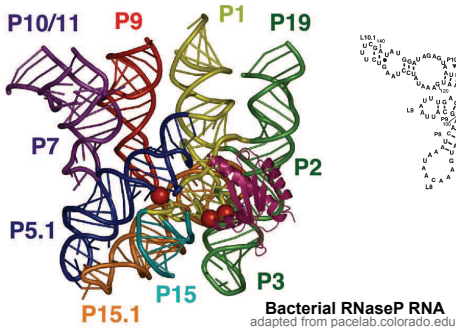


Minimal-AI:

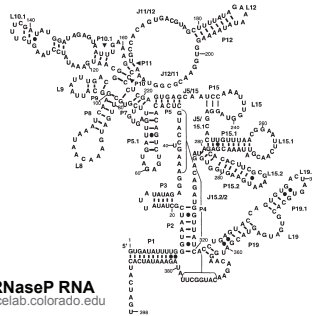
**Unsupervised learning
of the rules of RNA base pairing**

What does it take to learn the rules of RNA base pairing?



helical structures

Staphylococcus aureus RNaseP RNA



canonical base pairs

A:U G:C G:U
U:A C:G U:G

A lot less than you may think

Jay Pratap, Ryan Krueger, ER; Commun. Biol., 2026

To learn the rules of RNA base pairing

Deep models with **millions** of parameters

Minimal model?

Trained on **100 thousands** RNA seq/structures

Minimal inputs?

Minimal model

Thermodynamic models

Nearest Neighbors NN

ViennaRNA, RNAfold

minimum free energy

hard to train

~ 2k parameters, fixed

Probabilistic models

Stochastic Context-free grammars (SCFGs)

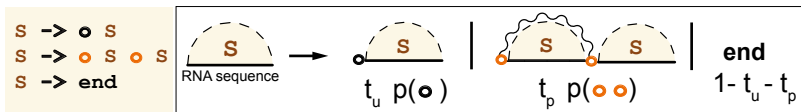
maximum probability

easy to train (from structures)

flexible (from 20 to thousands)

TORNADO, NN SCFG mimics

G5 Grammar (Ivo Hofacker)



Eddy&Durbin, Sakakibara&Haussler, 1994

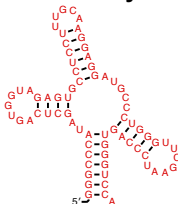
Dowell & Eddy, 2004

Minimal training inputs

RNA secondary structures?

structural
information

X-ray, NMR, CryoEM



	3'			
	A	C	G	U
5' A	0	0	0	1
C	0	0	10	0
G	0	5	0	2
U	4	0	0	0

maximum likelihood training

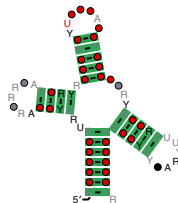
Contrafold, Do *et al.*, Bioinf., 2006
TORNADO, Rivas&Eddy, RNA, 2012

RNA alignments?

evolutionary
information

genomes, homology

```
GGGCCCAUAGCUCAGU--GGU--AGAGUCCUCCUUGGCAAGGAGGAGUC--CCUG--GGUUCGAAUCCAGUGGCCCA
CAUAGUAGCUCUAA--AG--CAAGUACUGGUCUCUUAACCAUUA--UAGUAAUUGAGCUCUAGCUCUAAU
GGGCCCGUAGCUCUAGUGGUAAGAGCGUUUGAUCUACGGAAUCAAAGGU--UAGG--GGUUCGACUCCUCCGGGCGG
GGGCCUGUAGCUCAGCUGUUGUAGAGCGCACCGCUGAUAAAGCUGAGGU--CGGU--GGUUCGACUCCUCCAGGCCCA
AGGGGCAUAGUUAAC--GGU--AGAAGAGAGGUCUCCAAAACUCCGG--UGUG--GGUUCGAAUCCUAGUCUCCCG
AGGGGCUUAGUUAAC--GGU--AGAAGAGAGGUCUCCAAAACUCCGG--UGUG--AGUUCGACUCCUCCCGCGC
SCUGUAGUUGGUCAGUUGU--AGAGCGCACCCUUGGUAAGGGUAGGU--CCCC--AGUUCGACUCCUCCGGUAGCAGCA
UGGGGCGUUGGCCAAGU--GGU--AAGGCGACGGGUGUUGGUCUGUUAU--CGGA--GGUUCGAAUCCUCCCGUCC
GCCCUUUUAUCUAGU--GGU--AGAGUAAUGCCUUGGUAAGGCAUAGU--CAUC--GGUUCGAAUCCUAGUAAAGGCGU
GGGCCCAUUGGCUAAU--GGU--AGAGGACAGAGGUCUCCAAAACUCCGG--UAGA--GGUUCGAAUCCUAGUGAGCGCA
CGUUCAGUGGCUAAU--GGU--AAGCGACCGCCACUCCUAAUUGUUAUUGGCG--GGUUCGAAUCCUCCUGUAGGCA
AGUAGGUCAGCUAA--UU--AAGCUAUCGGGCCACACCCCGAGAA--CGGU--GGUUCGAAUCCUCCCGUAGC
AGAUUUAUGUAAAU--CA--AUUACAUACUUGUCUCAAAGUUAAU--UAGA--GAUCAAUAUCCUUAUUAUCCU
GUUUCUGUUGUA--UU--ACAACGAUUAUUAUUAUUAUUAU--UCGC--AGUUGAAUGCUGUAGAAUA
GGUCUAGAGGUA--UU--UUAUUGGAAUUGGCAAUUGCAAGG--UGGA--GAGAAU--CUUUAAGC
UCCUUCUUGUUAU--UU--AAUUAACGAGCUCUCCAUUGAGGA--UUU--GAAUAAAC--CCAGAGAGAG
UAGAUGAAGCCAGUA--AU--AGGGUUAUUGCUGUUAACUAAAUUU--CGGA--GGUUCGAAUCCUCCCGACUCC
CACUUAAGAAUUA--UU--AGAGCGUUAACUUAUUAAGUUAAGUU--AGAG--ACCUUAAA--AUUCCUAGU
GUUAUAGCUCUUAUAAC--AAAGCAAGGACUCCAAAAGCUGUAGA--UGGA--U--AAUUGU--AUUCCUUAUA
UCUUAUAGUUAU--AGU--AAUCCUUGGUCUAGGAAUCAA--CCUU--GGUUCGAAUCCUCAAUAAGC
GGGCCUUAUAGCUCAGCUGGUAAGAGUCACCCUUGAAGGGUAGGU--CACA--AGUUCGACUCCUAGGCGCA
```



Infernal,
Eddy, Kolbe, Nawrocki, 2013

R-scape, Rivas, Clements, Eddy, Nat Meth, 2017

RNA sequences only??

5'-GGGCCCAUAGCUCAGUGGUAGAGUGCCUCCUUGCAAGGAGGAUGCCUUGGGUUCGAAUCCAGUGGGUCCA

Pratap, Krueger, Rivas, Comms Biol, 2026

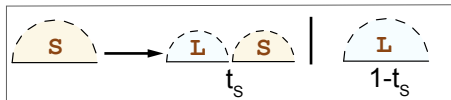
The not-deep-at-all model

G6 Grammar

Start

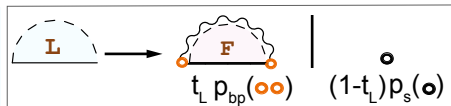
$S \rightarrow L S$

$S \rightarrow L$



$L \rightarrow \circ F \circ$ new helix starts, adds first pair

$L \rightarrow \bullet$ a single residue



$F \rightarrow \circ F \circ$ helix adds a base pair

$F \rightarrow L S$ helix ends



$\bullet$ an RNA residue

$\circ \circ$ an RNA base pair

S, L, F non-terminals (NT) transform following one of 2 rules

$$0 \leq t_S, t_L, t_F \leq 1$$

Knudsen & Hein, NAR, 2003
Dowell & Eddy, BMC Bioinf, 2004

21 free parameters

$$\mathbf{T}_6 = [t_S, t_L, t_F, p_s(a), p_{bp}(a,b)]$$

$S \rightarrow L S$ t_s
 $S \rightarrow L$ $1-t_s$

$L \rightarrow \bullet \quad 1-t_L$

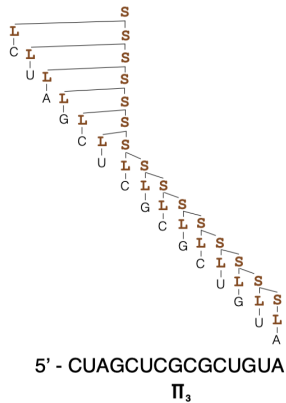
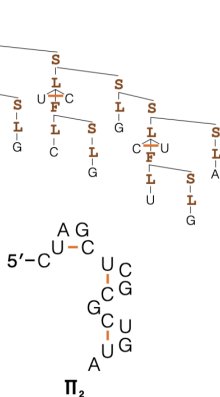
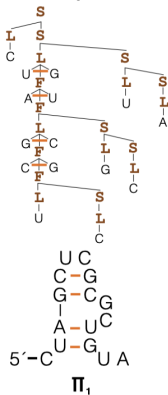
F $\rightarrow$ **L S** $1-t_F$ helix ends

[illegible]
$$P(\text{seq, structure2} \mid G6, T_6)$$

For this minimal experiment, we selected the G6 grammar [9], which has only 21 free probability parameters. The G6 model, first introduced in the method PFOLD [17], is described in Figure 1. The G6 grammar provides rules to generate sequences. It's built-in assumptions (implicit inductive biases) are:

- Residues can be either uncorrelated (unpaired) or pairwise correlated (paired).
- The ratio of unpaired to paired residues in a sequence is unconstrained.
- Arbitrary number of unpaired residues can occur interspersed in between any base pair.
- A residue cannot pair with more than one other residue.
- Paired residues can be disjoint or nested but they cannot cross.
- All unpaired residues are generated by the same rule.
- There are two distinct rules for paired residues, allowing (but not forcing) the model to distinguish terminal (or disjoint) base pairs from other base pairs that are nested together forming helices.

(b) sequence 5'-CUAGCUCGCGCUGUA



Thermodynamic models

Discriminative models

$$P(\pi \mid seq) = \frac{e^{-\Delta G(\pi, seq)}}{Z}$$

MacCaskill:

$$Z(seq) = \sum_{\pi} e^{-\Delta G(\pi, seq)}$$

Probabilistic models

Generative models

$$P(seq, \pi \mid SCFG)$$

Inside: $P(seq \mid SCFG) = \sum_{\pi} P(seq, \pi \mid SCFG)$

Maximize: $P(dataset \mid SCFG, T) = \prod_{seq \in dataset} P(seq \mid SCFG, T)$

Minimize:

$$-\log P(dataset \mid SCFG, T) = -\sum_{seq \in dataset} \log P(seq \mid SCFG, T)$$

The Loss

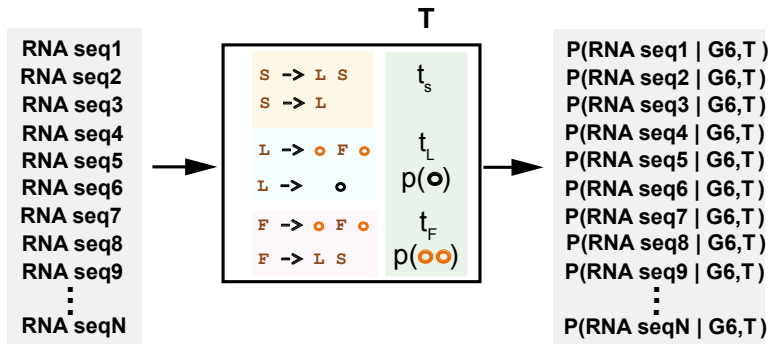
$$\begin{aligned}\min_T [-\log P(\text{dataset} \mid SCFG, T)] &= \min_T [-\sum_{seq \in \text{dataset}} \log P(seq \mid SCFG, T)] \\&= \min_T [-\sum_{seq} P_{data}(seq) \log P(seq \mid SCFG, T)] \\&= \min_T [\sum_{seq} P_{data}(seq) \log \frac{P_{data}(seq)}{P(seq \mid SCFG, T)}] \\&= \min_T KL(P_{data}(seq) \parallel P(seq \mid SCFG, T))\end{aligned}$$

Maximizing (in T) $P(seq \mid SCFG, T)$

is equivalent to

Minimizing the Kullback-Leibler (KL) divergence between
 $P_{data}(seq)$ and $P(seq \mid SCFG, T)$

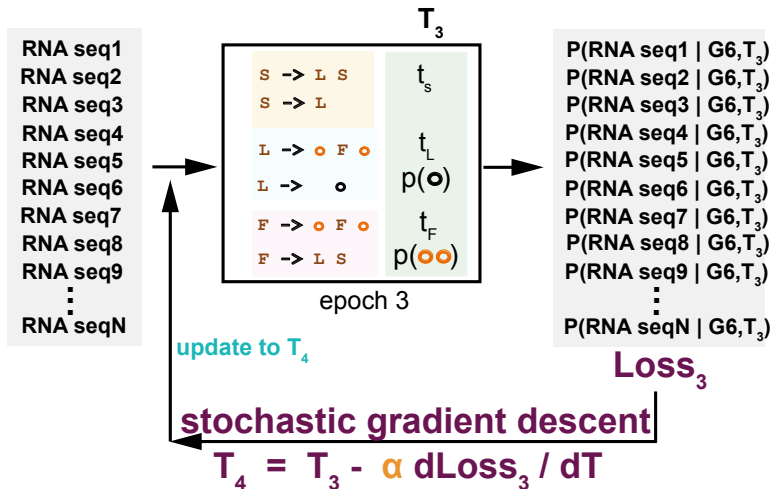
maximize the probability of the training sequences



T that minimizes

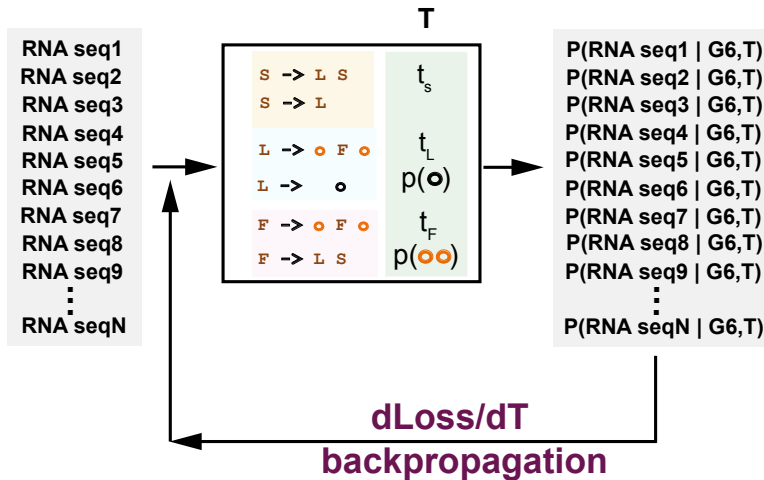
$$\text{Loss} = -\sum_i \log P(\text{seq}_i \mid G6, T)$$

maximize the probability of the training sequences



$T_0 \rightarrow T_1 \rightarrow T_2 \rightarrow T_3 \rightarrow \dots \rightarrow \text{optimal } T^*$

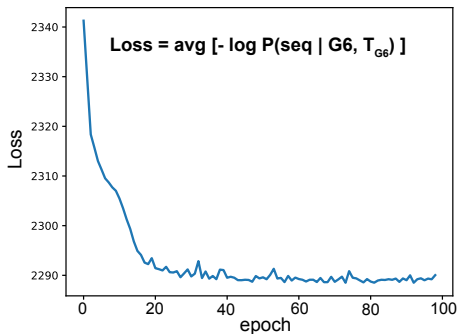
maximize the probability of the training sequences



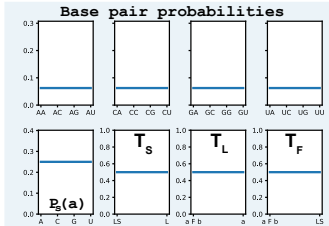
Python/JAX automatic differentiation

Learns the rule of RNA base pairing

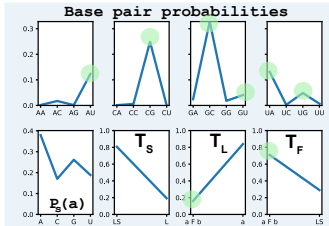
Training: RNaseP RNA 50 seqs



SGD epoch 0 (uniform)

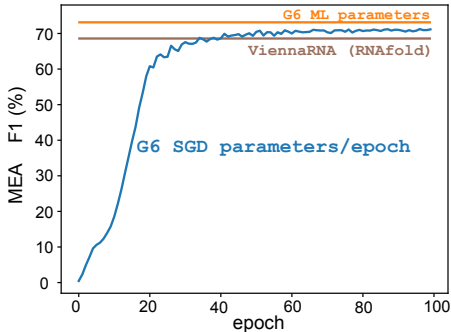


SGD epoch 99

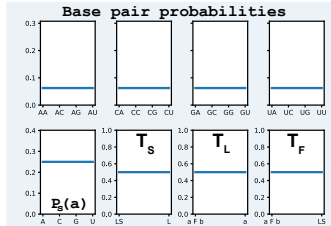


Learns the rule of RNA base pairing

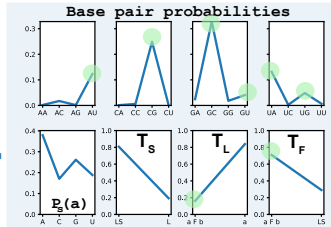
Testing: tRNA seqs



SGD epoch 0 (uniform)

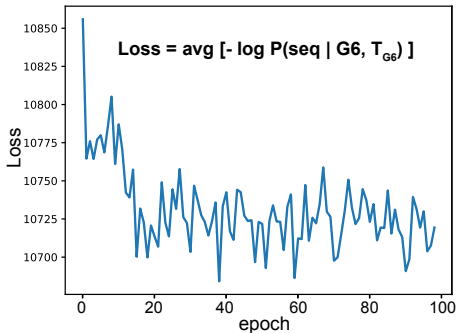


SGD epoch 99

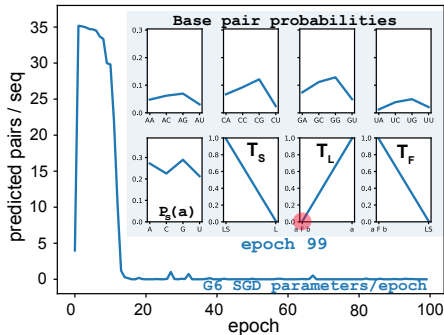


Training on random (shuffled) sequences

Training: shuffled RNaseP 225 seqs

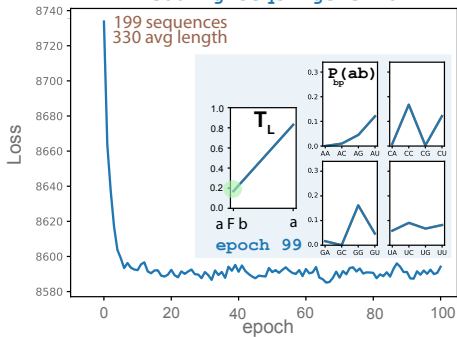


Testing: tRNAs

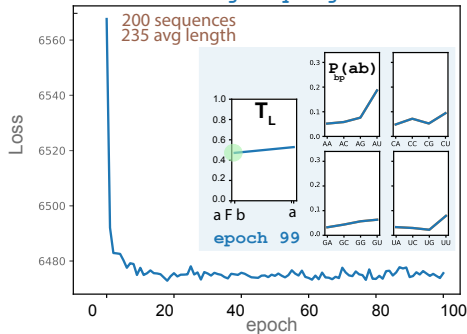


Training on mRNAs

mRNA coding seqs: gene HSP12

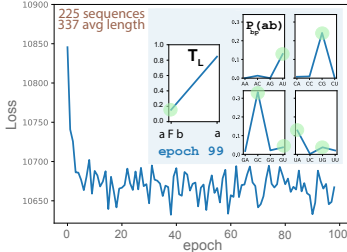


mRNA coding seqs: gene SBH2



not canonical RNA base pairs
different for different mRNAs

RNaseP RNA sequences



structural RNA

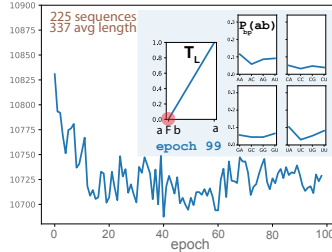
Pairwise interactions
 $T(L \rightarrow aFb) > 0$



WCF base pairing



shuffled RNaseP RNA sequences



random RNA

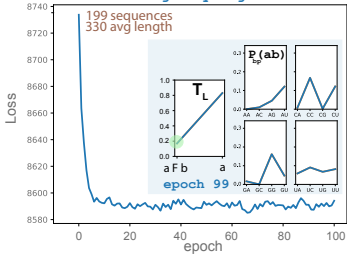
Pairwise interactions
 $T(L \rightarrow aFb) \sim 0$



WCF base pairing



mRNA coding seqs: gene HSP12



messenger RNA

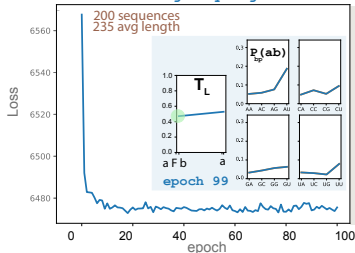
Pairwise interactions
 $T(L \rightarrow aFb) > 0$



WCF base pairing



mRNA coding seqs: gene SBH2



messenger RNA

Pairwise interactions
 $T(L \rightarrow aFb) > 0$



WCF base pairing



Are we ditching deep learning?
absolutely not!

We love:

working on fast hardware: **GPUs, TPUs**

computational frameworks to train parameters: **PyTorch, TensorFlow**

Easy automatic way to calculate gradients: **Backpropagation, JAX**

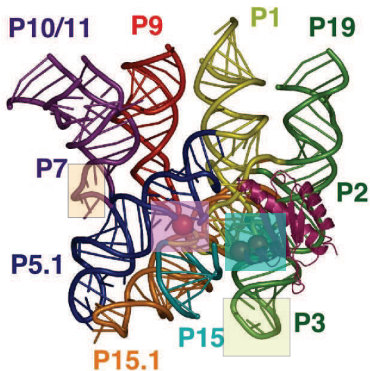
“room” to be surprised by what we can learn: **more parameters**

Learning from data w/o previous assumptions

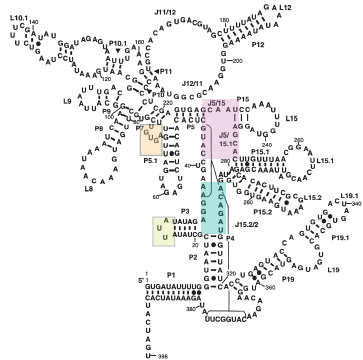
There is more to RNA structure than helices of canonical base pairs

loops

Important for molecule binding



Staphylococcus aureus RnaseP RNA



Bacterial RNaseP RNA

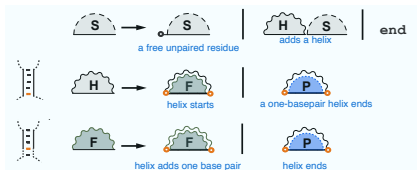
adapted from pacelab.colorado.edu

G6 Grammar

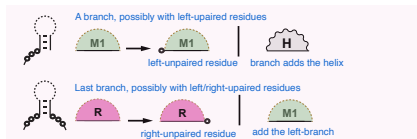
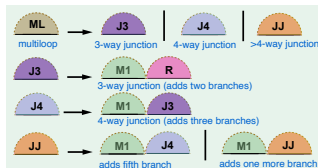


all unpaired residues are treated equally

RNA Basic Grammar (RBG^{J3J4})



what can happen at the end of a helix...

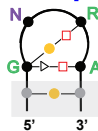
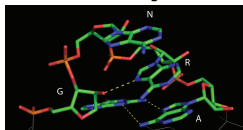


- an RNA residue, not forming any base pairing
- a set of contiguous unpaired RNA residues
- ○ an RNA base pair

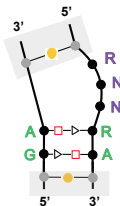
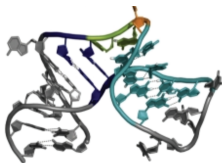
S, H, F, P, ML, M, J3, J4, JJ, M1, R
non-terminals that transform following one of the allowed rules

3D motifs in loops

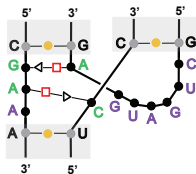
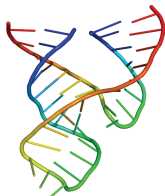
GNRA tetraloop



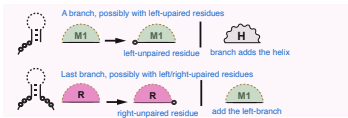
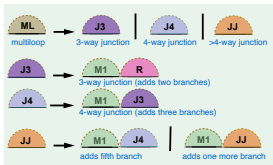
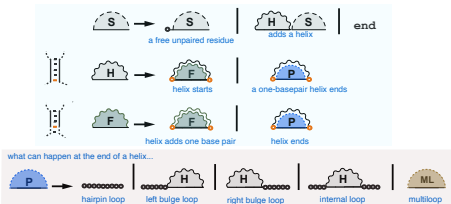
K Turn



Hammerhead ribozyme J3

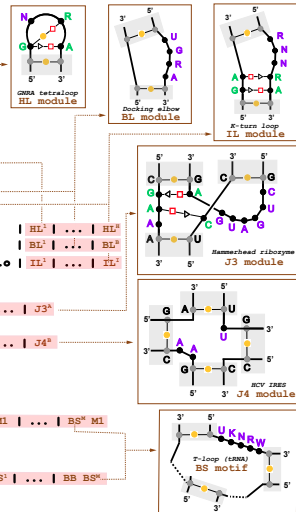


RNA Basic Grammar (RBGJ3J4)



W = AG ●—○— base Watson-Crick edge ●—●— cis Watson-Crick / Watson-Crick base pair
K = GU ●—□— base Hoogsteen edge ●—▷— trans Sugar-Edge / Hoogsteen base pair
W = AU ●—●— base Sugar edge ●—●— cis Watson-Crick / Hoogsteen base pair
N = A/G/U

RBGJ3J4-R3D Grammar



RNA 3D Motifs in the Literature

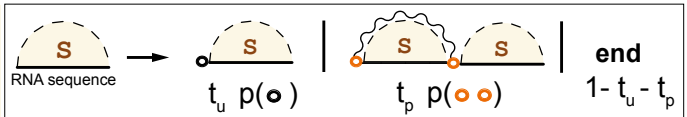
Type	Motif name	PDB	Rfam homology	CaCoFold-R3D	Other Methods	Motif Model
HL	GNRA-tetraloop	7E16	synthetic	170	—	Hendrix <i>et al.</i> , 2005 [17]
HL	U-turn	4WFL	RF00017_Metazoan_SRP	yes	—	Kemp <i>et al.</i> , 2014 [22]
HL	UNCG-tetraloop	1F7Y	synthetic	48	—	Hendrix <i>et al.</i> , 2005 [17]
HL	ANYA-tetraloop	6MSF	synthetic	18	—	Hendrix <i>et al.</i> , 2005 [17]
HL	CUYG-tetraloop	2L6I	synthetic	20	—	Hendrix <i>et al.</i> , 2005 [17]
HL	YGNN-tetraloop	1AFX	synthetic	13	—	Hendrix <i>et al.</i> , 2005 [17]
HL	GANC-tetraloop	3BWP	synthetic	15	—	Keating <i>et al.</i> , 2009 [21]
HL	UNAC-tetraloop	4A4R	synthetic	26	—	Zhao <i>et al.</i> , 2012 [99]
HL	T-loop-tetraloop	7SAM	RF01085_TLS-PK4	yes	—	RMfam [36]
HL	L8_RNaseP_bact_a	1U9S	RF00010_RNaseP_bact_a	yes	—	Das & Baker, 2010 [20]
HL	Sarcin-Ricin_loop	1SCL	RF02540_LSU_rRNA_archaea	yes	BayesPairing2	Szewczak <i>et al.</i> , 1993 [100]
HL	CsrA_binding	2MF0	RF00018_CsrB	yes	—	Duss <i>et al.</i> , 2014 [23]
HL	GAGUA_pentaloop_sars	1XJR	RF00164_Coronavirus_s2m motif	yes	—	Das & Baker, 2010 [20]
IL	Kink-turn_SAM_riboswitch	2GIS	RF00162_SAM_riboswitch	yes	BayesPairing2	Das & Baker, 2010 [20]
IL	Kink-turn_rRNA	1JJ2	RF02540_LSU_rRNA_archaeal	yes	RMDetect	Das & Baker, 2010 [20]
IL	LoopE	354D	RF00001_5S_rRNA	yes	—	Das & Baker, 2010 [20]
IL	GAAA_Tetraloop-receptor	1GID	RF00028_Group I intron	yes	—	Cate <i>et al.</i> , 1996 [8]
IL	C-loop	1872	RF02541_LSU_rRNA_bacterial	yes	RMDetect	Lescaute <i>et al.</i> , 2005 [84]
IL	G-Bulge	3DIL	RF00168_Lysine_riboswitch	yes	RMDetect	Serganov <i>et al.</i> , 2008 [87]
IL	G-Bulge_Das	1Q9A	RF02541_Bacterial LSU_RNA	yes	—	Das & Baker, 2010 [20]
IL	tandem GA	1SA9	RF00177_SSU_rRNA_bacteria	yes	RMDetect	Cruz & Westhof, 2011 [3]
IL	Twist up	1J5E	RF02541_LSU_rRNA_bacterial	no, 9	—	Zhong & Zhang, 2011 [101]
IL	UAA/GAN	6AHR	RF00009_RNaseP_nuc	yes	—	Lee <i>et al.</i> , 2006 [102]
IL	J4a/4b	2QBZ	RF00380_M-box_riboswitch	yes	—	Das & Baker, 2010 [20]
IL	J4/5	2R8S	RF00028_Group I intron	no, 6	—	Das & Baker, 2010 [20]
IL	GUA/GG_RRE	1CSL	RF00055_HIV-1 RRE	too conserved, 10	—	Das & Baker, 2010 [20]
IL	SRP RNA DOMAIN IV	1CQ5	RF00017_Metazoan_SRP	yes	—	Schmitz <i>et al.</i> , 1999 [65]
IL	Hook_turn_GAAC/CUA	1MHK	synthetic	32	—	Das & Baker, 2010 [20]
IL	Docking elbow-IL	3QIQ	RF00011_RNaseP_bact_b	yes	—	Lehmann <i>et al.</i> , 2012 [83]
IL	pK-turn	3OK7	RF00010_RNaseP_RNA	no, 45	—	Meyer <i>et al.</i> , 2012 [89]
J3	Purine_riboswitch_J3	2EEW	RF00167_Purine_riboswitch	yes	—	Das & Baker, 2010 [20]
J3	hammerhead_CUGA/A/C	359D	RF02275_Hammerhead_HH9	yes	—	Das & Baker, 2010 [20]
J3	J3_typeA	4RZD	RF02680_PreQ1-III	yes	—	Lescaute & Westhof, 2006 [103]
J3	J3_typeB	1J5E	RF00177_SSU_rRNA_bacteria	yes	—	Lescaute & Westhof, 2006 [103]
J3	J3_typeC	4LX6	RF03165_2dG-II_riboswitch	yes	—	Lescaute & Westhof, 2006 [103]
J3	J3_TPP	2GD1	RF00059_TPP_riboswitch	yes	—	Serganov <i>et al.</i> , 2006 [62]
J3	J3_groupII	5J01	RF02001_group-II-D1D4-3	yes	—	this work
J4	HCV_IRES_AA/0/U/0	1KH6	RF00061_IRES_HCV	yes	—	Das & Baker, 2010 [20]
J4	J4_U1RNA	3PGW	RF00003_U1_RNA	yes	—	Weber <i>et al.</i> , 2010 [104]
BS	T-loop	1EHZ	RF00005_tRNA	yes	—	Hendrix <i>et al.</i> , 2005 [17]
BS	LoopE-a	4FRN	RF01689_AdoCbl-II	yes	—	this work
BS	LoopE-b	4FRN	RF01689_AdoCbl-II	yes	—	this work
BS	CRC_binding	—	RF00195_RsmY	yes	—	Sonnleitner <i>et al.</i> , 2009 [105]
PK		5DDP	RF01739_Glutamine_riboswitch	yes	—	Ren <i>et al.</i> , 2015 [64]

Unsupervised Learning of RNA 3D Motifs

Can we learn the 3D motifs from RNA sequences alone?

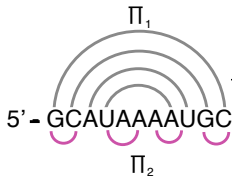
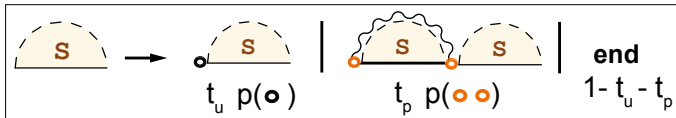
G5 SCFG

$S \rightarrow \bullet S$
 $S \rightarrow \circ S \circ S$
 $S \rightarrow \text{end}$



G5 Grammar

$S \rightarrow \bullet S$
 $S \rightarrow \bullet S \bullet S$
 $S \rightarrow \text{end}$



$P(\Pi_1)$

$P(\Pi_2)$

G5:

$$t_p^4 = 0.0067$$

=

$$t_p^4 = 0.0067$$

G6:

$$t_L \times t_F^3 = 0.0519$$

>

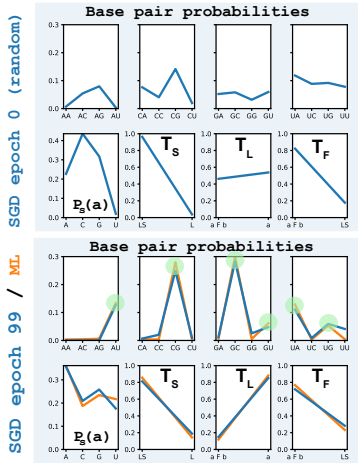
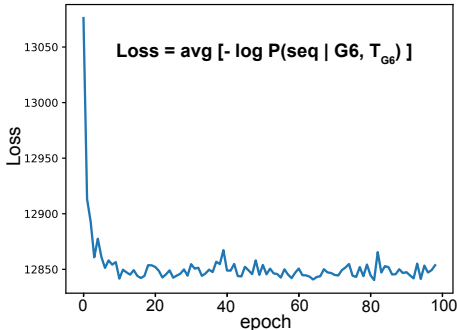
$$t_L^4 = 0.0006$$

G5 cannot favor helix stacking

Learns the rule of RNA base pairing

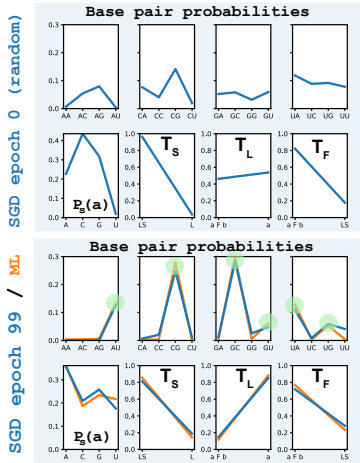
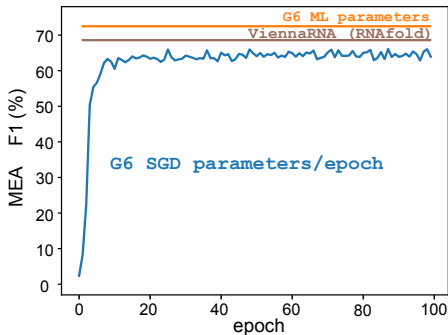
Training: 7 RNA Fams 400 seqs

RNaseP RNA, SRP RNA, 5S rRNA, telom RNA, tmRNA, group I, and group II introns



Learns the rule of RNA base pairing

Testing: tRNAs



To learn the rules of RNA base pairing

Deep models with **millions** of parameters

Minimal **model**

21 free parameters

Trained on **100 thousands** RNA seq/structures

Minimal **inputs**

25-50 RNA sequences only

Merging SCFGs with standard deep-learning methods:

Stochastic Gradient Descent

Backpropagation by automatic differentiation

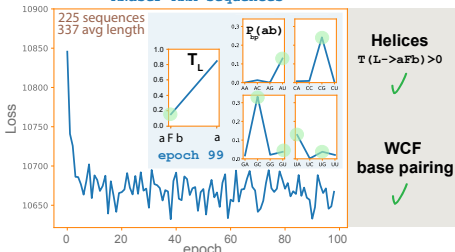
A loss that optimizes the marginal probability of the sequences (all structures integrated)

Loss is calculated exactly with Inside algorithm, (no need for “evidence lower bound”)

SCFGs directly interpretable: a structural RNA genefinder

structural RNA SEQUENCES

RNaseP RNA sequences



random RNA SEQUENCES

shuffled RNaseP RNA sequences

