### Converting long-range entanglement into mixture: a tensor network approach to local equilibration

Miguel Frías-Pérez arXiv: 2308.04291



#### **MAX PLANCK INSTITUTE** OF QUANTUM OPTICS

# Entanglement growth in non-equilibrium scenarios limits the applicability of TN

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Hinders simulations that could resolve both fundamental and practical questions

**Entanglement barrier** 

White and Feiguin, 2004 Vidal, 2004 Haegeman et al., 2011

Unitary evolution  $U(t) = e^{-iHt}$ 

Low entangled state or operator

t=0  $t=\infty$ 

#### Entanglement barrier

White and Feiguin, 2004 Vidal, 2004 Haegeman et al., 2011

Unitary evolution  $U(t) = e^{-iHt}$ 

Low entangled state or operator

Simple macroscopic behavior

$$t=0$$
  $t=\infty$ 

Entanglement barrier: global quench

White and Feiguin, 2004 Vidal, 2004 Haegeman et al., 2011

Unitary evolution  $U(t) = e^{-iHt}$ 

Product state

Thermal reduced density matrices

t=0  $t=\infty$ 



Calabrese and Cardy, 2005

#### Quasiparticle picture



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 $\left|\phi^{+}\right\rangle = \frac{1}{\sqrt{2}} \left(\left|00\right\rangle + \left|11\right\rangle\right)$ 

#### Quasiparticle picture



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Long-range entanglement decoupling (integrable)

$$H = -\sum_{n} \left( \sigma_{n}^{z} \sigma_{n+1}^{z} + g \sigma_{n}^{x} \right)$$

t

9

Long-range entanglement decoupling (integrable)

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Long-range entanglement decoupling (non-integrable)

$$H = -\sum_{n} \left( \sigma_{n}^{z} \sigma_{n+1}^{z} + g \sigma_{n}^{x} + J_{2} \sigma_{n}^{z} \sigma_{n+2}^{z} \right)$$

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Long-range entanglement decoupling (non-integrable)

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#### Mixing the long-range degrees of freedom



Fast degrees of freedom contribute via their reduced density matrices to the local observables in the neighbouring blocks

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Substitute them by the product of their marginals

#### Mixing the long-range degrees of freedom



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#### **Truncation results**



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#### Improved heuristic algorithm



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The original decomposition was a constructive way to construct states that preserved the marginals. We can also variationally look for states with smaller bond dimension that preserve them.

#### Improved heuristic algorithm



such that

**Results integrable** 
$$H = -\sum_{n} (\sigma_n^z \sigma_{n+1}^z + g \sigma_n^x) \qquad g = 2$$



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**Results non-integrable** 
$$H = -\sum_n \left(\sigma_n^z \sigma_{n+1}^z + g \sigma_n^x + J_2 \sigma_n^z \sigma_{n+2}^z\right)$$
  $\begin{array}{c} g = 2\\ J_2 = 0.1 \end{array}$ 



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  $g = 2$   
 $J_2 = 0.1$ 



#### Conclusions

- We identify the long-range entanglement produced after a quantum quench and propose a technique to convert it into mixture
- Our approach is inspired by the intuitive understanding of entanglement dynamics in terms of the radiation of quasiparticles
- We have generalized our intuition to an algorithm that goes beyond the quasiparticle regime

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## Thank you for your attention!





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