

Role of current conservation, reggeization and absorption in pion photoproduction

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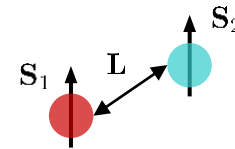
Excited QCD 2024 Workshop
Benasque Science Center, January 14-20, 2024



Hybrid mesons with exotic quantum numbers

- Mesons are experimentally characterized by quantum numbers:

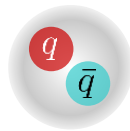
- Isospin
- Total angular momentum $J = L + S$ ($S = S_1 + S_2$)
- Parity $P = -(-1)^L$
- Charge conjugation $C = (-1)^{L+S}$



- The gluonic fields in hybrid mesons can give rise to states with **“exotic” quantum numbers**

“Smoking gun”

Conventional mesons

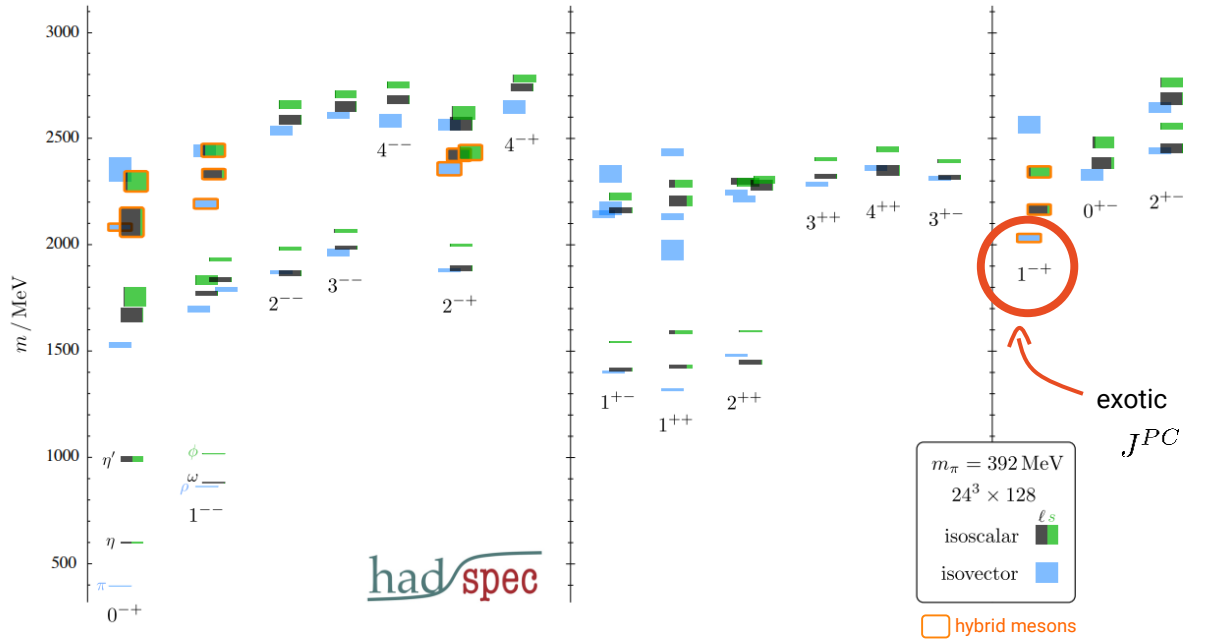


Hybrid mesons



J^{PC}	0^{--}	0^{++}	0^{-+}	0^{+-}
	1^{--}	1^{++}	1^{-+}	1^{+-}
	2^{--}	2^{++}	2^{-+}	2^{+-}
	3^{--}	3^{++}	3^{-+}	3^{+-}
	\vdots	\vdots	\vdots	\vdots

Spectrum of light mesons from lattice QCD

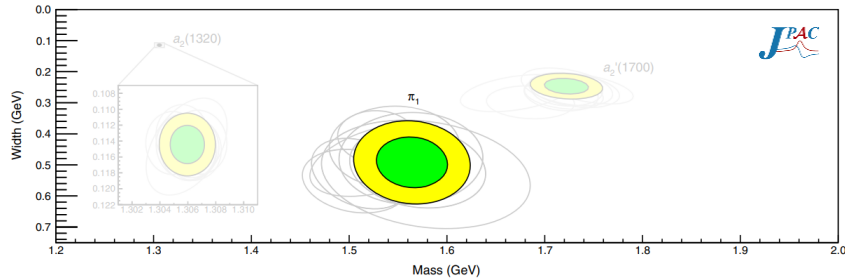


[J.J.Dudek, R.G.Edwards, P.Guo, and C.E.Thomas, *Phys.Rev.D* 88 (2013) 9, 094505]

Two experimental π_1 states vs one pole

- There are two 1^{-+} isovector states in the PDG.
- Coupled channel analyses favor the existence of only one broad 1^{-+} isovector state consistent with $\pi_1(1600)$ in the 1400–1600 MeV region.

[A.Rodas, A.Pilloni et al. *Phys.Rev.Lett.* 122 4, 042002 (2019)]



mass = $1564 \pm 24 \pm 86$ MeV
width = $492 \pm 54 \pm 102$ MeV



Data:
C.Adolph et al.,
Phys.Lett.B 740, 303 (2015)

$\pi_1(1400)$ $I^G(J^{PC}) = 1^-(1^{-+})$

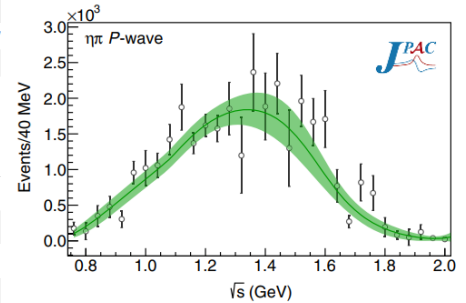
$\pi_1(1400)$ T-MATRIX POLE \sqrt{s} $(1405 \pm 4^{+15}_{-18}) - i(314 \pm 14^{+18}_{-69})$ MeV

$\pi_1(1400)$ MASS 1354 ± 25 MeV ($S = 1.8$)

$\pi_1(1400)$ WIDTH 330 ± 35 MeV

Decay Modes

Mode	Fraction (Γ_i / Γ)
Γ_1	$\eta\pi^0$ seen
Γ_2	$\eta\pi^-$ seen
Γ_3	$\eta'\pi$ not seen
Γ_4	$\rho(770)\pi$ not seen



$\pi_1(1600)$ $I^G(J^{PC}) = 1^-(1^{-+})$

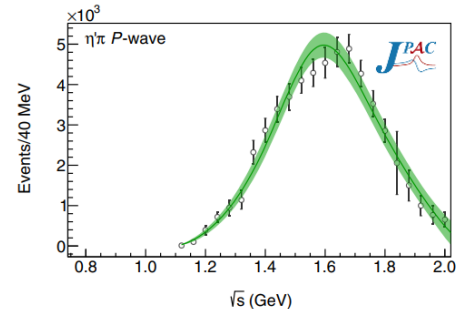
$\pi_1(1600)$ T-Matrix Pole \sqrt{s} $(1480 - 1680) - i(150 - 300)$ MeV

$\pi_1(1600)$ MASS 1661^{+15}_{-11} MeV ($S = 1.2$)

$\pi_1(1600)$ WIDTH 240 ± 50 MeV ($S = 1.7$)

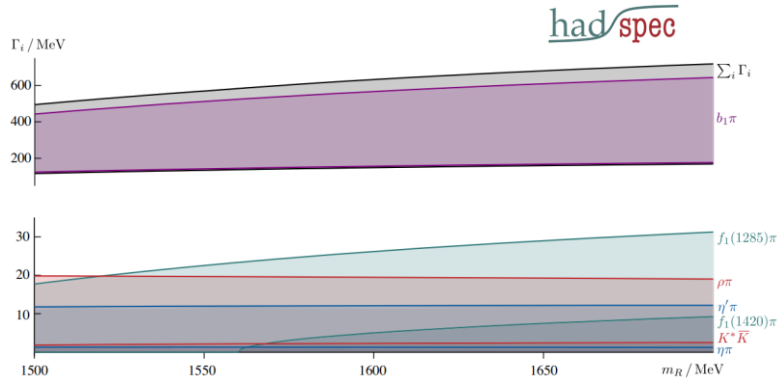
Decay Modes

Mode	Fraction (Γ_i / Γ)
Γ_1	$\pi\pi\pi$ seen
Γ_2	$\rho^0\pi^-$ seen
Γ_3	$f_2(1270)\pi^-$ not seen
Γ_4	$b_1(1235)\pi$ seen
Γ_5	$\eta'(958)\pi^-$ seen
Γ_6	$\eta\pi$ seen
Γ_7	$f_1(1285)\pi$ seen

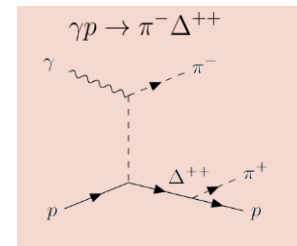
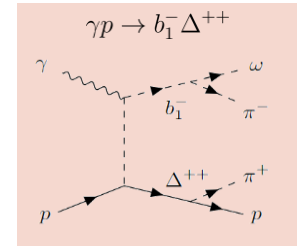
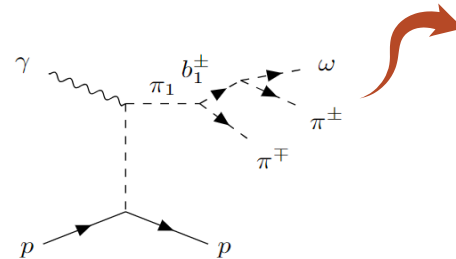


Search for the hybrid mesons

- Identifying the spectrum of hybrid mesons in photoproduction is the primary purpose of the **GLUEX** experiment at Jefferson Lab (Newport News, VA).
- Lattice QCD calculations suggest that $b_1\pi$ is the dominant decay channel of the $\pi_1(1600)$.



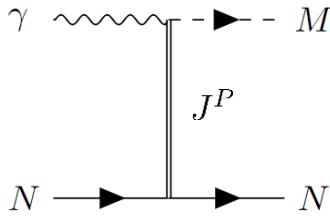
[A.J.Woss, J.J.Dudek, R.G.Edwards, C.E.Thomas and D.J.Wilson, *Phys.Rev.D* 103 5, 054502 (2021)]



[Talk by V. Shastry, Tue 15th]

- Understanding the production mechanism in light meson photoproduction reactions is essential for the hybrid meson searches in GlueX!

Generalities of meson photoproduction at high photon energies

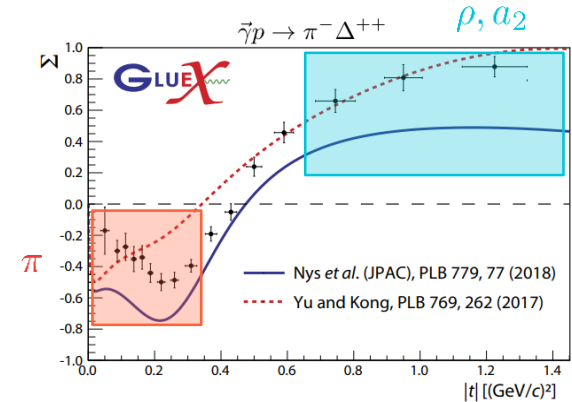
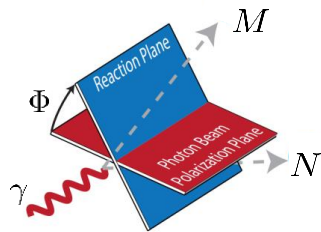


- At high energies, single meson photoproduction is dominated by the exchange of Regge trajectories in the t -channel.

- The beam polarization allows one to distinguish between exchange of

→ **unnatural** ($P(-1)^J = -1$) parity

→ **natural** ($P(-1)^J = 1$) parity



[GlueX Collaboration, Phys.Rev.C 103 (2021) 2, L022201]

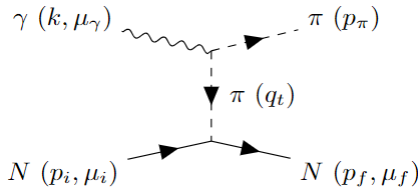
- In peripheral high energy **pion photoproduction**, pion exchange dominates at small momentum transfer:

- The t -channel pion exchange process is not gauge invariant by itself
- It is most susceptible to absorption corrections (longest range interaction)
- Reggeization scheme

Pion Born diagram

- s -channel reaction: $\gamma(k, \mu_\gamma) + N(p_i, \mu_i) \rightarrow \pi(p_\pi) + N(p_f, \mu_f)$
- Helicity amplitude: $A_{\mu_\gamma \mu_i \mu_f} = \epsilon_{\mu_\gamma}(k) \cdot J_{\mu_i \mu_f}$

t -channel Born diagram

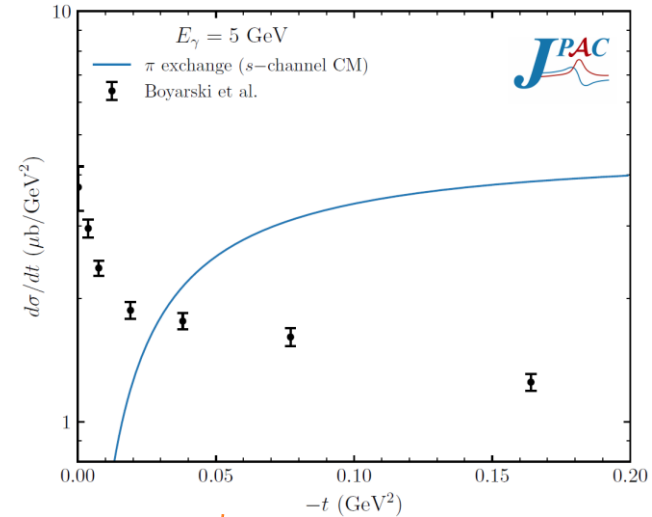


$$J_{\mu_i \mu_f, t}^\mu = -e_\pi g_{\pi NN} \frac{q_t^\mu - p_\pi^\mu}{t - \mu^2} \bar{u}_{\mu_f}(p_f) \gamma_5 u_{\mu_i}(p_i)$$

$$g_{\pi NN} = 13.48 \rightarrow \text{PS } \pi NN \text{ coupling}$$

→ The current is not conserved

↓
the amplitude is not gauge invariant
(frame dependent)



[G.Montana et al. (in preparation)]

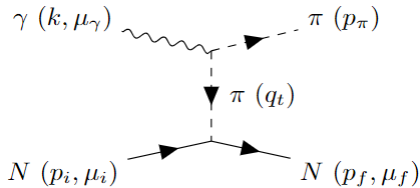
Pion exchange cannot reproduce experimental cross section at small momentum transfer

Adding the nucleon Born diagrams

- s -channel reaction: $\gamma(k, \mu_\gamma) + N(p_i, \mu_i) \rightarrow \pi(p_\pi) + N(p_f, \mu_f)$
- Helicity amplitude: $A_{\mu_\gamma \mu_i \mu_f} = \epsilon_{\mu_\gamma}(k) \cdot J_{\mu_i \mu_f}$

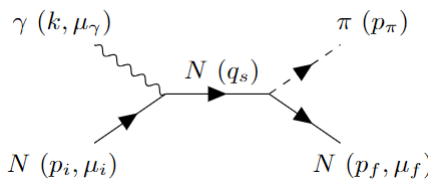
$$J_{\mu_i \mu_f}^\mu = J_{\mu_i \mu_f, t}^\mu + J_{\mu_i \mu_f, s}^\mu + J_{\mu_i \mu_f, u}^\mu \quad \longrightarrow \quad \text{The total current is conserved}$$

t -channel Born diagram



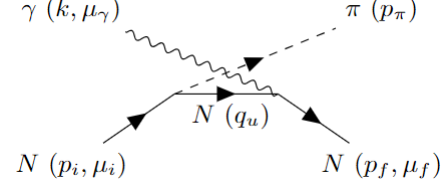
$$J_{\mu_i \mu_f, t}^\mu = -e_\pi g_{\pi NN} \frac{q_t^\mu - p_\pi^\mu}{t - \mu^2} \bar{u}_{\mu_f}(p_f) \gamma_5 u_{\mu_i}(p_i)$$

s -channel



$$J_{\mu_i \mu_f, s}^\mu = e_N g_{\pi NN} \bar{u}_{\mu_f}(p_f) \gamma_5 \frac{\not{q}_s + M}{s - M^2} \gamma^\mu u_{\mu_i}(p_i)$$

u -channel



$$J_{\mu_i \mu_f, u}^\mu = e_N g_{\pi NN} \bar{u}_{\mu_f}(p_f) \gamma^\mu \frac{\not{q}_u + M}{u - M^2} \gamma_5 u_{\mu_i}(p_i)$$

- Separate electric and magnetic contributions: $A_{\mu_\gamma \mu_i \mu_f} = A_{\mu_\gamma \mu_i \mu_f}^e + A_{\mu_\gamma \mu_i \mu_f}^m$

$$A_{\mu_\gamma \mu_i \mu_f}^e = 2g_{\pi NN} \left[e_\pi \frac{(\epsilon_{\mu_\gamma} \cdot p_\pi)}{t - \mu^2} + e_{N_i} \frac{(\epsilon_{\mu_\gamma} \cdot p_i)}{s - M^2} + e_{N_f} \frac{(\epsilon_{\mu_\gamma} \cdot p_f)}{u - M^2} \right] \bar{u}_{\mu_f}(p_f) \gamma_5 u_{\mu_i}(p_i)$$

$$A_{\mu_\gamma \mu_i \mu_f}^m = g_{\pi NN} \left[\frac{e_{N_i}}{s - M^2} + \frac{e_{N_f}}{u - M^2} \right] \bar{u}_{\mu_f}(p_f) \gamma_5 \not{k} \not{\epsilon}_{\mu_\gamma} u_{\mu_i}(p_i)$$

Electric term

$$A_{\mu\gamma\mu_i\mu_f}^e = 2g_{\pi NN} \left[e_{\pi} \frac{(\epsilon_{\mu\gamma} \cdot p_{\pi})}{t - \mu^2} + e_{N_i} \frac{(\epsilon_{\mu\gamma} \cdot p_i)}{s - M^2} + e_{N_f} \frac{(\epsilon_{\mu\gamma} \cdot p_f)}{u - M^2} \right] \bar{u}_{\mu_f}(p_f) \gamma_5 u_{\mu_i}(p_i)$$

- Using momentum conservation and electric charge conservation ($e_{N_i} = e_{\pi} - e_{N_f}$):

$$A_{\mu\gamma\mu_i\mu_f}^e = \boxed{g_{\pi NN} \left[2e_{\pi} \left(\frac{(\epsilon_{\mu\gamma} \cdot p_{\pi})}{t - \mu^2} + \frac{(\epsilon_{\mu\gamma} \cdot (p_i + p_f))}{s - u} \right) \right]} \longrightarrow \text{Minimal gauge invariant (m.g.i.)}$$

$$+ e_{N_i} \left(\frac{(\epsilon_{\mu\gamma} \cdot p_{\pi})}{s - M^2} + \frac{(\epsilon_{\mu\gamma} \cdot (p_i + p_f))}{s - u} \frac{t - \mu^2}{s - M^2} \right)$$

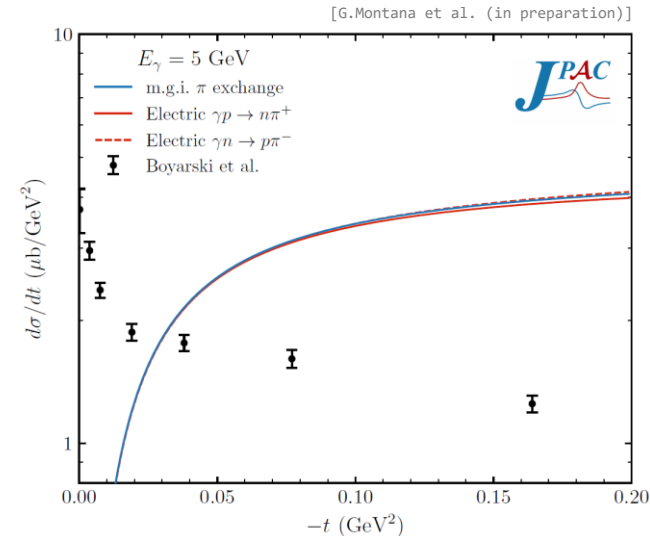
$$- e_{N_f} \left(\frac{(\epsilon_{\mu\gamma} \cdot p_{\pi})}{u - M^2} + \frac{(\epsilon_{\mu\gamma} \cdot (p_i + p_f))}{s - u} \frac{t - \mu^2}{u - M^2} \right) \bar{u}_{\mu_f}(p_f) \gamma_5 u_{\mu_i}(p_i)$$

- Differential cross section

$$\left(\frac{d\sigma}{dt} \right)_{\pi\text{-m.g.i.}} = 4 \left(\frac{s - M^2}{s - u} \right)^2 \left(\frac{d\sigma}{dt} \right)_{\pi\text{-bare, CM}} \stackrel{t \rightarrow t_{\min}}{\approx} \left(\frac{d\sigma}{dt} \right)_{\pi\text{-bare, CM}}$$

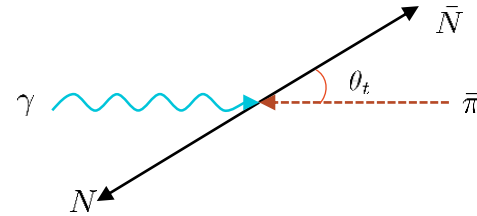
$$\left(\frac{d\sigma}{dt} \right)_{e, \gamma p \rightarrow \pi^+ n} = \left(\frac{d\sigma}{dt} \right)_{\pi\text{-bare, CM}}$$

$$\left(\frac{d\sigma}{dt} \right)_{e, \gamma n \rightarrow \pi^- p} = 4 \left(\frac{s - M^2}{M^2 - u} \right)^2 \left(\frac{d\sigma}{dt} \right)_{\pi\text{-bare, CM}} \stackrel{t \rightarrow t_{\min}}{\approx} \left(\frac{d\sigma}{dt} \right)_{\pi\text{-bare, CM}}$$



Pion pole in the t -channel rest frame

- t -channel reaction: $\gamma(k, \lambda_\gamma) + \bar{\pi}(-p_\pi) \rightarrow \bar{N}(-p_i, \lambda_i) + N(p_f, \lambda_f)$.



$$A_{\lambda_\gamma \lambda_i \lambda_f}^e = g_{\pi NN} \left[2e_\pi \left(\frac{1}{s-u} \right) + e_{N_i} \left(\frac{1}{s-M^2} - \frac{2}{s-u} \right) - e_{N_f} \left(\frac{1}{u-M^2} - \frac{2}{s-u} \right) \right] (\epsilon_{\lambda_\gamma} \cdot (p_i + p_f)) \bar{u}_{\lambda_f}(p_f) \gamma_5 v_{\lambda_i}(-p_i)$$

→ The nucleon Born terms contain a “pion pole” that arises from kinematical factors

$$\bar{\epsilon}_{\mu\nu} \equiv \sum_{\lambda_\gamma=\pm 1} \epsilon_{\lambda_\gamma, \mu}(k) \epsilon_{\lambda_\gamma, \nu}^*(k) = -g_{\mu\nu} - \frac{k_\mu k_\nu}{(k \cdot n)^2} + \frac{k_\mu n_\nu + k_\nu n_\mu}{k \cdot n} \quad \text{with } n = (1, \mathbf{0})$$

$$\bar{\epsilon}_{\mu\nu} P^\mu P^\nu = \frac{2(k \cdot P)(n \cdot P)(k \cdot n) - P^2(k \cdot n)^2 - (k \cdot P)^2}{(k \cdot n)^2} \sim \frac{1}{t - \mu^2} \quad \text{with } P^\mu = (p_i + p_f)^\mu$$

→ Reggeization of the pion should involve the electric components of the nucleon Born terms

Magnetic term

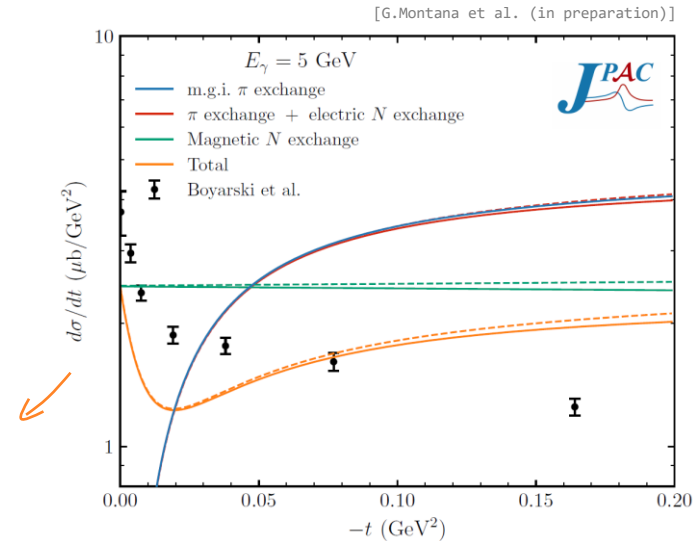
$$A_{\mu_\gamma \mu_i \mu_f}^m = g_{\pi NN} \left[\frac{e_{N_i}}{s - M^2} + \frac{e_{N_f}}{u - M^2} \right] \bar{u}_{\mu_f}(p_f) \gamma_5 \not{k} \not{\epsilon}_{\mu_\gamma} u_{\mu_i}(p_i)$$

- In the limit $t \rightarrow t_{\min}$:
 - The pion exchange diagram vanishes.
 - The electric component of the nucleon exchanges also vanish.
 - The magnetic component of the nucleon exchanges has small dependence in t .

The size of the cross section agrees reasonably well with the data when the magnetic contribution of the nucleon-exchange diagrams is taken into account.

Alternative explanations of the experimental data:

- Absorption corrections
- Pion conspiracy



Reggeization of pion exchange

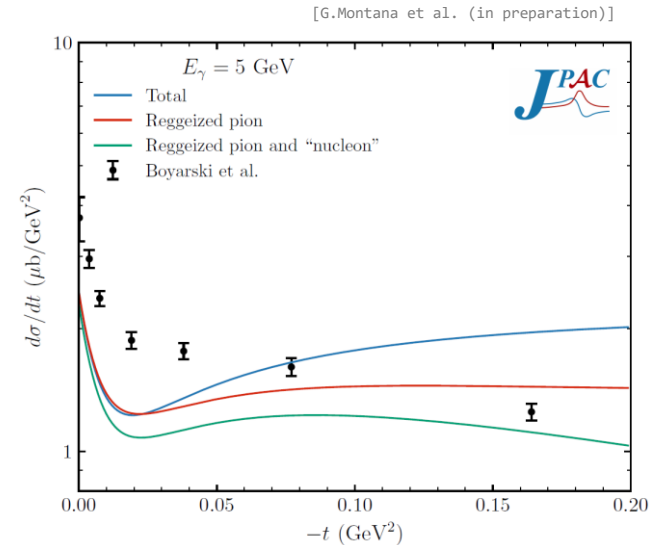
- The exchanged pion is expected to reggeize:
 - Consider the exchange of all the members of the pion trajectory i.e. all the particles with different spin J but the same parity $P = -(-1)^J$, isospin, as the pion.
- In the Regge-pole approximation:

$$\frac{1}{t - \mu^2} \rightarrow \mathcal{P}_\pi^{\text{Regge}} = \frac{\pi \alpha'_\pi}{2} \frac{1 + e^{-i\pi \alpha_\pi(t)}}{\sin \pi \alpha_\pi(t)} \left(\frac{s}{s_0} \right)^{\alpha_\pi(t)}$$

Pion trajectory: $\alpha_\pi(t) = \alpha'_\pi(t - \mu^2)$ with $\alpha'_\pi = 0.7$

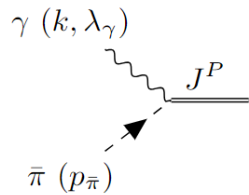
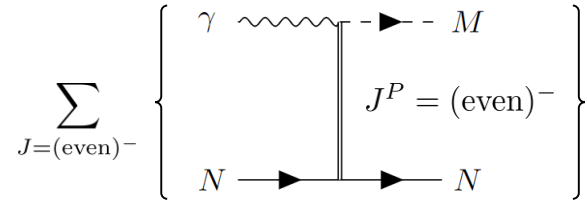
- In the VGL model, the full Born amplitude (pion and nucleon exchanges, electric and magnetic) was reggeized.

[M.Guidal, J.M.Laget and M. Vanderhaeghen, *Nucl.Phys.A* 627 (1997) 645-678]



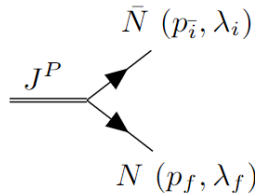
New approach to Reggeization of pion exchange

- Consider the explicit exchange of all the t-channel partial waves that have different spin J but the same parity, $P = -(-1)^J$, isospin, as the pion.
- Perform the summation over J
- Vertices coupling $\gamma\pi$ and $N\bar{N}$ to $J^P = (\text{even})^-$:



$$1^- \otimes 0^- = 1^+ \begin{cases} L = 1 & \text{for } J = 0 \\ L = \{J - 1, J + 1\} & \text{for } J \geq 2 \end{cases}$$

$$V_{\lambda_\gamma}^{\text{un}}(J) = 2e_{\pi} \left[k^{\nu_1} \dots k^{\nu_J} \epsilon_{\lambda_\gamma, \mu}(k) p_{\pi}^{\mu} - k^{\nu_1} \dots k^{\nu_{J-1}} \epsilon_{\lambda_\gamma}^{\nu_J}(k) (k \cdot p_{\pi}) \right] \epsilon_{\nu_1, \dots, \nu_J}^*(M)$$



$$\frac{1}{2}^+ \otimes \frac{1}{2}^- = 0^- \oplus 1^- \longrightarrow L = J$$

helicity non-flip helicity flip

$$V_{\lambda_i \lambda_f}^{\text{un, NF}}(J) = g P^{\nu_1} \dots P^{\nu_J} \epsilon_{\nu_1, \dots, \nu_J}(M) \bar{u}_{\lambda_f}(p_f) \gamma_5 v_{\lambda_i}(p_i)$$

$$V_{\lambda_i \lambda_f}^{\text{un, F}}(J) = g P^{\nu_1} \dots P^{\nu_{J-1}} \epsilon_{\nu_1, \dots, \nu_J}(M) \bar{u}_{\lambda_f}(p_f) \gamma^{\nu_J} \gamma_5 v_{\lambda_i}(p_i)$$

New approach to Reggeization of pion exchange

- Compute the full helicity amplitudes. We take the frame in which the exchanged particle is at rest (t -channel frame).

$$\begin{aligned} A_{\lambda_\gamma \lambda_i \lambda_f}^{\text{un,NF}}(J) &= [(k \cdot P)(\epsilon_{\lambda_\gamma} \cdot p_{\bar{\pi}}) - (k \cdot p_{\bar{\pi}})(\epsilon_{\lambda_\gamma} \cdot P)] A_J(s, t) \bar{u}_{\lambda_f}(p_f) \gamma_5 v_{\lambda_i}(-p_i) \\ &= -(k \cdot p_{\bar{\pi}}) 2|\mathbf{p}| d_{\lambda_\gamma 0}^1(\theta_t) A_J(s, t) \bar{u}_{\lambda_f}(p_f) \gamma_5 v_{\lambda_i}(-p_i) \end{aligned}$$

$$\begin{aligned} A_{\lambda_\gamma \lambda_i \lambda_f}^{\text{un,F}}(J) &= \bar{u}_{\lambda_f}(p_f) [(k \cdot \gamma)(\epsilon_{\lambda_\gamma} \cdot p_{\bar{\pi}}) - (k \cdot p_{\bar{\pi}})(\epsilon_{\lambda_\gamma} \cdot \gamma)] \gamma_5 v_{\lambda_i}(-p_i) A_J(s, t) \\ &= (k \cdot p_{\bar{\pi}}) \lambda' \delta_{\lambda' \pm 1} 4\sqrt{2} |\mathbf{p}| d_{\lambda_\gamma \lambda'}^1(\theta_t) A_J(s, t) \end{aligned}$$

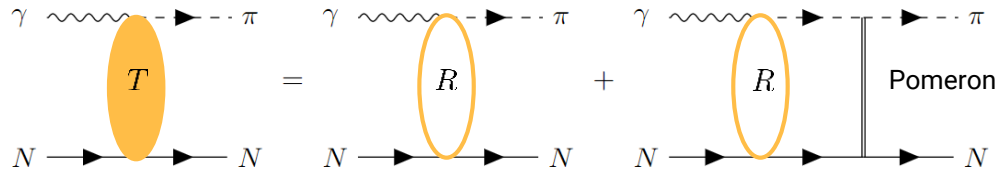
with the scalar function ($J \geq 2$) $A_J(s, t) = -(-1)^{J+\lambda'} 2e_{\bar{\pi}} g \mathcal{P}_J(2|\mathbf{k}||\mathbf{p}|)^{J-1} (c_J)^2 \frac{J+1}{2J} P_{J-1}^{|\lambda_\gamma - \lambda'|, |\lambda_\gamma + \lambda'|}(z_t)$,

- Extend the definition to $J = 0$ by comparing with m.g.i. pion exchange amplitude.
- Next, sum the Regge poles (work in progress):

$$\sum_{J=0,2,4,\dots} A_J(s, t) \quad \text{using the Reggeon propagator } \mathcal{P}_J \rightarrow \mathcal{P}_J^{\text{Regge}} = \frac{\alpha'}{J - \alpha(t)}$$

Absorption

- Multiple elastic rescattering of the final state particles.
- We can write a Bethe-Salpeter-like equation that combines the Reggeized exchange amplitude with an elastic scattering amplitude (Pomeron exchange):



$$A_{\lambda,\lambda'}^T(\mathbf{k}, \mathbf{p}) = A_{\lambda,\lambda'}^R(\mathbf{k}, \mathbf{p}) - i \sum_{\lambda''} \int \frac{dq^4}{(2\pi)^4} \frac{A_{\lambda,\lambda''}^R(\mathbf{k}, \mathbf{q}) A_{\lambda'',\lambda'}^P(\mathbf{k}, \mathbf{p})}{[q^2 - m^2][(P - q)^2 - M^2]}$$

$$\equiv A_{\lambda,\lambda'}^R(\mathbf{k}, \mathbf{p}) + \delta A_{\lambda,\lambda'}^R(\mathbf{k}, \mathbf{p})$$

- For the partial waves:

$$a_{\lambda,\lambda'}^{T,J}(s) = a_{\lambda,\lambda'}^{R,J}(s) + \delta a_{\lambda,\lambda'}^{R,J}(s)$$

- Absorptive Regge cut models rely on the fit a free parameter, accounting for the “strength” of the intermediate inelastic channels

$$A_{\lambda,\lambda'}^T(s, t) = A_{\lambda,\lambda'}^R(s, t) + \lambda \delta A_{\lambda,\lambda'}^R(s, t) \quad \text{with } \lambda > 1$$

[F.Henyey, G.L.Kane, J.Pumplin, M.H.Ross, *Phys.Rev.* 182 (1969) 1579-1594]

- If λ is too large, the lowest partial waves undergo an unphysical sign change instead of being absorbed

↪ over-absorption (no fundamental physics behind)

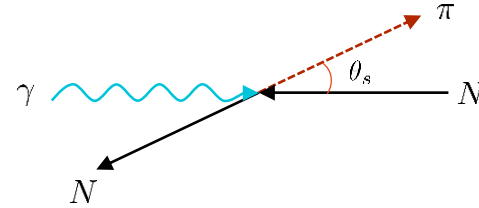
SUMMARY

- Understanding the features of pion exchange in hadronic reactions has been of fundamental interest for many decades, and not yet satisfactorily established.
- A precise comprehension of the production mechanisms is crucial for the light hybrid meson searches.
- At high energies, meson photoproduction reactions are dominated by the exchange of Regge trajectories, in particular, the pion trajectory plays a major role at low momentum transfer.
- In single pion photoproduction, pion exchange is not able to explain the cross-section data at small t :
 - The t -channel pion exchange process is not gauge invariant.
 - Electric current conservation requires to include the s - and u -channel nucleon exchanges.
 - The magnetic contribution of the nucleon exchanges gives a non-zero cross section at $t = 0$ of similar size than the data.
 - Proper Reggeization of the pion exchange has to take into account gauge invariance.
 - New approach to Reggeization is on its way:
 - Explicit exchange of all the members of the pion trajectory.

Frame dependence of pion exchange

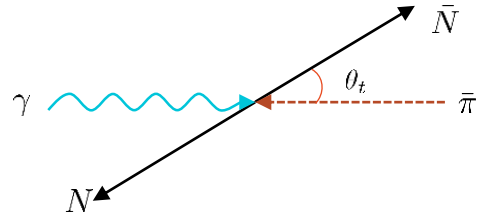
- s -channel reaction: $\gamma(k, \mu_\gamma) + N(p_i, \mu_i) \rightarrow \pi(p_\pi) + N(p_f, \mu_f)$

$$A_{\mu_\gamma \mu_i \mu_f}^{e, s\text{-CM}} = g_{\pi NN} \left[2e_\pi \left(\frac{1}{t - \mu^2} - \frac{1}{s - u} \right) + 2e_{N_i} \left(\frac{1}{s - u} \right) - 2e_{N_f} \left(\frac{1}{u - M^2} + \frac{1}{s - u} \right) \right] (\epsilon_{\mu_\gamma} \cdot p_\pi) \bar{u}_{\mu_f}(p_f) \gamma_5 u_{\mu_i}(p_i)$$

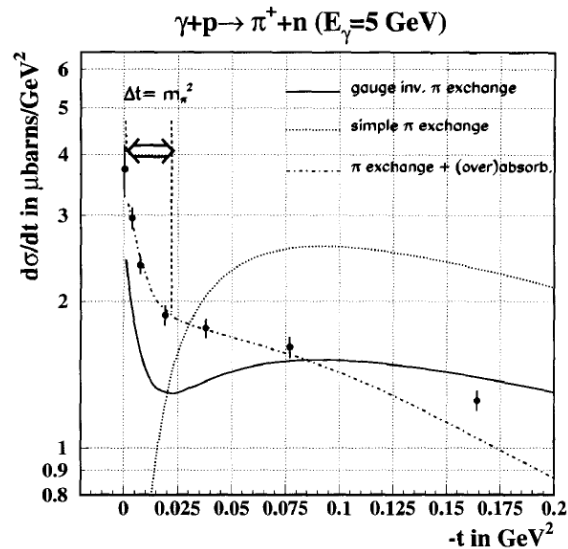


- t -channel reaction: $\gamma(k, \lambda_\gamma) + \bar{\pi}(-p_\pi) \rightarrow \bar{N}(-p_i, \lambda_i) + N(p_f, \lambda_f)$

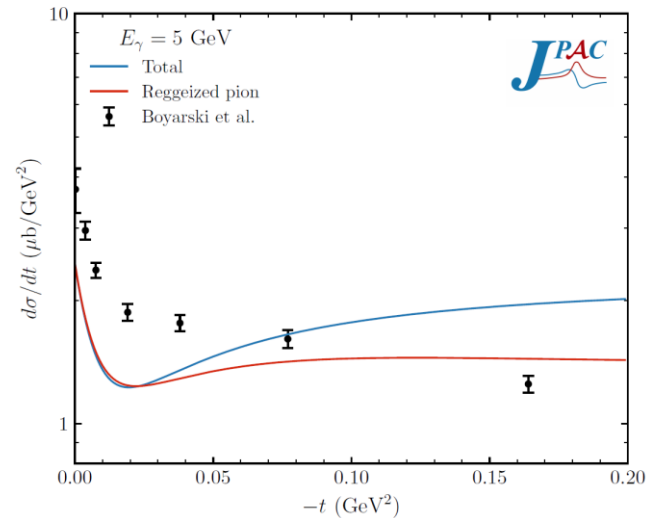
$$A_{\lambda_\gamma \lambda_i \lambda_f}^e = g_{\pi NN} \left[2e_\pi \left(\frac{1}{s - u} \right) + e_{N_i} \left(\frac{1}{s - M^2} - \frac{2}{s - u} \right) - e_{N_f} \left(\frac{1}{u - M^2} - \frac{2}{s - u} \right) \right] (\epsilon_{\lambda_\gamma} \cdot (p_i + p_f)) \bar{u}_{\lambda_f}(p_f) \gamma_5 v_{\lambda_i}(-p_i)$$



Reggeization of pion exchange (comparison with VGL)



[M.Guidal, J.M.Laget and M. Vanderhaeghen, *Nucl.Phys.A* 627 (1997) 645-678]



[G.Montana et al. (in preparation)]