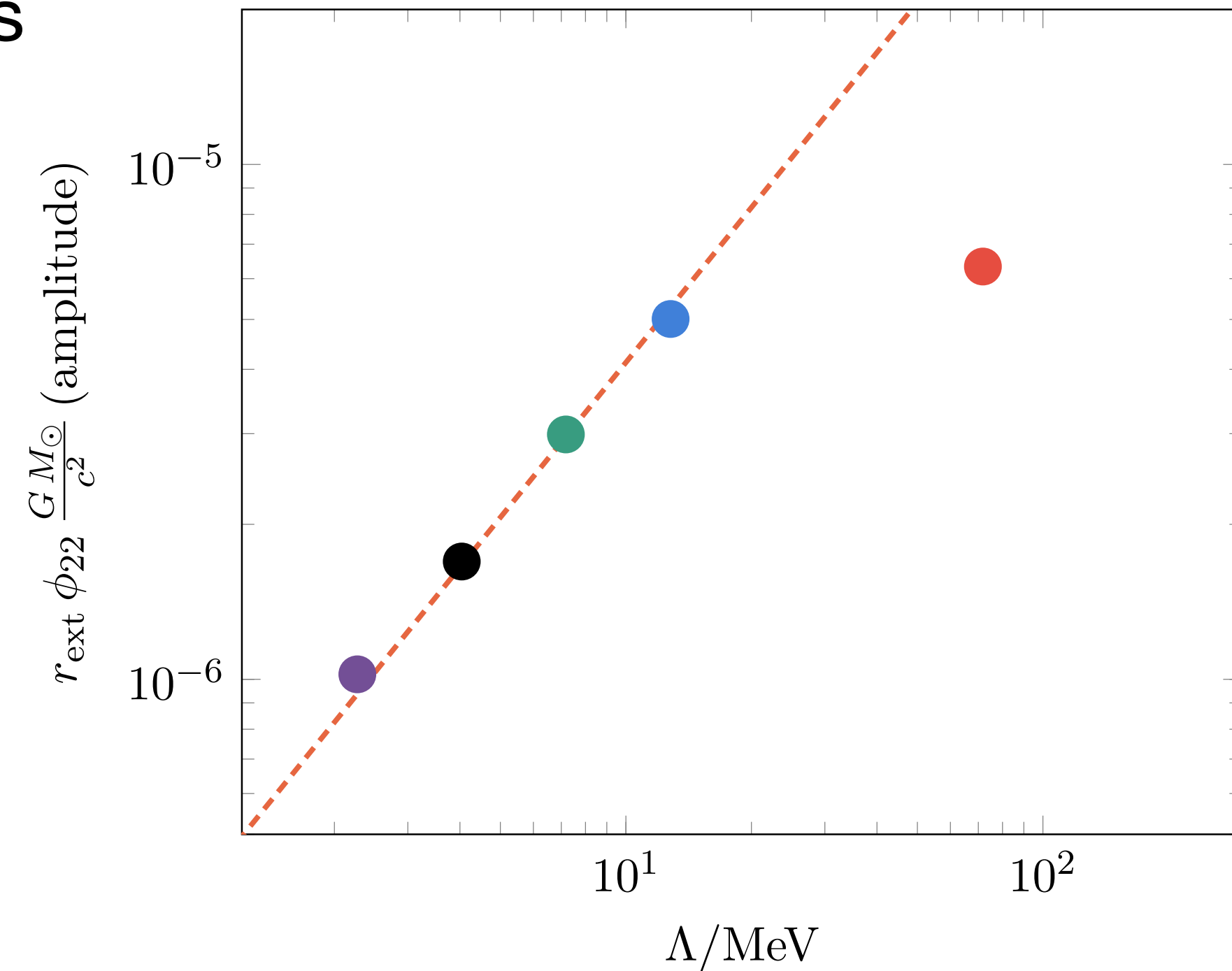
Evolution: stellar oscillations



$$\phi_{22} \simeq -\alpha \sqrt{16\pi G} \partial_t^2 \varphi + O\left(\frac{1}{r^2}\right)$$

Dynamics of Screened NS

Evolution: stellar oscillations



$$\phi_{22} , \text{ SNR} \propto \Lambda$$

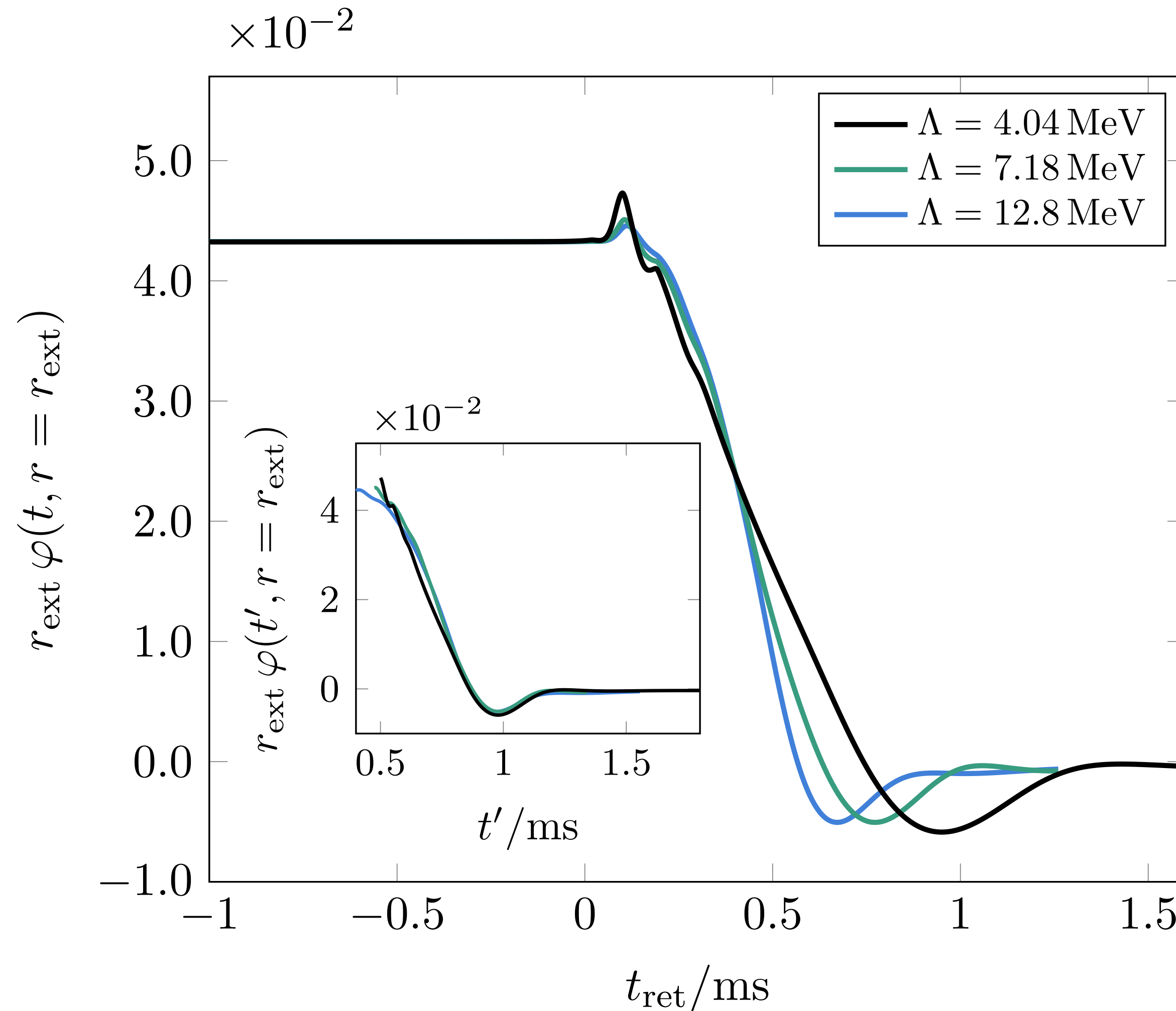
For Ad LIGO at 8 kpc

Dynamics of Screened NS

Evolution: collapse in a BH

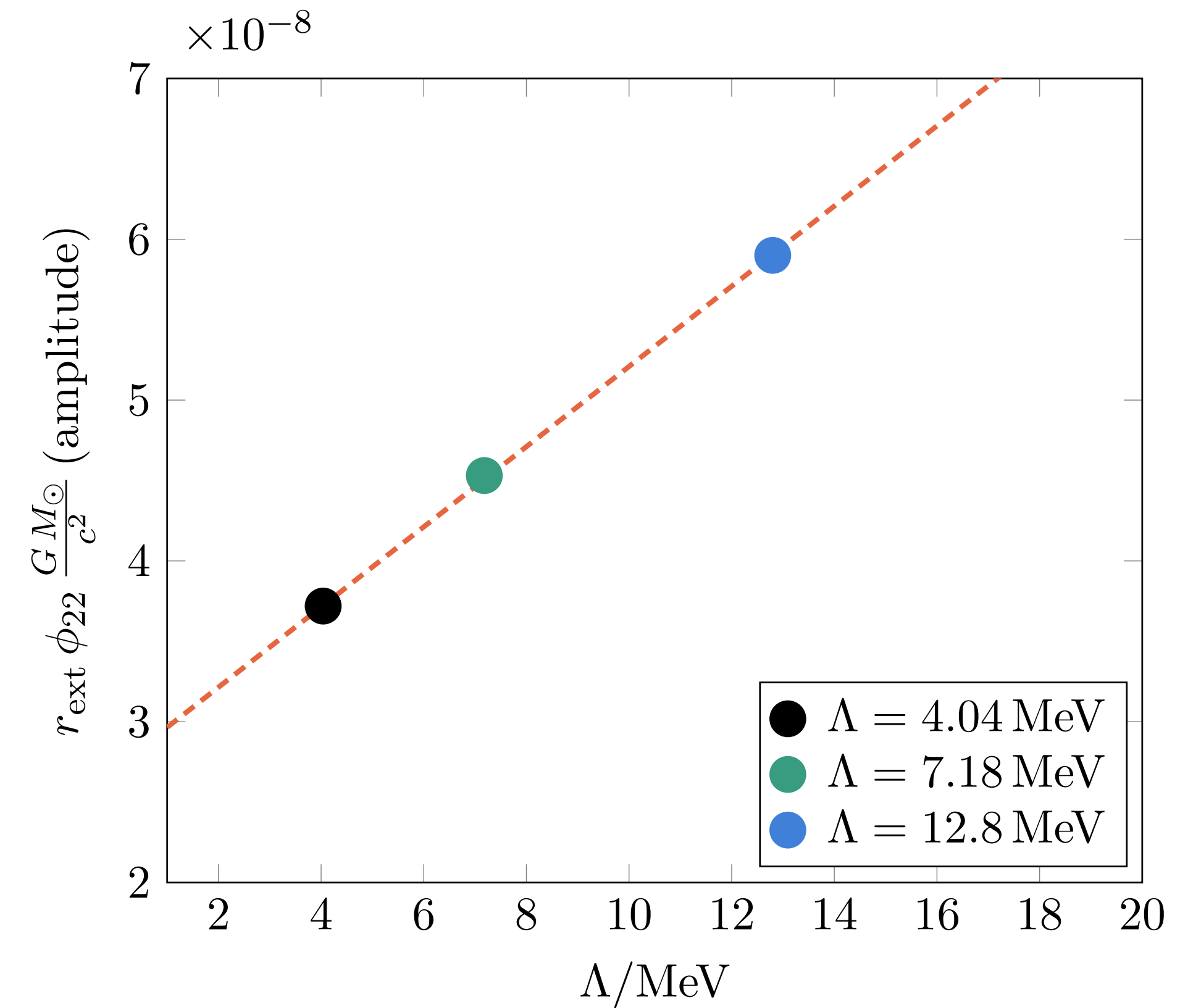
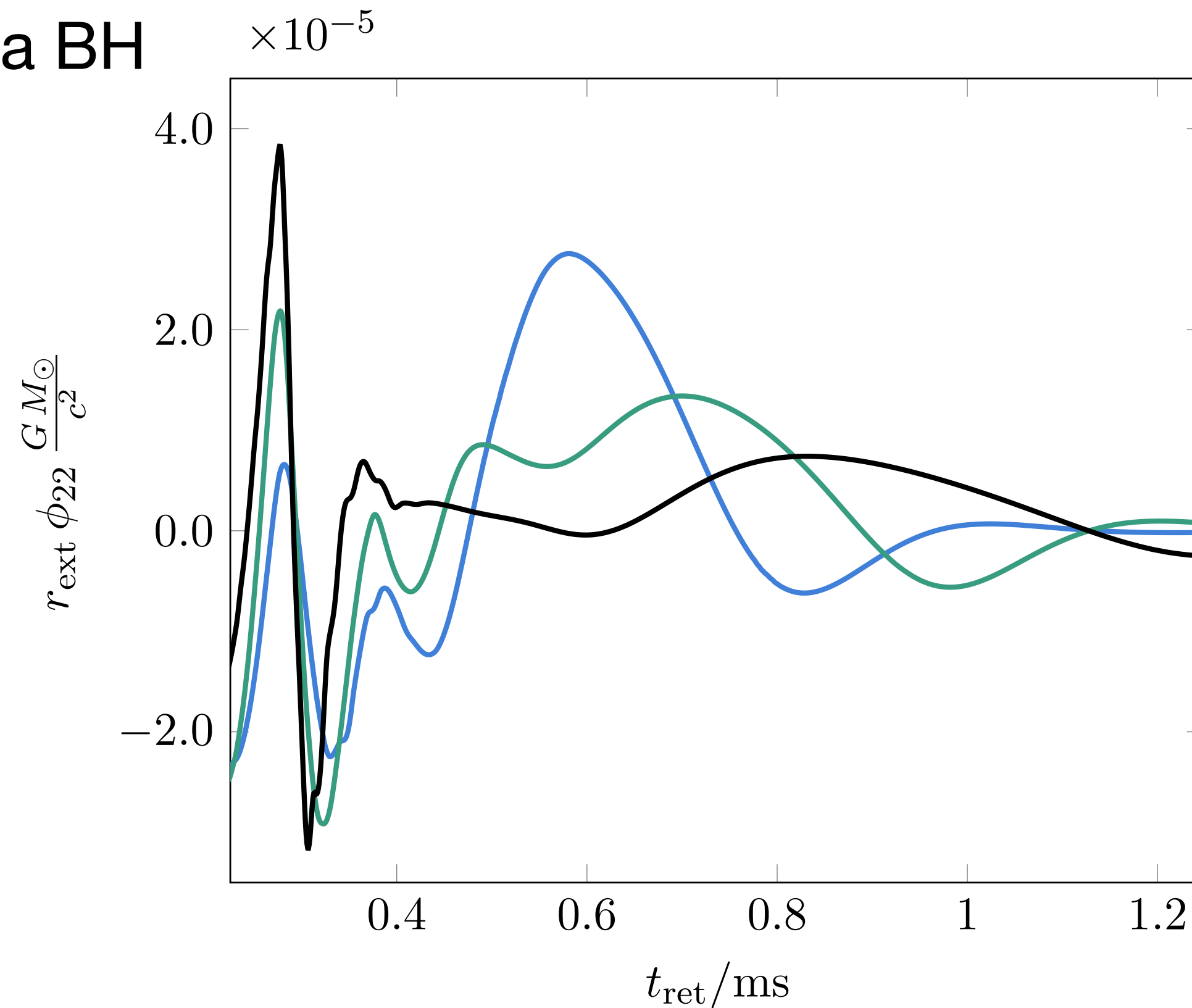
$$f \propto \sqrt{\Lambda}$$

$$\phi_{22} \propto (2\pi f)^2 \varphi \propto \Lambda$$



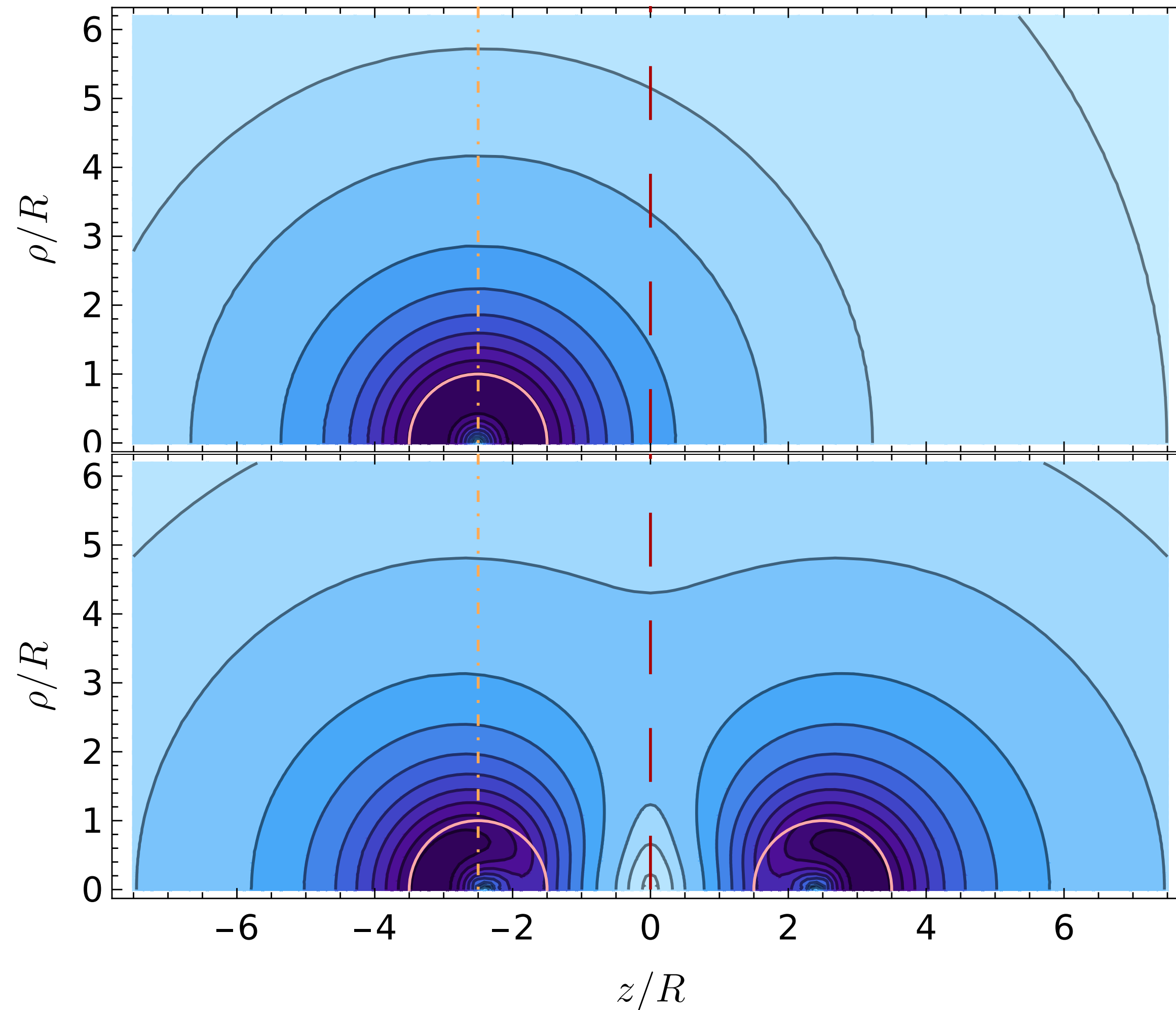
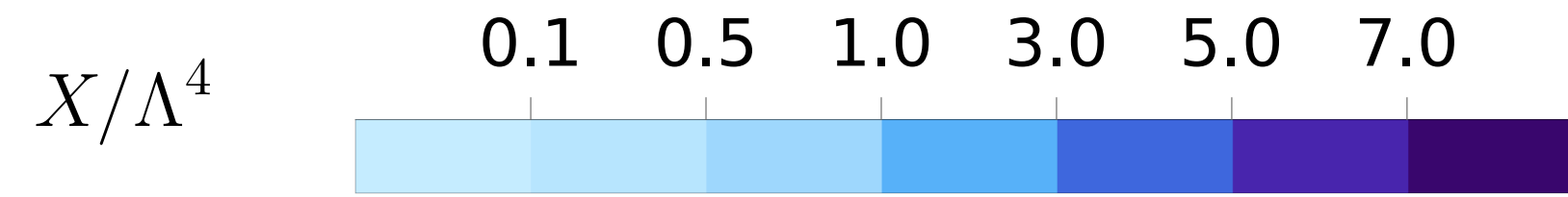
Dynamics of Screened NS

Evolution: collapse in a BH

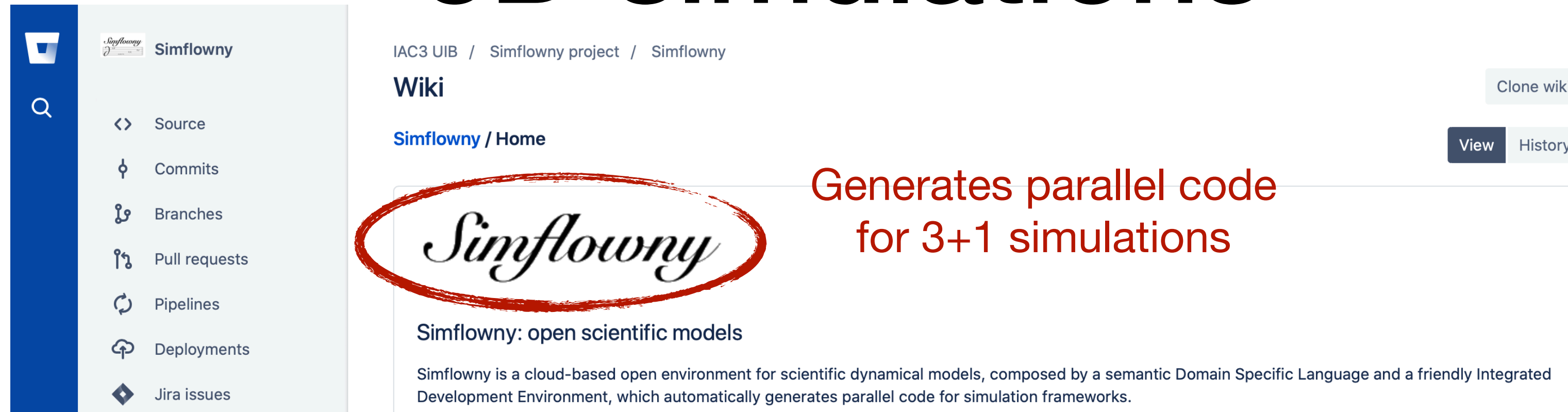


For LISA at 8 kpc, $\text{SNR}(\Lambda_{\text{DE}}) \sim 30 - 40$

2 body problem



3D simulations



IAC3 UIB / Simflowny project / Simflowny

Wiki

Clone wiki

View History

Simflowny / Home

Simflowny

Generates parallel code for 3+1 simulations

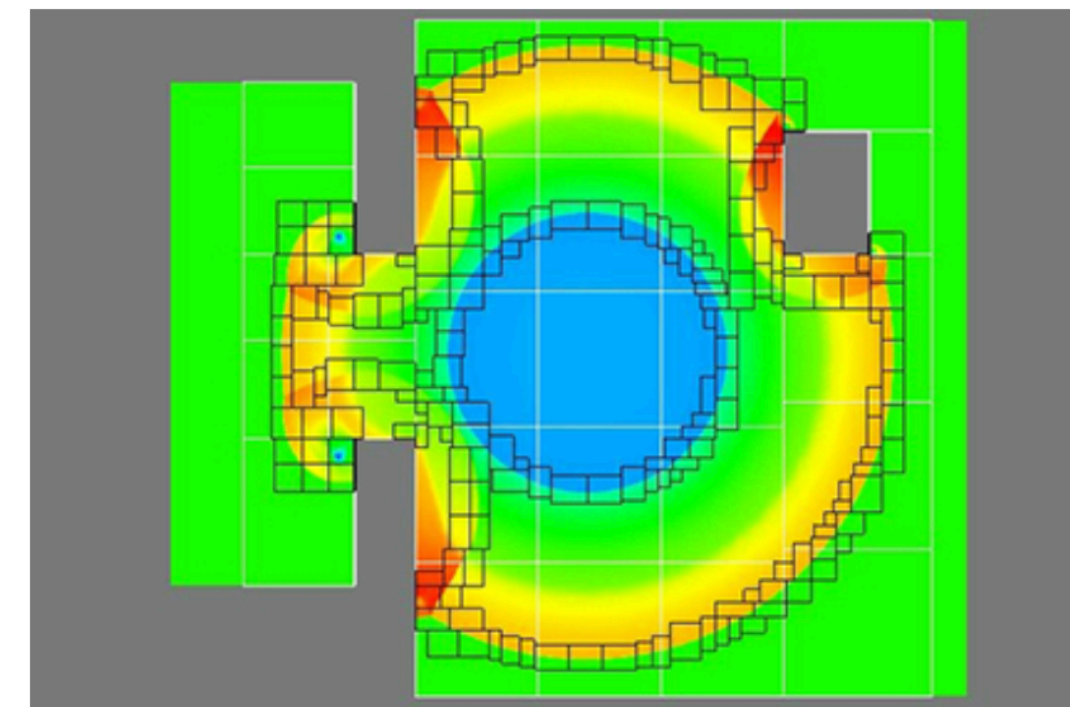
Simflowny: open scientific models

Simflowny is a cloud-based open environment for scientific dynamical models, composed by a semantic Domain Specific Language and a friendly Integrated Development Environment, which automatically generates parallel code for simulation frameworks.

SAMRAI: Structured Adaptive Mesh Refinement Application Infrastructure

AMR

Exploring application, numerical, parallel computing, and software issues associated with structured adaptive mesh refinement



LORENE

Langage Objet pour la RELativité Numérique

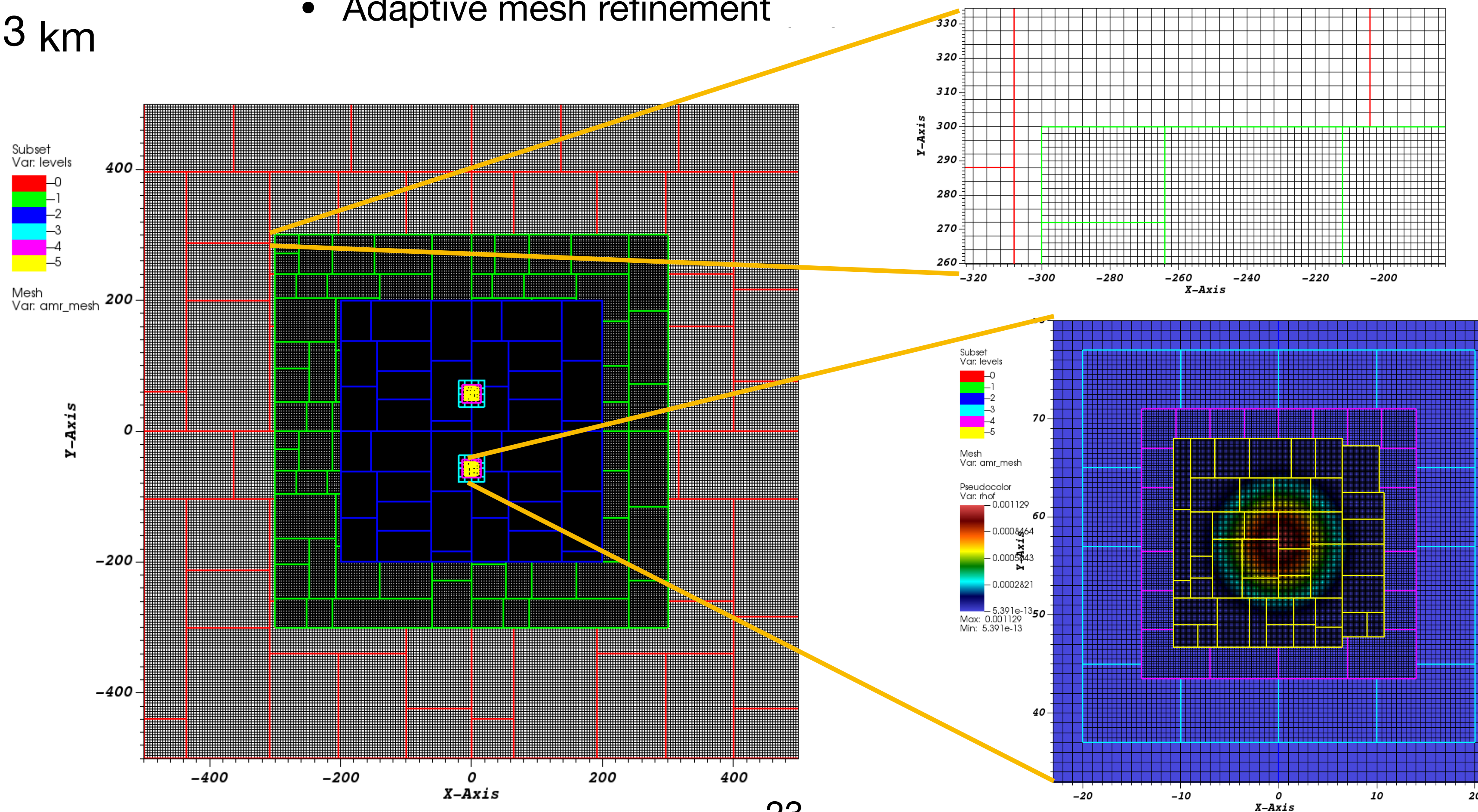
Initial Data

3D simulations

SAMRAI

- Parallelization: divide the domain in patches to be evolved in parallel in different processors → faster simulations
- Adaptive mesh refinement

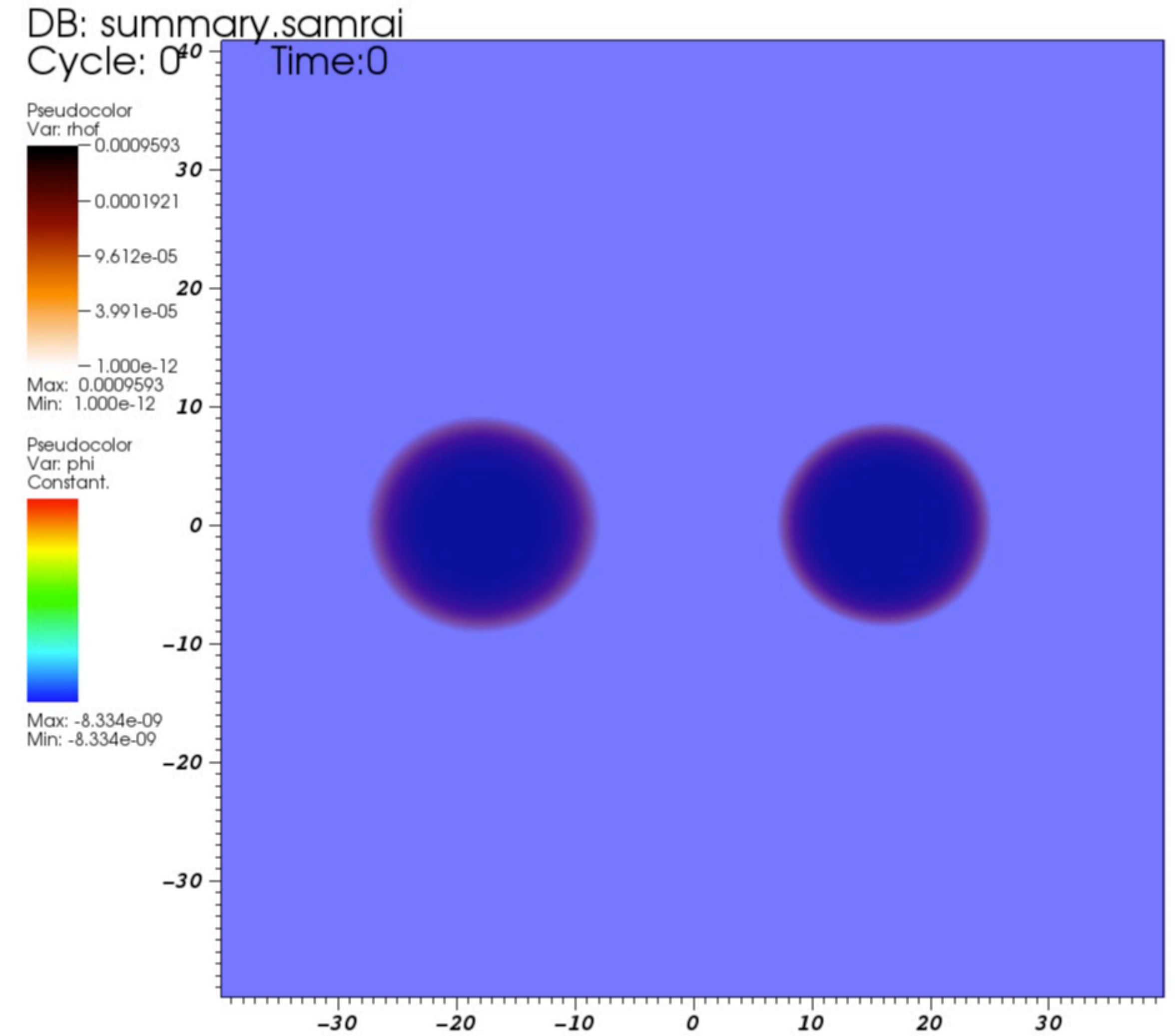
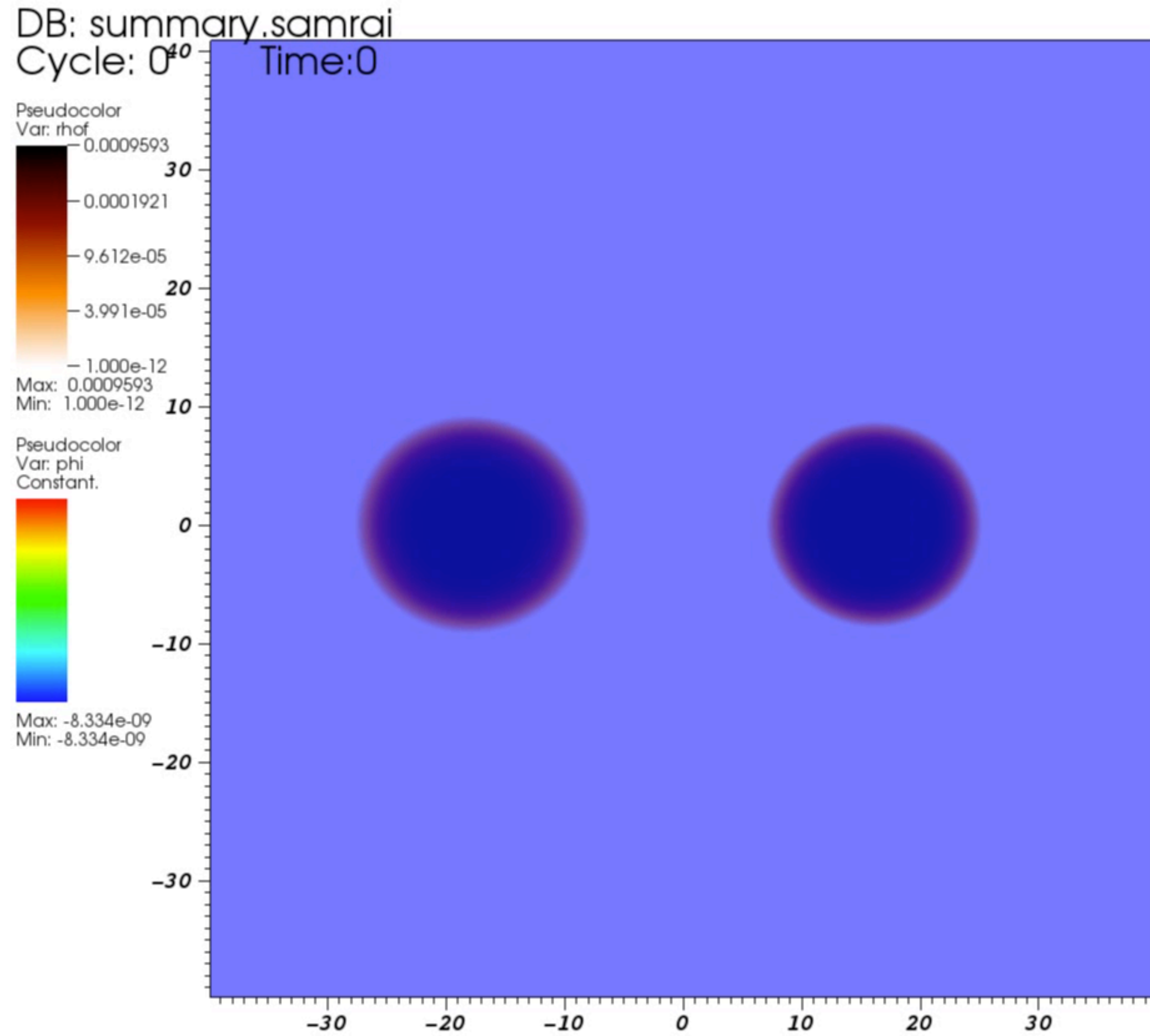
$[-1500, 1500]^3$ km



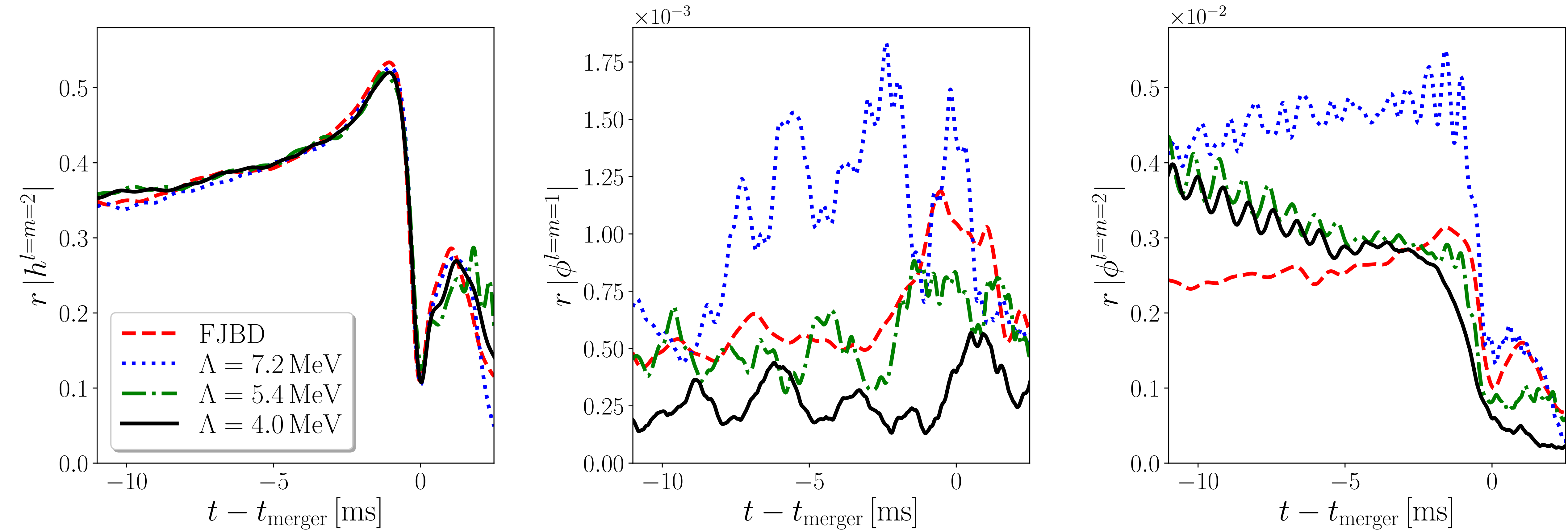
6 levels of refinement

$\Delta x = 300$ m

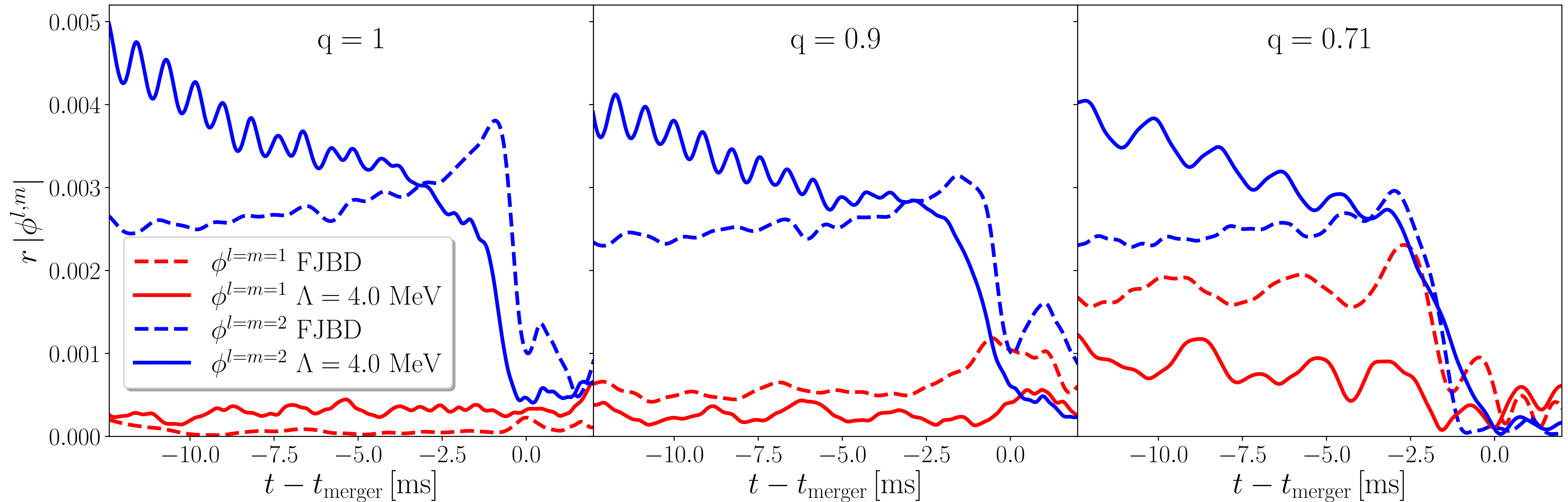
Binary NSs merger



Binary NSs merger



Binary NSs merger



Conclusions

- Screening mechanisms allow to reconcile large and short distances
- Test them in the dynamical regime of binary mergers
- Long overdue
- Interesting deviations from GR