

Searching for new fundamental physics in astrophysical objects

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UNDARK School



THE ROYAL SOCIETY

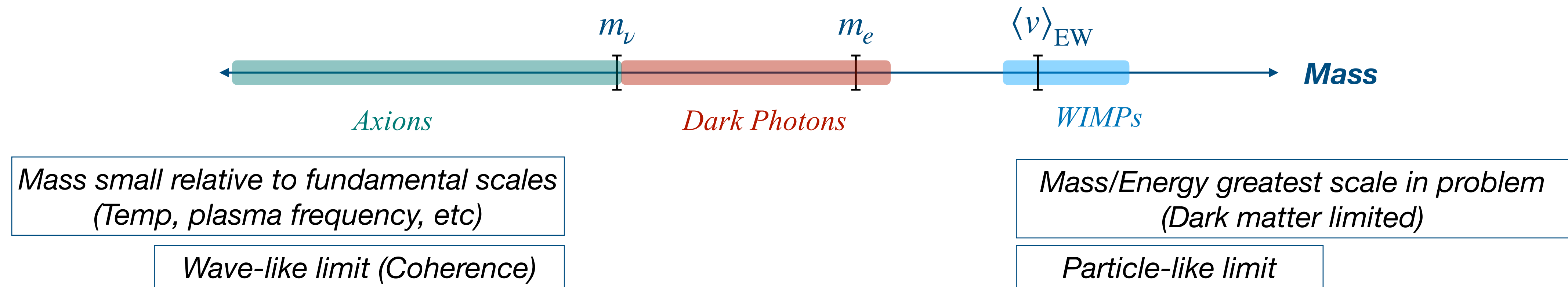


UNIVERSITY OF
OXFORD



Overview of lecture 1

- What sort of fundamental physics will we discuss? How do we traditionally attempt to search for these particles (needed to contextualize complementarity of astro searches)?



- What do compact astrophysical objects offer in the search for these particles? Which objects are we interested in?
- The Sun as a first example
- Lectures 2-4: will focus on selected topics related to neutron stars, black holes, etc*

General properties of axions

***Motivation:** Strong CP problem, simple dark matter production mechanism, string axiverse, etc*

$$\mathcal{L} \supset \quad (\text{Dim-5}) \quad \frac{a}{f_a} G_{\mu\nu} \tilde{G}^{\mu\nu}, \quad \frac{a}{f_a} \underbrace{F_{\mu\nu} \tilde{F}^{\mu\nu}}_{\vec{E} \cdot \vec{B}}, \quad \frac{1}{f_a} \partial_\mu a \bar{\psi} \gamma^\mu \gamma^5 \psi, \quad \frac{m_\psi}{f_a^2} a^2 \bar{\psi} \psi + \dots$$

(*QCD axion only*)
 $\propto m_\psi a \bar{\psi} \gamma^5 \psi$
Mass Shifts

(spin density coupling)

General properties of axions

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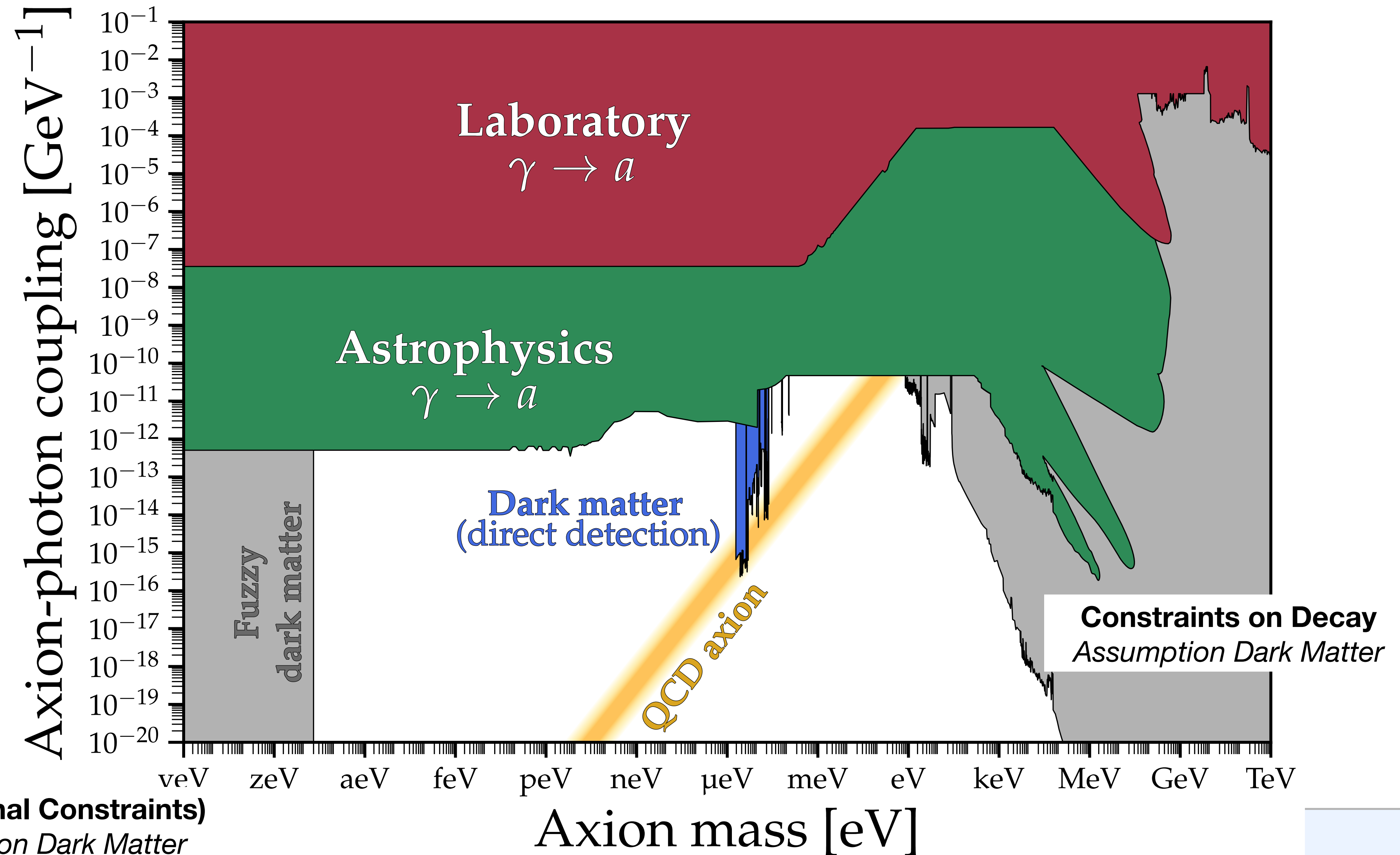
$$\begin{aligned}
 \mathcal{L} \supset \quad & \text{(Dim-5)} \quad \frac{a}{f_a} G_{\mu\nu} \tilde{G}^{\mu\nu}, \quad \frac{a}{f_a} \underbrace{F_{\mu\nu} \tilde{F}^{\mu\nu}}_{\vec{E} \cdot \vec{B}}, \quad \frac{1}{f_a} \partial_\mu a \bar{\psi} \gamma^\mu \gamma^5 \psi, \quad \frac{m_\psi}{f_a^2} a^2 \bar{\psi} \psi + \dots \\
 & \text{(*QCD axion only*)} \qquad \qquad \qquad \propto m_\psi a \bar{\psi} \gamma^5 \psi \qquad \text{(spin density coupling)} \qquad \text{Mass Shifts} \\
 \text{(Dim-6)} \quad & \frac{a^2}{f_a^2} F_{\mu\nu} F^{\mu\nu}, \quad \frac{a}{f_a m_\psi} F_{\mu\nu} i \bar{\psi} \sigma^{\mu\nu} \gamma^5 \psi + \dots \quad \text{(*CP violating*)} \quad m_\psi \frac{a}{f_a} \bar{\psi} \psi \\
 & \text{Effective axion mass /} \qquad \qquad \qquad \text{Neutron EDM} \qquad \qquad \qquad \text{5th forces} \\
 & \text{shift in fine structure}
 \end{aligned}$$

Aspects of axion detection

To the blackboard

Intro to axion electrodynamics

Status of axion searches

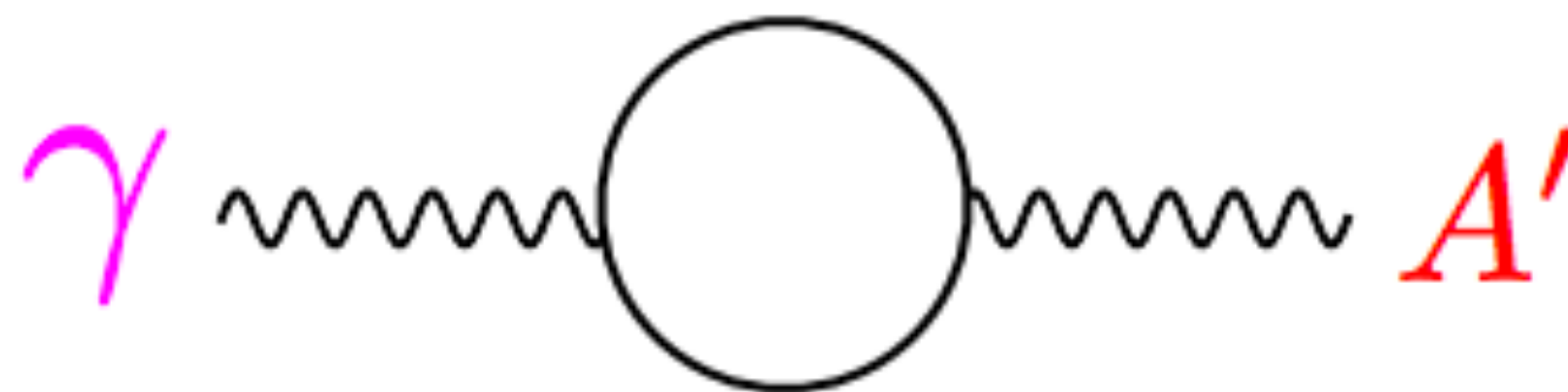


General properties of dark photons

Motivation: General & minimal extension of SM

New $U(1)$ with gauge field A'_μ and mass $m_{\gamma'}$ (either Higgsed or Stuckelberg)

$$\mathcal{L} = \underbrace{-\frac{1}{4}F_{\mu\nu}F^{\mu\nu} + J^\mu A_\mu}_{\text{E\&M}} - \underbrace{\frac{1}{4}F'_{\mu\nu}F'^{\mu\nu} + \frac{m_{\gamma'}^2}{2}A'_\mu A'^\mu}_{\text{Dark (Massive) E\&M}} - \underbrace{\frac{\chi}{2}F_{\mu\nu}F'^{\mu\nu}}_{\text{Mixing term}}$$



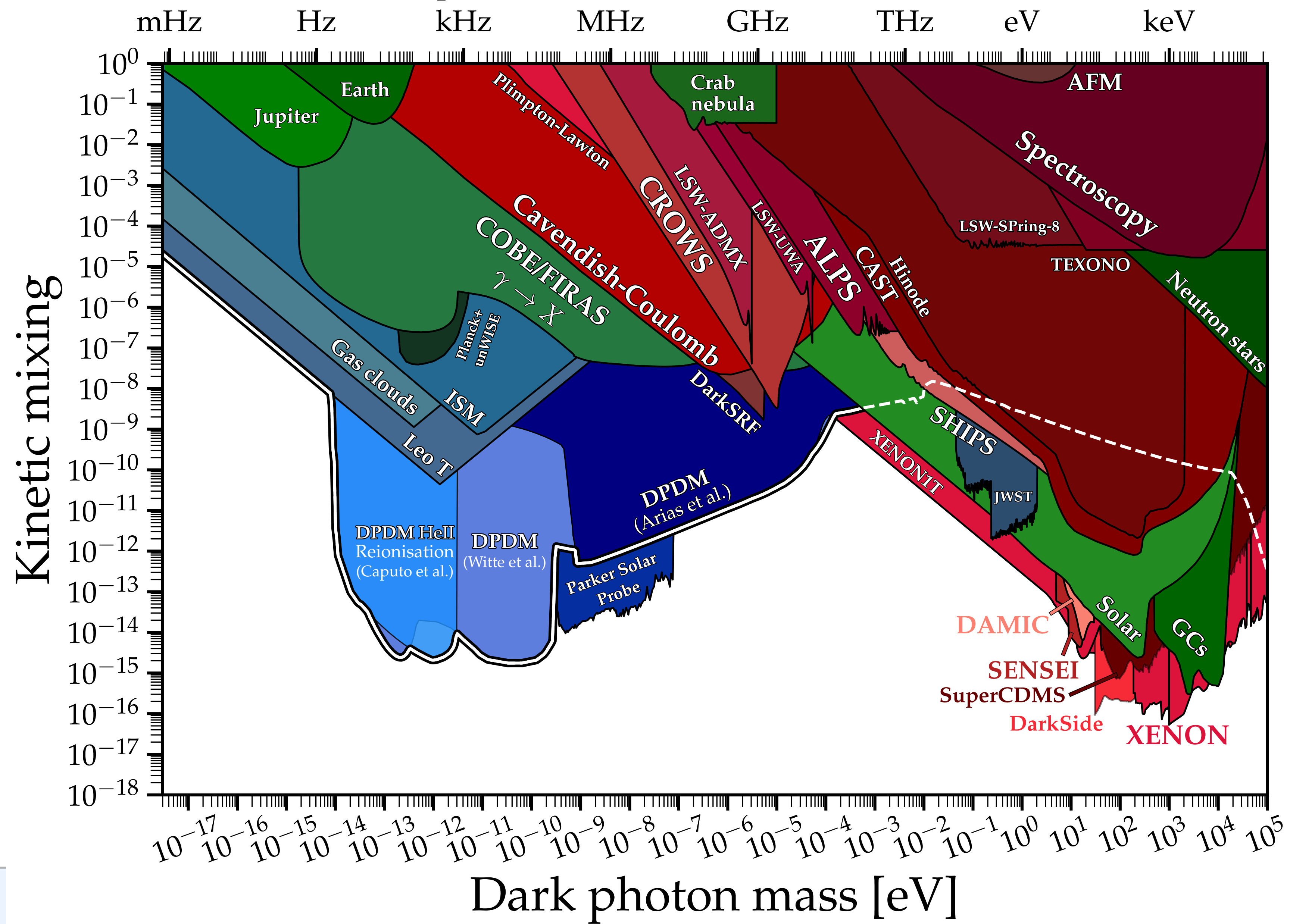
$$\chi \sim \frac{eg_D}{16\pi^2} \sim \mathcal{O}(10^{-3})g_D$$

Aspects of dark photon detection

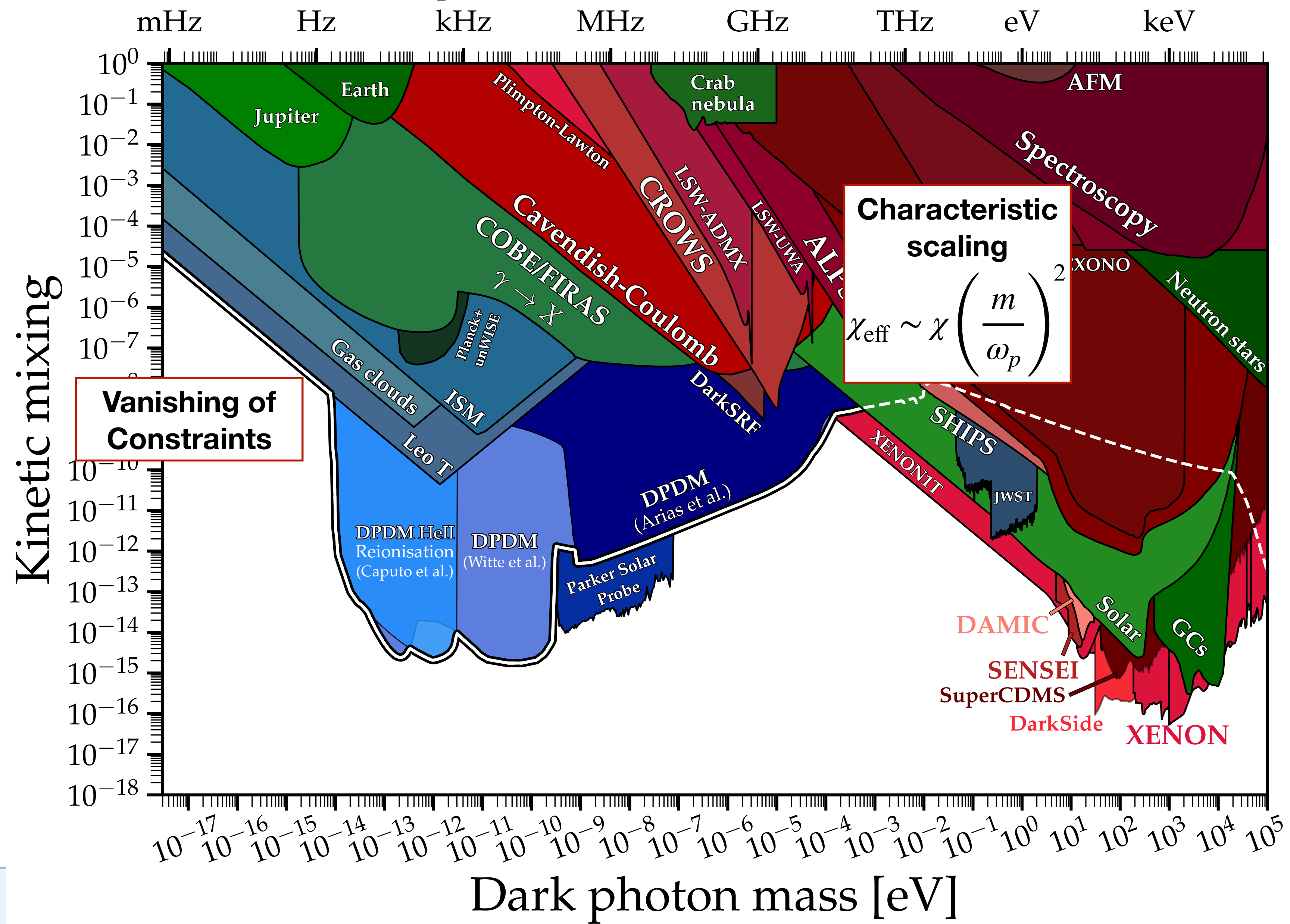
To the blackboard

Quick intro to dark photon electrodynamics

Status of dark photon searches



Status of dark photon searches



WIMPs

***Motivation:** New physics @ EW scale (hierarchy problem),
simple thermal dark matter*

Traditional definition:

- Interactions mediated by Z/H
- Produced via thermal freeze-out

$$m_\chi \lesssim \mathcal{O}(100 \text{ TeV}) \quad (\text{Unitarity } \langle \sigma v \rangle \sim g^2/m_{\text{DM}}^2)$$

$$m_\chi \gtrsim \mathcal{O}(\text{GeV}) \quad (\text{Lee-Weinberg bound } \sigma \sim m^2/M^4)$$

(ways to evade...)

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Modern (2000s) definition often slightly looser:

- Interactions mediated by new particle

$$m_\chi \gtrsim \mathcal{O}(\text{MeV}) \quad (\text{BBN})$$

Free parameters: dark matter mass m_χ , mediator mass m_Z , dark matter coupling g_χ , SM coupling g_{SM}

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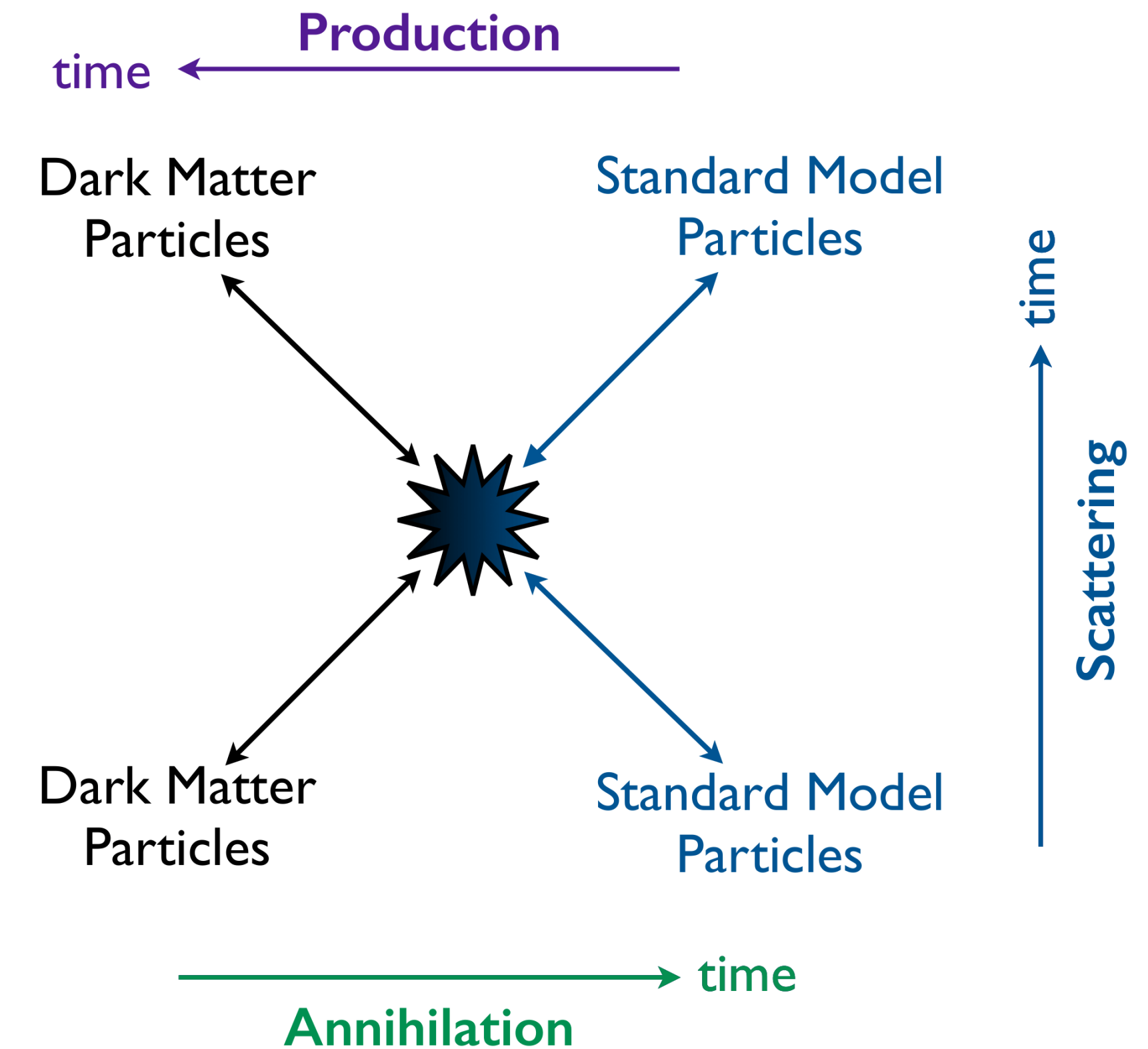
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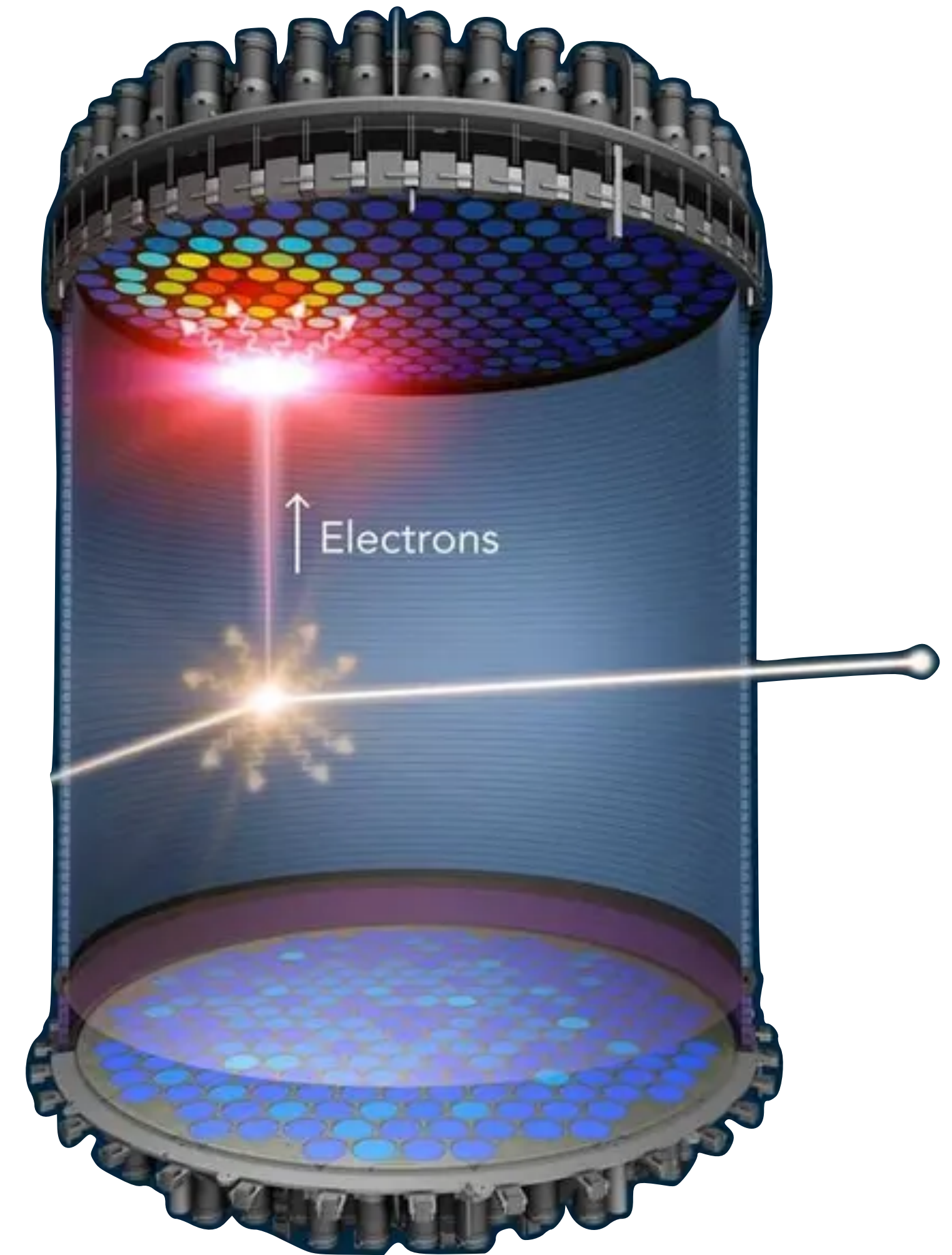
Thermal production mechanism fixes $g_\chi \times g_{\text{SM}}$ for any set of masses



WIMP direct detection

- Direct detection probes product of coupling $(g_\chi g_q)^2$
*Can couple to nucleon **number** $\sigma \propto A^2$ or **spin** $\sigma \propto \langle S_N \rangle^2$*

$$\sigma_N \propto \left(\frac{q}{\mu_r} \right)^{2n} v_\perp^{2m} \quad n, m \in \text{Integers}$$



WIMP direct detection

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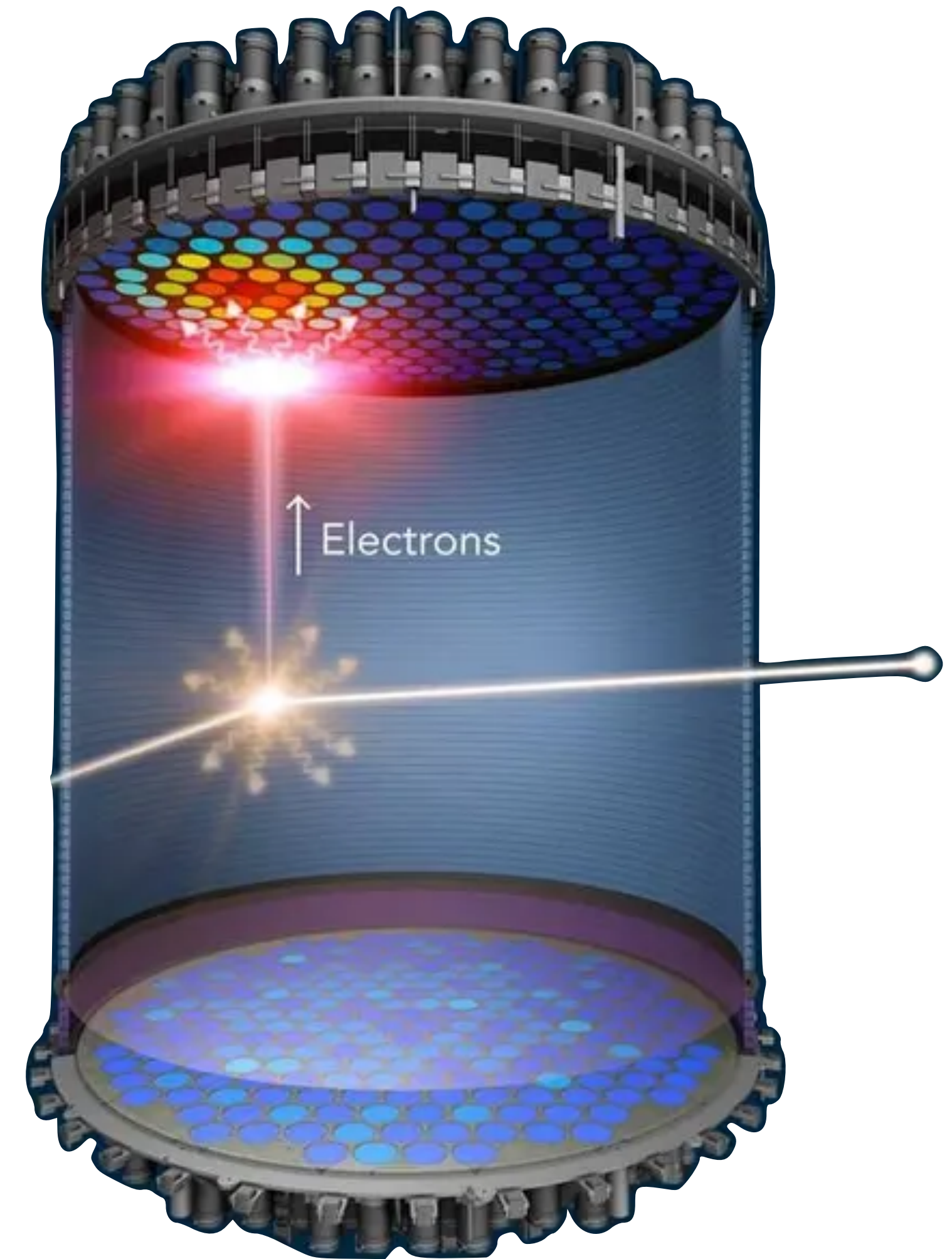
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$$\sigma_N \propto \left(\frac{q}{\mu_r} \right)^{2n} v_\perp^{2m} \quad n, m \in \text{Integers}$$

$$L_{\text{eff}} \sim \bar{\chi} \chi \bar{q} q \quad L_{\text{eff}} \sim \bar{\chi} \gamma^\mu \gamma^5 \chi \bar{q} \gamma_\mu \gamma^5 q$$

$$\sigma_{N,SI} \propto A^2 \quad \sigma_{N,SI} \propto A^2 q^2 v_\perp^2$$

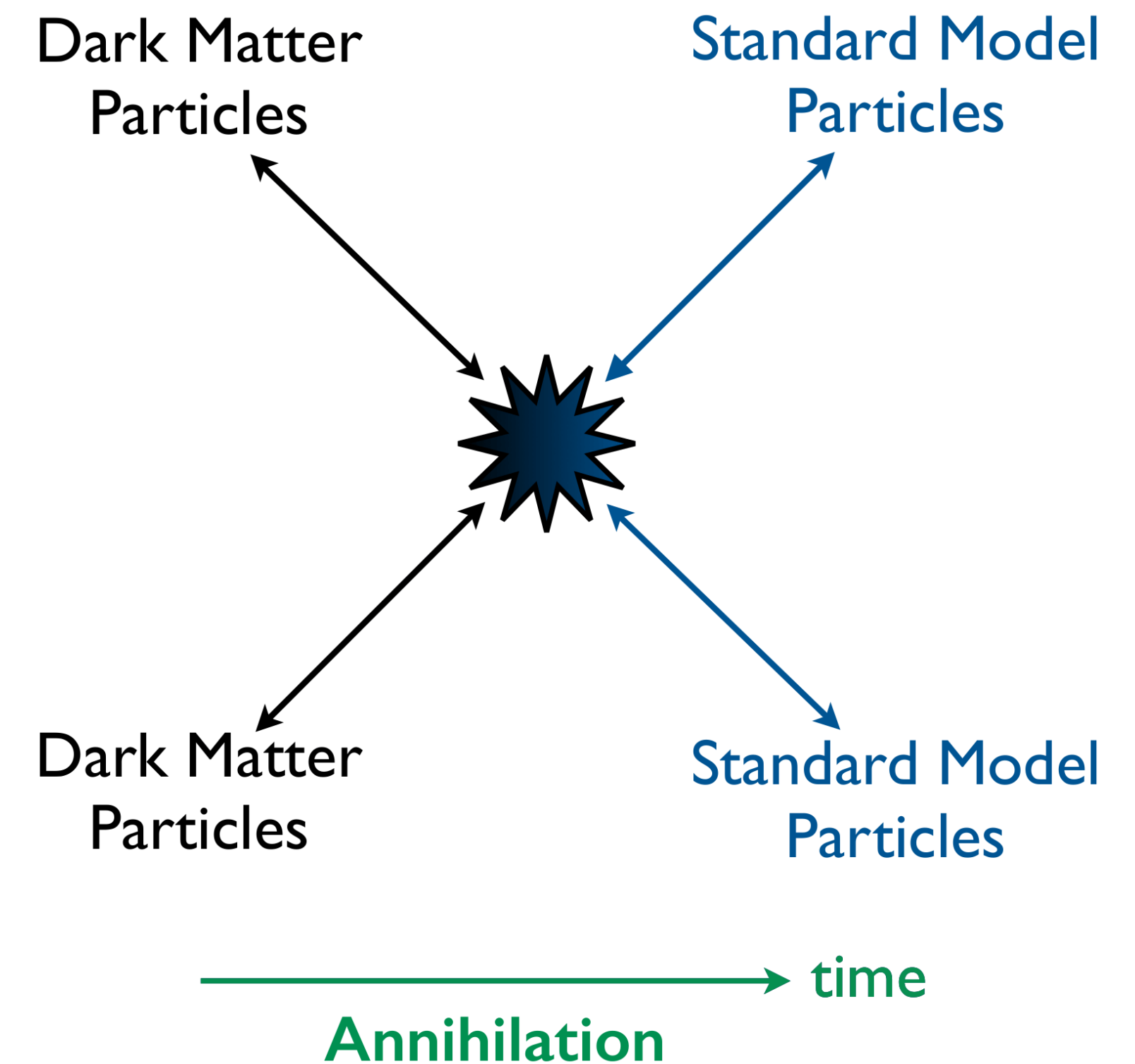
12 orders of magnitude difference in scattering cross section



WIMP indirect detection

- Annihilation cross section $\langle\sigma v\rangle_{fo} \sim 2 \times 10^{-26} \text{cm}^3/\text{s}$

Constraints on $\langle\sigma v\rangle_{\text{today}} \lesssim 2 \times 10^{-26} \text{cm}^3/\text{s} @ m_\chi \lesssim \mathcal{O}(100 \text{ GeV})$



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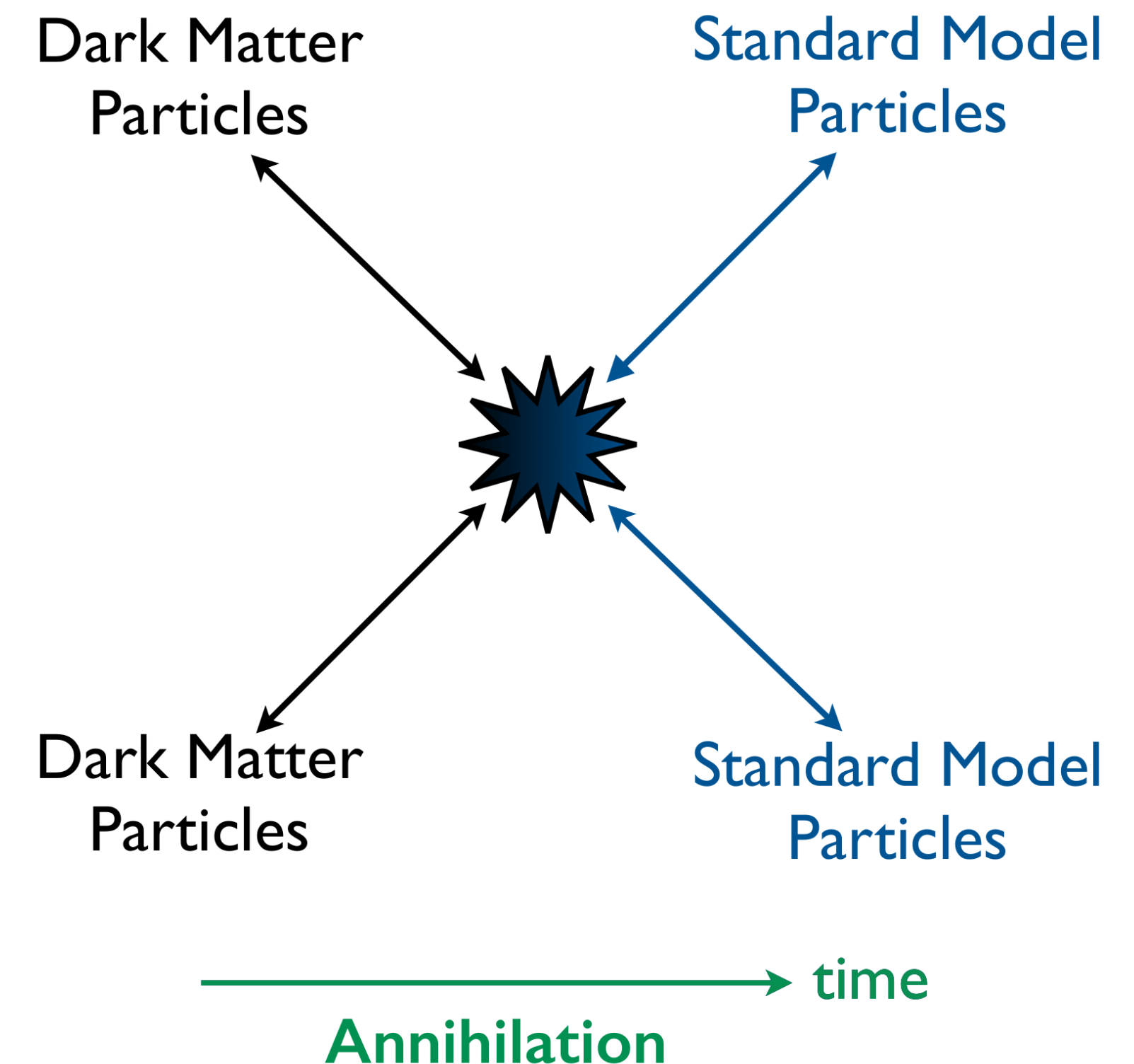
$$\langle\sigma v\rangle_{fo} \neq \langle\sigma v\rangle_{\text{today}}$$

$$\langle\sigma v\rangle \sim \sum_L \sigma_i v^{2L}$$

Partial wave expansion with initial orbital ang. mom L

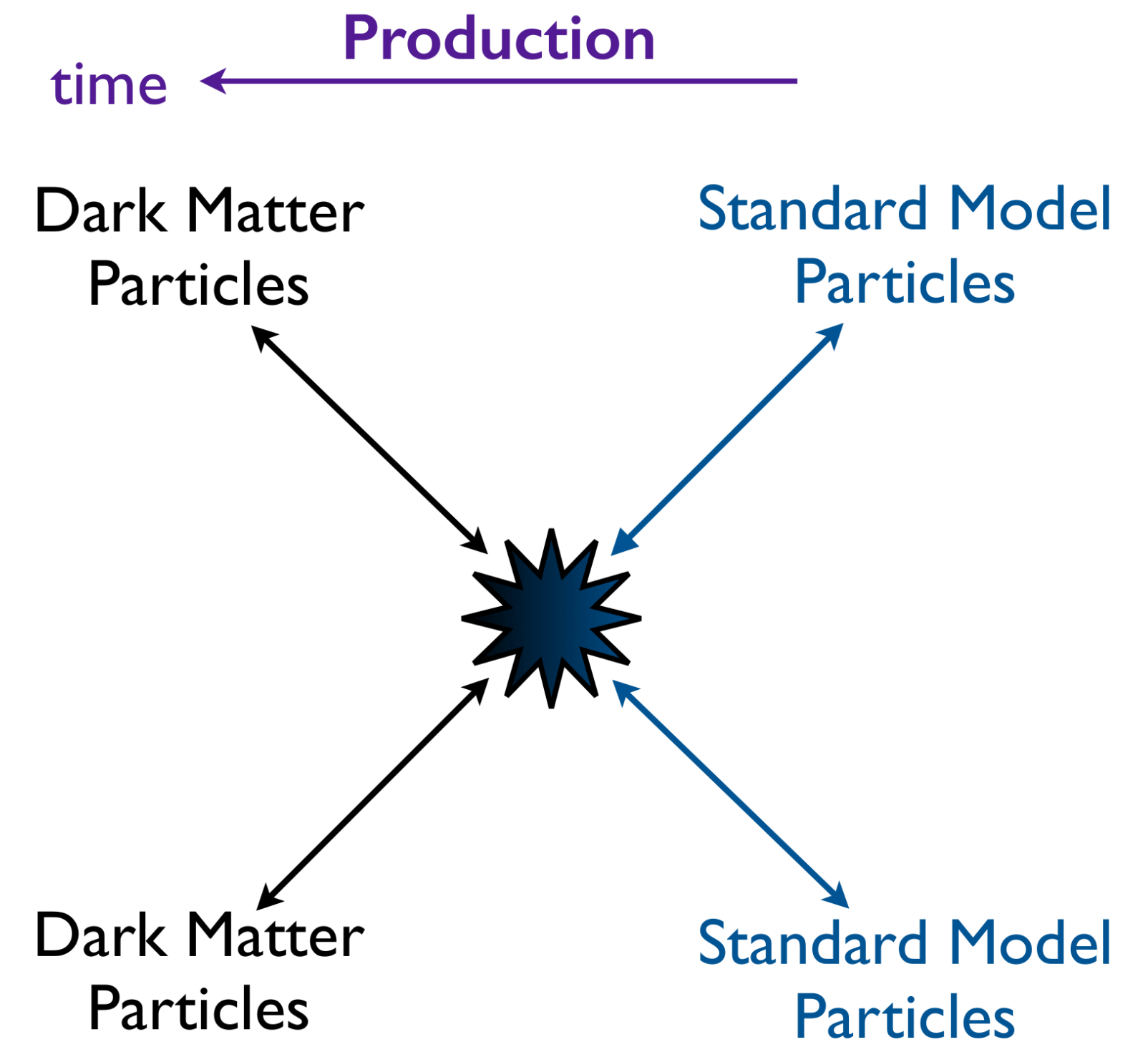
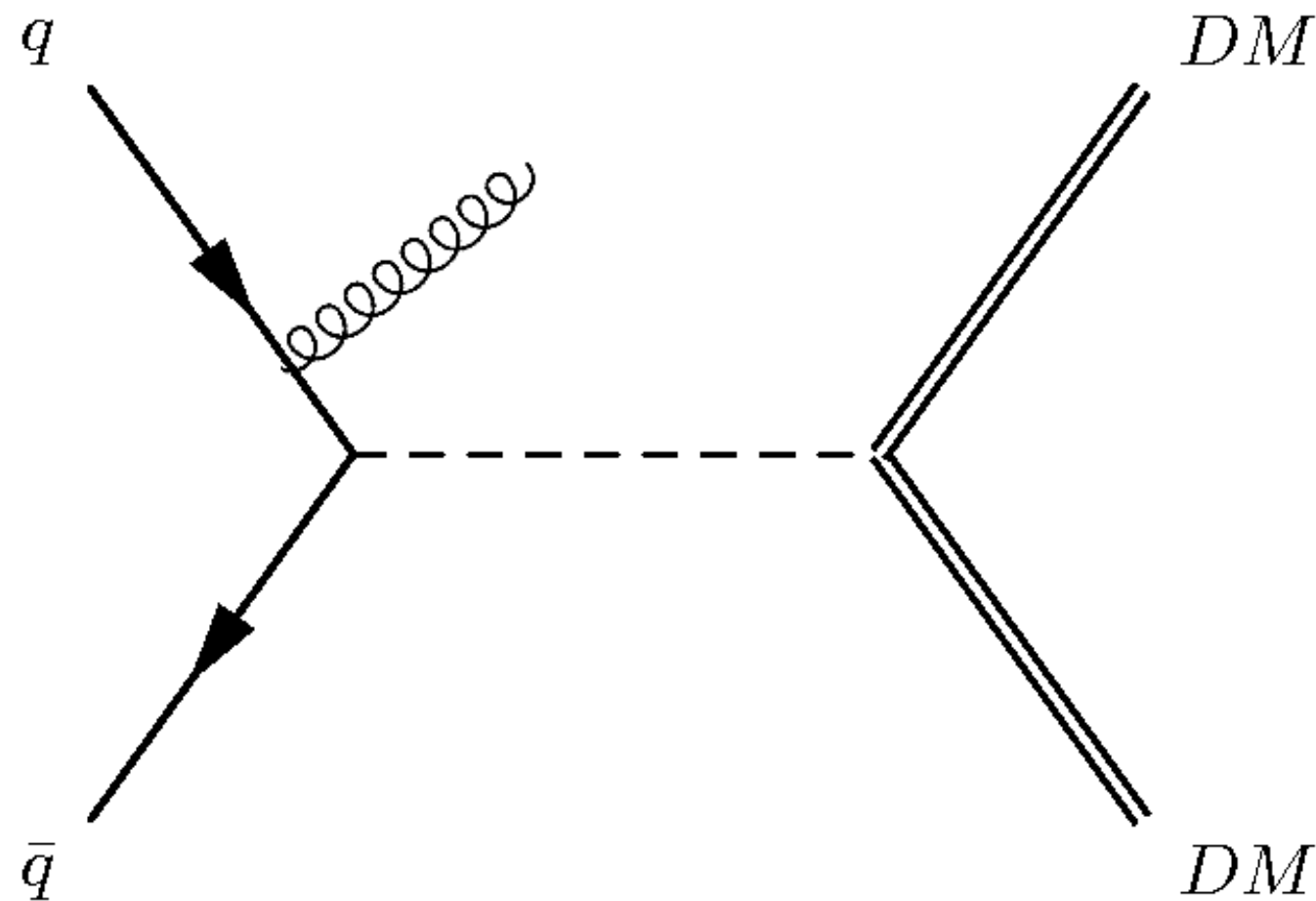
Vanishing s-wave contribution has large implications

(Can also play with asymmetry in the dark sector...)



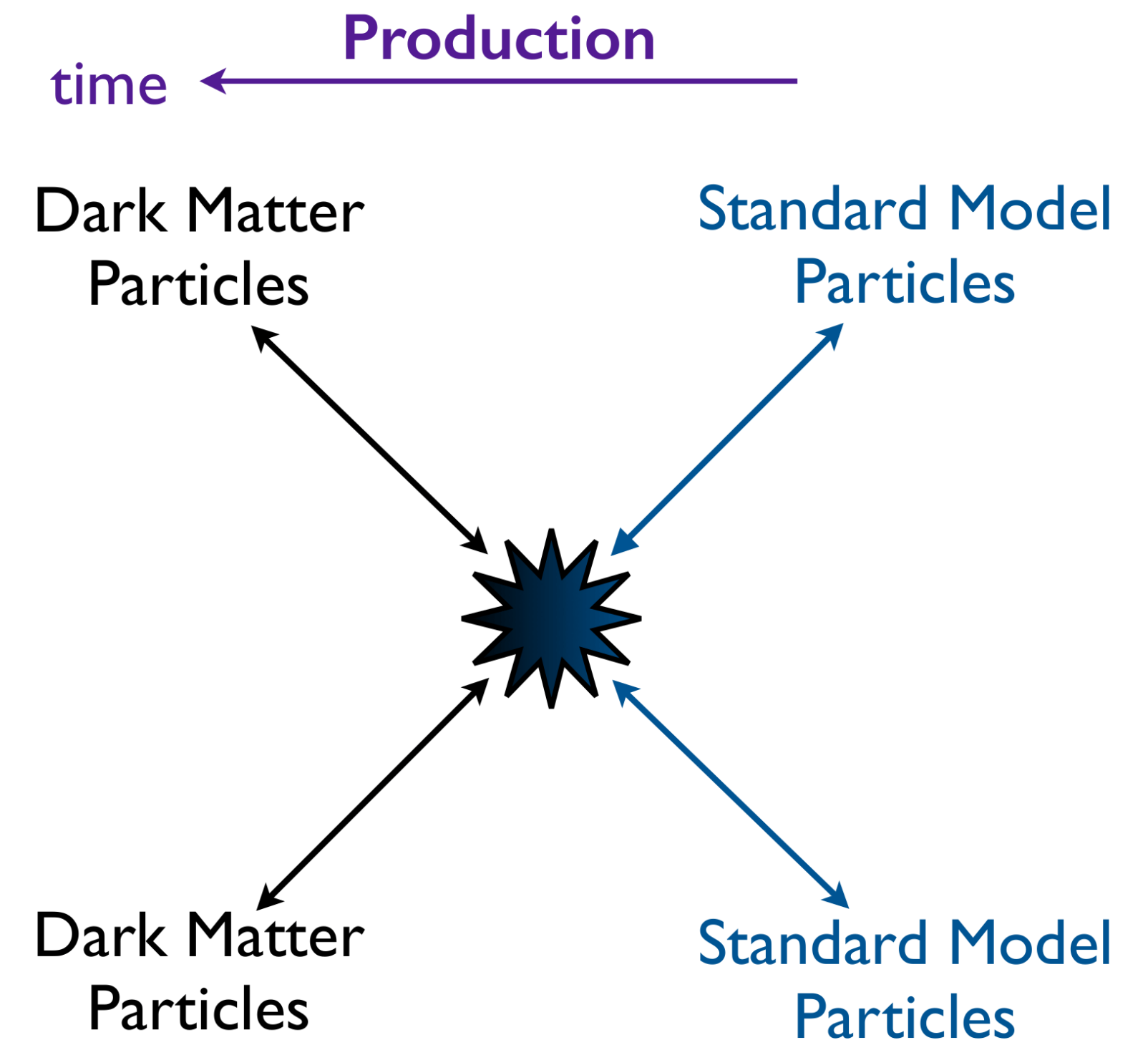
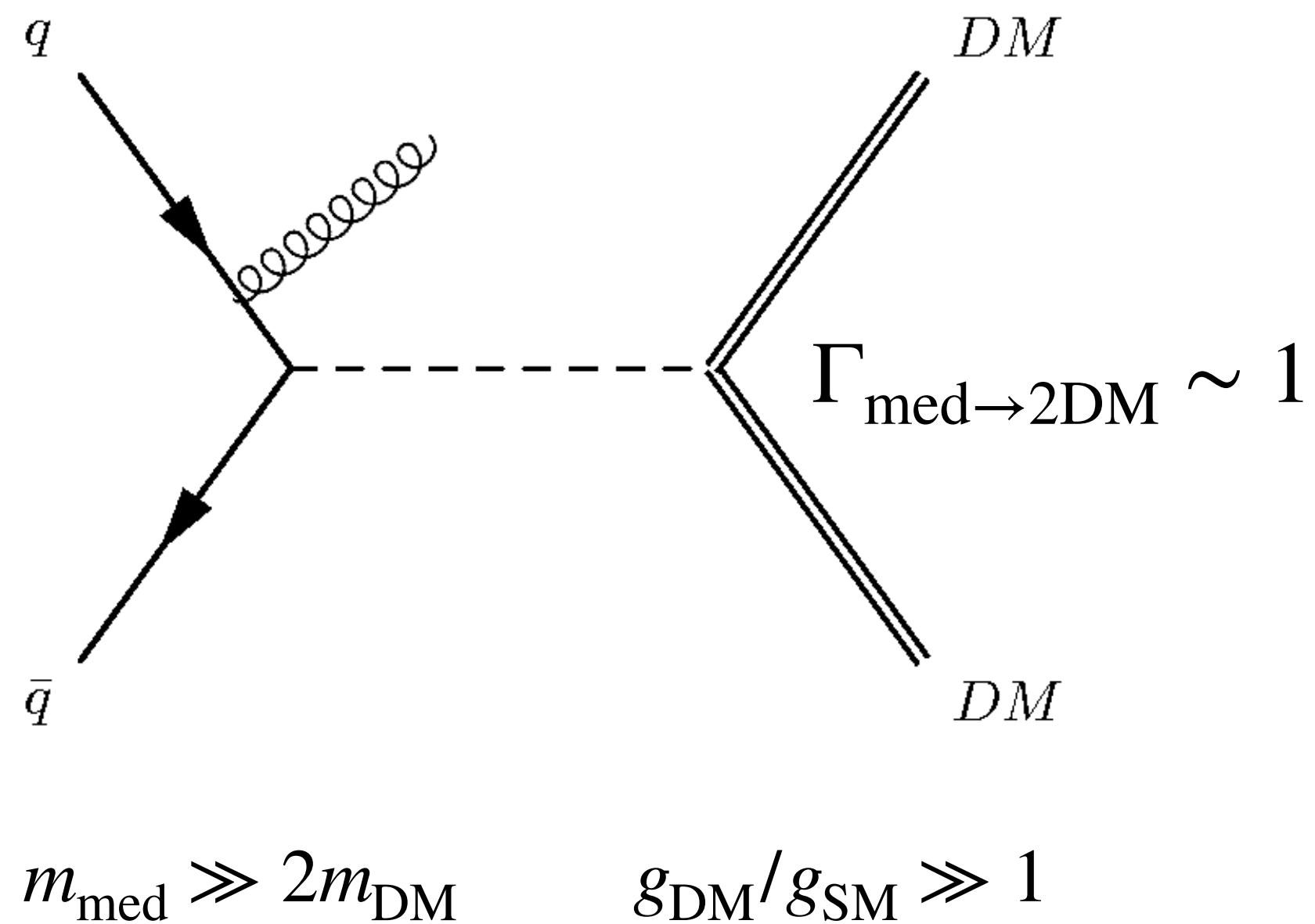
WIMP production at colliders

- Colliders typically *most* sensitive to the mediator-SM coupling



WIMP production at colliders

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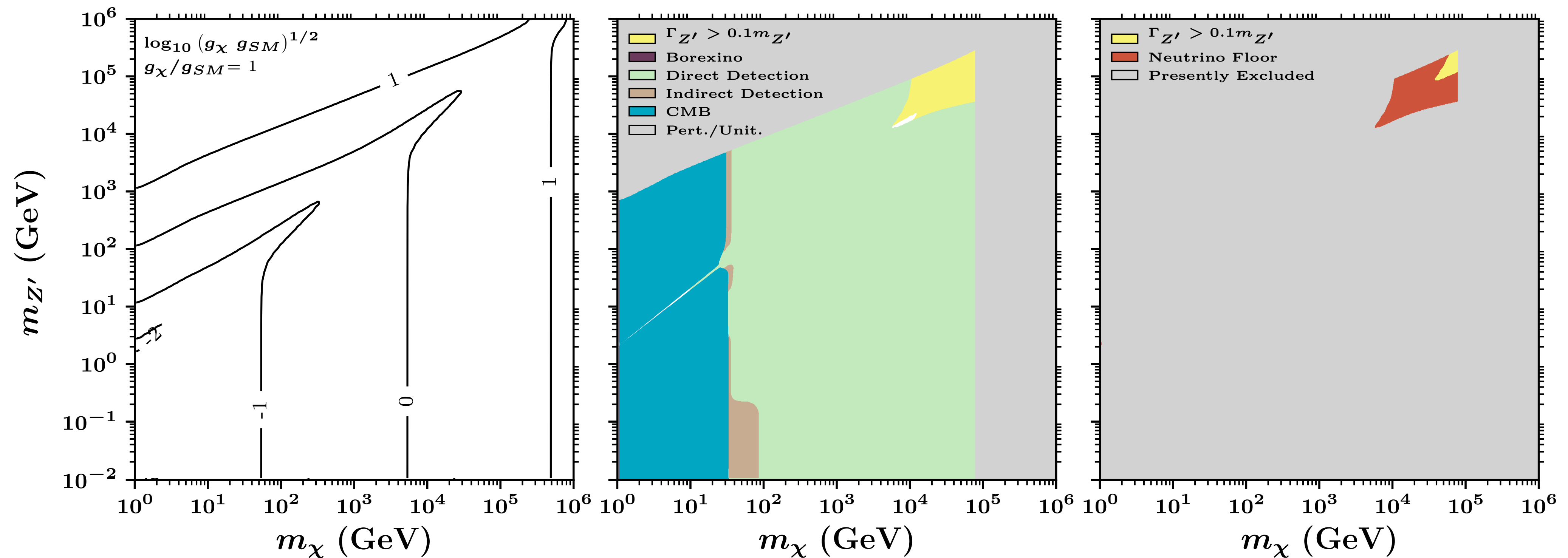


Small SM couplings means mediator never produced

Status of WIMP searches (as of 2018)

Dirac fermion coupled to universally to SM

Free parameters: dark matter mass m_χ , mediator mass $m_{Z'}$, dark matter coupling g_χ , SM coupling g_{SM}



Blanco, Escudero, Hooper, SJW (2018)

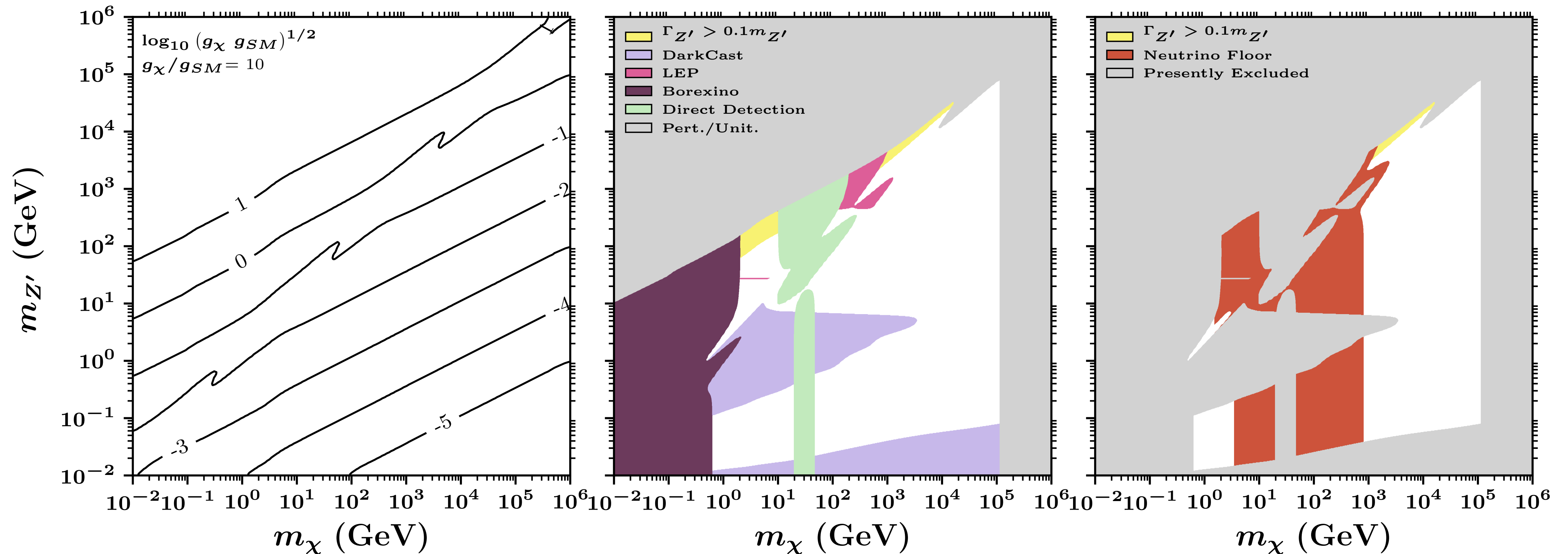
See also e.g. Escudero et al (2016), Arcadi et al (2024)

Status of WIMP searches (as of 2018)

Majorana fermion coupled to all SM leptons

$$\mathcal{L} \supset g' q_\chi Z'_\mu \bar{\chi} \gamma^\mu \gamma_5 \chi$$

[p-wave, q^2 suppressed]



Why astrophysical objects?

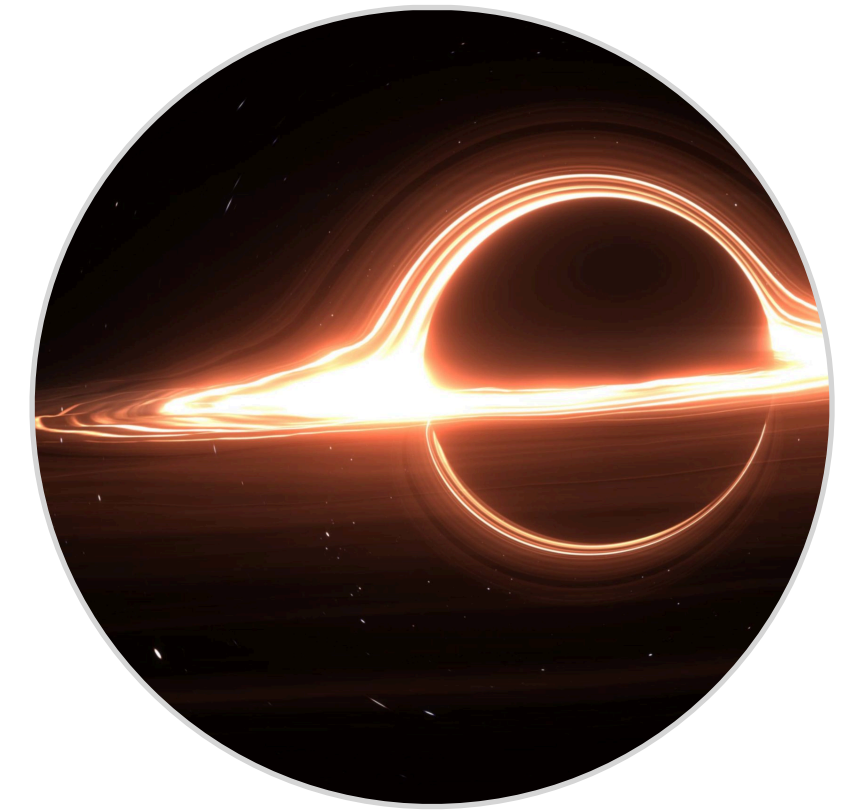
Nature has already given us the most extraordinary laboratories...



Strong electromagnetic fields



High densities



Strong gravity

*High temperatures /
Low temperatures*

Different baselines

Why astrophysical objects?

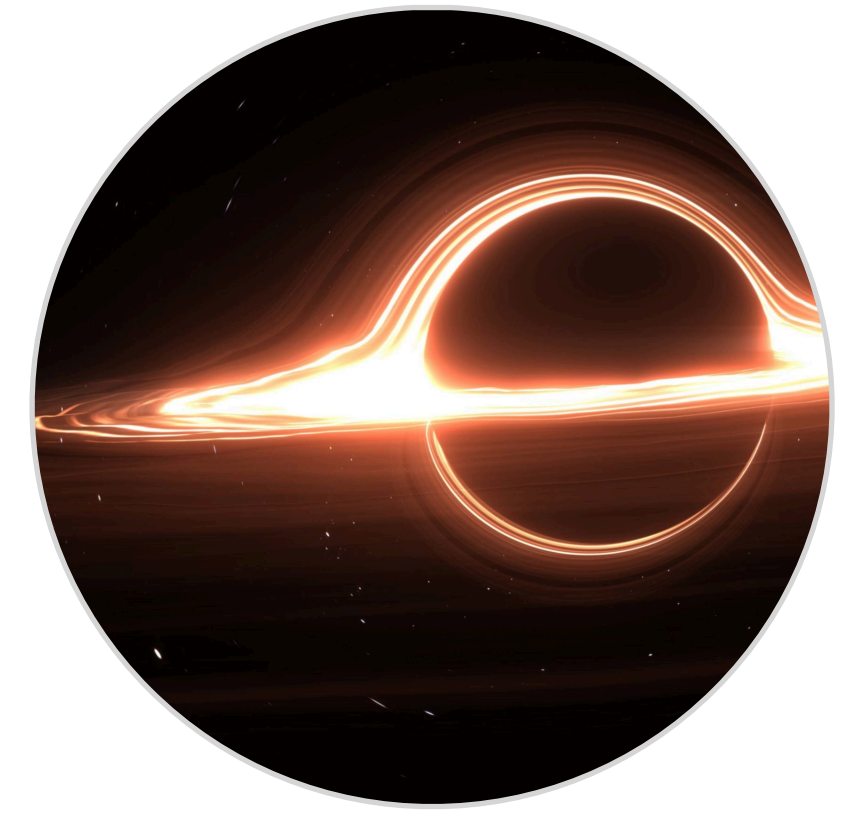
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Different baselines

E.g. Axion @ Earth \neq Axions @ compact object

Relevant questions to be asking...



- **For a given object, what makes it particularly special?**

Informs what physics you search for and what physics must be included...

- **How do we identify meaningful observables?**

Intrinsic trade-off between robustness and precision

- **How are these probes complementary to other searches?**

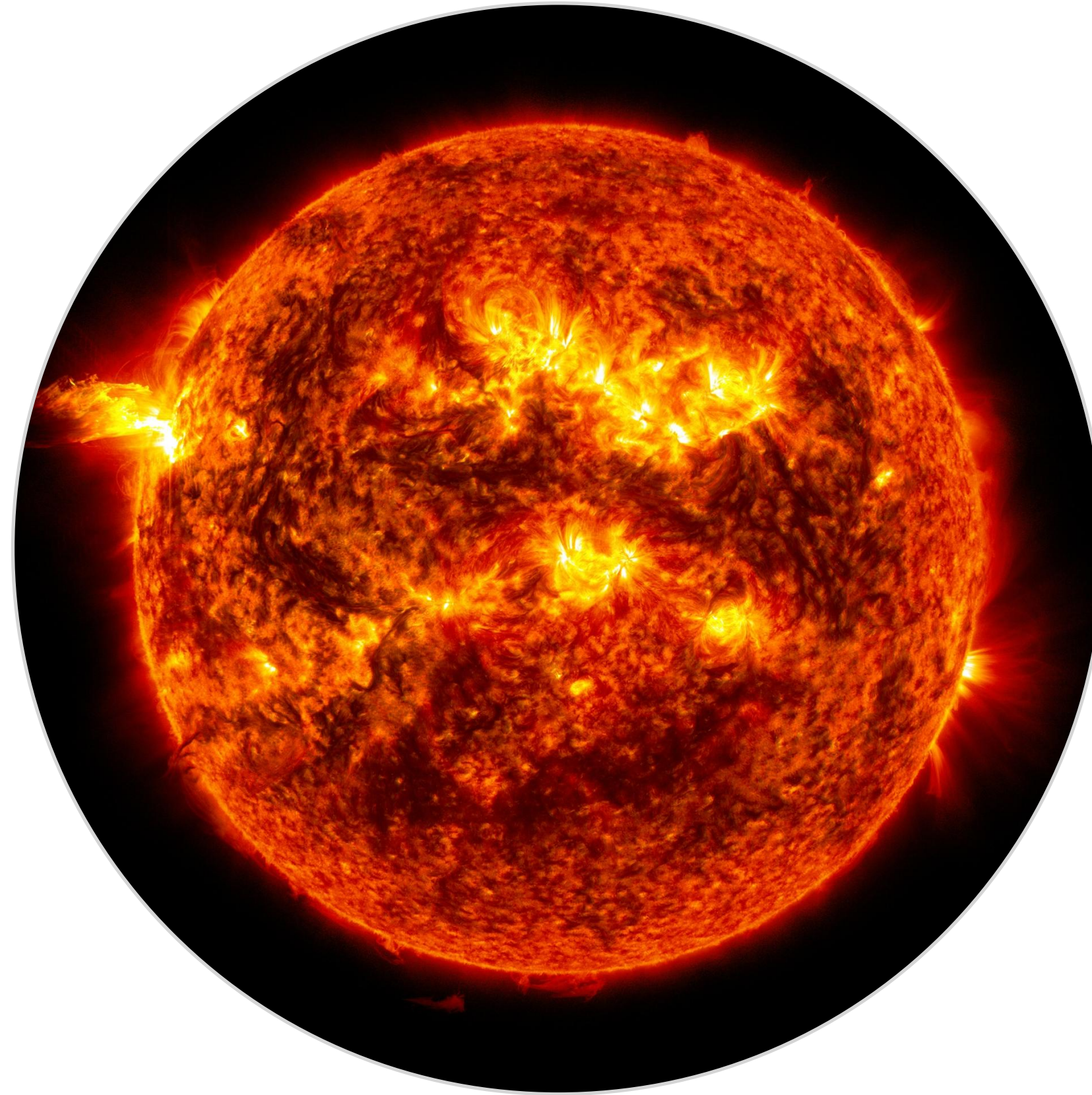
Different underlying assumptions, expediate laboratory searches, extract secondary information, ...

The Sun as an example

Why?

It's close to Earth

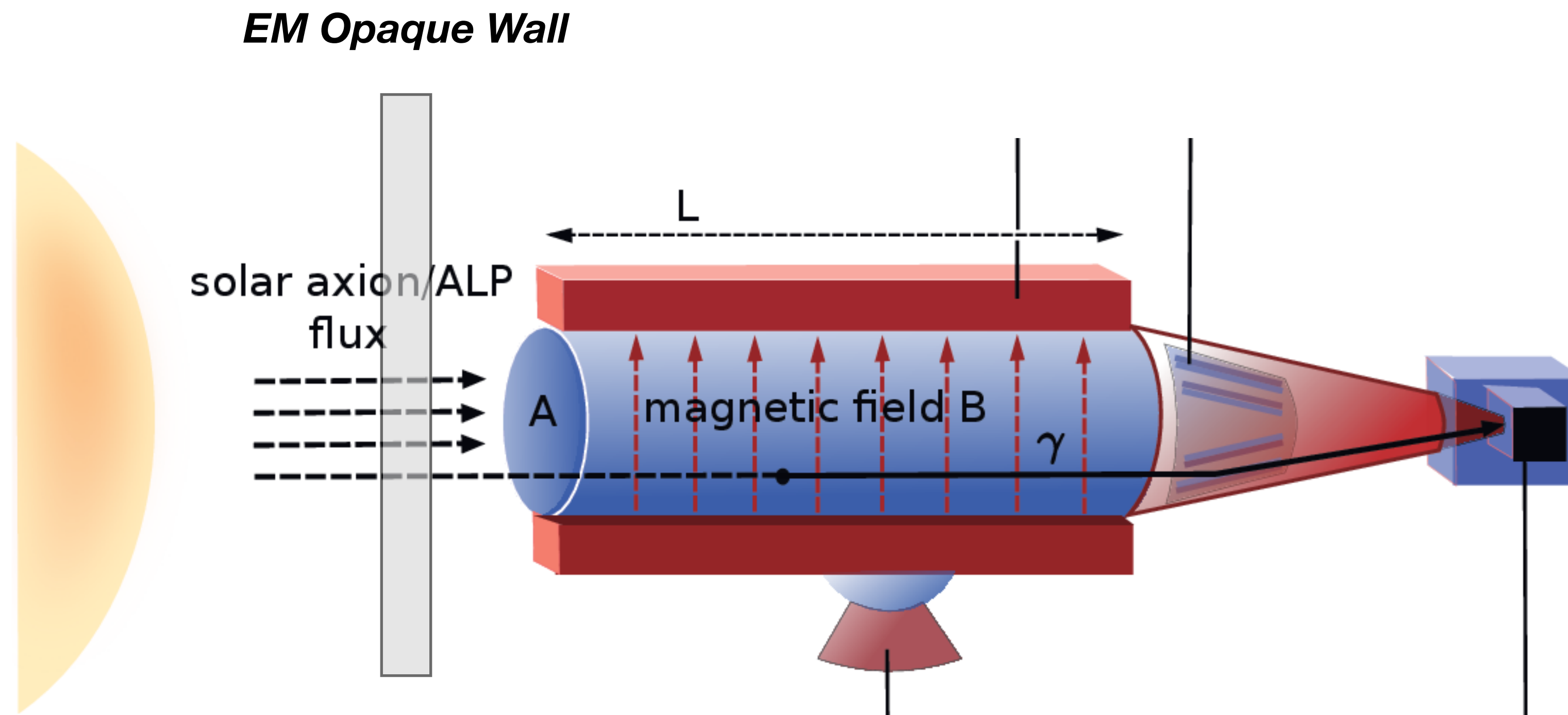
*It's relatively mundane
(low systematics)*



The Sun as an example: Axions

What makes the Sun special?

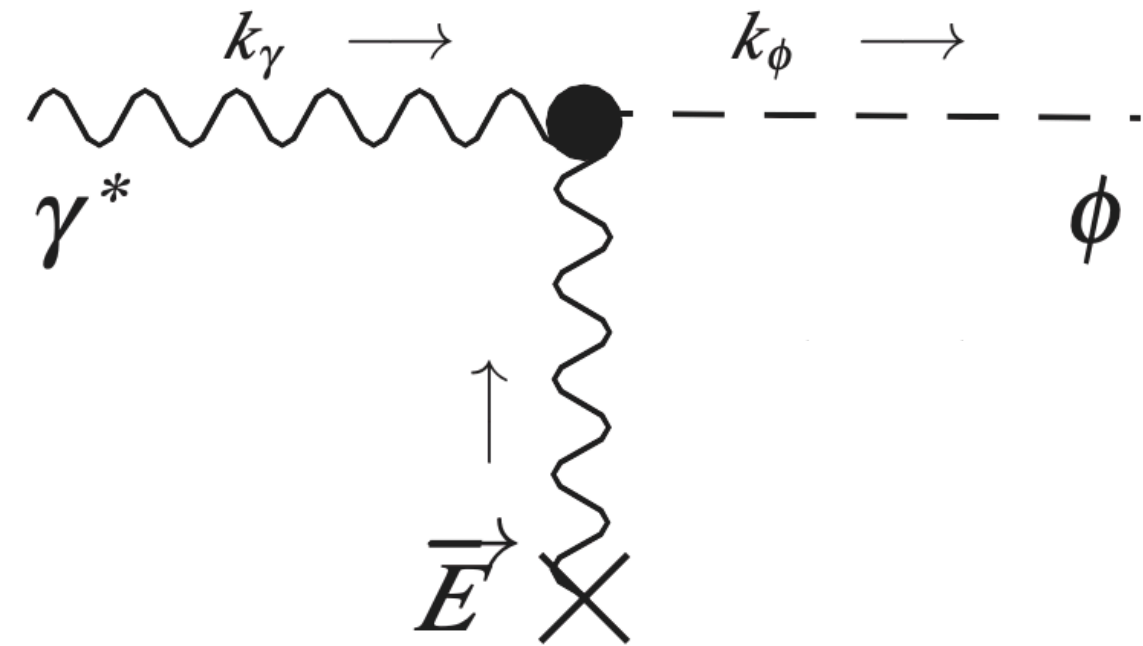
Large, hot-ish nearby thermal bath



The Sun as an example: Axions

How are axions produced in the Sun?

Primakoff



$$\gamma + (Ze) \rightarrow (Ze) + a$$

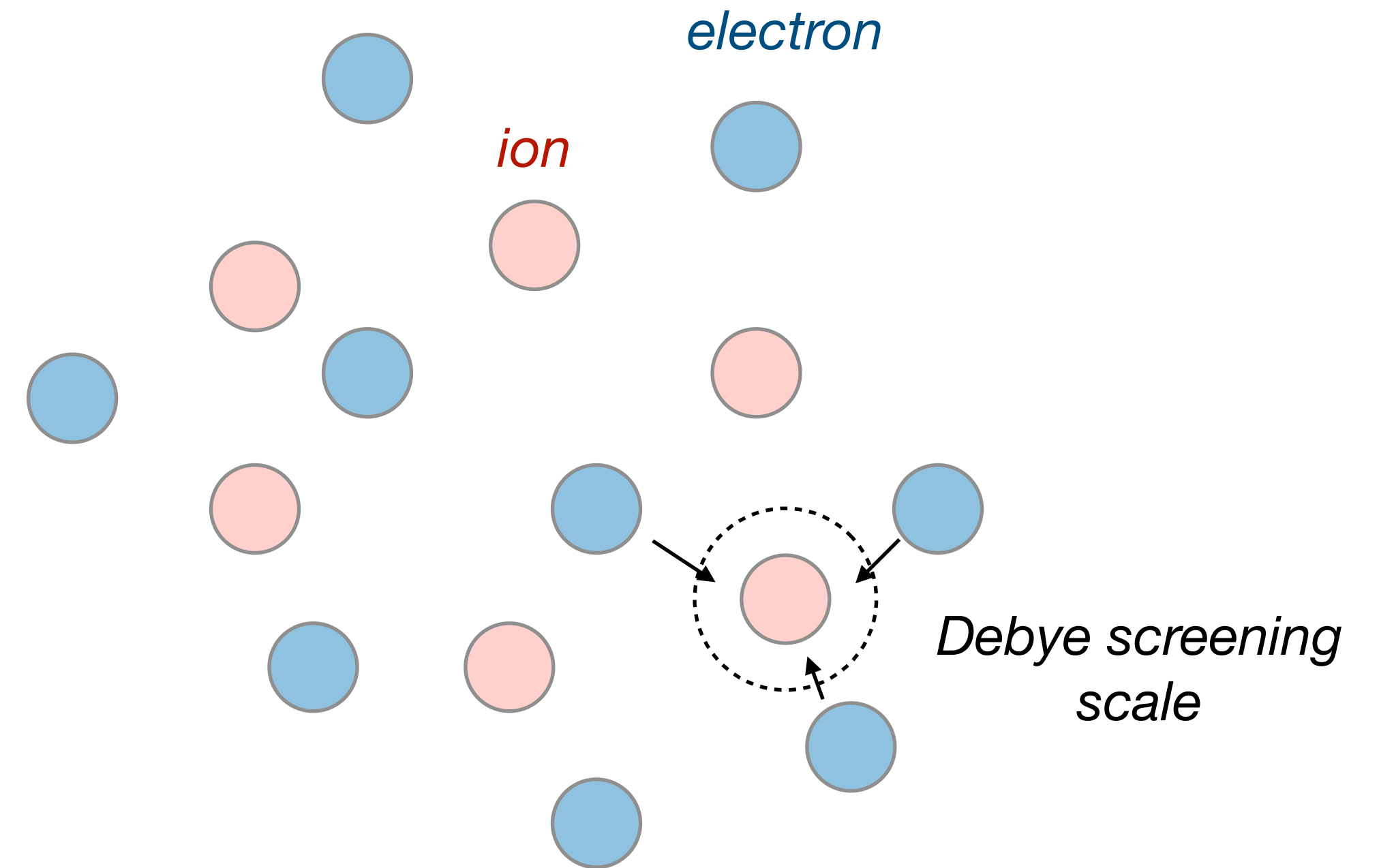
$$L_a \sim \int dV \int d^3k \omega_\gamma f_\gamma(\omega_\gamma) \sum_{i \in \text{species}} (g_{a\gamma} Z_i e)^2 n_i K(k) D(k)$$

*Bose-Einstein
Distribution*

Coupling

*Kinematic
factors (T)*

Screening

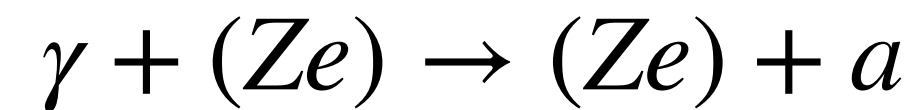
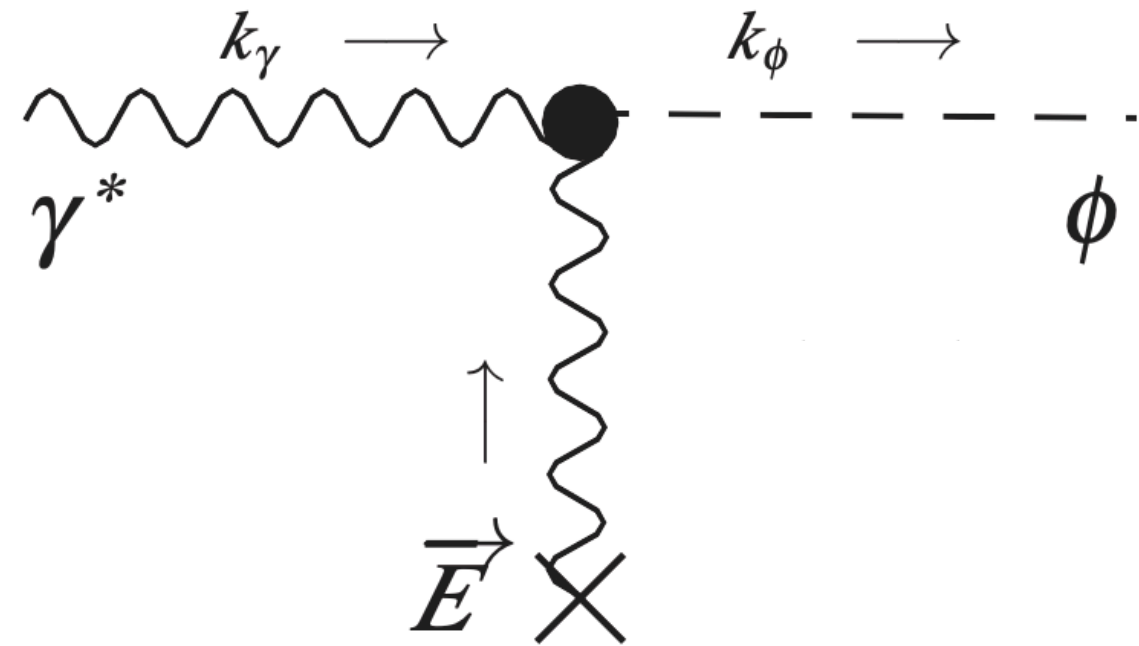


See e.g. Raffelt (1988), Review 2401.13728

The Sun as an example: Axions

How are axions produced in the Sun?

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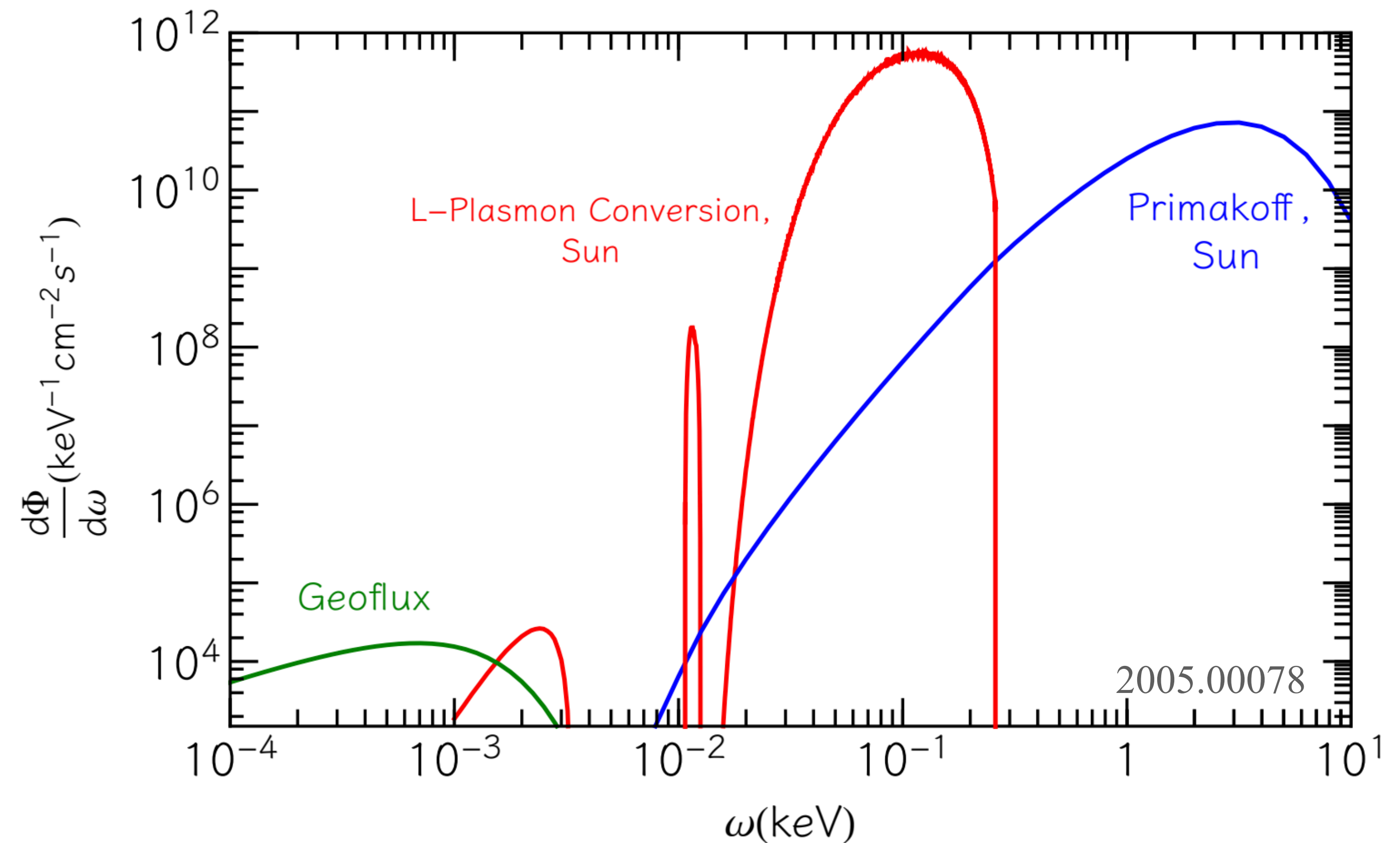
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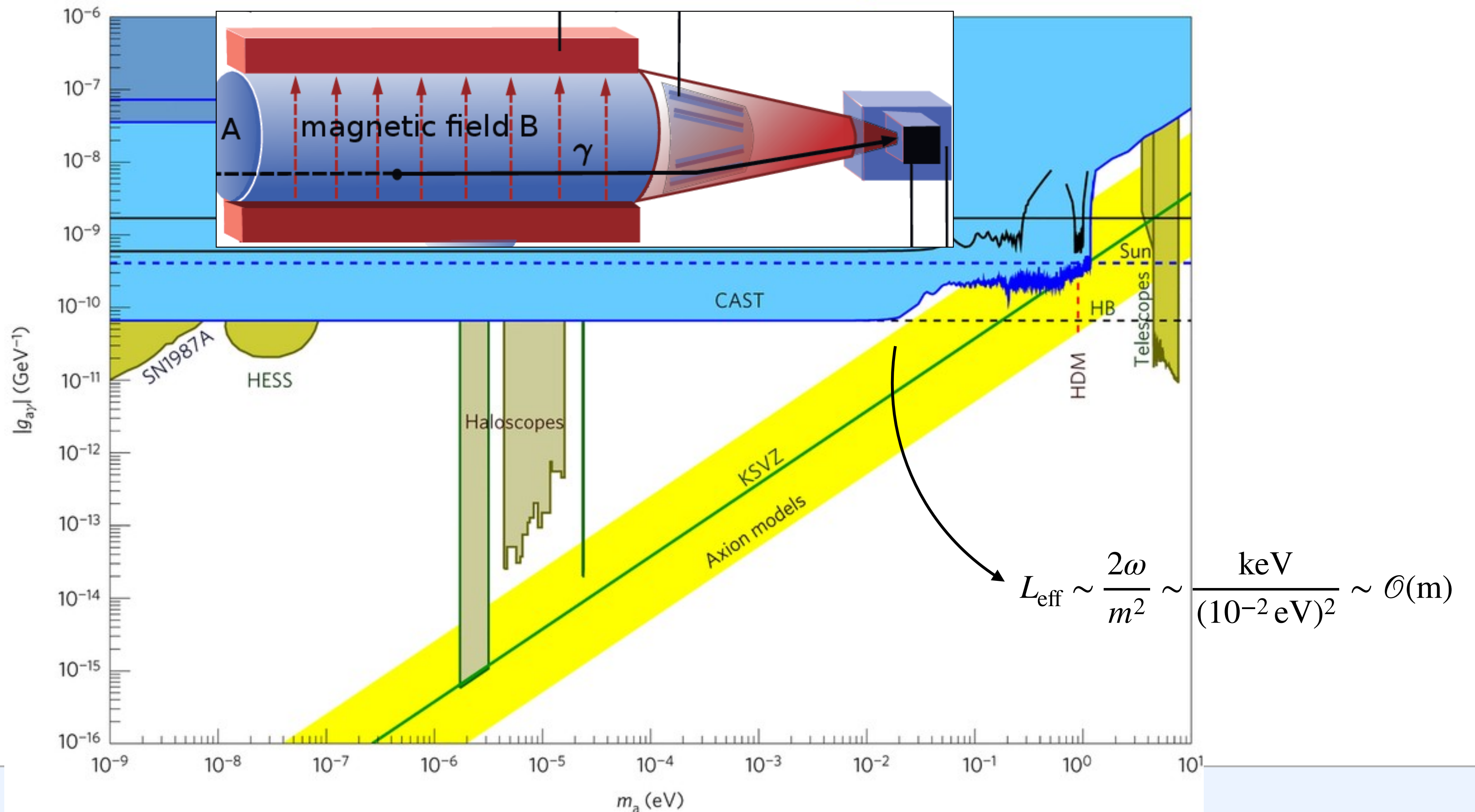
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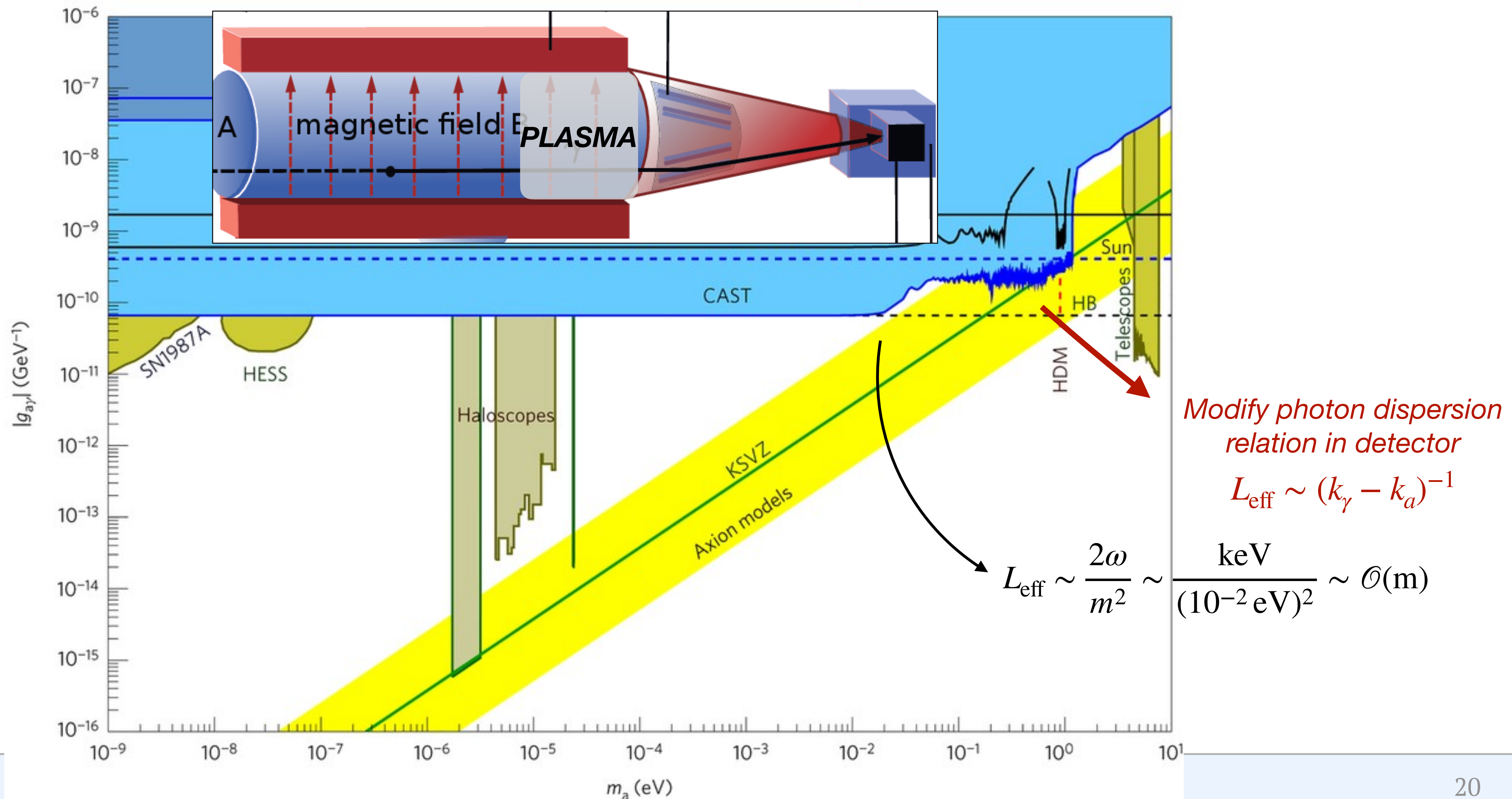


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The Sun as an example: Axions

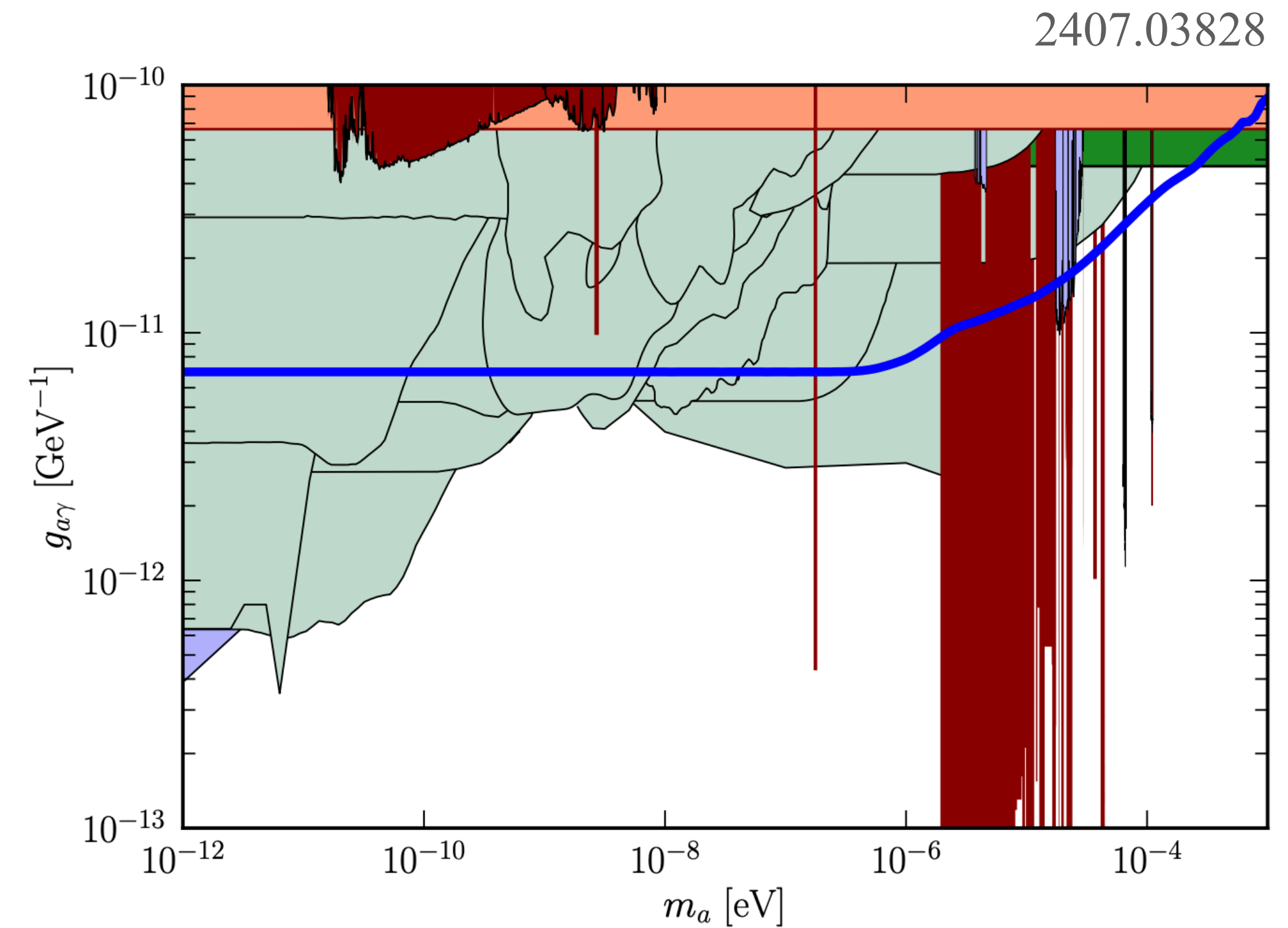
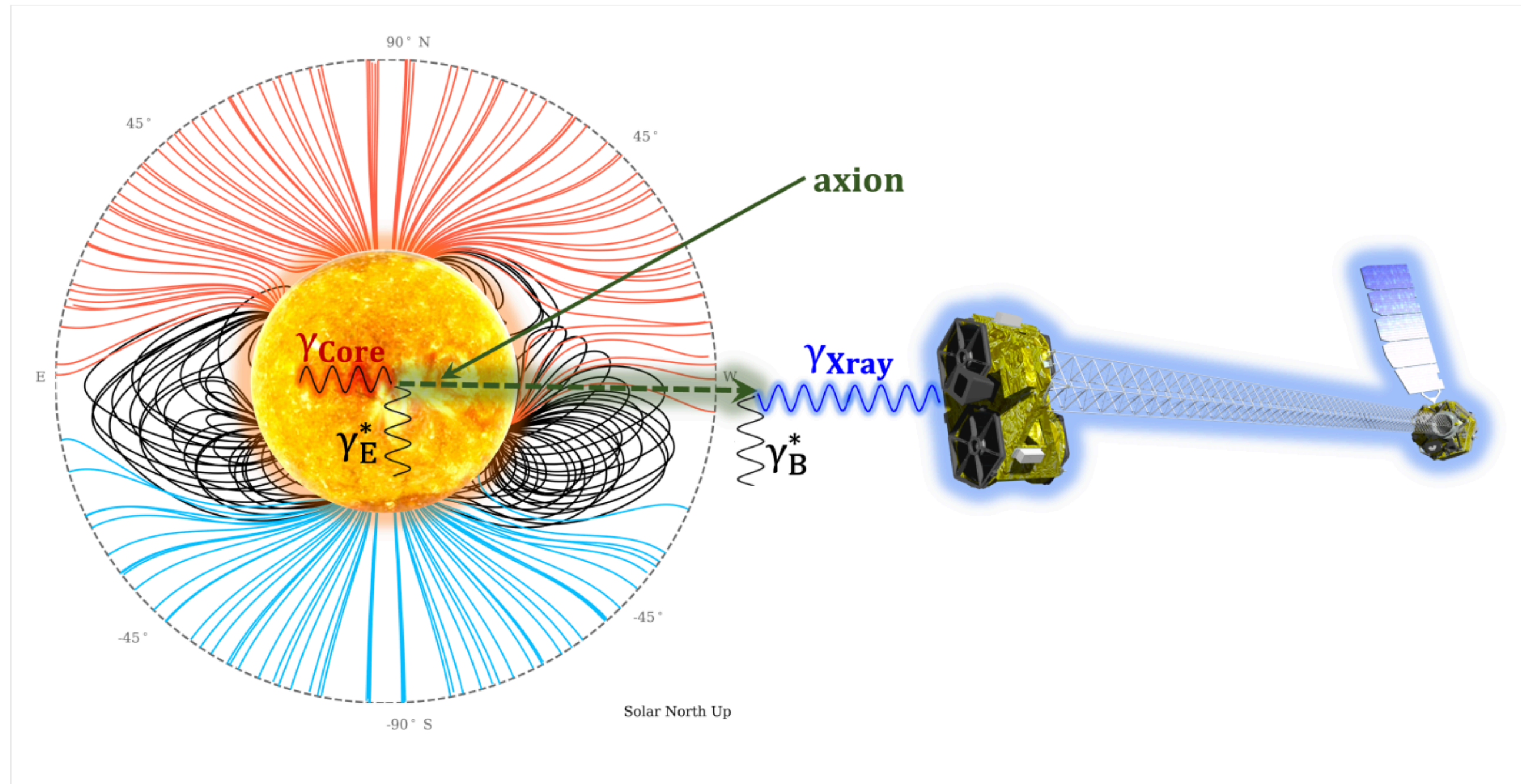


The Sun as an example: Axions

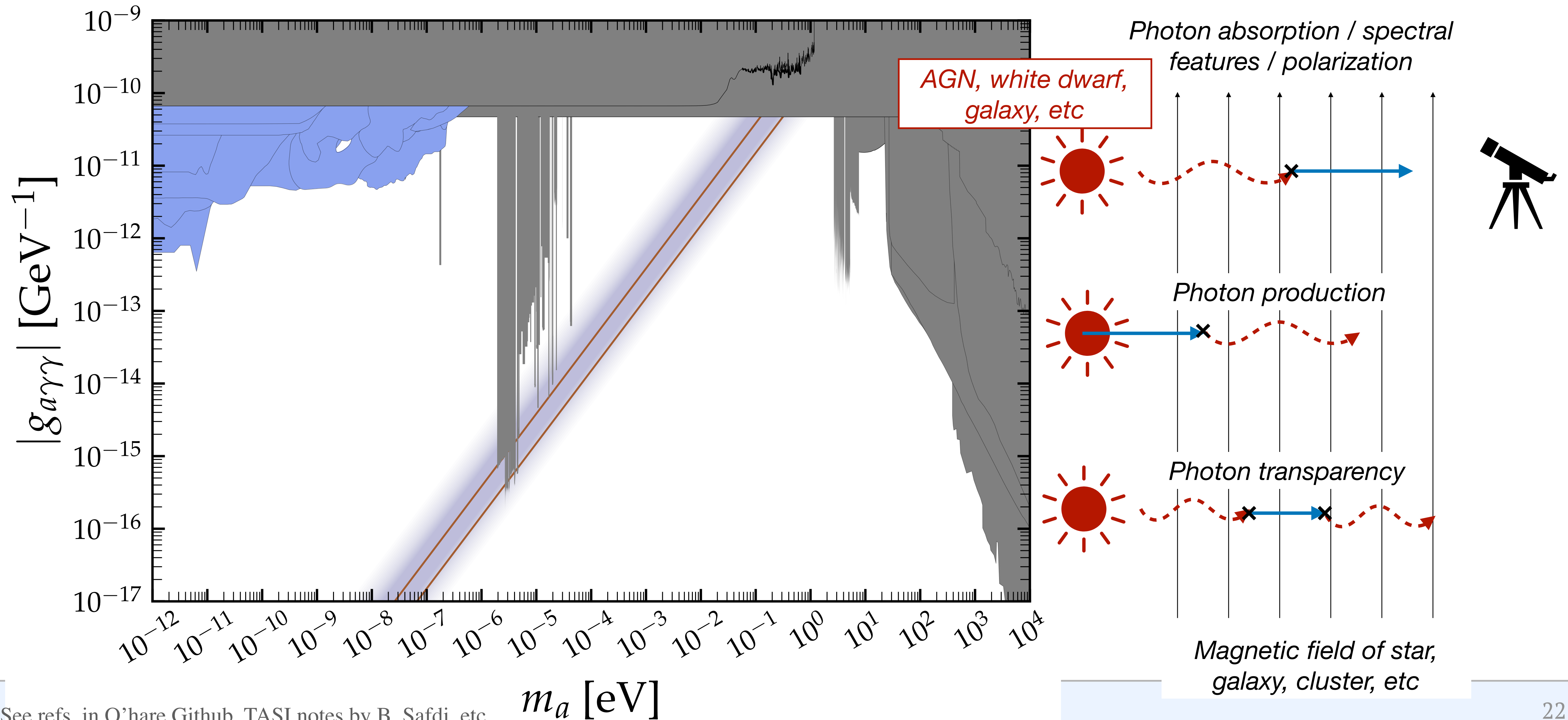


The Sun as an example: Axions

Can also try to re-convert using solar magnetic fields



Similar searches using other objects...



The Sun as an example: Dark Photons

What makes the Sun special?

Large, hot-ish nearby thermal bath

$$\mathcal{L} \supset \frac{1}{2} m_{\gamma'}^2 S^\mu S_\mu - \chi m_{\gamma'}^2 S^\mu A_\mu + J^\mu A_\mu$$

Sterile state

EM Coupled state

The Sun as an example: Dark Photons

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Sterile state

EM Coupled state

Coupled Equations of motion

$$(\omega^2 - k^2 - \pi^{\mu\nu}) A_\nu + \chi m_{\gamma'}^2 S^\mu = 0$$

Polarization tensor (defines dispersion relation)

ω_p^2 (Trans.)

$\omega_p^2 - k^2$ (Long.)

$$(\omega^2 - k^2 - m_{\gamma'}^2) S^\mu + \chi m_{\gamma'}^2 A^\mu = 0$$

The Sun as an example: Dark Photons

Going to mass basis:

$$A_i \rightarrow \tilde{A}_i + \chi \frac{m_{\gamma'}^2}{\pi_i - m_{\gamma'}^2} \tilde{S}_i \quad i = \text{T/L}$$

EM
Coupled *Photon* *Dark Photon*

See e.g. 0801.1527 (Redondo), An et al (2013, 2020)

The Sun as an example: Dark Photons

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EM Coupled *Photon* *Dark Photon*

$$L_\chi \sim \int dV \int d^3k \, \omega_\gamma f_\gamma(\omega_\gamma) \Gamma_i \left(\frac{\chi m_{\gamma'}^2}{\pi_i - m_{\gamma'}^2} \right)^2$$

Bose-Einstein Distribution *Rate* *Contribution of dark photon to A*

See e.g. 0801.1527 (Redondo), An et al (2013, 2020)

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*EM
Coupled*

Photon

Dark Photon

Start from Boltzmann Eqn

$$(\partial_t + v\partial_x)f = \Gamma_E(1+f) - \Gamma_A f = \Gamma_E - (\Gamma_A - \Gamma_E)f \equiv \Gamma_A^*$$

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Bose-Einstein Distribution (points to $f_\gamma(\omega_\gamma)$)

Rate (points to Γ_i)

Contribution of dark photon to A (points to $\left(\frac{\chi m_{\gamma'}^2}{\pi_i - m_{\gamma'}^2} \right)^2$)

Start from Boltzmann Eqn

$$(\partial_t + v\partial_x)f = \Gamma_E(1+f) - \Gamma_A f = \Gamma_E - (\Gamma_A - \Gamma_E)f \equiv \Gamma_A^*$$

Equilibrium implies RHS = 0

$$\Gamma_A = e^{\omega/T} \Gamma_E$$

$$\Gamma \equiv \Gamma_A^* = \Gamma_A(1 - e^{-\omega/T})$$

Consider deviations from Equil.

$$\Delta f = f - f_{\text{eq}}$$

$$(\partial_t + v\partial_x)\Delta f = -\Gamma\Delta f$$

See e.g. 0801.1527 (Redondo), An et al (2013, 2020)

The Sun as an example: Dark Photons

Redondo (2008)

Observables:

- Sun is roughly 4.57 Gyr, halfway through hydrogen burning
- Neutrino fluxes (depend on T_c)
 - Excess luminosity (via transverse / longitudinal conversion) shorten lifetime
- Dark photons re-converting to x-rays in CAST (*no magnetic field necessary*)

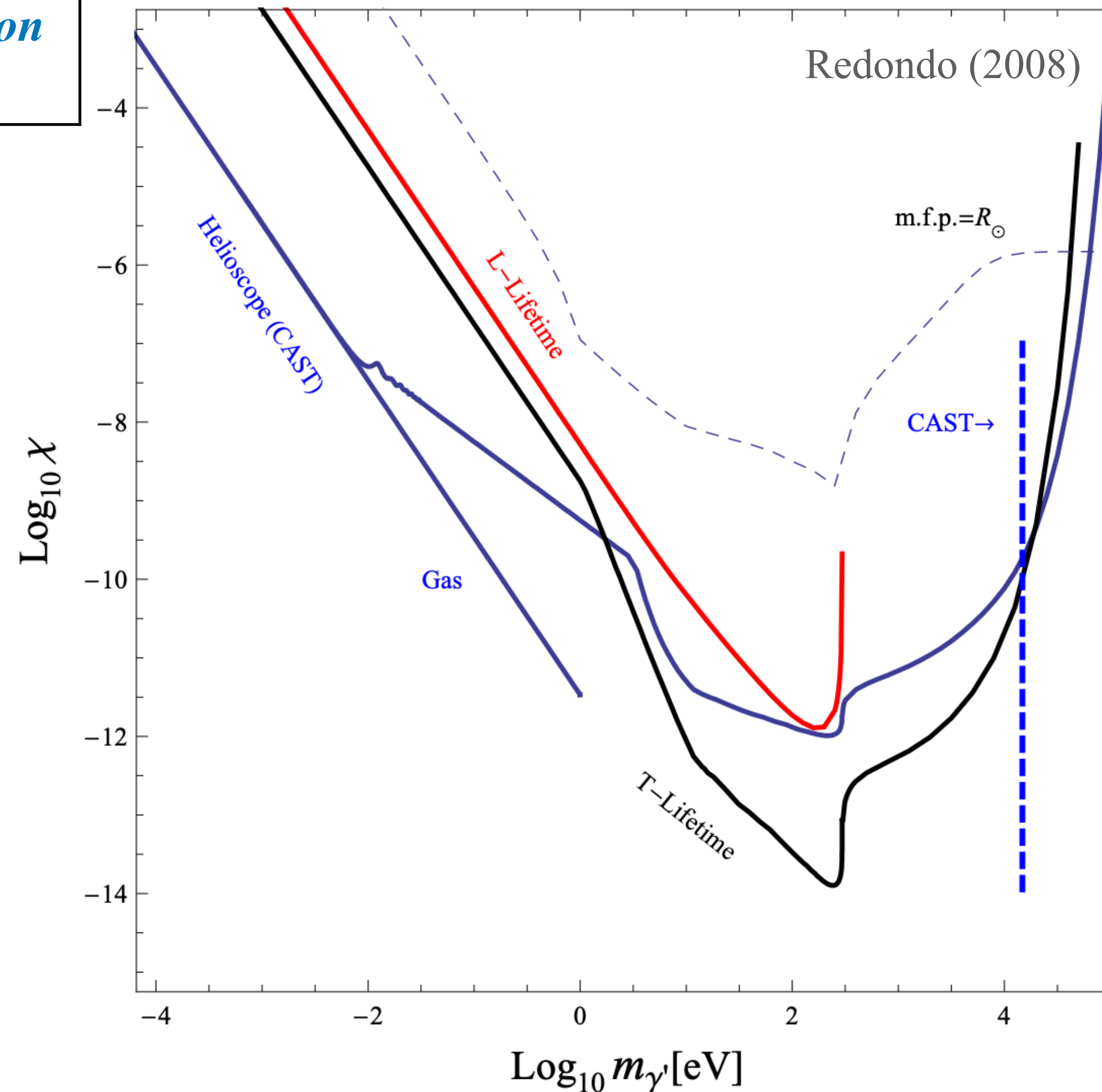
The Sun as an example: Dark Photons

In-medium suppression

$$\chi_{\text{eff}} \sim \chi(m_{\gamma'}/\omega_p)^2$$

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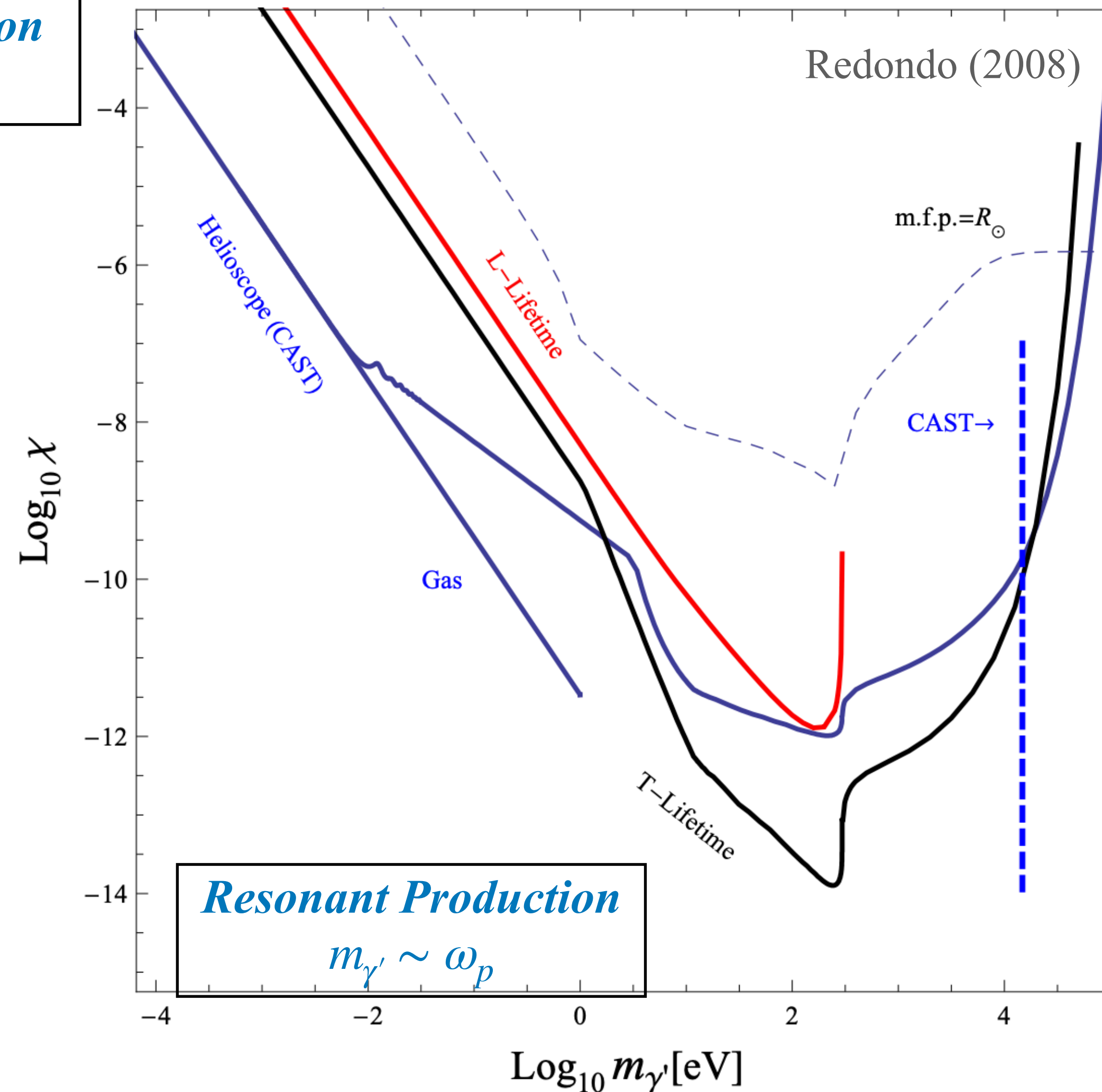
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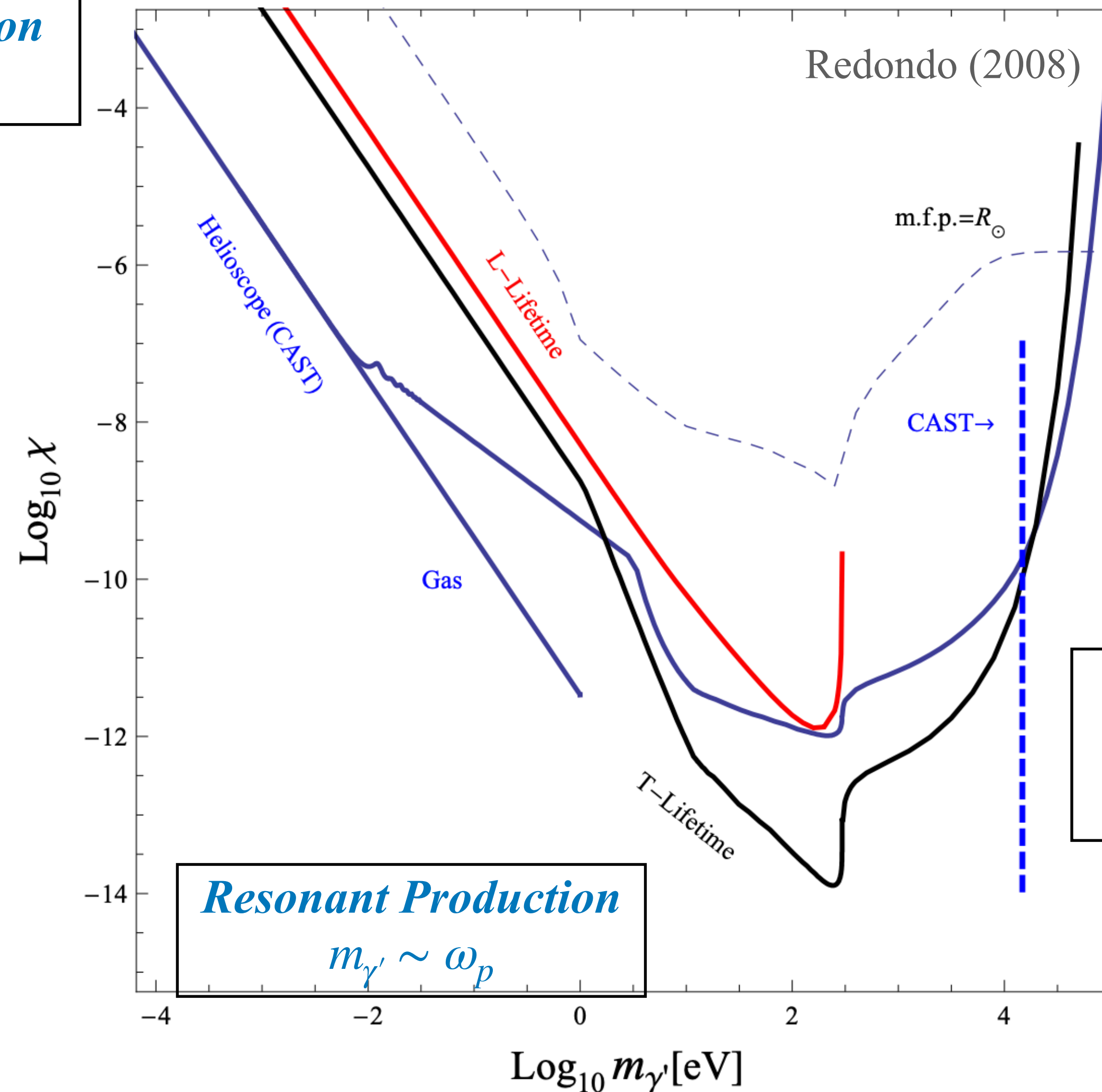
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Unsuppressed production

$$\omega > \omega_p$$

$$\chi_{\text{eff}} \sim \chi$$

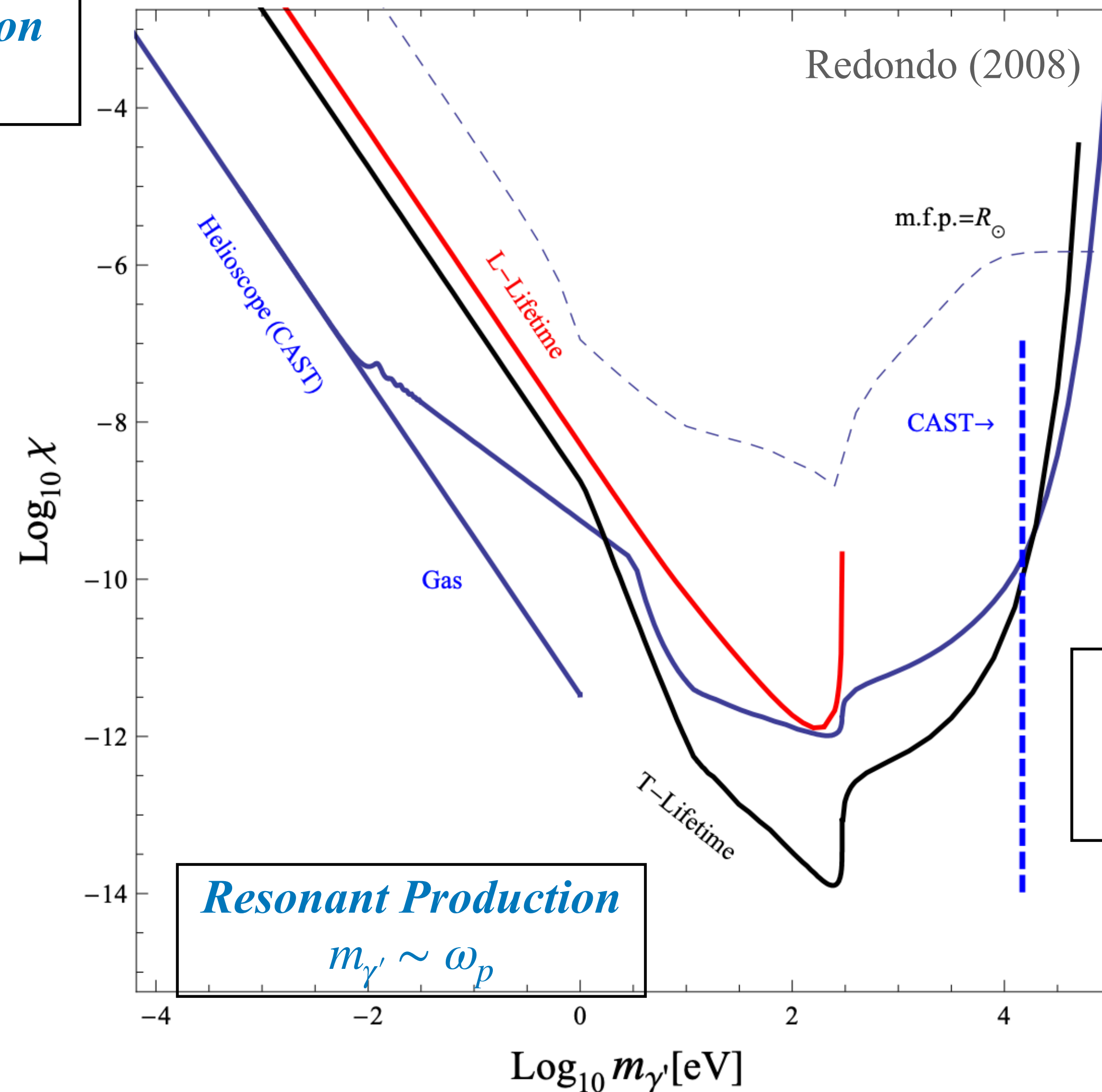
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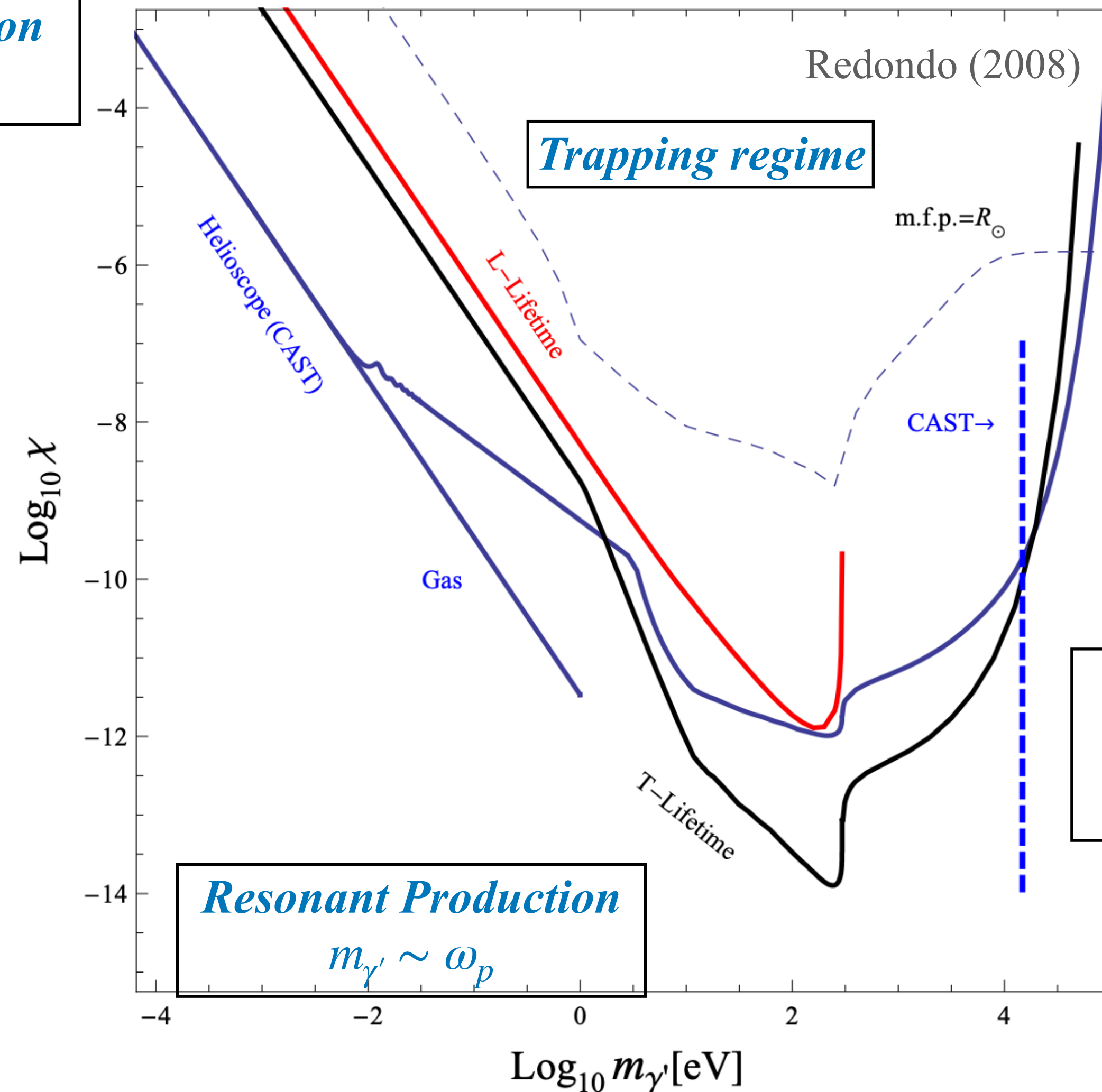
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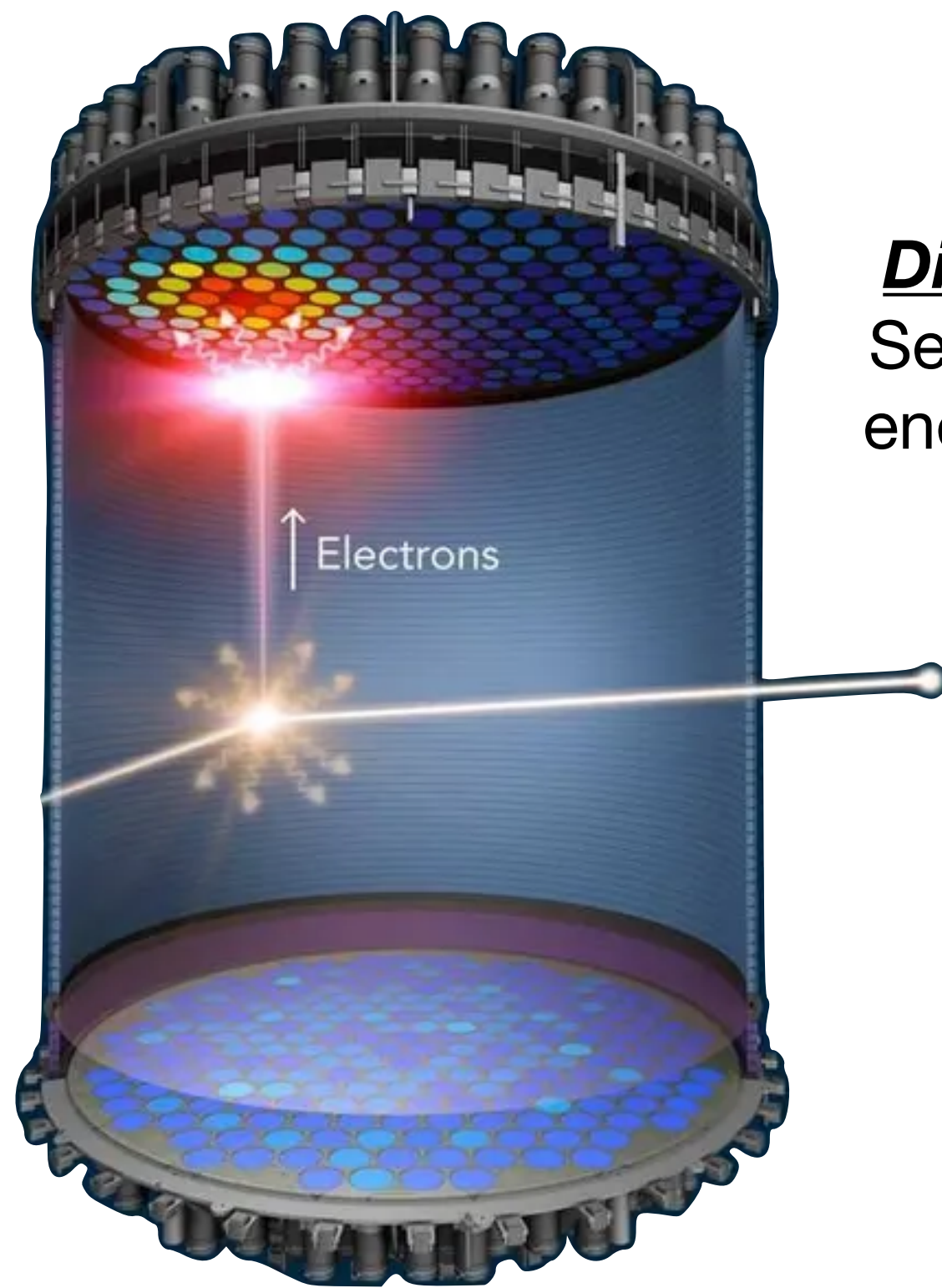
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The Sun as an example: WIMPs

What makes the Sun special?

Giant ball of nucleons

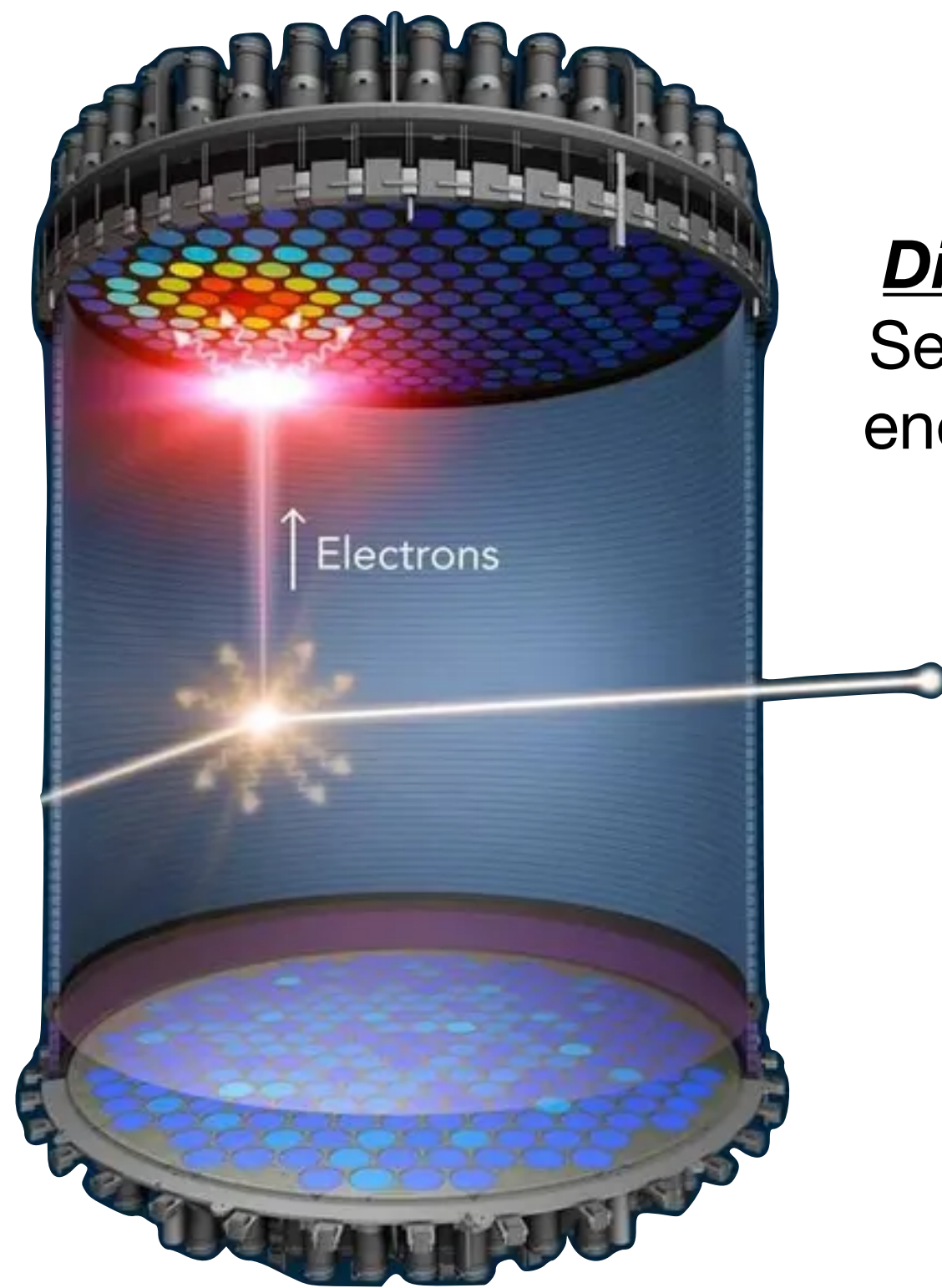


Direct detection:
Search for kinetic
energy deposition

The Sun as an example: WIMPs

What makes the Sun special?

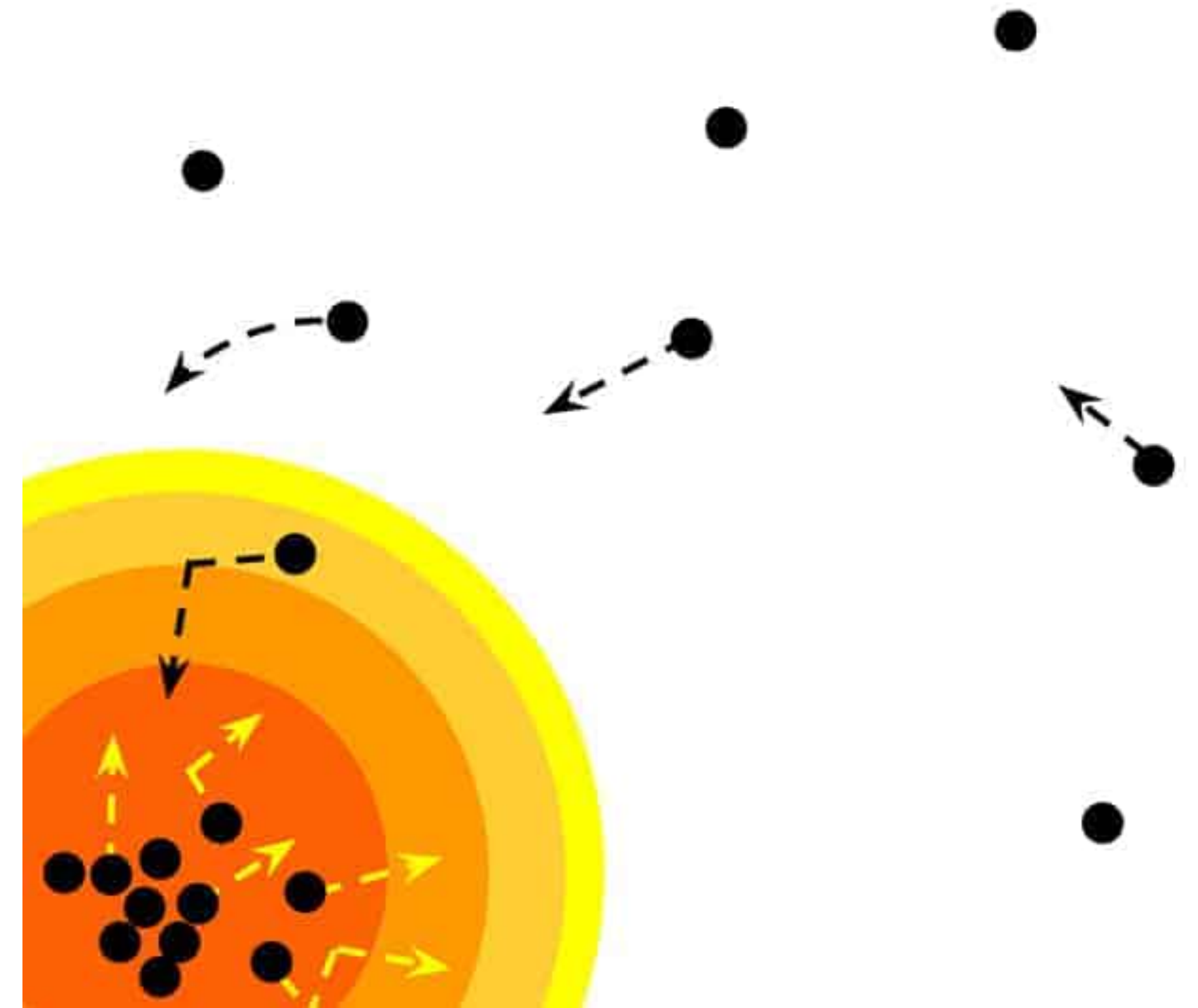
Giant ball of nucleons



Direct detection:
Search for kinetic
energy deposition

Here:
Kinetic energy
negligible

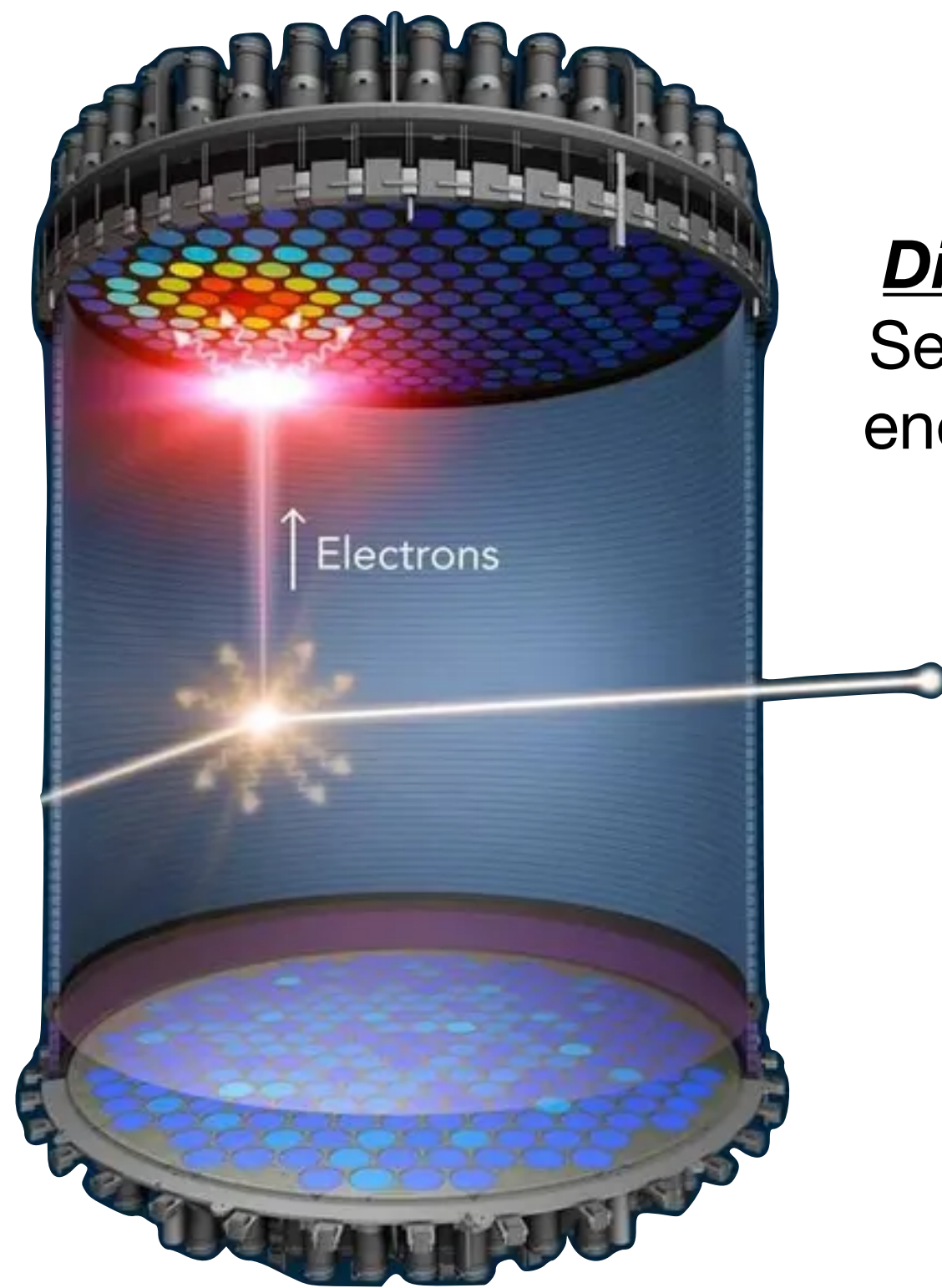
$$\frac{(\text{KE flux DM})}{(\text{Sun's Luminosity})} \ll 10^{-10}$$



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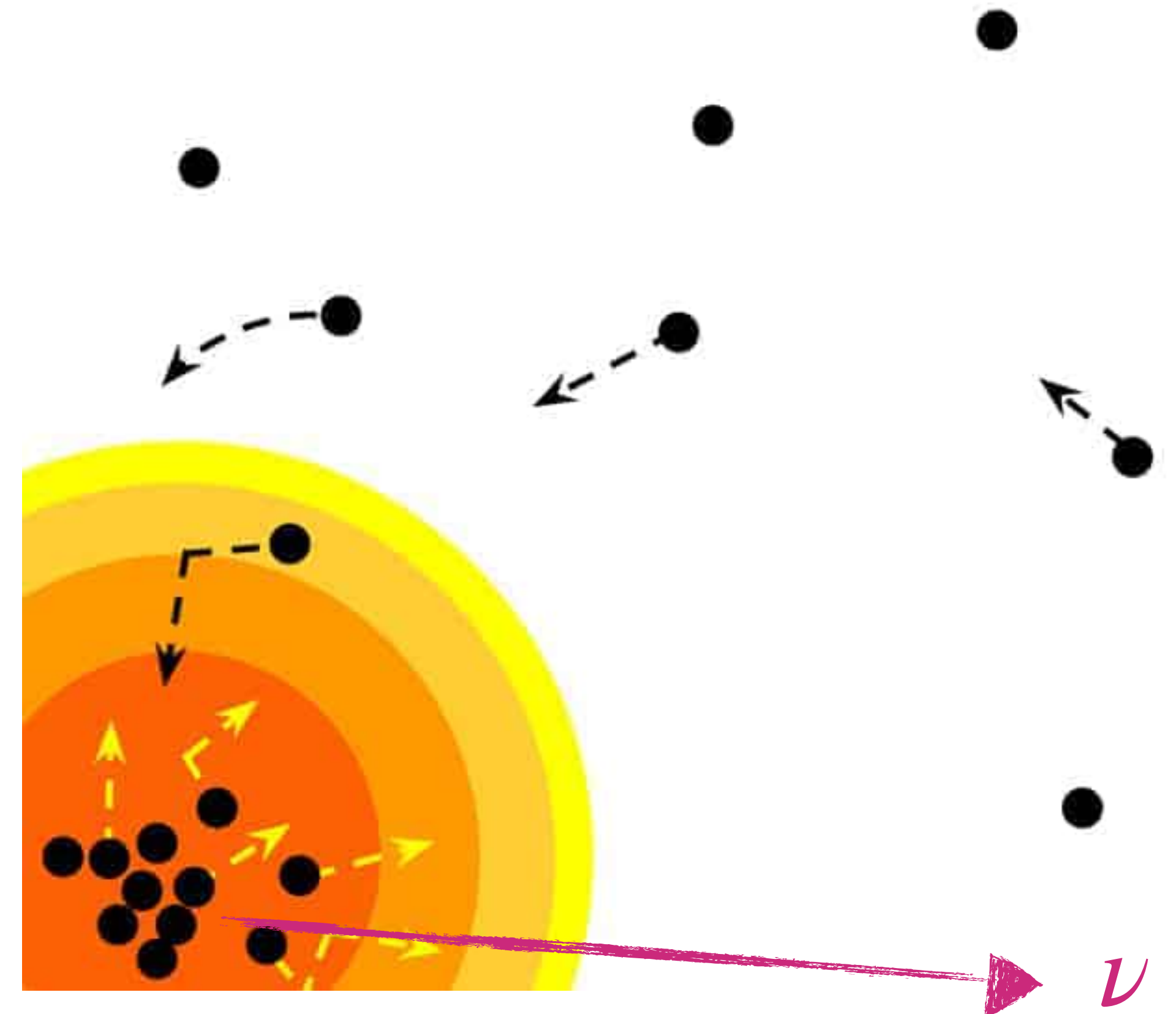
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$$\frac{dN}{dt} = \Gamma_{\text{capt}} - \Gamma_{\text{evap}} - 2\Gamma_{\text{ann}}$$

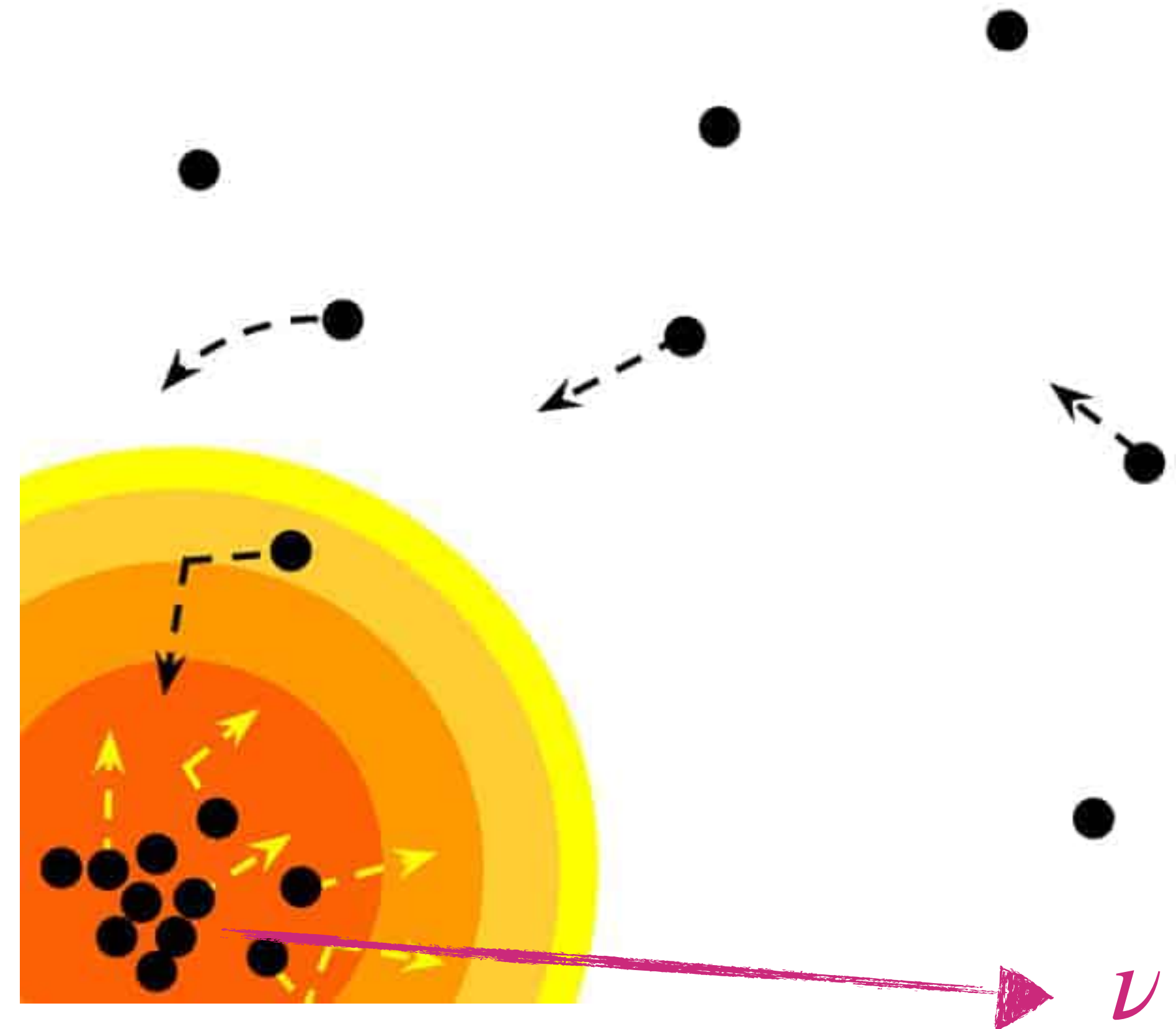
Capture rate: $\Gamma_{\text{capt}} \sim n_{\text{DM}} N_N \langle v_{\text{rel}} \rangle \sigma_N P_{\text{capture}}$

Capture Probability

Evaporation rate: $\Gamma_{\text{eval}} \sim n_{\text{capt}} N_N \sigma_N \langle v_{\text{rel}} \rangle P_{\text{evap}}$

Evaporation Probability

Annihilation rate of bound WIMPs: $2\Gamma_{\text{ann}} = \int dV n^2 \langle \sigma v \rangle$



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Equilibrium Distribution: $n(r) \propto e^{-r^2/r_0^2}$

$$r_0 \sim 10^{-2} R_{\odot} \sqrt{\frac{100 \text{ GeV}}{m_{\text{DM}}}}$$

*(From Virial Theorem
 $\langle K \rangle = -\frac{1}{2} \langle V \rangle$)*

$$\frac{dN}{dt} = \Gamma_{\text{capt}} - \Gamma_{\text{evap}} - 2\Gamma_{\text{ann}}$$

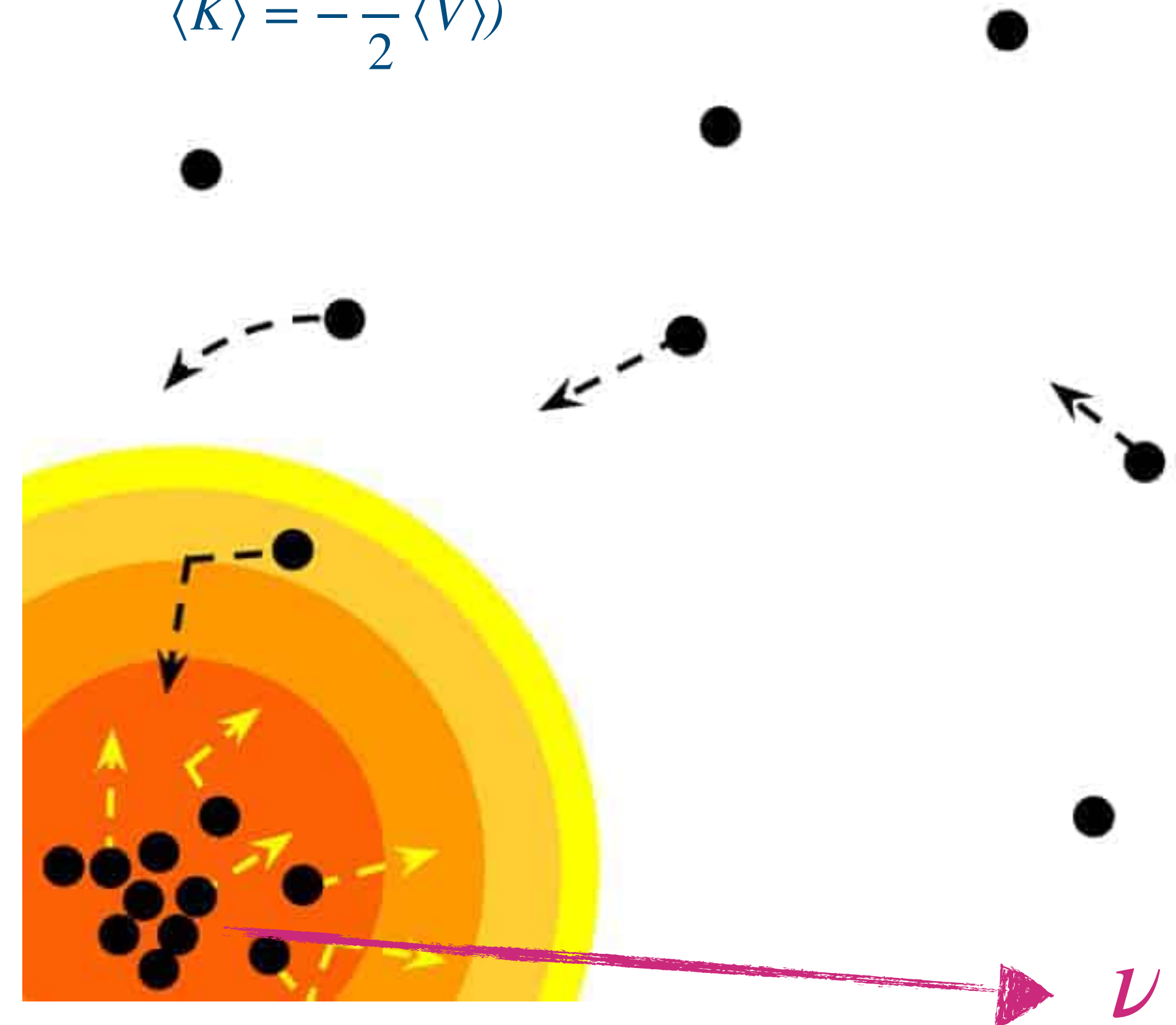
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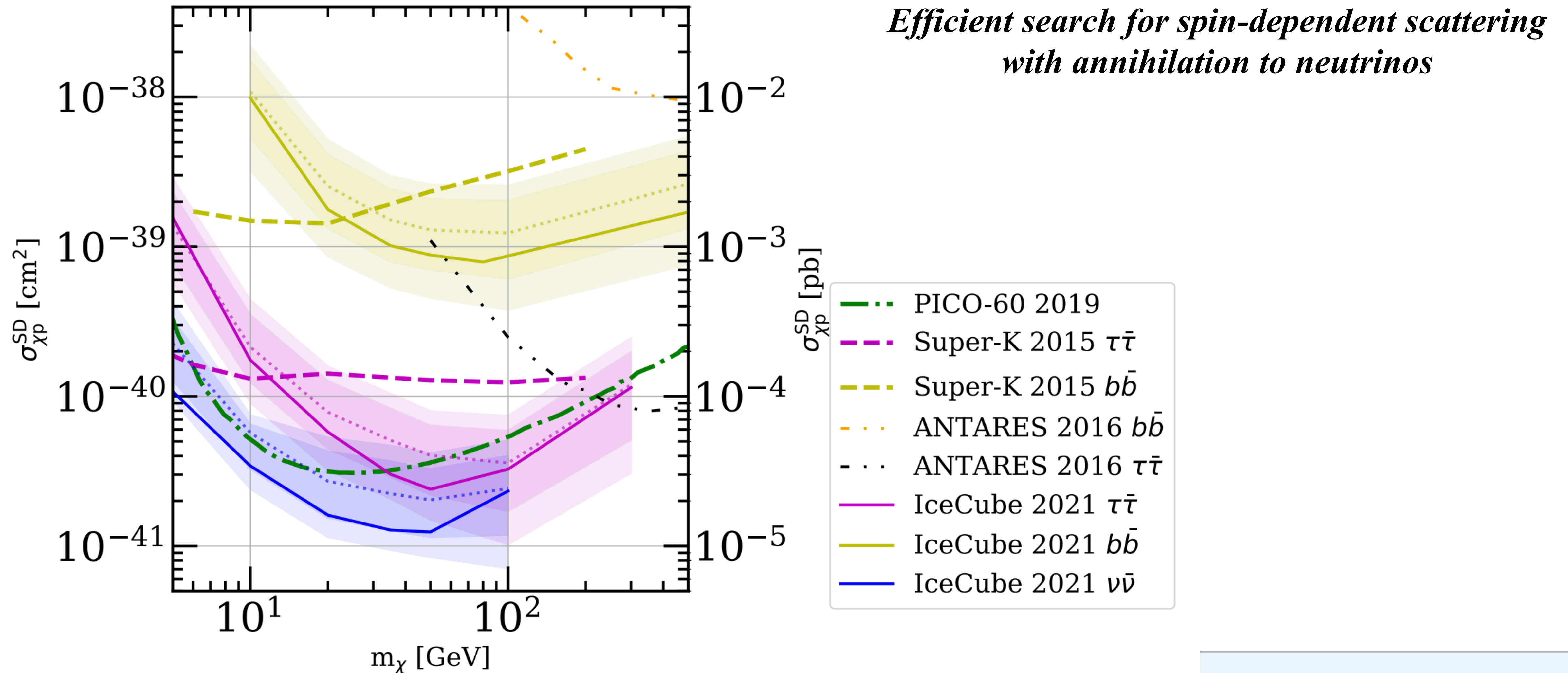
Annihilation rate of bound WIMPs: $2\Gamma_{\text{ann}} = \int dV n^2 \langle \sigma v \rangle$

Capture Probability

Evaporation Probability



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2405.05312

*Can play similar game with any other
astrophysical object*

	Celestial Body Properties				
	Escape velocity [c]	Mass [\mathcal{M}_{\odot}]	Radius [R_{\odot}]	T_{core} [K]	σ_{tr} [cm^2]
Neutron Star	0.7	1.4	10^{-5}	10^5	10^{-45}
White Dwarf	10^{-2}	0.6	10^{-2}	10^5	10^{-41}
Average MS Star	10^{-3}	0.3	0.3	10^7	10^{-36}
Sun	10^{-3}	1	1	10^7	10^{-35}
Brown Dwarf	10^{-3}	10^{-2}	0.1	10^4 – 10^6	10^{-35}
Jupiter	10^{-4}	10^{-3}	0.1	10^4	10^{-34}
Earth	10^{-5}	10^{-6}	10^{-2}	10^4	10^{-33}

(Also relevant: DM density, DM velocity, Distance)

