

Quark mass dependence of the $D_{s0}^*(2317)$

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D meson functions

- ◆ Heavy meson masses from χPT with HQSS at one loop order

$$\frac{1}{4}(D + 3D^*) = m_H + \alpha_a - \sum_{X=\pi,K,\eta} \beta_a^{(X)} \frac{M_X^3}{16\pi f^2} + \sum_{X=\pi,K,\eta} (\gamma_a^{(X)} - \lambda_a^{(X)} \alpha_a) \frac{M_X^2}{16\pi^2 f^2} \log(M_X^2/\mu^2) + c_a$$

$$(D^* - D) = \Delta + \sum_{X=\pi,K,\eta} (\gamma_a^{(X)} - \lambda_a^{(X)} \Delta) \frac{M_X^2}{16\pi^2 f^2} \log(M_X^2/\mu^2) + \delta c_a$$

* E. E. Jenkins, Nucl. Phys. B 412, 181 (1994), hep-ph/9212295

$$\left. \begin{array}{l} \frac{1}{4}(D + 3D^*) = m_H + f(\sigma, a, b, c, d) \\ (D^* - D) = \Delta + g(\Delta^{(\sigma)}, \Delta^{(a)}) \end{array} \right\} \begin{array}{l} 2 \cdot 12 \text{ tree level} \\ \text{parameters} \\ + \\ 7 \text{ parameters} \end{array} \xrightarrow{\hspace{1cm}} \begin{array}{l} 31 \text{ parameters} \\ 160 \text{ points} \end{array}$$

LASSO Regression Method

$$\chi_P^2(p, d) = \chi^2(p, d) + \lambda^4 \sum_i^n |p_i| \rightarrow$$

70% of data $\chi_P^2(p, d_{train})$
30% of data $\chi_P^2(p, d_{test})$

*J. Landay, M. Döring, C. Fernández-Ramírez, B. Hu, and R. Molina, Phys. Rev. C 95, 015203 (2017), 1610.07547.

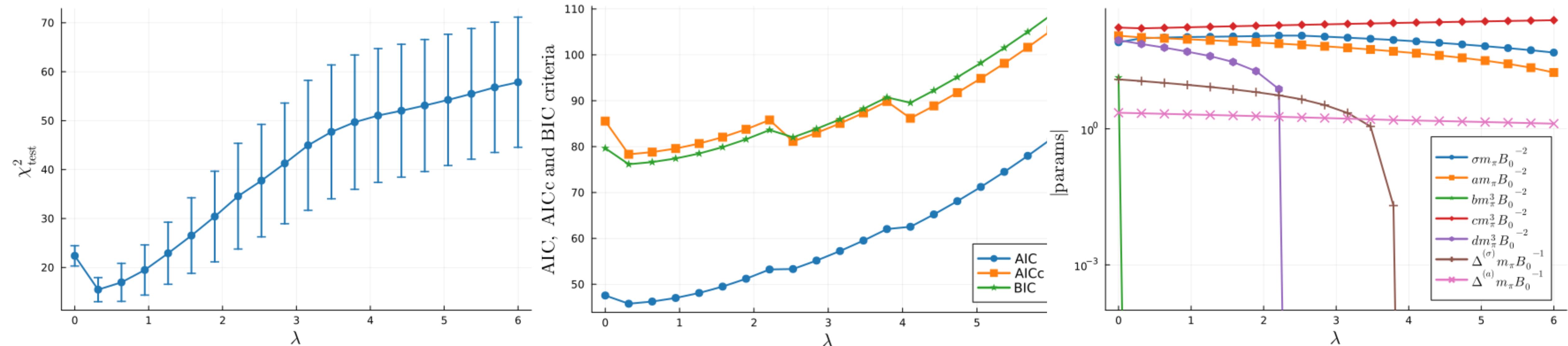
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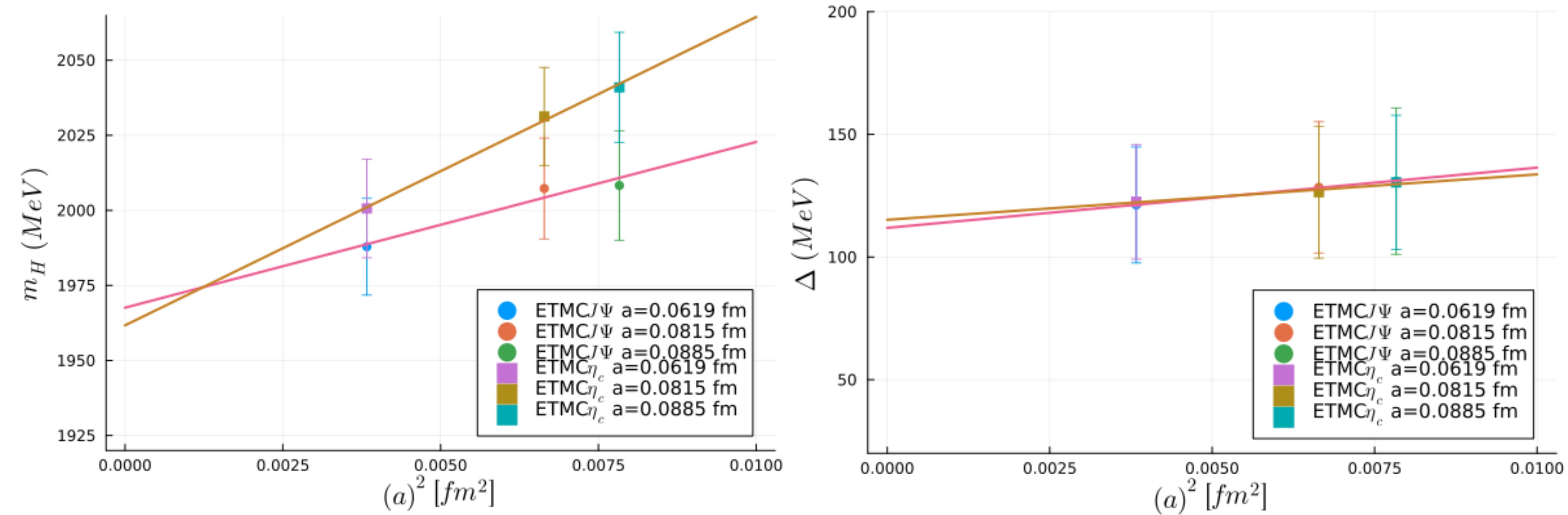
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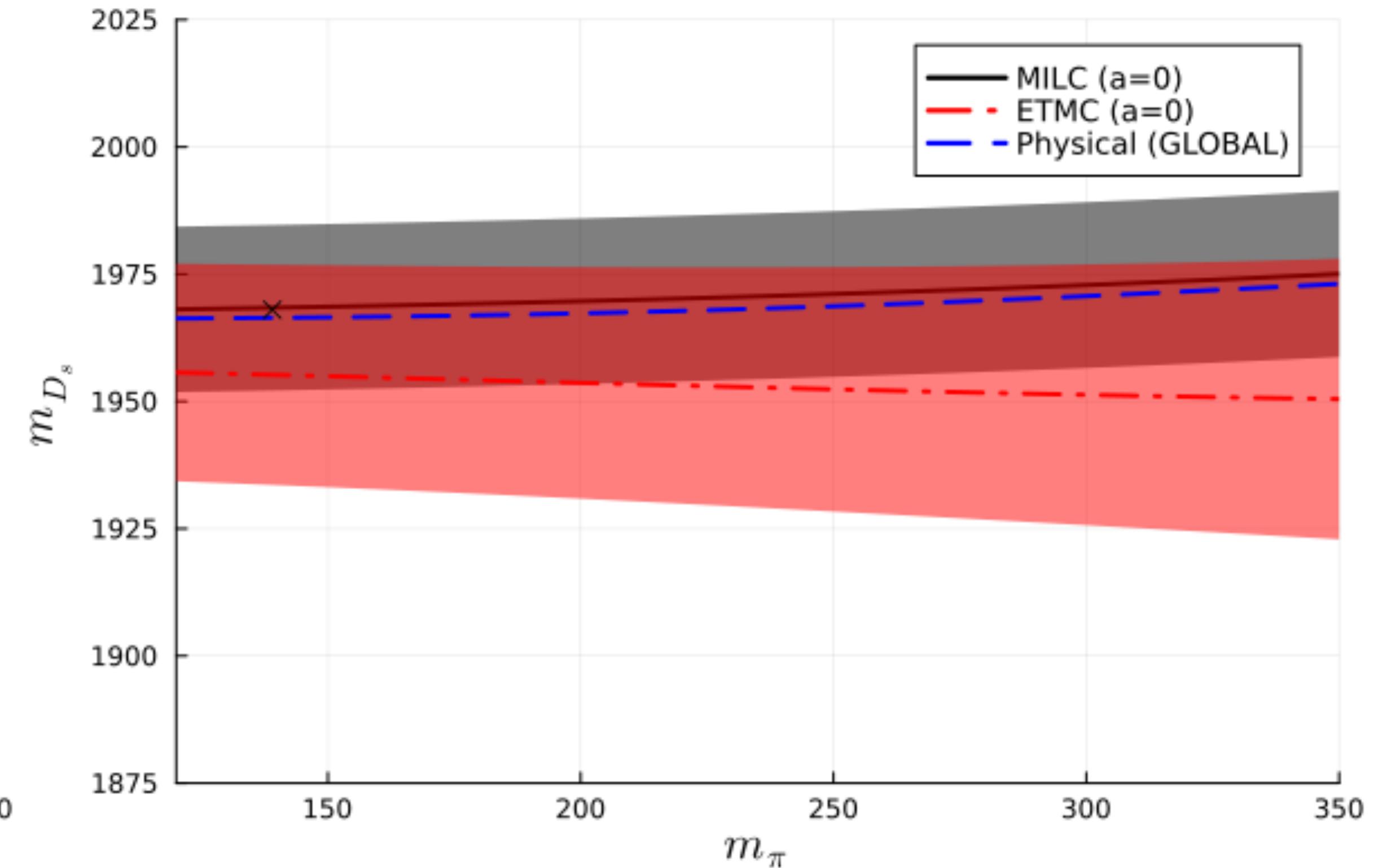
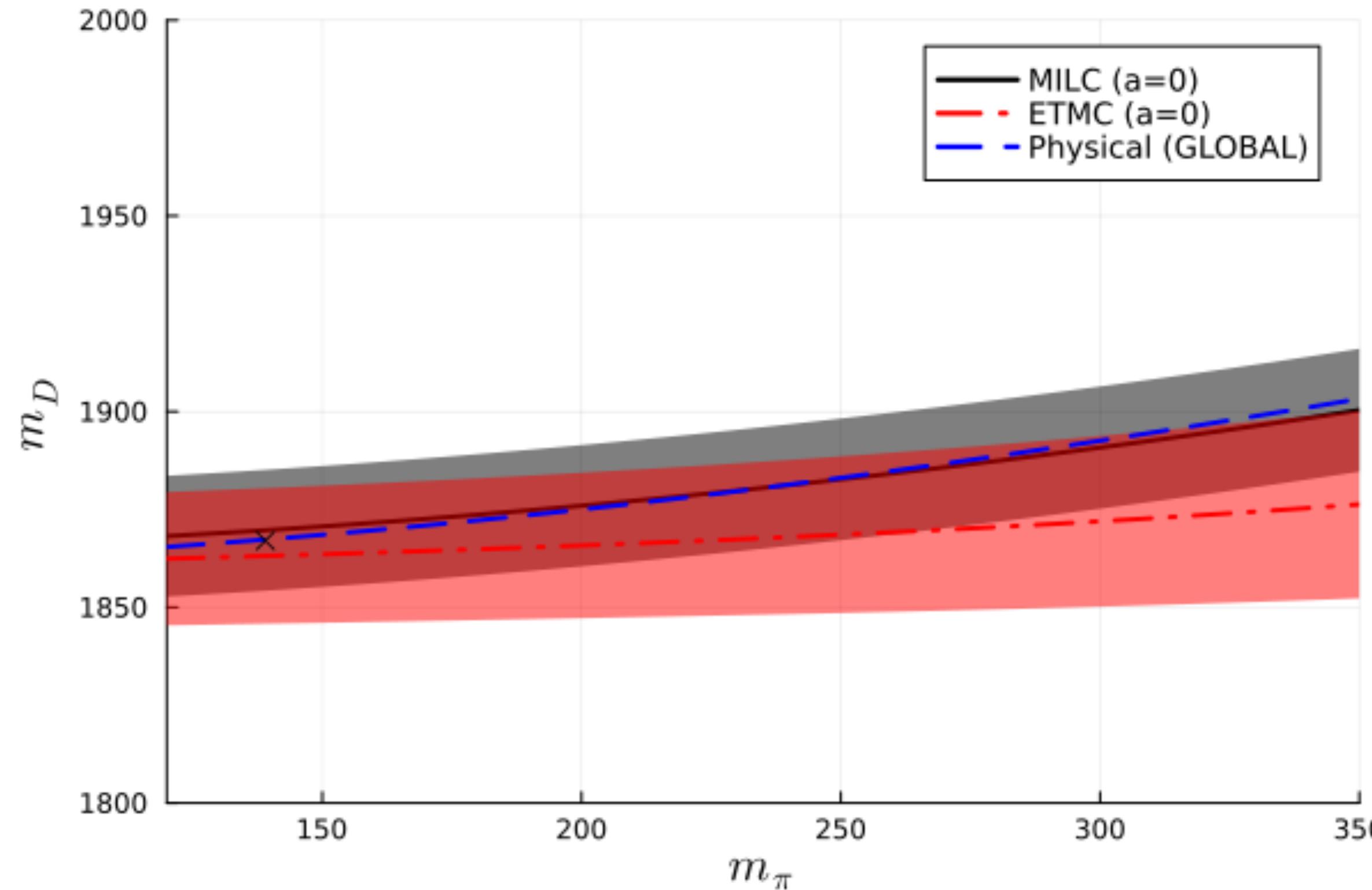
For ETMC data:



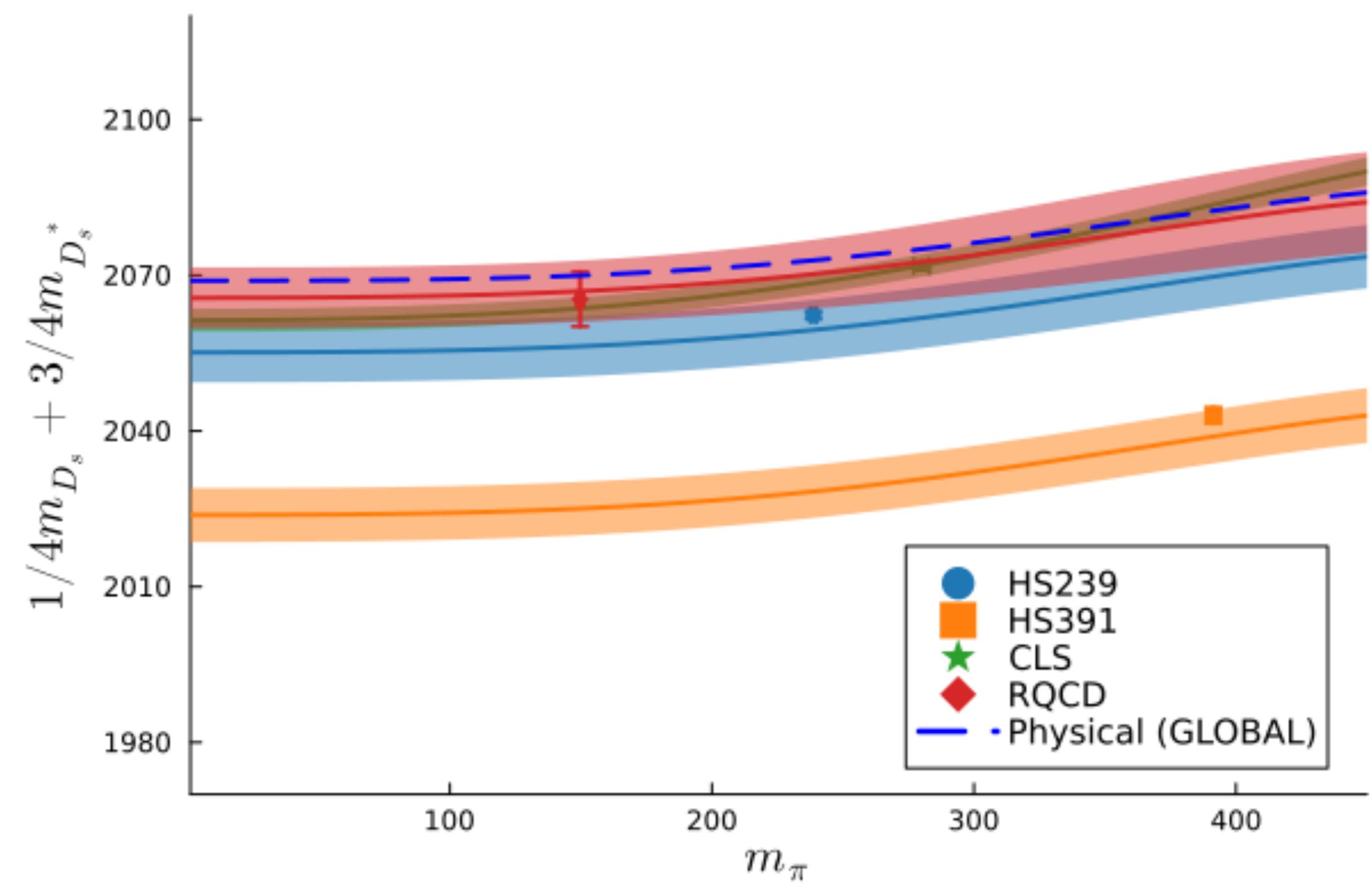
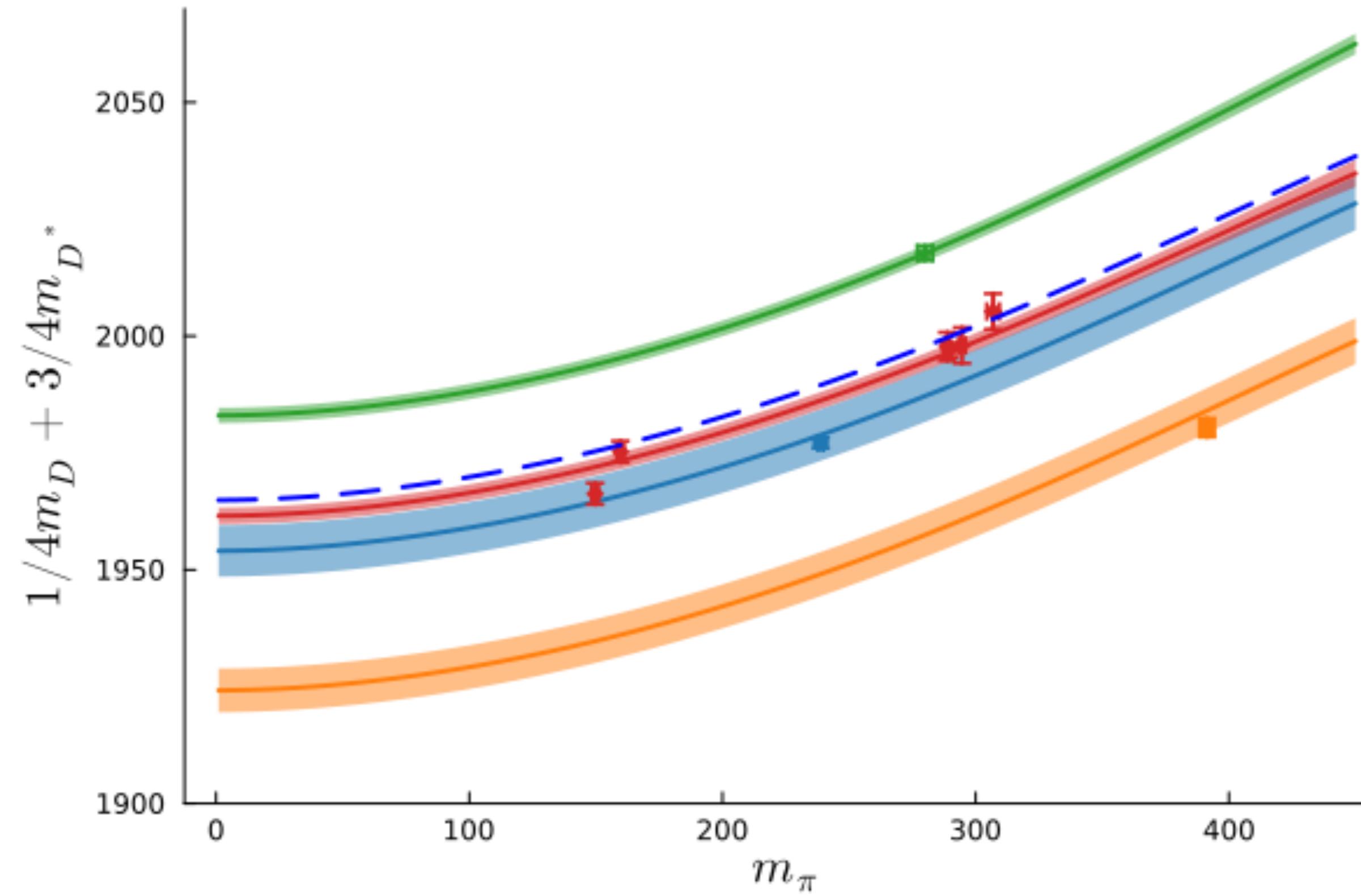
ETMC continuum extrapolation



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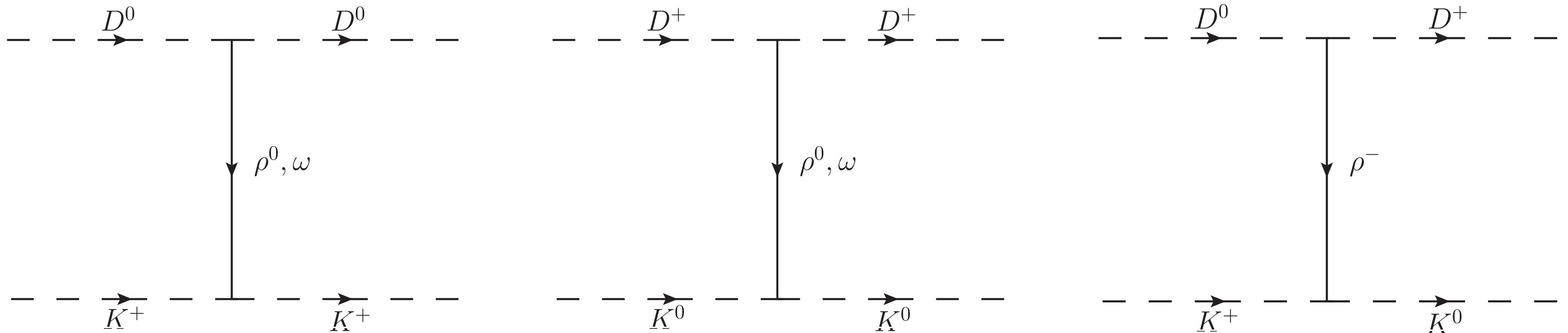
D and D_s meson mass functions



Scattering amplitude for DK I=0

- ♦ Lagrangian from Hidden gauge symmetry formalism

$$\mathcal{L}_{VPP} = ig < [\partial_\mu \Phi, \Phi] V^\mu >$$



$$V = -\frac{s - u}{2f_\pi^2}$$

Coupling with a bare $c\bar{s}$ state

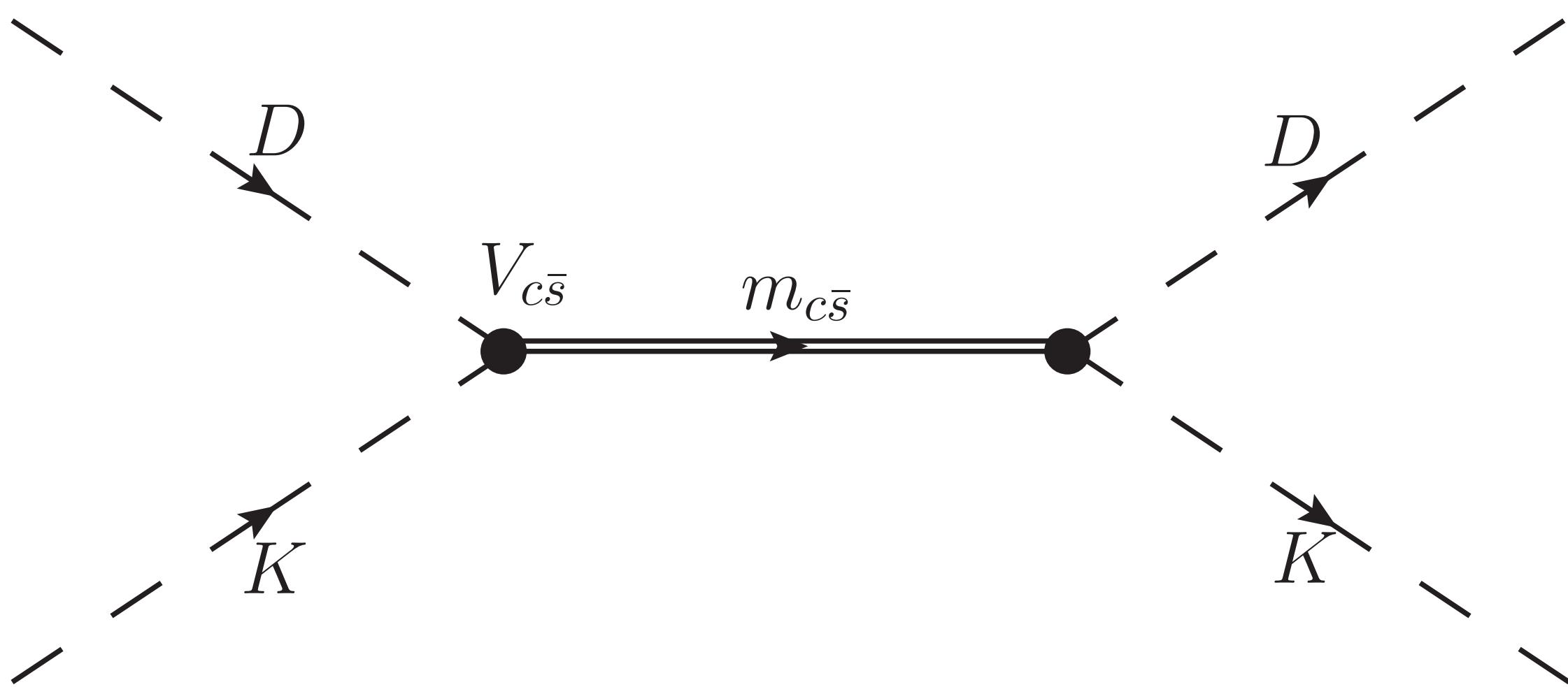
$$V \rightarrow V + V_{ex}$$

$$V_{ex} = \frac{V_{c\bar{s}}^2}{s - m_{c\bar{s}}^2}$$

$$V_{c\bar{s}}(s) = -\frac{c}{f}\sqrt{M_D m_{c\bar{s}}} \frac{s + m_K^2 - M_D^2}{\sqrt{s}},$$

+2 parameters

$c, m_{c\bar{s}}$



Parameters for the energy levels fit

- ◆ Total amplitude from Bethe-Salpeter equation

$$T = \frac{V}{1 - \tilde{G}V}$$

$$\tilde{G}(s, \alpha) = G^{DM}(s, \alpha) + \lim_{q_{\max} \rightarrow \infty} \Delta G(s, q_{\max})$$

$$\Delta G = \frac{1}{L^3} \sum_{q_i}^{q_{\max}} I(\vec{q}_i) - \int_0^{q_{\max}} \frac{d^3 q}{(2\pi)^3} I(\vec{q})$$

The subtraction constant
is defined as

$$\alpha = \alpha_1 + \alpha_2 m_\pi^2$$

+2 parameters
 α_1, α_2

Fit I

2 parameters: α_1, α_2

Fit II

4 parameters: $\alpha_1, \alpha_2, c, m_{c\bar{s}}$

Finite volume energy levels

♦ HSC energy levels

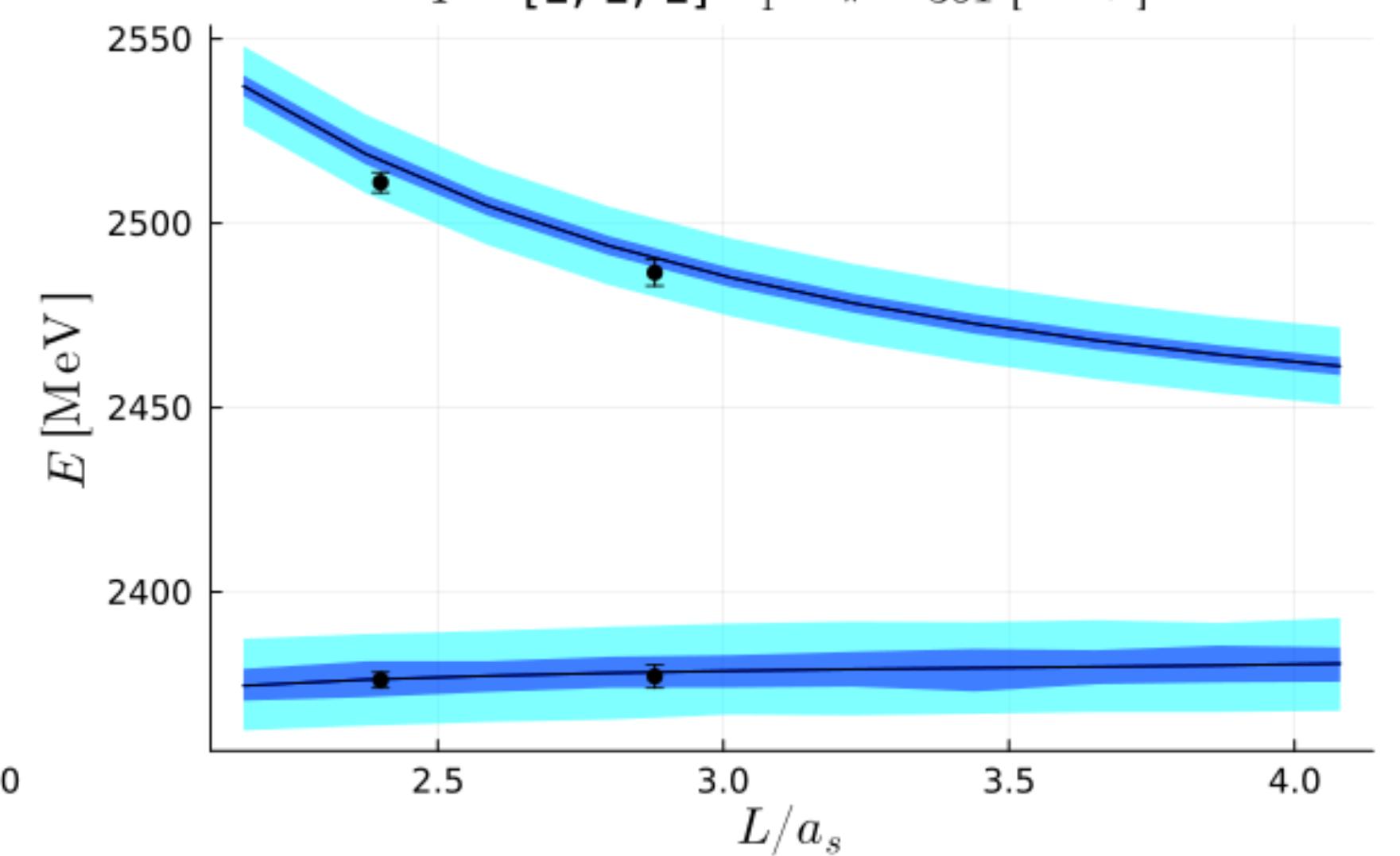
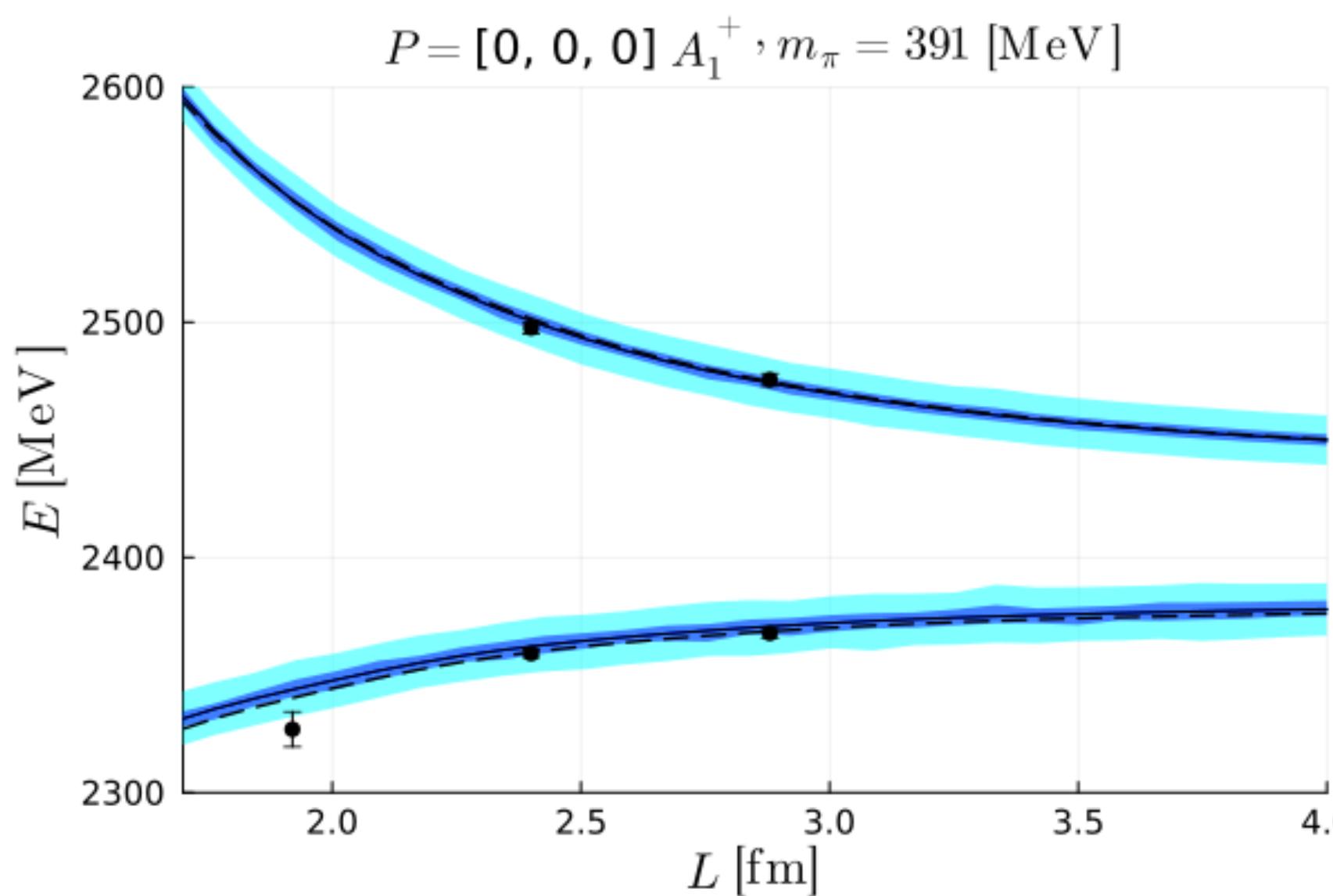
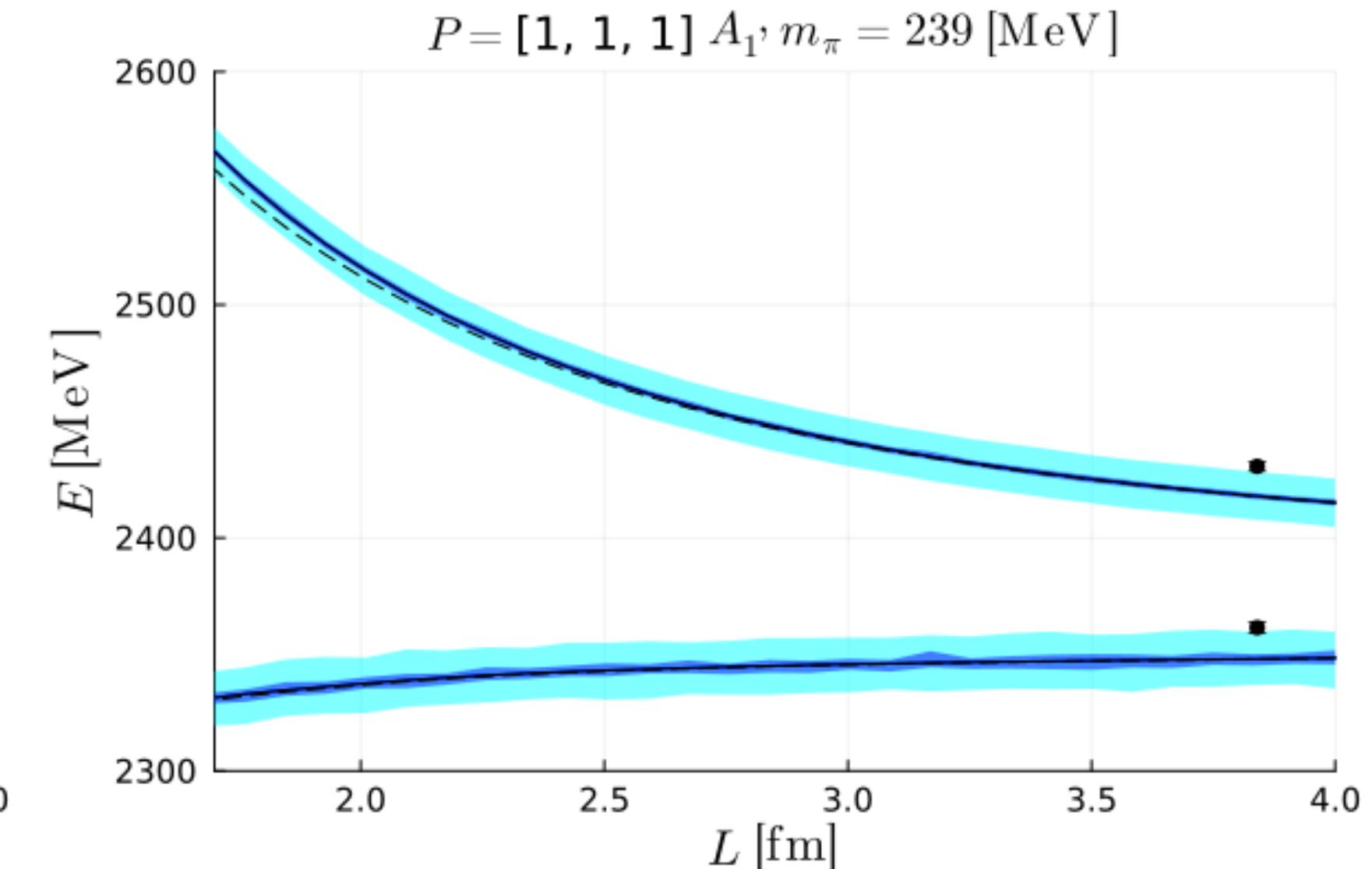
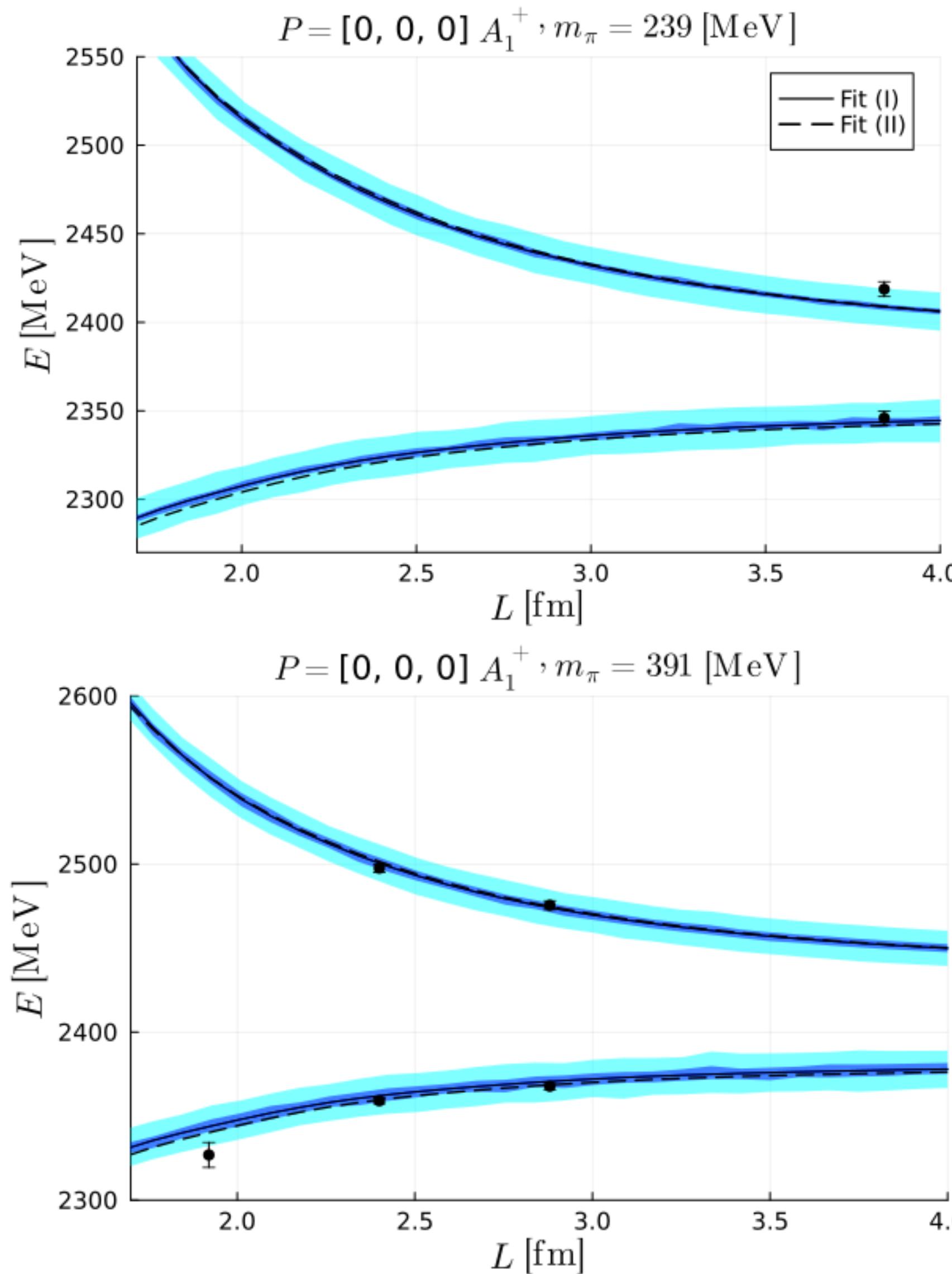
♦ $m_\pi = 239$ MeV

(13 points)

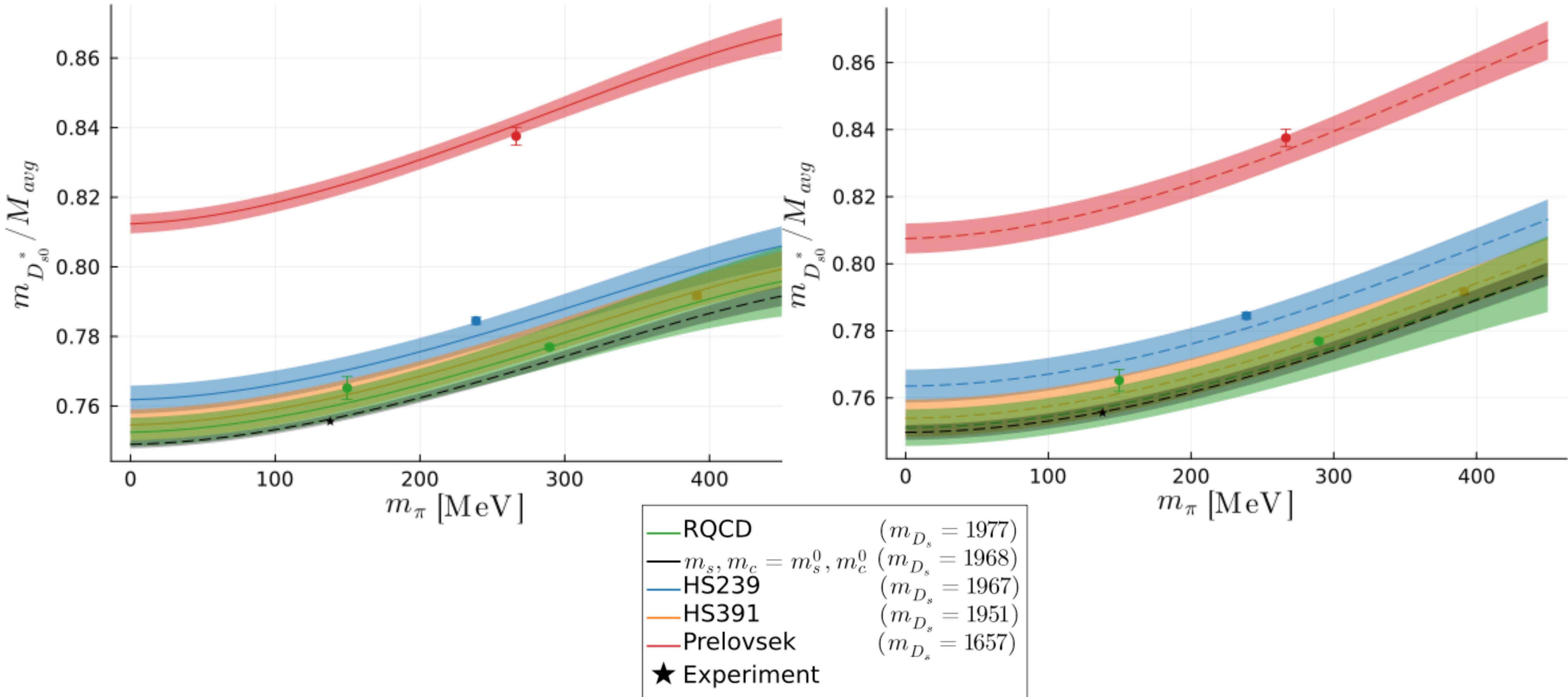
♦ $m_\pi = 391$ MeV

(17 points)

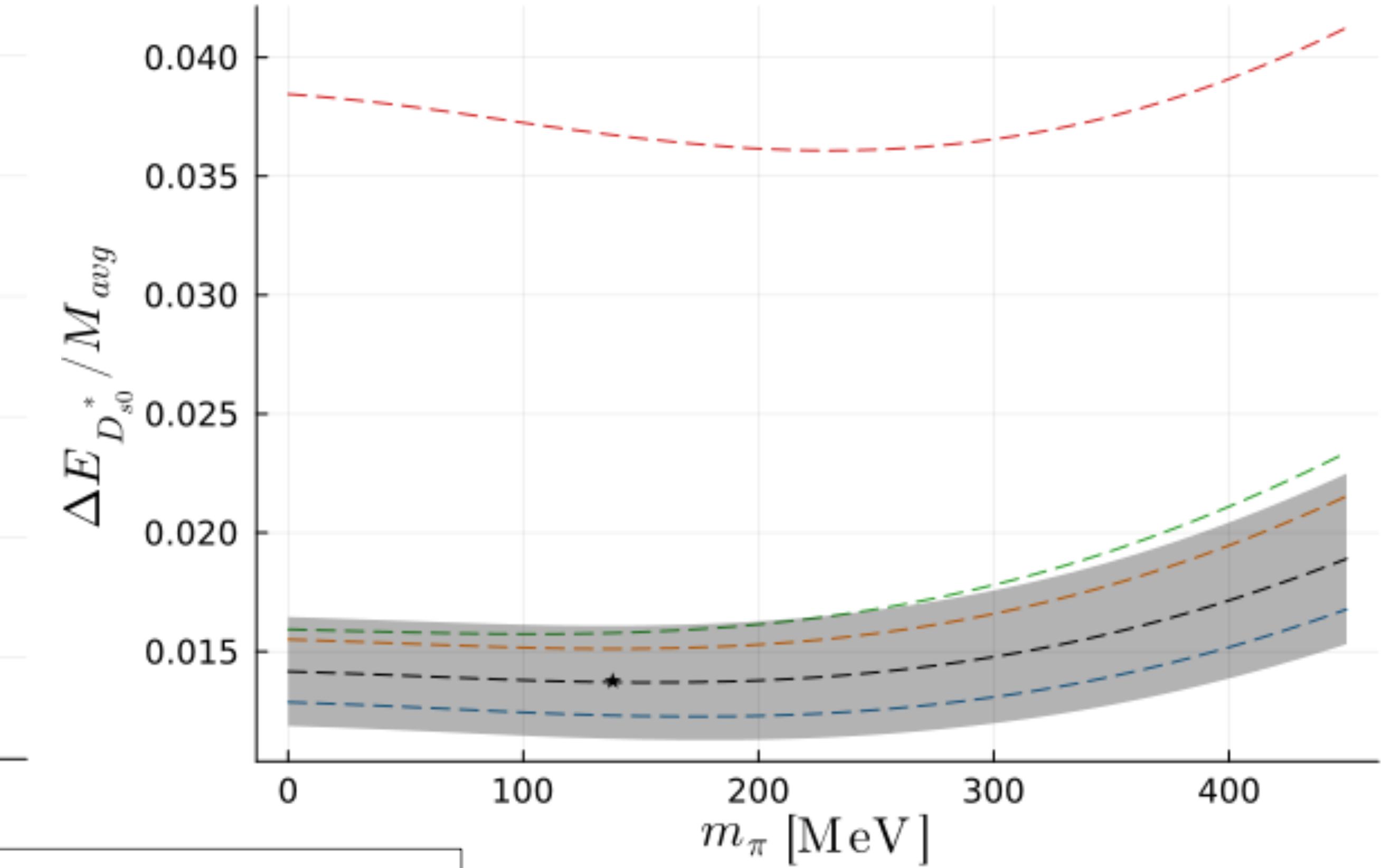
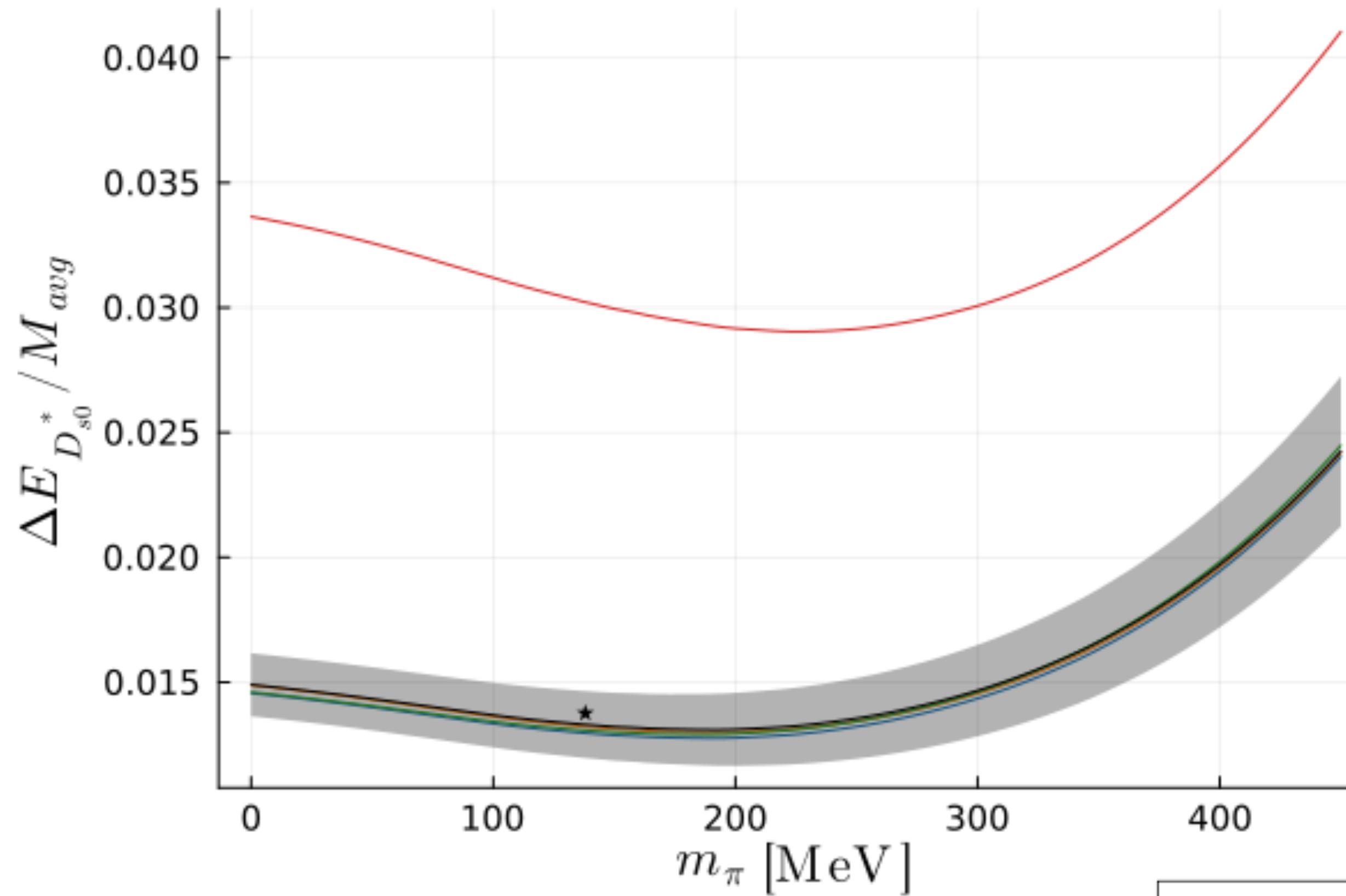
*G. K. C. Cheung, C. E. Thomas, D. J. Wilson, G. Moir, M. Peardon and S. M. Ryan (Hadron Spectrum), JHEP02, 100 (2021), 2008.06432.



$D_{s0}^*(2317)$ pole

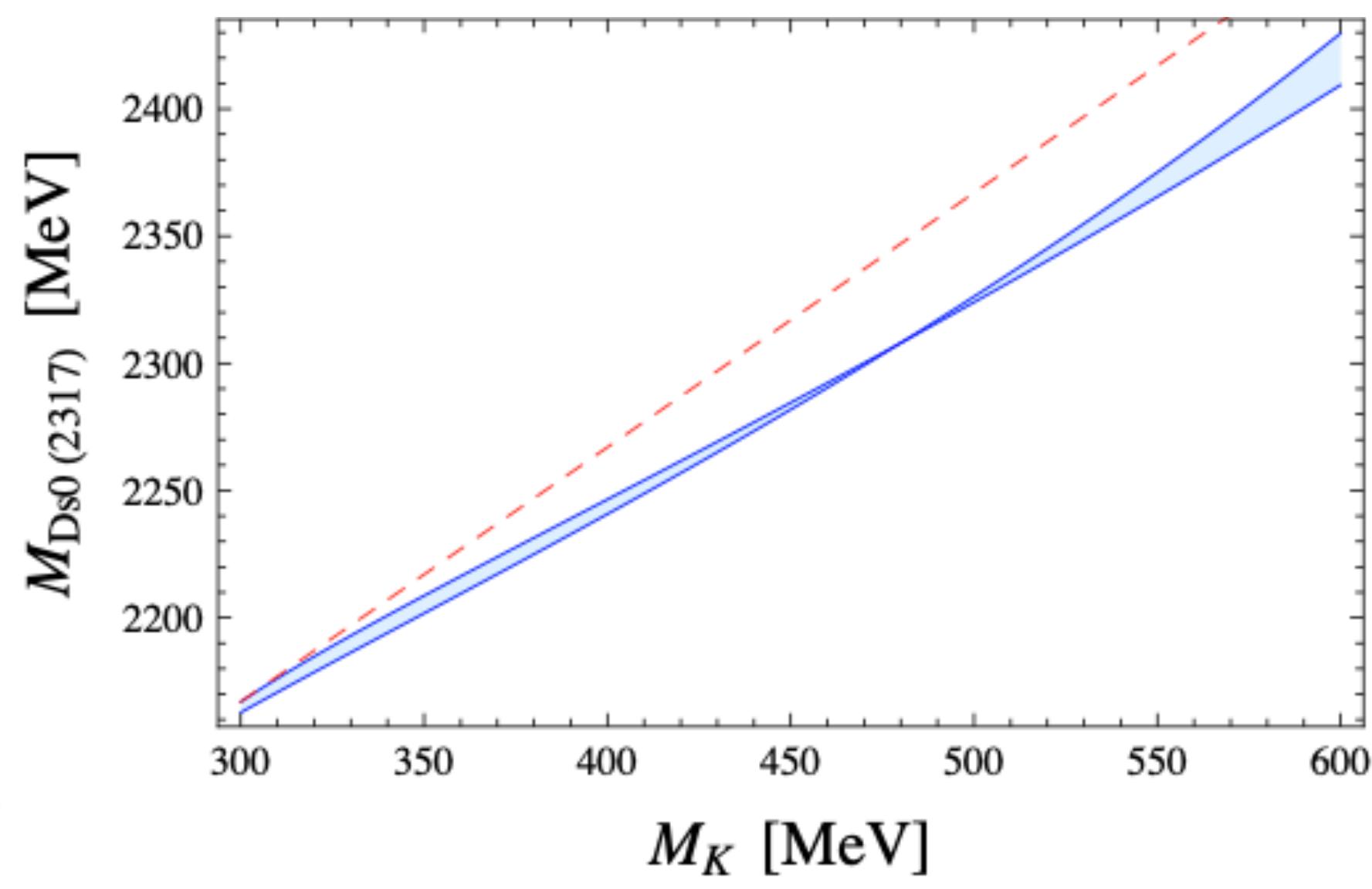
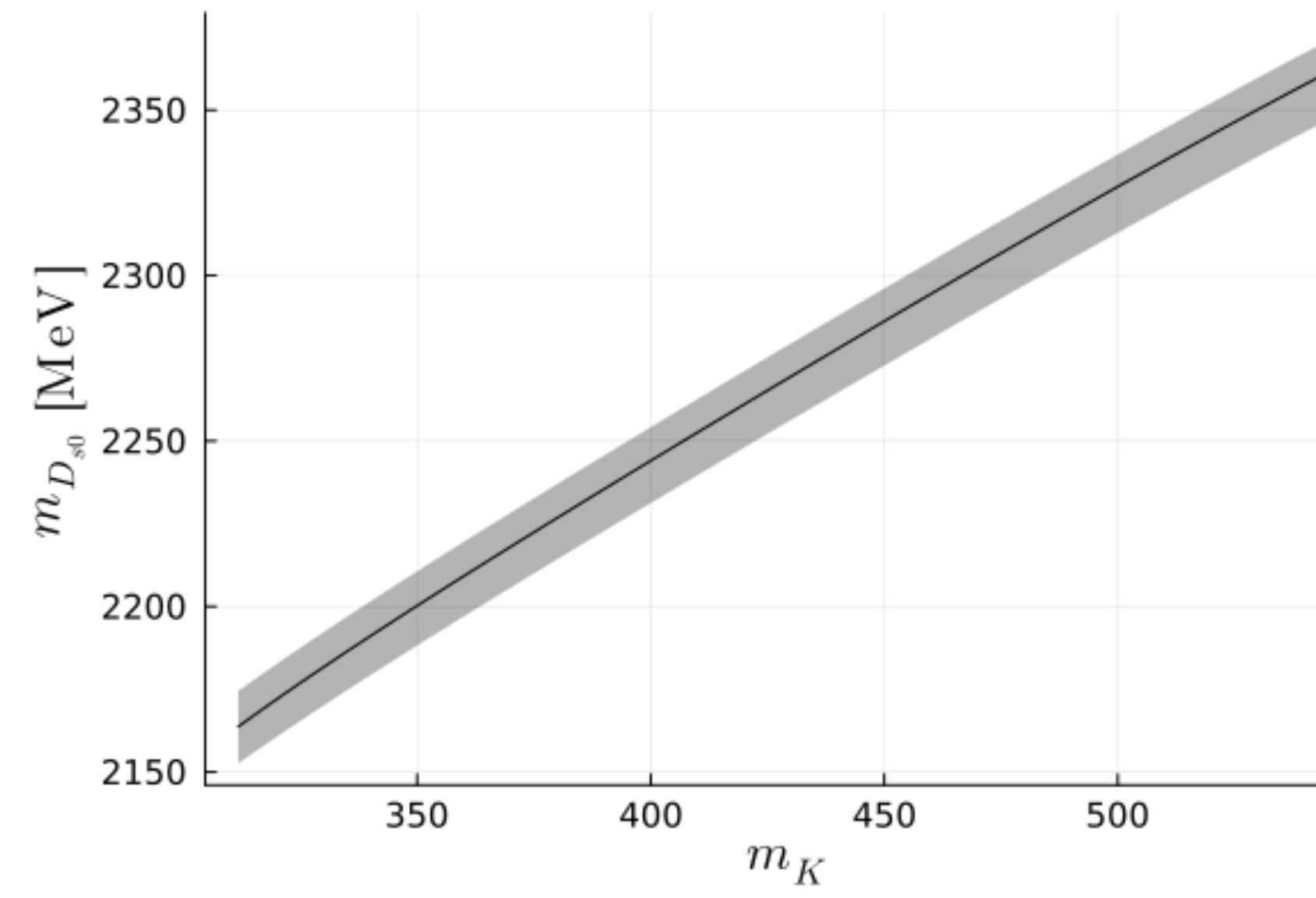
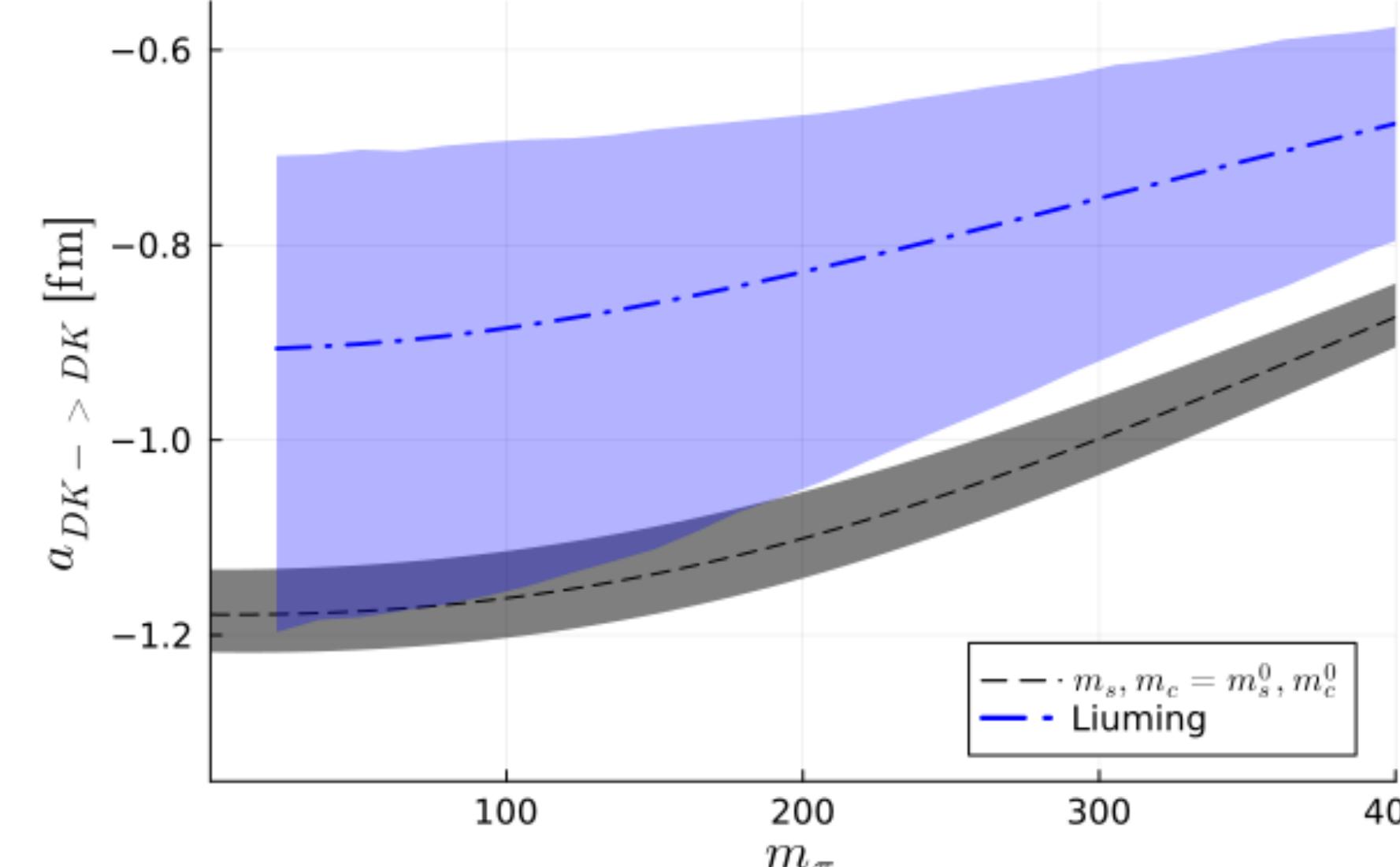
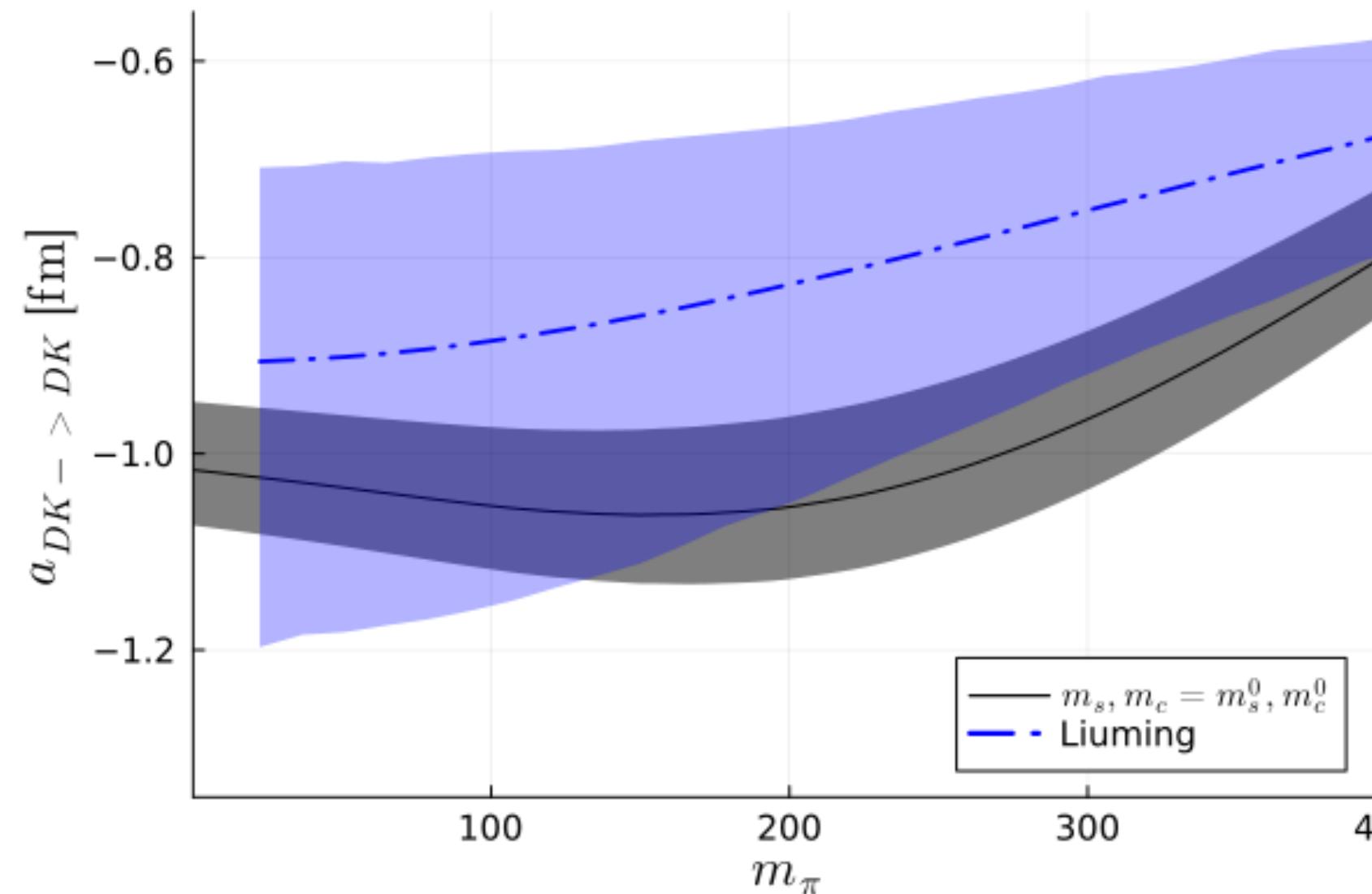


Binding energy



RQCD	$(m_{D_s} = 1977)$
$m_s, m_c = m_s^0, m_c^0$	$(m_{D_s} = 1968)$
HS239	$(m_{D_s} = 1967)$
HS391	$(m_{D_s} = 1951)$
Prelovsek	$(m_{D_s} = 1657)$
★ Experiment	

Comparison with previous results

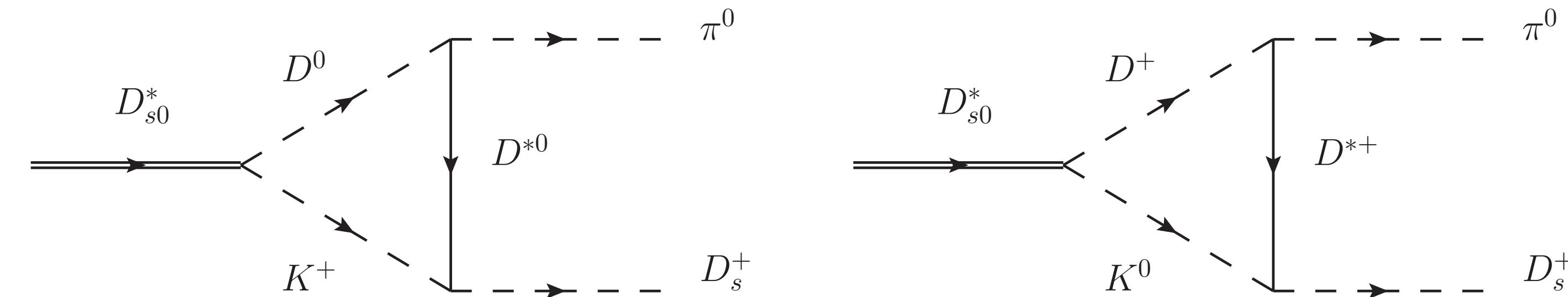
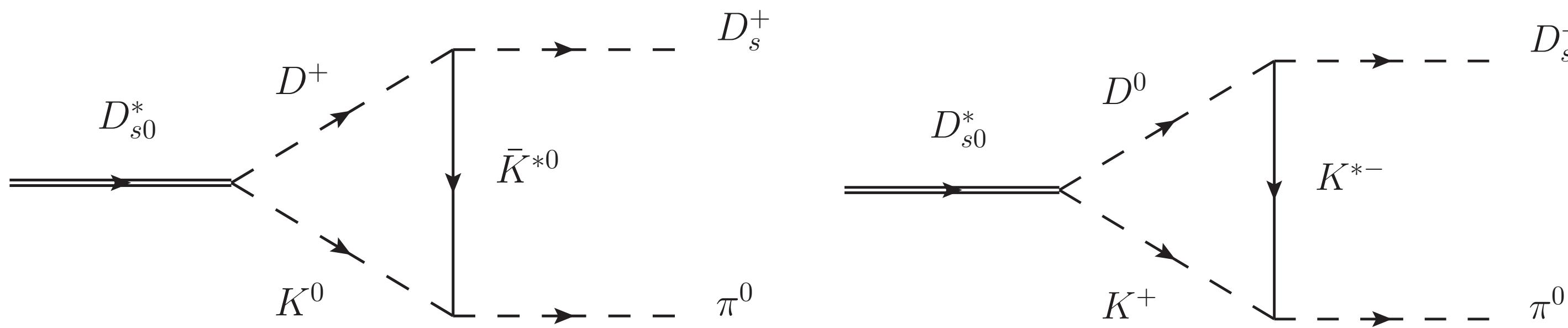


*L. Liu, K. Orginos, F.-K. Guo, C. Hanhart, and U.-G. Meissner,
Phys. Rev. D 87, 014508
(2013), 1208.4535.

*M. Cleven, F.-K. Guo, C. Hanhart, and U.-G. Meissner,
Eur. Phys. J. A 47, 19 (2011),
1009.3804.

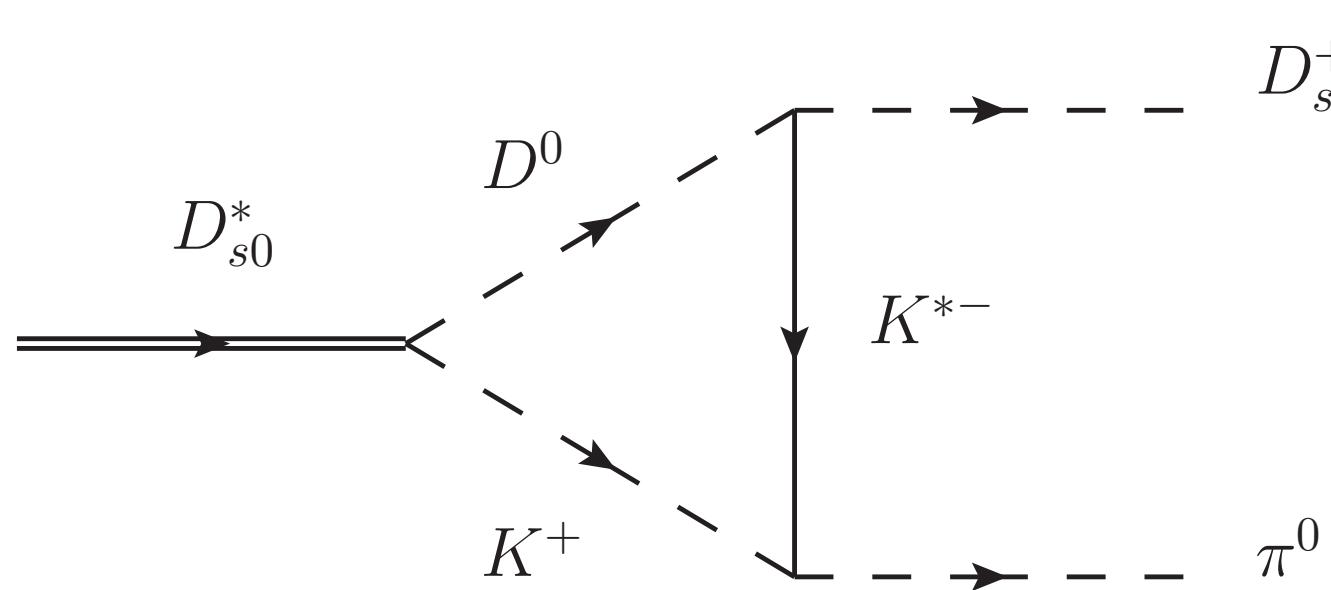
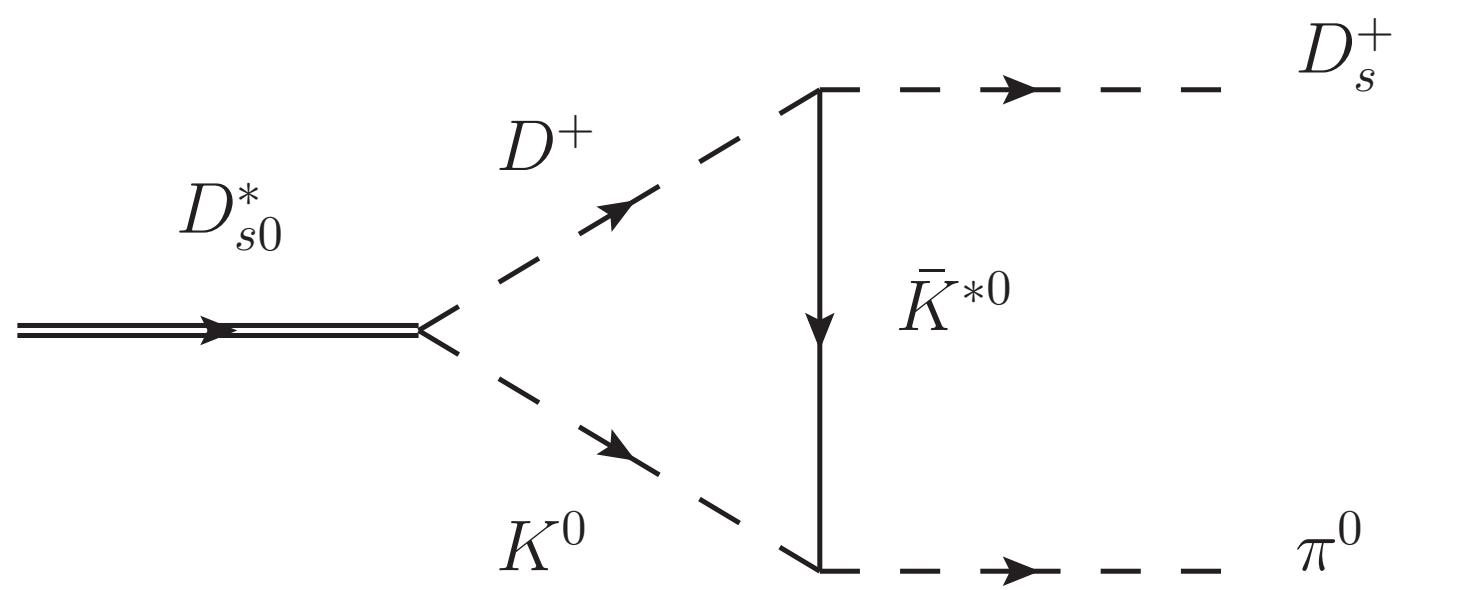
Decay width of the $D_{s0}^*(2317) \rightarrow D_s^+ \pi^0$

$$t = \int \frac{d^4 q}{(2\pi)^4} \frac{g_X g^2 c_1(p - p_f + q)(p + p_f - q)}{\left[(p - q)^2 - m_2 + i\epsilon\right] \left[(q - p + p_f)^2 - M + i\epsilon\right] (q^2 - m_1 + i\epsilon)}$$

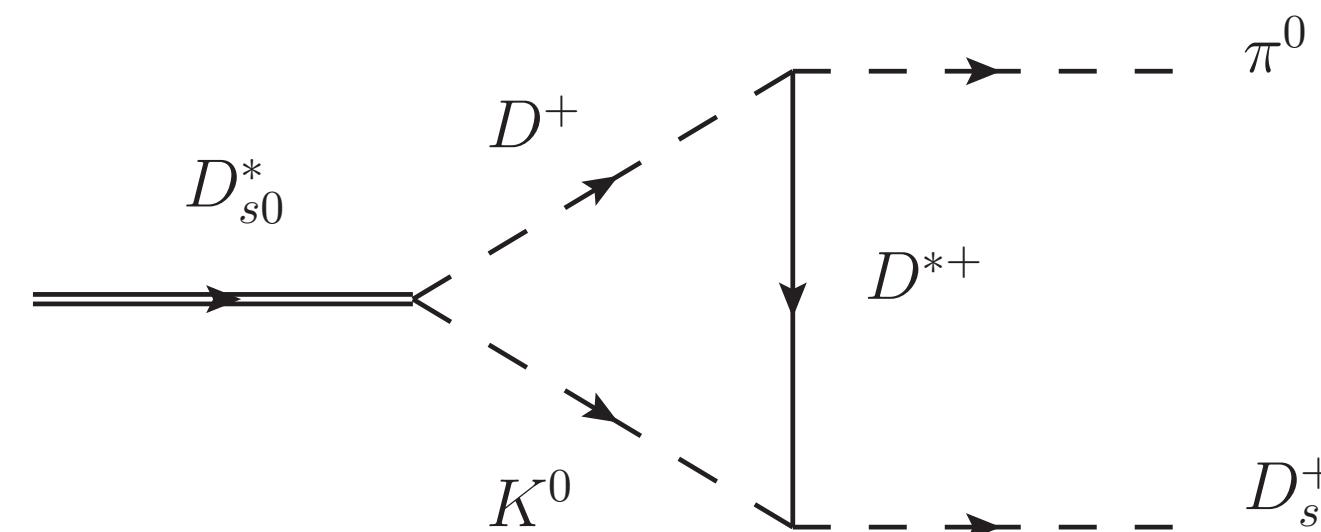
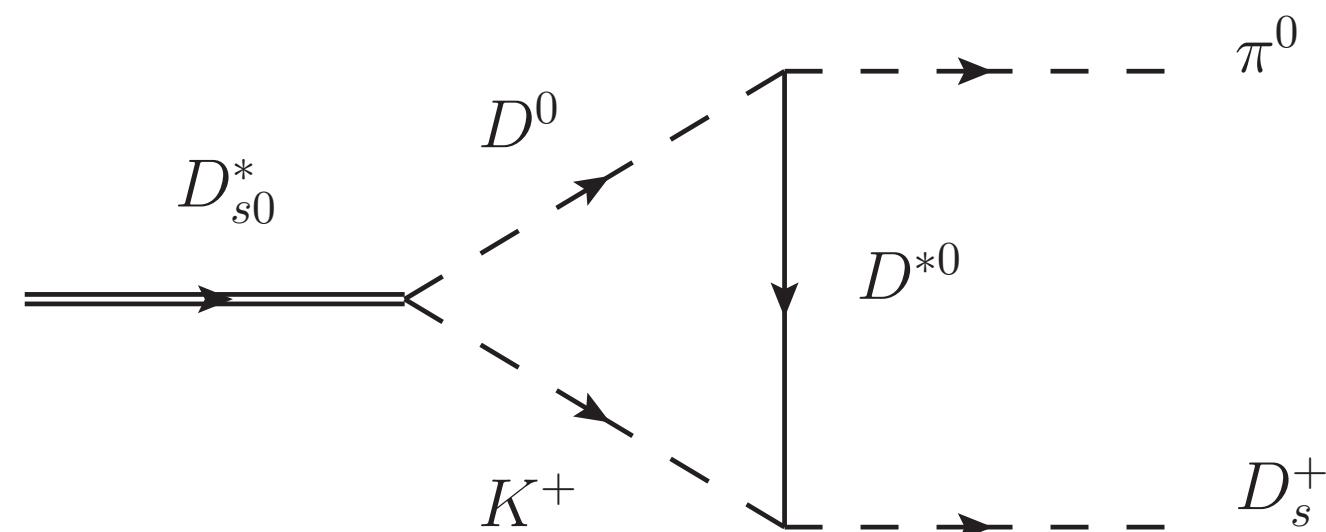


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$$\Gamma_X = |\vec{p}_f| \frac{|t|^2}{8\pi m_X^2}$$



$$\Gamma_{D_{s0}^*} = 128 \pm 40 \text{ KeV}$$

Conclusions

- ◆ The results of the HSC data analysis agree reasonably well with experiment, and with other previous LQCD studies on DK, suggesting the possibility of a global fit.
- ◆ Our results suggest that the attractive DK interaction reduces with the charm quark mass, and becomes large for high pion masses. We obtain that this state is predominantly molecular.
- ◆ Future LQCD data analyses for different pion masses than the ones included in our fit, could be a good test for this study.