

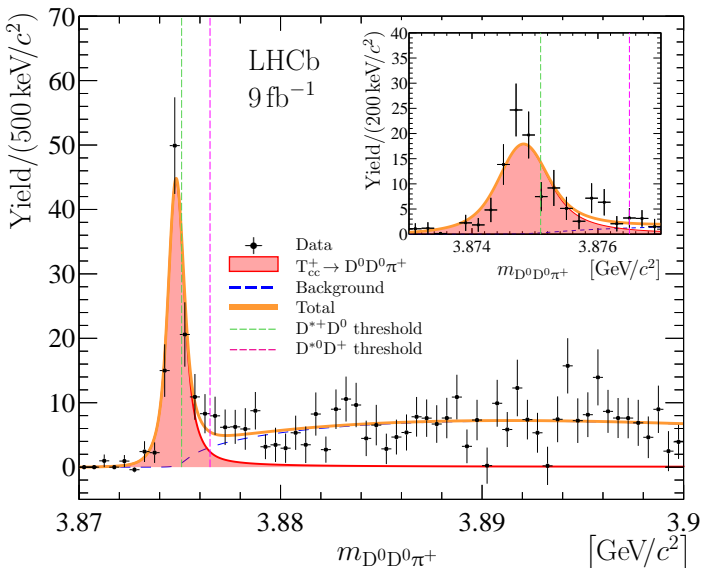
# Doubly charmed exotic state $T_{cc}^+$ — nature, properties, pion dynamics and all that

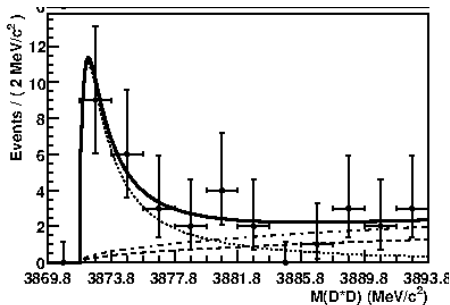
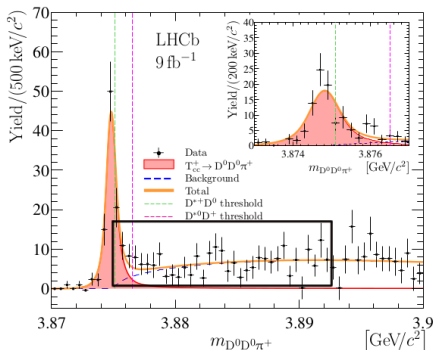
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Josef Stefan Institute, Ljubljana, Slovenia



Benasque-2024

$T_{cc}^+(cc\bar{u}\bar{d})$  @ LHCb (Nature Phys. 18 (2022) 7, 751)

$T_{cc}^+$  versus  $X(3872)$ 

- Higher precision: smaller bins & better known resolution function
- Larger statistics: small uncertainties
- Data below two-body threshold: clear below-threshold peak

$T_{cc}^+$  versus  $X(3872)$ 

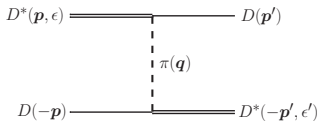
## Common features:

- **Isoscalars**
- Definitely contain a **pair of heavy quarks**
- Reside incredibly **close to 2-hadron thresholds**  $D\bar{D}^*/DD^*$
- Decay to **open-charm** final states  $D\bar{D}\pi/DD\pi$  and  $D\bar{D}\gamma/DD\gamma$
- Important consequences from  $D^* \rightarrow D\pi$  decay

## Difference:

- $X$  contains  $c\bar{c}$  pair while  $T_{cc}^+$  contains  $cc$
- $X$  decays to **hidden-charm** states while  $T_{cc}^+$  does **not**
- Short-range core (if any):  $c\bar{c}$  charmonium vs tetraquark  $cc\bar{u}\bar{d}$

# Pion exchange in $I = 0$ $DD^*$ system



$$V_\pi(\mathbf{p}, \mathbf{p}') = \left( \frac{g_c}{2f_\pi} \right)^2 \langle \boldsymbol{\tau} \cdot \boldsymbol{\tau} \rangle \frac{(\boldsymbol{\epsilon} \cdot \mathbf{q})(\mathbf{q} \cdot \boldsymbol{\epsilon}'^*)}{u - m_\pi^2}$$

$$\begin{aligned} &\Rightarrow \left( \frac{g_c}{2f_\pi} \right)^2 \left( -1 + \overbrace{\frac{\mu_\pi^2}{q^2 + [m_\pi^2 - (m_{D^*} - m_D)^2]}}^{\text{Long-range OPE}} \right) \\ &\text{central} \\ &\text{recoil} \end{aligned}$$

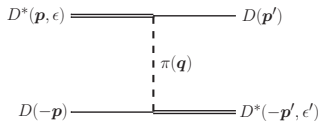
Effective mass  $\mu_\pi^2$

- Short-range OPE absorbed by (re-fitted) contact interaction
- Perturbative long-range OPE as per

$$\alpha_\pi^{\text{eff}} = \frac{g_c^2 |\mu_\pi^2|}{f_\pi^2} \ll 1$$

(XEFT: Voloshin'2004, Fleming et al.'2007,...)

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Long-range OPE

$$\Rightarrow \left( \frac{g_c}{2f_{\pi}} \right)^2 \left( -1 + \frac{\mu_{\pi}^2}{2 + \dots} \right)$$

Is pion exchange important in  $T_{cc}^+$ ?

- Short-range OPE absorbed by (re-fitted) contact interaction
- Perturbative long-range OPE as per

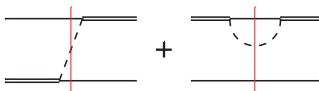
$$\alpha_{\pi}^{\text{eff}} = \frac{g_c^2 |\mu_{\pi}^2|}{f_{\pi}^2} \ll 1$$

(XEFT: Voloshin'2004, Fleming et al.'2007,...)

## Comment on pion exchange in $T_{cc}^+$

- Physical  $T_{cc}^+$  ( $m_\pi < m_{D^*} - m_D \implies \mu_\pi^2 < 0$  &  $|\mu_\pi| \ll m_\pi$ ):

$\implies$  3-body unitarity:

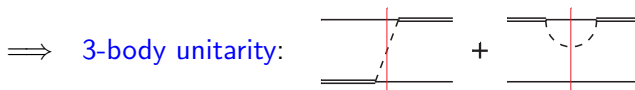


$\implies$   $T_{cc}^+$  spin partner at  $D^*D^*$  threshold

$$\alpha_\pi^{D\text{-wave}} \simeq g_c^2 q_{\text{typ}}^2 / f_\pi^2 \simeq g_c^2 m_D (m_{D^*} - m_D) / f_\pi^2 > 1$$

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- Lattice  $T_{cc}^+$  ( $m_\pi^{\text{lat}} > m_{D^*}^{\text{lat}} - m_D^{\text{lat}} \implies (\mu_\pi^{\text{lat}})^2 > 0$  &  $\mu_\pi^{\text{lat}} > m_\pi^{\text{ph}}$ ):

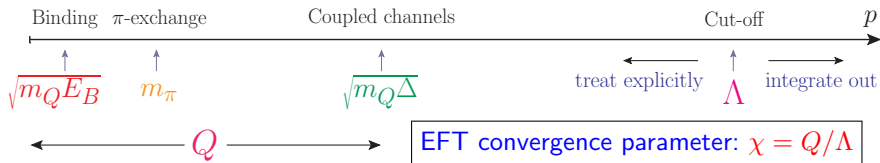
$\implies \alpha_\pi = g_c^2 \mu_\pi^2 / f_\pi^2 \sim 1$

- $\implies$  Left-hand cut in partial-wave amplitudes

$$\int d\Omega_{\hat{k}\hat{k}'} V_\pi(\mathbf{k} - \mathbf{k}') \sim \log \frac{\mu_\pi^2 + (k + k')^2}{\mu_\pi^2 + (k - k')^2} \xrightarrow{k' = k = p} \log \left( 1 + \frac{4p^2}{\mu_\pi^2} \right)$$



# Effective field theory for hadronic molecules

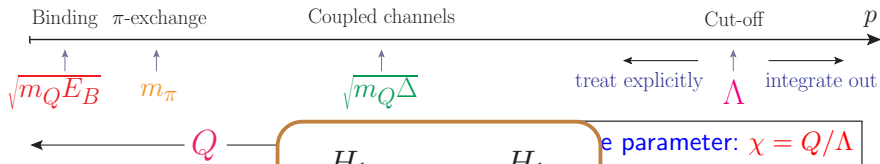


Interaction potential between heavy hadrons:

- Includes all **relevant interactions**  $\times + \text{---}\pi\text{---} + \dots$
- Complies with **relevant symmetries** (chiral, HQSS, etc)
- Incorporates **coupled-channel dynamics**
- **Expanded** in powers of  $p^2/\Lambda^2$  and **truncated** at necessary order (LO, NLO...)
- **Iterated** to all orders via (multichannel) Lippmann-Schwinger equation

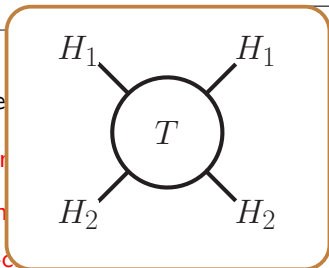
$$T = V - VGT$$

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+ ...  
(etc)

$$T = V - VGT$$

# EFT approach to $T_{cc}^+$

$$\gamma_B = \sqrt{m_D E_B} \simeq 25 \text{ MeV}$$

$$p_{\text{data}}^{\text{max}} = \sqrt{m_D \Delta E_{\text{data}}} \simeq 100 \text{ MeV}$$

$$p_{\text{coupl.ch.}} = \sqrt{m_D(m_{D^*} - m_D)} \simeq 500 \text{ MeV}$$



$\Lambda = 500 \text{ MeV}$

Potential at LO

OPE included

No couple channels

EFT approach to  $T_{cc}^+$ 

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- Lippmann-Schwinger equation for scattering amplitude ( $v_0$  — free parameter)

$$T = V - VGT$$

$$V = v_0 + V_\pi$$

- Production amplitude ( $P$  — free parameter = overall normalisation)

$$U = P - PGT$$

EFT approach to  $T_{cc}^+$ 

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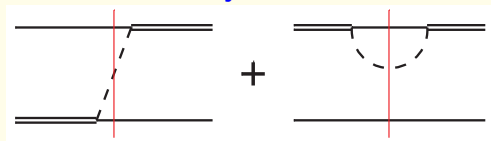
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$\Lambda = 500 \text{ MeV}$   
Potential at LO  
OPE included

multiple channels

3-body effects:



- Lippmann-Schwinger

(free parameter)

- Production amplitude ( $P$  — free parameter = overall normalisation)

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# Fitting schemes, results, and conclusions

$$\Gamma_{D^*} = \text{const}, \text{OPE}$$

$$\Gamma_{D^*}(p, M), \text{OPE}$$

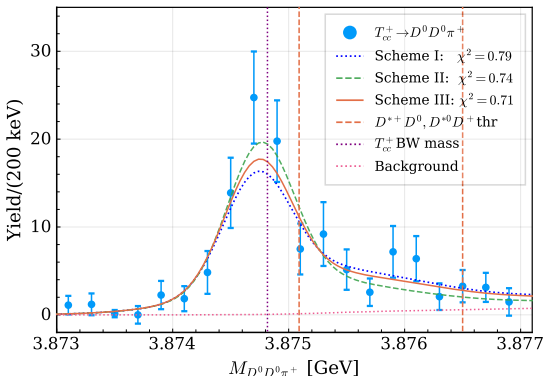
$$\Gamma_{D^*}(p, M), \text{OPE}$$

 $\chi^2/\text{d.o.f.}$ 

0.79

0.74

0.71

 $v_0 [\text{GeV}^{-2}]$ 
 $-23.34 \pm 0.08$ 
 $-22.88^{+0.08}_{-0.06}$ 
 $-5.04^{+0.10}_{-0.08}$ 
 $\text{Pole} [\text{keV}]$ 
 $-368^{+43}_{-42} - i(37 \pm 0)$ 
 $-333^{+41}_{-36} - i(18 \pm 1)$ 
 $-356^{+39}_{-38} - i(28 \pm 1)$ 


- (Quasi)bound state just below  $D^{*+} D^0$  threshold
- Compositeness: 70% & 30%

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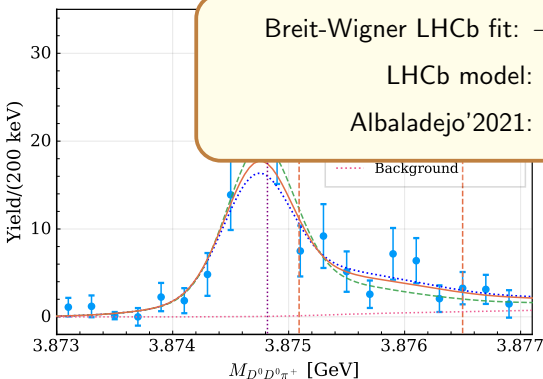
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Pole [keV]

 $-368^{+43}_{-42} - i(37 \pm 0)$  $-333^{+41}_{-36} - i(18 \pm 1)$  $-356^{+39}_{-38} - i(28 \pm 1)$ 

state just below  
 $D^0 D^0$  threshold

- Compositeness: 70% & 30%

## Spin partner $T_{cc}^{*+}$

HQSS:  $V^{I=0}(D^*D^* \rightarrow D^*D^*, 1^+) = V^{I=0}(D^*D \rightarrow D^*D, 1^+) = v_0$

$T_{cc}^+$  at  $D^*D$  threshold hints existence of  $T_{cc}^{*+}$  at  $D^*D^*$  threshold

Scheme I:  $\delta_{cc}^{*+} = -1.4$  MeV

Scheme II:  $\delta_{cc}^{*+} = -1.1$  MeV

Scheme III:  $\delta_{cc}^{*+} = -0.5$  MeV

where  $\delta_{cc}^{*+} = m_{T_{cc}^{*+}} - m_c^* - m_0^*$



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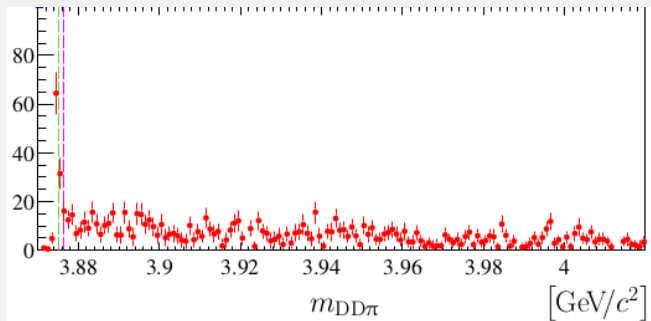
Disclaimer:

- Coupled-channel effects  $D^*D$ - $D^*D^*$  neglected
- Multi-body effects & OPE included not selfconsistently

Conclusion:  $T_{cc}^{*+}$  is likely to exist but no reliable prediction is possible yet

Spin partner  $T_{cc}^{*+}$ 

$$\text{HQSS: } V^{I=0}(D^*D^* \rightarrow D^*D^*, 1^+) = V^{I=0}(D^*D \rightarrow D^*D, 1^+) = v_0$$

 $T_{cc}^+$  atLHCb Collab., Nature Communications, **13**, 3351 (2022)

Disclaimer

- C
- M

Conclusion:  $T_{cc}^{*+}$  is likely to exist but no reliable prediction is possible yet

## $T_{cc}^+$ in lattice QCD

- “Signature of a Doubly Charm Tetraquark Pole in  $DD^*$  Scattering on Lattice,”  
M. Padmanath and S. Prelovsek,  
Phys. Rev. Lett. **129**, 032002 (2022)

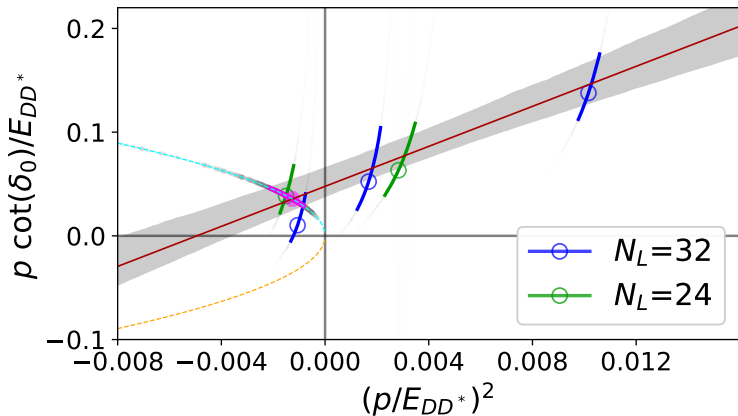
$$m_\pi = 280 \text{ MeV} \quad 2 \text{ points in } m_c \quad (5\text{-point update coming soon})$$

- “ $T_{cc}^+(3875)$  relevant  $DD^*$  scattering from  $N_f = 2$  lattice QCD,”  
S. Chen, C. Shi, Y. Chen, M. Gong, Z. Liu, W. Sun and R. Zhang,  
Phys. Lett. B **833**, 137391 (2022)

$$m_\pi = 348 \text{ MeV}$$

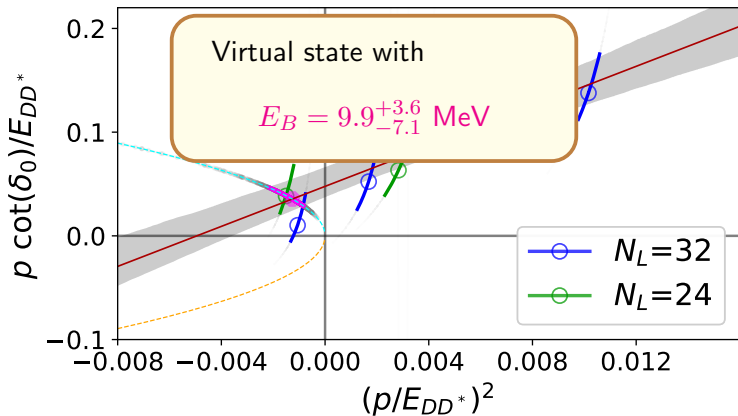
- “Doubly Charmed Tetraquark  $T_{cc}^+$  from Lattice QCD near Physical Point,”  
Y. Lyu, S. Aoki, T. Doi, T. Hatsuda, Y. Ikeda and J. Meng,  
Phys. Rev. Lett. **131**, 161901 (2023)

$$m_\pi = 146 \text{ MeV} \quad \text{HALQCD technique}$$

ERE analysis of lattice data for  $T_{cc}^+$ 

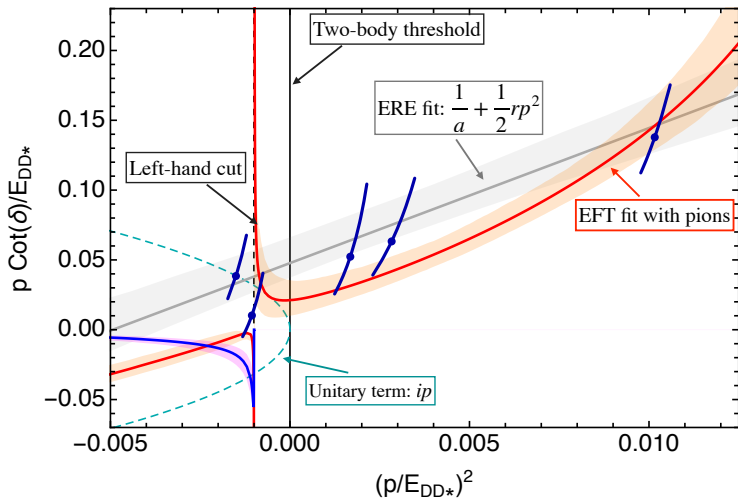
(Padmanath &amp; Prelovsek'2022)

$$-\frac{2\pi}{\mu} T^{-1}(E) = p \cot \delta - ip = \frac{1}{a_0} + \frac{1}{2} r_0 p^2 - ip$$

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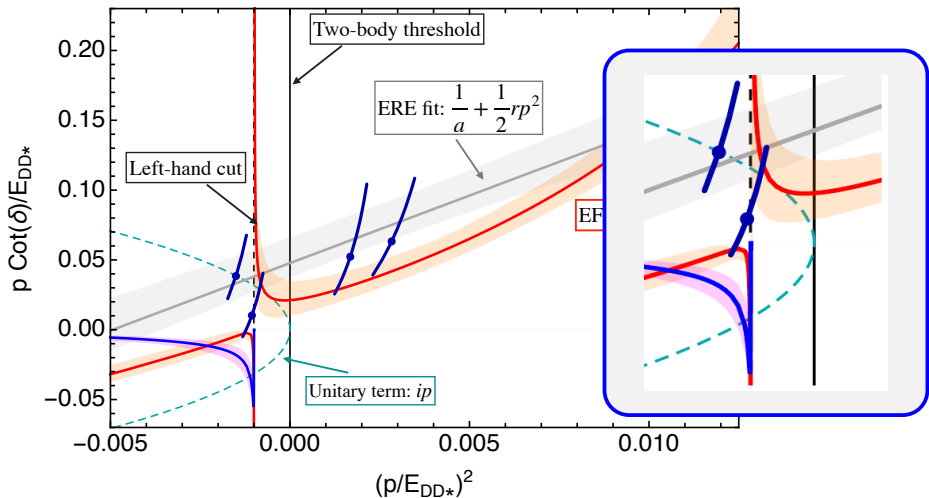
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Lattice data: Padmanath & Prelovsek, Phys.Rev.Lett. 129 (2022), 032002  
Theoretical curve: Du et al., Phys.Rev.Lett. 131 (2023), 131903

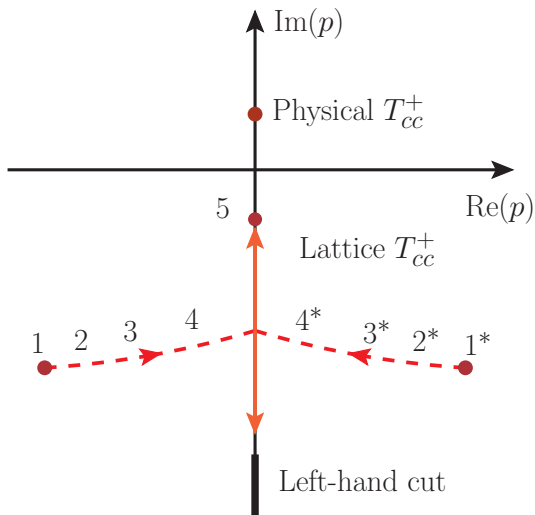
# EFT analysis of lattice data for $T_{cc}^+$



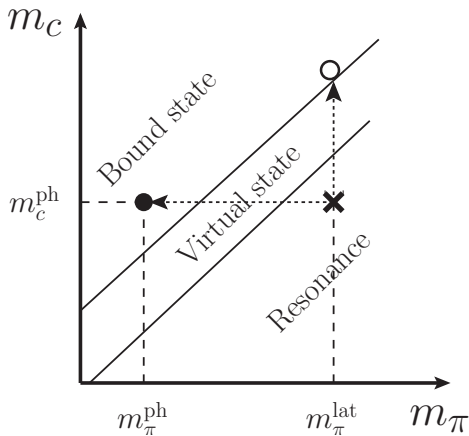
Lattice data: Padmanath & Prelovsek, Phys.Rev.Lett. 129 (2022), 032002

Theoretical curve: Du et al., Phys.Rev.Lett. 131 (2023), 131903

# Lattice $T_{cc}^+$ pole motion with increased $m_c$





$T_{cc}^+$  pole motion on  $(m_c, m_\pi)$  plane

- Filled circle — physical  $T_{cc}^+$
- Cross — starting lattice point
- Open circle — lattice  $T_{cc}^+$  as shallow bound state

# Conclusions

- $T_{cc}^+$  — a new **surprise** from experiment
- Another prominent example of **hadronic molecule** (bound state)
- Two **complementary** sources of information: **experiment** & **lattice**
- **Well established theoretical** tools  $\implies$  **reliable** conclusions
- Further questions to address:
  - **Binding** mechanisms?
  - Is  $T_{cc}^+$  a **cousin** of  $X(3872)$ ?
  - Do they have **further siblings**?
  - **Spin** &  $SU(3)$  partners?
  - How about  $T_{bc}$  (lattice & experiment) and  $T_{bb}$  (lattice)?

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- **Deuteron** (100),  $X$  (20),  $Z$  (10), **pentaquarks** (9),  $X(6900)$  (3),  $T_{cc}^+$  (2),...

## References & acknowledgments

Collaboration with colleagues from China, Germany, India, Slovenia, Spain is gratefully acknowledged!

- V. Baru, X. K. Dong, M. L. Du, A. Filin, F. K. Guo, C. Hanhart, A. Nefediev, J. Nieves, Q. Wang, “Effective range expansion for narrow near-threshold resonances,” Phys. Lett. B **833**, 137290 (2022)
- M. L. Du, V. Baru, X. K. Dong, A. Filin, F. K. Guo, C. Hanhart, A. Nefediev, J. Nieves, Q. Wang, “Coupled-channel approach to  $T_{cc}^+$  including three-body effects,” Phys. Rev. D **105**, 014024 (2022)
- M. L. Du, V. Baru, X. K. Dong, E. Epelbaum, A. Filin, F. K. Guo, C. Hanhart, A. Nefediev, J. Nieves, Q. Wang, “Role of left-hand cut contributions on pole extractions from lattice data: Case study for  $T_{cc}(3875)^+$ ”, Phys. Rev. Lett. **131**, 13 (2023)
- S. Collins, A. Nefediev, M. Padmanath, S. Prelovsek, in preparation

Thank you for your attention!