



# Weak Lensing Cosmology

Hironao Miyatake  
KMI, Nagoya University

# Outline

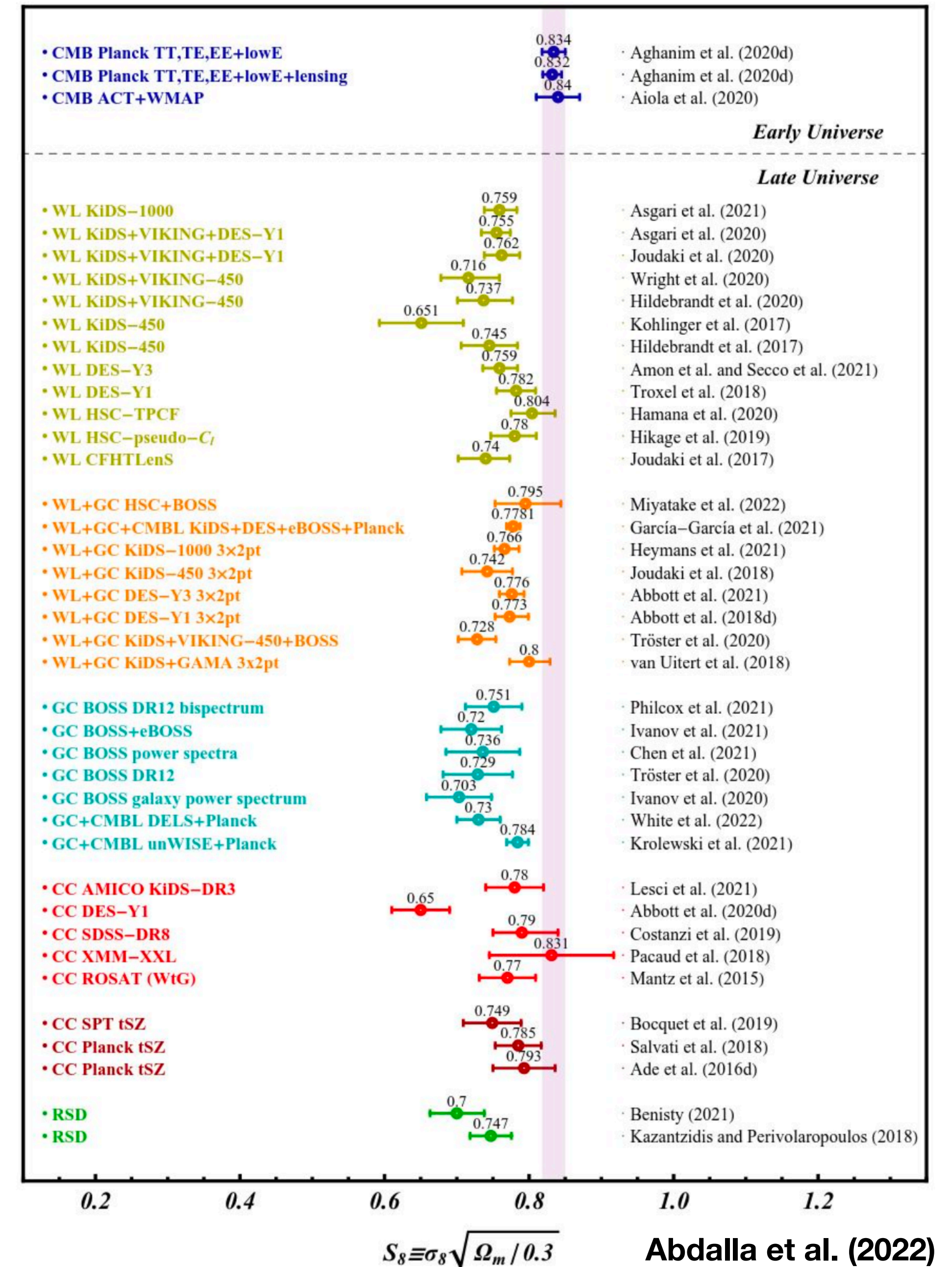
- $S_8$  tension and weak lensing surveys
- Review of Stage-III survey results (**biased towards HSC!**)
  - Differences in analysis choices
  - Approaches for systematics
    - Non-linear regime
    - redshift uncertainties
    - intrinsic alignment
    - baryonic effects
- Cosmology with CMB lensing tomography with high- $z$  galaxies

# $S_8$ Tension

$$S_8 \equiv \sigma_8 \sqrt{\Omega_m / 0.3}$$

- $\sigma_8$  : Amplitude of linear power spectrum on the scale of 8 Mpc/h
- $\Omega_m$  : Energy dense of matter (incl. dark matter)

Most **large scale structure** probes prefer smaller  $S_8$  compared to **CMB**, if we assume  $\Lambda$ CDM.

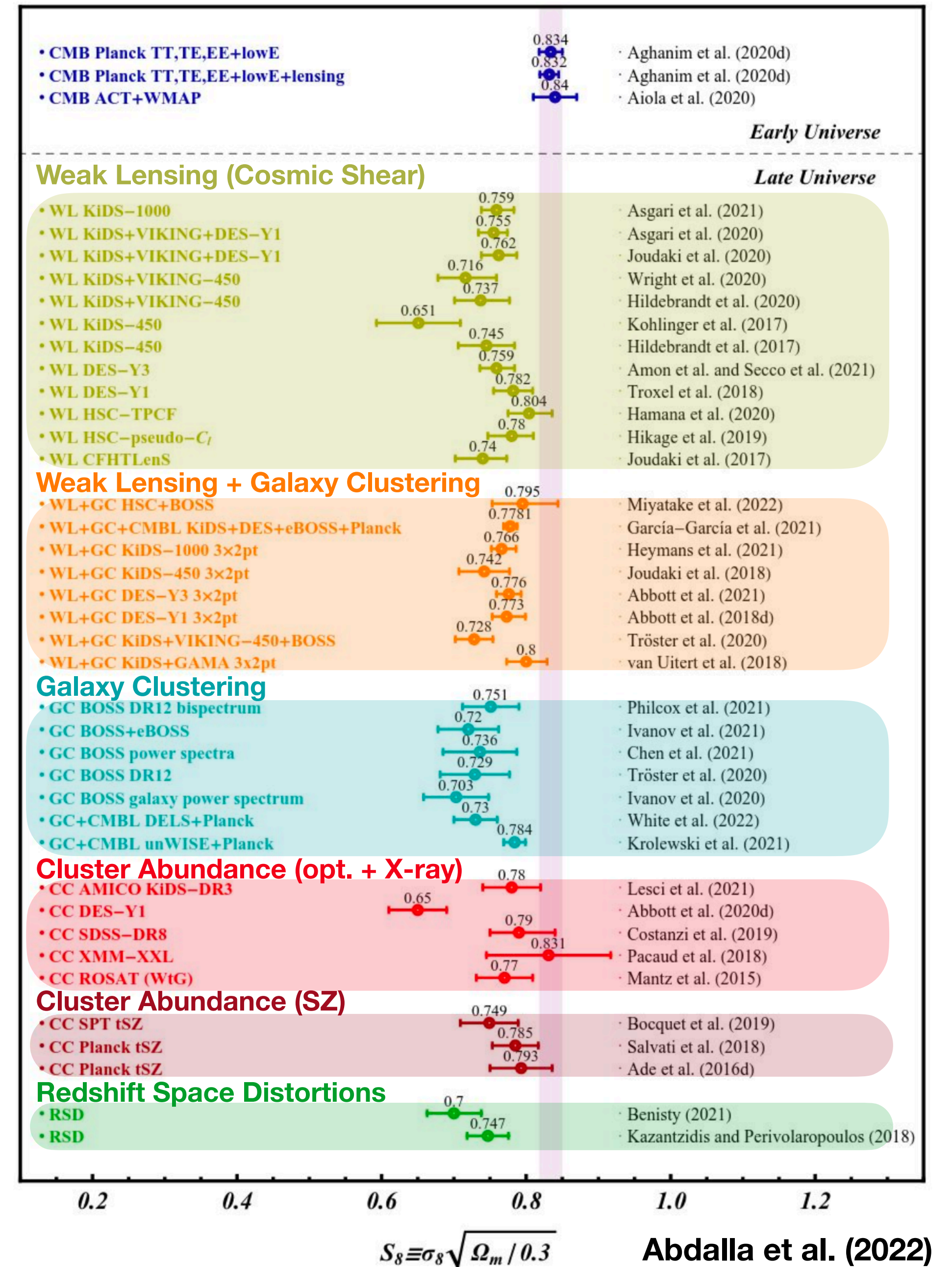


# $S_8$ Tension

$$S_8 \equiv \sigma_8 \sqrt{\Omega_m / 0.3}$$

- $\sigma_8$  : Amplitude of linear power spectrum on the scale of 8 Mpc/h
- $\Omega_m$  : Energy dense of matter (incl. dark matter)

Most **large scale structure** probes prefer smaller  $S_8$  compared to **CMB**, if we assume  $\Lambda$ CDM.

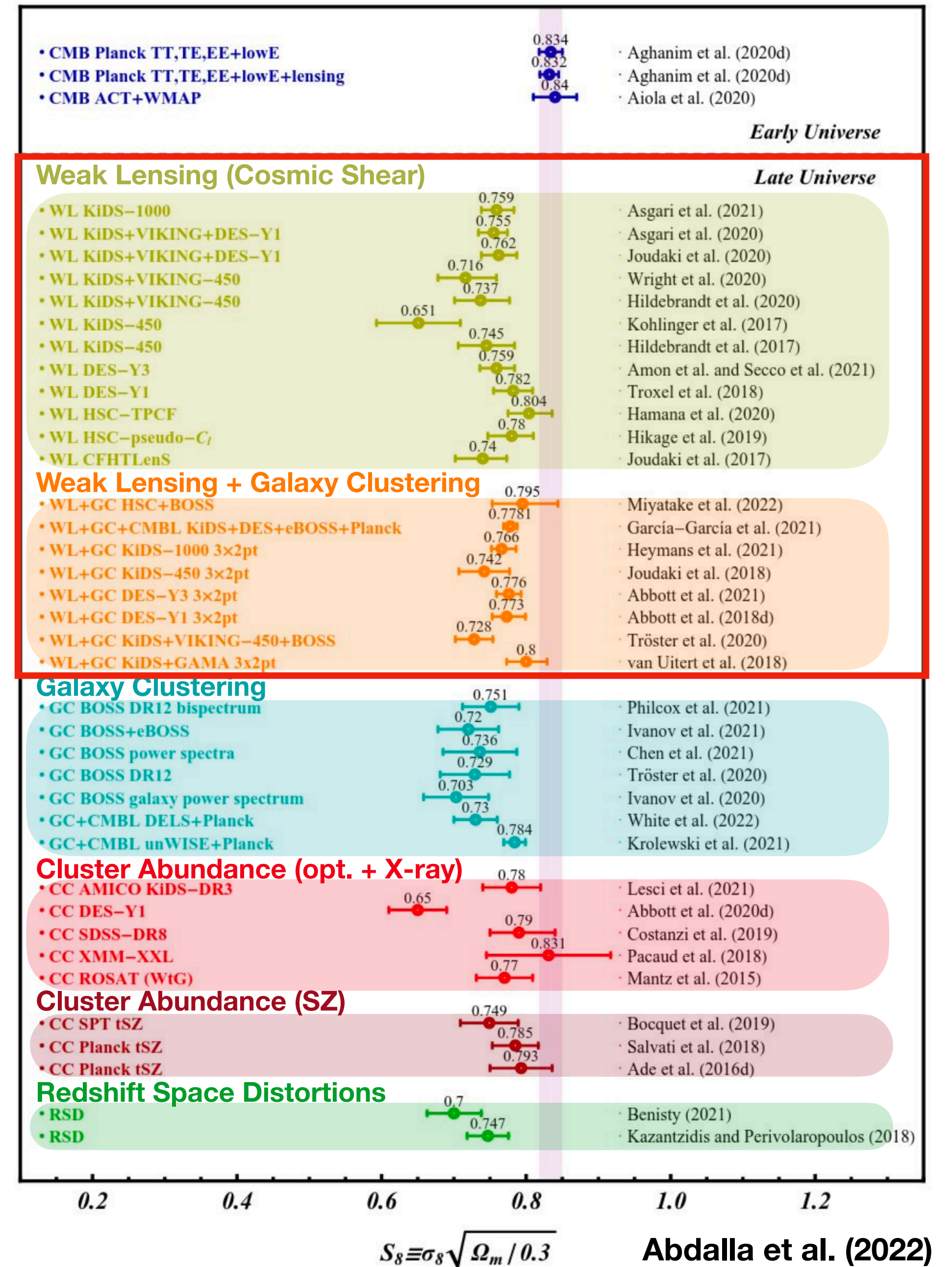


# $S_8$ Tension

$$S_8 \equiv \sigma_8 \sqrt{\Omega_m / 0.3}$$

- $\sigma_8$  : Amplitude of linear power spectrum on the scale of 8 Mpc/h
- $\Omega_m$  : Energy dense of matter (incl. dark matter)

Most **large scale structure** probes prefer smaller  $S_8$  compared to **CMB**, if we assume  $\Lambda$ CDM.

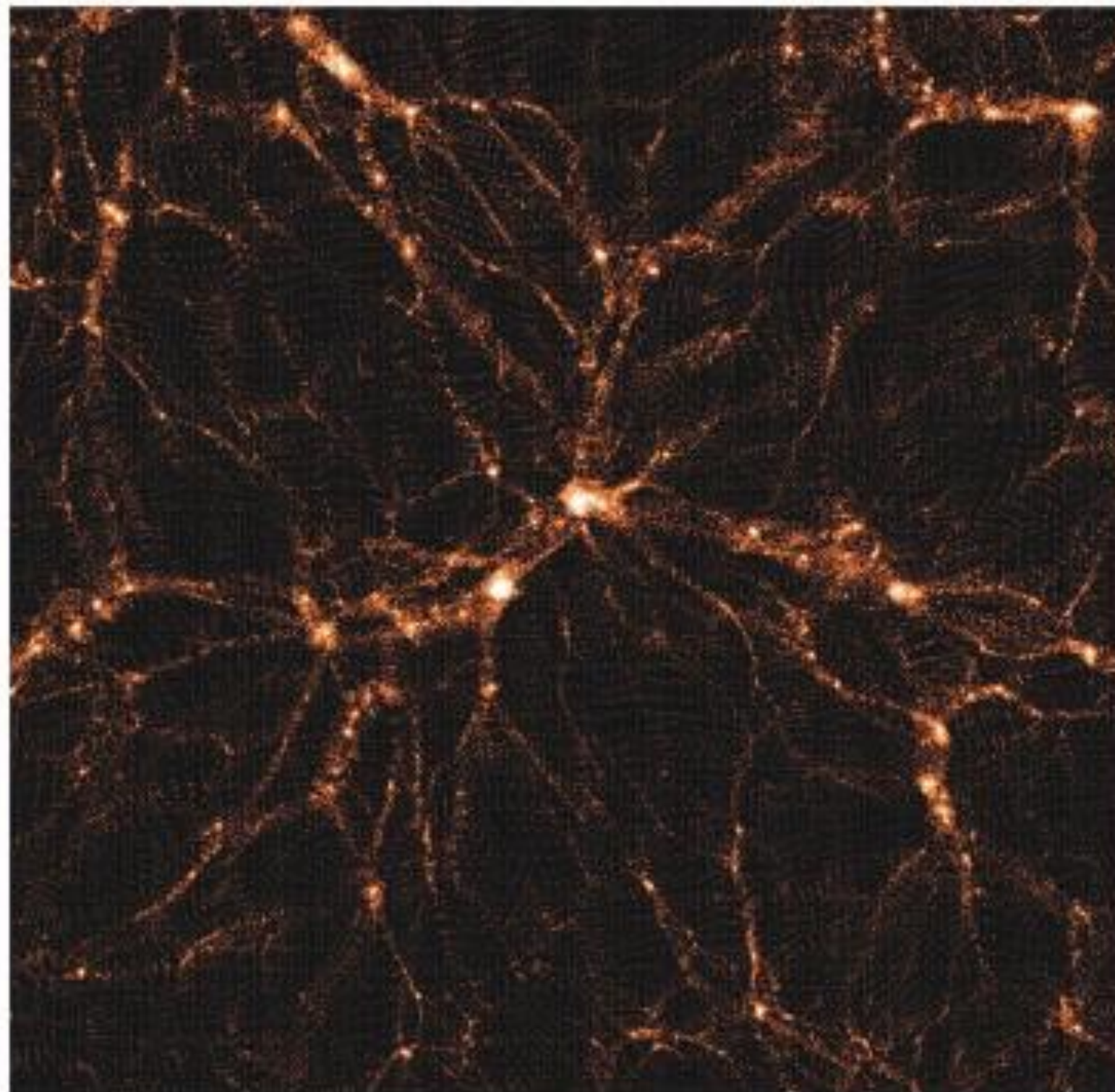


CMB

Large Scale Structure

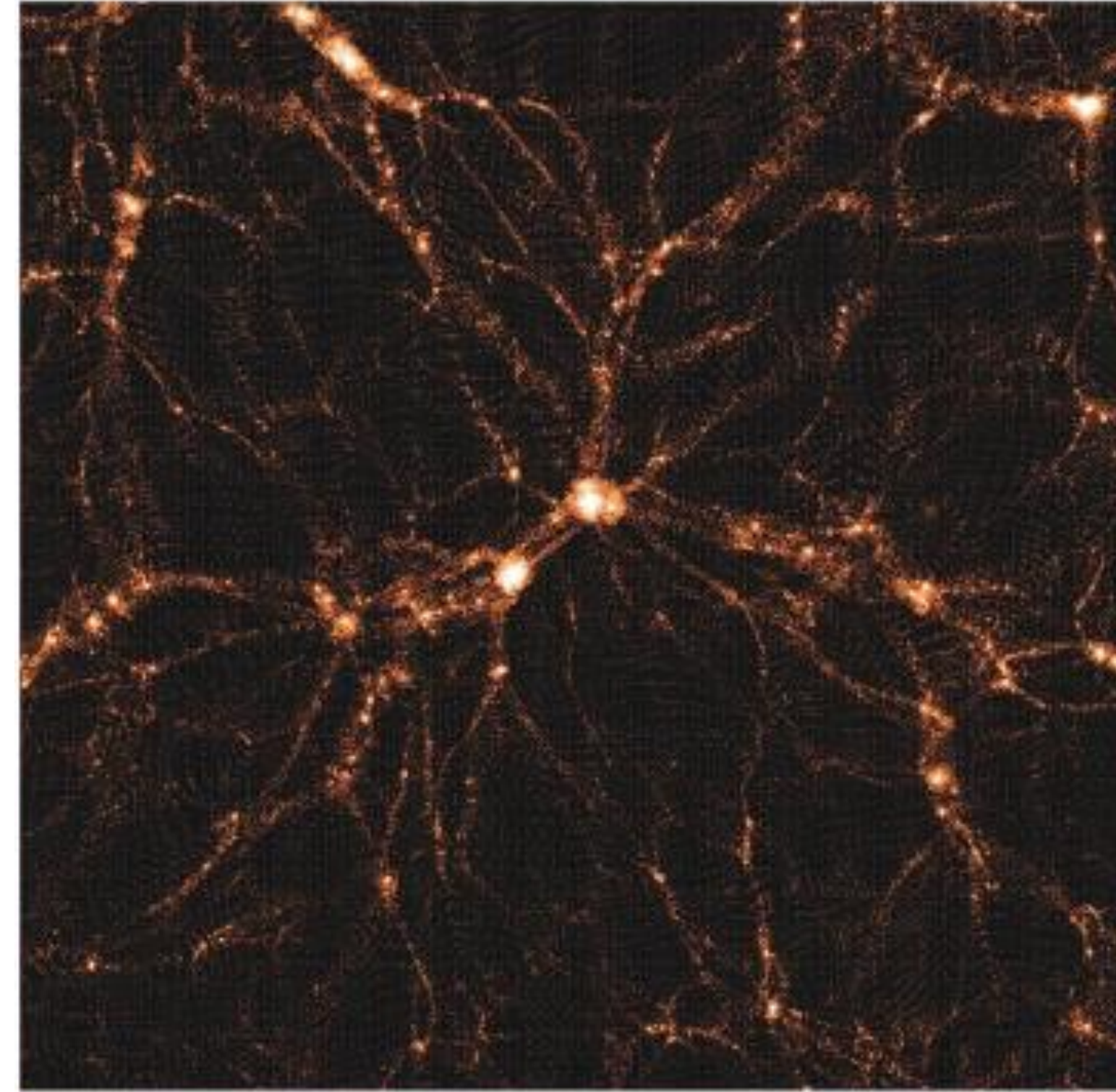
# Large Scale Structure

HSC-Y1 cosmic shear:  $S_8 = 0.78$



Hikage et al. (2019)

Planck 2020 Primary CMB:  $S_8 = 0.83$



Planck Collaboration (2020)

Credit: T. Nishimichi

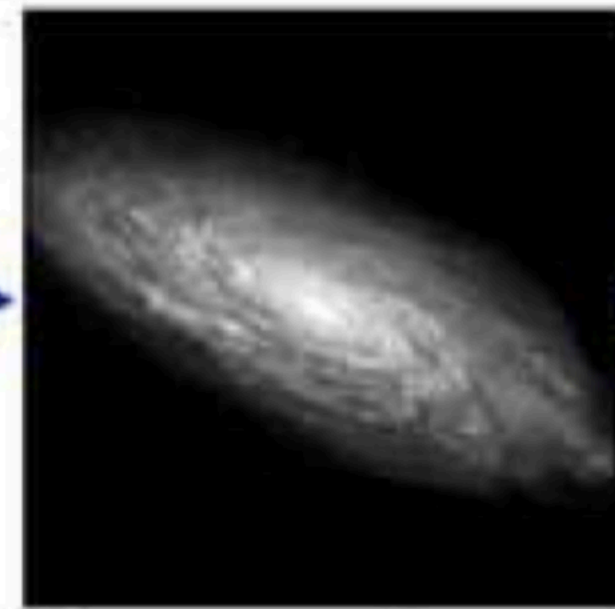
We need to measure the difference between LSS above.  
Challenge: Most of the matter is dark matter

# Weak Gravitational Lensing

Credit: S. Bridle



Intrinsic galaxy  
(shape unknown)



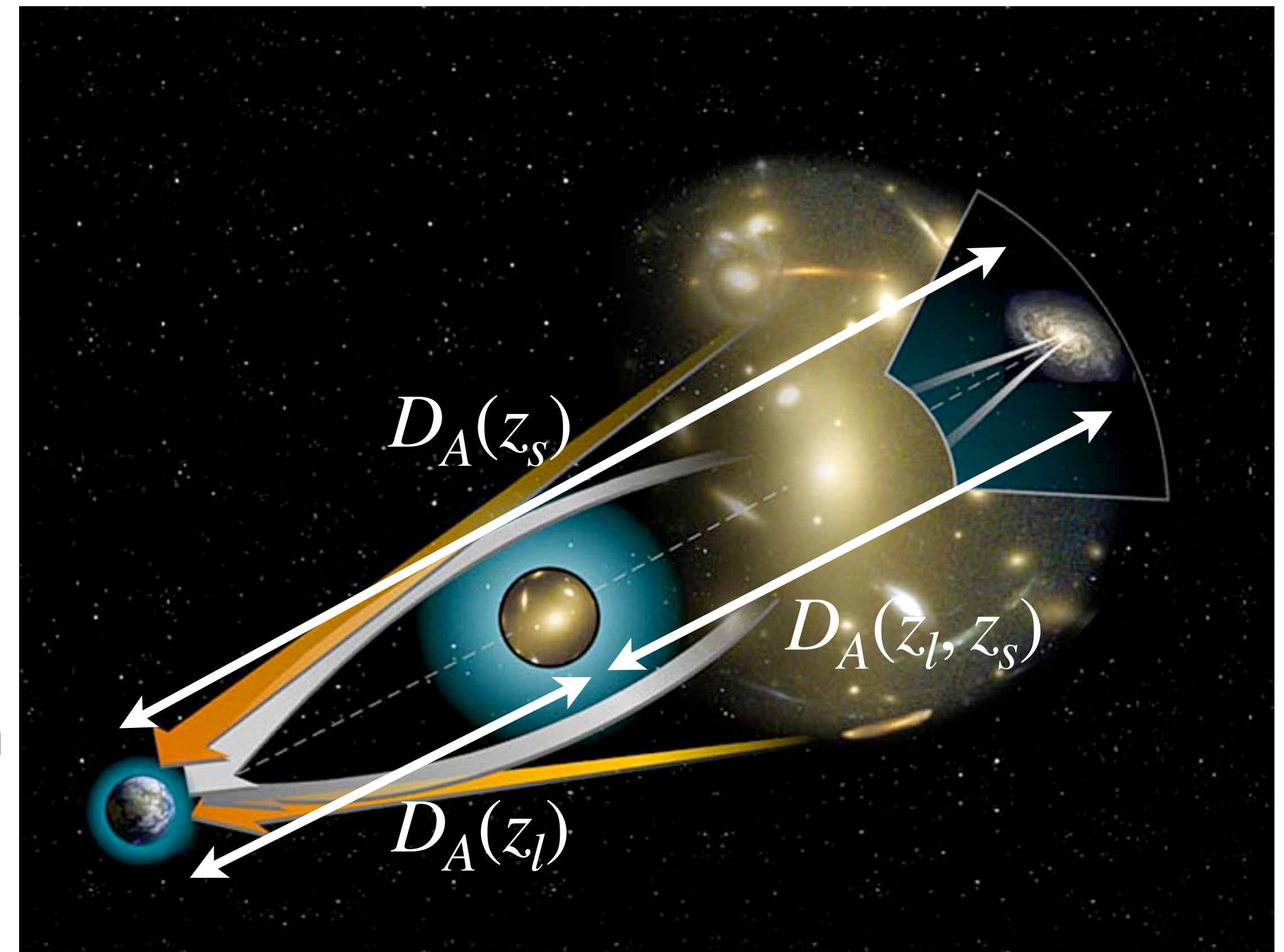
Gravitational lensing  
causes a **shear**

$$\gamma \sim \Omega_m \frac{D_A(z_l, z_s) D_A(z_l)}{D_A(z_s)} \delta_m(z_l)$$

Weak lensing shear

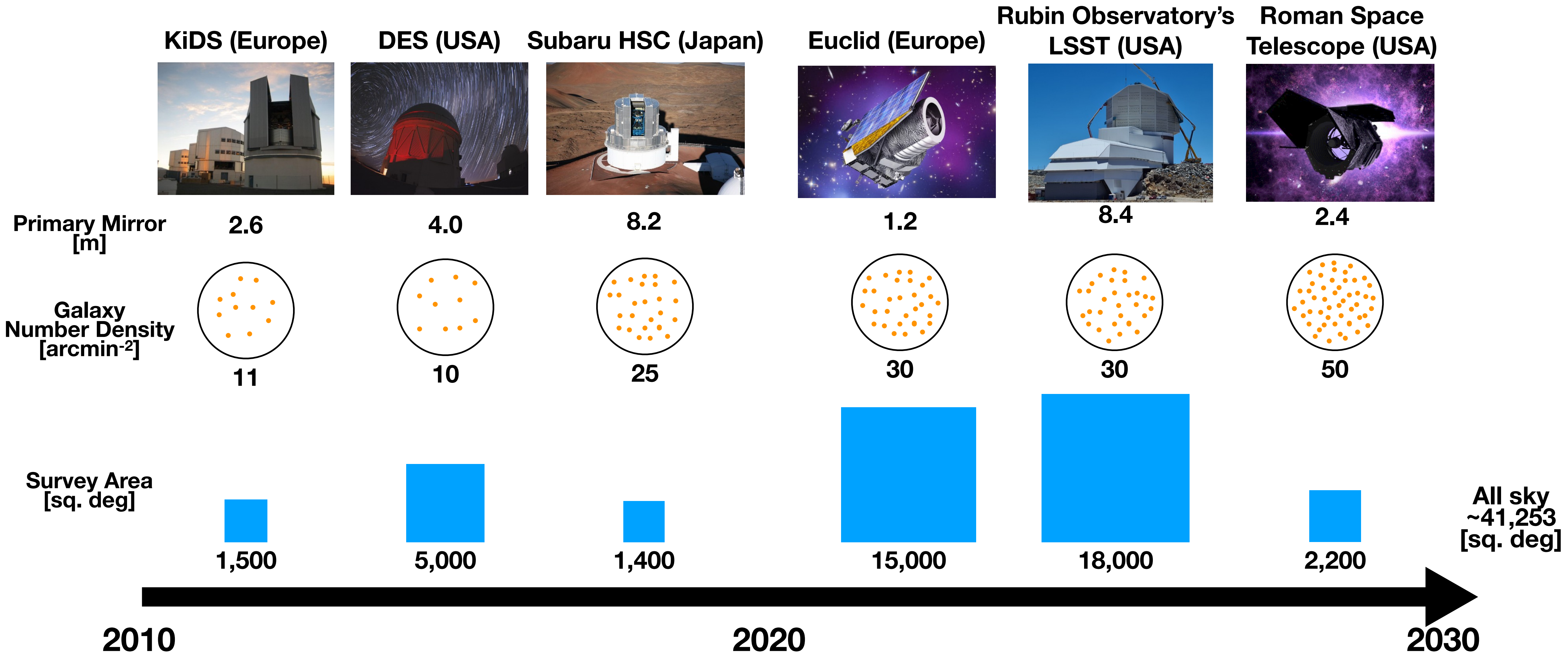
Geometry of the Universe

Matter density fluctuation



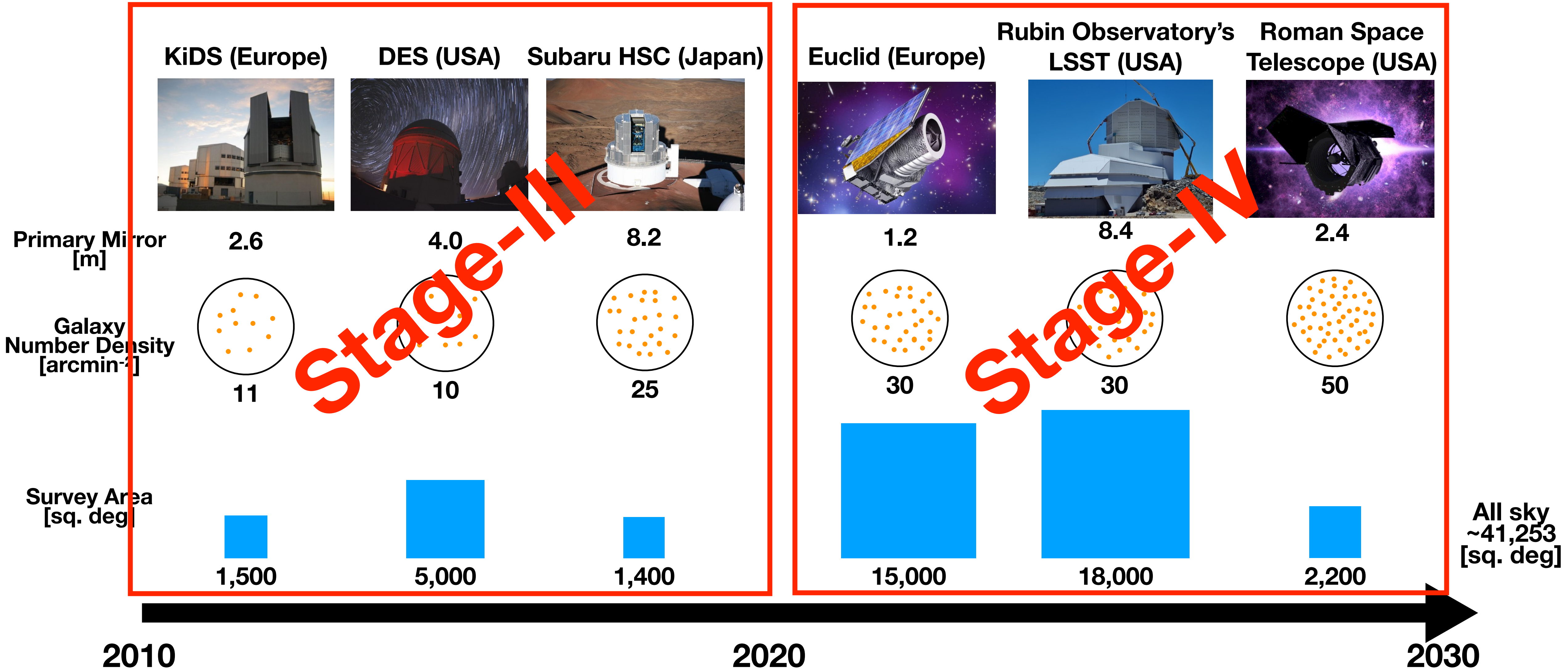
Weak lensing enables us to measure matter (incl. **dark matter**) distributions in the Universe.

# Weak Lensing Surveys: Now and Future

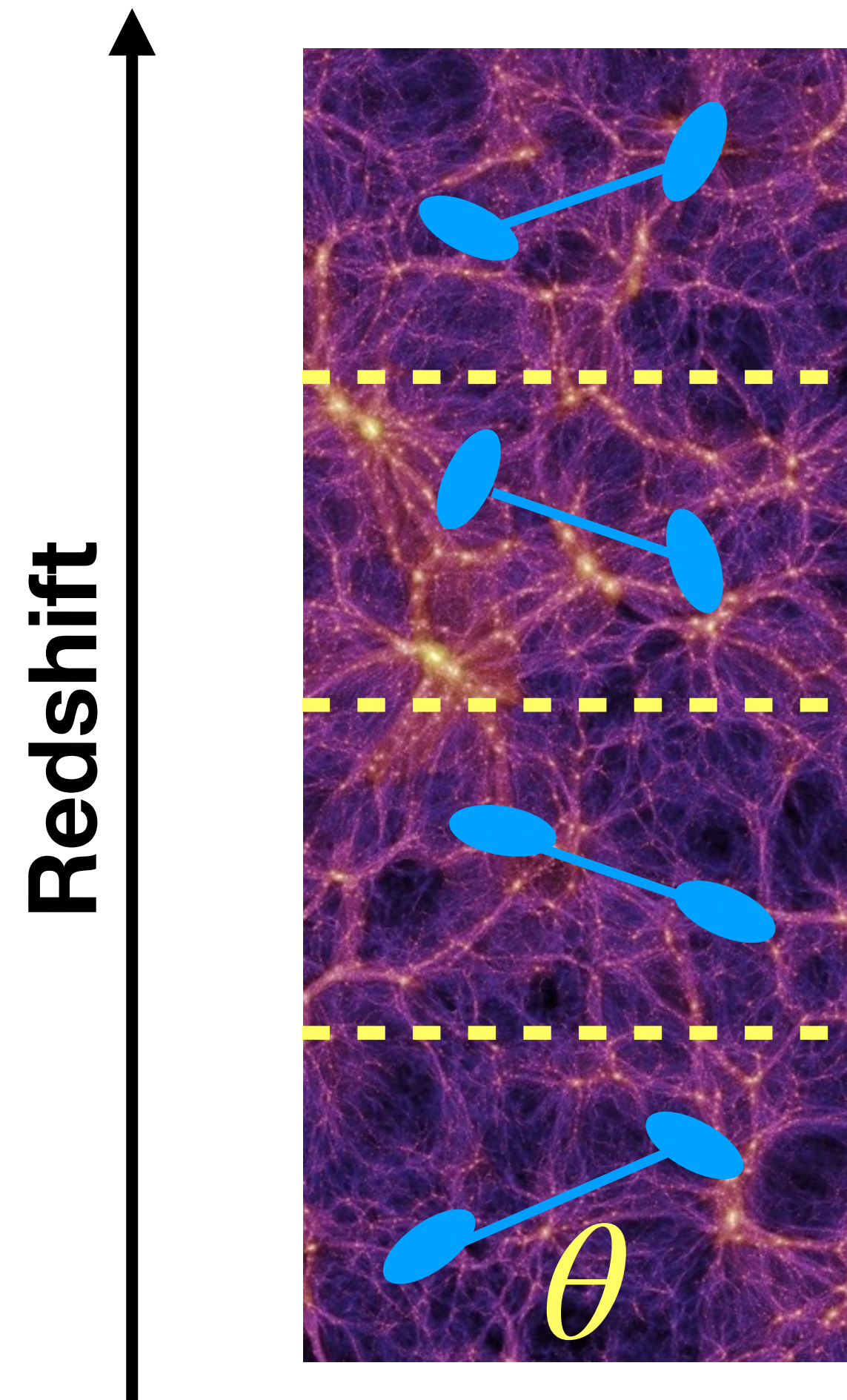




# Weak Lensing Surveys: Now and Future



# Cosmic Shear

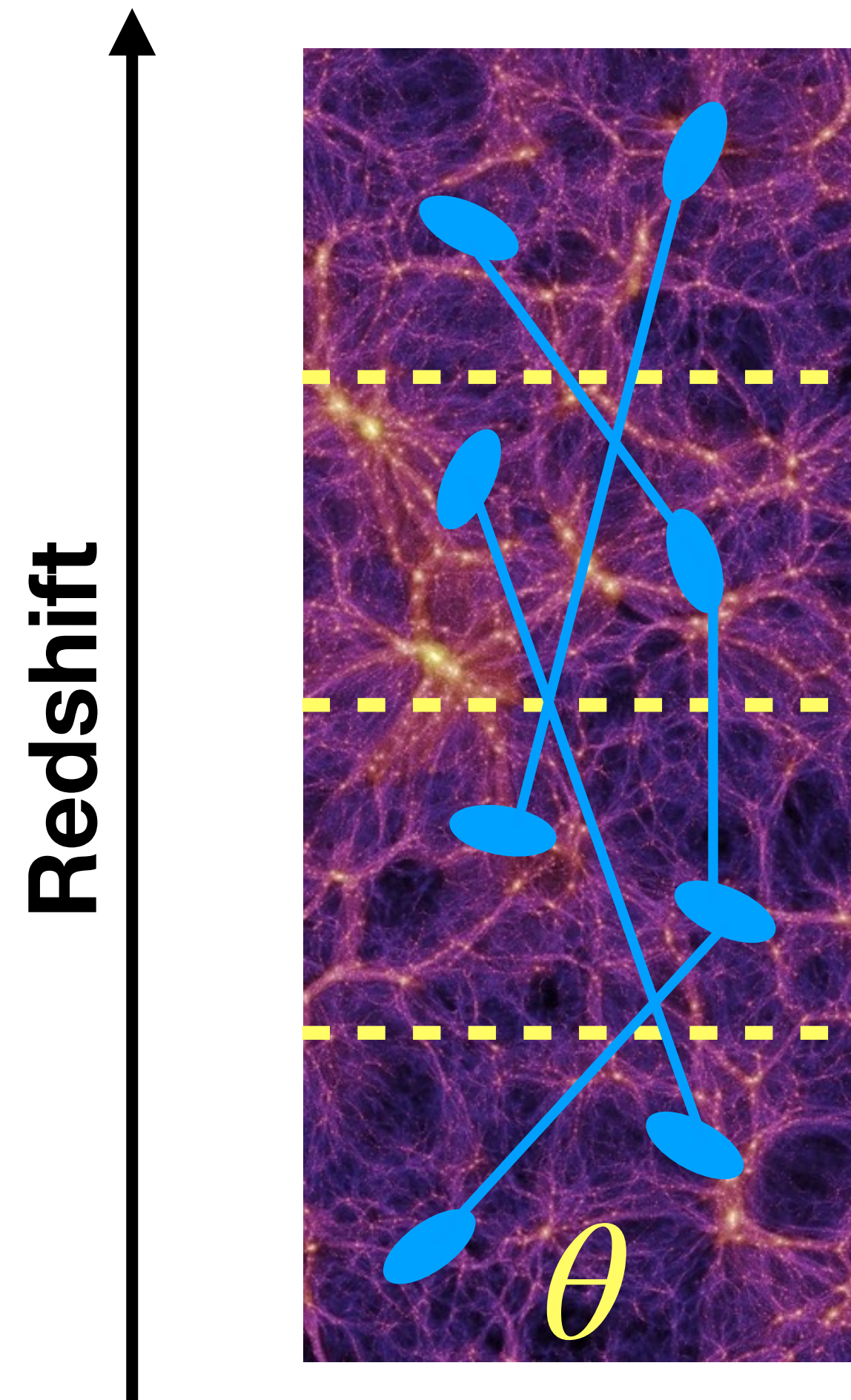


$$\xi_{\pm}(\theta) = \langle \gamma_{+}(\theta') \gamma_{+}(\theta' + \theta) \rangle_{\theta'} \pm \langle \gamma_{\times}(\theta') \gamma_{\times}(\theta' + \theta) \rangle_{\theta'}$$
$$\sim \xi_{\text{mm}}(\theta; \sigma_8, \Omega_m)$$

Note:  $\theta$  is angular scales (not separation between galaxies)

Correlation can be computed within a redshift bin

# Cosmic Shear

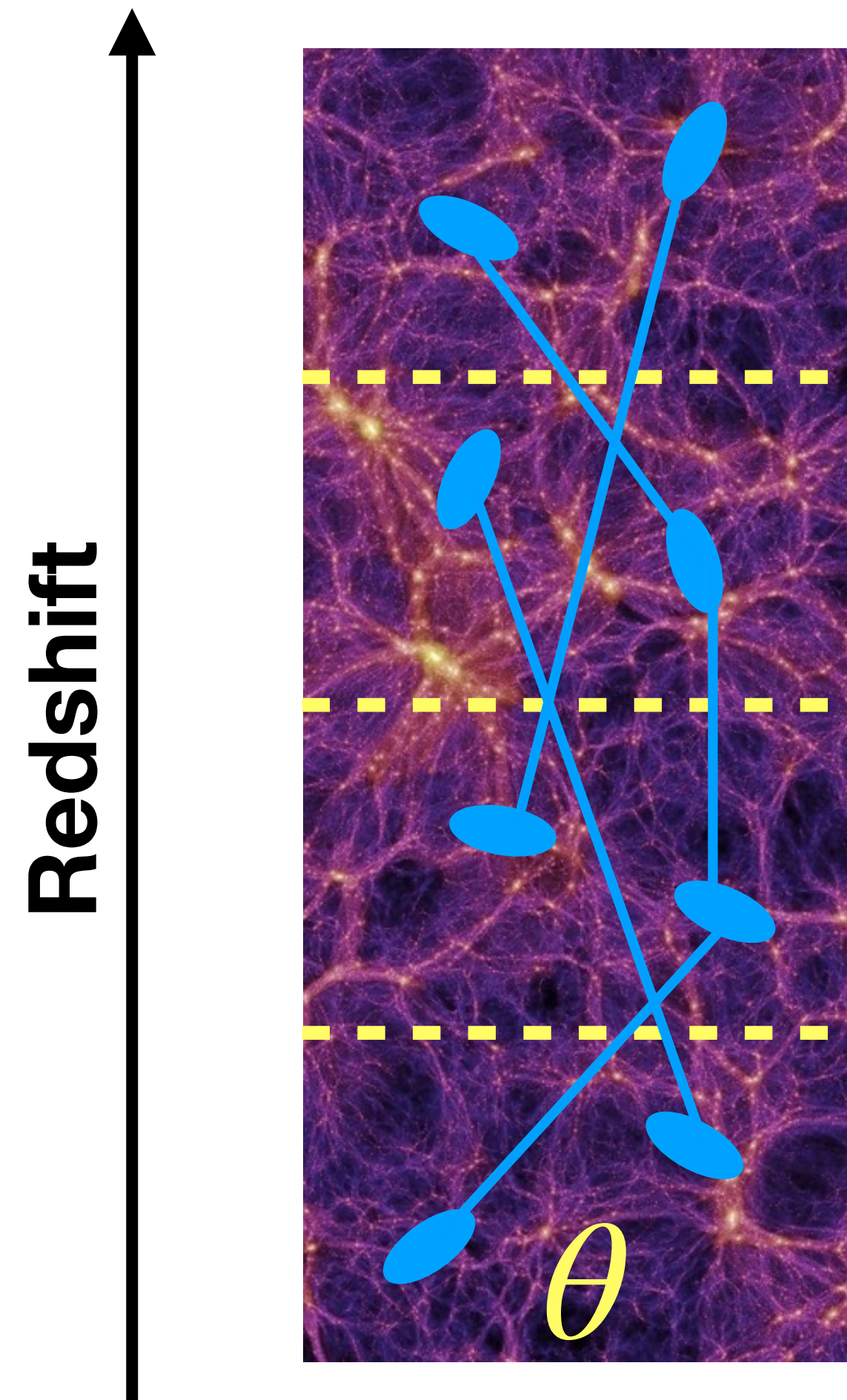


$$\xi_{\pm}(\theta) = \langle \gamma_{+}(\theta')\gamma_{+}(\theta' + \theta) \rangle_{\theta'} \pm \langle \gamma_{\times}(\theta')\gamma_{\times}(\theta' + \theta) \rangle_{\theta'}$$
$$\sim \xi_{\text{mm}}(\theta; \sigma_8, \Omega_m)$$

Note:  $\theta$  is angular scales (not separation between galaxies)

Correlation can be computed within a redshift bin  
or across redshift bins

# Cosmic Shear



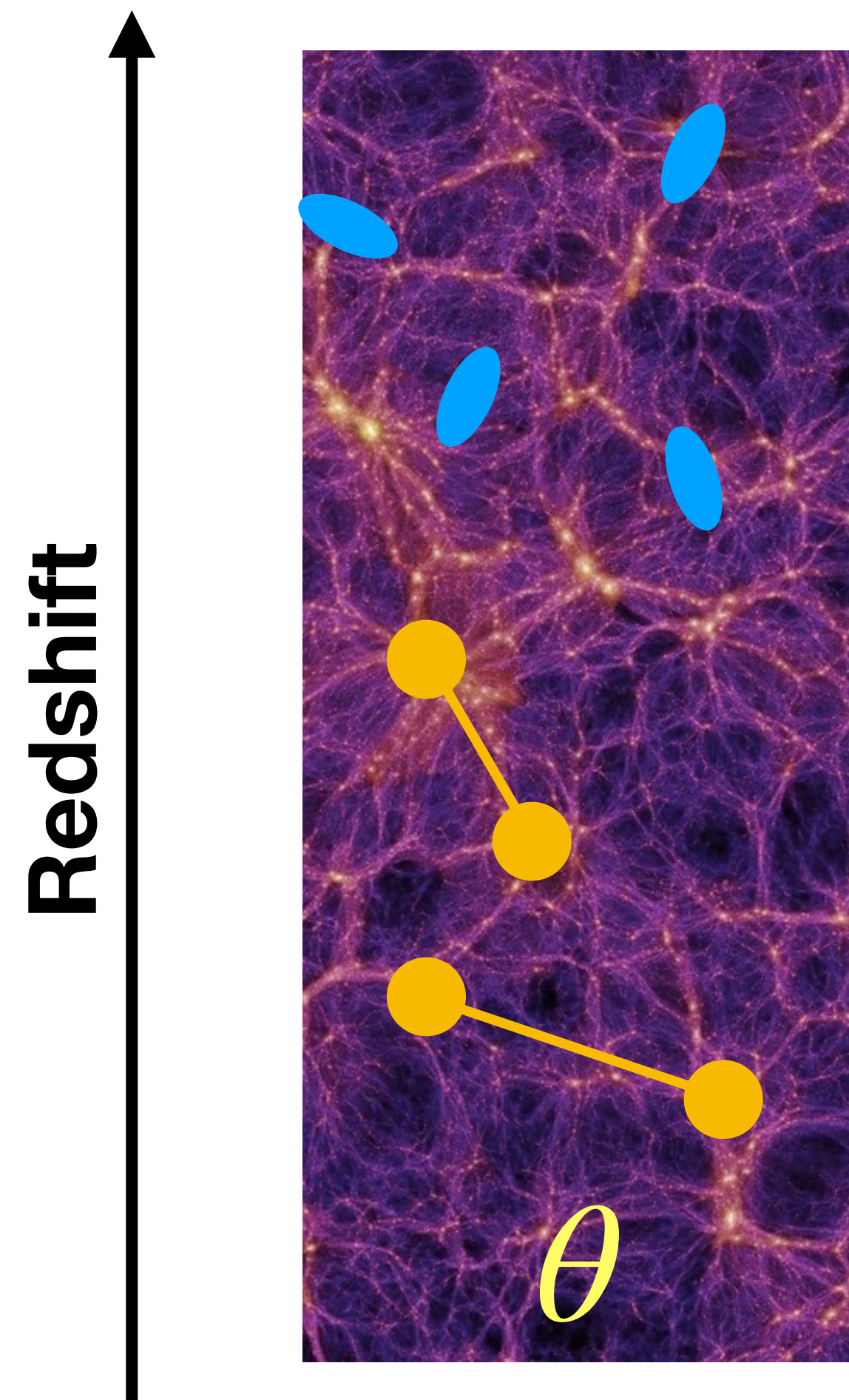
$$\xi_{\pm}(\theta) = \langle \gamma_{+}(\theta') \gamma_{+}(\theta' + \theta) \rangle_{\theta'} \pm \langle \gamma_{\times}(\theta') \gamma_{\times}(\theta' + \theta) \rangle_{\theta'}$$
$$\sim \xi_{\text{mm}}(\theta; \sigma_8, \Omega_m)$$

Note:  $\theta$  is angular scales (not separation between galaxies)

Correlation can be computed within a redshift bin or across redshift bins

Fourier space measurements  $C_{EE}(l)$ ,  $C_{BB}(l)$  are also common now.

# 2x2pt: Galaxy-galaxy Clustering and Lensing



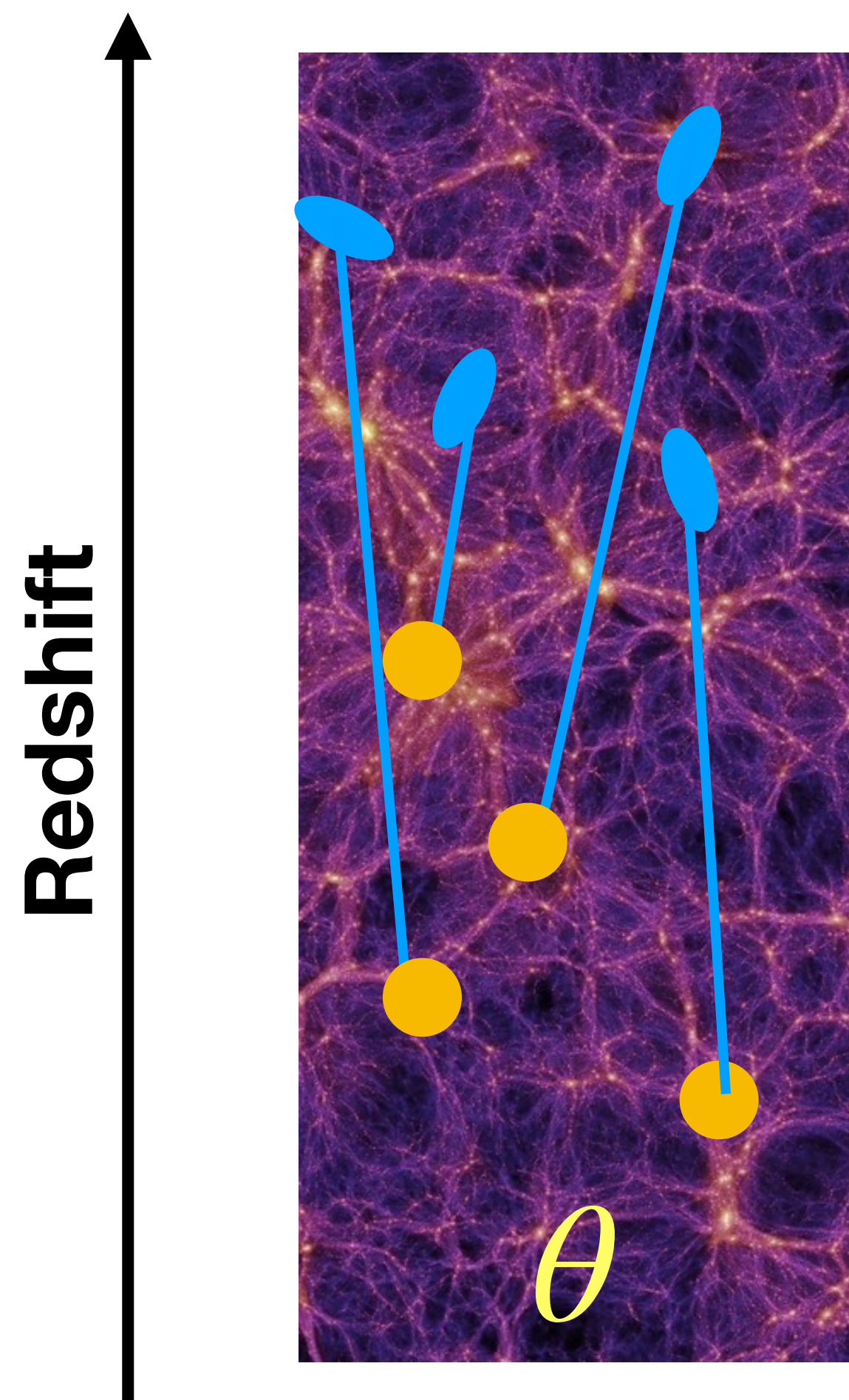
(Projected) Galaxy-galaxy clustering

$$w(\theta) \sim \langle \delta_g(\theta') \delta_g(\theta' + \theta) \rangle_{\theta'} \sim b^2 \xi_{mm}(\theta; \sigma_8, \Omega_m)$$

Linear bias factor

Linear bias approximation:  $\delta_g \sim b\delta_m$  (valid at large scales)

# 2x2pt: Galaxy-galaxy Clustering and Lensing



(Projected) Galaxy-galaxy clustering

$$w(\theta) \sim \langle \delta_g(\theta') \delta_g(\theta' + \theta) \rangle_{\theta'} \sim b^2 \xi_{mm}(\theta; \sigma_8, \Omega_m)$$

Linear bias factor

Linear bias approximation:  $\delta_g \sim b \delta_m$  (valid at large scales)

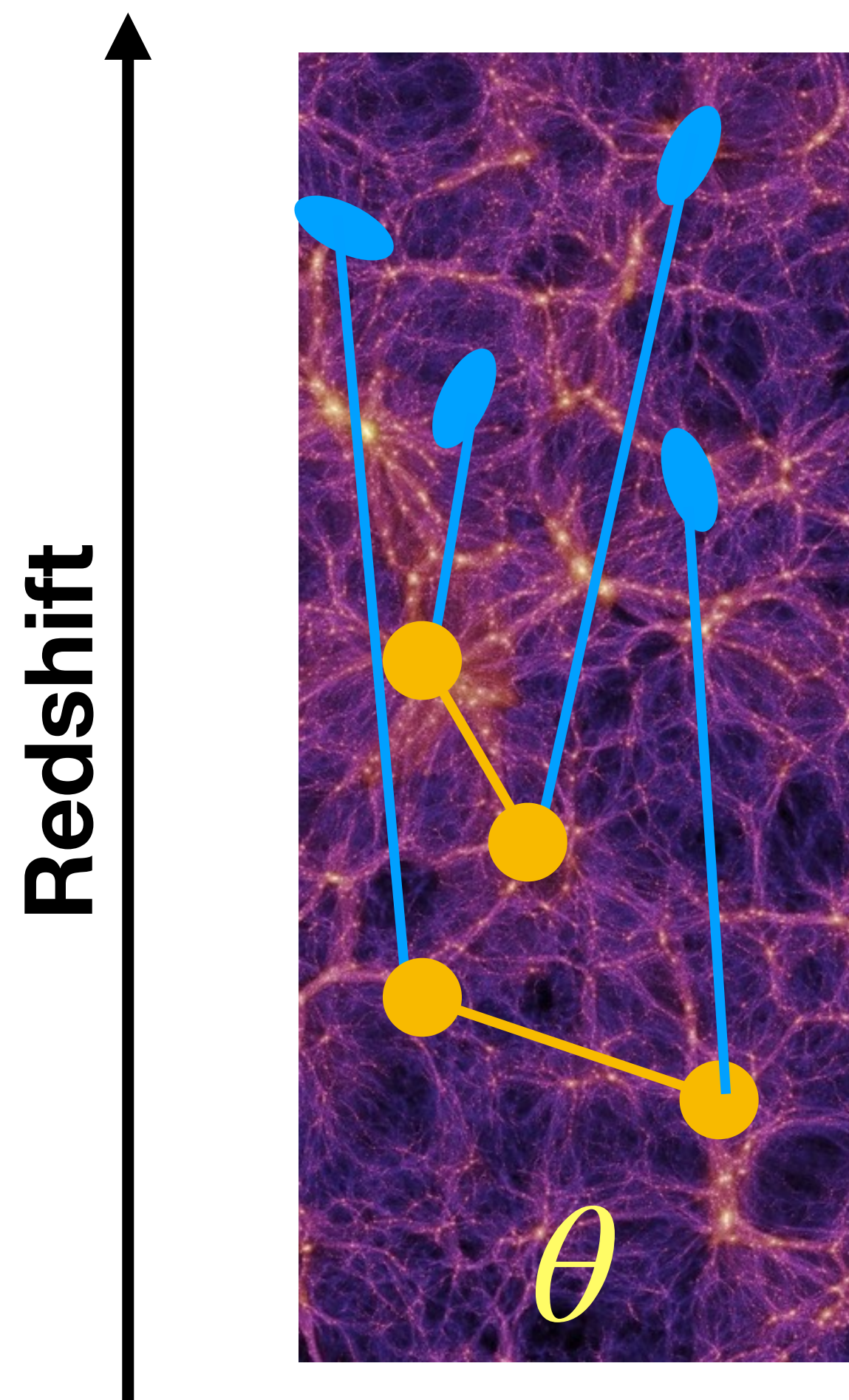
Galaxy-galaxy lensing

$$\begin{aligned} \gamma(\theta) &\sim \Omega_m \Sigma_{\text{cr}}(z_l, z_s)^{-1} \langle \delta_g(\theta') \delta_m(\theta' + \theta) \rangle_{\theta'} \\ &\sim \Omega_m \Sigma_{\text{cr}}(z_l, z_s)^{-1} b \xi_{mm}(\theta; \sigma_8, \Omega_m) \end{aligned}$$

where

$$\Sigma_{\text{cr}} \propto \frac{D_A(z_s)}{D_A(z_l, z_s) D_A(z_l)}$$

# 2x2pt: Galaxy-galaxy Clustering and Lensing



(Projected) Galaxy-galaxy clustering

$$w(\theta) \sim \langle \delta_g(\theta') \delta_g(\theta' + \theta) \rangle_{\theta'} \sim b^2 \xi_{mm}(\theta; \sigma_8, \Omega_m)$$

Linear bias factor

Linear bias approximation:  $\delta_g \sim b \delta_m$  (valid at large scales)

Galaxy-galaxy lensing

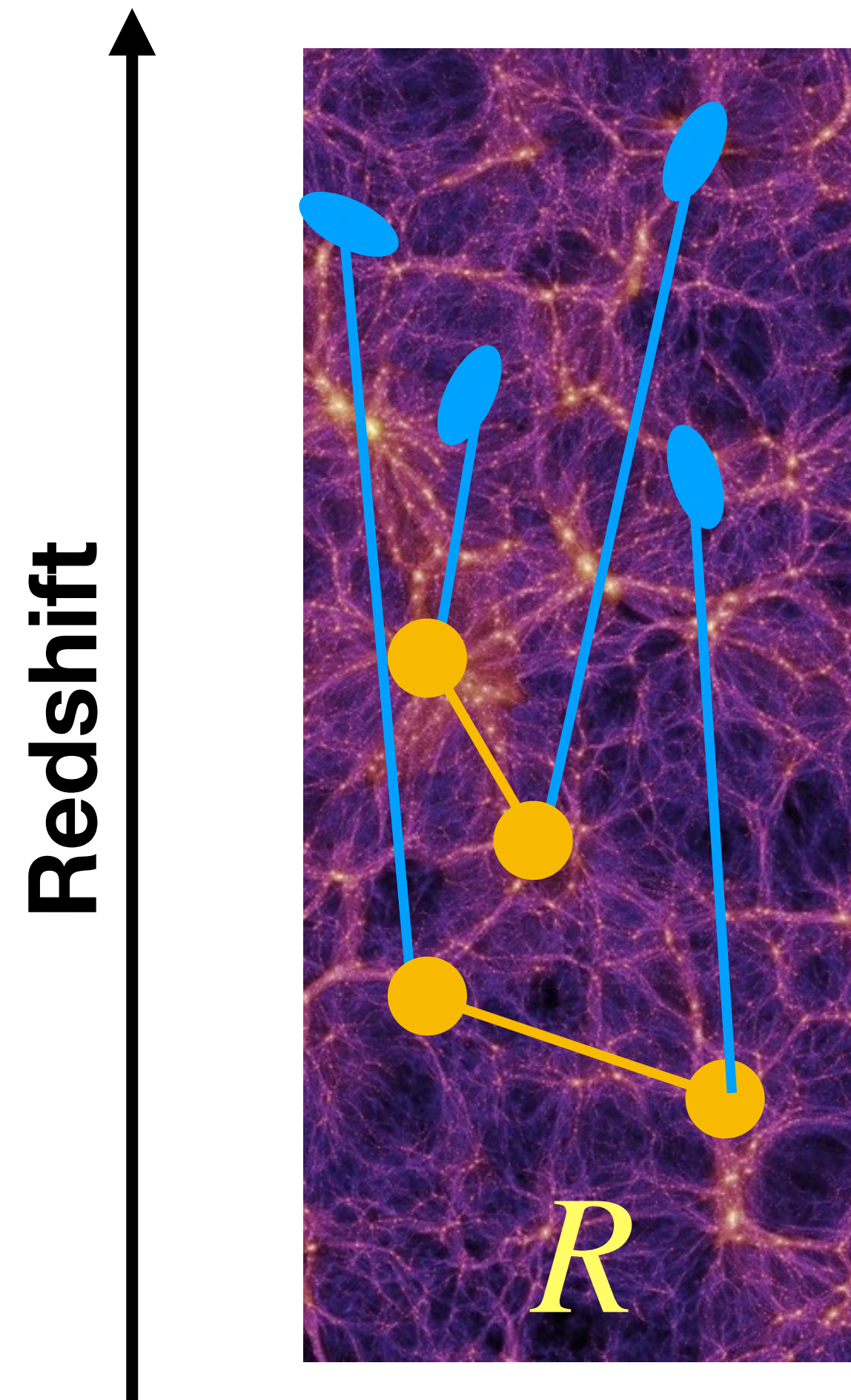
$$\begin{aligned} \gamma(\theta) &\sim \Omega_m \Sigma_{\text{cr}}(z_l, z_s)^{-1} \langle \delta_g(\theta') \delta_m(\theta' + \theta) \rangle_{\theta'} && \text{where} \\ &\sim \Omega_m \Sigma_{\text{cr}}(z_l, z_s)^{-1} b \xi_{mm}(\theta; \sigma_8, \Omega_m) && \Sigma_{\text{cr}} \propto \frac{D_A(z_s)}{D_A(z_l, z_s) D_A(z_l)} \end{aligned}$$

Combination of Galaxy-galaxy clustering and lensing

breaks the degeneracy between  $b$  and  $(\sigma_8, \Omega_m)$ .

Foreground galaxies are called tracers.

# 2x2pt: Galaxy-galaxy Clustering and Lensing



If we have a spectroscopic sample for clustering

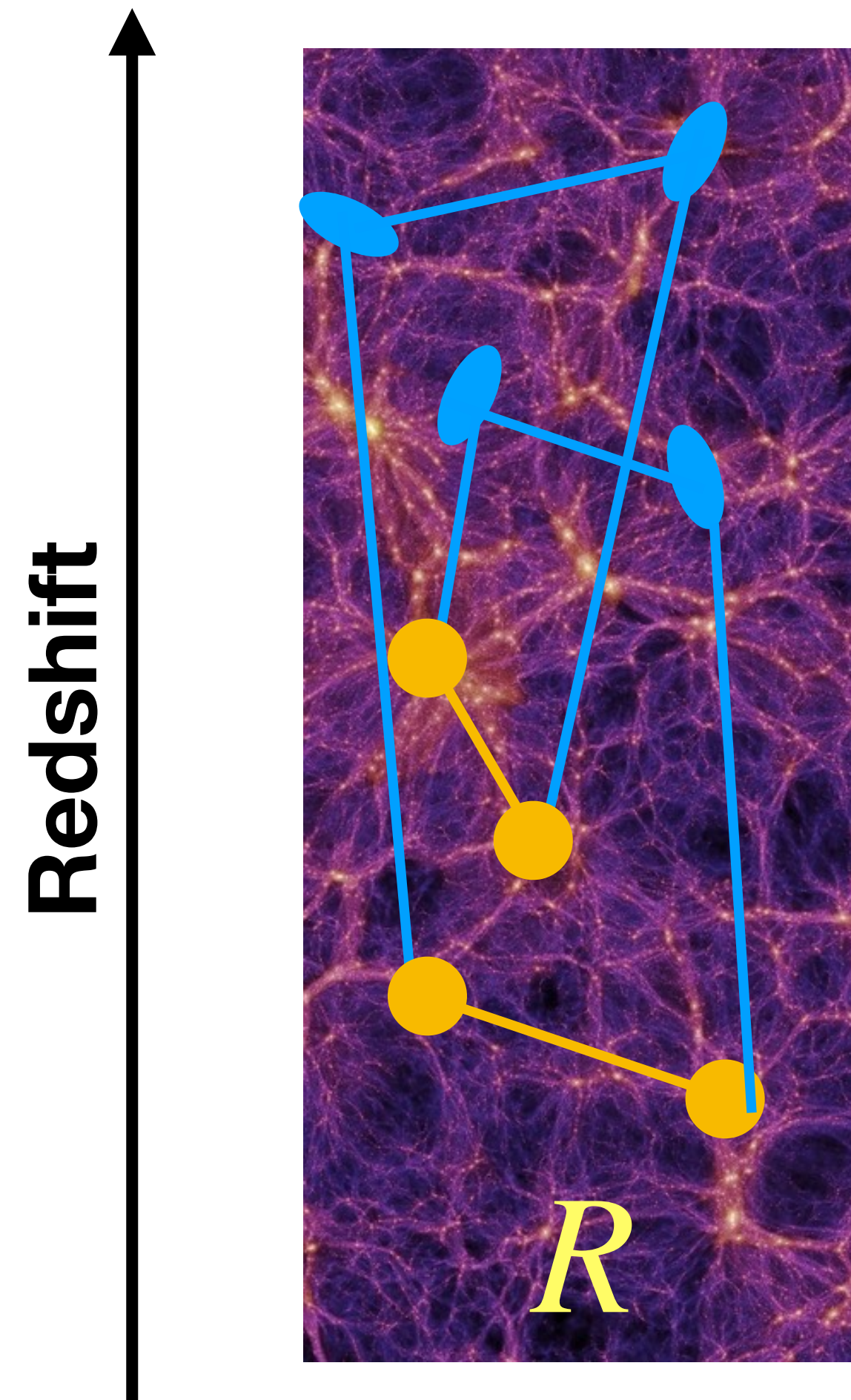
$$w_p(R) \sim \langle \delta_g(R') \delta_g(R' + R) \rangle_{R'}$$

$$\Delta\Sigma(R) \sim \Sigma_{\text{cr}}(z_l, z_s) \gamma(R) \equiv \Sigma_{\text{cr}}(z_l, z_s) \langle \delta_g(R') \delta_m(R' + R) \rangle_{R'}$$





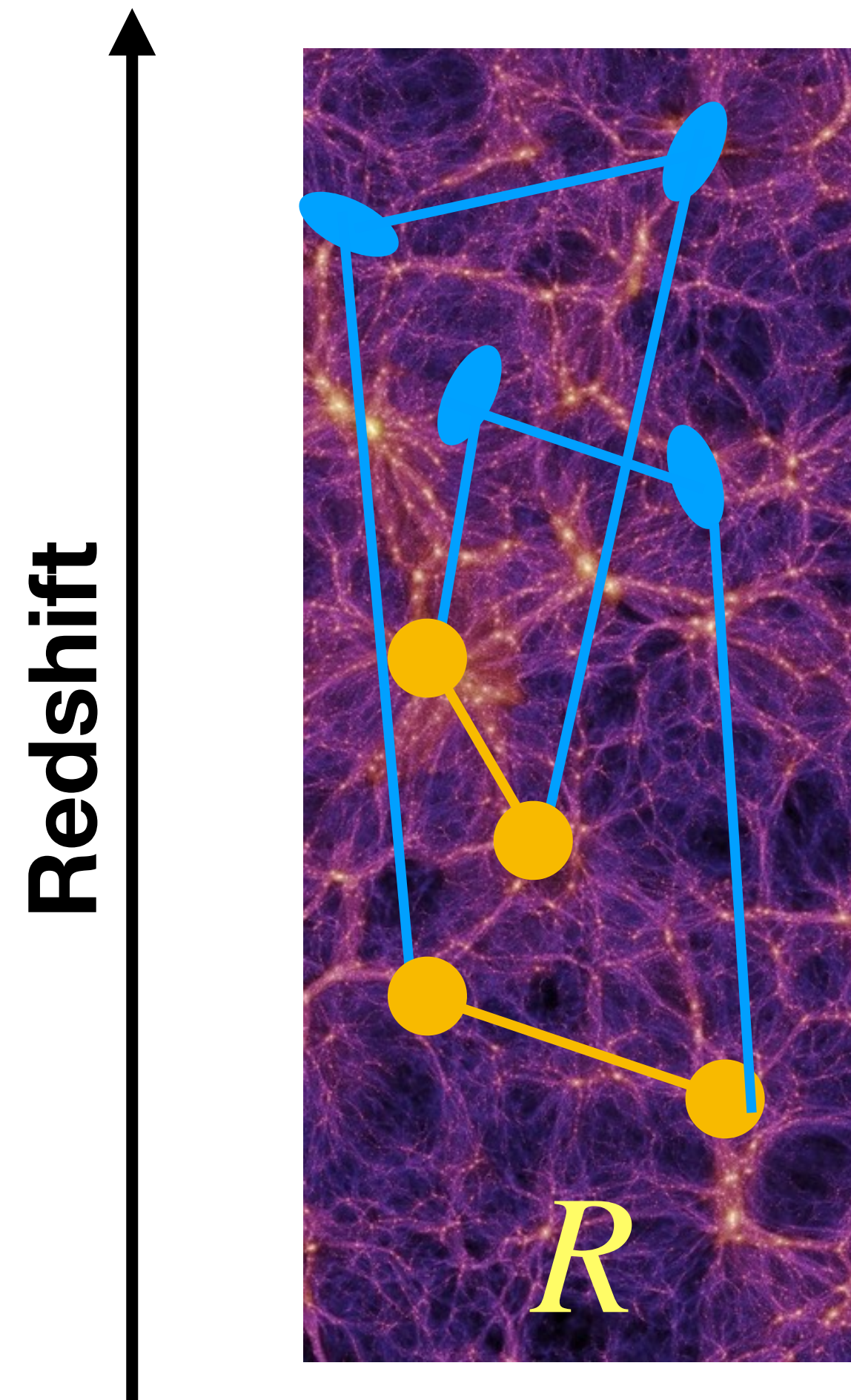
# 3x2pt: Cosmic Shear + 2x2pt



Now we can combine everything :)

$$\xi_{\pm}(\theta), w(\theta), \gamma(\theta)$$

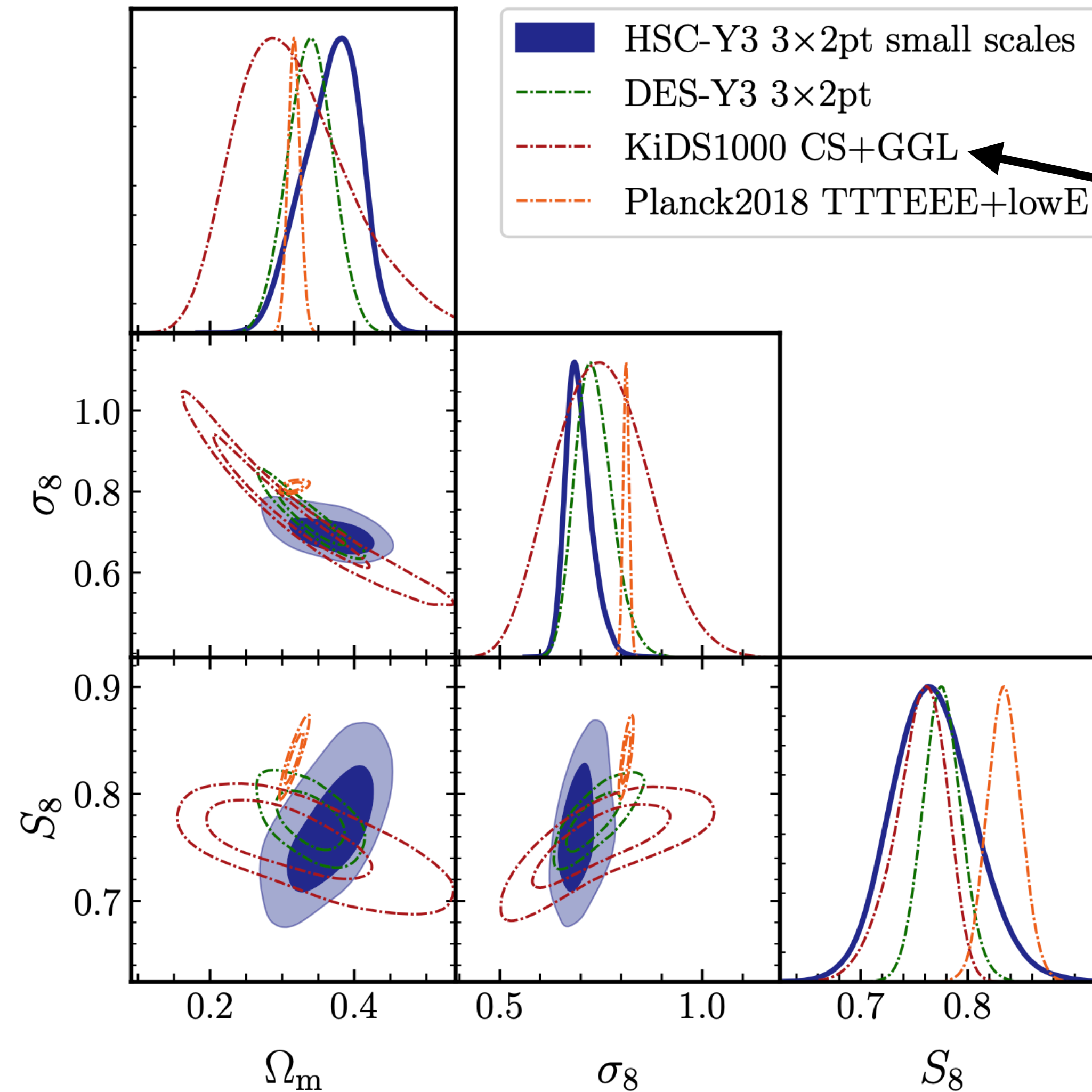
# 3x2pt: Cosmic Shear + 2x2pt



Now we can combine everything :)

$$\xi_{\pm}(\theta), w(\theta), \gamma(\theta)$$

# Latest 3x2pt Analyses of Stage-III Surveys

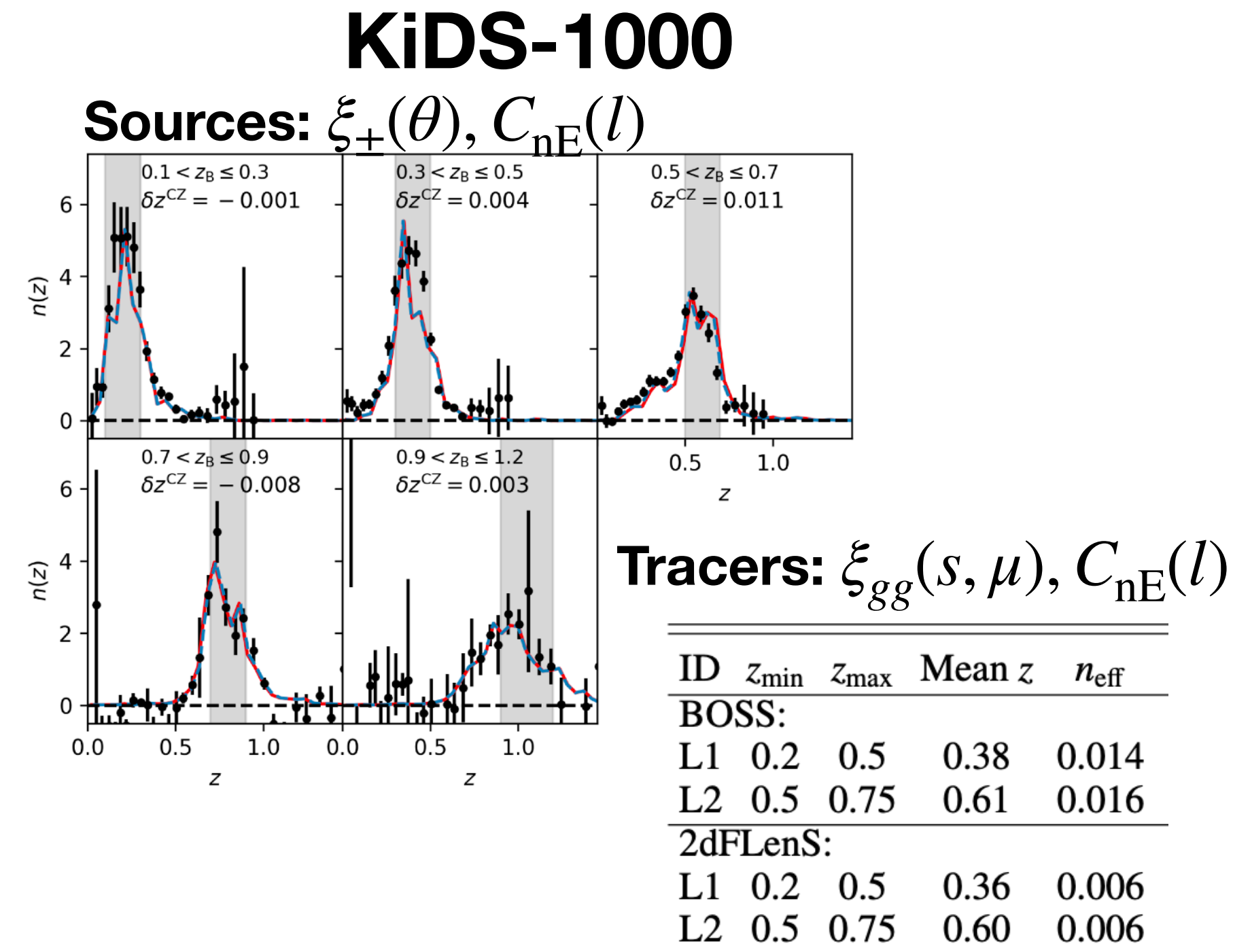
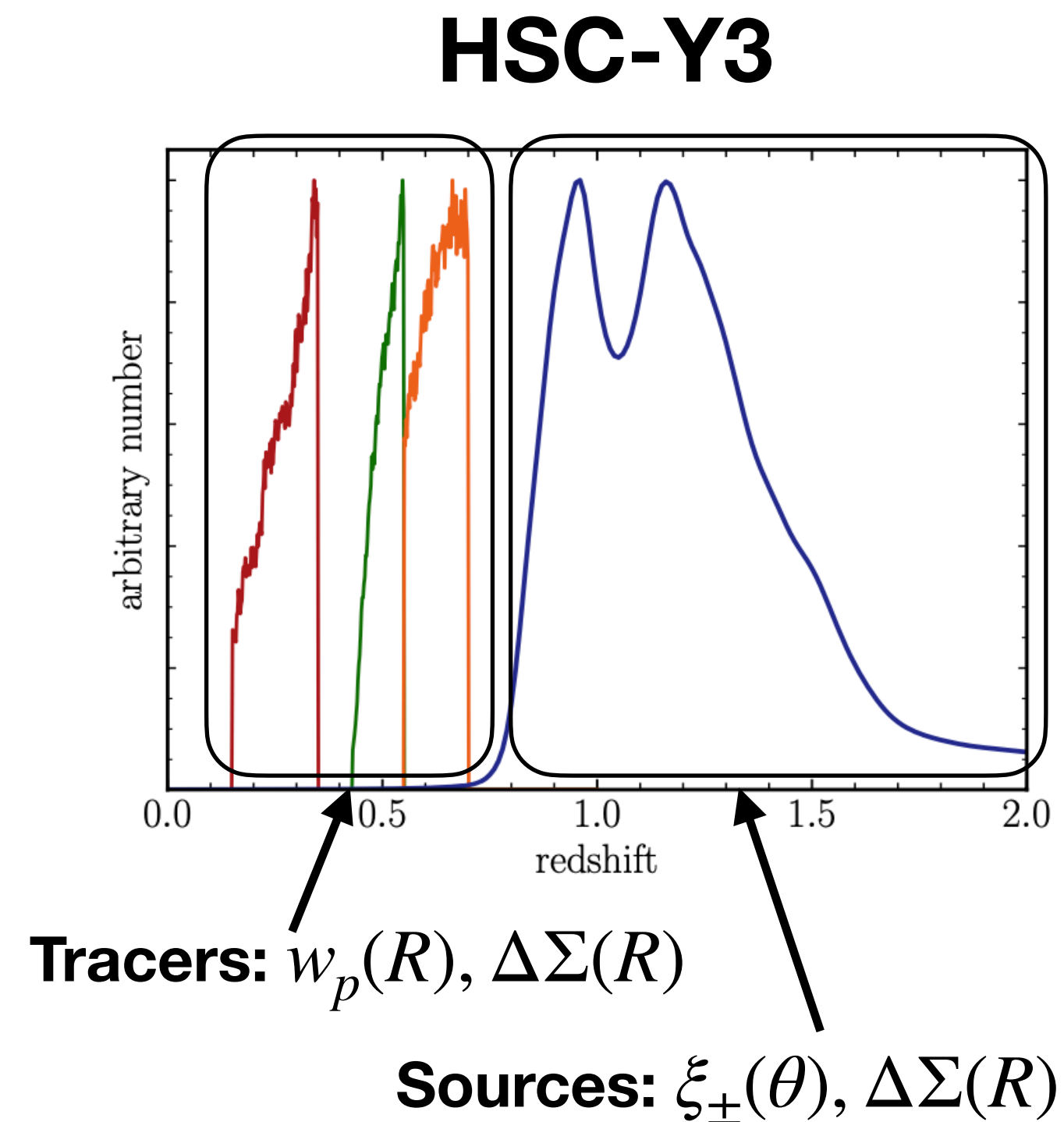
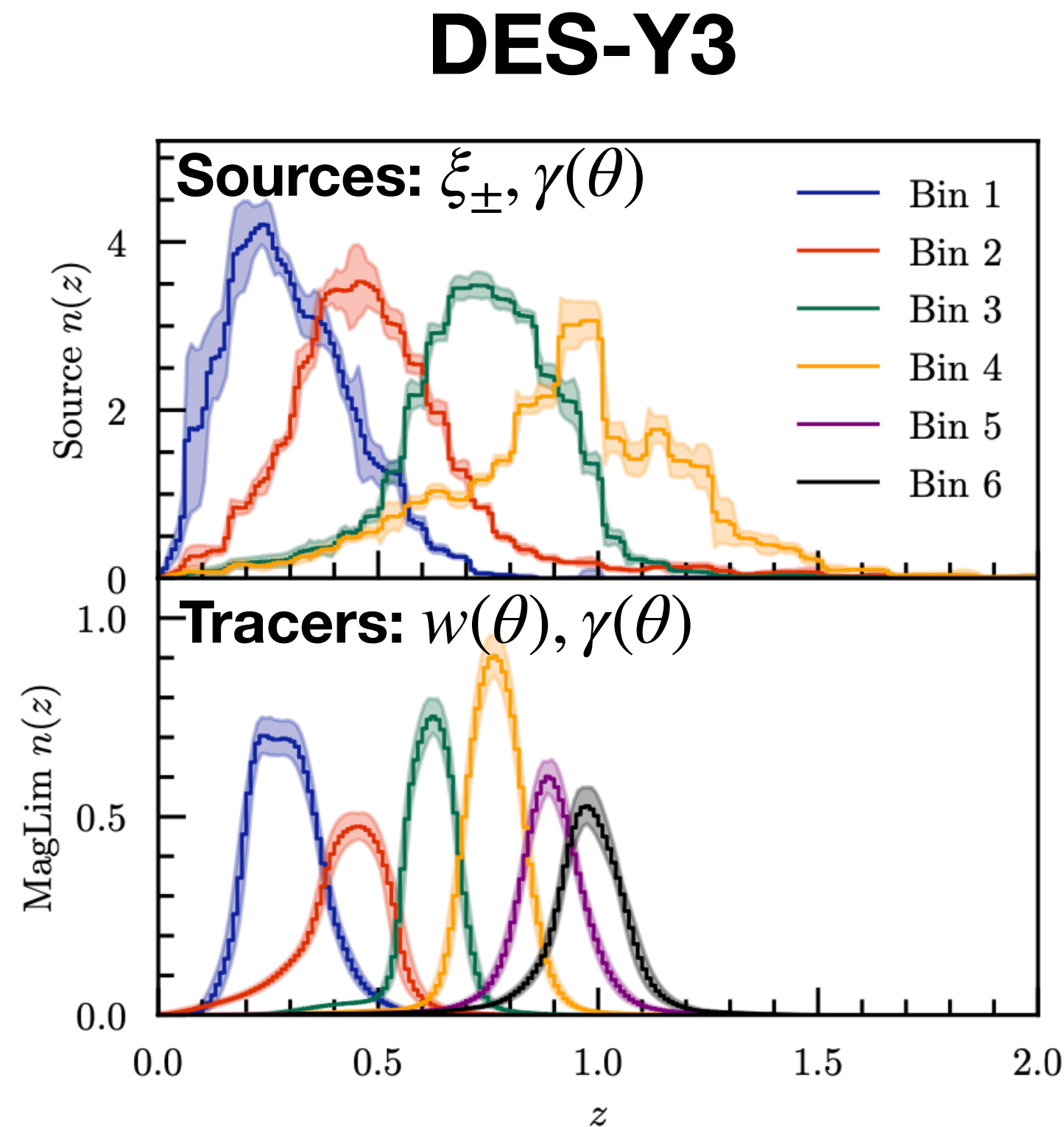


KiDS 3x2pt is not shown here since the constraint on  $\Omega_m$  is quite tight due to the use of BAO.

# Analysis Choice: Summary Statistics

	<b>DES-Y3</b> DES collaboration (2022)	<b>HSC-Y3</b> Sugiyama et al. (2023) Miyatake et al. (2023)	<b>KiDS-1000</b> Heymans et al. (2021)
Cosmic Shear	Real Space $\xi_{\pm}(\theta)$	Real space $\xi_{\pm}(\theta)$	Fourier Space $C_{EE}(l)$
Galaxy-galaxy clustering	Projected clustering with photometric galaxies $w(\theta)$	Projected clustering from BOSS $w_p(R)$	3D clustering from BOSS and 2dFLenS $\xi_{gg}(s, \mu)$
Galaxy-galaxy lensing	Use photometric galaxies as a tracer $\gamma(\theta)$	Use BOSS galaxies as a tracer $\Delta\Sigma(R)$	Use BOSS and 2dFLenS galaxies as a tracer $C_{nE}(l)$ equiv. To $\gamma(\theta)$

# Analysis Choice: Redshift Bins



- DES uses lens-source pairs even if there is an overlap in redshift.
- HSC uses sources well separated from lenses. Cosmic shear is measured in a single redshift bin (Cosmic shear only analyses were done using multiple source redshift bins. See Li et al. (2023) and Dalal et al. (2023)).
- KiDS uses lens-source pairs when a source bin is behind a lens bin.

# Analysis Choice: Scale Cuts

	DES-Y3 DES collaboration (2022)	HSC-Y3 Sugiyama et al. (2023) Miyatake et al. (2023)	KiDS-1000 Heymans et al. (2021)
Cosmic shear	$\xi_+$ : $\sim 3 \text{ arcmin} < \theta < \sim 220 \text{ arcmin}$ $\xi_-$ : $\sim 40 \text{ arcmin} < \theta < \sim 220 \text{ arcmin}$ (depends on redshift bin)	$\xi_+$ : $8 \text{ arcmin} < \theta < 50 \text{ arcmin}$ $\xi_-$ : $30 \text{ arcmin} < \theta < 150 \text{ arcmin}$	$100 < l < 2000$ ( $\sim 5 \text{ arcmin} < \theta < \sim 100 \text{ arcmin}$ )
Galaxy-galaxy clustering	$R > 8 \text{ Mpc/h}$	$2 \text{ Mpc/h} < R < 30 \text{ Mpc/h}$	$20 \text{ Mpc/h} < s < 160 \text{ Mpc/h}$ (Includes BAO information)
Galaxy-galaxy lensing	$R > 6 \text{ Mpc/h}$	$3 \text{ Mpc/h} < R < 30 \text{ Mpc/h}$	$l < 300$ ( $\theta > \sim 36 \text{ arcmin}$ or $R \sim 15 \text{ Mpc/h}$ )

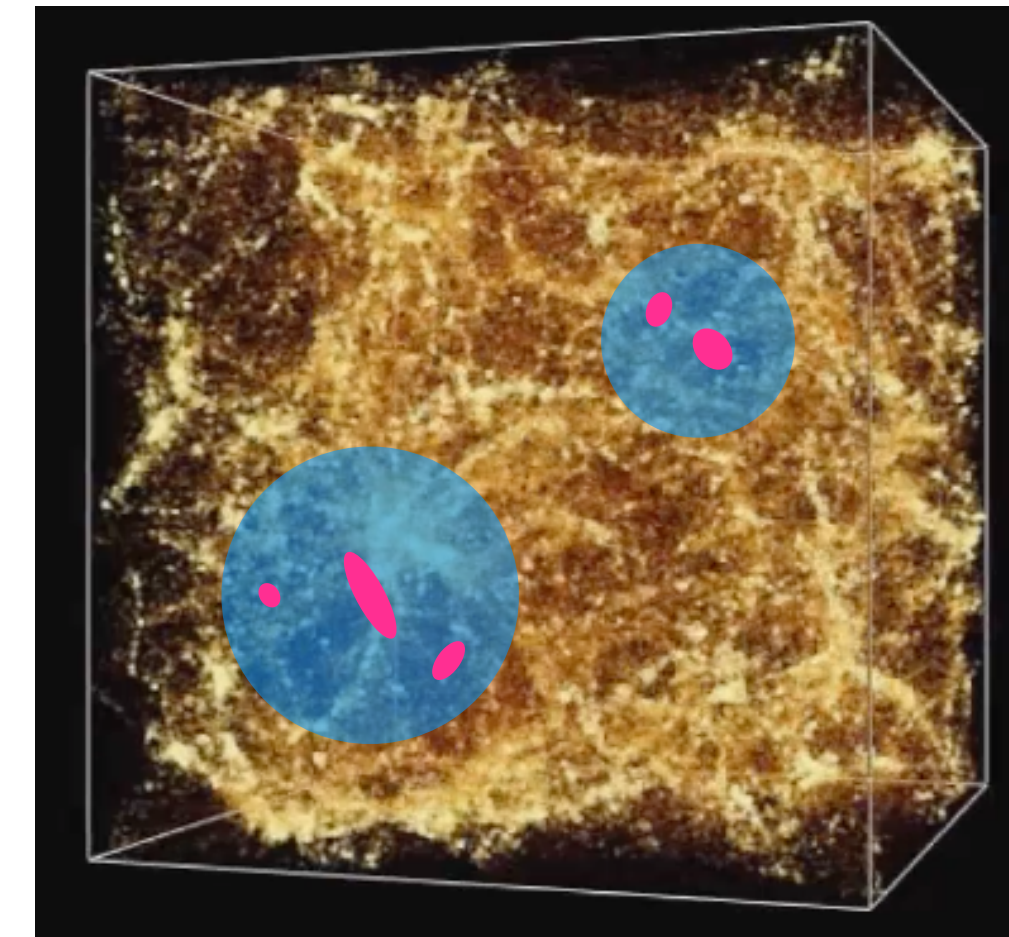
HSC uses much smaller scale cuts for clustering and lensing, in which they need to consider non-linear regime.

# Systematics: Non-linear Effect

HSC-Y3 used non-linear scales to gain S/N

## Challenges

- Accurate modeling of non-linear regimes
- Proper treatment of uncertainties in galaxy-halo connection



dark matter

dark matter halos

galaxies

Cosmo. Params.  
( $\sigma_8, \Omega_m, \dots$ )



$$\xi_{hh} = \langle \delta_h \delta_h \rangle$$

$$\xi_{hm} = \langle \delta_h \delta_m \rangle$$



$$\xi_{gg} = \langle \delta_g \delta_g \rangle$$

$$\xi_{gm} = \langle \delta_g \delta_m \rangle$$



Observables

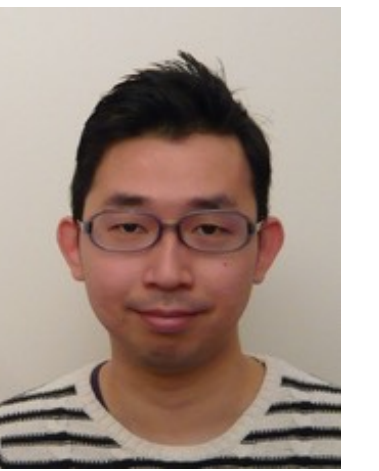
Clustering:  $w_p(R)$   
Weak Lensing:  $\Delta\Sigma(R)$

Projection to 2-d

**Modeling non-linear regimes**  
Prediction by **Dark Emulator**  
achieved a few % accuracy

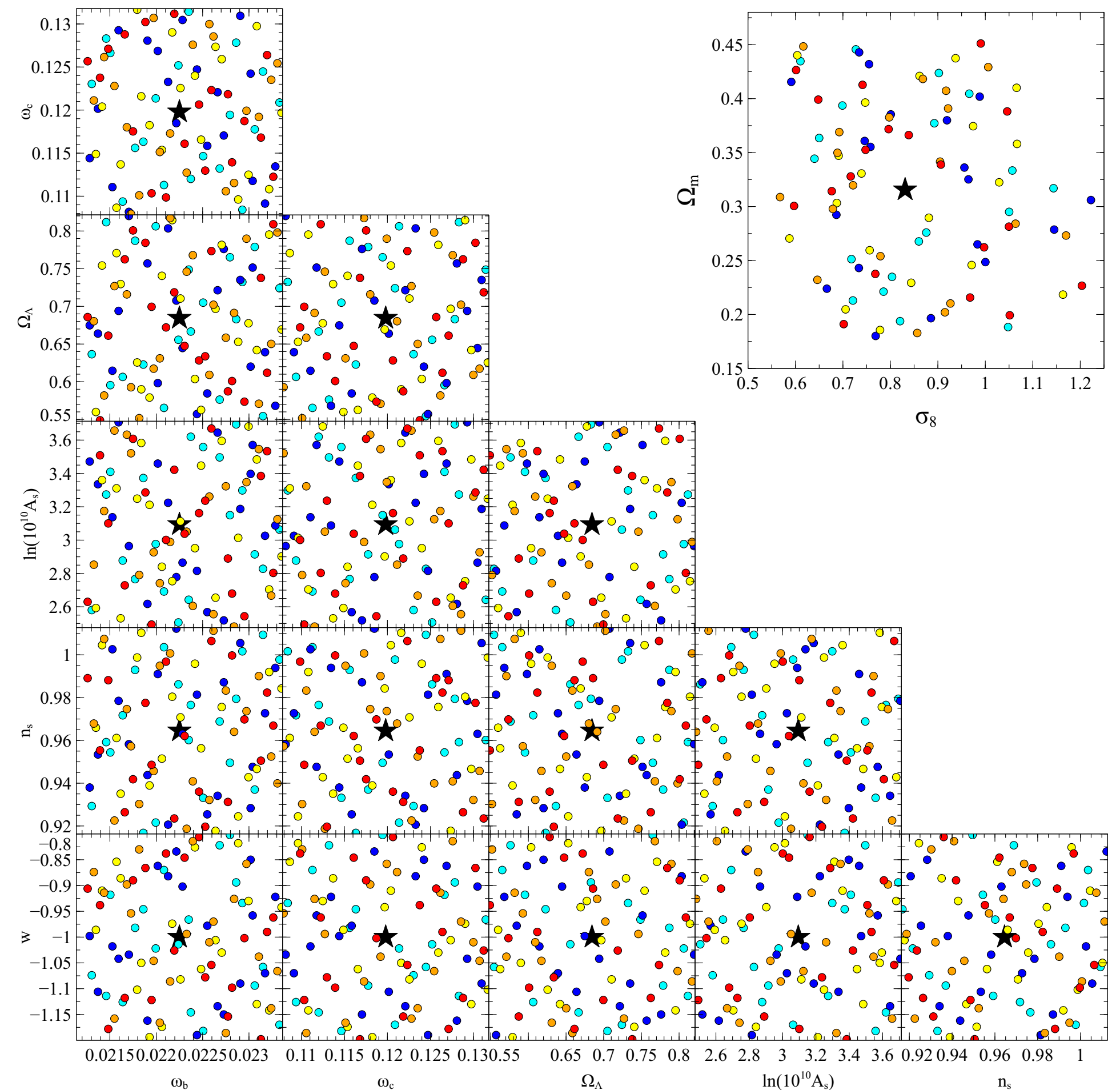
**Uncertainties between galaxy-halo connection**  
Analytical convolution of HOD and marginalize  
over the HOD parameters

# Dark Emulator: accurate non-linear model



T. Nishimichi (Kyoto)

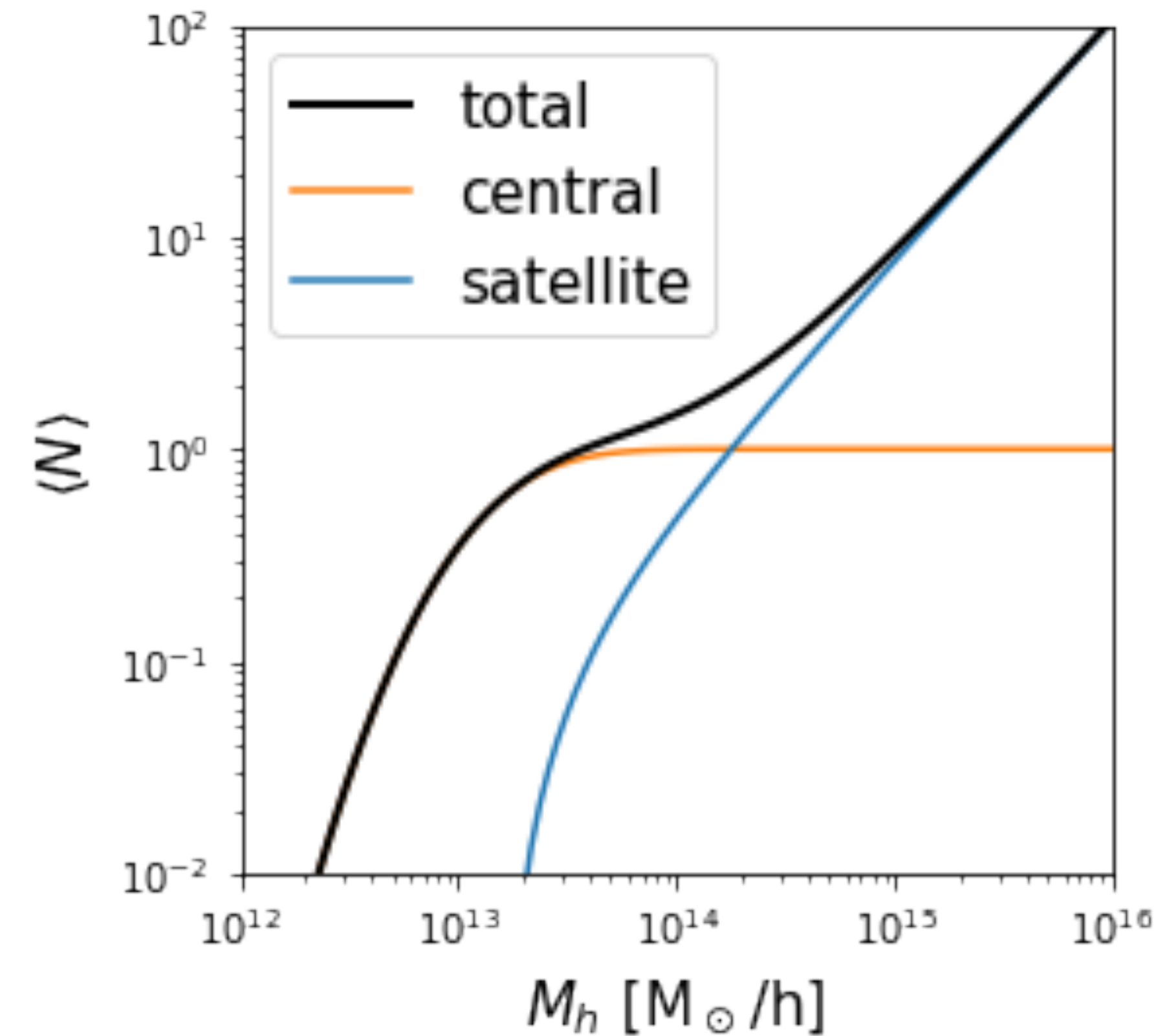
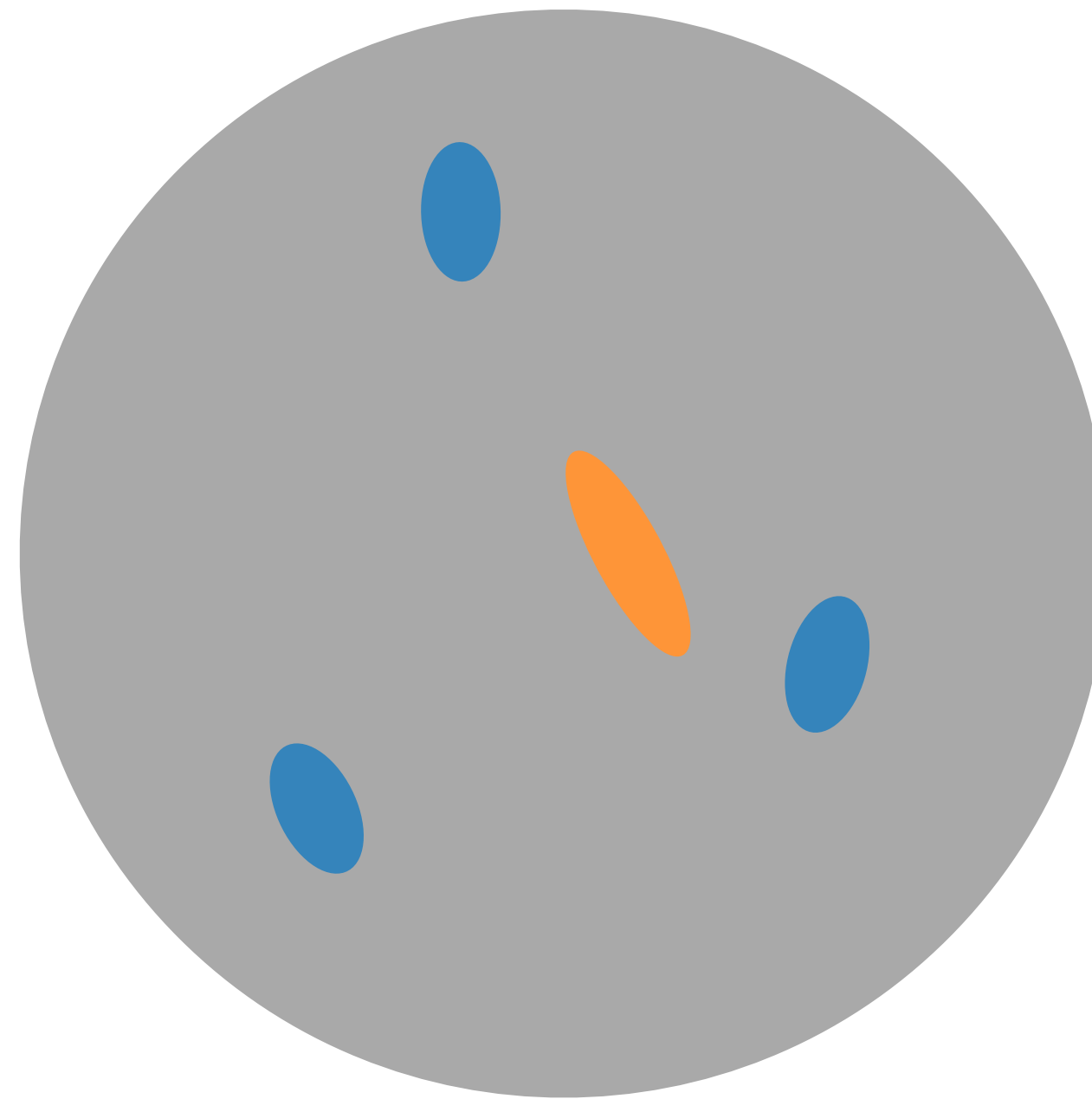
- Run N-body simulations under 101 sets of cosmological parameters.  
 $\vec{C} = (\omega_b, \omega_c, \Omega_\Lambda, A_s, n_s, w)$
- Run the Rockstar halo finder.
- Measure correlation functions, i.e.,  $\xi_{hh}(r; \vec{C})$  and  $\xi_{hm}(r; \vec{C})$ .
- Interpolate correlation functions across the cosmological parameter sets using PCA and Gaussian process.
- Achieved an accuracy for  $\xi_{hh}(r; \vec{C})$  and  $\xi_{hm}(r; \vec{C})$  better than 2%.
- **Unique cosmic emulator with halo statistics**



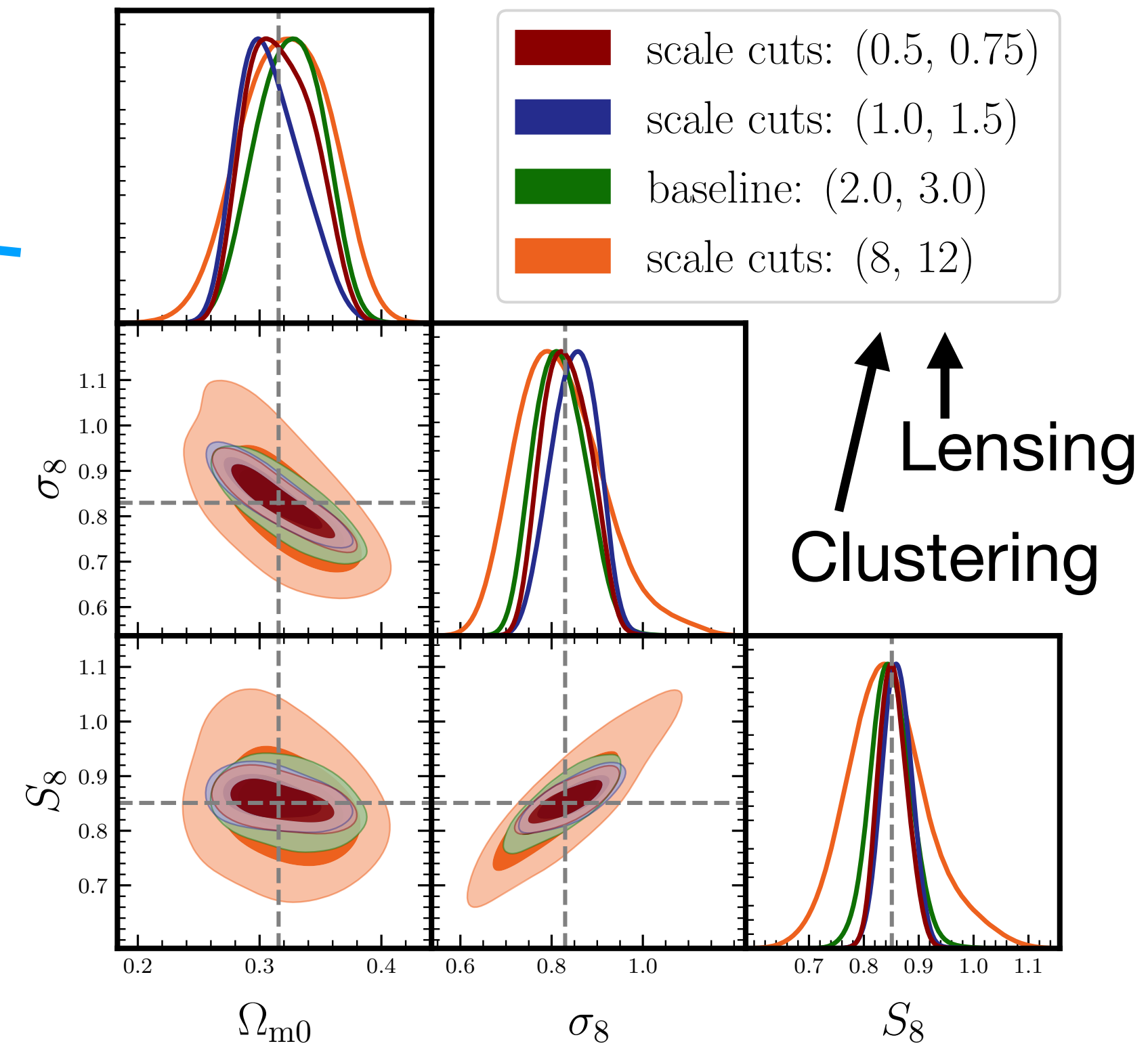
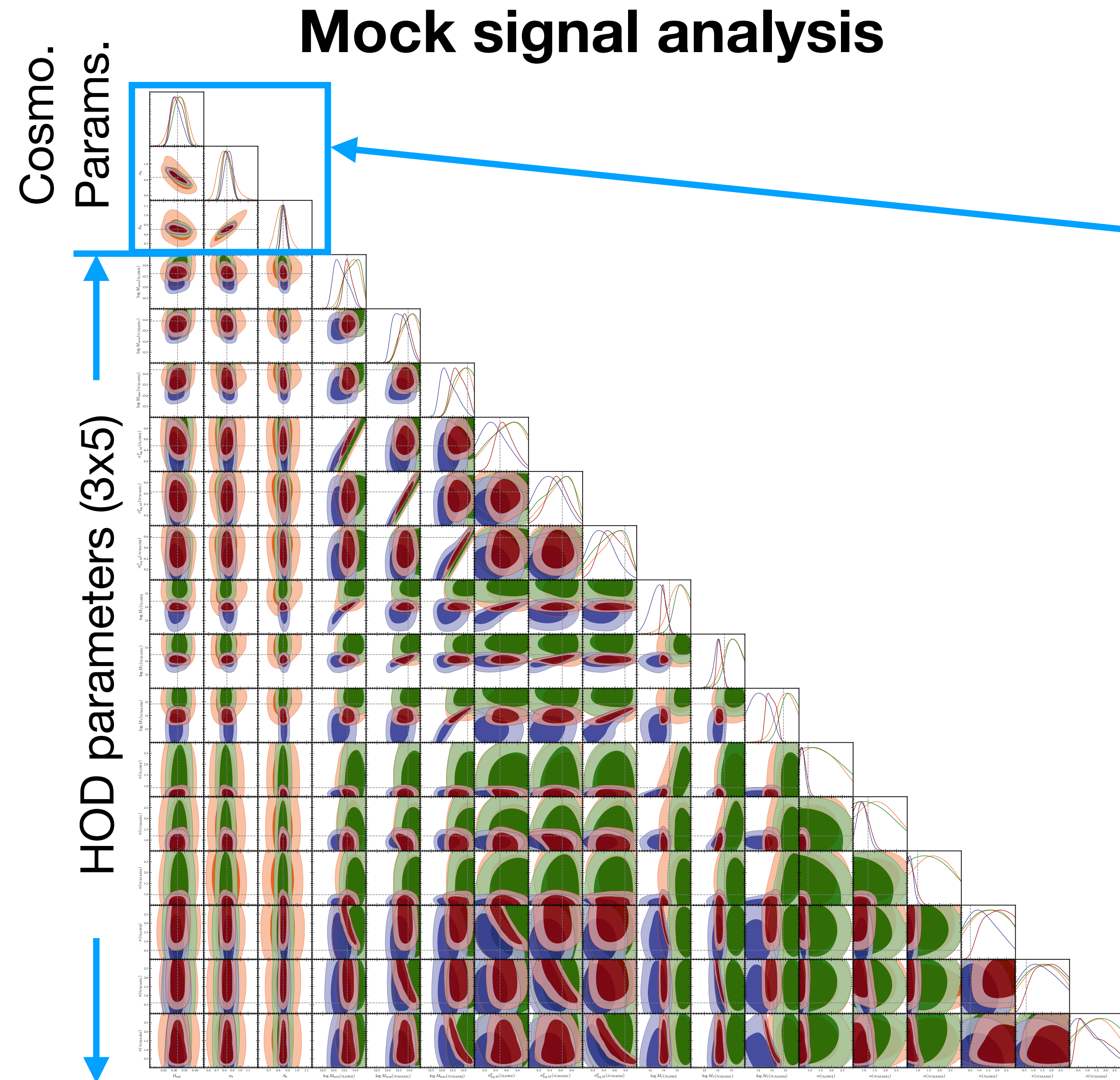


# Galaxy-halo connection

- Use halo occupation distribution (HOD; 5 parameters) to distribute galaxies in a dark matter halo.
- Take into account the uncertainties in galaxy physics by marginalizing HOD parameters.



# Information Content in Small Scales



We cannot extract information from scales less than  $\sim 2$  Mpc/h because of the HOD marginalization.

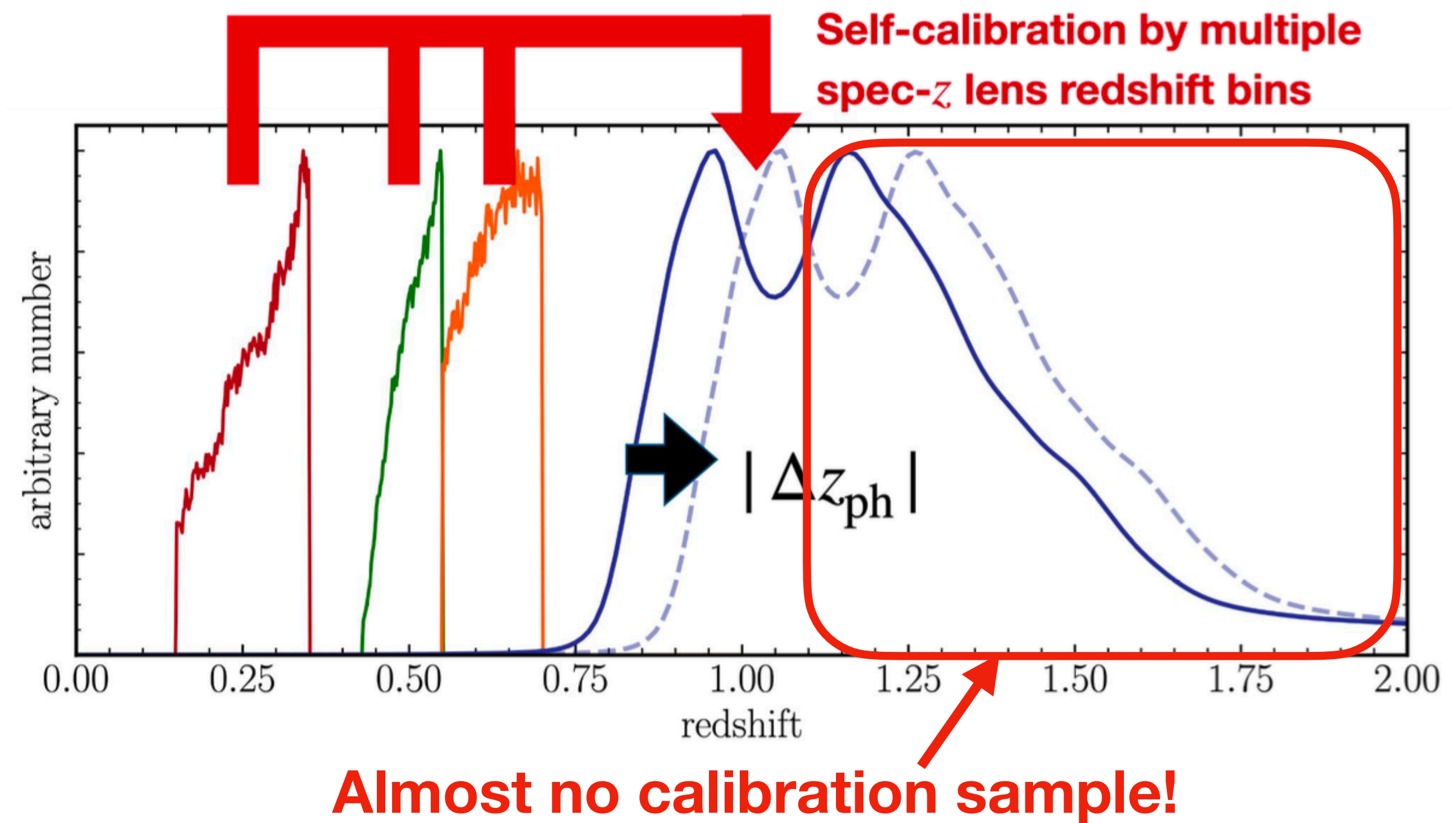
# Systematics: Redshift Uncertainties

- Bias in a lens or source redshift causes systematic bias in lensing signal.
- When using a spectroscopic sample for lenses, there is no bias in lens redshift.
- For source galaxies, photometric redshift (photo-z) is used, so we should always care about bias.
- When using a spectroscopic sample for lenses we only care about **mean** of source redshifts.

$$\begin{aligned}\langle \gamma \rangle &= \langle \Sigma_{\text{cr}}(z_l, z_s)^{-1} \Delta \Sigma(z_l) \rangle \\ &= 4\pi G(1 + z_l)^{-2} \chi_l \left[ 1 - \chi_l \left\langle \frac{1}{\chi_s} \right\rangle \right] \Delta \Sigma(z_l)\end{aligned}$$

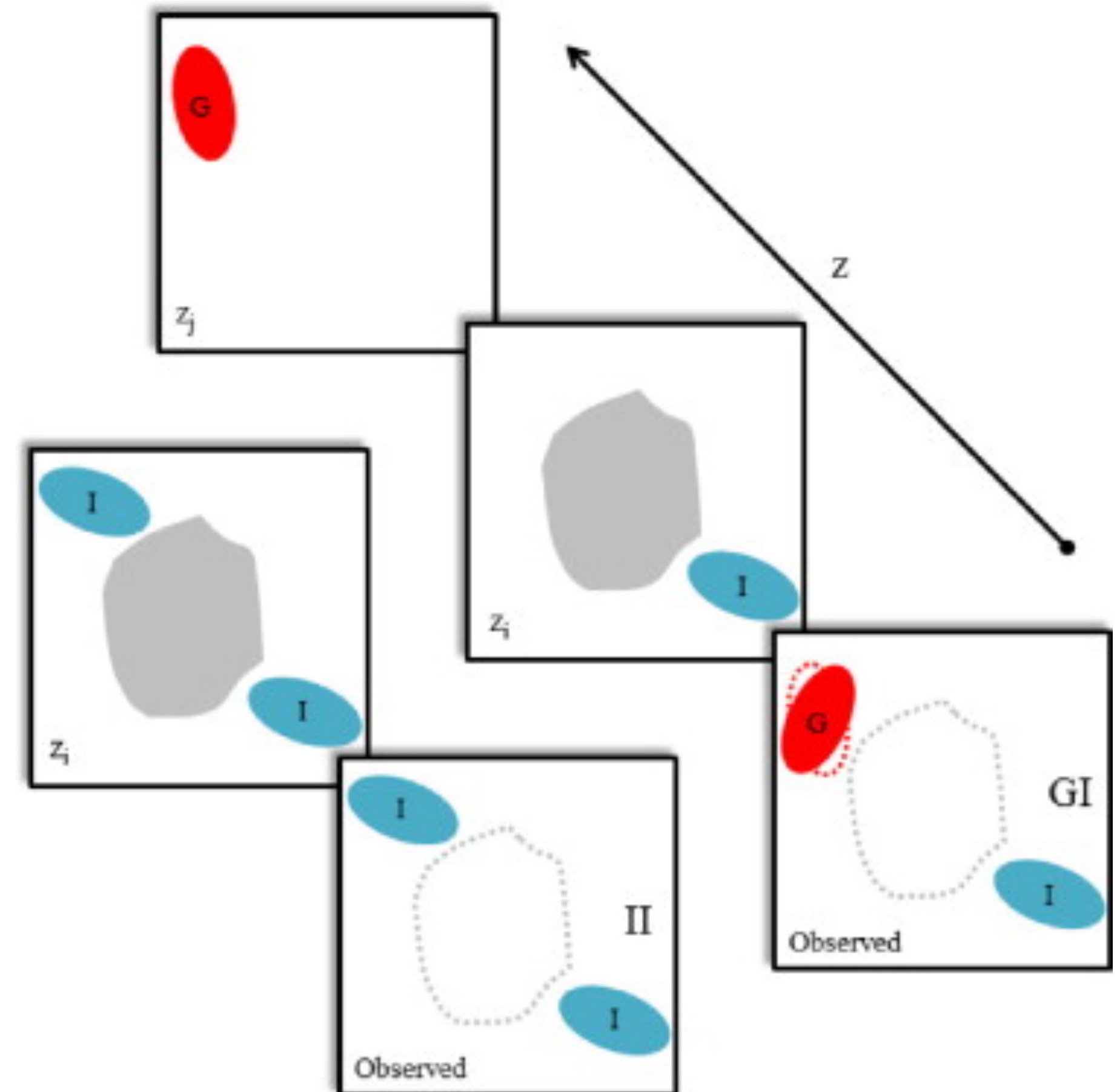
# An Extreme Case: HSC-Y3

- We had almost no calibration sample except for COSMOS 30-band photo-z at  $z > 1.1$ .
- We decided to use a flat prior  $\Pi(\Delta z_{\text{ph}}) = \mathcal{U}(-1, 1)$ , and self-calibrate by using multiple lens samples (Oguri & Takada, 2011).
- $\Delta z_{\text{ph}} = -0.05 \pm 0.09$
- If we fix  $\Delta z_{\text{ph}}$ , our  $S_8$  constraint is shifted by  $0.5\sigma$ .
- Downside: the error on  $S_8$  is doubled once we use the flat prior.



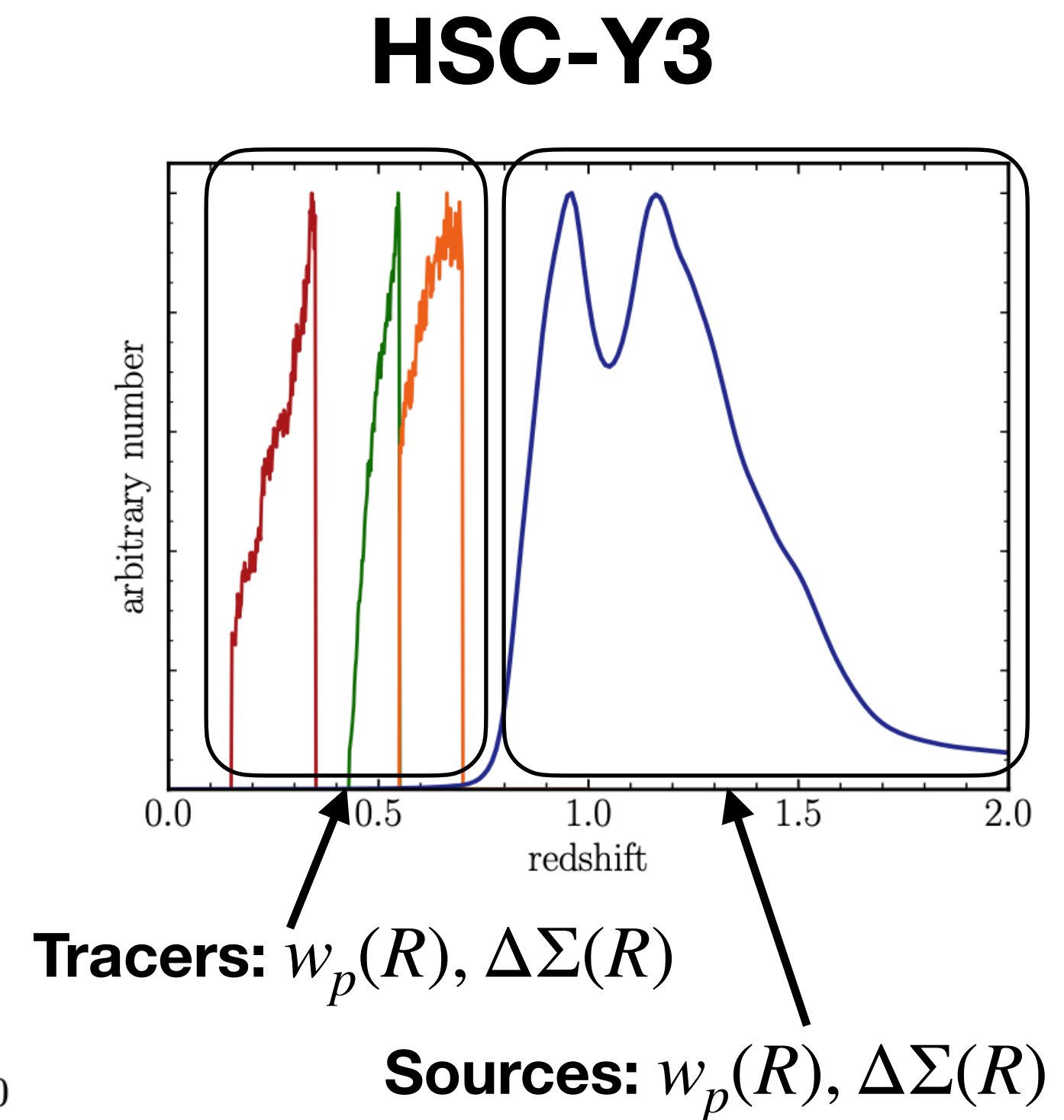
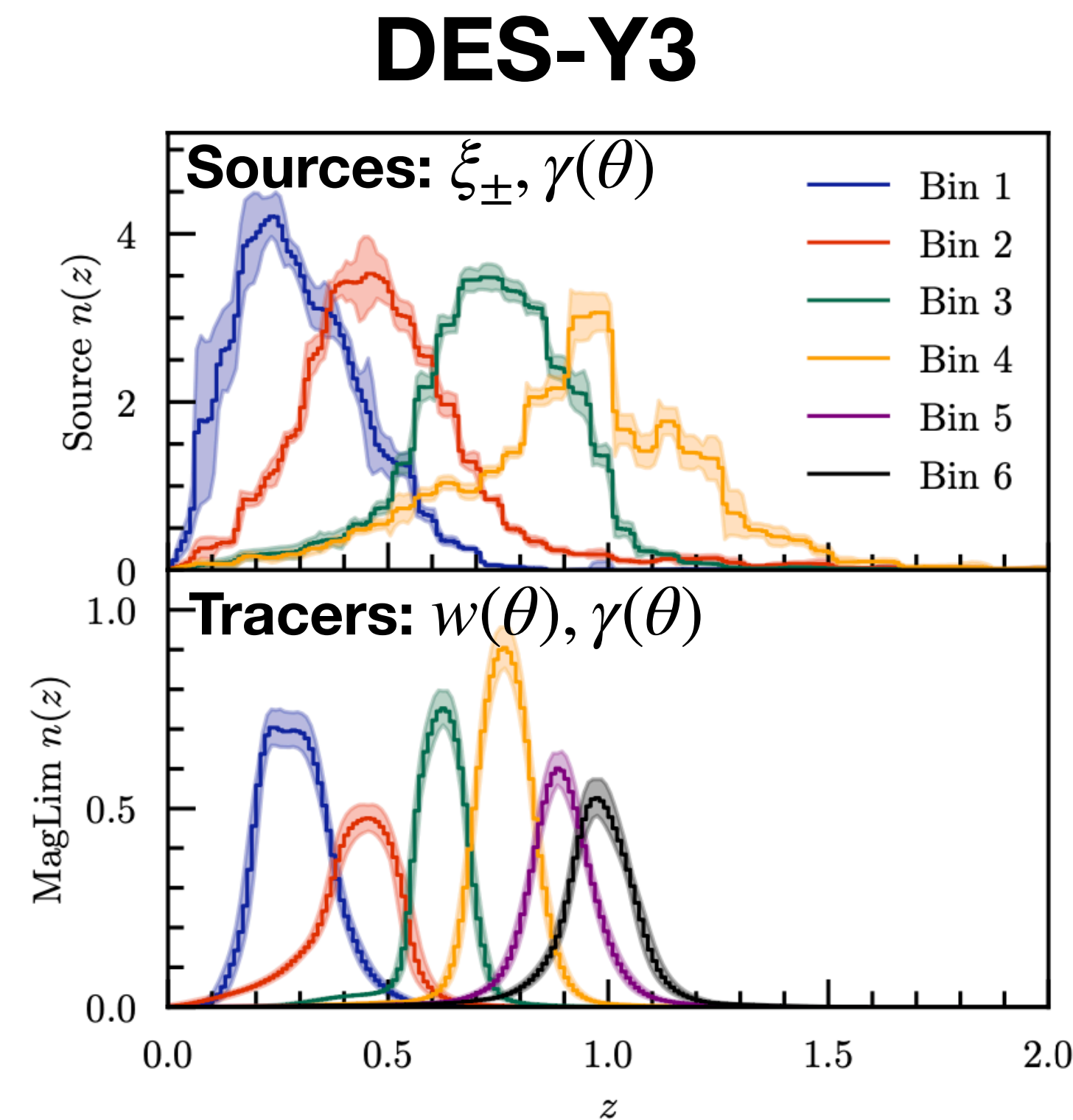
# Systematics: Intrinsic Alignment

- Intrinsic shape of galaxies is affected by the tidal forces of a dark matter structure.
- There are two terms: II and GI.
- Both II and GI cause a systematic bias in cosmic shear (GI is dominant).
- II causes a systematic bias in galaxy-galaxy lensing.
- There are two models
  - NLA: Assumes galaxies linearly align with the tidal field.
  - TATT: Uses nonlinear perturbation theory to expand the field of intrinsic galaxy shapes interns of the tidal field and matter overdensity.



# Intrinsic Alignment in Stage-III Surveys

- For cosmic shear, all surveys incorporated IA in their models.
- For galaxy-galaxy lensing, DES and KiDS incorporated IA in their models, but HSC not, due to the use of spectroscopic galaxies as a tracer and conservative selection for source galaxies.



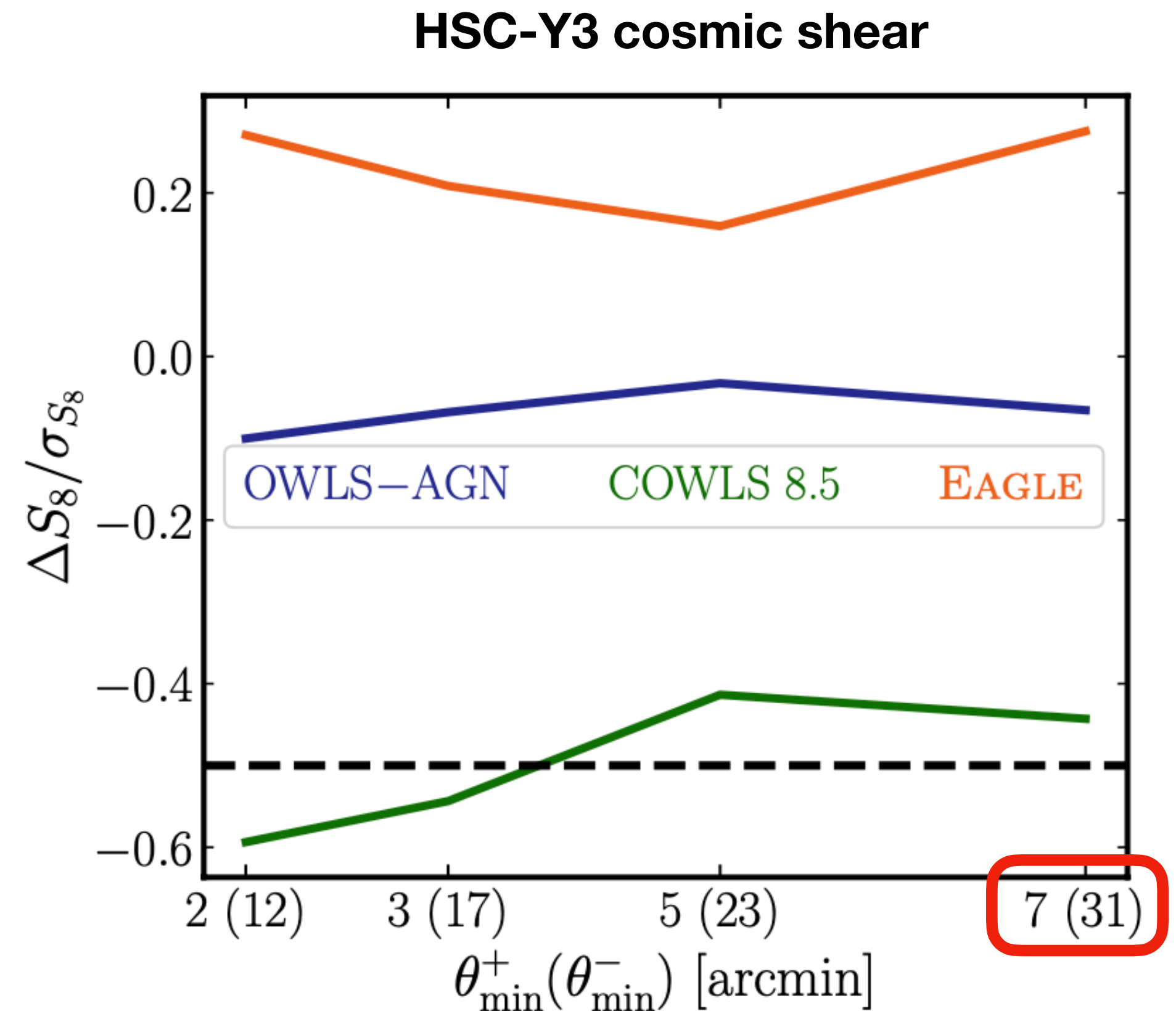
# Intrinsic Alignment in Stage-III Surveys

	<b>DES-Y3</b> DES collaboration (2022)	<b>HSC-Y3</b> Sugiyama et al. (2023) Miyatake et al. (2023)	<b>KiDS-1000</b> Heymans et al. (2021)
<b>NLA</b>	No IA detection	No IA detection	3 sigma detection Did not affect $S_8$ constraint ( $\sim 0.1\sigma$ ).
<b>TATT</b>	Fiducial No IA detection	N/A	N/A

**Note: HSC tomographic cosmic shear analyses (Dalal et al, 2023; Li et al, 2023) adopted TATT as fiducial, did not detect IA, and  $S_8$  constraints were not affected.**

# Systematics: Baryonic Effect

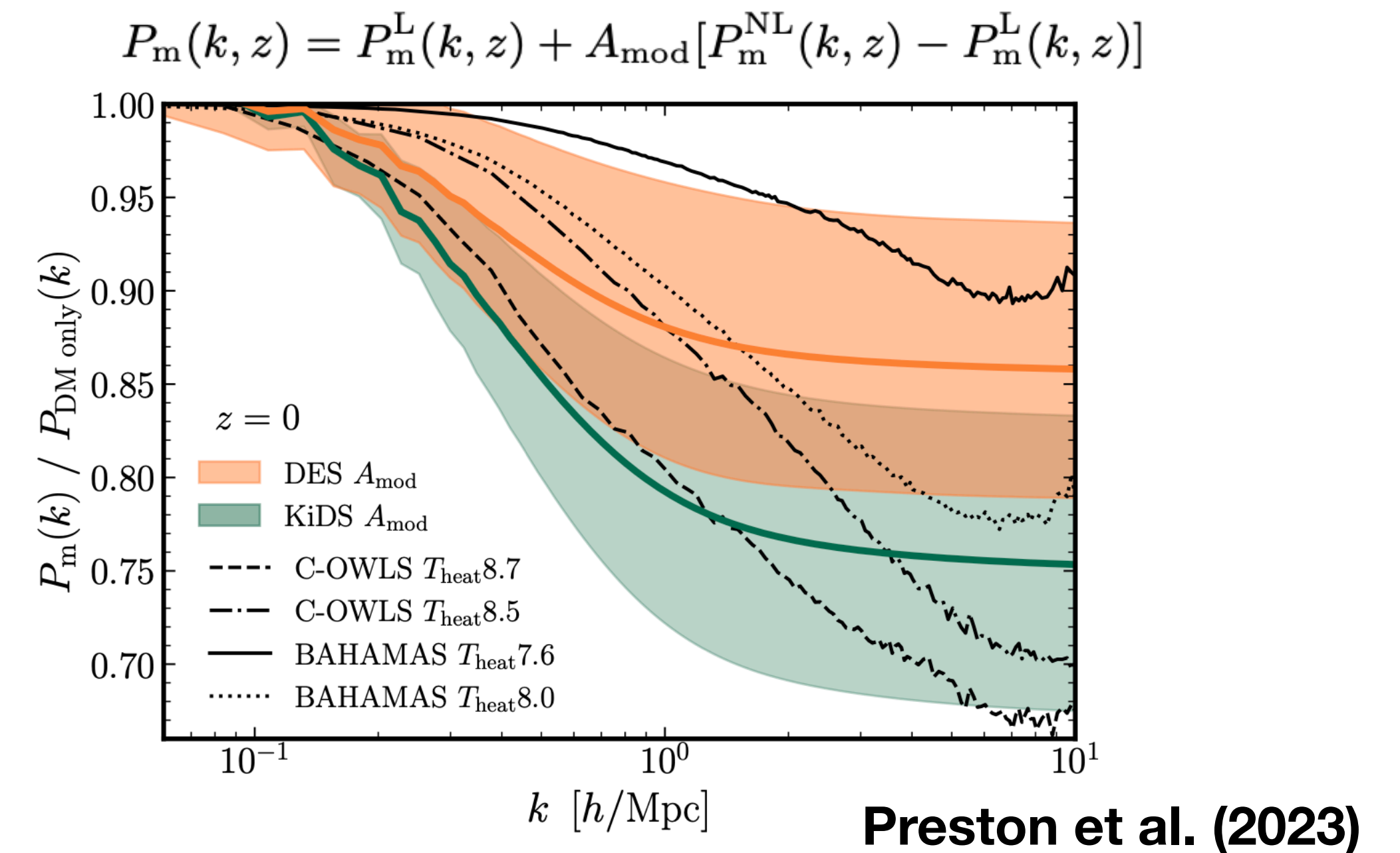
- AGN feedback pushes matter away from halo center and modifies small scale signals.
- Scale cut for small scales in cosmic shear measurements is applied to avoid scales affected by AGN feedback.





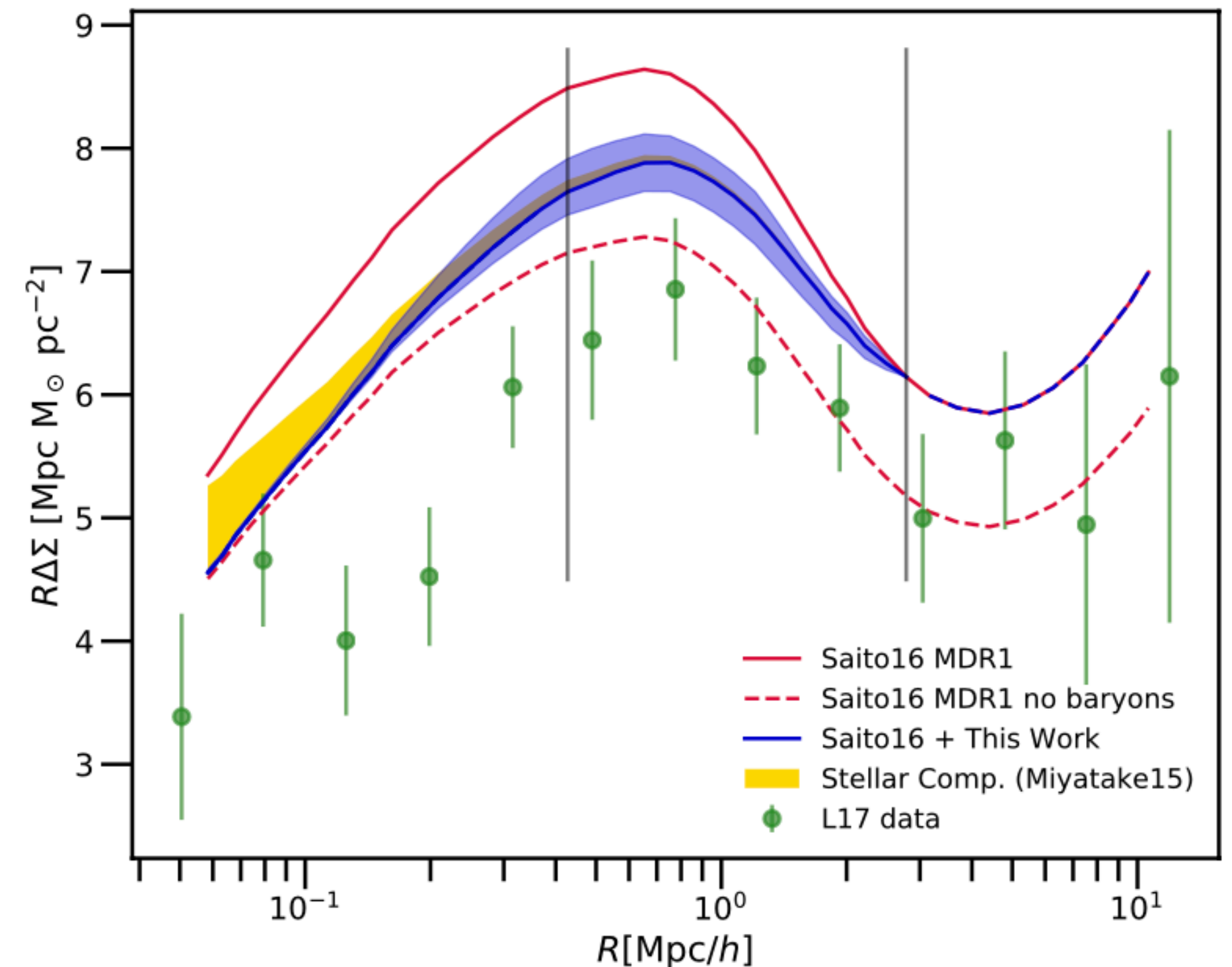
# Baryonic Effect on Cosmic Shear

- To recover Planck  $S_8$  from DES and KiDS cosmic shear including small scales (data points outside of scale cuts), AGN feedback is required to extend to mildly non-linear scale ( $k \sim 0.2$  h/Mpc).
- It may be unrealistic to explain the  $S_8$  tension only by Baryonic effect.



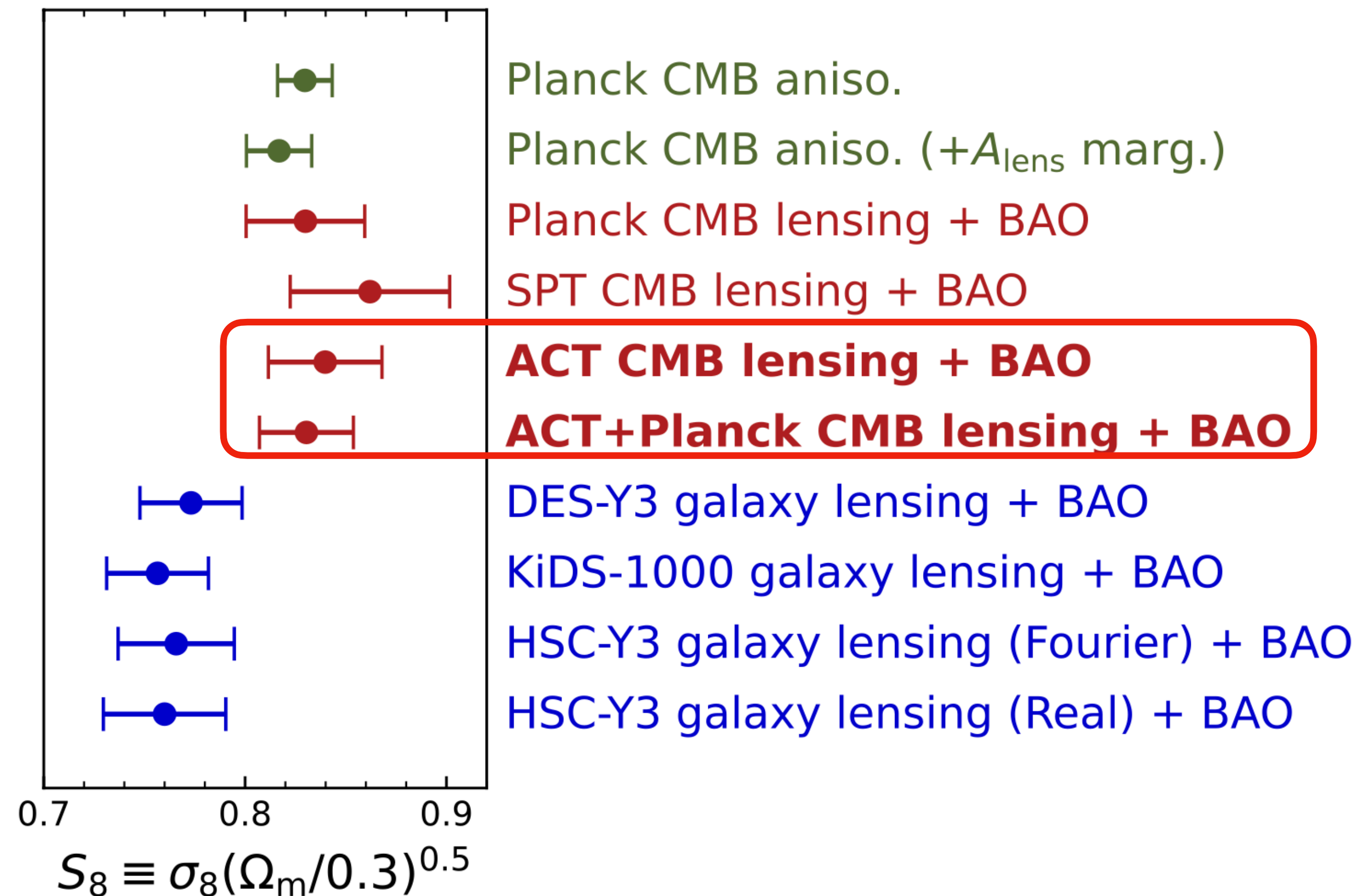
# Baryonic Effect on Galaxy-galaxy Lensing

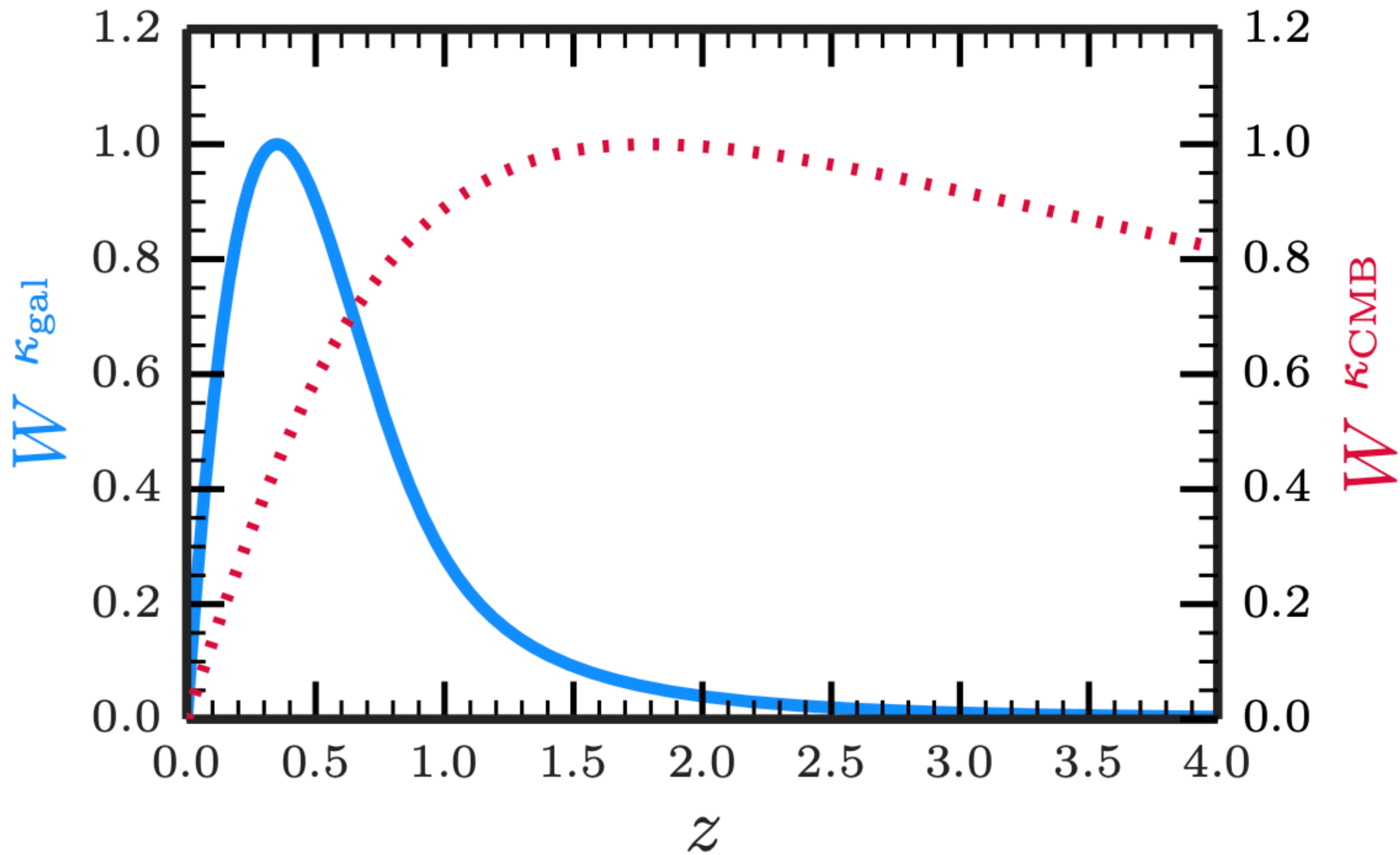
- ACT measured AGN feedback around CMASS sample through kSZ and tSZ signals.
- They also found large AGN feedback up to  $\sim 3$  Mpc/h in lensing signal.
- HSC-Y3 scale cut ( $R > 3$  Mpc/h) safely avoids the small scales affected by AGN feedback.
- Better to use  $\Delta\Sigma(R)$  than  $\gamma(\theta)$  to avoid mixing in angular scales.

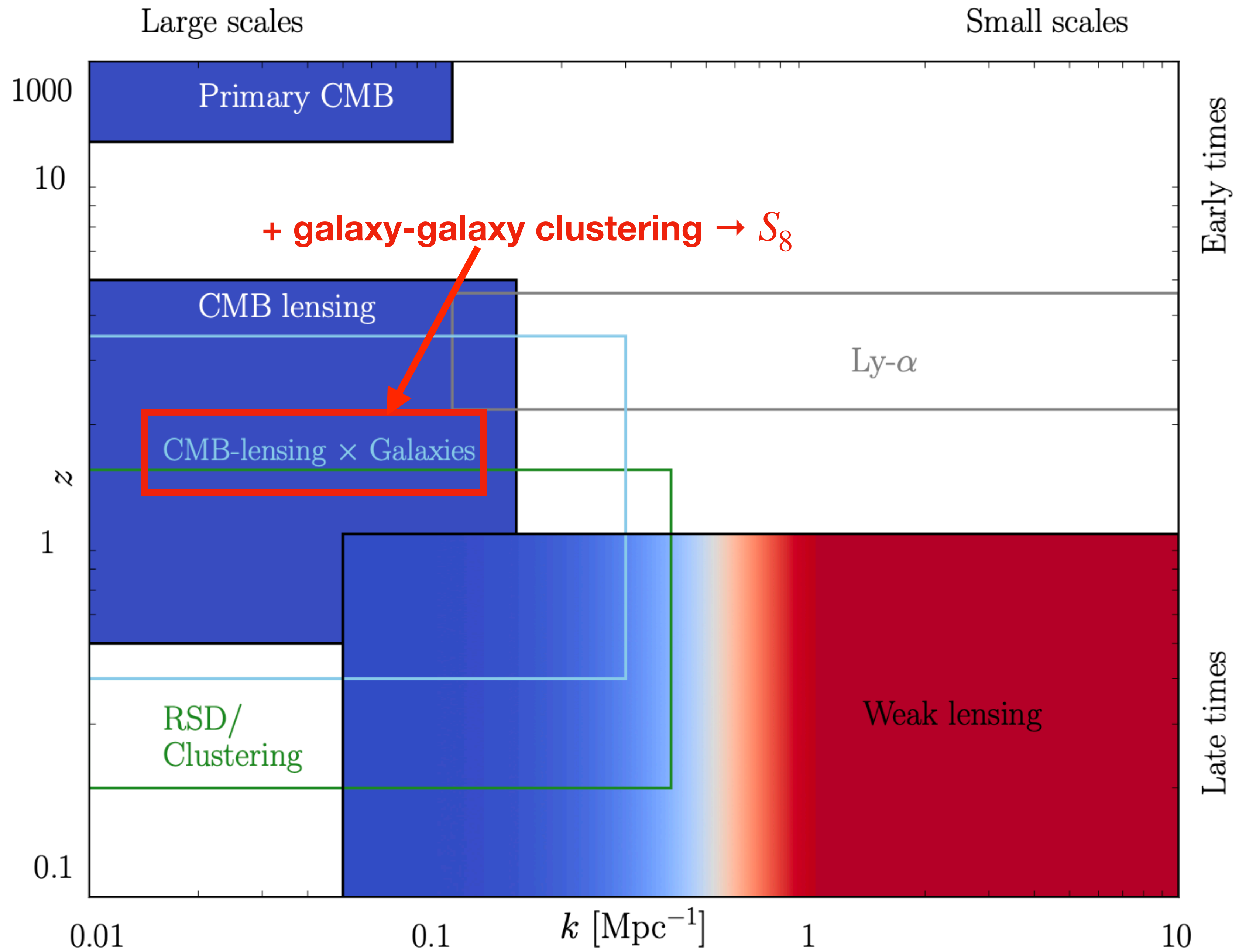


Amodeo et al. (2021)

# $S_8$ Tension Updated

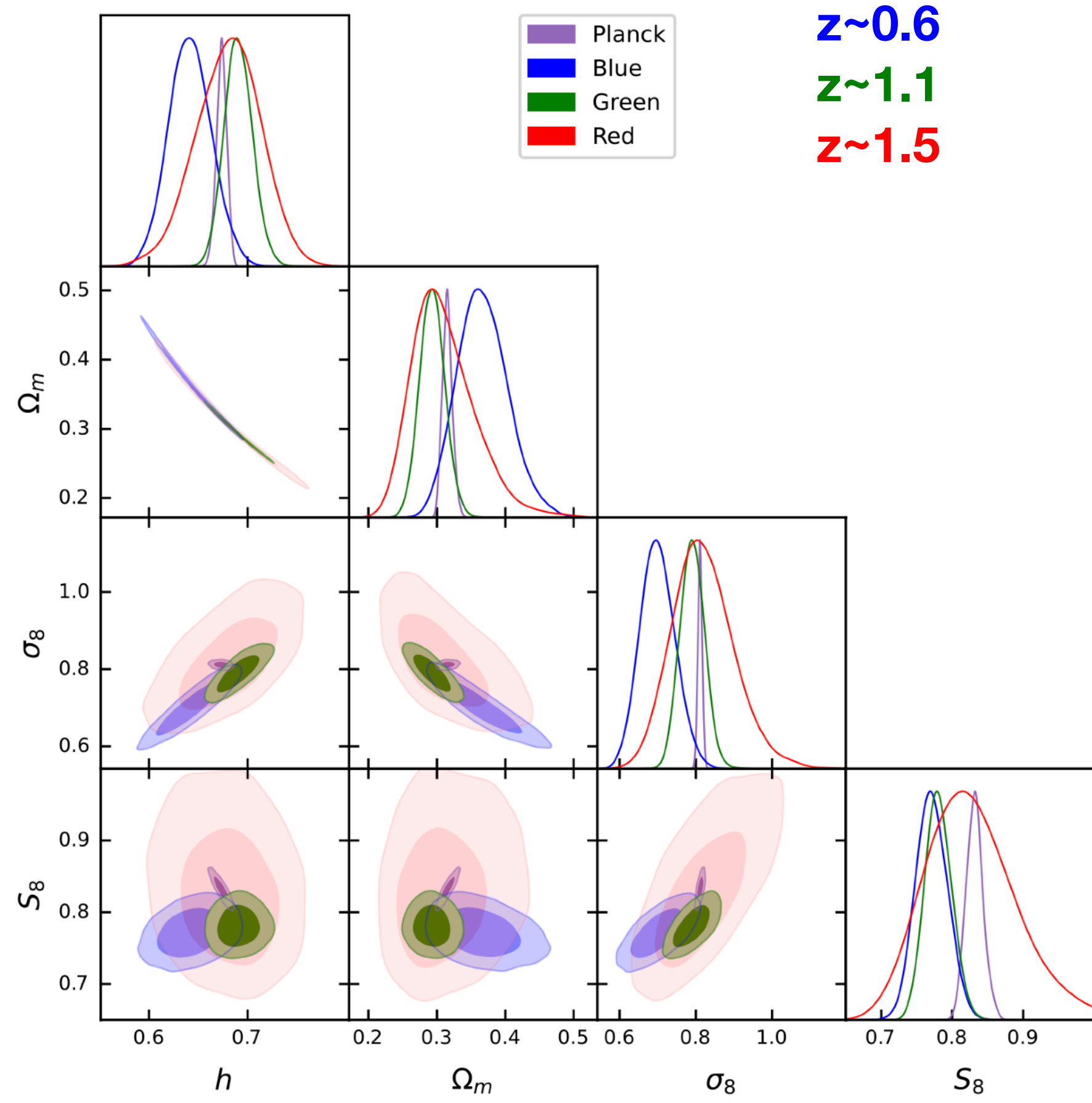






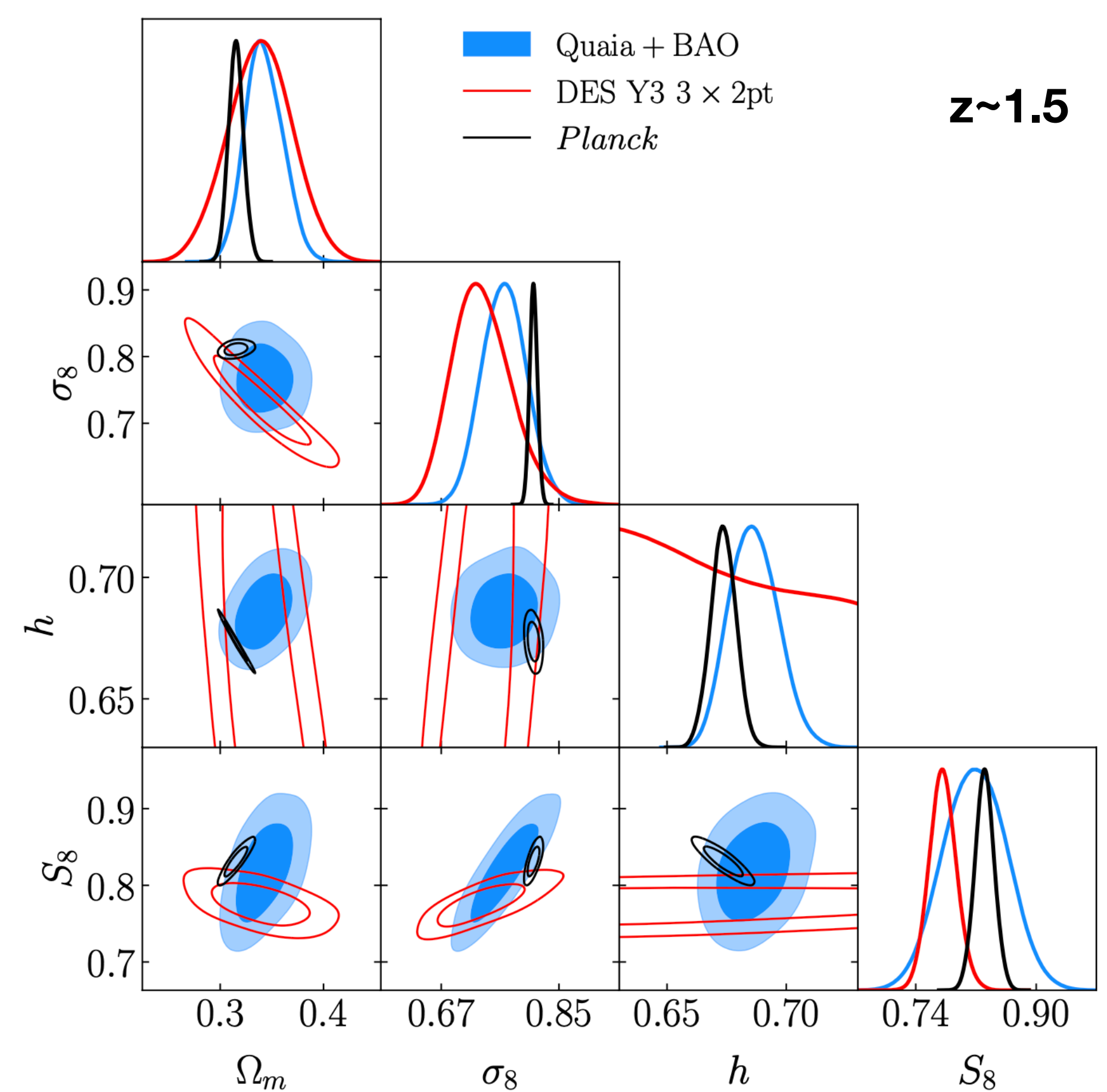
# Recent Galaxy x CMB-lensing Studies

unWISE galaxies x Planck



Krolewski (2021)

Gaia-unWISE quasars x Planck

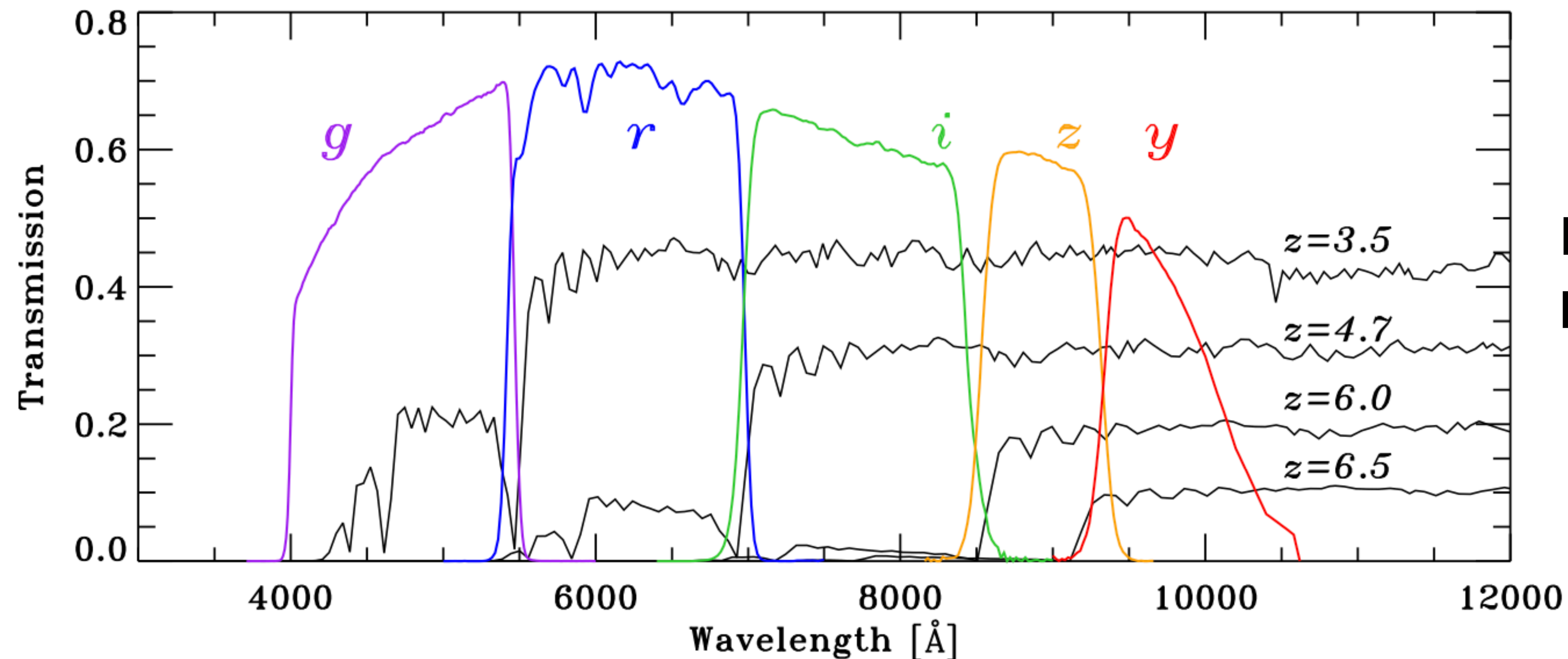


Alonso et al. (2023)

**Going beyond  $z > 2$ !**

# Selecting High-z Galaxies: Dropout Technique

- Broadband photometry can capture the Lyman break at  $912\text{\AA}$ .
- Selecting distant galaxies with Lyman break is called dropout technique, and these galaxies are called **Lyman break galaxies (LBG)**.

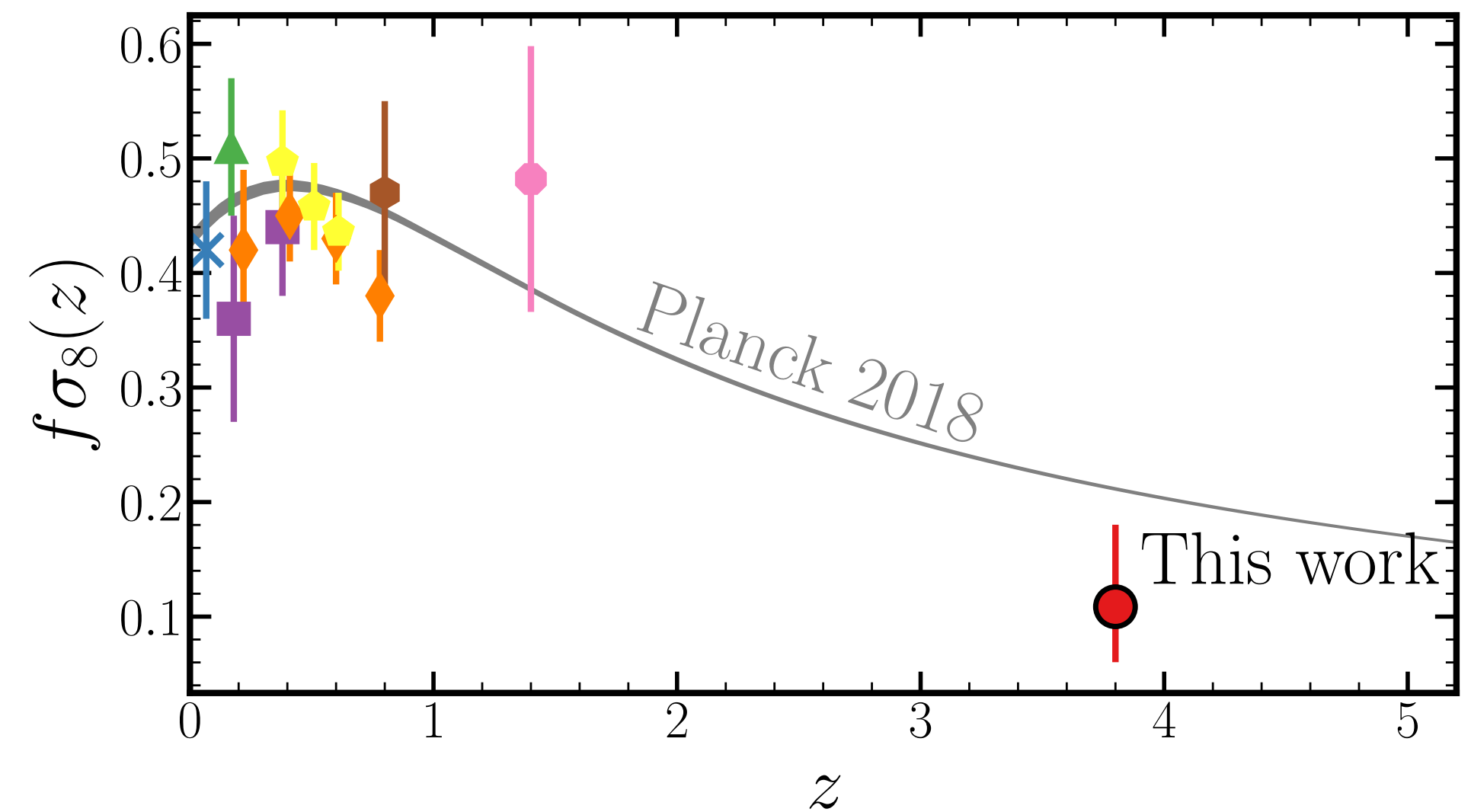
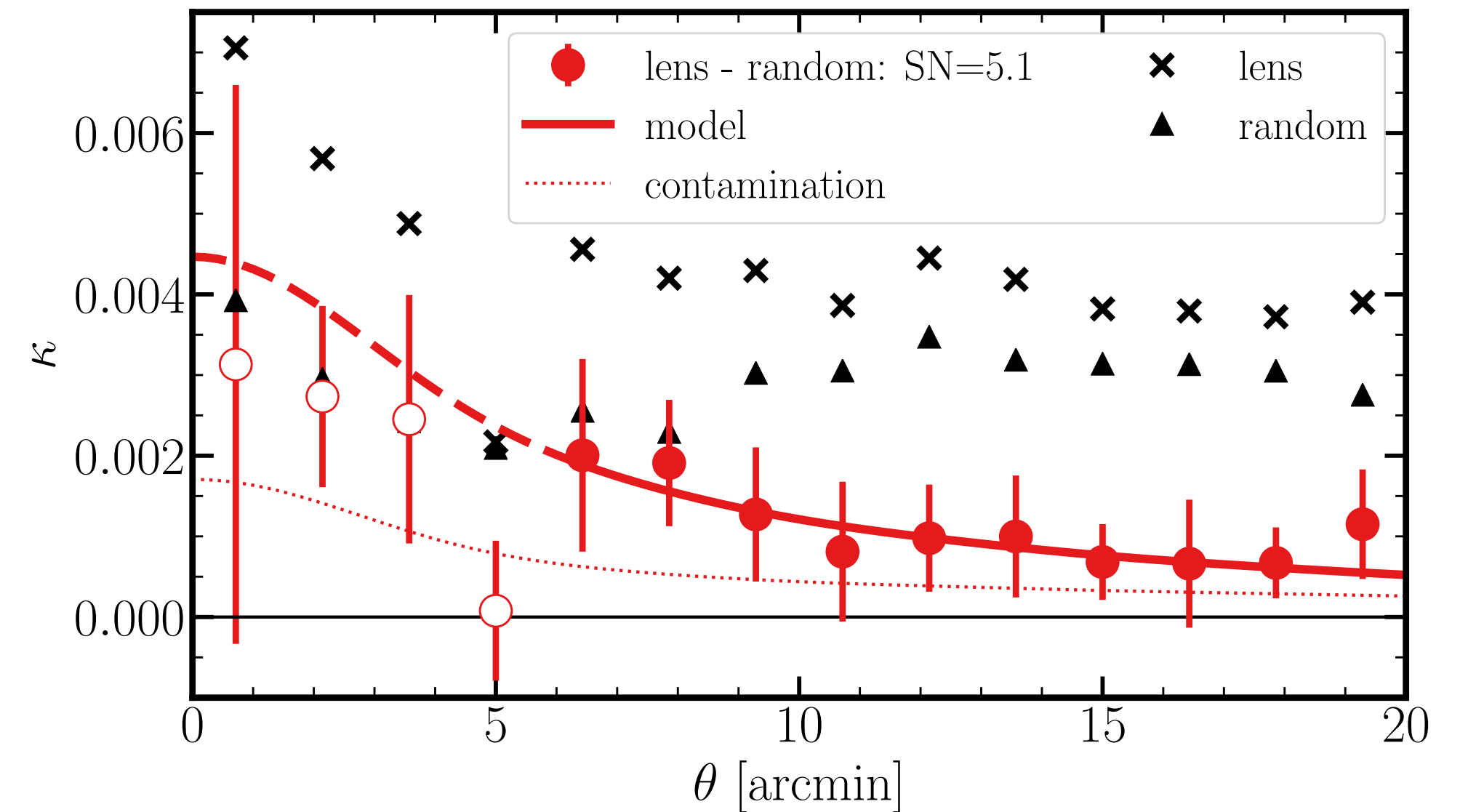


**Note: u-dropout provides  $z\sim 2.5$  galaxies**



# LBG x Planck CMB Lensing

- $\sim 1.5\text{M}$  LBG galaxies over  $300 \text{ deg}^2$  of HSC field.
- Stacked Planck lens map behind LBGs
- Contamination from low- $z$  galaxies is quantified by WL measurements with HSC.
- Obtained  $3.5\sigma$  significance against the contamination signal.



# The Future

## Near future (in 2-3 years)

- The HSC LBG sample will be tripled with the final HSC data.
- ACT DR6 has a large overlap with HSC. Noise level is 5 x smaller than Planck.

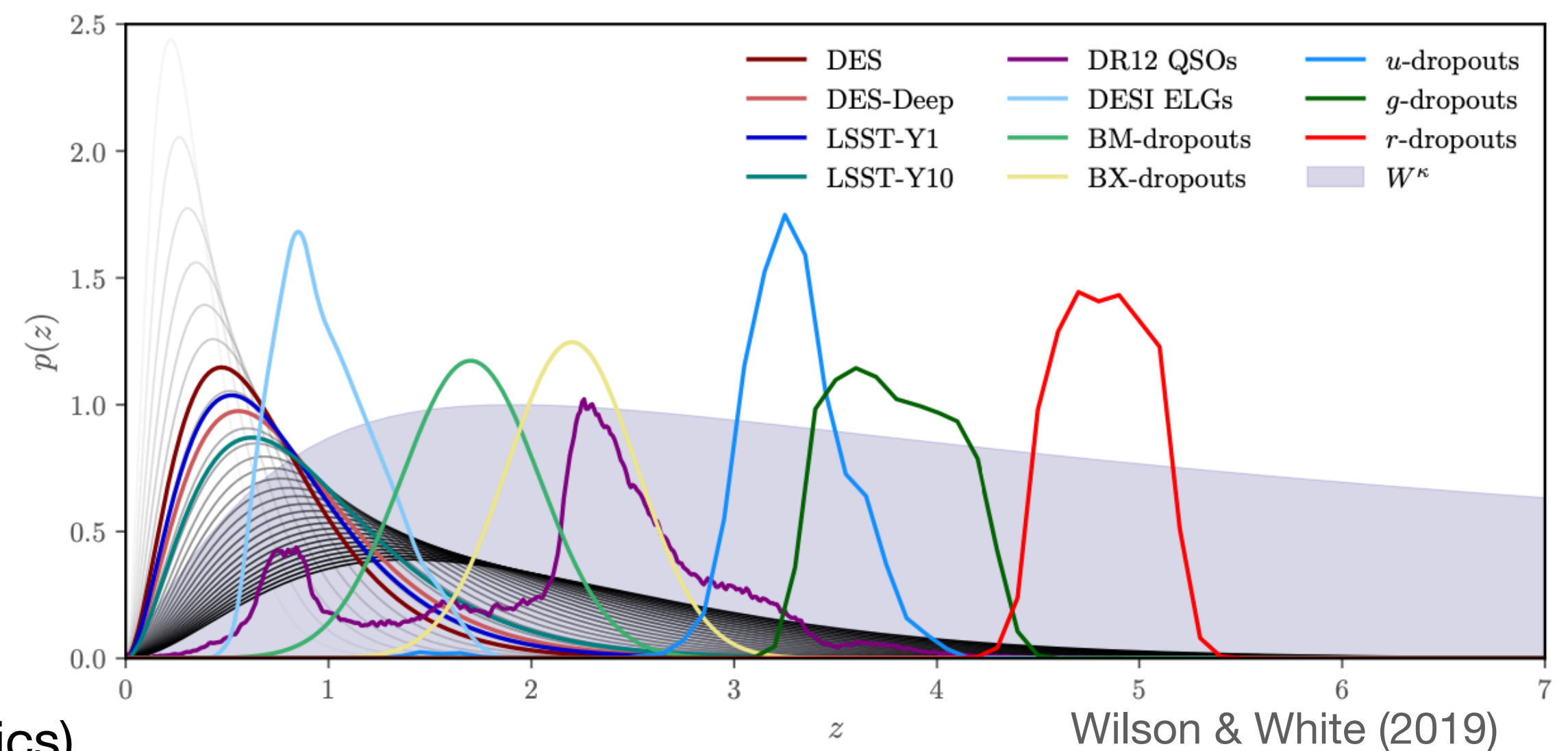
➡ **S/N ~ 15**

## Future (beyond 2-3 years)

- More galaxies from upcoming imaging surveys, according to Wilson & White (2019), for Rubin
  - $z \sim 3$  dropouts:  $4 \times 10^7$  galaxies
  - $z \sim 4$  dropouts:  $10^8$  galaxies
  - $z \sim 5$  dropouts:  $2 \times 10^7$  galaxies
- CMB-S4: 30 x smaller noise level compared to Planck.

➡ **S/N ~ 200**

(Can be optimistic since we need to deal with systematics)



# Systematics to consider

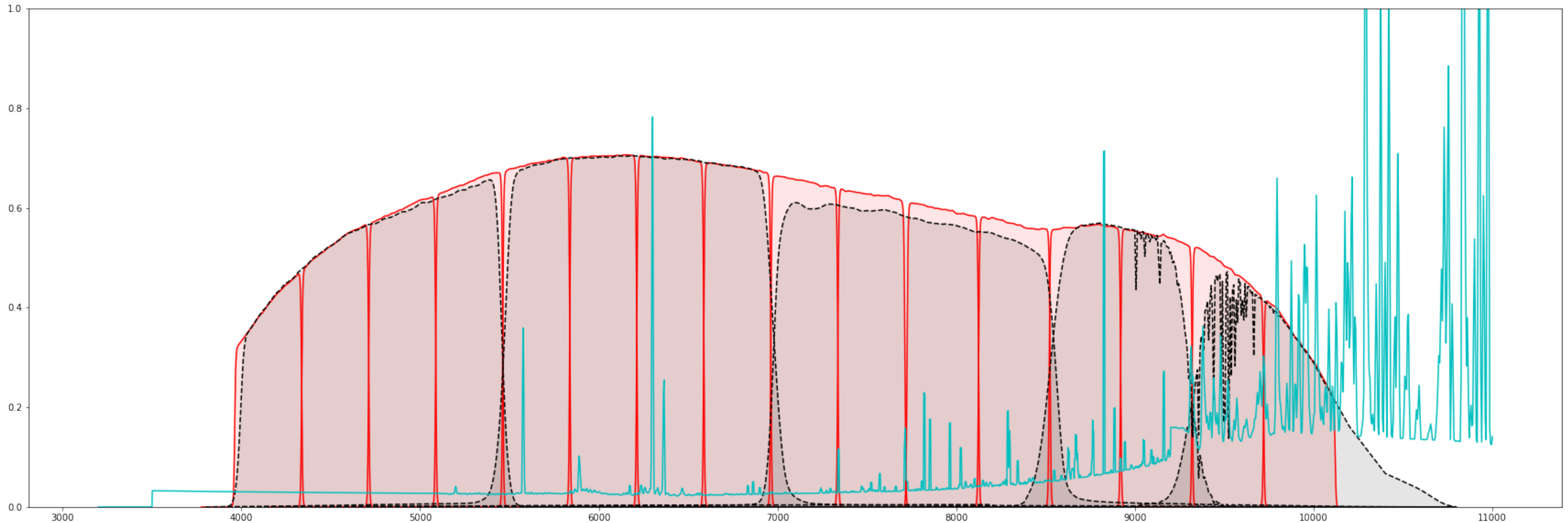
Severeness

- Redshifts/contaminations
  - Majority of contaminations are in low redshift: misidentification of  $4000\text{\AA}$  break as Lyman break.
  - But the redshift distribution should be measured for precision cosmology.
  - Currently we have  $\sim 1000$  spec-zs. PFS, MSE and MegaMapper should help. See next slide for a medium-band survey.
  - For the CMB lensing signal, contaminations can be quantified by weak lensing.
- Cosmic Infrared Background (CIB)
  - CIB lowers CMB lensing signal.
- Magnification bias
  - Lens galaxies can be preferentially selected where LSS along the line-of-sight is prominent, which can cause magnification bias in the CMB lensing signal. We checked our measurement is not prone to magnification bias, but it should be revisited to carry out precision cosmology.

# HSC Medium-Band (MB) Filters

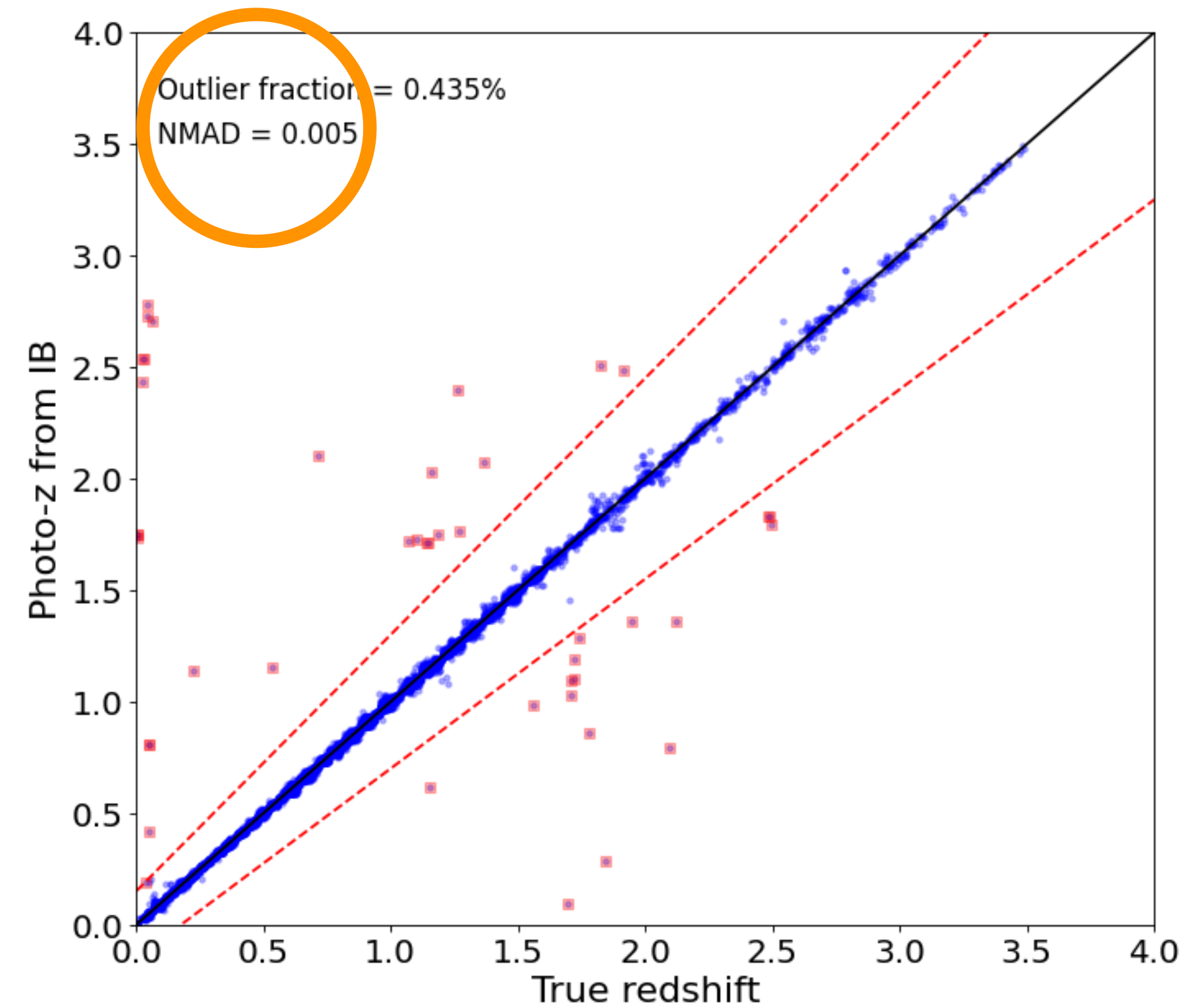
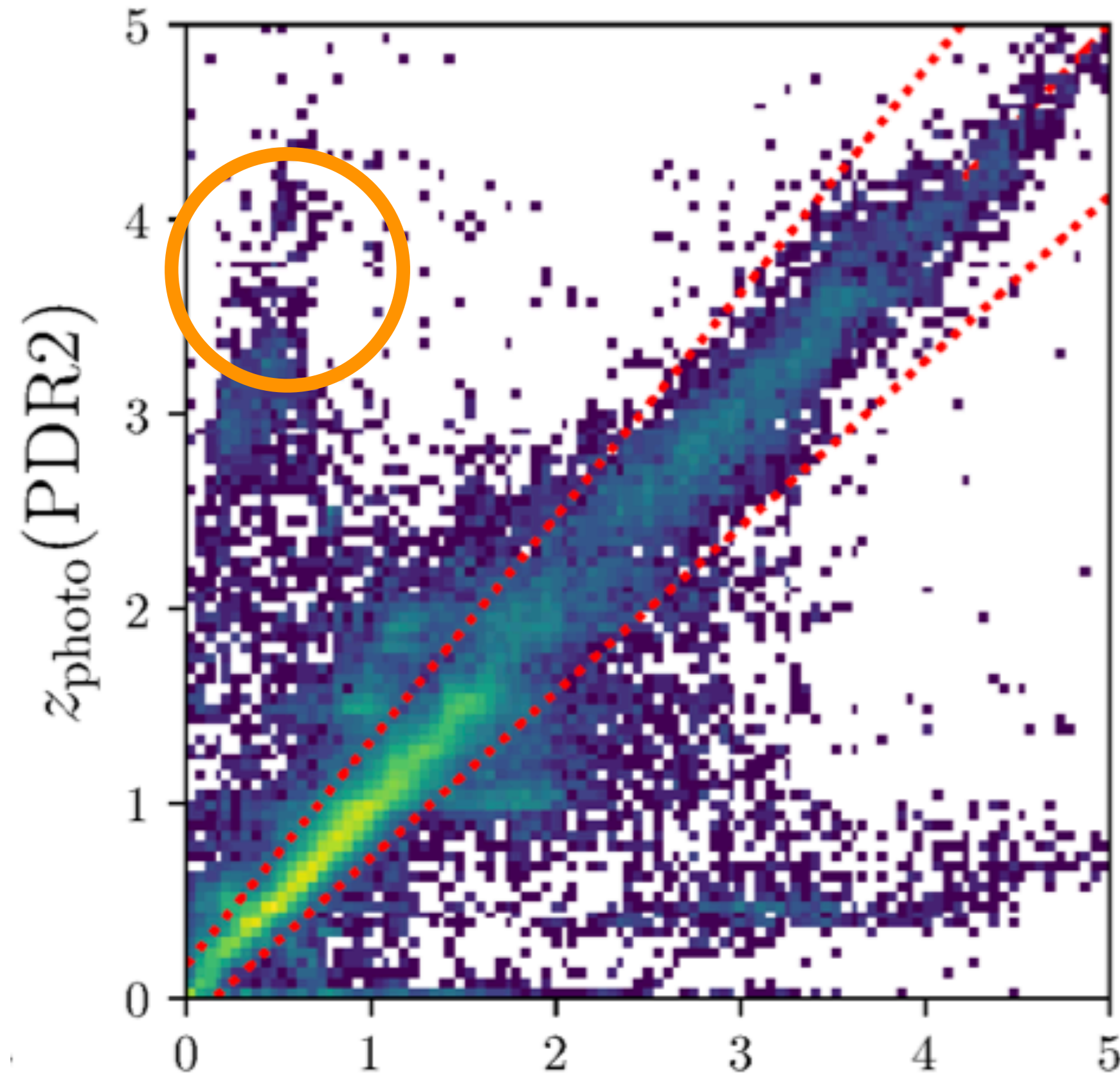


A. J. Nishizawa



- 16 or 20 medium-band (MB) filters that cover 4000-10000Å.
- Fabrication cost is funded (12 filters), and filters will be ready by S25A.

# Performance of MB Filters



MB filters can be used for calibration to remove contamination.

# Summary

- All the stage-III weak lensing surveys released intermediate results
  - Despite of different analysis choices, they consistently exhibit smaller  $S_8$  compared to primary CMB.
  - A number of systematics were carefully tested in their analyses and follow-up studies: non-linear regime, photo-z, intrinsic alignment, baryonic effect.
- ACT lensing showed  $S_8$  consistent with Planck primary CMB.
  - $S_8$  changes as a function of redshift?
  - In addition to the default science case of Stage-IV weak lensing surveys, where they measure large-scale structure at  $z < \sim 2$ , we should to go higher redshift using galaxy-CMB lensing cross correlations!

# Backup Slides

