

# Theoretical approaches to cosmic tensions

Tanvi Karwal



Understanding cosmological observations, Benasque

31<sup>st</sup> July, 2023

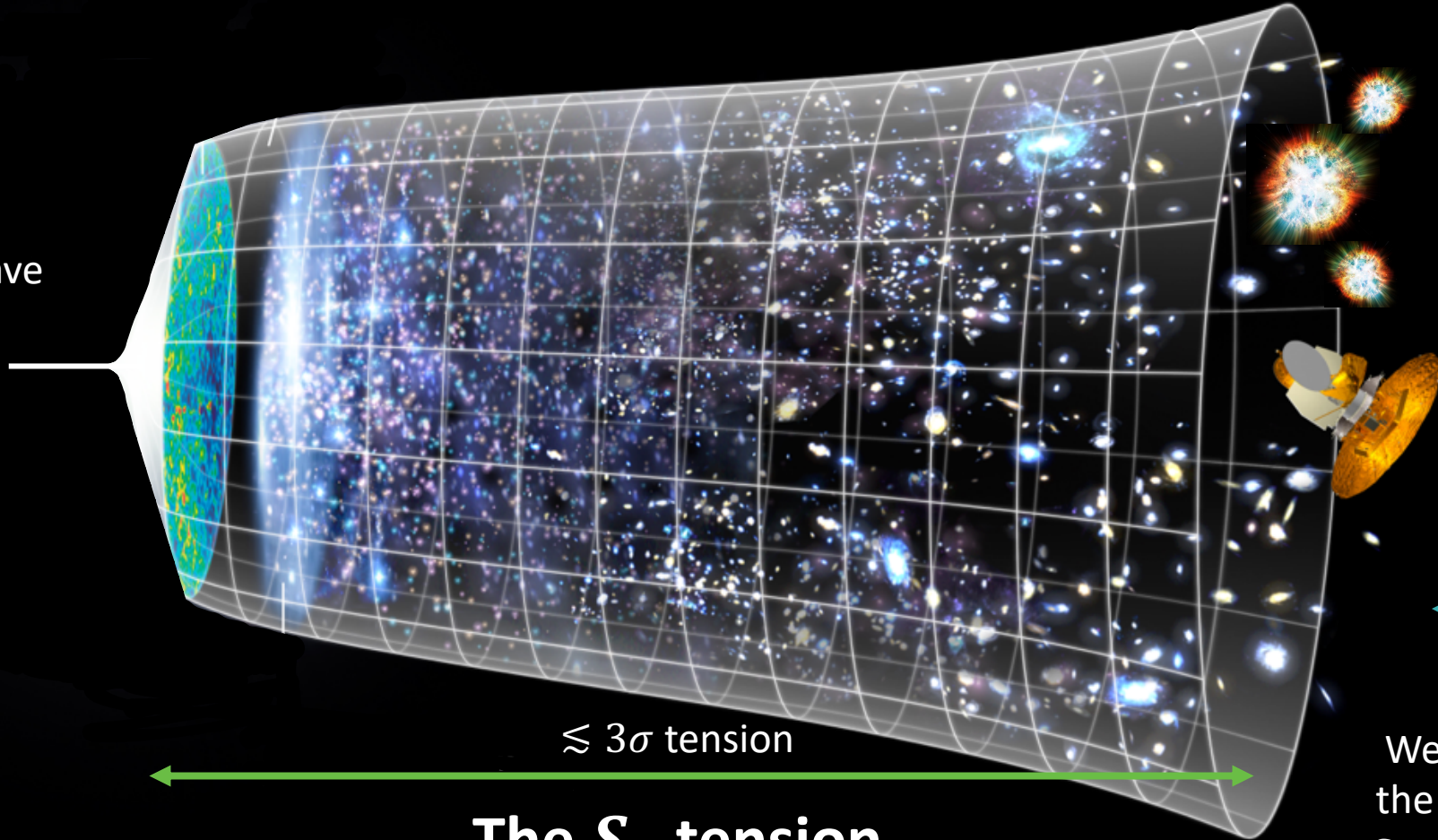
Fit  $\Lambda$ CDM to the CMB  
 $H_0 = 67.4 \pm 0.5$   
km/s/Mpc

$5.7\sigma$  tension

Cepheid distance ladder  
 $H_0 = 73.29 \pm 0.90$   
km/s/Mpc

## The Hubble tension

Cosmic microwave  
background  
+  
Cosmological  
assumptions



Late universe +  
astro/cosmo  
assumptions

Fit  $\Lambda$ CDM to the CMB  
 $S_8 = 0.832 \pm 0.013$

$\approx 3\sigma$  tension

Weak lensing in  
the late universe  
 $S_8 = 0.759^{+0.024}_{-0.021}$

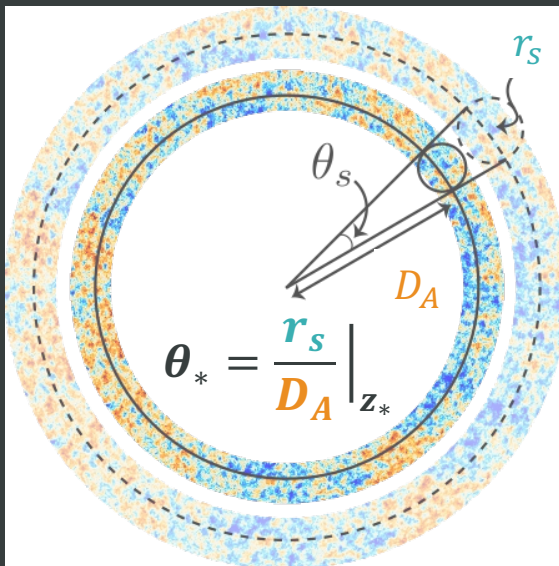
## The $S_8$ tension

# Model-building insights for cosmic tensions

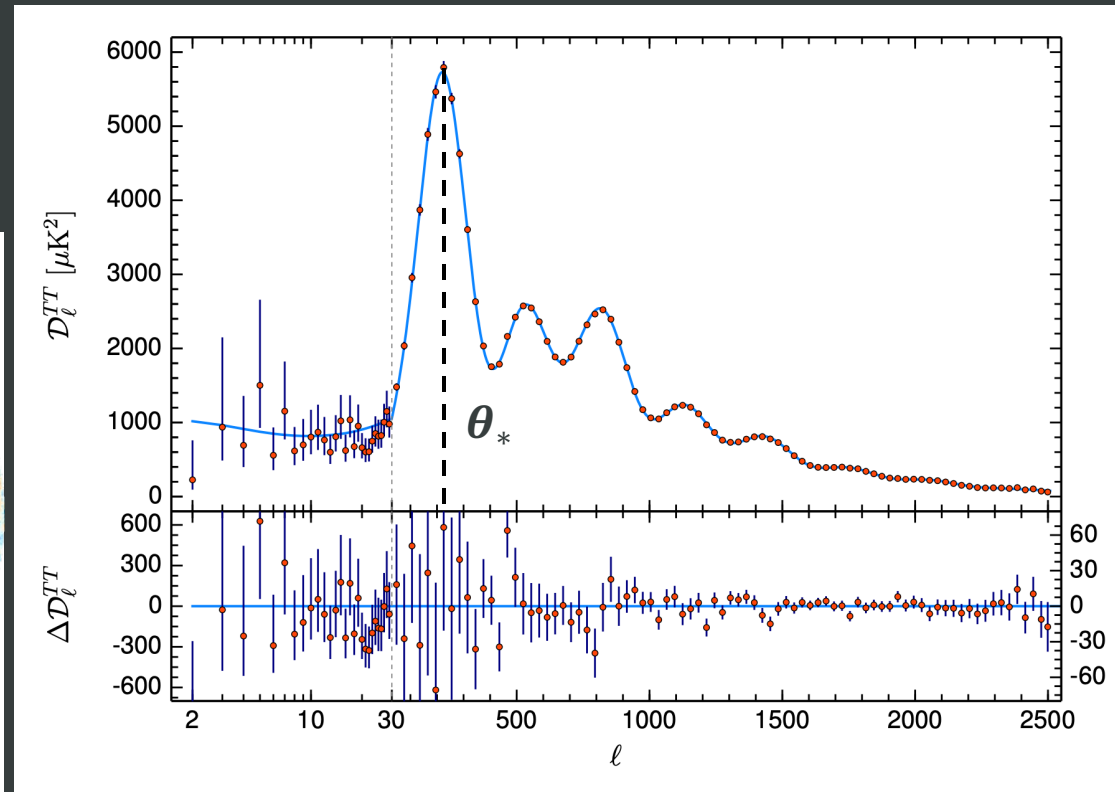
- How to solve the Hubble tension
- Potential  $H_0$  solutions
- How to solve the weak-lensing tension
- Potential  $S_8$  solutions

# How to solve the Hubble tension

Precisely measured  $\theta_*$  is an approximate proxy for CMB peak locations



Cartoon by Tristan L. Smith



Planck 2018

$$r_s = \int dz \frac{c_s}{H_{pre}}$$

$$= f_{\Lambda\text{CDM}}(\omega_b, \omega_c)$$

$$D_A \propto 1/H_{post}$$

$$\theta_* \sim \frac{r_s}{1/H_{post}} \sim r_s H_0$$

For constant  $\theta_*$ ,  
 $r_s \propto 1/H_0$

In support of an early-universe modification:

- Karwal et al [1608.01309]
- Bernal et al [1607.05617]
- Evslin et al [1711.01051]
- Planck [1807.06209]
- Aylor et al [1811.00537]
- Raveri et al [2002.11707]
- Schöneberg et al [2107.10291]

...

# How to solve the Hubble tension

Hubble Tension  $\leftrightarrow$  Sound Horizon Tension

Distance ladder and other late universe

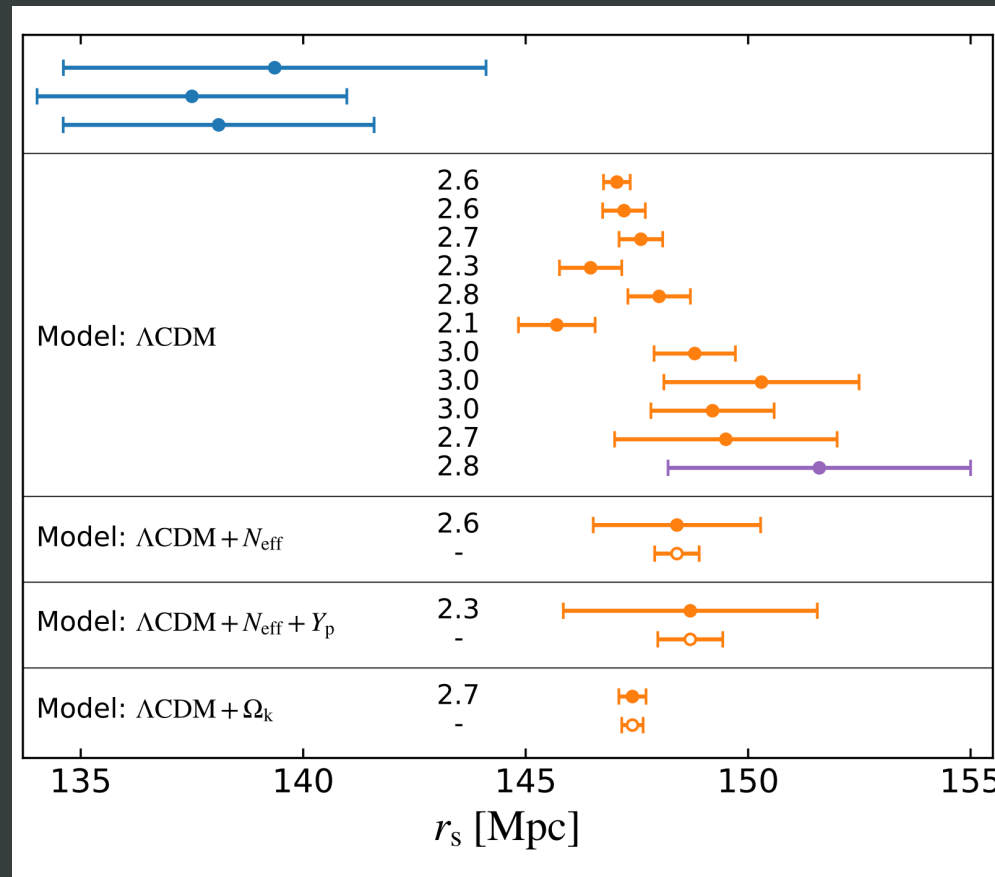
CMB, early universe

No CMB data, early universe

Higher  $H_0$  measured


Lower  $H_0$  inferred

Lower  $H_0$  inferred



Aylor et al [1811.00537]

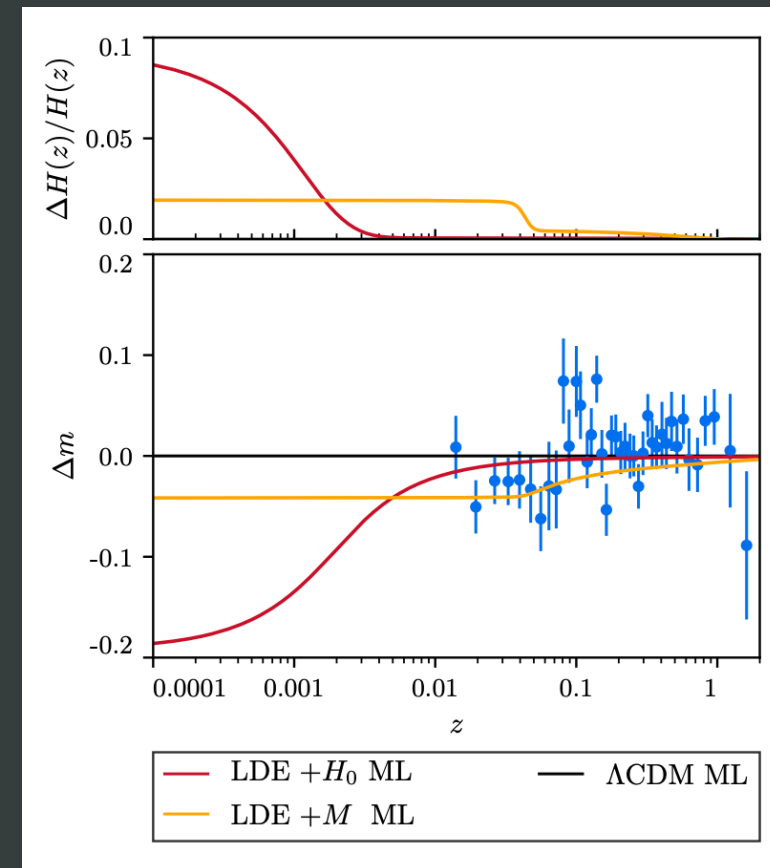
# How to solve the Hubble tension

- Maintaining a good fit to the CMB requires  $r_s \propto 1/H_0$ .  
Decrease the sound horizon  $r_s$  to increase the predicted  $H_0$ .  
Because  $r_s \propto 1/H_{pre}(z)$ , new physics must be added before the CMB
- New physics must vanish post recombination  Models that don't work or create new tensions

# How **not** to solve the Hubble tension

## Late transitions in dark energy

- The distance-ladder  $H_0$  is **not** actually a measurement at  $z = 0$
- The true source of the tension is at  $z \simeq 0.15$
- Late proposals of resolution must target the SN absolute magnitude calibration  $M_b$



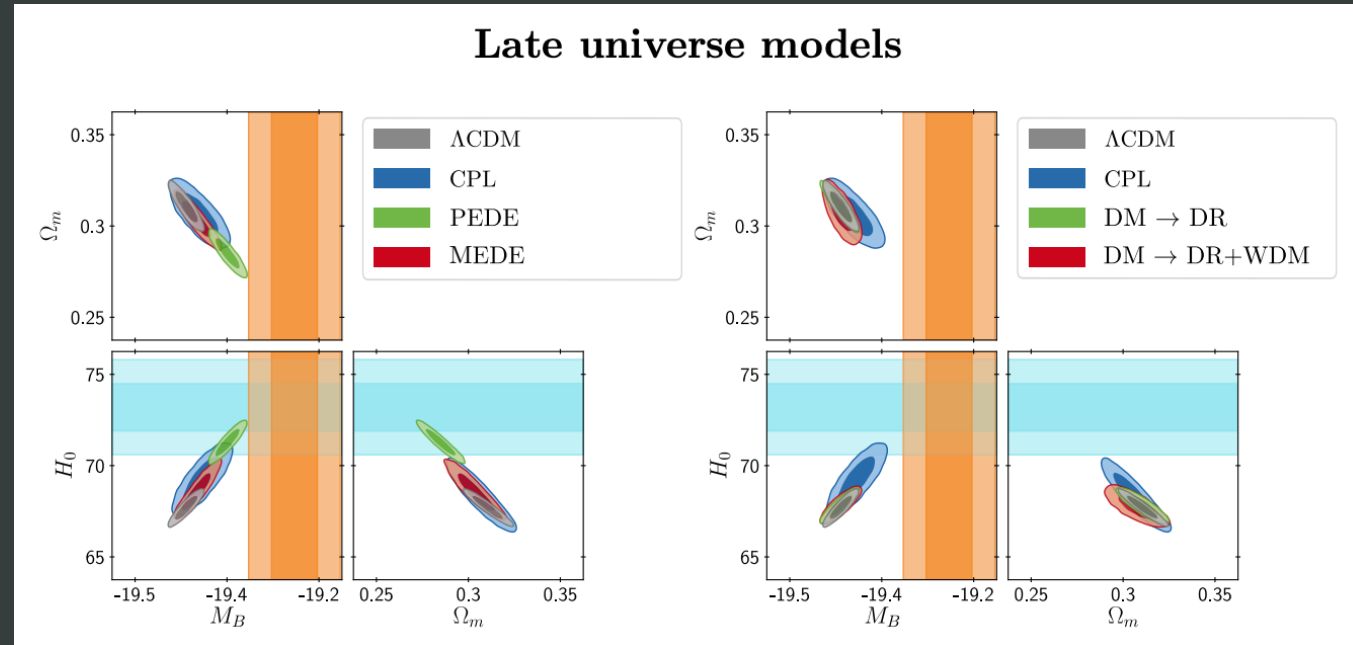
Also  
Bernal et al  
[2102.05066]

Efstathiou  
[2103.08723]

Benevento, Hu, Raveri  
[2002.11707]

# How **not** to solve the Hubble tension

Schöneberg et al  
[2107.10291]



Late-universe solutions are strongly constrained by data

- CMB lensing
- CMB low- $\ell$  ISW
- CMB-BAO agreement
- Pantheon supernovae



# How to solve the Hubble tension

- Decrease the sound horizon  $r_s$  to increase the predicted  $H_0$ . So new physics must be added before the CMB
- New physics must vanish post recombination
  - Very-late  $H(z)$  modifications do not resolve the tension more correctly parameterised by  $M_b$
  - Modifications to  $D_A$  introduce new tensions between CMB and BAO
  - Late-universe modifications to  $w(z)$  are tightly constrained by supernovae

# Models that work

- Early dark energy
- Early modified gravity / coupled scalar fields
- Varying the electron mass
- Certain dark radiation models

# Models that work

Farthest distance that sound waves travelled

$$\sim r_s \sim \theta_*$$

Electrons and protons have to combine sooner

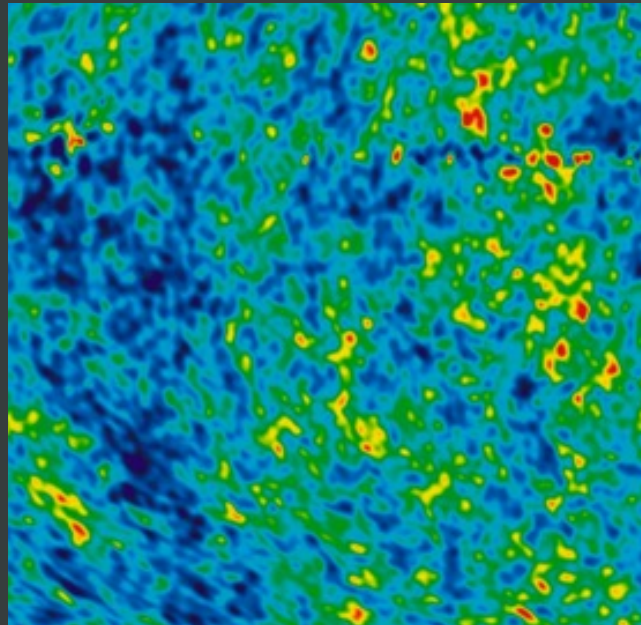
Modify the Universe at very early times, before the CMB was emitted

Sound waves travel a shorter distance if CMB is emitted earlier

Cool the Universe faster through expansion / modify atomic energy levels

WMAP, NASA

# Models that work



Observed CMB

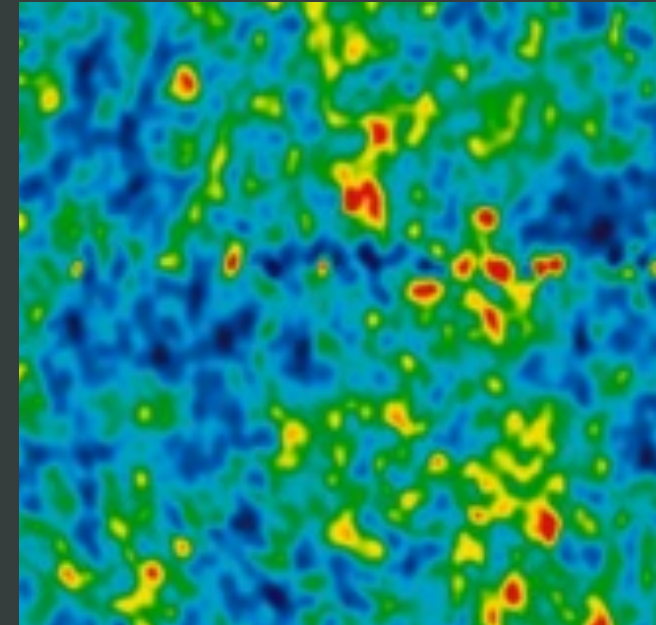


Increase  
 $H_0$



Add modification to  
early  $\Lambda$ CDM

Decrease  
 $r_s$



Disagreement with  
observed CMB

# Models that work

## Early dark energy

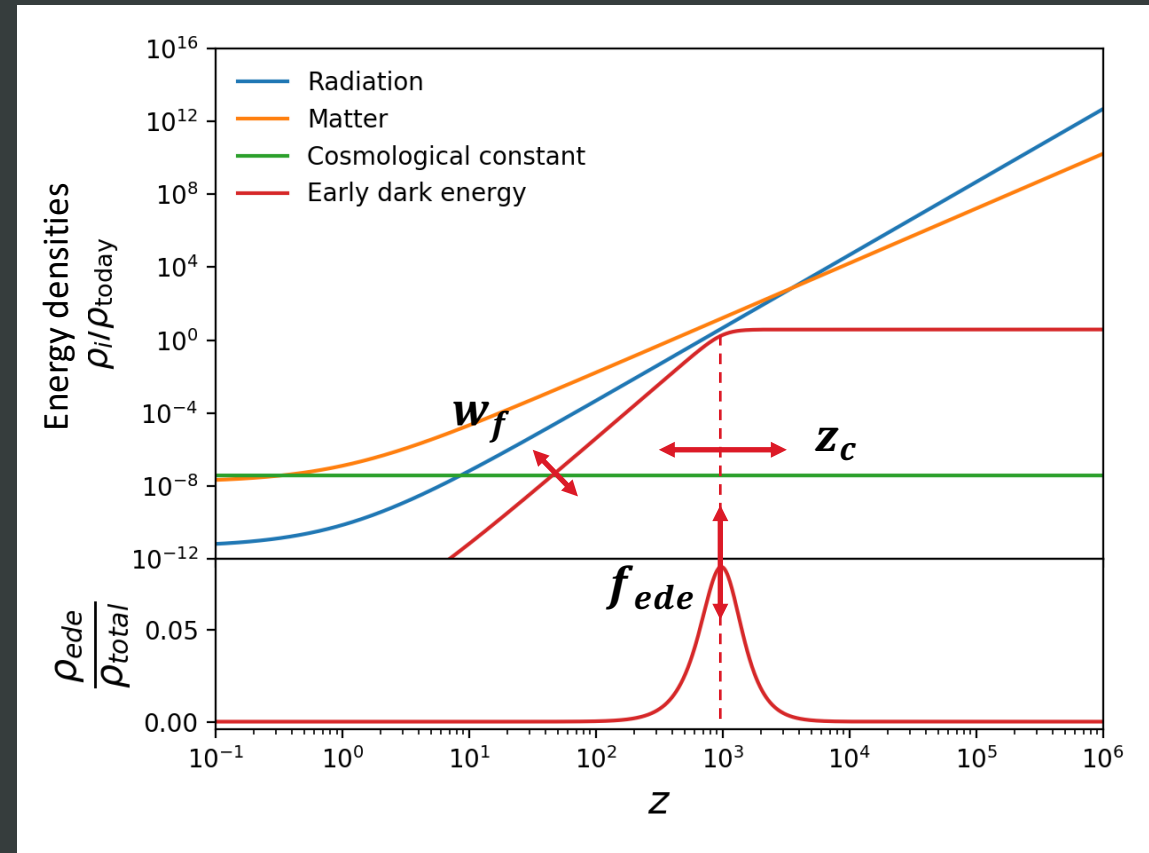
$$H^2 \sim \rho_{total}$$

Expansion rate  $\sim$  energy content

Additional energy component with the properties:

- $\Lambda$ -like behaviour initially
- Then dilutes faster than matter at  $w_f$
- Localised peak in  $f_{ede} = \frac{\rho_{ede}}{\rho_{total}}$  at  $z_c$

$f_{ede}$  - how much EDE  
 $z_c$  - when EDE appears  
 $w_f$  - how fast it disappears



# Models that work

## Early dark energies

- Dark energy at early times, the Hubble parameter, and the string axiverse  
TK & Kamionkowski [1608.01309]
- Cosmological implications of ultralight axionlike fields  
Poulin, TK et al [1806.10608]
- Early Dark Energy Can Resolve The Hubble Tension  
Poulin, TK et al [1811.04083]
- Thermal Friction as a Solution to the Hubble Tension  
Berghaus & TK [1911.06281]
- Chameleon Early Dark Energy and the Hubble Tension  
TK, Raveri, Jain, Khoury, Trodden [2106.13290]
- Thermal Friction as a Solution to the Hubble and Large-Scale Structure Tensions  
Berghaus & TK [2204.09133]
- Also ask **Kim Boddy**, **José Luis Bernal** and **Anthony Lewis**

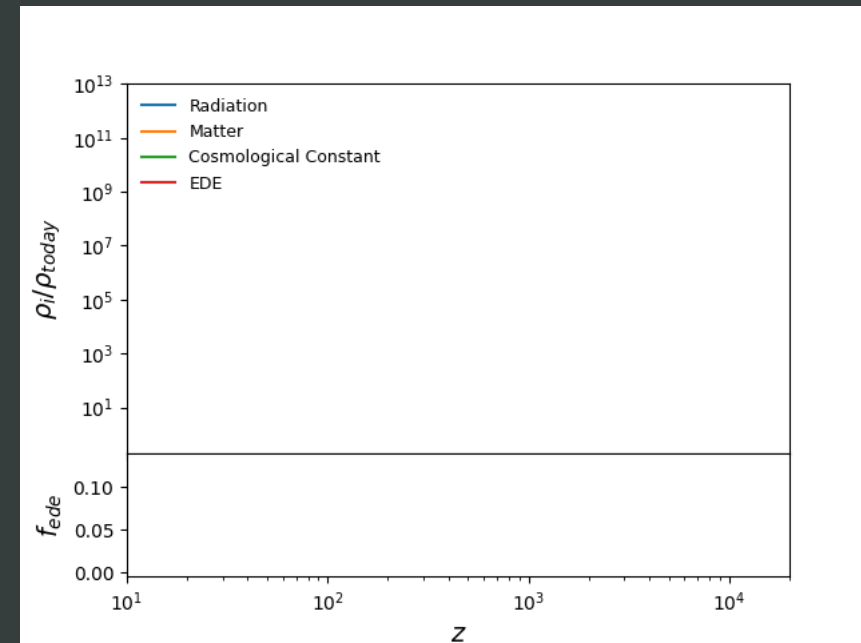
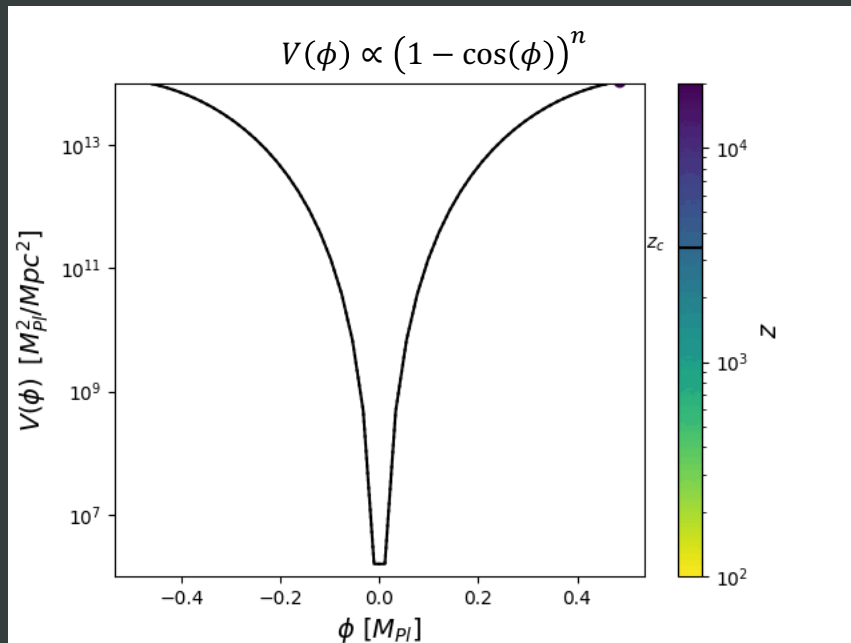
Non-comprehensive list:

- Rock 'n' Roll Solutions to the Hubble Tension. Agrawal et al [1904.01016]
- Axion-Dilaton Destabilization and the Hubble Tension. Alexander & McDonough [1904.08912]
- Acoustic Dark Energy: Potential Conversion of the Hubble Tension. Lin, Raveri, Hu [1905.12618]
- Oscillating scalar fields and the Hubble tension: a resolution with novel signatures. Smith, Poulin, Amin [1908.06995]
- New Early Dark Energy. Neidermann & Sloth [1910.10739]
- Early Dark Energy from Massive Neutrinos as a Natural Resolution of the Hubble Tension. Sakstein & Trodden [1911.11760]
- Unifying Inflation with Early and Late-time Dark Energy in F(R) Gravity. Nojiri et al [1912.13128]
- Is the Hubble tension a hint of AdS phase around recombination? Ye & Piao [2001.02451]
- Unified framework for early dark energy from  $\alpha$ -attractors. Braglia et al [2005.14053]
- A novel early Dark Energy model. Garcia, Castaneda, Tejeiro [2009.07357]
- Neutrino-Assisted Early Dark Energy: Theory and Cosmology. Gonzalez et al [2011.09895]
- The Early Dark Sector, the Hubble Tension, and the Swampland. McDonough, .. Hill, Hu, et al [2112.09128]
- Effects of a Geometrically Realized Early Dark Energy Era on the Spectrum of Primordial Gravitational Waves, Oikonomou et al [2206.00721]
- Early dark energy and the screening mechanism, Sadjadi et al [2205.15693]
- Early Dark Energy from a Higher-dimensional Gauge Theory, Kojima et al [2205.13777]
- Unifying inflation with early and late dark energy with multiple fields: Spontaneously broken scale invariant two measures theory, Guendelman et al [2201.06470]
- ...



# Models that work

## Early dark energy – Ultra-light axions EDE



Based on Poulin, Smith, TK, Kamionkowski  
[arxiv:1806.10608]

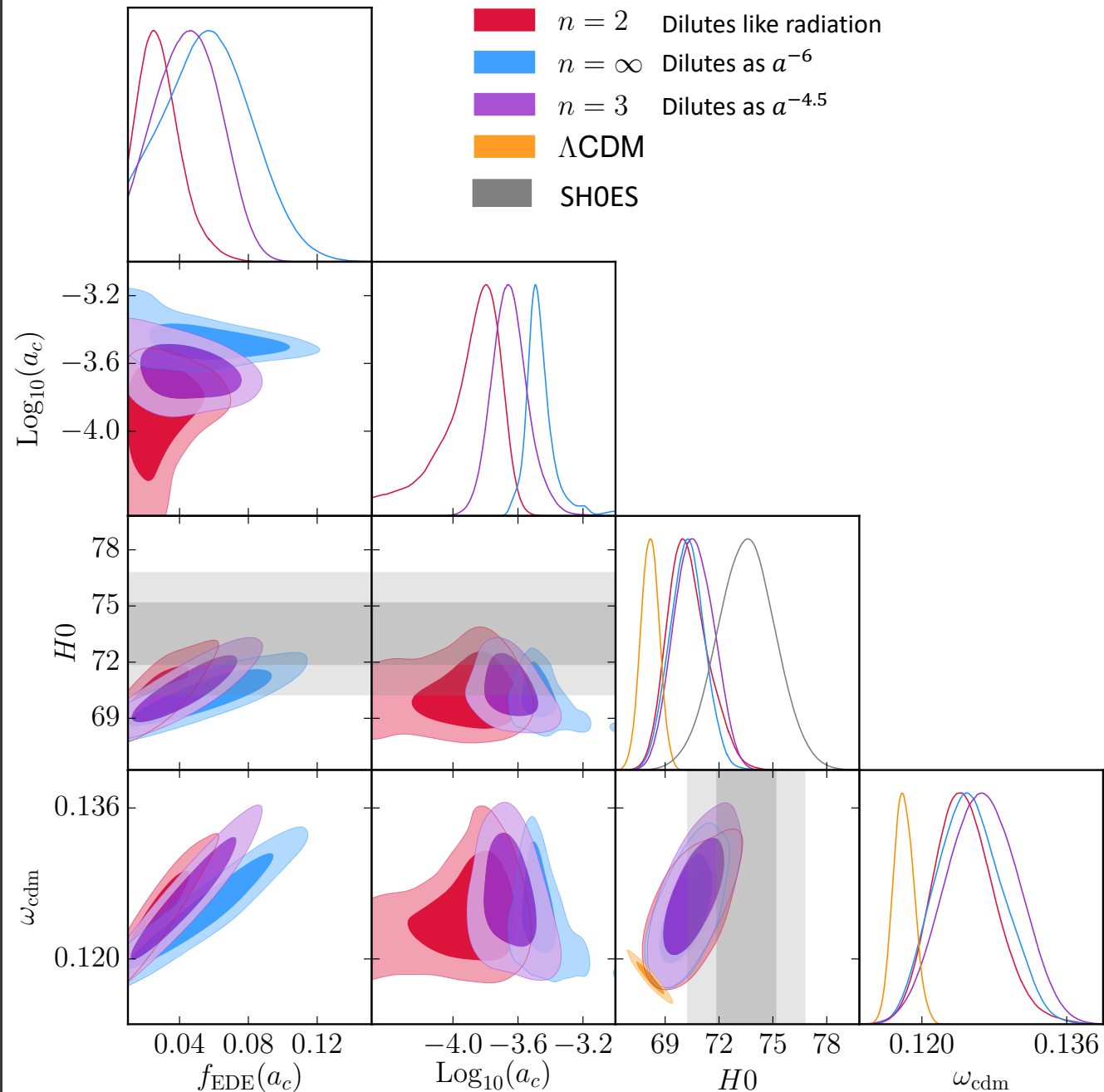
# Models that work Early dark energy – ULA

Fit to CMB+BAO+SNe+H0

- $\omega_{cdm}$  = amount of cold dark matter today
- $f_{ede}(a_c)$  = fractional energy density in the axion field at critical redshift  $z_c \approx 1/a_c$
- $w_f = \frac{n-1}{n+1}$

We find an improved  $\chi^2$  for  $\Lambda$ CDM + EDE for combined datasets

Poulin, TK et al [1811.04083]



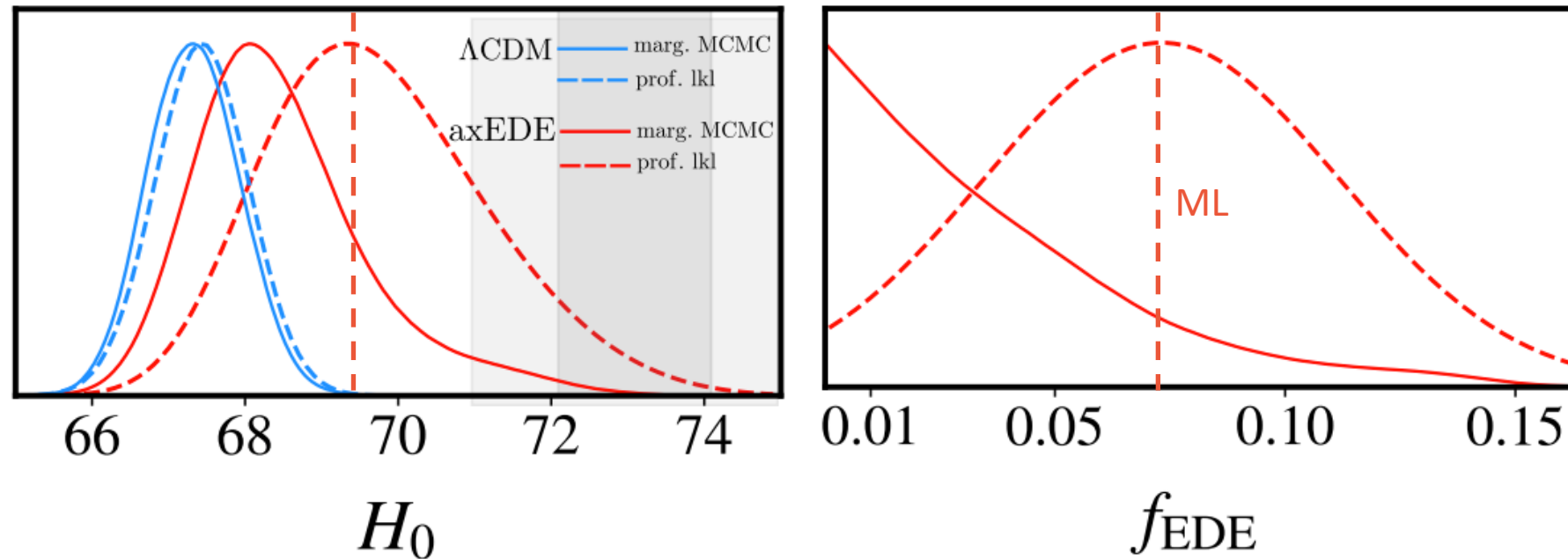


# Models that work

## Early dark energy – without a SH0ES prior

Fit to CMB+BAO+SNe,  
no  $H_0$  prior

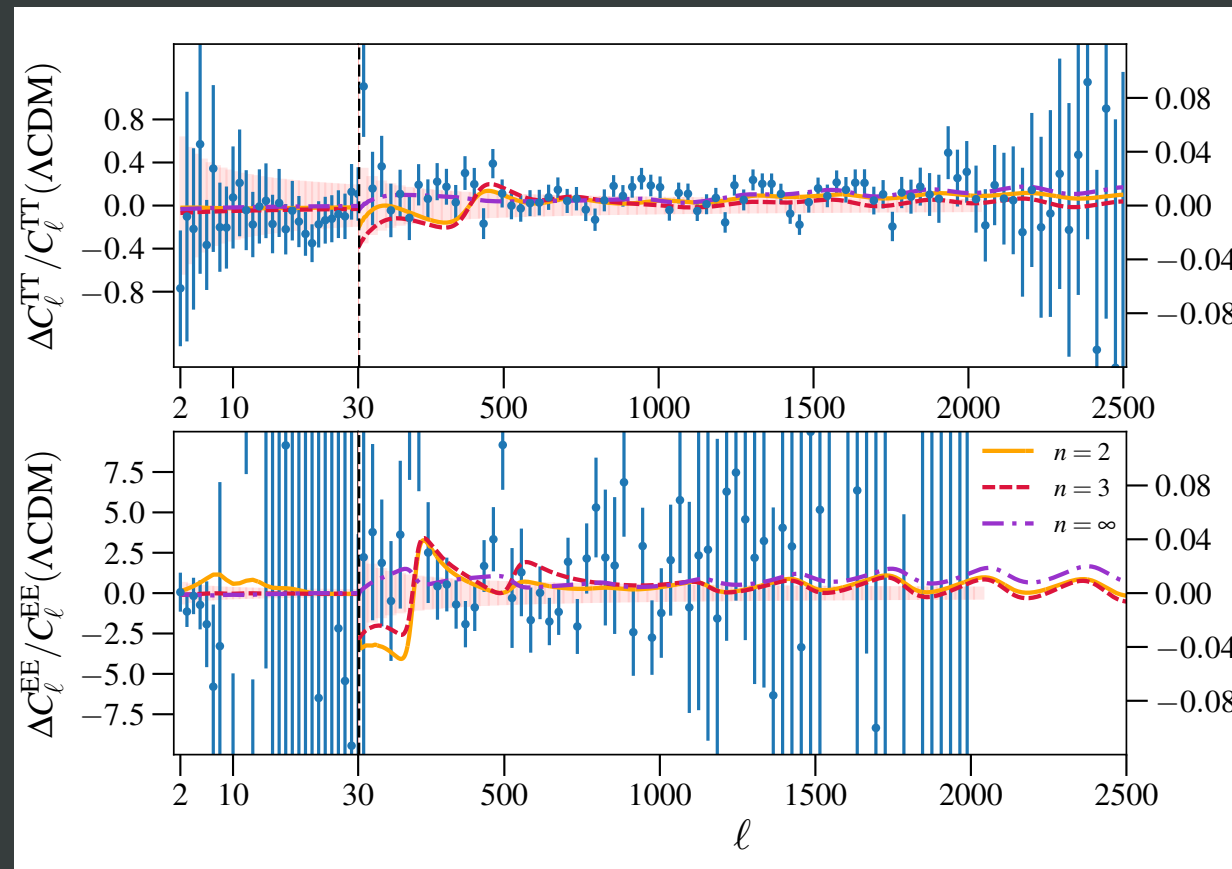
Prior volume increases as  $f_{ede} \rightarrow 0$   
 $z_c$  and  $w_f$  become unconstrained



Poulin, Smith and TK [2302.09032]

# Models that work

## Early dark energy – detection in the CMB



Poulin, TK et al [1811.04083]

Could detect EDE in  
cosmic-variance-limited,  
high- $\ell$   
CMB polarisation data

ACT and SPT show  
preference for EDE at  $\geq$   
 $3\sigma$  level when high- $\ell$   
CMB TT data is excluded

Smith et al [2202.09379]  
Hill et al [2109.04451]

Also  
Lin et al [2009.08974]  
Chudaykin et al [2004.13046]  
and [2011.04682]

# Models that work

## Chameleon early dark energy

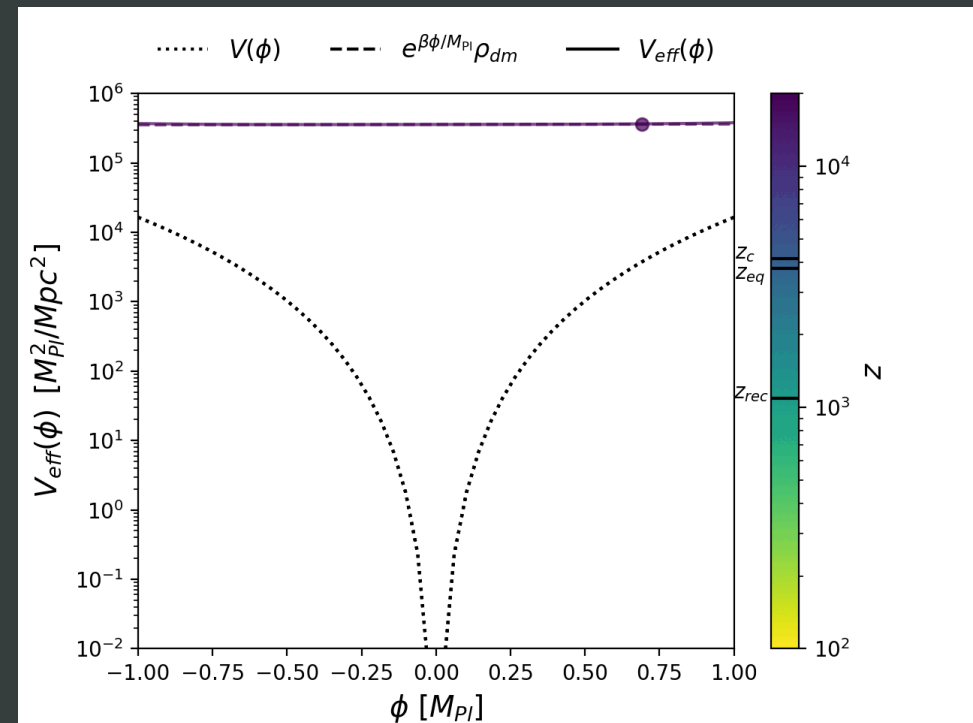
Conformally couple a scalar field to dark matter

$$\rho_{total} += \rho_{dm} A(\phi)$$

$$V_{eff}(\phi) = V(\phi) + \rho_{dm} A(\phi)$$

- Modifies **DM** evolution  $\rightarrow S_8$  ?
- Tie the redshift of **EDE** to  $z_{eq}$  through coupling  $A(\phi)$

$$V(\phi) \sim \phi^4 \quad A(\phi) \sim e^{\beta\phi}$$



TK et al [2106.13290]

# Models that work

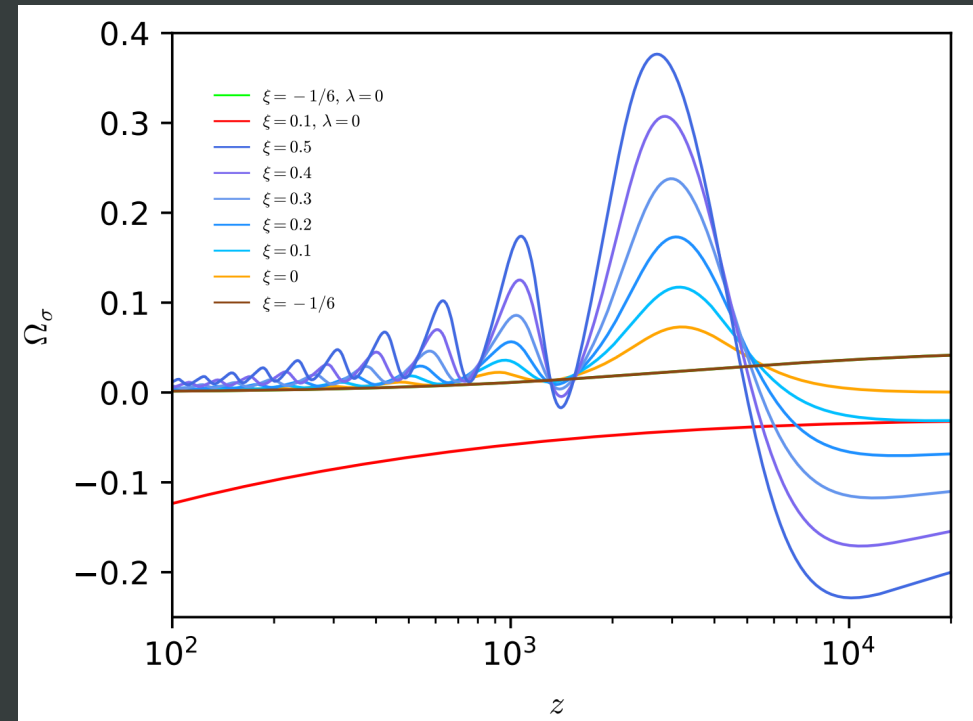
## Early modified gravity

Early dark energy scalar field  $\sigma$   
coupled to the Ricci scalar  $R$

$$\mathcal{S} \ni \int d^4x \sqrt{-g} \frac{\xi \sigma^2}{2} R$$

Similar EDE models that introduce  
couplings to DM/ $\nu$ :

- Neutrino-assisted EDE  
Sakstein and Trodden [1911.11760]
- Chameleon EDE  
Karwal et al [2106.13290]
- Early dark sector  
McDonough et al [2112.09128]  
Lin et al [2212.08098]



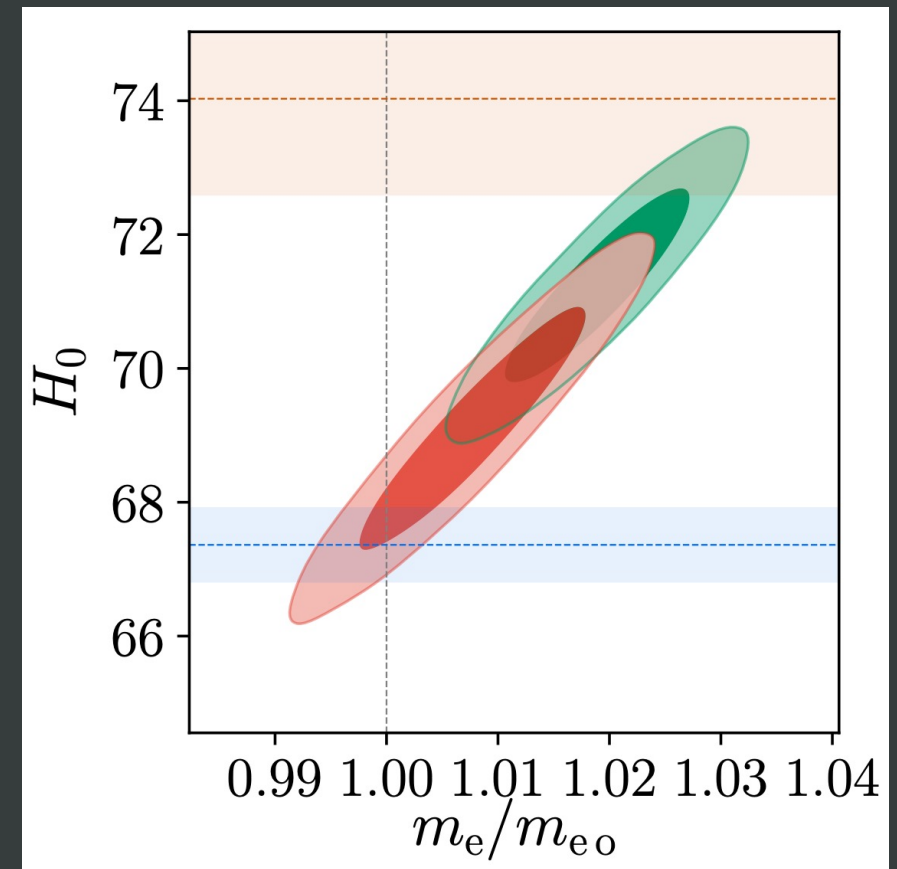
Braglia et al [2011.12934]

# Models that work

## Varying the electron mass $m_e$

- Atomic energy levels  $\propto m_e$
- Higher ionisation energy for  $H$
- Earlier recombination
- Smaller  $r_s$

Also Sekiguchi and Takahashi [2007.03381]



Hart and Chluba [1912.03986]

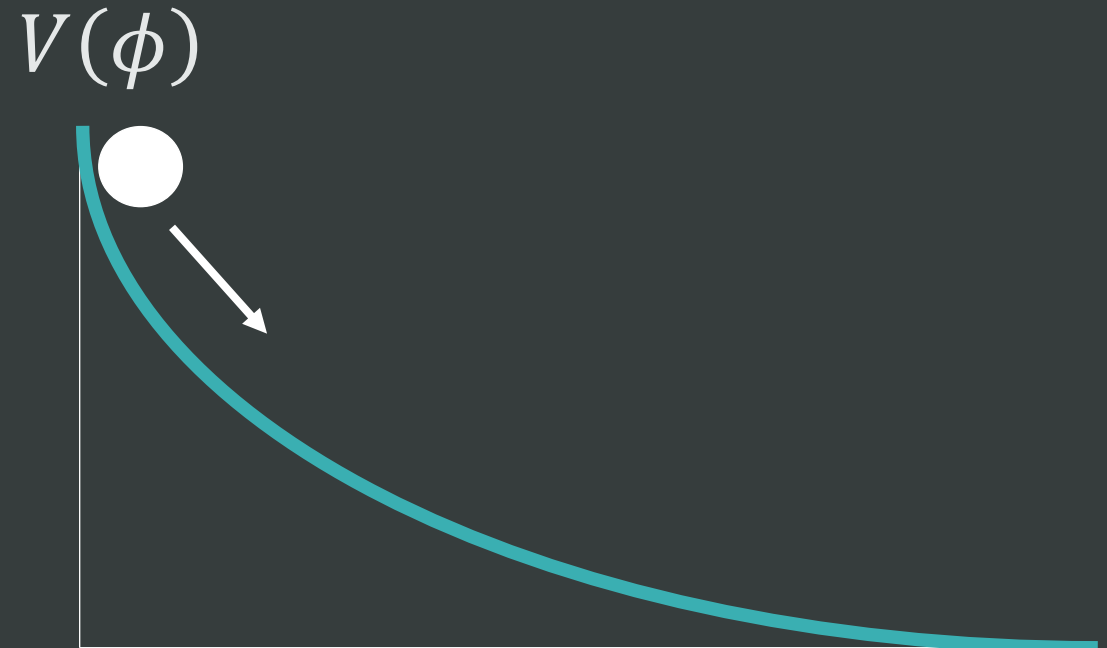
# Models that work ?

## Dark radiation – Dissipative axion EDE

Uncoupled scalar experiences **Hubble friction**. Uncoupled DR dilutes as  $(1+z)^4$

$$\ddot{\phi} + (3H) \dot{\phi} + V_{\phi} = 0$$

$$\dot{\rho}_{dr} = -4H\rho_{dr}$$



Berghaus & Karwal [1911.06281]

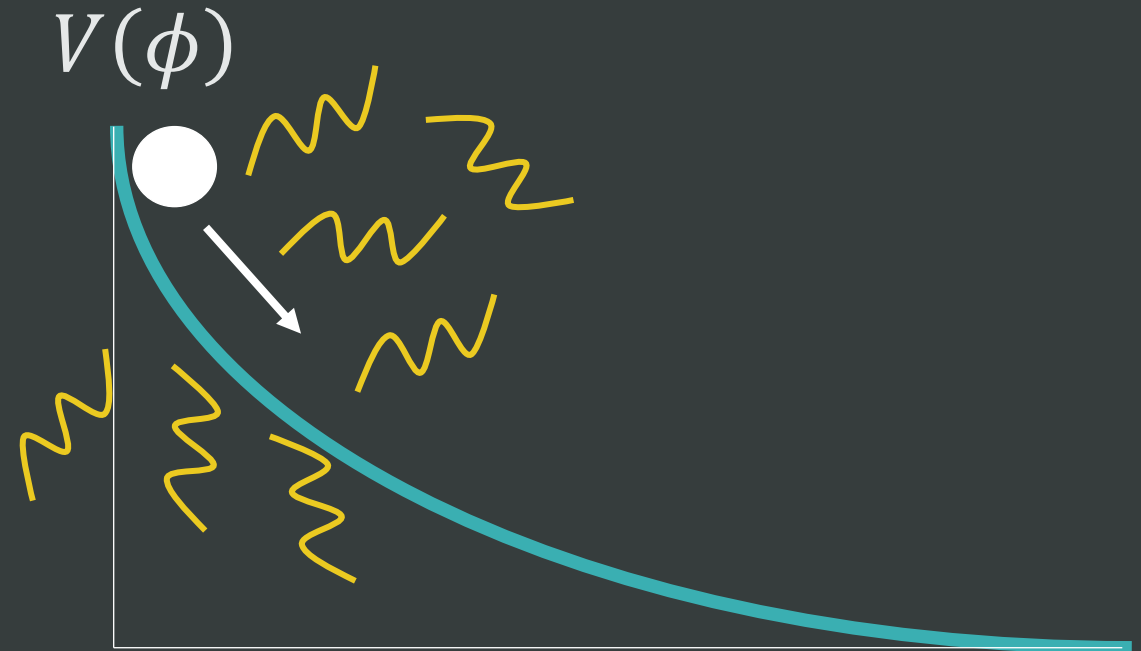
# Models that work ?

## Dark radiation – Dissipative axion EDE

Scalar coupled to DR **additionally**  
experiences **thermal friction**

$$\ddot{\phi} + (3H + \Upsilon) \dot{\phi} + V_{\phi} = 0$$

$$\dot{\rho}_{dr} = -4H\rho_{dr} + \Upsilon\dot{\phi}^2$$



Berghaus & Karwal [1911.06281]

# Models that work ?

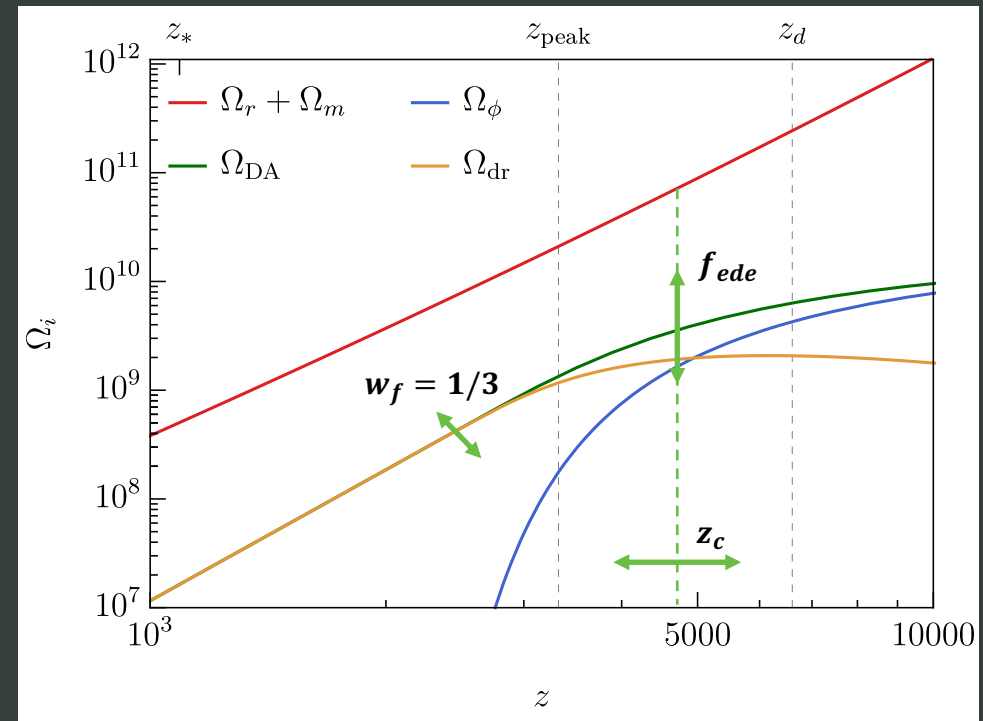
## Dark radiation – Dissipative axion EDE

$$\ddot{\phi} + (3H + \Upsilon(T_{dr})) \dot{\phi} + V_{\phi} = 0$$

$$\dot{\rho}_{dr} = -4H\rho_{dr} + \Upsilon(T_{dr})\dot{\phi}^2$$

$$\begin{aligned} m, \phi_i &\rightarrow f_{ede} \\ m, \Upsilon(T_{dr}) &\rightarrow z_c \\ w_f &= 1/3 \end{aligned}$$

Robust to choice of  $V(\phi)$



Berghaus & Karwal [1911.06281]



# Models that don't work

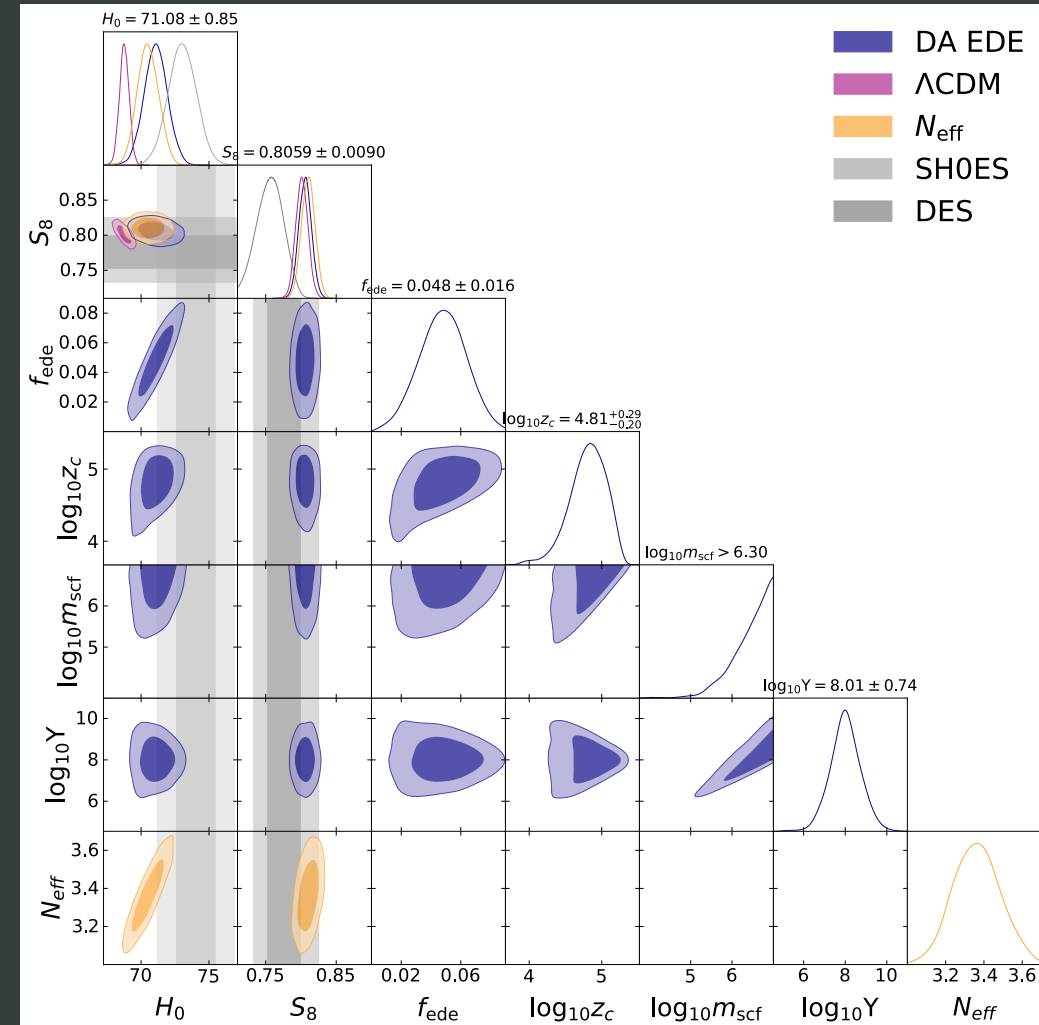
## Dark radiation – Dissipative axion EDE

Fit to CMB+BAO+SNe+H0+DES

- Higher Hubble than  $\Lambda$ CDM and  $N_{eff}$
- Similar  $S_8$  to  $\Lambda$ CDM and  $N_{eff}$
- Extra radiation preferred over EDE-like injection
- Similar fit to CMB as  $\Lambda$ CDM, but worse than  $\Lambda$ CDM fit to concordant data

Dissipative axion performs better than  $N_{eff}$  but suffers the same CMB constraints as other extra radiation

Berghaus & TK [2204.09133]



# Models that work

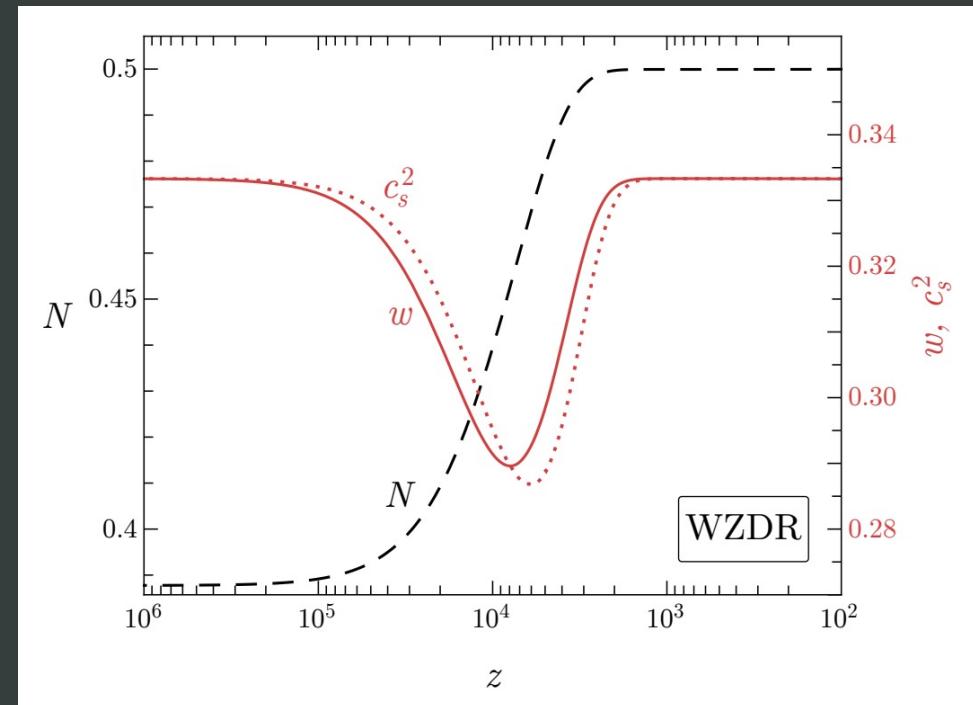
## Certain dark radiation models

Not all DR models work:

- $N_{eff}$  – Planck [1807.06209]
- DA EDE – Berghaus and TK [2204.09133]
- Free-streaming / self-interacting DR, both Brinckmann et al [2012.11830]
- SIDR that scatters on DM see Schöneberg et al [2107.10291]
- SI- $\nu$  and free-streaming DR Kreisch et al [1902.00534] and others
- SI- $\nu$  with an energy injection Sandner et al [2305.01692]

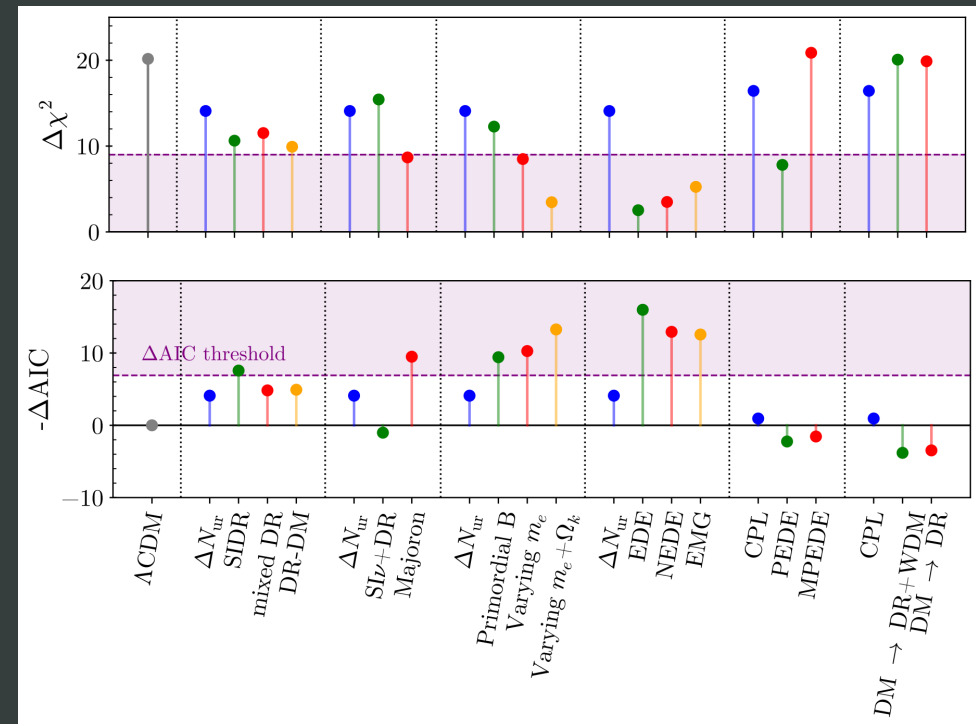
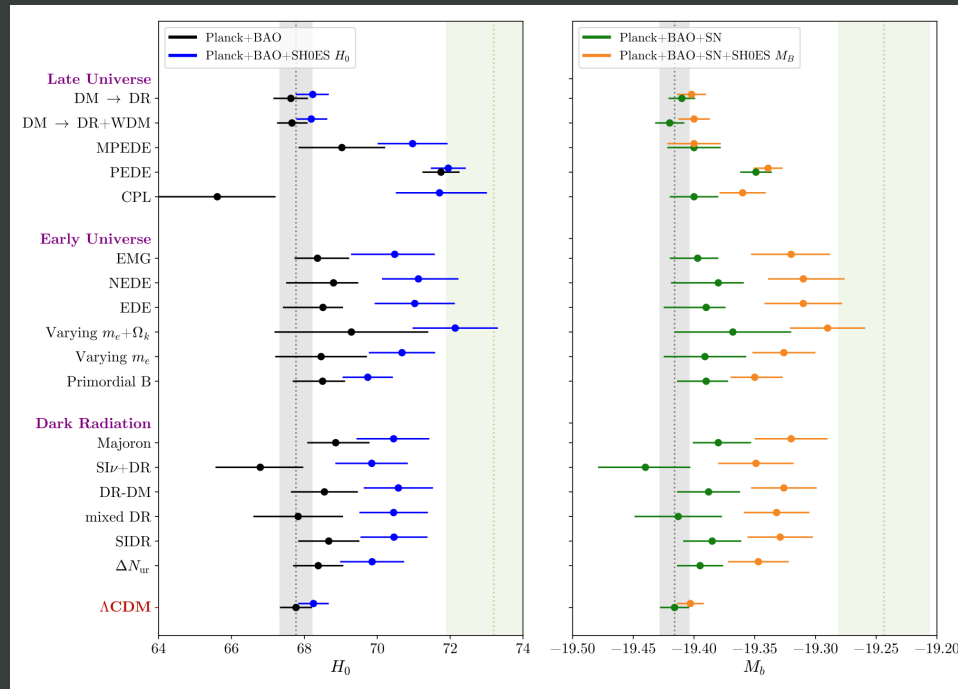
But some do:

- WZDR - SIDR with an energy injection →



Aloni et al [2111.00014]

# Models that work Posteriors and $\chi^2$ 's



Schöneberg et al [2107.10291]



Fit  $\Lambda$ CDM to the CMB  
 $H_0 = 67.4 \pm 0.5$   
km/s/Mpc

Homogeneous, isotropic background

Cepheid distance ladder  
 $H_0 = 73.29 \pm 0.90$   
km/s/Mpc

# The Hubble tension

Cosmic microwave  
background

Fit  $\Lambda$ CDM to the CMB  
 $S_8 = 0.832 \pm 0.013$

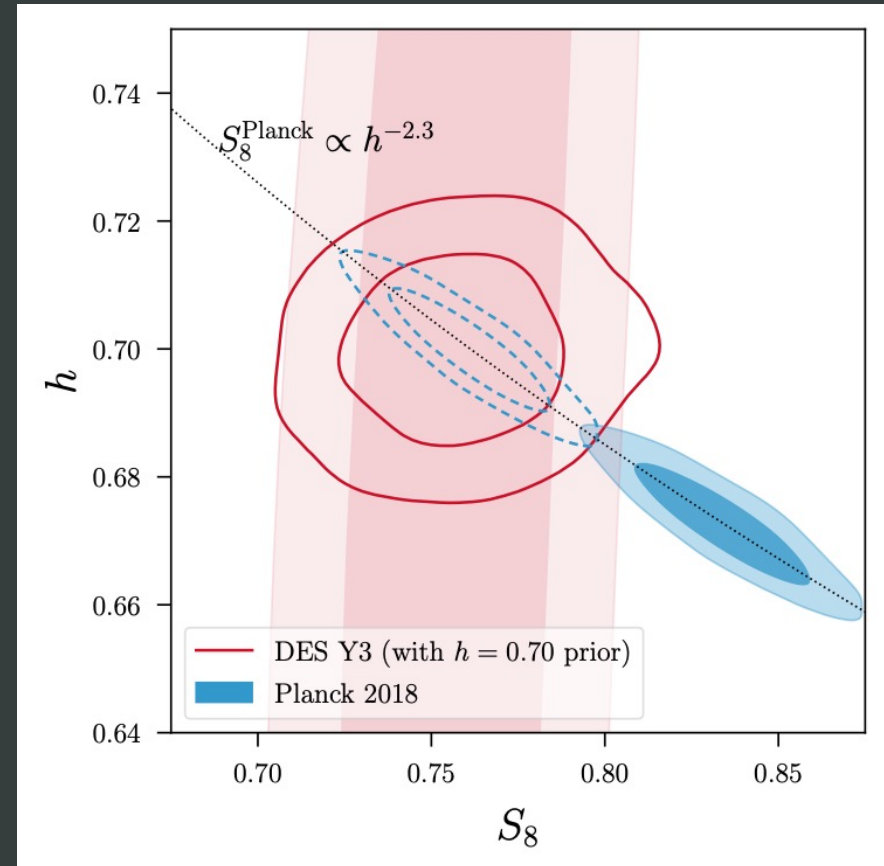
Perturbative universe

# The $S_8$ tension

Weak lensing in  
the late universe  
 $S_8 = 0.759^{+0.024}_{-0.021}$

# How to solve the $S_8$ tension

- CMB and WL are both model-dependent
- $S_8 = \sigma_8 \sqrt{\Omega_m / 0.3}$  in WL
  - Best-constrained parameter direction
  - Independent of  $H_0$
- $S_8$  in CMB
  - Complicated function of  $(\omega_b, \omega_c, A_s, n_s, h, G)$
  - Both background and perturbations

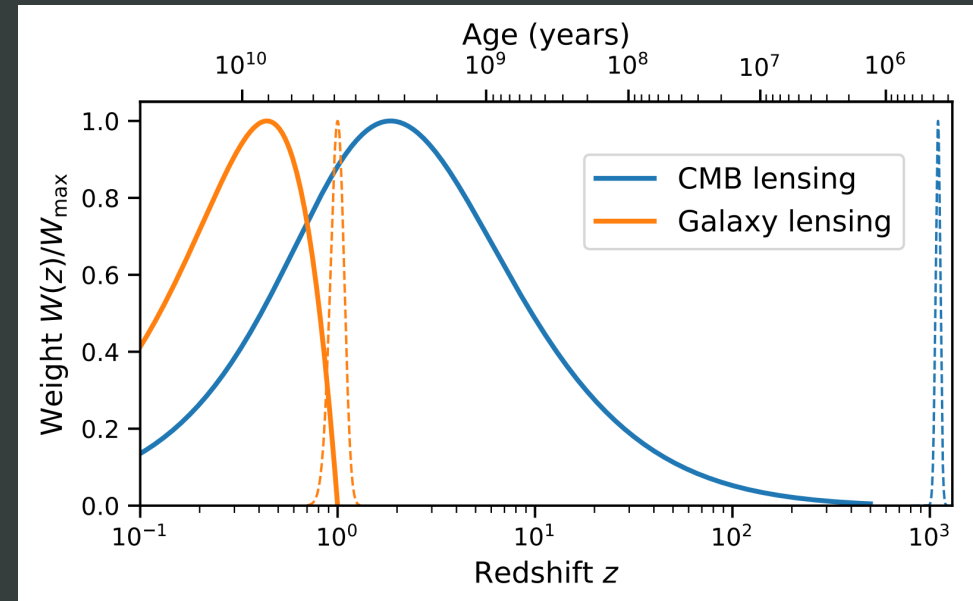


Secco, TK, Krause, Hu  
[2209.12997]



# How to solve the $S_8$ tension

- CMB lensing does not find tension
- Peak sensitivity at different redshifts  
→ when to introduce new physics
  - Late-universe  $H_0$  tension caveats apply
- Probe different scales → what scales to impact



Madhavacheril, ACT [2304.05203]  
And numerous ACT members at Bensaque

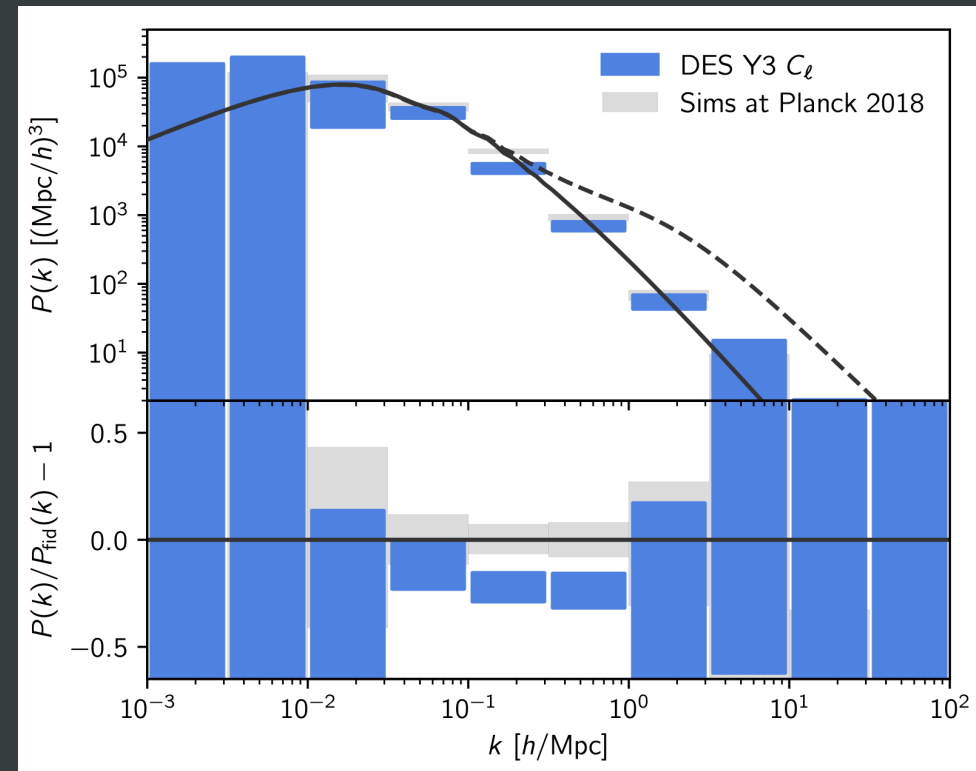
# How to solve the $S_8$ tension

Consistency test between DES and Planck:

- Fix cosmology to Planck 2018
- Predict Planck linear  $P(k)$  at  $z = 0$
- Use DES  $C_\ell$  to predict linear  $P(k)$  at  $z = 0$

Observe scale-dependent suppression of power

New physics can target these scales to improve the tension



Doux et al [2203.07128]

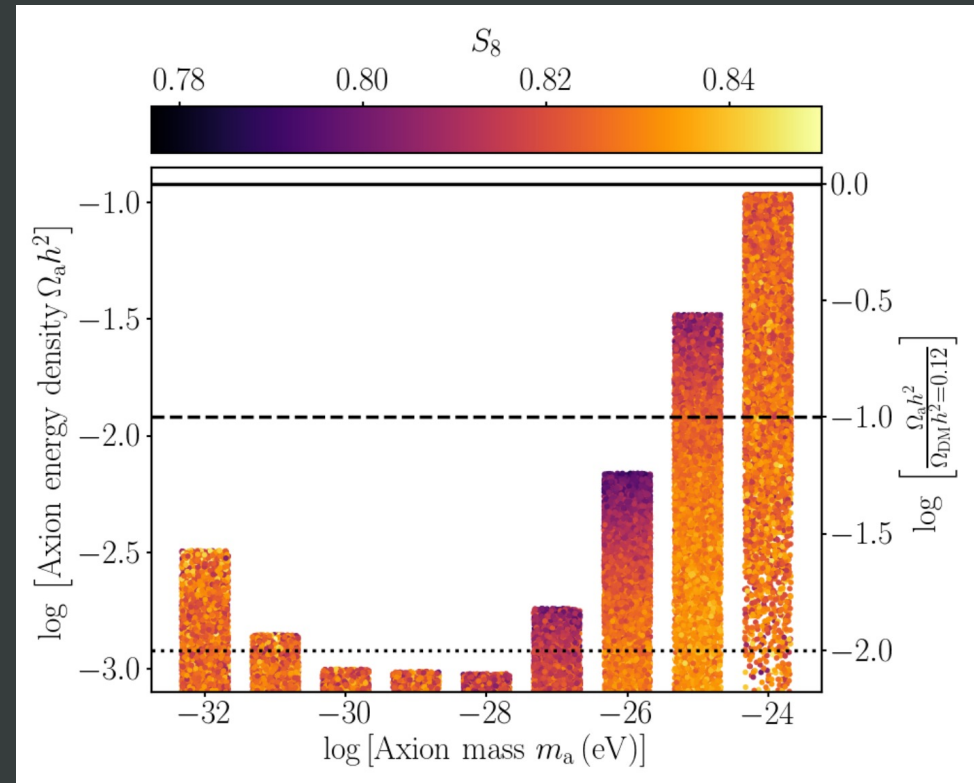


# Models that work But **worsen** the $H_0$ tension

Ultra-light axions in the mass range  
 $10^{-28} \text{ eV} \leq m_a \leq 10^{-25} \text{ eV}$

- Injected pre-recombination
- Form a fraction of DM today
- Reduce  $S_8$  tension to  $1.6\sigma$
- Worsen  $H_0$  tension because the energy injection lingers in the late universe

Ask [Mateja Gosenca](#) about ULA DM



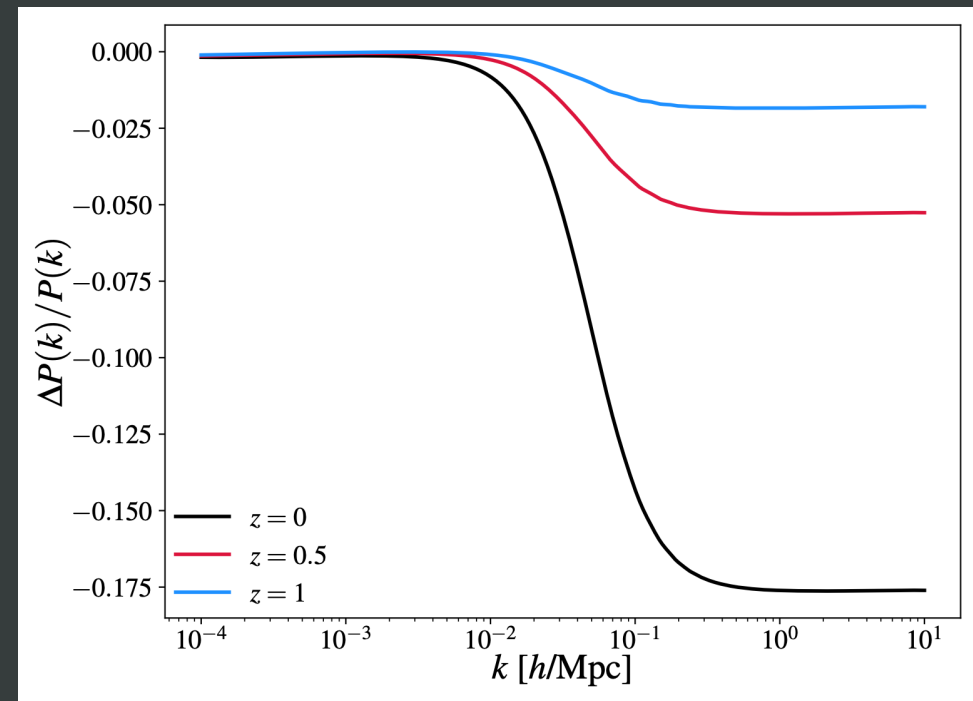
Rogers et al [2301.08361]

# Models that work

## Perturbative modifications

Friction drag between DM and DE

- Turns on around matter-DE equality
- Resolves the tension
- Possible non-linear imprints in WL
- No modification to background



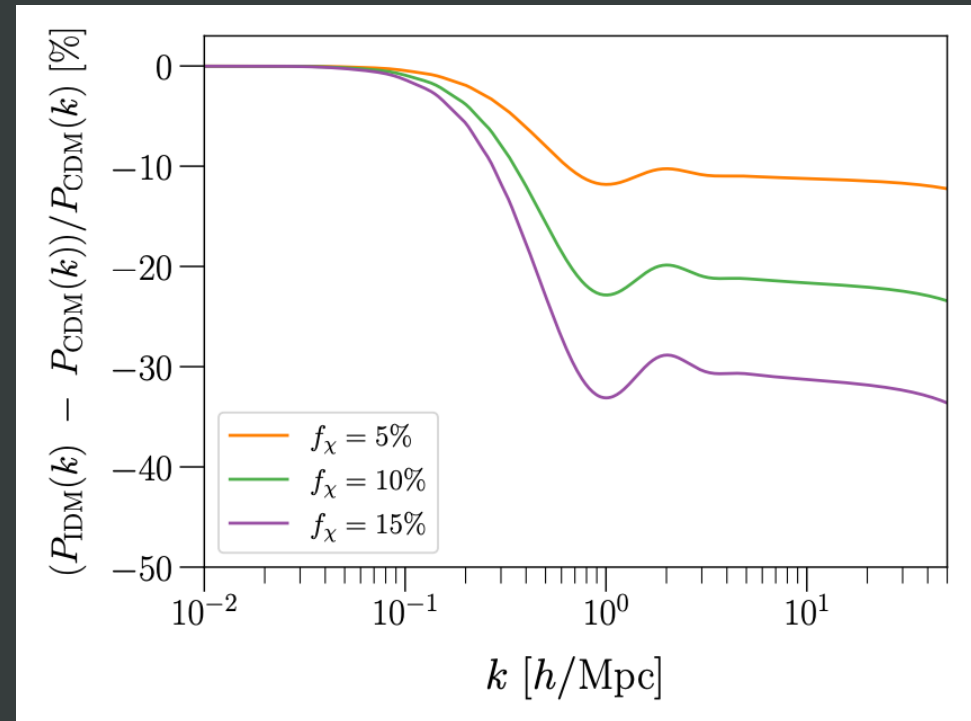
Poulin et al [2209.06217]

# Models that work

## Perturbative modifications

Fraction of DM scatters off baryons

- 10% DM of mass 1  $MeV$  interacts
- Small-scale power suppressed
- No background modifications



He et al [2301.08260]

# Models that work

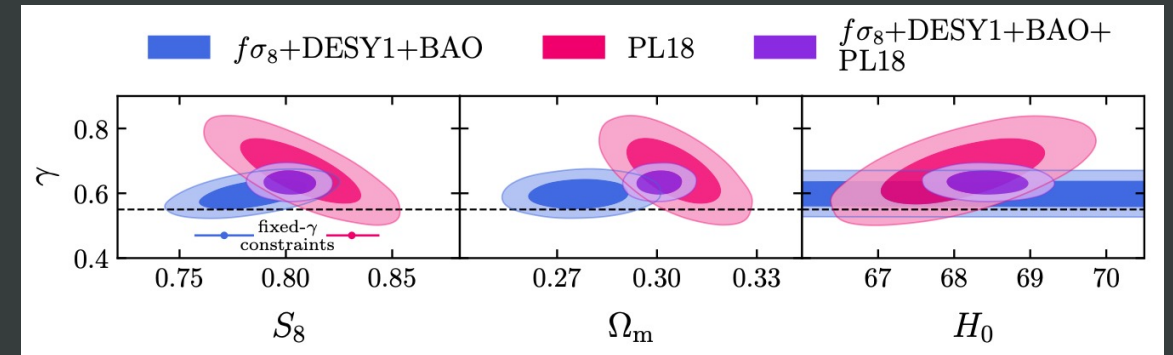
## Phenomenological insight

Allow growth index  $\gamma$  to vary

$$f(a) = \Omega_m^\gamma(a)$$

relative to  $\gamma_{\Lambda\text{CDM}} = 0.55$

- $\gamma > 0.55$  implies suppression of growth
- $\gamma = 0.55$  excluded at  $\sim 4\sigma$
- Shifts both WL and CMB  $S_8$  resolving tension
  - WL  $S_8$  increases
  - CMB  $S_8$  decreases



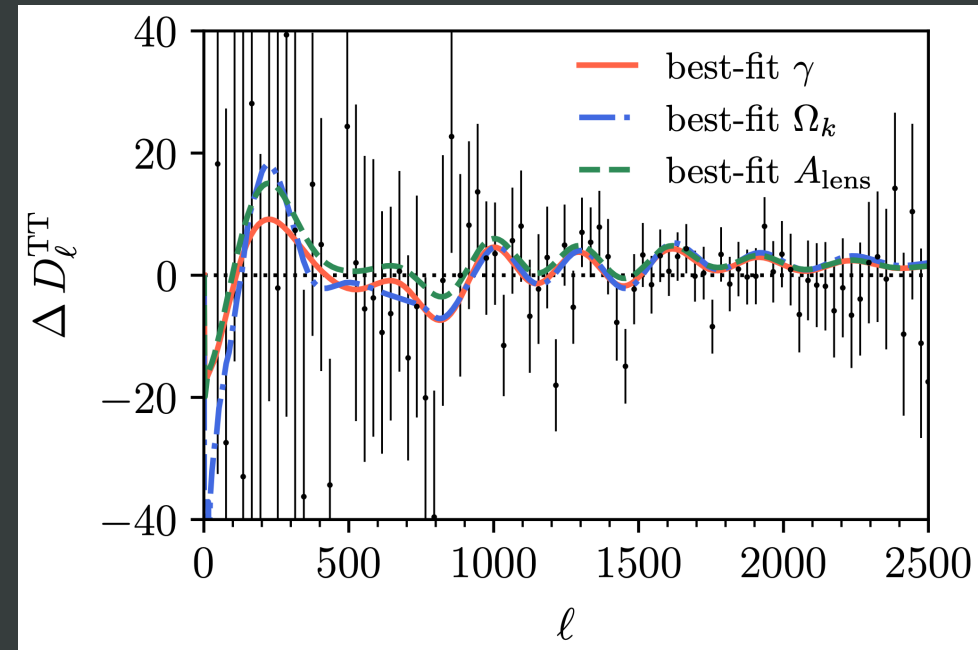
Nguyen et al [2302.01331]

# Models that work

## Phenomenological insight

Varying growth index  $\gamma$

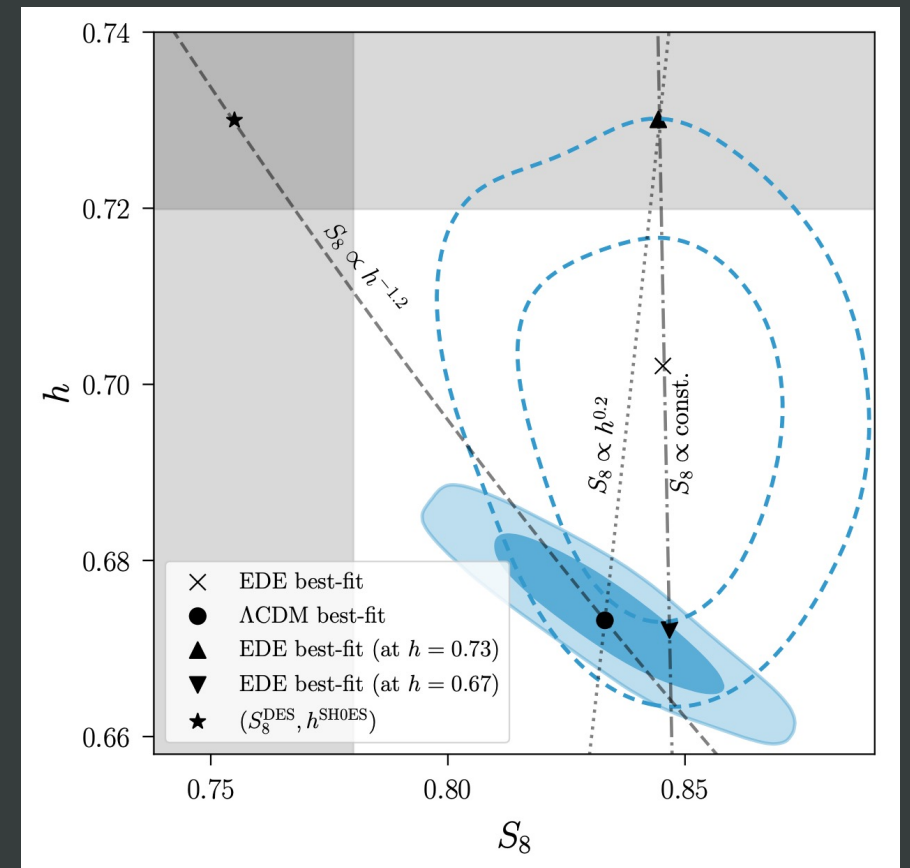
- Mimics the effect of varying  $\Omega_k$  or  $A_{lens}$  in the CMB residuals
- No background modification



Nguyen et al [2302.01331]

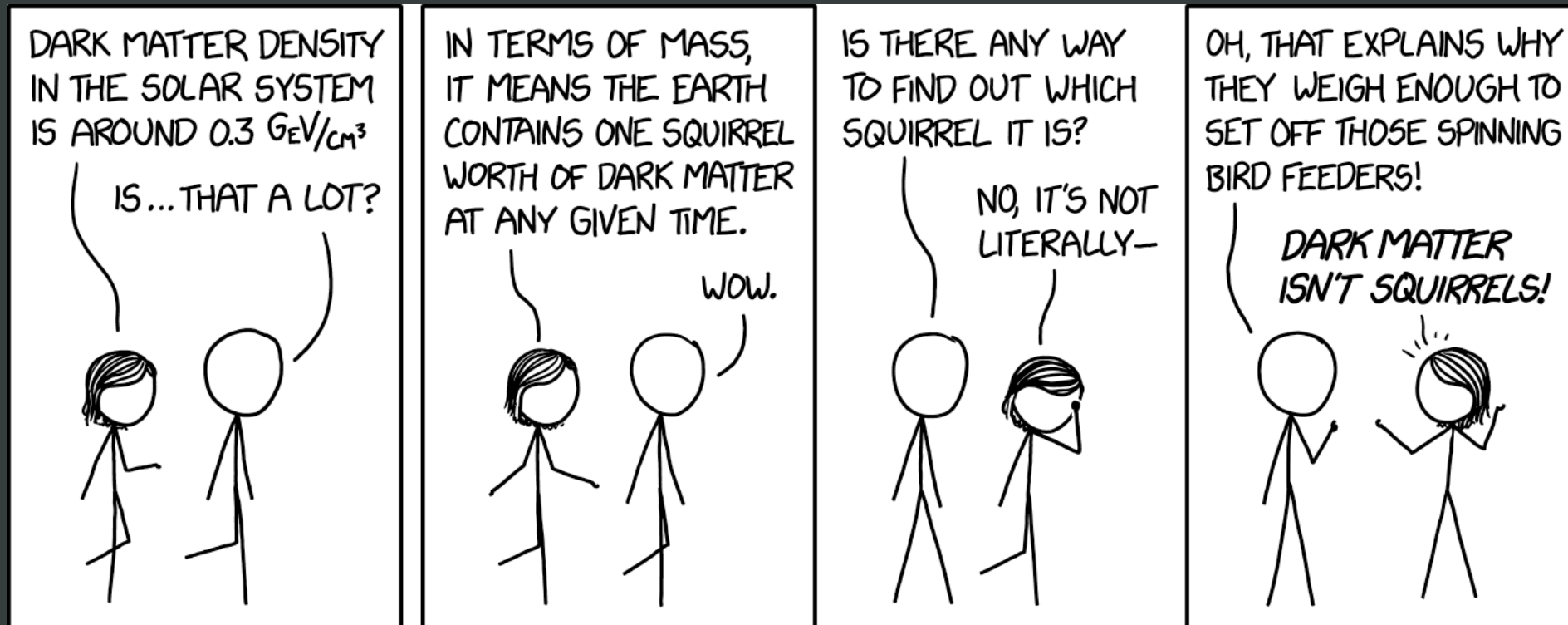
# How to solve cosmic tensions

- New physics that targets both tension simultaneously must modify the background and perturbative universe
  - Modify the early background, not late for  $H_0$
  - Scale-dependent impact on  $P(k)$  for  $S_8$
- Background modifications that target only one tension tend worsen the other
- If we split them up:
  - The Hubble tension requires an early background modification
  - The  $S_8$  tension can be targeted with just perturbative modifications



Secco, TK, Krause, Hu [2209.12997]

# Lets get creative with dark sector physics!

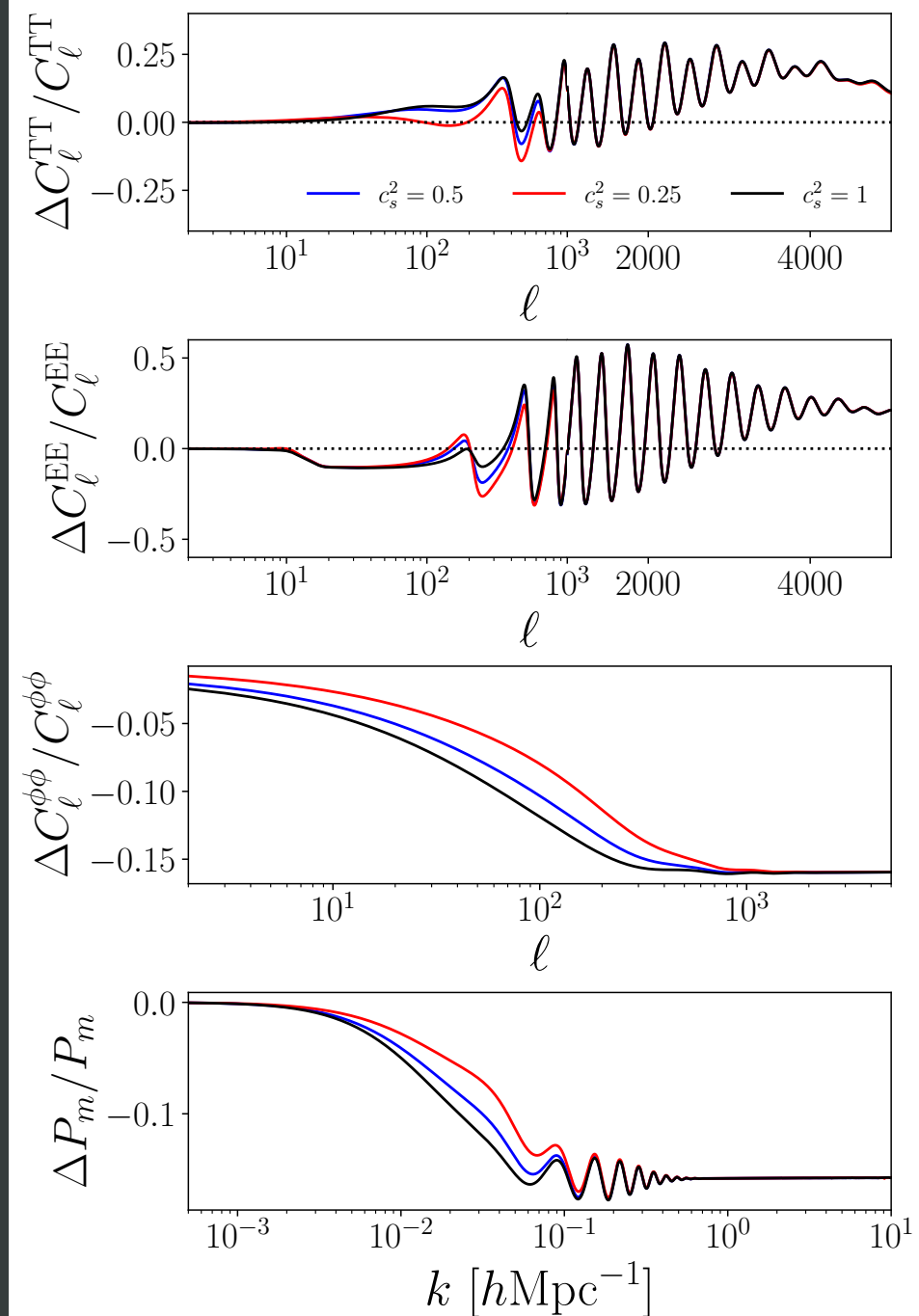


XKCD: 2186





# Differentiation in CMB data



Poulin, Smith and TK [2302.09032]